


Recent results on angular momentum and strangeness in the nucleon

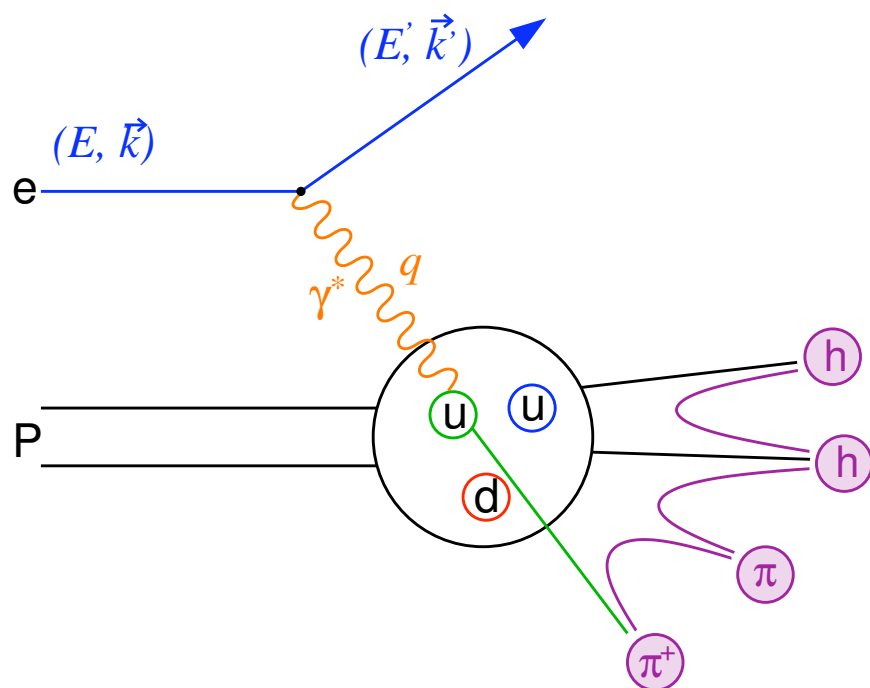
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(DESY)

for the  collaboration

- Transverse single-spin asymmetries on hydrogen target
⇒ Collins and Sivers effects
- extraction of strange quark distributions from an isoscalar deuteron target

DIS: probing the nucleon structure

$e^{+,-}$ @ 27.6 GeV (HERA)



$$Q^2 = -q^2 = -(k - k')^2$$

$$\nu \stackrel{lab}{=} E - E'$$

$$x = \frac{Q^2}{2M\nu}$$

$$z \stackrel{lab}{=} \frac{E_{had}}{\nu}$$

Targets:

H: $\langle P_{trans} \rangle \sim 74 \pm 6\%$

D: $\langle P_{long} \rangle \sim 84.5 \pm 3.5\%$

Cross section contains **Distribution Functions** and **Fragmentation Functions**:

$$\sigma^{ep \rightarrow eh} \sim \sum_q DF^{p \rightarrow q} \otimes \sigma^{eq \rightarrow eq} \otimes FF^{q \rightarrow h}$$

DF: distribution of quarks in the nucleon

FF: fragmentation of (struck) quark into hadronic final state

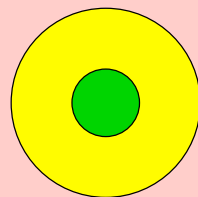
Distribution functions

Leading twist:

