Deciphering the Nature of the Higgs boson *CP and beyond*

Henning Bahl

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- \rightarrow What is still left to explore?

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So, everything left to do is to confirm the SM with even more precision? → No!

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- Existing measurements already provide strong guidance for BSM model building.
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 \Rightarrow Strong motivation for on-going and future Higgs precision programs.

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• Higgs precision measurements put stringent constraints on many BSM scenarios.

Simplified scaling analysis:

• 1% precision level can constrain BSM particles with mass from 100 GeV to several TeV (within reach of the LHC or future colliders).

Conservative Scaling for Upper Limit on Mass Scale Probed by Higgs Precision

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We also shouldn't forget about the interplay with direct searches!

Interplay with direct searches

- Important interplay between Higgs precision measurements and direct searches for BSM particles.
- Cannot be captured in EFT framework \rightarrow use 2HDM here as a benchmark model.
- Searches for BSM scalars ϕ :

a) CMS:
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\nd) ATLAS: $pp \rightarrow \phi \rightarrow WW, ZZ, WZ$
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Have we found the SM Higgs?

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[figure by J. Braathen]

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Is the Higgs trilinear also a discovery tool?

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- Additional enhancement by 2L corrections.
- Maximal size bounded by perturbative unitarity.
- Currently strongest experimental limit on κ_1 :

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Already current experimental limits on κ_{λ} probe so-far unconstrained BSM parameter space!

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Consider toy model:

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- $\mathcal{O}(\text{MeV})$ constraints on Γ_H .
- But depends on assumption that there is no other BSM contribution to $H \rightarrow ZZ$ production.

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CP provides an "additional dimension"

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\sum \text{ Rewrite:} \quad \mathcal{L}_{\text{yuk}} = - \sum \limits_{f=u,d,c,s,t,b,e,\mu,\tau} \frac{y_f^{\text{SM}}}{\sqrt{2}} \bar{f}(c_f + i \gamma_5 \tilde{c}_f) fH,
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What is the current status?

Fermions

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Fermions

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Fermions

- CP structure of HWW , HZZ interactions is comparably wellconstrained. [ATLAS,CMS:..,2002.05315, 2104.12152,2109.13808,2202.06923,2205.05120]
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What about future colliders?

Future collider outlook

Limits set on: $f_{CP}^{HX} \equiv \frac{\Gamma_{H \rightarrow X}^{CP \, \text{odd}}}{\Gamma_{H \rightarrow X}^{CP \, \text{odd}} + \Gamma_{H \rightarrow X}^{CP \, \text{even}}}$

[Snowmass Higgs CP report, 2205.07715]

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New ideas/techniques are needed to make the most of current and future data!

Constraining CP violation

CP violation in the Higgs sector can be constrained using:

- **Pure CP-odd observables**:
	- Unambiguous markers for CP violation: e.g.
		- EDM measurements,
		- decay angle in $H \to \tau^+ \tau^-$.
	- Typically requires to access polarization of particles coupling to the Higgs.
	- Experimentally difficult for many LHC processes (i.e., top-associated Higgs production).
	- Almost impossible for $H \to b\overline{b}$ or $H \to \mu^+\mu^-$

Constraining CP violation

CP violation in the Higgs sector can be constrained using:

- **Pure CP-even observables**:
	- Many rate measurements are indirectly sensitive: e.g. ggH .
	- Decay rates: e.g., $\Gamma_{H\rightarrow b\bar{b}} \propto c_b^2 + \tilde{c}_b^2$.
	- Subtle effects in kinematic distributions of CP-even observables (e.g. $p_{T,H}$ in $t\bar{t}H$).
	- Deviations from SM need not be due to CP violation \rightarrow degeneracies with non-CPV BSM effects.

Constraining CP violation

CP violation in the Higgs sector can be constrained using:

- **Multivariate analyses:**
	- Exploit full kinematic information using machine learning.
	- Often mixes CP-even and CP-odd observables.
	- High sensitivity.
	- Can be difficult to reinterpret.

[e.g. simulation-based inference, Brehmer et al.,1805.00013, …]

Exploit and combine all three complementary approaches to learn as much as possible!

Improving LHC CP measurements I

CP-sensitive STXS extension for $t\bar{t}H$

[HB,Carnelli,Deliot,Fuchs,Kotsokechagia,Marsault,Menen,Schoeffel,Saimpert; to appear]

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- Many CP-sensitive observables have been proposed in the literature.
- Test them against each other for
	- $H \rightarrow \gamma \gamma$
	- $H \rightarrow b\overline{b}$
	- $H \rightarrow$ multi-lepton

Investigated observables

- Tested 11 observables (1D) in different reference frames and their 2D combinations.
- In total, 465 different combinations
- Apply channel-specific smearing factors and reconstruction efficiencies to mimic existing experimental analysis.
- Removed rate information for $H \to b\overline{b}$, multi-lepton because of large backgrounds.
- Parameterize top Yukawa as $\mathcal{L}_{\text{top-Yuk}} = \frac{y_t^{\text{SM}} g_t}{\sqrt{2}} \bar{t} (\cos \alpha_t + i \gamma_5 \sin \alpha_t) tH$

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Use significance *S* to exclude $\alpha_t = 35^\circ$ as performance metric.

