

# CP structure of the top-Yukawa interaction: Phenomenology status and prospects

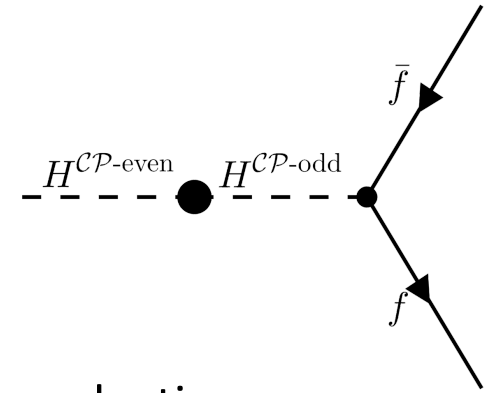
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# A CP-violating top-Yukawa coupling?



- CP violation can manifest in many Higgs couplings.
- CP violation in  $HVV$  couplings already tightly constrained via VBF and  $pp \rightarrow VH$  production as well as  $H \rightarrow 4l$  decay. [ATLAS,CMS: ...,2002.05315, 2104.12152,2109.13808,2202.06923,2205.05120]
- CP-violating  $HVV$  coupling can only be induced at the loop level  $\rightarrow$  expected to be small in most BSM theories.
- CP violation in Higgs–fermion couplings can be induced at the tree level.
- The largest Higgs–fermion coupling is the top-Yukawa coupling making it the prime target for current and future studies.

Focus of this talk: Overview of current status and prospects for constraining the CP structure of the **top-Yukawa coupling at the LHC.**

Note: Most studies concentrate on  $t\bar{t}H$ , but also  $tH$ ,  $tWH$ ,  $t\bar{t}$ , ... have been studied and can potentially be important.

# Different methods to constrain CP violation

## 1. Direct approach — pure CP-odd observables:

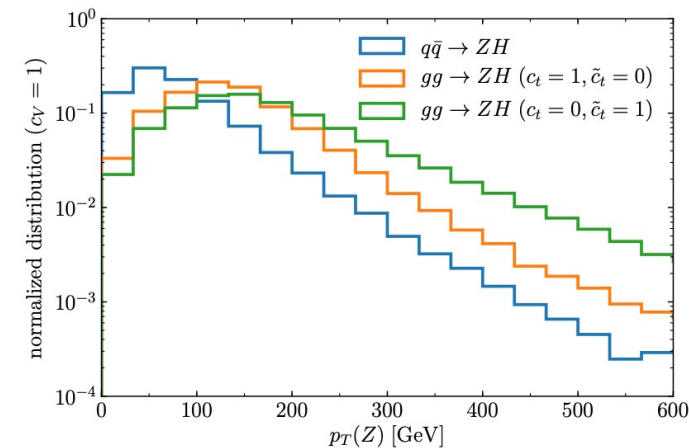
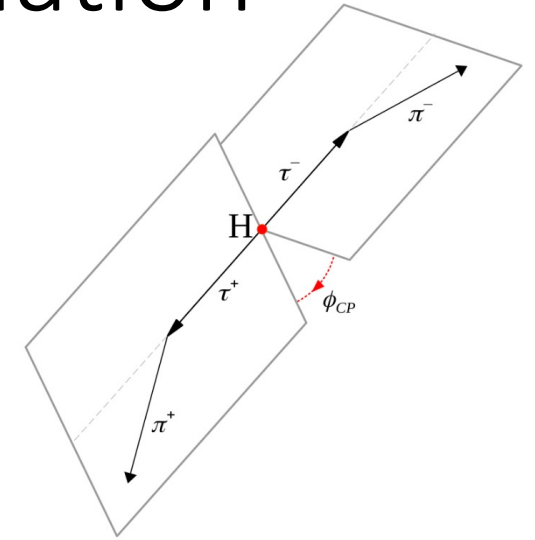
- Unambiguous markers for CP violation: e.g.
  - EDM measurements,
  - decay angle in  $H \rightarrow \tau^+ \tau^-$ .
- Experimentally difficult since often polarization information is needed.

## 2. Indirect approach — pure CP-even observables:

- Many rate measurements are indirectly sensitive: e.g.  $ggH$  or  $H \rightarrow \gamma\gamma$ .
- Deviations from SM need not be due to CP violation.

## 3. Kinematic approach:

- CP-odd coupling affects kinematics.
- High sensitivity expected if all available kinematic information is used.
- Deviations from SM do not have to be due to CP violation.



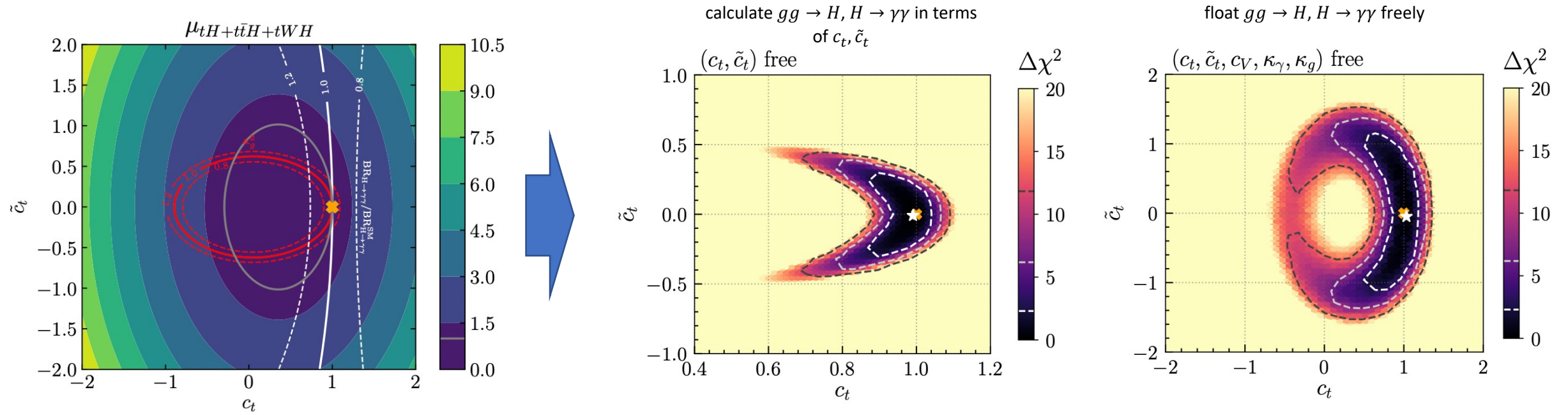
Exploit all three complementary approaches to learn as much as possible!