3 DFs survive integration over transverse quark momenta

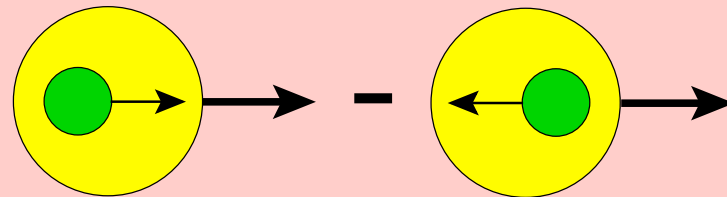
momentum distribution

$$q(x)$$



helicity distribution

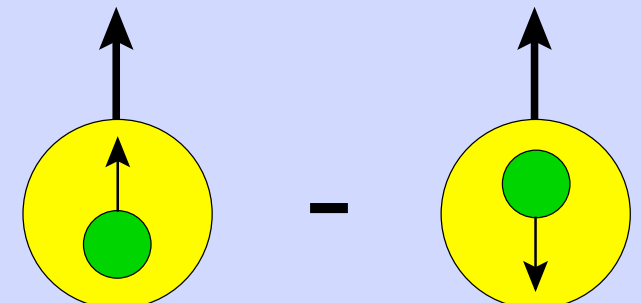
$$\Delta q(x)$$



helicity basis

transversity distribution

$$\delta q(x) = h_1^q(x)$$

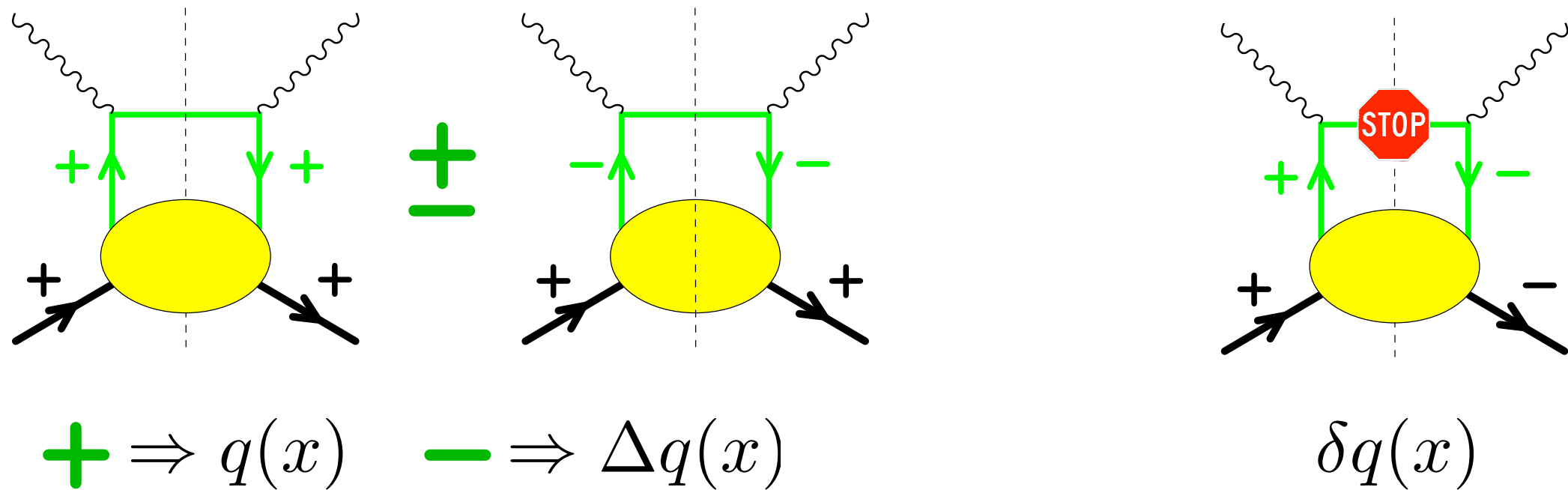


basis of transv. spin eigenstates

all three DFs needed for complete description of the nucleon!

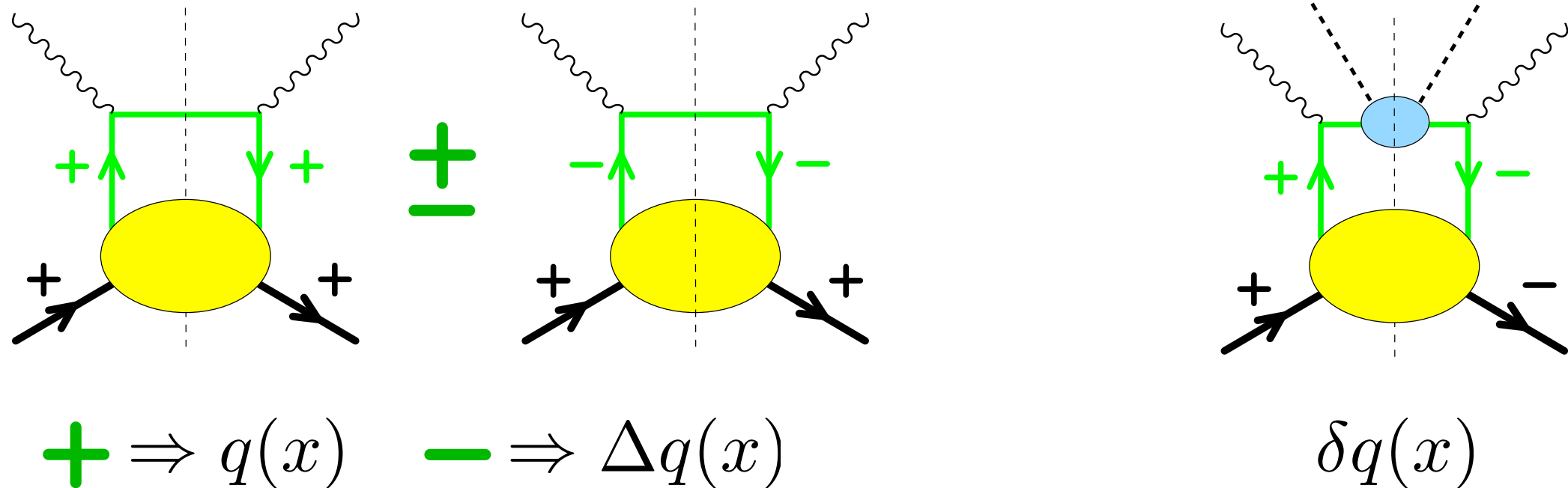
Transversity δq

- non-relativistic quarks: $\Delta q = \delta q$
- δq : helicity-flip of the quark \Rightarrow chiral-odd