Significance tables

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- Most sensitive combination: $(\Delta \phi_{t\bar{t}}^{\rm lab}, b_2^{t\bar{t}})$ with $S=1.67$
- Most sensitive combination with p_{TH} : $(p_{T,H}^{\text{lab}}, b_2^{\tilde{t}})$ with $S = 1.65$

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Extending the current STXS by a second dimension provides near optimal sensitivity!

Expected limits

Improving LHC CP measurements

Classifying the CP nature of Higgs + 2 jet production

[HB,Hannig,Menen,Fuchs,2309.03146]

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- Two additional jets in the final state allow to construct CP-odd observables \rightarrow direct CP test.
- Allows for indirect constraint of CP character of top-Yukawa interaction.

ggF2j— amplitude structure

• Effective Lagrangian (after integrating out the top quark, SM: $c_g = 1$, $\tilde{c}_g = 0$):

 ${\cal L}_{Hgg}=-\frac{1}{4v}H\left(-\frac{\alpha_S}{3\pi}c_gG_{\mu\nu}^aG^{a,\mu\nu}+\frac{\alpha_S}{2\pi}\tilde{c}_gG_{\mu\nu}^a\right.$ (heavy top limit enforced by p_T cut)

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• Amplitude splits up into three pieces:

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|\mathcal{M}_{ggF2j}|^2 = c_g^2 |\mathcal{M}_{even}|^2 + 2c_g \tilde{c}_g Re[\mathcal{M}_{even} \mathcal{M}_{odd}^*] + \tilde{c}_g^2 |\mathcal{M}_{odd}|^2
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interference

• Existing measurements focus on CP-odd $\Delta\phi_{jj}$ observable to constrain interference term.

Analysis flow $X = ggF2j, VBF$ **VBF** $|\mathcal{M}_{\rm even}|^2$ $\operatorname{Classifier}$ $P(|\mathcal{M}_{\rm even}|^2)$ Classifier $X-$ Limits X-Interf. $\mathrm{ggF}2\mathrm{j}$ production production $\operatorname{Classifier}$ $P($ Interf. $)$ $\left|\mathcal{M}_\mathrm{odd}\right|^2$ VH

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- Then, train two classifiers to distinguish
	- $|\mathcal{M}_{\rm even}|^2$ vs. $|\mathcal{M}_{\rm odd}|^2 \to P(|\mathcal{M}_{\rm even}^2|)$, and
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	- (positive intf.) vs (negative intf) \rightarrow P(Interf.).
- Build two observables: CP-even $P(c_g^2)$ and CP-odd $P_+ P_-$.

ggF2j signal region

- ggF2j signal region outperforms VBF signal region (not shown),
- $\Delta \phi_{ij}$ limit is significantly worse.

Complementarity with EDM measurements

What do EDM measurements tell us about the Higgs CP nature?

[HB et al., 2202.11753; see also Brod et al., 2203.03736]

Complementarity with EDM constraints

- Several EDMs are sensitive to CP violation in the Higgs sector.
- Consider here only constraints from theoretically cleanest EDM: the electron EDM. [Brod et al.,1310.1385,1503.04830, 1810.12303, 2203.03736;Panico et al.,1810.09413;Altmannshofer et al.,2009.01258]
- Limit by ACME collaboration: $d_e^{\rm ACME}=1.1\cdot 10^{-29}e$ cm at 90% CL. [ACME, Nature 562 (2018) 7727, 355-360]

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- $\cdot \frac{d_e}{dA}$ d_e^A $\frac{u_e}{A C M E} \simeq c_e (870.0 \tilde{c}_t + 3.9 \tilde{c}_b + 3.4 \tilde{c}_\tau + \cdots) + \tilde{c}_e (610.1 c_t + 3.1 c_b + 2.8 c_\tau - 1082.6 c_V + \cdots)$

Complementarity with EDM constraints

- Several EDMs are sensitive to CP violation in the Higgs sector.
- Consider here only constraints from theoretically cleanest EDM: the electron EDM. [Brod et al.,1310.1385,1503.04830, 1810.12303, 2203.03736;Panico et al.,1810.09413;Altmannshofer et al.,2009.01258]
- Limit by ACME collaboration: $d_e^{\rm ACME}=1.1\cdot 10^{-29}e$ cm at 90% CL. [ACME, Nature 562 (2018) 7727, 355-360]
- $\cdot \frac{d_e}{dA}$ d_e^A $\frac{u_e}{A C M E} \simeq \frac{c_e}{370.0 \tilde{c}_t + 3.9 \tilde{c}_b + 3.4 \tilde{c}_\tau + \cdots) + \tilde{c}_e}{610.1 c_t + 3.1 c_b + 2.8 c_\tau - 1082.6 c_V + \cdots)}$
- Bounds strongly depend on assumptions about electron-Yukawa coupling.