# CP-sensitive rate measurements

[Freitas `12; Djouadi `13; Agrawal `12; Ellis `13; Chang `14; He `15; Boudjema `15; Demartin `15,`16; Kobakhidze `16; Hou `18; Cao `19; Fuchs `20; HB `20,`22; Brod `22]

- The total rate of many processes is indirectly sensitive to the CP structure of the top-Yukawa coupling:

$$gg \rightarrow H, H \rightarrow \gamma\gamma, t\bar{t}H, tH, tWH, gg \rightarrow ZH, t\bar{t}, t\bar{t}t\bar{t}, \text{ etc.}$$



→ To improve indirect constraints in the future, need to disentangle channels ( $t\bar{t}H$  vs  $tH$ ,  $q\bar{q} \rightarrow ZH$  vs  $gg \rightarrow ZH$ ).

# CP-odd observables for $t\bar{t}H$

[Ellis `13; Boudjema `15; Buckley `15; Mileo `16; Azevedo `17; Goncalves `18; Faroughy `19; Bortolato `20; Goncalves `21; Barman `21; Azevedo `21]

- Writing  $\mathcal{L}_{\text{top-Yuk}} = -\frac{y_t^{\text{SM}}}{\sqrt{2}} \bar{t}(c_t + i\gamma_5 \tilde{c}_t)tH$ , we can split up the  $t\bar{t}H$  amplitude into a CP-even and a CP odd part:  $\mathcal{M}_{t\bar{t}H} = c_t \mathcal{M}_{t\bar{t}H}^{\text{CP-even}} + \tilde{c}_t \mathcal{M}_{t\bar{t}H}^{\text{CP-odd}}$ .

- The squared amplitude is then decomposed as:

$$|\mathcal{M}_{t\bar{t}H}|^2 = c_t^2 |\mathcal{M}_{t\bar{t}H}^{\text{CP-even}}|^2 + 2c_t \tilde{c}_t \text{Re}[\mathcal{M}_{t\bar{t}H}^{\text{CP-even}} \mathcal{M}_{t\bar{t}H}^{\text{CP-odd}*}] + \tilde{c}_t^2 |\mathcal{M}_{t\bar{t}H}^{\text{CP-odd}}|^2$$

- CP violation is only caused by the second term, which involves a factor

$$\text{Tr}[\gamma^\mu \gamma^\nu \gamma^\sigma \gamma^\rho \gamma^5] \propto \epsilon^{\mu\nu\rho\sigma}$$

⇒ At least four independent four-vectors are needed to construct CP-odd observables.

⇒ We need to reconstruct the top-quark polarization vectors.

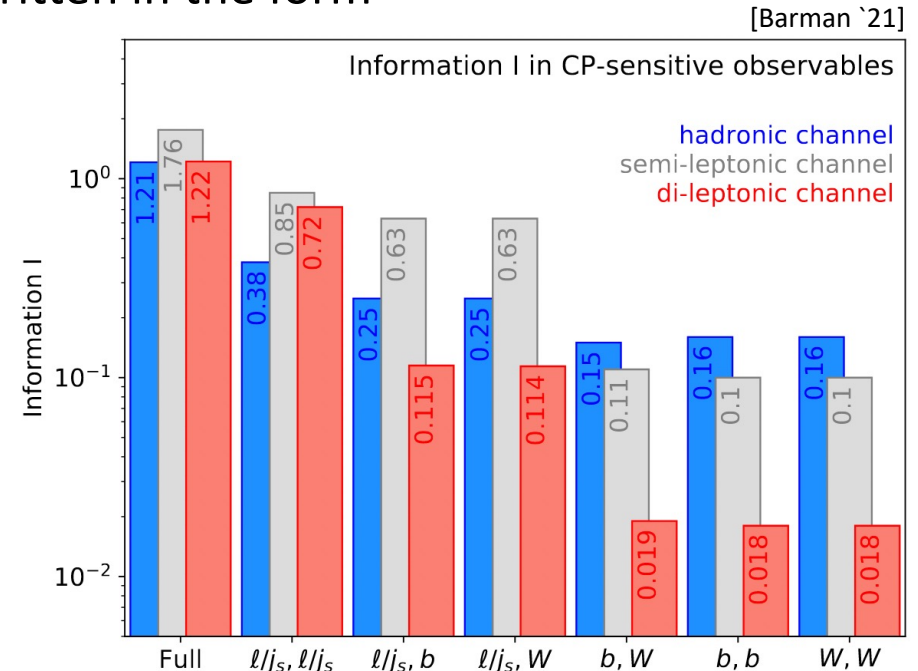
# CP-odd observables for $t\bar{t}H$ – top decays

- The polarization of the top-quarks can be reconstructed from the top decay products: works best for leptons, worse for light jets, even worse for b-jets and W bosons.  
 $\Rightarrow$  Trade-off between rate and spin analyzing power.