Transversity δq

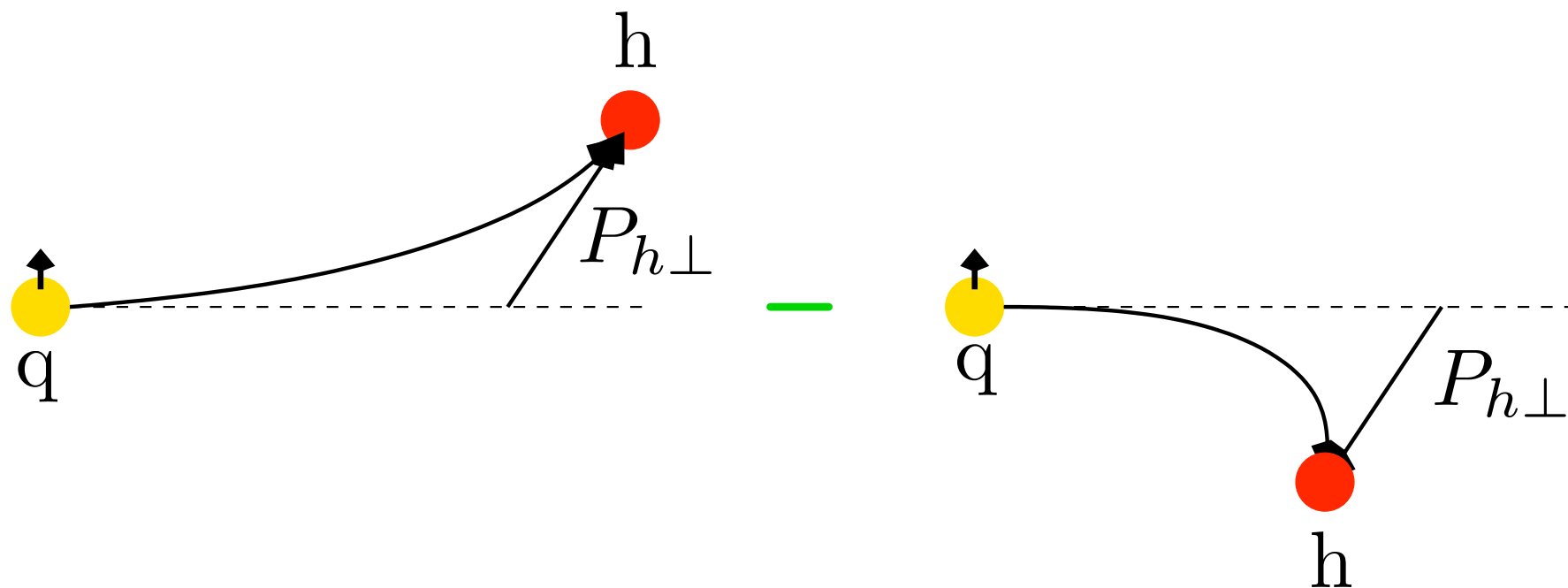
- non-relativistic quarks: $\Delta q = \delta q$
- δq : helicity-flip of the quark \Rightarrow chiral-odd



- access to δq in combination with another chiral odd object
 \Rightarrow Collins-FF H_1^\perp

Collins Effect

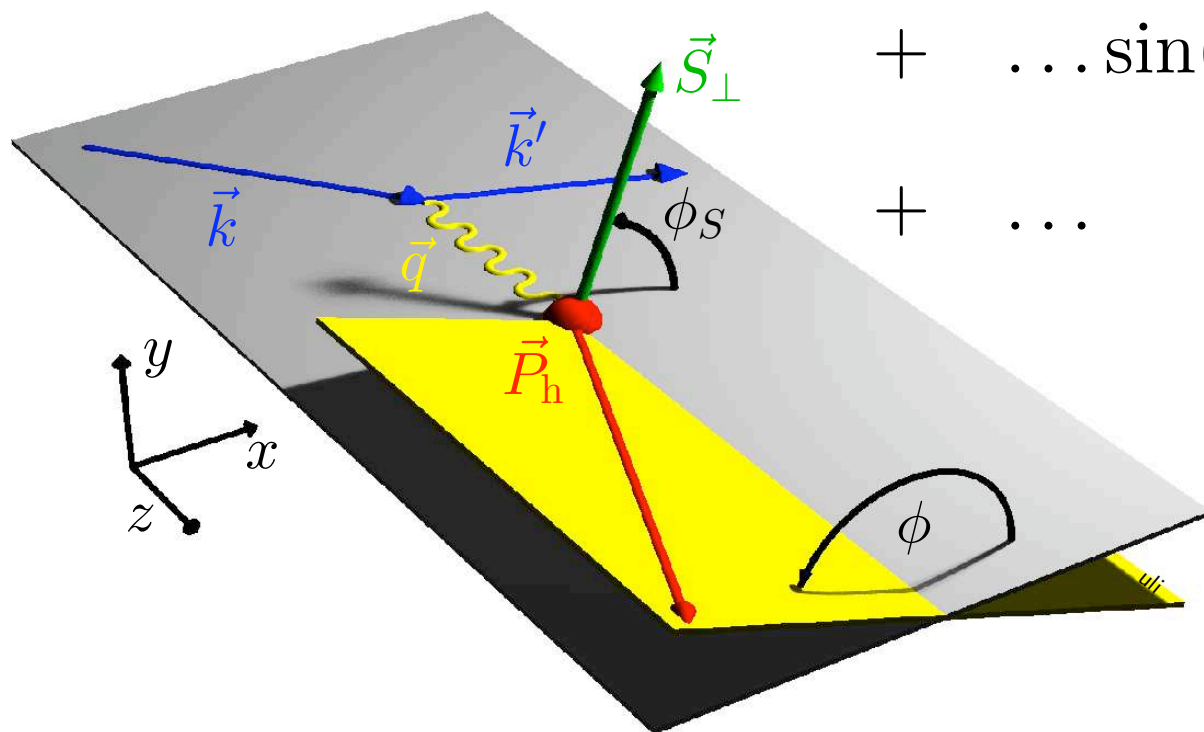
- Collins fragmentation function H_1^\perp
- naive time reversal odd \iff final state interactions
 \implies azimuthal single-spin asymmetries
- describes **correlation** between **transverse polarisation of fragmenting quark** and the **transverse momentum $P_{h\perp}$ of the produced (unpolarised) hadron**



Azimuthal Asymmetries

Measurement of cross-section asymmetries depending on the azimuthal angles ϕ and ϕ_S

$$\begin{aligned}
 A_{UT}(\phi, \phi_S, \dots) &= \frac{1}{S_{\perp}} \frac{\sigma^{\uparrow} - \sigma^{\downarrow}}{\sigma^{\uparrow} + \sigma^{\downarrow}} \\
 &\sim \dots \sin(\phi + \phi_S) \frac{\sum_q e_q^2 \mathcal{I} \left[\dots \delta q(x, \vec{p}_T^2) \cdot H_1^{\perp q}(z, \vec{k}_T^2) \right]}{\sum_q e_q^2 q(x) \cdot D_1^q(z)} \\
 &+ \dots \sin(\phi - \phi_S) \frac{\sum_q e_q^2 \mathcal{I} \left[\dots f_{1T}^{\perp q}(x, \vec{p}_T^2) \cdot D_1^q(z, \vec{k}_T^2) \right]}{\sum_q e_q^2 q(x) \cdot D_1^q(z)} \\
 &+ \dots
 \end{aligned}$$



