

# Constraining the MSSM Higgs sector at the LHC and beyond

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Introduction

Higgs mass calculation

Higgs benchmark scenarios

HL-LHC and ILC projections

Conclusions

## Introduction

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# Motivation

Current situation:

- ▶ No direct evidence for BSM physics at LHC yet,
- ▶ most known particles studied intensively confirming SM predictions.

## Where to look for new physics?

→ One promising place: the **Higgs sector**

- ▶ Higgs boson properties still leave room for deviations from SM,
- ▶ Higgs boson can be coupled easily to BSM particles,
- ▶ why should there be only one scalar particle?  
→ Searches for additional Higgs bosons.

How much can we learn from current Higgs measurements about extended Higgs sectors?

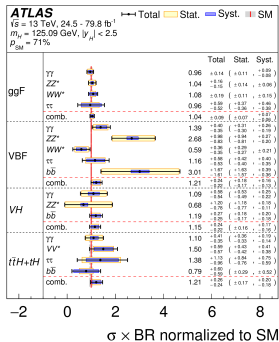
# Higgs measurements: examples

- Higgs mass: [Aad et al.,1503.07589]

$$M_h^{\text{exp}} = 125.08 \pm 0.21 \text{ (stat.)} \pm 0.11 \text{ (sys.) GeV}$$

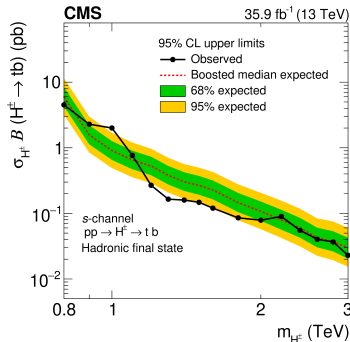
- Coupling measurements:

[1909.02845,ATLAS]



- Additional Higgs bosons:

[2001.07763,CMS]



# Complementarity of the constraints

- ▶ The different measurements can not be compared directly.
- ▶ Need specific BSM model to explore the complementarity between the different constraints!

## This talk:

Use MSSM as a benchmark model with a focus on collider phenomenology.

In addition, Higgs physics can also be constrained by

- ▶ flavour measurements,
- ▶ EDM measurements,
- ▶ ...

## The MSSM Higgs sector – potential

- ▶ Two Higgs doublets

$$\Phi_i = \left( \begin{array}{c} \phi_i^+ \\ \frac{1}{\sqrt{2}}(v_i + \phi_i + i\chi_i) \end{array} \right),$$

- ▶ general THDM Higgs potential has 9 non-SM parameters

$$\begin{aligned} V_{\text{THDM}}(\Phi_1, \Phi_2) = & m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 - (m_{12}^2 \Phi_1^\dagger \Phi_2 + \text{h.c.}) \\ & + \frac{1}{2} \lambda_1 (\Phi_1^\dagger \Phi_1)^2 + \frac{1}{2} \lambda_2 (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1)(\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2)(\Phi_2^\dagger \Phi_1) \\ & + \left( \frac{1}{2} \lambda_5 (\Phi_1^\dagger \Phi_2)^2 + \lambda_6 (\Phi_1^\dagger \Phi_1)(\Phi_1^\dagger \Phi_2) + \lambda_7 (\Phi_2^\dagger \Phi_2)(\Phi_1^\dagger \Phi_2) + \text{h.c.} \right), \end{aligned}$$

- ▶ SUSY reduces these to 2

$$\lambda_1 = \lambda_2 = \frac{1}{4}(g^2 + g_y^2), \lambda_3 = \frac{1}{4}(g^2 - g_y^2), \lambda_4 = -\frac{1}{2}g^2, \lambda_{5,6,7} = 0$$

→ predictive model!

## The MSSM Higgs sector – mass eigenstates

Diagonalizing the Higgs mass matrices yields mass eigenstates

$$\begin{pmatrix} h \\ H \end{pmatrix} = R(\alpha) \begin{pmatrix} \phi_1 \\ \phi_2 \end{pmatrix}, \quad \begin{pmatrix} A \\ G \end{pmatrix} = R(\beta) \begin{pmatrix} \chi_1 \\ \chi_2 \end{pmatrix}, \quad \begin{pmatrix} H^\pm \\ G^\pm \end{pmatrix} = R(\beta) \begin{pmatrix} \phi_{1^\pm} \\ \phi_{2^\pm} \end{pmatrix}$$

→ five physical Higgs states:  $h, H, A, H^\pm$

- ▶ Two non-SM input parameters:  $M_A$  and  $\tan \beta = v_2/v_1$ ,
- ▶ tree-level relations:

$$m_{h,H}^2 = \frac{1}{2} \left( M_A^2 + M_Z^2 \mp \sqrt{(M_A^2 + M_Z^2)^2 - 4M_A^2 M_Z^2 \cos^2 2\beta} \right),$$
$$m_{H^\pm}^2 = M_A^2 + M_W^2,$$
$$\tan 2\alpha = \frac{M_A^2 + M_Z^2}{M_A^2 - M_Z^2} \tan 2\beta.$$



# The MSSM Higgs sector – decoupling limit

Decoupling limit,  $M_A \gg M_Z$ , implies:

- ▶ masses:

$$m_h^2 \rightarrow M_Z^2 \cos^2(2\beta),$$

$$m_H^2 \rightarrow M_A^2 + M_Z^2 \sin^2(2\beta),$$

⇒ all Higgses, apart from  $h$ , decouple.