- In the  $t\bar{t}$  rest frame. the CP-odd observables can be written in the form

$$\Delta\phi_{ik}^{t\bar{t}} = \text{sgn} [\vec{p}_t \cdot (\vec{p}_i \times \vec{p}_k)] \arccos \left[ \frac{|\vec{p}_t \times \vec{p}_i|}{|\vec{p}_t \times \vec{p}_k|} \cdot \frac{|\vec{p}_t \times \vec{p}_k|}{|\vec{p}_t \times \vec{p}_i|} \right].$$

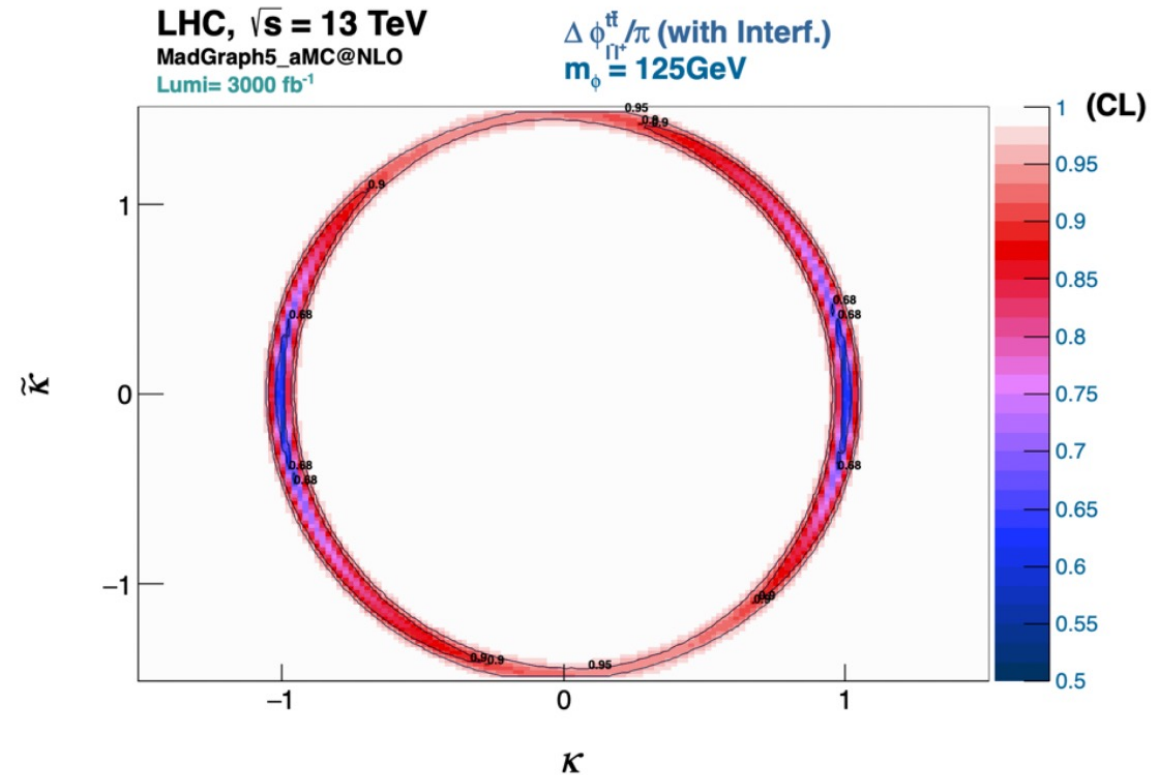
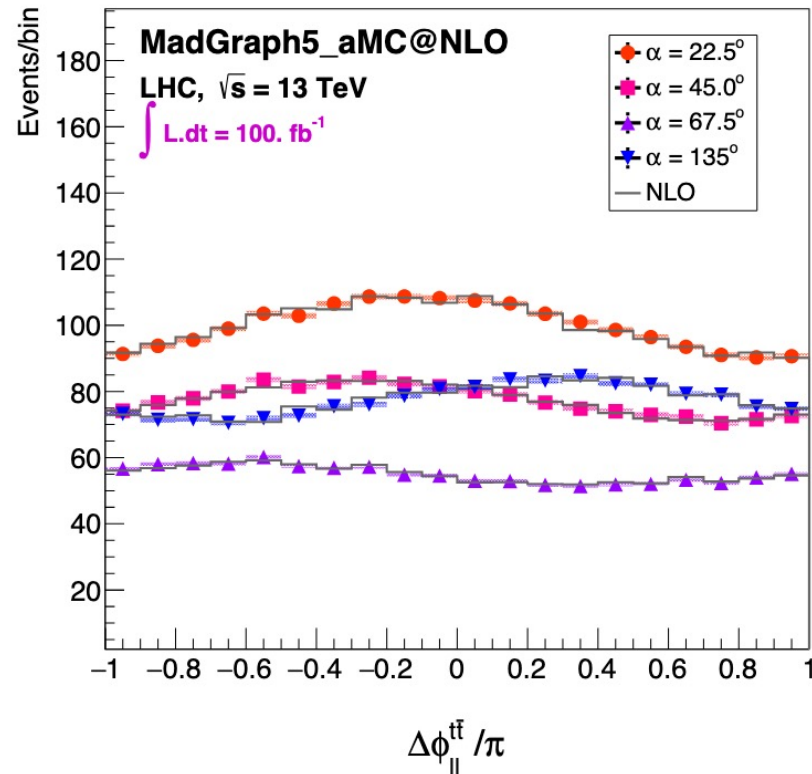
$\Rightarrow \Delta\phi_{\ell\ell}^{t\bar{t}}$  and  $\Delta\phi_{\ell j_{\text{soft}}}^{t\bar{t}}$  most promising.