$\mathcal{I} [\dots]$: convolution integral over initial (\mathbf{p}_T) and final (\mathbf{k}_T) quark transverse momenta

Azimuthal Asymmetries

Measurement of cross-section asymmetries depending on the azimuthal angles ϕ and ϕ_S

$$A_{UT}(\phi, \phi_S, \dots) = \frac{1}{S_{\perp}} \frac{\sigma^{\uparrow} - \sigma^{\downarrow}}{\sigma^{\uparrow} + \sigma^{\downarrow}}$$

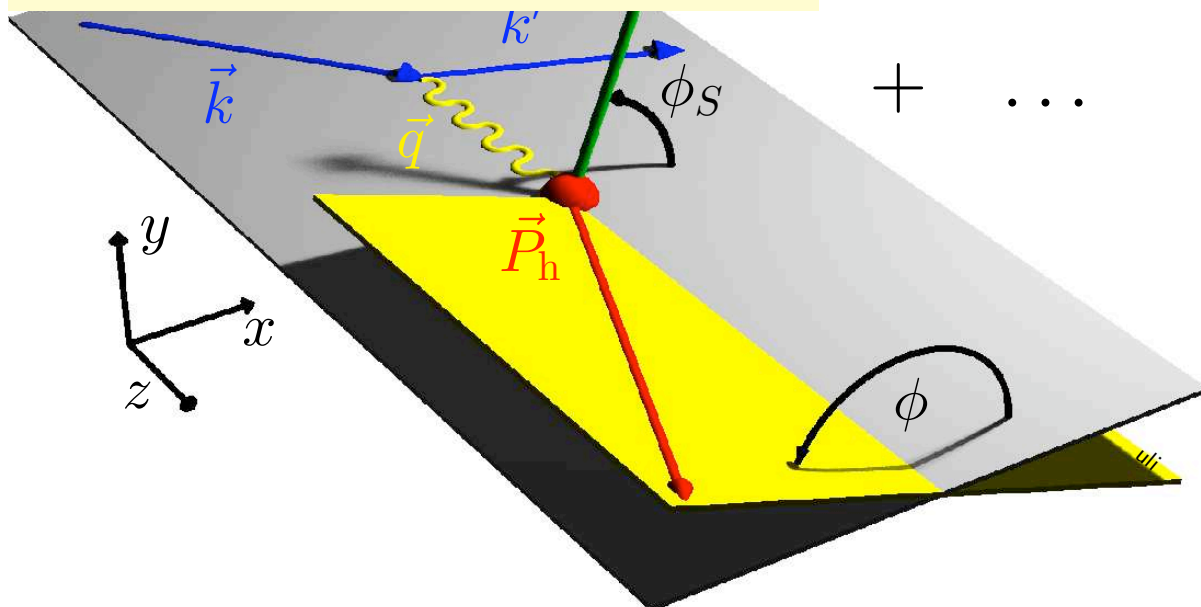
Collins Amplitude

$$\sim \dots \sin(\phi + \phi_S) \frac{\sum_q e_q^2 \mathcal{I} \left[\dots \delta q(x, \vec{p}_T^2) \cdot H_1^{\perp q}(z, \vec{k}_T^2) \right]}{\sum_q e_q^2 q(x) \cdot D_1^q(z)}$$

Sivers Amplitude

$$+ \dots \sin(\phi - \phi_S) \frac{\sum_q e_q^2 \mathcal{I} \left[\dots f_{1T}^{\perp q}(x, \vec{p}_T^2) \cdot D_1^q(z, \vec{k}_T^2) \right]}{\sum_q e_q^2 q(x) \cdot D_1^q(z)}$$

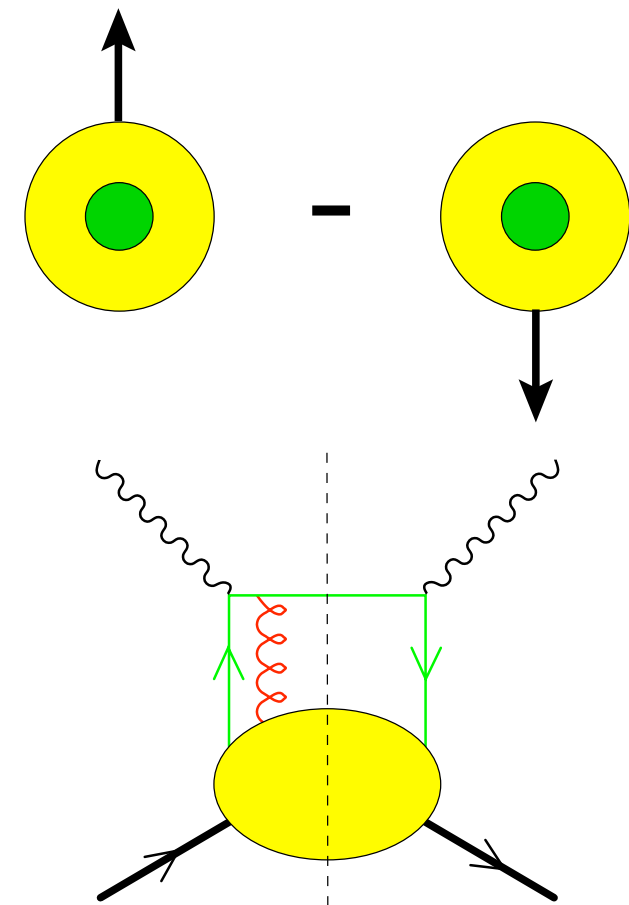
+ ...