- ▶ couplings:

$$\alpha \rightarrow \beta - \pi/2$$

⇒ couplings of  $h$  boson SM-like

- ▶ Yukawa sector: THDM type II

$$g_{Hbb}/g_{hbb} \sim \tan \beta, \quad g_{H\tau\tau}/g_{h\tau\tau} \sim \tan \beta, \quad g_{Htt}/g_{h tt} \sim 1/\tan \beta$$

$$g_{Abb}/g_{hbb} \sim \tan \beta, \quad g_{A\tau\tau}/g_{h\tau\tau} \sim \tan \beta, \quad g_{Att}/g_{h tt} \sim 1/\tan \beta$$

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# Higgs mass calculation I

## Special feature of MSSM

Mass of lightest  $\mathcal{CP}$ -even Higgs,  $M_h$ , is calculable in terms of model parameters  $\Rightarrow$  can be used as a precision observable

- ▶ at tree-level  $M_h^2 \simeq M_Z^2 \cos^2(2\beta) \leq M_Z^2$ ,
- ▶  $M_h$  is however heavily affected by loop corrections,
- ▶ directly sensitive to the SUSY scale.

To fully profit from experimental precision, higher order calculations are crucial!

- ▶ Many tools on the market: FeynHiggs, FlexibleSUSY, SARAH/SPheno, SOFTSUSY, ...
- ▶ In this talk, I will focus on FeynHiggs  
[HB, Hahn, Heinemeyer, Hollik, Paßehr, Rzehak, Sobolev, Weiglein].

## Higgs mass calculation II

Three approaches are used:

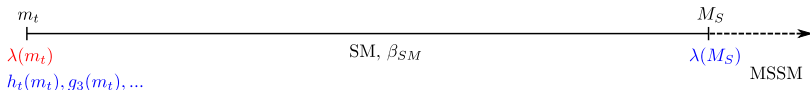
- ▶ Fixed-order (FO) approach:
  - + Precise for low SUSY scales,
  - but for high scales  $\ln(M_t^2/M_t^2)$  terms spoil convergence of perturbative expansion.
- ▶ effective field theory (EFT) approach:
  - + Precise for high SUSY scales (logs resummed),
  - but for low scales  $\mathcal{O}(M_t/M_{\text{SUSY}})$  terms are missed if higher-dimensional operators are not included.
- ▶ hybrid approach:
  - ++ Precise for low and high SUSY scales.

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## EFT calculation (simplest framework)



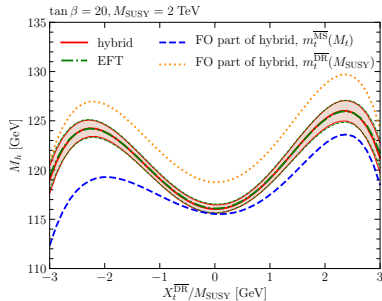
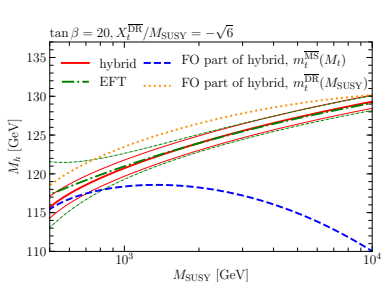
- ▶ Integrate out all SUSY particles  $\rightarrow$  SM as EFT,
- ▶ Higgs self-coupling fixed at matching scale

$$\lambda(M_{\text{SUSY}}) = \frac{1}{4}(g^2 + g_y^2) + \frac{6y_t^4}{(4\pi)^2} \left[ \left( \frac{X_t}{M_{\text{SUSY}}} \right)^2 - \frac{1}{12} \left( \frac{X_t}{M_{\text{SUSY}}} \right)^4 \right] + \dots,$$

- ▶ run Higgs self-coupling down to electroweak scale,
- ▶ calculate Higgs mass:  $M_h^2 = \lambda(M_t)v^2 + \dots$ ,
- ▶ recent progress:
  - NNLL resummation beyond the gaugeless limit  
[1908.01670, Bagnaschi, Degrandi, Slavich, Paßehr],
  - partial N<sup>3</sup>LL resummation [1910.03595, Harlander, Klappert, Voigt],
  - $X_t$  resummation [2003.04639, Kwasnitza, Stöckinger, Voigt].

