

# Multiwavelength anomalous diffraction at high x-ray intensity

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**Center for Free-Electron Laser Science**

CFEL is a scientific cooperation of the three organizations:  
DESY – Max Planck Society – University of Hamburg

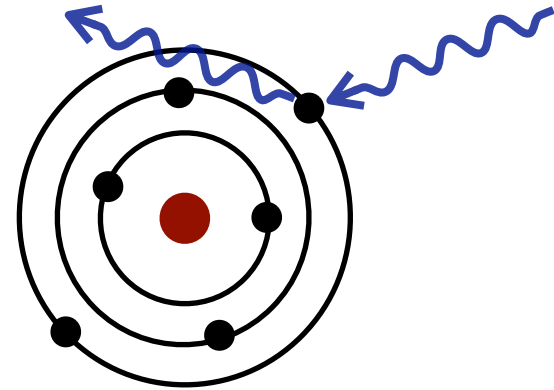


# X-ray scattering

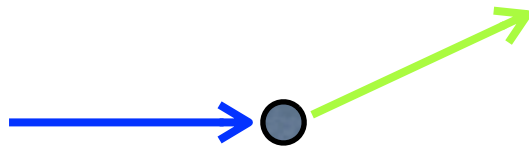
- > Elastic x-ray scattering form factor

$$f^0(\mathbf{Q}) = \int d^3r \rho(\mathbf{r}) e^{i\mathbf{Q}\cdot\mathbf{r}}$$

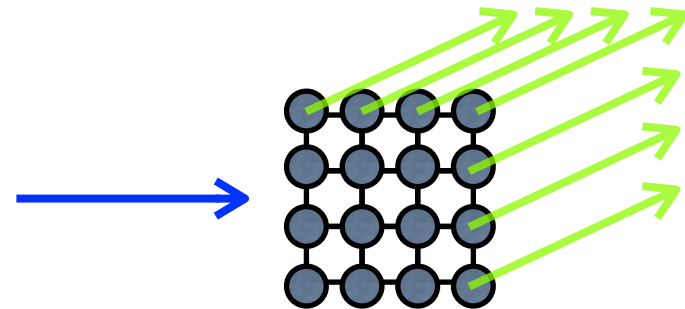
$$\frac{d\sigma(\mathbf{Q})}{d\Omega} = \left( \frac{d\sigma}{d\Omega} \right)_T |f^0(\mathbf{Q})|^2$$



- > Carbon at synchrotron radiation: 12 keV,  $10^6$  photons on  $10\mu\text{m} \times 10\mu\text{m}$



scattering  
probability  $\sim 10^{-12}$



$\sim 10^8$  molecules in a crystal:  
diffraction patterns  
 $\rightarrow$  X-ray crystallography

# Bottlenecks in X-ray crystallography



phase

crystal

Figure taken from <http://www.jic.ac.uk/staff/david-lawson/xtallog/summary.htm>

# Phase problem

- > Phase problem: a fundamental obstacle in constructing an electronic density map from x-ray diffraction

$$f^0(\mathbf{Q}) = \int d^3r \rho(\mathbf{r}) e^{i\mathbf{Q}\cdot\mathbf{r}} = |f^0(\mathbf{Q})| e^{i\phi^0(\mathbf{Q})}$$

- > Phases are essential for structural determination, but they are lost in measurement.
- > Phasing method: how to recover phases
- > MAD (Multiwavelength Anomalous Diffraction) is one of the most powerful phasing methods.