Complementarity with EDM constraints: t and τ

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[see also Fuchs et al.,1911.08495]

EDM > LHC? No.

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CP-insensitive $H \to \mu^+ \mu^-$ rate measurement outperforms EDM constraint.
Dependence on electron-Yukawa coupling

- Electron Yukawa-coupling only very weakly constrained ($g_e \le 268$ at 95% CL).
- If c_e smaller, eEDM significantly weakened.
- Moreover, we can fine-tune CP-odd electron-Yukawa coupling such that $d_e < d_e^{\rm ACME}.$
- Neutron EDM has similar dependence on firstgeneration quark-Yukawa couplings.

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LHC bounds important since they do not depend on 1st gen. Yukawa couplings.

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The Higgs will keep us busy for many decades to come!

Appendix

Case study: real singlet extension of the SM

$$
V(\Phi, S) = V_{\rm SM}(\Phi) + \frac{1}{2}\mu_s^2 S^2 + \frac{1}{4!} \lambda_s S^4 + \lambda_{S\Phi} S^2 \Phi^{\dagger} \Phi
$$

If S does not get a vev, $\lambda_{HHH} = \lambda_{HHH}^{SM}$ at the tree-level ($m_S^2 = \mu_S^2 + \lambda_{S\Phi} v^2$).

The 1L correction to λ_{HHH} scales like ($\lambda_\Phi^{\rm SM} \sim 0.25$)

$$
\kappa_\lambda \equiv \frac{\lambda_{HHH}}{\lambda_{HHH}^{\rm SM}}\!=\!1+\frac{1}{(4\pi)^2}\frac{m_S^4}{v^4\lambda_\Phi^{\rm SM}}\bigg(1-\frac{\mu_S^2}{m_S^2}\bigg)^3
$$

whereas the dominant correction to other Higgs couplings scale like

$$
\kappa_g \equiv \frac{g}{g^{SM}} = 1 + \frac{1}{(4\pi)^2} \frac{m_S^2}{v^2} \left(1 - \frac{\mu_S^2}{m_S^2} \right)^2
$$

Deviation in λ_{HHH} enhanced by a factor $\frac{m_S^2}{n^2\lambda^2}$ $v^2\lambda_\Phi^{\rm SI}$ $\frac{\frac{2}{5}}{\text{SM}}\left(1-\frac{\mu_S^2}{m^2}\right)$ $\left(\frac{\mu_S}{m_S^2}\right)$ w.r.t. to other Higgs couplings!

Interlude: HiggsTools [HB et al., 2210.09332]

C++ interface for high performance; Python and Mathematica interfaces for ease of use.

[Joecy et al.,9410282;Kainulainen et al.,0105295, 0202177;Prokopec et al., 0312110, 0406140;Konstandin et al.,1302.6713, 1407.3132]

- VIA approach yields consistently higher results by orders of magnitude.
- We use VIA approach with bubble wall parameters close to optimal values for Y_B : [de Vries,1811.11104;Fuchs et al.,2003.00099,2007.06940;Shapira,2106.05338]

$$
\frac{Y_B}{Y_B^{\rm obs}} \simeq 28 \tilde{c}_t - 0.2 \tilde{c}_b - 11 \tilde{c}_\tau + \cdots
$$

/ values should be regarded as **upper bound** on what is theoretically achievable.

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$$
\lambda_{HHH}^{1L} \propto \frac{g_{HSS}^{3}}{(4\pi)^{2}} C_{0}(\dots) \propto \frac{g_{HSS}^{3}}{(4\pi)^{2}} \frac{1}{m_{S}^{2}} \propto \frac{1}{(4\pi)^{2}} \frac{m_{S}^{4}}{v^{3}} \left(1 - \frac{\mu_{S}^{2}}{m_{S}^{2}}\right)^{3} \Rightarrow \kappa_{\lambda} \equiv \frac{\lambda_{HHH}}{\lambda_{HHH}^{SML}} = 1 + \frac{1}{(4\pi)^{2}} \frac{m_{S}^{4}}{v^{4} \lambda_{\Phi}^{SM}} \left(1 - \frac{\mu_{S}^{2}}{m_{S}^{2}}\right)^{3}
$$

whereas the dominant correction to other Higgs couplings scale like

$$
g^{1L} \propto \frac{g_{HSS}^2}{(4\pi)^2} B_0'(\dots) \cdot g_{\text{tree}} \propto \frac{1}{(4\pi)^2} \frac{m_S^2}{v^2} \left(1 - \frac{\mu_S^2}{m_S^2}\right)^2 \Rightarrow \kappa_g \equiv \frac{g}{g^{SM}} = 1 + \frac{1}{(4\pi)^2} \frac{m_S^2}{v^2} \left(1 - \frac{\mu_S^2}{m_S^2}\right)^2
$$