# Comparison of approaches [HB,Heinemeyer,Hollik,Weiglein,1912.04199]

Single-scale scenario with all non-SM particles at  $M_{\text{SUSY}}$



## “Rule of thumb”

Remaining theoretical uncertainties (for  $\overline{\text{DR}}$  stop input parameter):

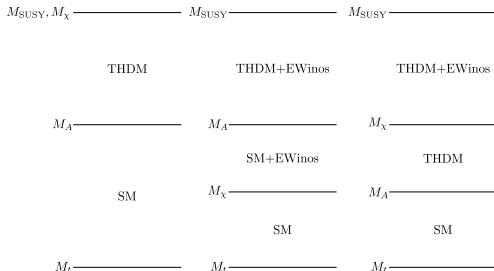
$$X_t/M_{\text{SUSY}} = 0 \rightarrow \Delta M_h \sim 0.5 \text{ GeV},$$

$$X_t/M_{\text{SUSY}} = \sqrt{6} \rightarrow \Delta M_h \sim 1 \text{ GeV}$$

Slightly higher for OS stop input parameters.

# What happens in non-degenerate scenarios?

Large hierarchy between SUSY particles  $\rightarrow$  EFT tower needed.



EFTs implemented in FeynHiggs:

- ▶ SM (resums  $\ln(M_{\tilde{t}}/M_t)$ ),
- ▶ SM+EWinos (resums  $\ln(M_{\tilde{t}}/M_{\tilde{\chi}^-})$ ),
- ▶ SM+Gluino (resums  $\ln(M_{\tilde{t}}/M_{\tilde{g}})$  if  $M_{\tilde{g}} < M_{\tilde{t}}$ ),
- ▶ SM+EWinos+Gluino,
- ▶ THDM (resums  $\ln(M_{\tilde{t}}/M_A)$ ),
- ▶ THDM+EWinos,
- ▶ THDM+EWinos+Gluino.



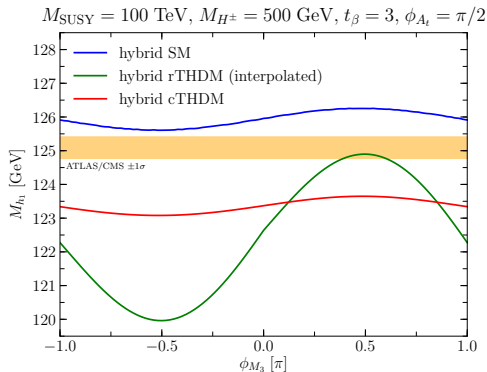
# THDM as EFT

- ▶ For low  $M_A$ , the EFT of the MSSM is not the THDM type-II,
    - both Higgs doublets couple to e.g. top quarks,
  - ▶ loop corrections induce non-zero (potentially complex) values for  $\lambda_{5,6,7}$
- ⇒ Large number of EFT parameters complicating the calculation.

Recent progress:

- ▶ complex THDM as EFT [HB,Murphy,Rzehak,1909.00726,2010.04711],
- ▶ calculation of  $\mathcal{O}(\alpha_t^2)$  threshold corrections [HB,Sobolev, 2010.01989].

# Complex THDM as EFT



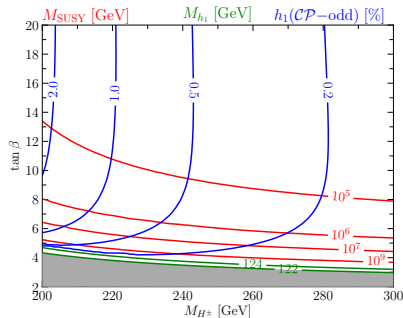
Including phase dependence fully in

- ▶ 2L RGEs,
- ▶ one-loop threshold corrections,
- ▶  $\mathcal{O}(\alpha_t \alpha_s)$   $\lambda_i$ -threshold corrections.

## Intermezzo: $\mathcal{CP}$ -odd component of the SM-like Higgs boson

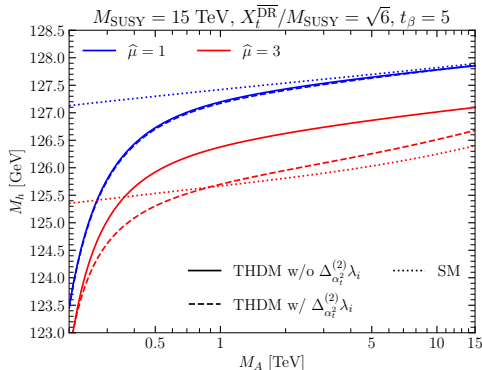
Sizeable  $\mathcal{CP}$ -odd component requires

- ▶ Large mixing with  $\mathcal{CP}$ -odd A boson
  - imaginary parts of couplings have to be large ( $\phi_{A_t} = 2\pi/3, \phi_{M_3} = \pi/4$ )
  - $\tan\beta$  and  $M_{H^\pm}$  must be small
- ▶ large SUSY scale required to ensure  $M_h \sim 125$  GeV  
→  $\mathcal{CP}$ -mixing decouples



Potential discovery of  $\mathcal{CP}$ -odd component at the LHC would probably exclude the MSSM.