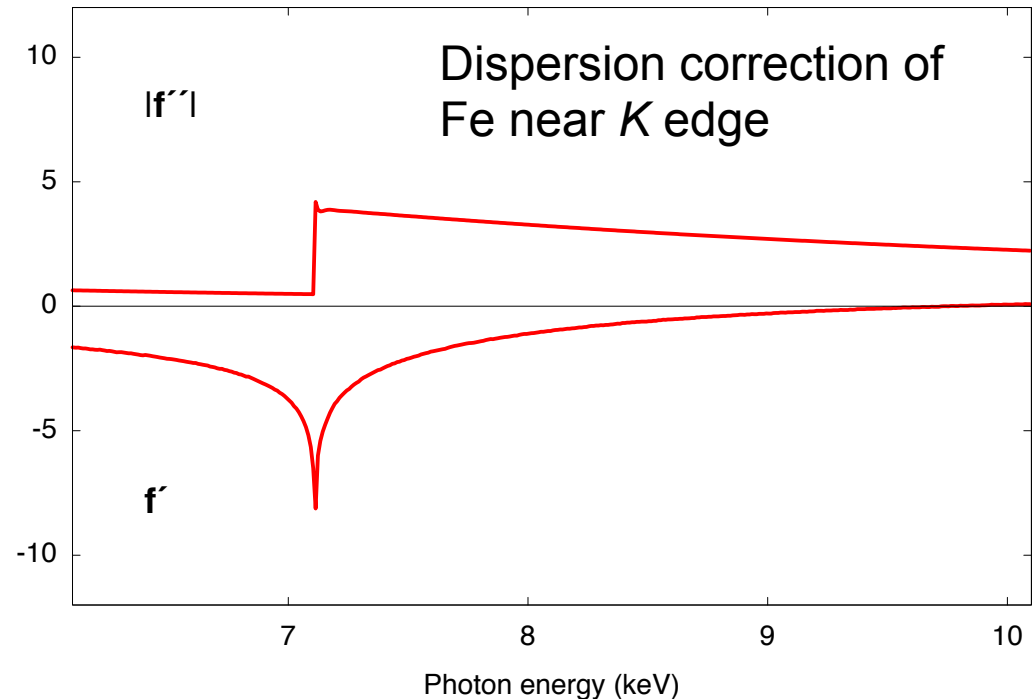
# Multiwavelength Anomalous Diffraction

> Dispersion correction:  $f(\mathbf{Q}, \omega) = f^0(\mathbf{Q}) + f'(\omega) + i f''(\omega)$

> MAD phasing:  
The Karle-Hendrickson equation provides a simple way for phasing from the contrast at two or more wavelengths.

Karle, *Int. J. Quant. Chem.* **18**,  
Suppl. S7, 357 (1980).

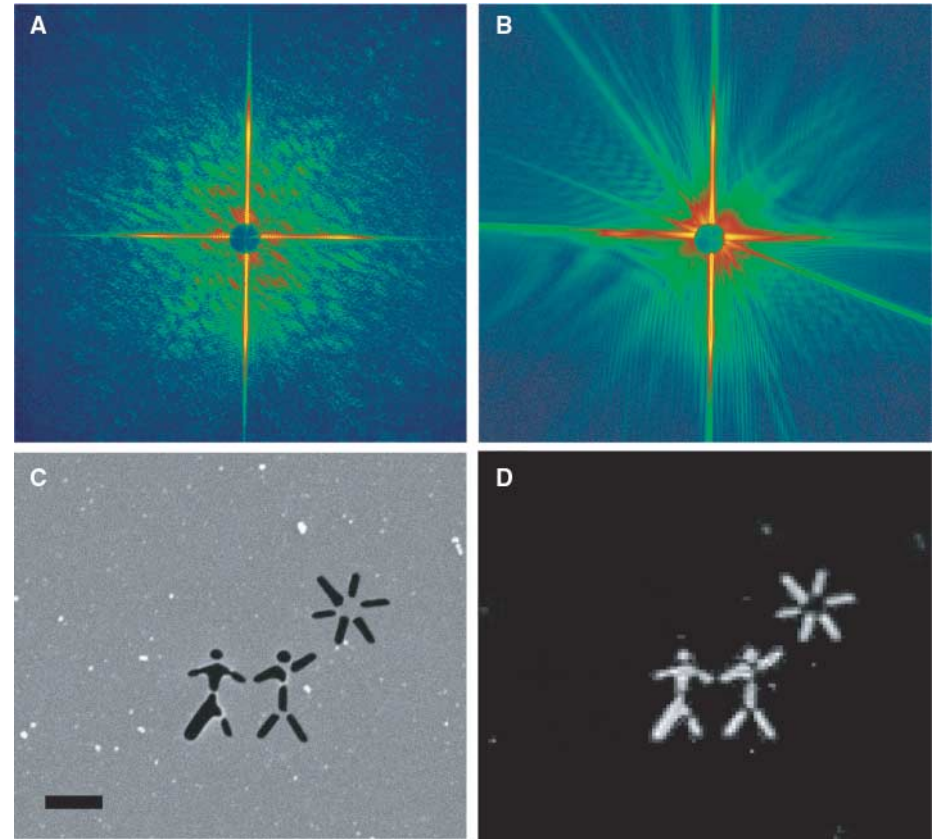
Hendrickson, *Trans. Am. Crystalgr.  
Assoc.* **21**, 11 (1985).