Deviation in λ_{HHH} enhanced by a factor $\frac{m_S^2}{v^2\lambda_{\Phi}^{SM}}\left(1-\frac{\mu_S^2}{m_S^2}\right)$ w.r.t. to other Higgs couplings!

 $-\overline{H} \left(\frac{S}{S}\right)$

 $S\sim\begin{matrix}5\\1\\1\\3\\3\\4\end{matrix}$

Calculating BSM corrections to κ_{λ}

• Need to calculate Higgs three-point function:

• Alternatively, employ zero momentum approximation and then use effective potential:

$$
\lambda_{hhh}\equiv\frac{\partial^3 V_{\text{eff}}}{\partial h^3}\bigg|_{\text{min}}\equiv\lambda_{hhh}^{(0)}+\kappa\delta^{(1)}\lambda_{hhh}+\kappa^2\delta^{(2)}\lambda_{hhh}
$$

• Using V_{eff} , 1L and 2L corrections have been calculated in various BSM Higgs models (see e.g. [Braathen,Kanemura,1911.11507]).

Calculating BSM corrections to κ_{λ} [Braathen,Kanemura,1911.11507]

- Large non-decoupling corrections found in several BSM models.
- Analysis assumed that all BSM masses are equal M_{Φ} .
- No phenomenological analysis has been performed.

Idea of this work:

Can we constrain these models based on the large corrections to κ ₂?

2HDM parameter scan

- We checked for
	- vacuum stability and boundedness-from-below,
	- NLO perturbative unitarity, [Grinstein et al., 1512.04567; Cacchio et al., 1609.01290]
	- electroweak precision observables (calculated at the 2L level using THDM_EWPOS), [Hessenberger & Hollik,1607.04610,2207.03845]
	- SM-like Higgs measurements via HiggsSignals, [Bechtle et al., 2012.09197]
	- direct searches for BSM scalars via HiggsBounds, [Bechtle et al., 2006.06007]
	- b-physics constraints.
- Most constraints checked using ScannerS. [Mühlleitner et al., 2007.02985]
- For each point passing the constraints, we calculate κ_λ at the 1L and 2L level ($\kappa_\lambda^{(1)}$ and $\kappa_\lambda^{(2)}$). [Braathen,Kanemura,1911.11507]

2HDM parameter scan — results

- Largest corrections for $m_A \simeq m_{H^{\pm}}$, $m_H < m_{H^{\pm}}$ and $m_H \simeq m_{H^{\pm}}$, $m_A < m_{H^{\pm}}$ (κ_{λ} of up to 9).
- 2L corrections have sizeable impact (up to 70%).

Can we apply the experimental constraints on κ_{λ} ?

Assumptions of experimental bound:

- All other Higgs couplings are SM-like.
	- \triangleright 2HDM in the alignment limit with heavy BSM masses.
- Higgs-boson pair production only deviates from the SM via a modified trilinear Higgs coupling.
	- \triangleright No resonant contribution because *Hhh* coupling is zero in alignment limit.
	- \triangleright Other BSM contributions to hh production?

 \triangleright We include the all corrections leading in the large coupling $g_{hh\Phi\Phi}$ at the NLO and NNLO level.

Other extension of SM Higgs sector

- Large loop corrections to κ_{λ} possible in various models.
- κ_{λ} very sensitive to BSM scalar couplings.
- Automatized calculation of κ_{λ} available in Python package anyH3.
- See also [1704.01953,1902.05936,2209.00666] for other models/more discussion.

Strong motivation for the experimental di-Higgs program!

Momentum dependence

Smearing and reconstruction efficiencies

Interpretation in terms of top-Yukawa coupling

• Effective Lagrangian (SM: $c_t = 1$, $\tilde{c}_t = 0$)

$$
\mathcal{L}_{\text{yuk}} = -\frac{y_t^{\text{SM}}}{\sqrt{2}}\bar{t}\left(c_t+i\gamma_5\tilde{c}_t\right)tH
$$

• If no colored BSM particles at low energies: $c_g \simeq c_t$, $\tilde{c}_g \simeq \tilde{c}_t$