# $\mathcal{O}(\alpha_t^2)$ threshold corrections to $\lambda_i$



- ▶ compared different calculation methods,
- ▶ easiest methods: calculate 2L four-point functions in the unbroken phase,
- ▶ calculation fully includes CP-violating phases.

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## Higgs benchmark scenarios – why do we need them?

- ▶ MSSM has large number of free parameters,
- ▶ interpretation of Higgs properties and searches for additional Higgs bosons would require large parameter scans.



Focus on benchmark scenarios with only two free parameters:

- ▶ Typically presented in  $M_A$ - $\tan\beta$  plane (or  $M_{H^\pm}$ - $\tan\beta$ ),
- ▶ fix stop mass scale and other parameters such that SM-like Higgs with mass of  $\sim 125$  GeV exists,
- ▶ each scenario has a different phenomenology,
- ▶ provide interpretation frameworks for experiments.

# Six scenarios with sfermion mass scale $M_{\text{SUSY}} \sim 1.5 \text{ TeV}$

[Bagnaschi, HB, Fuchs, Hahn, Heinemeyer, Liebler, Patel, Slavich, Stefaniak, Wagner, Weiglein, 1808.07542]

Defined using:

- ▶ FeynHiggs → Higgs masses and branching ratios,
- ▶ SusHi → Higgs production cross-sections,
- ▶ HiggsBounds → direct searches for extra Higgs bosons,
- ▶ HiggsSignals → SM-like Higgs signal strengths.

Benchmark scenarios:

- ▶  $M_h^{125}$  scenario → all SUSY particles at the TeV scale,
- ▶  $M_h^{125}(\tilde{\tau})$  scenario → light Stau, Bino and Winos,
- ▶  $M_h^{125}(\tilde{\chi})$  scenario → light Bino, Winos and Higgsinos,
- ▶  $M_h^{125}(\text{alignment})$  scenario → alignment without decoupling,
- ▶  $M_H^{125}$  scenario → heavy  $\mathcal{CP}$ -even Higgs is SM-like,
- ▶  $M_{h_1}^{125}(\text{CPV})$  scenario →  $\mathcal{CP}$ -violation in the Higgs sector.

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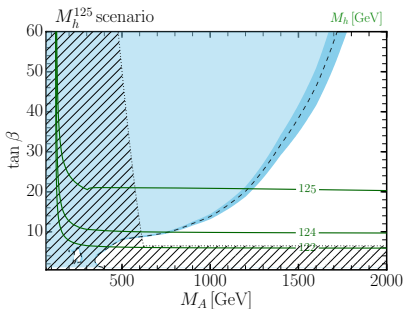
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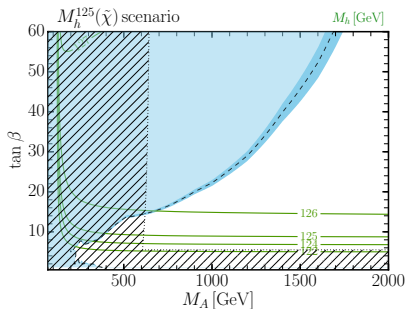
# $M_h^{125}$ and $M_h^{125}(\tilde{\chi})$ scenarios

$$M_{Q_3} = M_{U_3} = M_{D_3} = 1.5 \text{ TeV}, \quad M_{L_3} = M_{E_3} = 2 \text{ TeV},$$

$$M_3 = 2.5 \text{ TeV}, \quad X_t = 2.8 \text{ TeV}, \quad A_b = A_\tau = A_t.$$



$$\mu = M_1 = M_2 = 1 \text{ TeV}$$

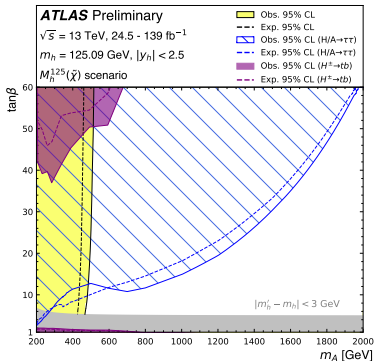
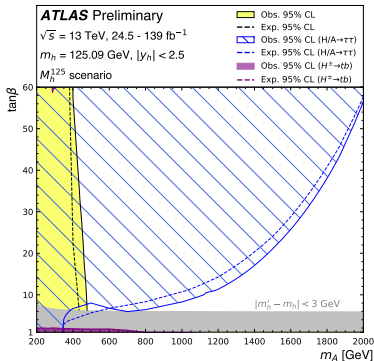


$$\mu = M_2 = 180 \text{ GeV}, M_1 = 160 \text{ GeV}$$

- ▶ Blue: excluded by direct searches for heavy Higgs bosons,
- ▶ hashed: excluded by SM-like Higgs signal strengths / mass.