# CP-odd observables for $t\bar{t}H$ – HL-LHC sensitivity.

[Azevedo, Capucha, Onofre, Santos `22]

$$\mathcal{L} = \kappa_t y_t \bar{t} (\cos \alpha + i \gamma_5 \sin \alpha) t \phi = y_t \bar{t} (\kappa + i \gamma_5 \tilde{\kappa}) t \phi,$$



After taking into account shower and detector effects, CP asymmetries are quite small  
 $\Rightarrow$  Interference term will be hard to measure even at HL-LHC.

# Kinematic approach – CP-sensitive observables I

[Gunion '96; Ellis '13; Yue '14; Demartin '14, '15, '16; He '15; Buckley '15; Gritsan '16; Azevedo '17; Goncalves '18; Cao '20; Barman '21; HB '21; Azevedo '22; ATLAS '22]

Various CP-sensitive (but not CP-odd) observables have been investigated and used in the literature:

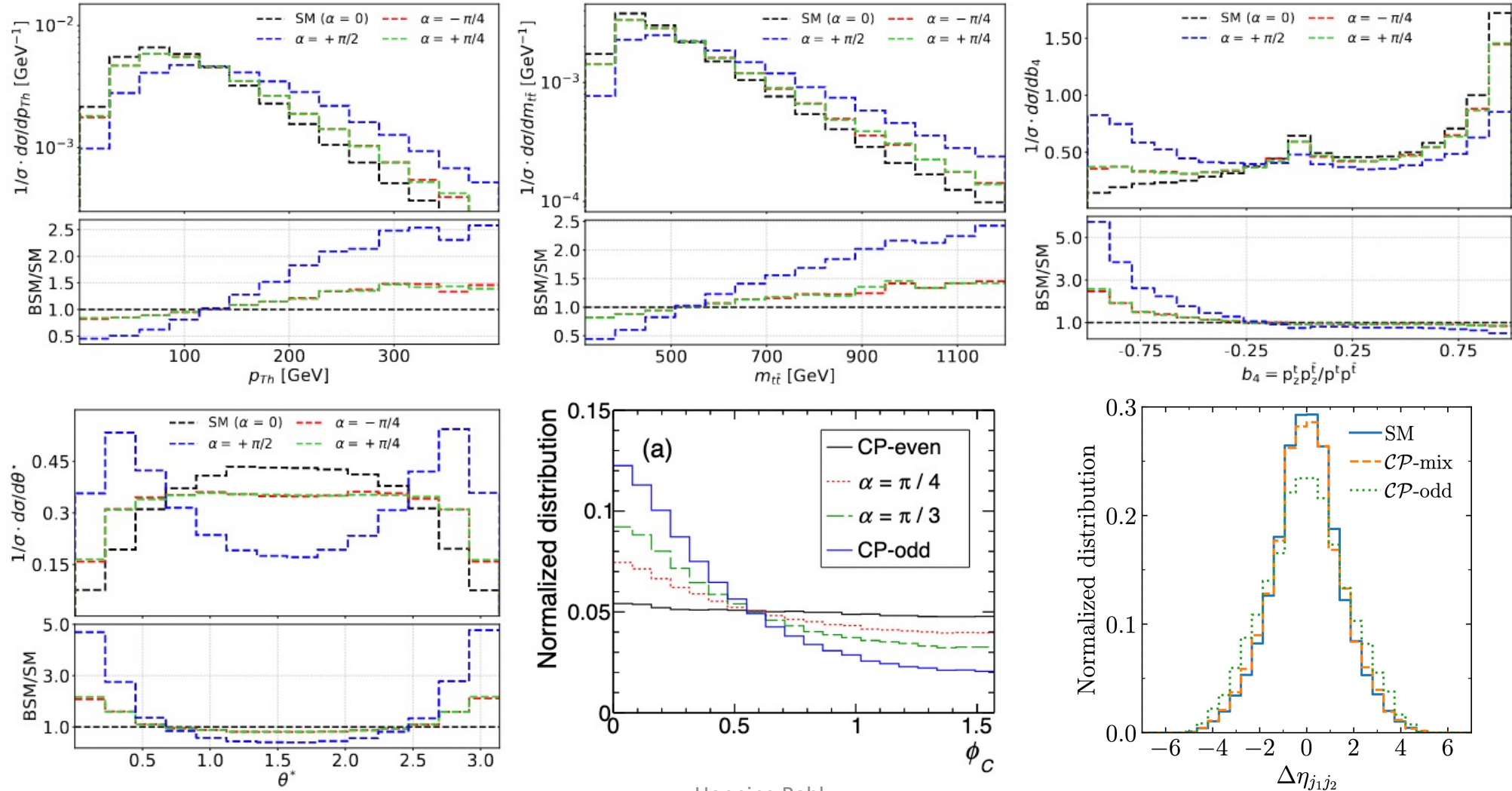
- Higgs transverse momentum:  $p_{T,H}$ ,
- invariant mass of the top-quark system:  $m_{t\bar{t}}$ ,
- angle between top-beam and anti-top-beam planes:  $b_2 = (\vec{p}_t \times \hat{n}) \cdot (\vec{p}_{\bar{t}} \times \hat{n}) / (|\vec{p}_t| |\vec{p}_{\bar{t}}|)$
- projection of top-quark momenta:  $b_4 = p_t^z p_{\bar{t}}^z / p_t p_{\bar{t}}$ ,
- angle between the top quark and the beam direction in the  $t\bar{t}$  CM frame:  $\theta^*$ ,
- angular separations between the two leading jets:  $\Delta\phi_{j_1 j_2}, \Delta\eta_{j_1 j_2}$ ,
- angle between plane of incoming protons and  $t\bar{t}$  plane in Higgs CMS:  $\phi_C$
- etc.