$\mathcal{I} [\dots]$: convolution integral over initial (\mathbf{p}_T) and final (\mathbf{k}_T) quark transverse momenta

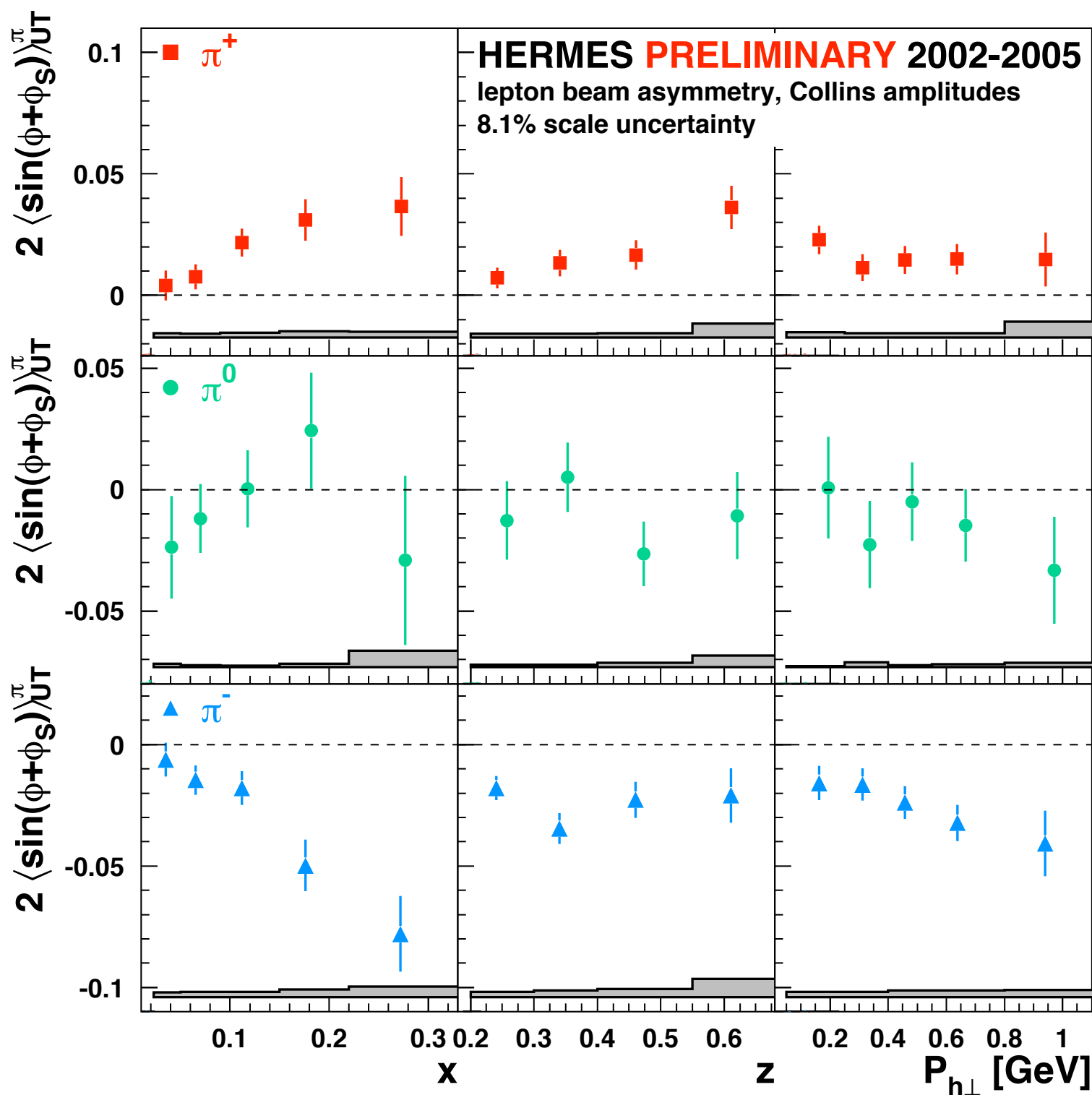
Sivers function

- describes **correlation** between **intrinsic transverse quark momentum (p_T)** and **transverse nucleon spin**
- Chiral-even function
- T-odd functions allowed due to **final state interactions (FSI)**:
 quark rescattering via a soft gluon
 ➔ time-reversal invariance condition changes
 ➔ naive T-odd
- non-zero Sivers function requires **non-vanishing orbital angular momentum** in the nucleon wave function (**can contribute to nucleon spin!**)