# $M_h^{125}$ and $M_h^{125}(\tilde{\chi})$ scenarios – experimental results

[ATLAS-CONF-2020-053]



## Benchmark scenarios for the low $\tan\beta$ region

[HB,Liebler,Stefaniak,1901.05933]

In scenarios with  $M_{\text{SUSY}} \sim 1.5$  TeV, region of  $\tan\beta \lesssim 8$  excluded, since mass  $M_h < 125 \pm 3$  GeV:

$M_{h,\text{tree}} \xrightarrow{t_\beta \rightarrow 1} 0 \Rightarrow$  need to raise  $M_{\text{SUSY}}$  to push  $M_h$  upwards.

### Concept

Take existing scenarios and raise  $M_{\text{SUSY}}$  at every point such that  $M_h \sim 125$  GeV (upper limit:  $M_{\text{SUSY}} \leq 10^{16}$  GeV).

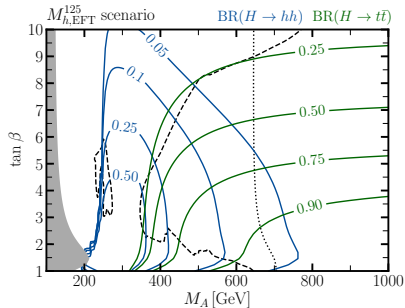
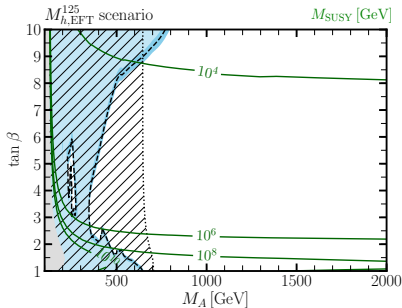
- large hierarchy between  $M_A$  and  $M_{\text{SUSY}}$
- using THDM as EFT crucial.

Two low- $\tan\beta$  benchmark scenarios:

- ▶  $M_{h,\text{EFT}}^{125}$  scenario resembling  $M_h^{125}$  scenario,
- ▶  $M_{h,\text{EFT}}^{125}(\tilde{\chi})$  scenario resembling  $M_h^{125}(\tilde{\chi})$  scenario.

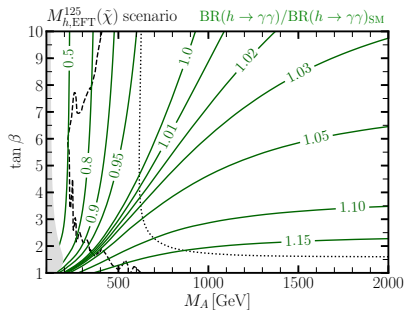
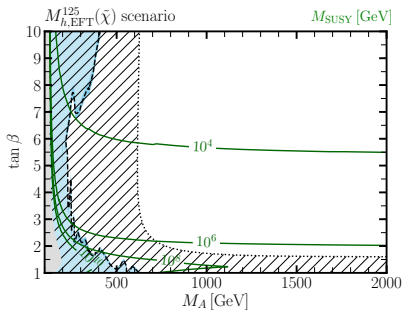
# $M_{h,EFT}^{125}$ scenario

Similar to hMSSM scenario [1307.5205,1307.5205,....,Djouadi et al.]



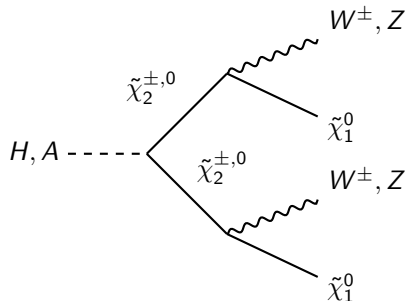
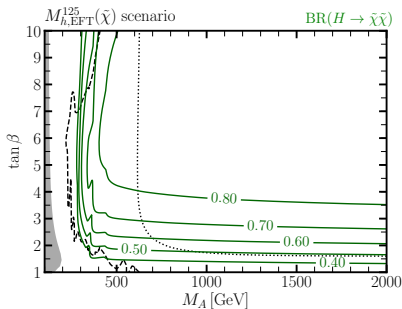
- ▶ Gray:  $M_h < 122$  GeV,
- ▶ blue: Excluded by direct searches for heavy Higgs bosons,
- ▶ hashed: Excluded by Higgs signal strengths.