→ Sensitivity of various observables depends on Higgs decay process, kinematic region, ...



# Kinematic approach – CP-sensitive observables II

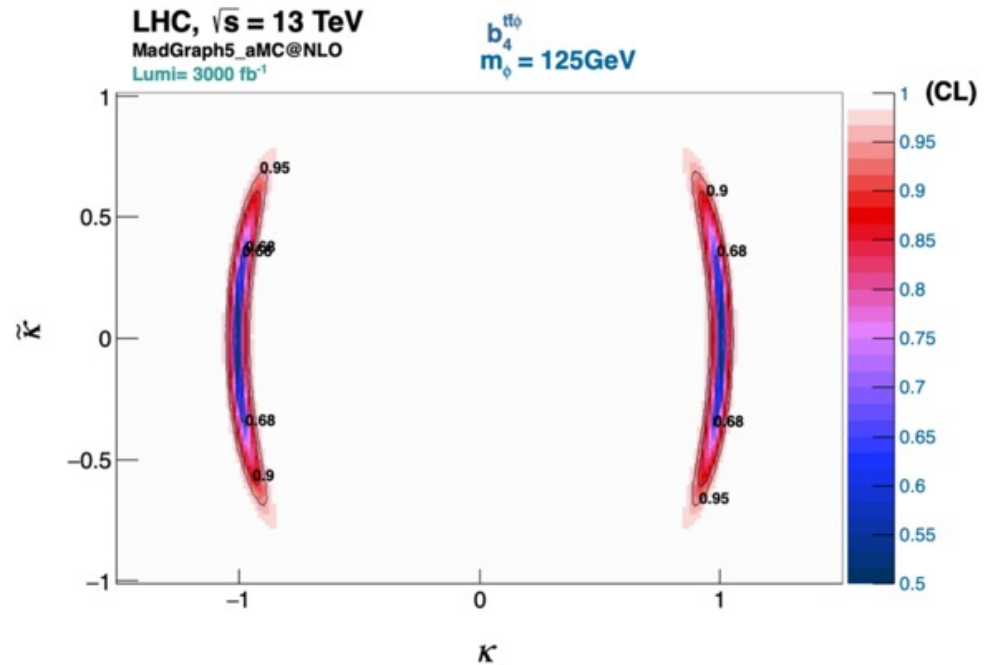
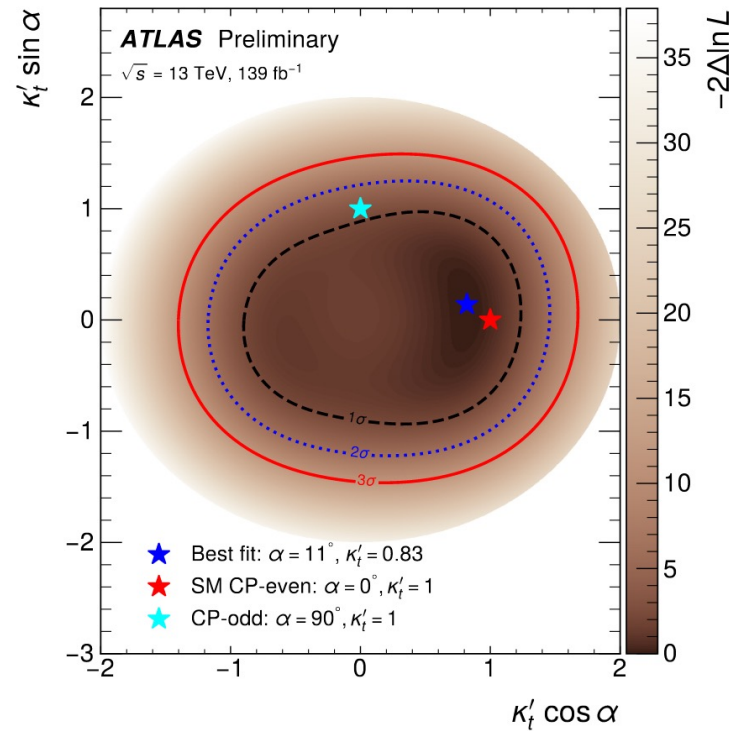
[Cao, Xie, Zhang, Zhang '20; Barman, Goncalves, Kling '21; HB, Brass '21]



# Kinematic approach – CP-sensitive observables III

[Azevedo '22, ATLAS '22]

(projected) limits for  $t\bar{t}H$  with  $H \rightarrow \bar{b}b$  based on CP-sensitive observables:



# Kinematic approach – multivariate analyses I

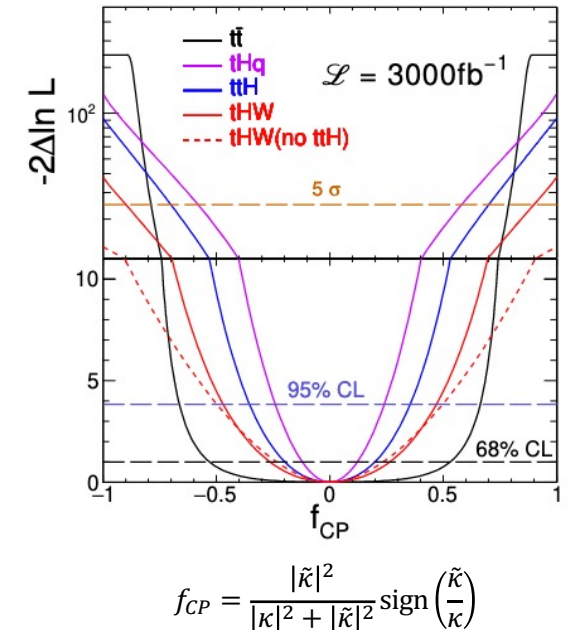
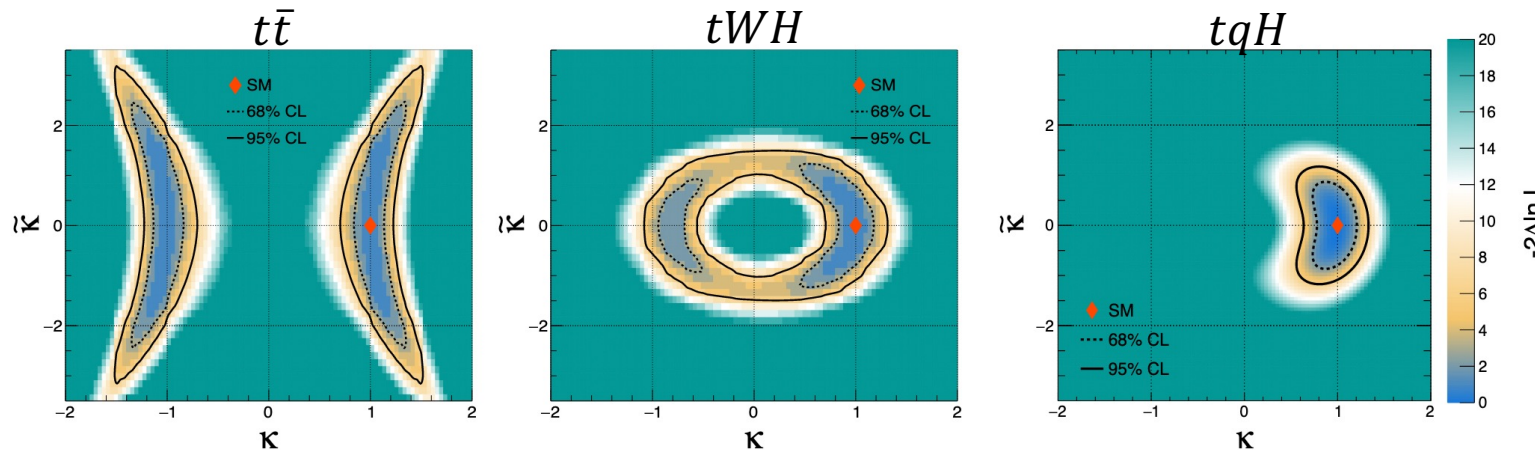
[Gritsan`16; Ren`19; Kraus`19; CMS`20,`21,`22; ATLAS`20,`22; Martini`21; Butter`22]

## 1. Matrix-element approach:

$$P(\mathbf{x}|\alpha) = \frac{1}{\sigma(\alpha)} \int d^n y \frac{d^n \sigma(\mathbf{y}|\alpha)}{dy_1 \dots dy_n} W(\mathbf{y}, \mathbf{x})$$

$$-\log(\mathcal{L}) = -\sum_{i=1}^N \log(P(\mathbf{x}_i|\alpha))$$

Transfer function encodes parton shower and detector effects.