Collins Amplitudes for Pions

$$A_C \propto \delta q \otimes H_1^\perp$$



- positive amplitudes for π^+
- large negative π^- amplitude

$$u \rightarrow \pi^+ \Rightarrow H_1^{\perp, \text{fav}}$$

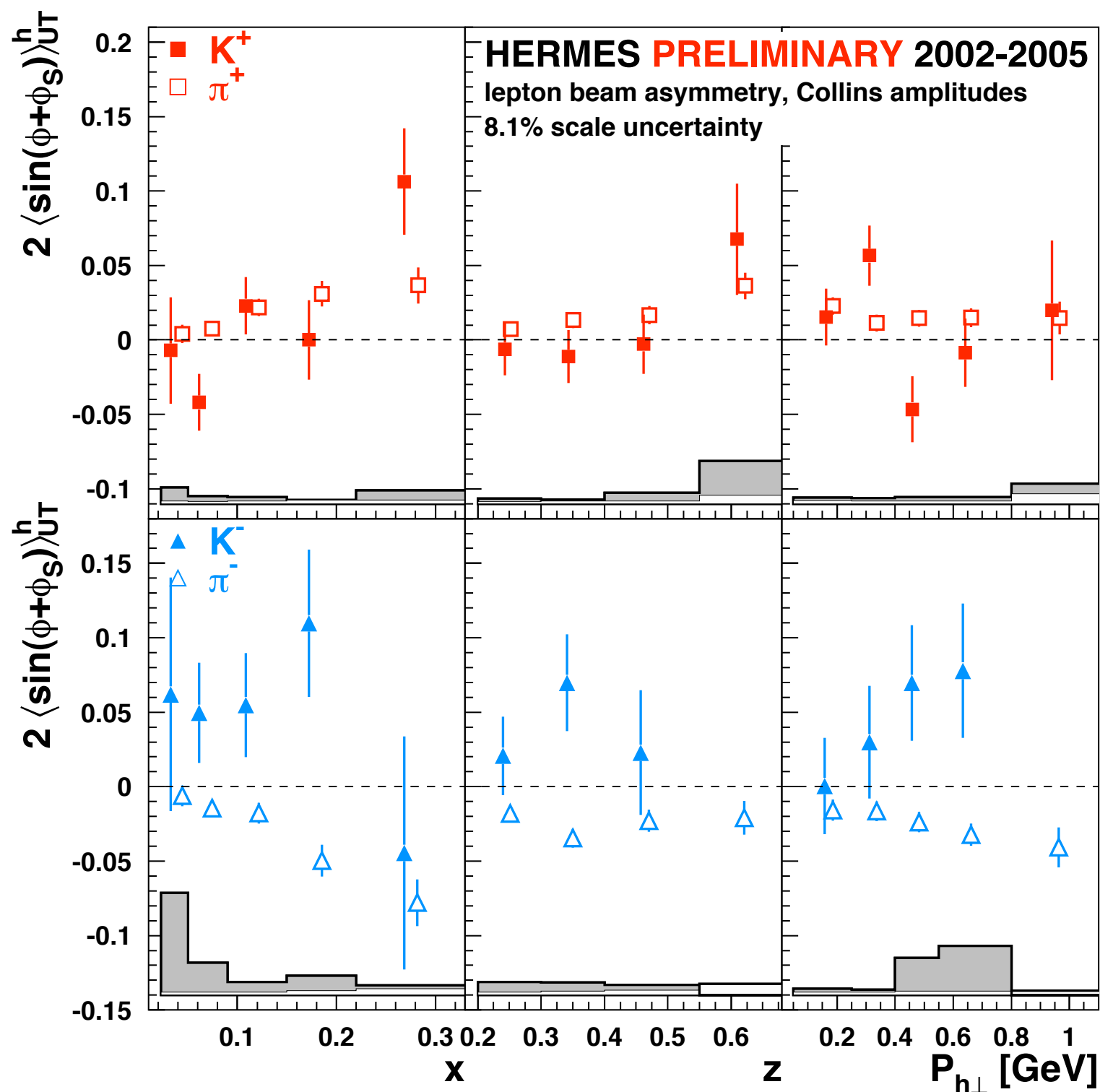
$$u \rightarrow \pi^- \Rightarrow H_1^{\perp, \text{unfav}}$$

$$\Rightarrow H_1^{\perp, \text{fav}} \approx -H_1^{\perp, \text{unfav}}$$

- isospin symmetry of π -mesons is fulfilled
- information from another process on Collins FF (BELLE) allows extraction of δq (eg Anselmino et al Phys.Rev.D75:054032,2007)

Collins Amplitudes for Kaons

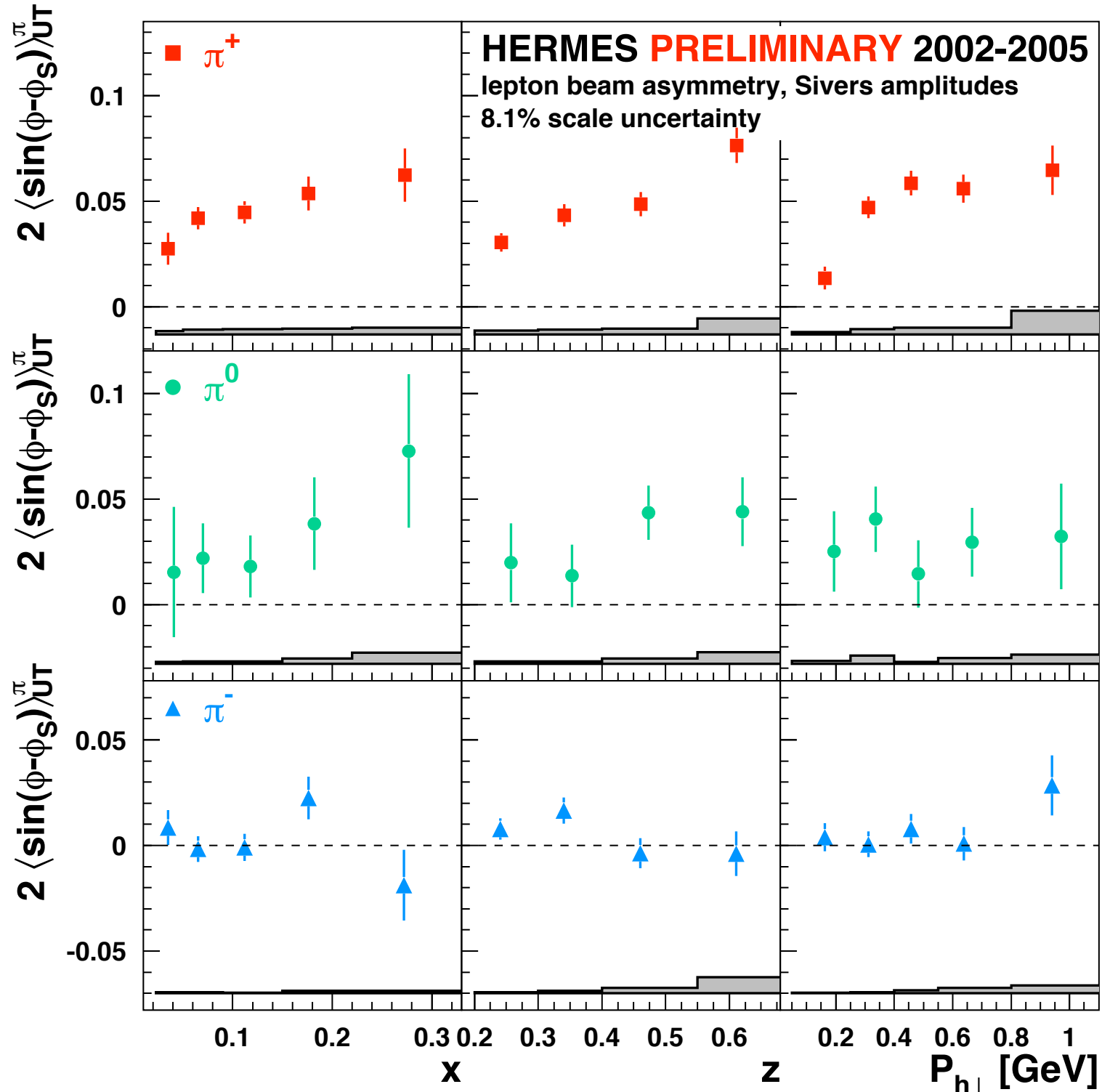
$$A_C \propto \delta q \otimes H_1^\perp$$