# $M_{h,\text{EFT}}^{125}(\tilde{\chi})$ scenario



- ▶ Gray:  $M_h < 122$  GeV,
- ▶ blue: Excluded by direct searches for heavy Higgs bosons,
- ▶ hashed: Excluded by Higgs signal strengths.

# $M_{h,EFT}^{125}(\tilde{\chi})$ scenario – $H, A, H^\pm \rightarrow \tilde{\chi}\tilde{\chi}$



- ▶ Interesting  $H, A \rightarrow \tilde{\chi}_i \tilde{\chi}_j \rightarrow E_{T,\text{miss}} + W^\pm, Z, h$  signatures,
- ▶ no experimental searches yet,
- ▶ EWino production via heavy Higgs can exceed direct production,
- ▶ particularly sensitive for compressed EWino spectrum.

[Gori et al.,1811.11918;Wagner et al,2006.07389;...]

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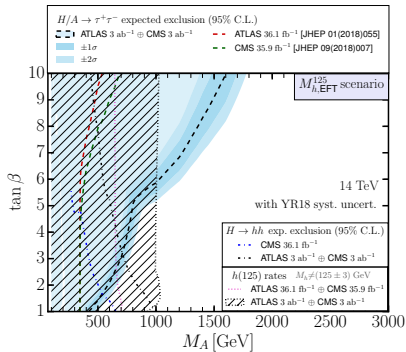
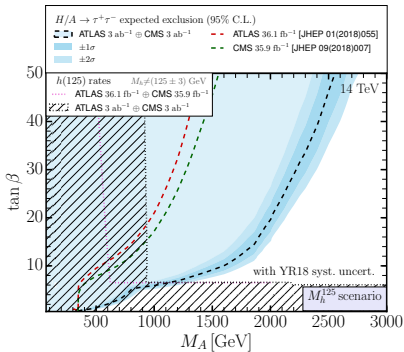
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# HL-LHC projections – $M_h^{125}$ and $M_{h,EFT}^{125}$ scenarios

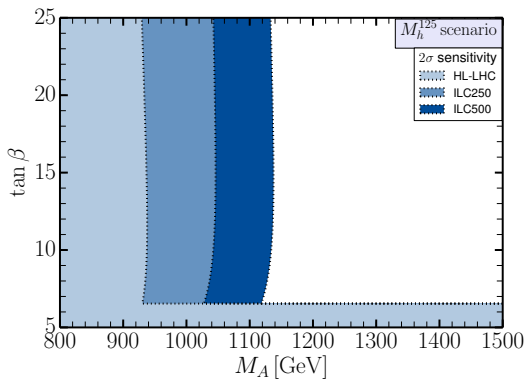
[HB,Bechtle,Heinemeyer,Liebler,Stefaniak,Weiglein,2005.14536]



- Assumption: discovered Higgs has SM-like couplings.

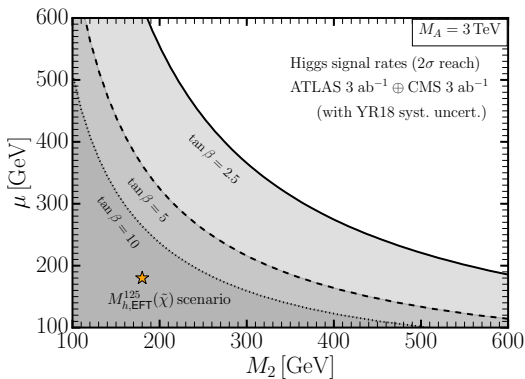


# ILC projections – $M_h^{125}$ scenario



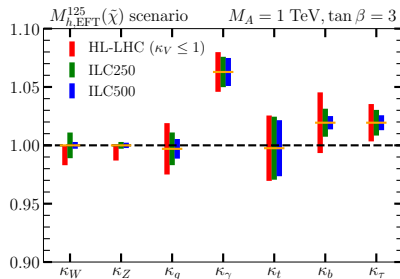
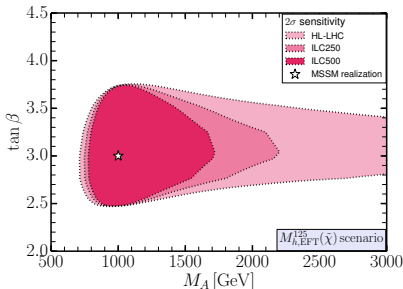
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# HL-LHC projections – $M_{h,EFT}^{125}(\chi)$ scenario



- ▶ Assumption: discovered Higgs has SM-like couplings.

# What if $M_{h,\text{EFT}}^{125}(\tilde{\chi})$ scenario is realized?



- Assumption: discovered Higgs has couplings as predicted for  $M_A = 1 \text{ TeV}$  and  $\tan \beta = 3$ .