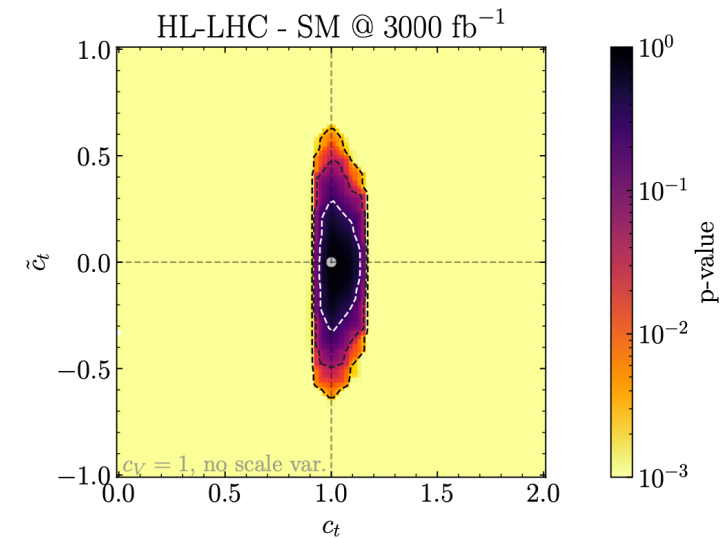
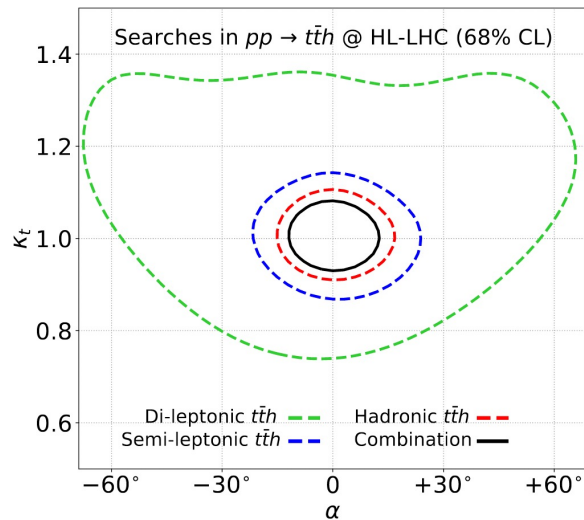
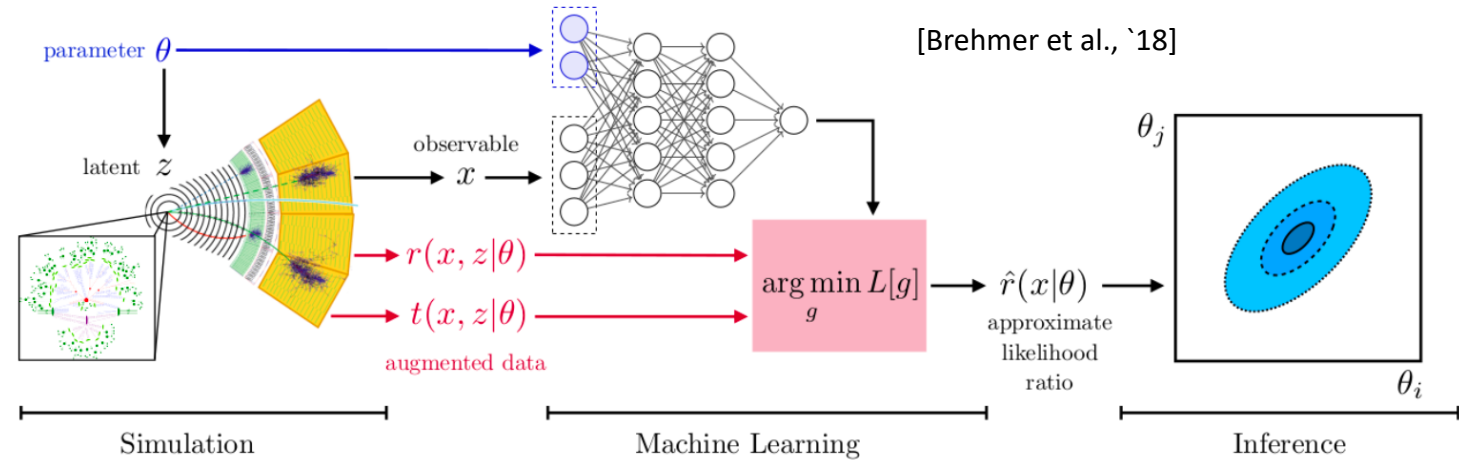
$$f_{CP} = \frac{|\tilde{\kappa}|^2}{|\kappa|^2 + |\tilde{\kappa}|^2} \text{sign}\left(\frac{\tilde{\kappa}}{\kappa}\right)$$

## 2. BDTs: Train BDT to differentiate CP-even and CP-odd events.

# Kinematic approach – multivariate analyses II

[Barman '21; HB '21]

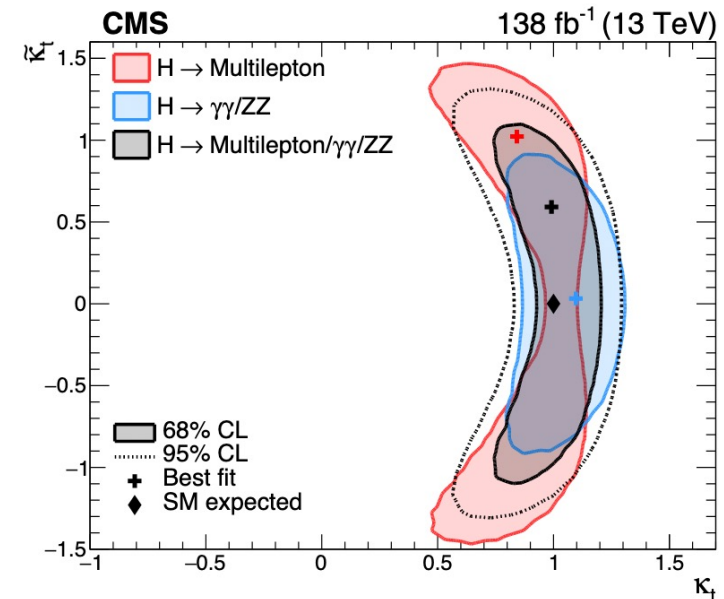
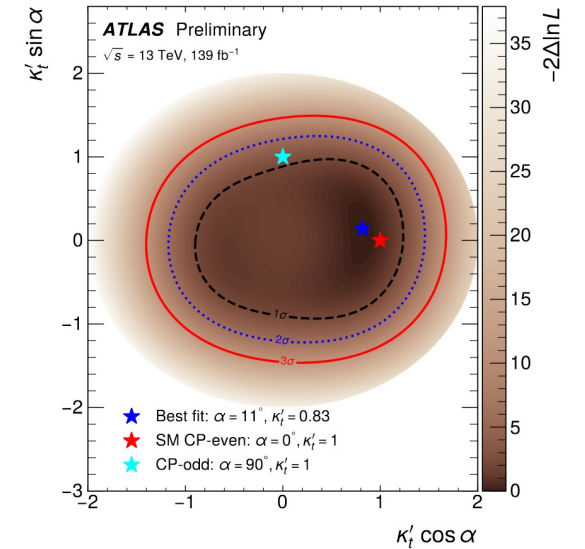
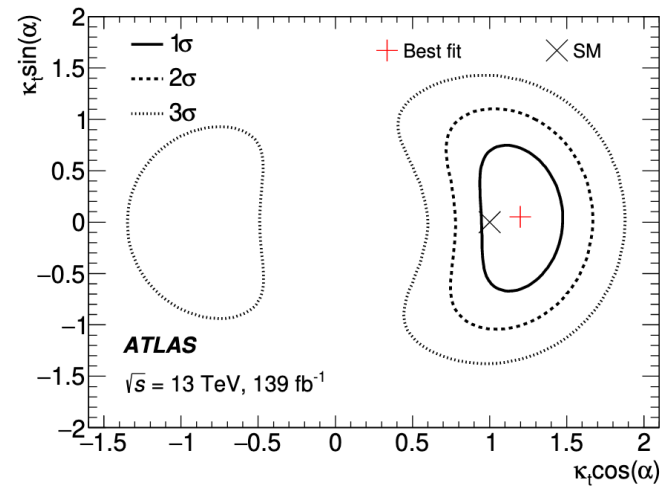
### 3. Machine-learning-based inference: Train neural network to learn likelihood directly.