> The MAD method has been a well-established phasing method with synchrotron radiation sources since late 80's: *Science* **241**, 806 (1998); *PNAS* **86**, 2190 (1989); *Science* **249**, 1398 (1990); *Science* **254**, 51 (1991).

# X-ray free-electron laser

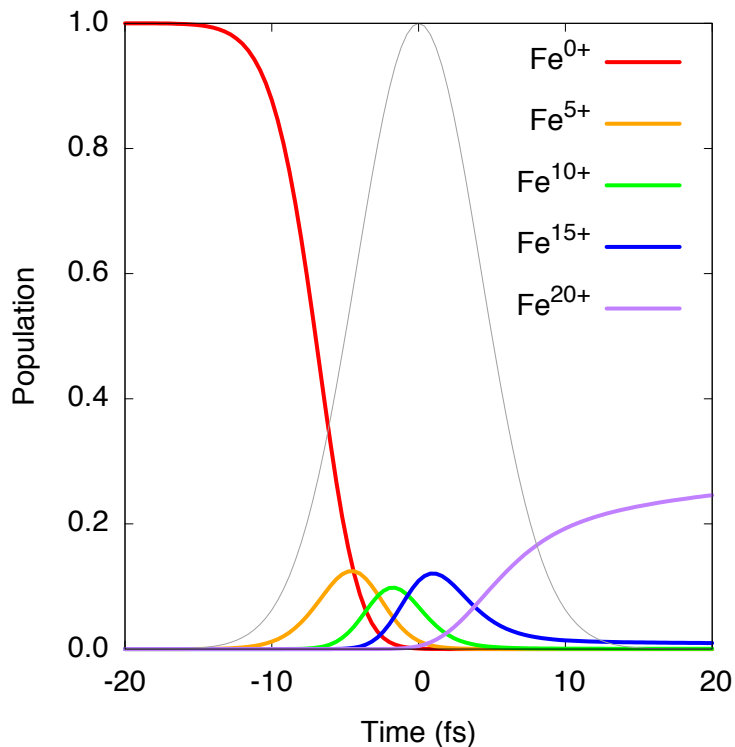
- Growing high-quality crystals is one of major bottlenecks in x-ray crystallography.
- Unprecedented high x-ray fluence from XFEL ( $\times 10^6$  larger than synchrotron radiation)
- Enough signals from nano-sized crystals and single molecules
- Single-shot molecular imaging: revolutionary impact on structural biology