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## Conclusions

Higgs mass calculation:

- ▶ Unique observable directly sensitive to SUSY scale,
- ▶ theoretical uncertainty of  $\lesssim 1$  GeV.

Higgs benchmark scenarios:

- ▶ Help to interpret LHC results,
- ▶ Higgs couplings  $\rightarrow$  lower bound on  $M_A$  ( $M_A \gtrsim 600$  GeV),
- ▶ Higgs searches  $\rightarrow$  strong constraints for large  $\tan\beta$ ,
- ▶ low  $\tan\beta$  region challenging to probe at the LHC.

HL-LHC and ILC constraints:

- ▶ tightening constraints,  $M_A \gtrsim 900$  GeV,
- ▶ ILC especially beneficial to pinpoint specific model in case of deviation.

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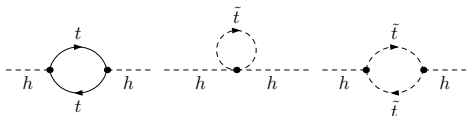
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**Thanks for your attention!**

## Fixed-order techniques



$$M_h^2 = m_h^2 + \frac{6y_t^4}{(4\pi)^2} v^2 \left[ \ln \frac{M_{\tilde{t}}^2}{M_t^2} + \left( \frac{X_t}{M_{\tilde{t}}} \right)^2 - \frac{1}{12} \left( \frac{X_t}{M_{\tilde{t}}} \right)^4 \right] + \dots$$

- ▶ Stop mass scale  $M_{\tilde{t}} = \sqrt{M_{\tilde{t}_1} M_{\tilde{t}_2}}$ ,
- ▶ status:  $\mathcal{O}(\text{full 1L}, \alpha_s(\alpha_b + \alpha_t), (\alpha_b + \alpha_t)^2, \alpha_s^2 \alpha_t)$ .

[1708.05720,1802.09886,1901.03651,1910.02094,...]

Advantages and disadvantages:

- + Precise for low SUSY scales,
- but for high scales  $\ln(M_{\tilde{t}}^2/M_t^2)$  terms spoil convergence of perturbative expansion.

## How to deal with intermediary SUSY scales?

For sparticles in the LHC range, both logs and suppressed terms might be relevant. We could try to improve

- ▶ fixed-order calculation → need to calculate more three- and two-loop corrections,
- ▶ EFT calculation → need to include higher-dimensional operators into calculation.

or ...



### Hybrid approach

Combine both approaches to get precise results for both regimes

Such an approach is implemented e.g. in FeynHiggs

[HB,Hahn,Heinemeyer,Hollik,Paßehr,Rzehak,Weiglein;1312.4937,1608.01880,1706.0034,1812.06452]

other approaches: 1609.00371,1703.03267,1710.03760,1910.03595;

other codes: FlexibleEFTHiggs, SARAH/SPheno



## Procedure in FeynHiggs

1. Calculation of diagrammatic fixed-order self-energies  $\hat{\Sigma}_{hh}$
2. Calculation of EFT prediction  $\lambda(M_t)v^2$
3. Add non-logarithmic terms contained in fixed-order result and the logarithms contained in EFT result

$$\hat{\Sigma}_{hh}(m_h^2) \longrightarrow [\hat{\Sigma}_{hh}(m_h^2)]_{\text{nolog}} - [v^2\lambda(M_t)]_{\text{log}}$$

In practice, this is achieved by using subtraction terms.

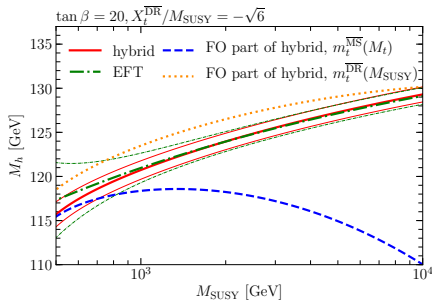
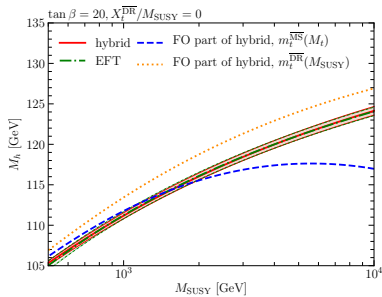
Additional complication:

FH by default uses OS scheme, for EFT calculation however  $\overline{\text{DR}}$  parameters needed (i.e.  $X_t^{\overline{\text{DR}}}$ )