- no significant non-zero Collins amplitudes for both K^+ and K^-
- Collins amplitudes for K^+ are within statistical accuracy consistent with π^+

Sivers Amplitudes for Pions

$$A_S \propto f_{1T}^\perp \otimes D_1^q$$



- significantly positive for π^+
- implies non-zero angular momentum of quarks
- consistent with zero for π^-
- isospin symmetry of π -mesons fulfilled

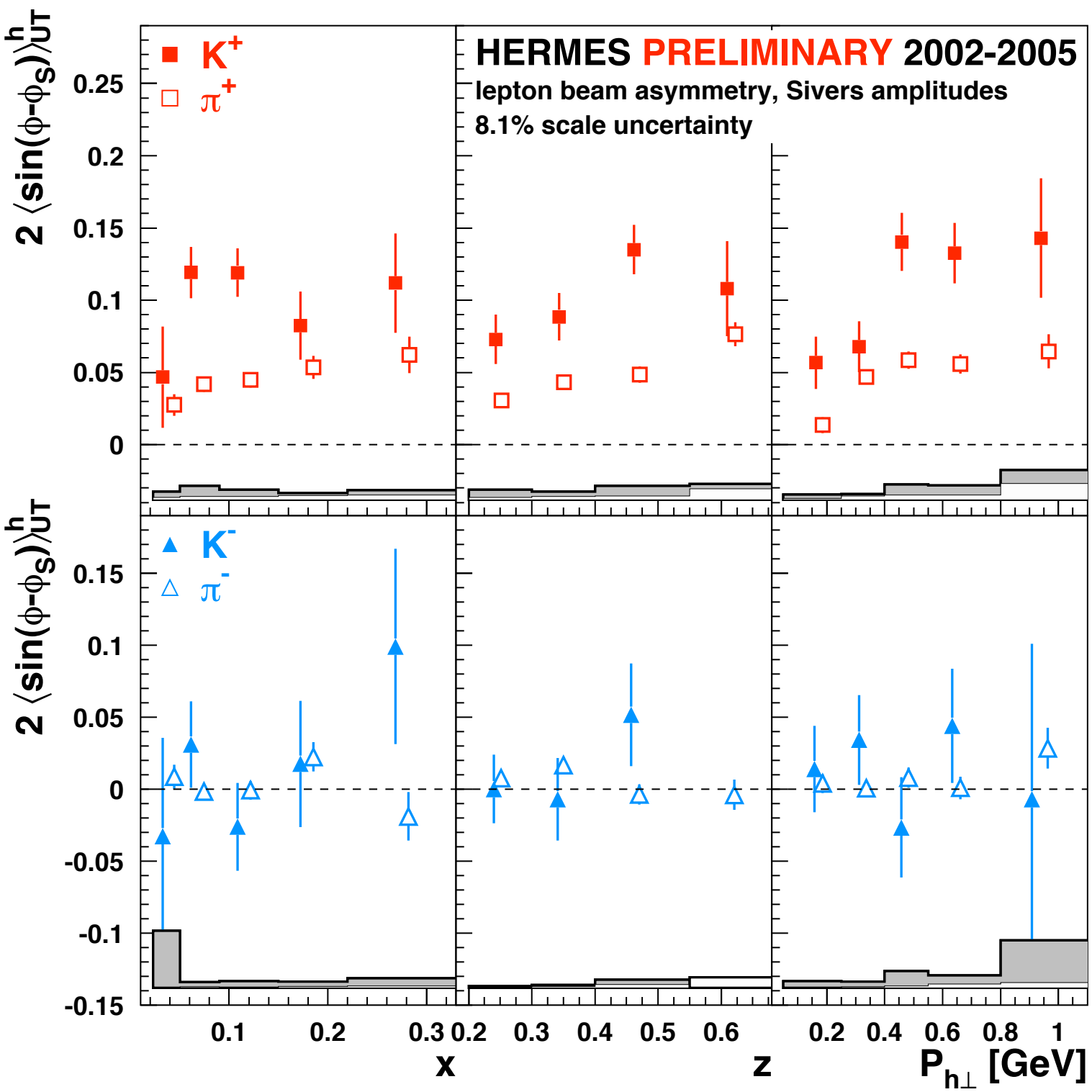
Sivers Amplitudes for Kaons

$$A_S \propto f_{1T}^\perp \otimes D_1^q$$

- significantly positive for K^+
- implies non-zero angular momentum of quarks
- consistent with zero for K^-
- K^+ amplitude larger than π^+ amplitude