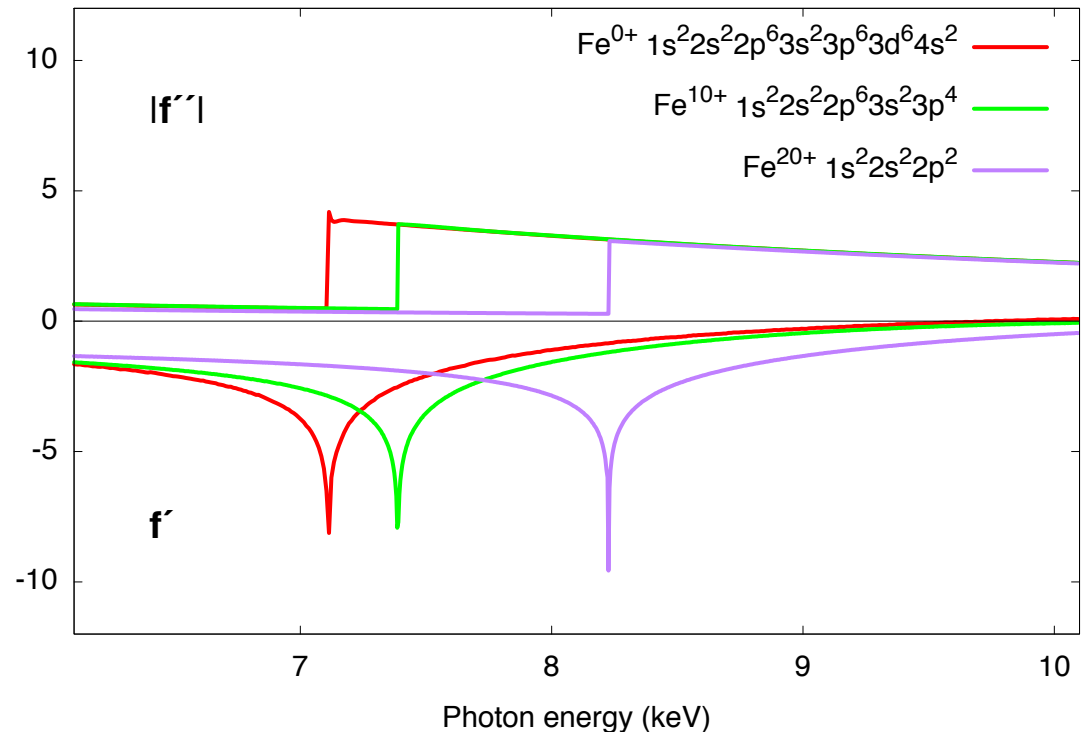
Chapman *et al.*, *Nature Phys.* **2**, 839 (2006).  
Figure taken from Gaffney & Chapman, *Science* **316**, 1444 (2007).

# Electronic damage to heavy atoms

Population dynamics of Fe charge states during an XFEL pulse (8 keV,  $5 \times 10^{12}$  photons/ $\mu\text{m}^2$ , 10 fs FWHM)



Dispersion corrections of atomic form factors of Fe and its ions



Adapted from Son, Chapman & Santra, *PRL* **107**, 218102 (2011).

# Prior speculations regarding MAD at XFEL

- > Unavoidable electronic damage, esp. to heavy atoms
- > Dramatic change of anomalous scattering for high charge states
- > Stochastic electronic damage to heavy atoms would destroy coherent scattering signals in nanocrystals
- > MAD would not be an applicable route for phasing at XFEL...?



- > We demonstrate the existence of a Karle-Hendrickson-type equation in the high-intensity regime.
- > We show that MAD not only works, but also the extensive electronic rearrangements at high x-ray intensity provide a new path to phasing.

Son, Chapman & Santra, *PRL* **107**, 218102 (2011).



# Scattering intensity including elec. damage

$$\frac{dI(\mathbf{Q}, \omega)}{d\Omega} = \mathcal{FC}(\Omega) \int_{-\infty}^{\infty} dt g(t) \sum_I P_I(t) \left| F_P^0(\mathbf{Q}) + \sum_{j=1}^{N_H} f_{I_j}(\mathbf{Q}, \omega) e^{i\mathbf{Q} \cdot \mathbf{R}_j} \right|^2$$

$$I = (I_1, I_2, \dots, I_{N_H}), \quad P_I(t) = \prod_{j=1}^{N_H} P_{I_j}(t)$$

$$f_{I_j}(\mathbf{Q}, \omega) = f_{I_j}^0(\mathbf{Q}) + f'_{I_j}(\omega) + i f''_{I_j}(\omega)$$

- $P$ : protein,  $H$ : heavy atoms; only heavy atoms scatter anomalously and undergo damage dynamics during an x-ray pulse.
- All changes among  $N_H$  heavy atoms are included.
- Heavy atoms are ionized independently.
- Only one species of heavy atoms is considered.

Son, Chapman & Santra, *PRL* **107**, 218102 (2011).