→ 1L log only conversion of  $X_t$  sufficient

# Comparison of approaches [HB,Heinemeyer,Hollik,Weiglein,1912.04199]

Single-scale scenario with all non-SM particles at  $M_{\text{SUSY}}$



## “Rule of thumb”

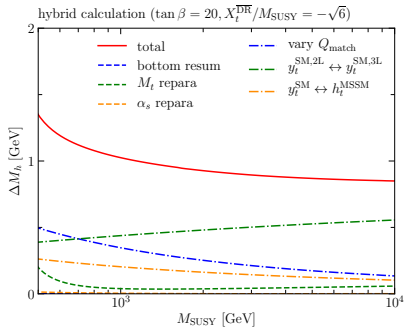
Remaining theoretical uncertainties (for  $\overline{\text{DR}}$  stop input parameter):

$$X_t/M_{\text{SUSY}} = 0 \rightarrow \Delta M_h \sim 0.5 \text{ GeV},$$

$$X_t/M_{\text{SUSY}} = \sqrt{6} \rightarrow \Delta M_h \sim 1 \text{ GeV}$$

Slightly higher for OS stop input parameters.

# Remaining uncertainties – individual sources

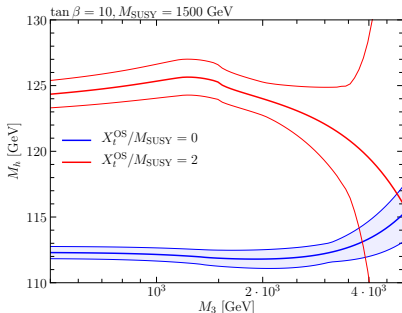


Uncertainty estimate dominated by:

- ▶ Uncertainty from higher order threshold corrections:
  - vary matching scale between SM and MSSM,
  - reexpress threshold correction in terms of  $h_t^{\text{MSSM}}$  instead of  $y_t^{\text{SM}}$ .
- ▶ Uncertainty of SM input couplings:
  - $y_t(M_t)$  extracted at the 2- or 3-loop level out of OS top mass.

One exception:  $M_{\tilde{g}} \gg M_{\tilde{t}}$

Increasingly relevant due to tightening LHC gluino limits.



Large uncertainty due to  $M_3$  power-enhanced terms appearing at the two-loop level in  $\overline{\text{DR}}$  EFT calculation (do not appear in OS scheme).

Needed EFT: MSSM without gluino

Expressions for unknown so far ...

# Solution: Absorb power-enhanced terms into renormalization scheme

[HB,Sobolev,Weiglein,1912.10002]

Use  $\overline{\text{MDR}}$  instead of  $\overline{\text{DR}}$  in EFT,

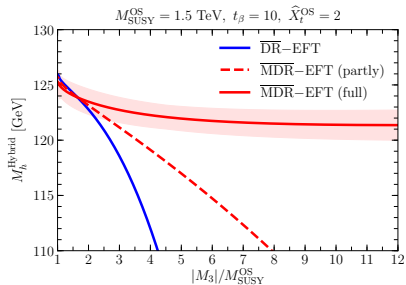
$$\left(m_{\tilde{t}_{L,R}}^{\overline{\text{MDR}}}\right)^2 = \left(m_{\tilde{t}_{L,R}}^{\overline{\text{DR}}}\right)^2 \left[ 1 + \frac{\alpha_s}{\pi} C_F \frac{|M_3|^2}{m_{\tilde{t}_{L,R}}^2} \left( 1 + \ln \frac{Q^2}{|M_3|^2} \right) \right],$$

$$x_t^{\overline{\text{MDR}}}(Q) = x_t^{\overline{\text{DR}}}(Q) - \frac{\alpha_s}{\pi} C_F M_3 \left( 1 + \ln \frac{Q^2}{|M_3|^2} \right),$$

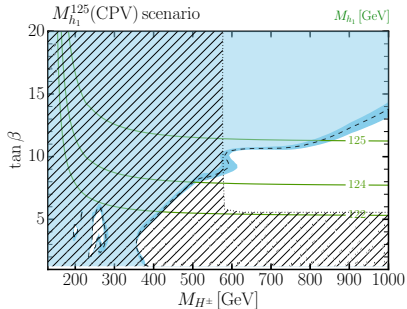
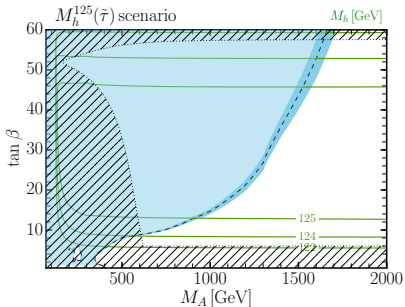
resums all  $\mathcal{O}(\alpha_s^n M_3^{2n}, \alpha_s^n M_3^n)$  terms.



Drastically reduced uncertainty.



# $M_h^{125}(\tilde{\tau})$ and $M_h^{125}(\text{CPV})$ scenarios



# $M_h^{125}$ (alignment) and $M_H^{125}$ scenarios