# Experimental results

Several Run-2 results are already available:

- **ATLAS:** [2004.04545, ATLAS-CONF-2022-016]
  - $t\bar{t}H + tH$  with  $H \rightarrow \gamma\gamma$  (BDTs)
  - $t\bar{t}H + tH$  with  $H \rightarrow \bar{b}b$  (CP-sensitive observables + BDTs)
- **CMS:** [2003.10866, 2104.12152, 2208.02686]
  - $t\bar{t}H$  with  $H \rightarrow \gamma\gamma$  (BDTs)
  - $t\bar{t}H$  with  $H \rightarrow 4l$  (BDTs)
  - $t\bar{t}H + tH$  with  $H \rightarrow WW, \tau\tau$  (BDTs)



# Literature overview

## Indirect approach via rate measurements

- Freitas & Schwaller, <https://arxiv.org/pdf/1211.1980.pdf>
- Agrawal et al., <https://arxiv.org/pdf/1211.4362.pdf>
- Djouadi & Moreau, <https://arxiv.org/pdf/1303.6591.pdf>
- Ellis et al., <https://arxiv.org/pdf/1312.5736.pdf>
- Chang et al., <https://arxiv.org/pdf/1403.2053.pdf>
- He et al., <https://arxiv.org/pdf/1501.00012.pdf>
- Boudjema et al., <https://arxiv.org/pdf/1501.03157.pdf>
- Demartin et al., <https://arxiv.org/pdf/1504.00611.pdf>
- Demartin et al., <https://arxiv.org/pdf/1607.05862.pdf>
- Kobakhidze et al., <https://arxiv.org/pdf/1610.06676.pdf>
- Hou et al., <https://arxiv.org/pdf/1806.06018.pdf>
- Cao et al., <https://arxiv.org/pdf/1901.04567.pdf>
- Fuchs et al., <https://arxiv.org/pdf/2003.00099.pdf>
- Brod et al., <https://arxiv.org/pdf/2203.03736.pdf>
- Bahl et al. <https://arxiv.org/pdf/2007.08542.pdf>
- Bahl et al. <https://arxiv.org/pdf/2202.11753.pdf>

## CP-sensitive observables

- Gunion & He, <https://arxiv.org/pdf/hep-ph/9602226.pdf>
- Ellis et al., <https://arxiv.org/pdf/1312.5736.pdf>
- Yue, <https://arxiv.org/pdf/1410.2701.pdf>
- Demartin et al., <https://arxiv.org/pdf/1407.5089.pdf>
- He et al., <https://arxiv.org/pdf/1501.00012.pdf>
- Demartin et al., <https://arxiv.org/pdf/1504.00611.pdf>
- Buckley & Goncalves, <https://arxiv.org/pdf/1507.07926.pdf>
- Demartin et al., <https://arxiv.org/pdf/1607.05862.pdf>
- Gritsan et al., <https://arxiv.org/pdf/1606.03107.pdf>
- Azevedo et al., <https://arxiv.org/pdf/1711.05292.pdf>
- Goncalves et al., <https://arxiv.org/pdf/1804.05874.pdf>
- Cao et al., <https://arxiv.org/abs/2008.13442>
- Martini et al., <https://arxiv.org/pdf/2104.04277.pdf>
- Barman et al., <https://arxiv.org/pdf/2110.07635.pdf>
- Bahl & Brass, <https://arxiv.org/pdf/2110.10177.pdf>
- Azevedo et al., <https://arxiv.org/pdf/2208.04271.pdf>

## Multivariate analyses

- Gritsan et al., <https://arxiv.org/pdf/1606.03107.pdf>
- Ren et al., <https://arxiv.org/pdf/1901.05627.pdf>
- Kraus et al., <https://arxiv.org/pdf/1908.09100.pdf>
- Martini et al., <https://arxiv.org/pdf/2104.04277.pdf>
- Barman et al., <https://arxiv.org/pdf/2110.07635.pdf>
- Bahl & Brass, <https://arxiv.org/pdf/2110.10177.pdf>
- Butter et al., <https://arxiv.org/pdf/2210.00019.pdf>

## Experimental results

- CMS, <https://arxiv.org/pdf/2003.10866.pdf>
- ATLAS, <https://arxiv.org/pdf/2004.04545.pdf>
- CMS, <https://arxiv.org/pdf/2104.12152.pdf>
- CMS, <https://arxiv.org/pdf/2208.02686.pdf>
- ATLAS, <http://cds.cern.ch/record/2805772/files/ATLAS-CONF-2022-016.pdf>



# Conclusions

- Many BSM theories predict largest amount of CP violation in Higgs–fermion couplings.  
→ much work has been invested in constraining the CP character of the top-Yukawa interaction.
- Three different approaches can be pursued:
  - Indirect approach based on rate measurements  
→ very strong but model-dependent constraints.
  - Direct approach based on CP-odd observables  
→ easily interpretable results but low sensitivity.
  - Kinematic approach (specific observables or multivariate analysis)  
→ strong constraints possible but deviations need not be due to CP violation.



Exploit all three complementary approaches to learn as much as possible!

**Thanks for your attention!**