# Generalized Karle-Hendrickson equation

$$\begin{aligned} \frac{dI(\mathbf{Q}, \omega)}{d\Omega} = \mathcal{FC}(\Omega) & \left[ |F_P^0(\mathbf{Q})|^2 + |F_H^0(\mathbf{Q})|^2 \tilde{a}(\mathbf{Q}, \omega) \right. \\ & + |F_P^0(\mathbf{Q})| |F_H^0(\mathbf{Q})| b(\mathbf{Q}, \omega) \cos \Delta\phi^0(\mathbf{Q}) \\ & + |F_P^0(\mathbf{Q})| |F_H^0(\mathbf{Q})| c(\mathbf{Q}, \omega) \sin \Delta\phi^0(\mathbf{Q}) \\ & \left. + N_H |f_H^0(\mathbf{Q})|^2 \{a(\mathbf{Q}, \omega) - \tilde{a}(\mathbf{Q}, \omega)\} \right] \end{aligned}$$

- > MAD coefficients:  $a(\mathbf{Q}, \omega)$ ,  $b(\mathbf{Q}, \omega)$ ,  $c(\mathbf{Q}, \omega)$ , and  $\tilde{a}(\mathbf{Q}, \omega)$   
→ measured or calculated with time evolution of config. populations
- > 3 unknowns:  $|F_P^0(\mathbf{Q})|$ ,  $|F_H^0(\mathbf{Q})|$ ,  $\Delta\phi^0(\mathbf{Q}) [= \phi_P^0(\mathbf{Q}) - \phi_H^0(\mathbf{Q})]$   
→ solvable with measurements at 3 different wavelengths.

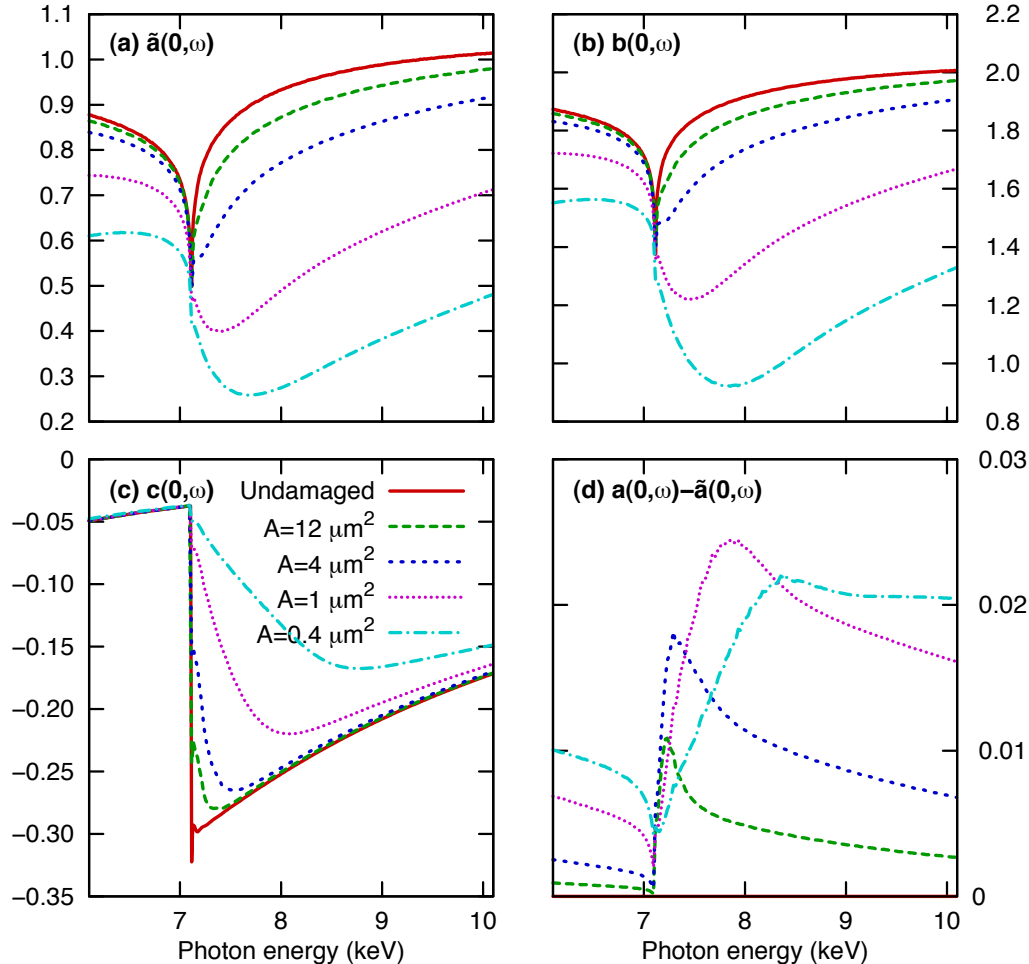
Son, Chapman & Santra, *PRL* **107**, 218102 (2011).

# XATOM: x-ray and atomic physics toolkit

- > X-ray-induced atomic processes for any given element and configuration
  - photoionization cross section
  - Auger / Coster-Kronig decay rate
  - fluorescence rate
  - coherent x-ray scattering form factor and dispersion correction
  - shake-off branching ratio
- > Rate equation model to simulate ionization and relaxation dynamics
- > Applications
  - Nonlinear x-ray absorption processes; *PRL* **106**, 083002 (2011); *PRA* **85**, 023414 (2011)
  - Charge distribution analysis of noble gases in XFELs; Rudek *et al.*, submitted
  - Photoelectron / Auger / fluorescence spectra; Son & Santra, in preparation
  - Scattering with electronic damage dynamics at high intensity; *PRA* **83**, 033402 (2011)
  - Multi-wavelength anomalous diffraction at high intensity; *PRL* **107**, 218102 (2011)

# MAD coefficients

Fe in an x-ray pulse of  $2 \times 10^{12}$  photons and 10 fs FWHM



- > calculated by XATOM
- > bleaching effect: minimum deepened and edge broadened
- > **MAD works:** enhanced contrast at different wavelengths
- > **alternative phasing method** similar to SIR (single isomorphic replacement) or RIP (radiation-damage induced phasing)

Son, Chapman & Santra,  
*PRL* **107**, 218102 (2011).

# Conclusion

phase

crystal

MAD

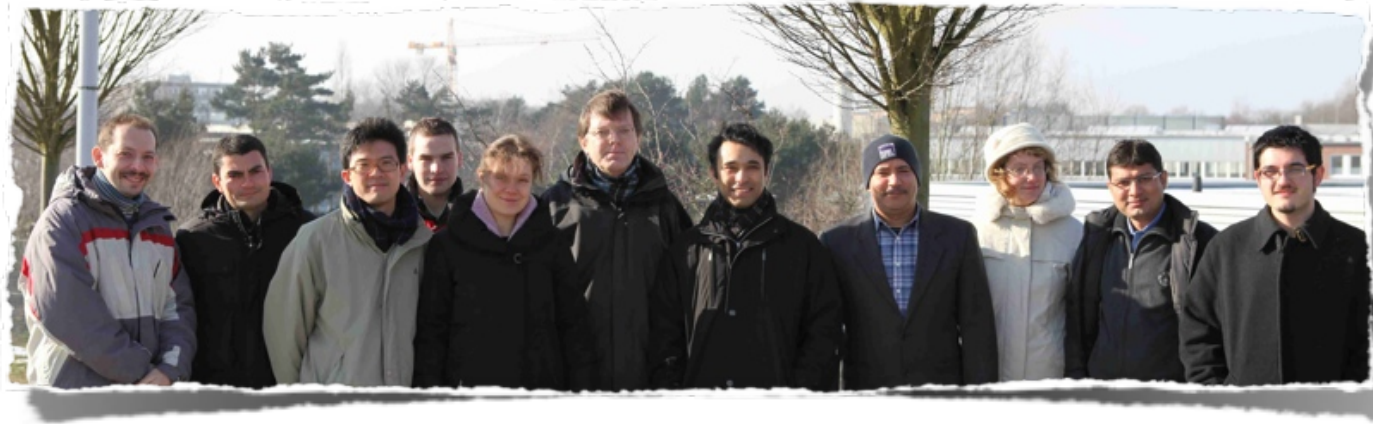
+

FEL

MAD at high x-ray intensity

# Acknowledgment

## CFEL Theory Division



*Thank you for your attention!*