➔ strange contribution to Sivers mechanism may be important

$$\pi^+ = |u\bar{d}\rangle \quad K^+ = |u\bar{s}\rangle$$



Strangeness in the nucleon

Strange PDFs with isoscalar target

Assumptions:

- isospin symmetry between proton and neutron
- charge conjugation invariance in fragmentation

- strange quarks carry no isospin $\Rightarrow s(x)_{\text{Proton}} = s(x)_{\text{Neutron}}$

- deuteron target (isoscalar!):

fragmentation process in DIS can be described by isospin independent FFs

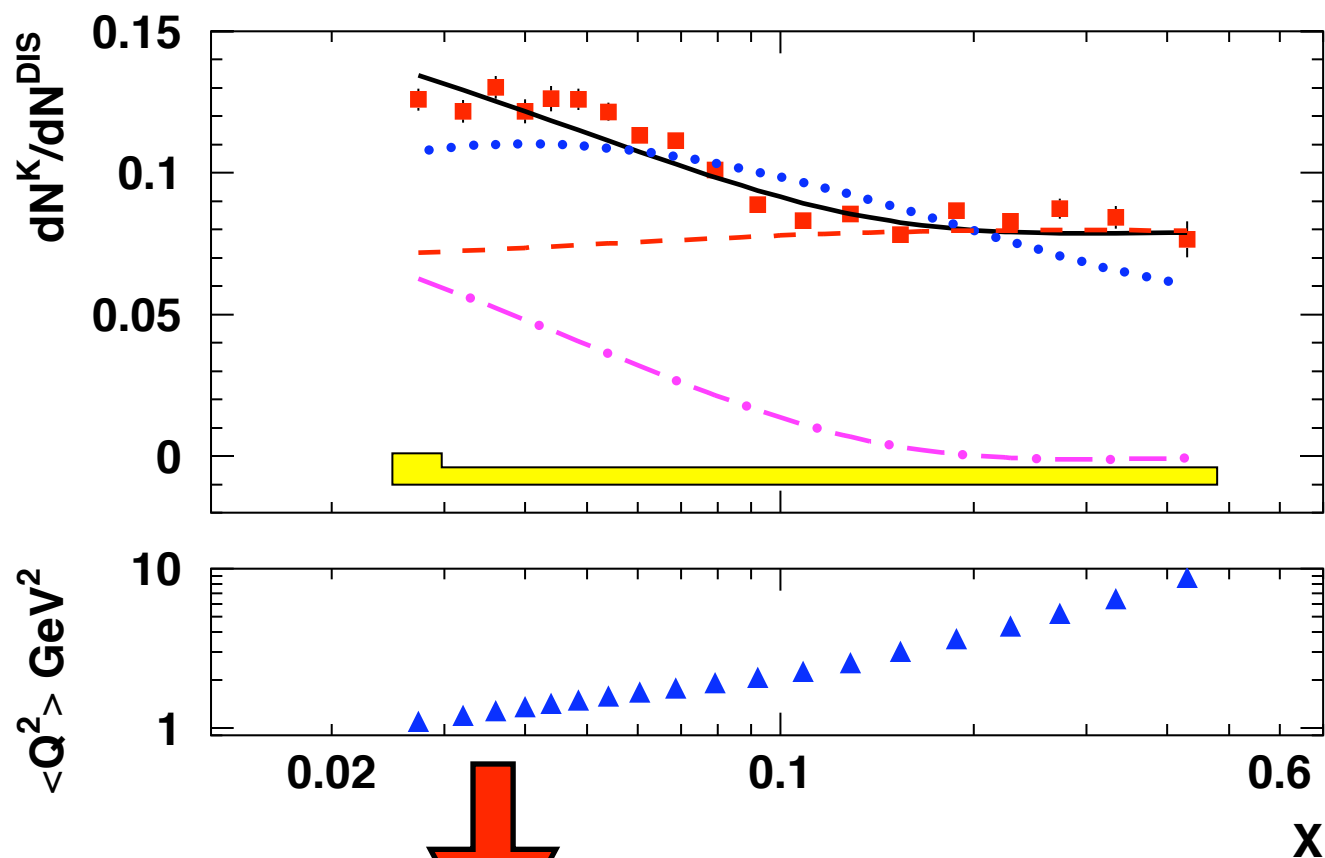
- Charged kaon multiplicity in LO:

$$\frac{dN^K(x)}{dN^{\text{DIS}}(x)} = \frac{Q(x) \int D_Q^K(z) dz + S(x) \int D_S^K(z) dz}{5Q(x) + 2S(x)}$$

$$Q(x) \equiv u(x) + \bar{u}(x) + d(x) + \bar{d}(x) \quad D_Q^K \equiv 4D_u^K(z) + D_d^K(z)$$

$$S(x) \equiv s(x) + \bar{s}(x) \quad D_S^K(z) \equiv 2D_s^K(z)$$

Fitting $dN^K(x)/dN^{DIS}(x)$



Assuming $S(x)=0$ for $x>0.15$:

$$\int_{0.2}^{0.8} D_Q^K(z) dz = 0.398 \pm 0.010$$

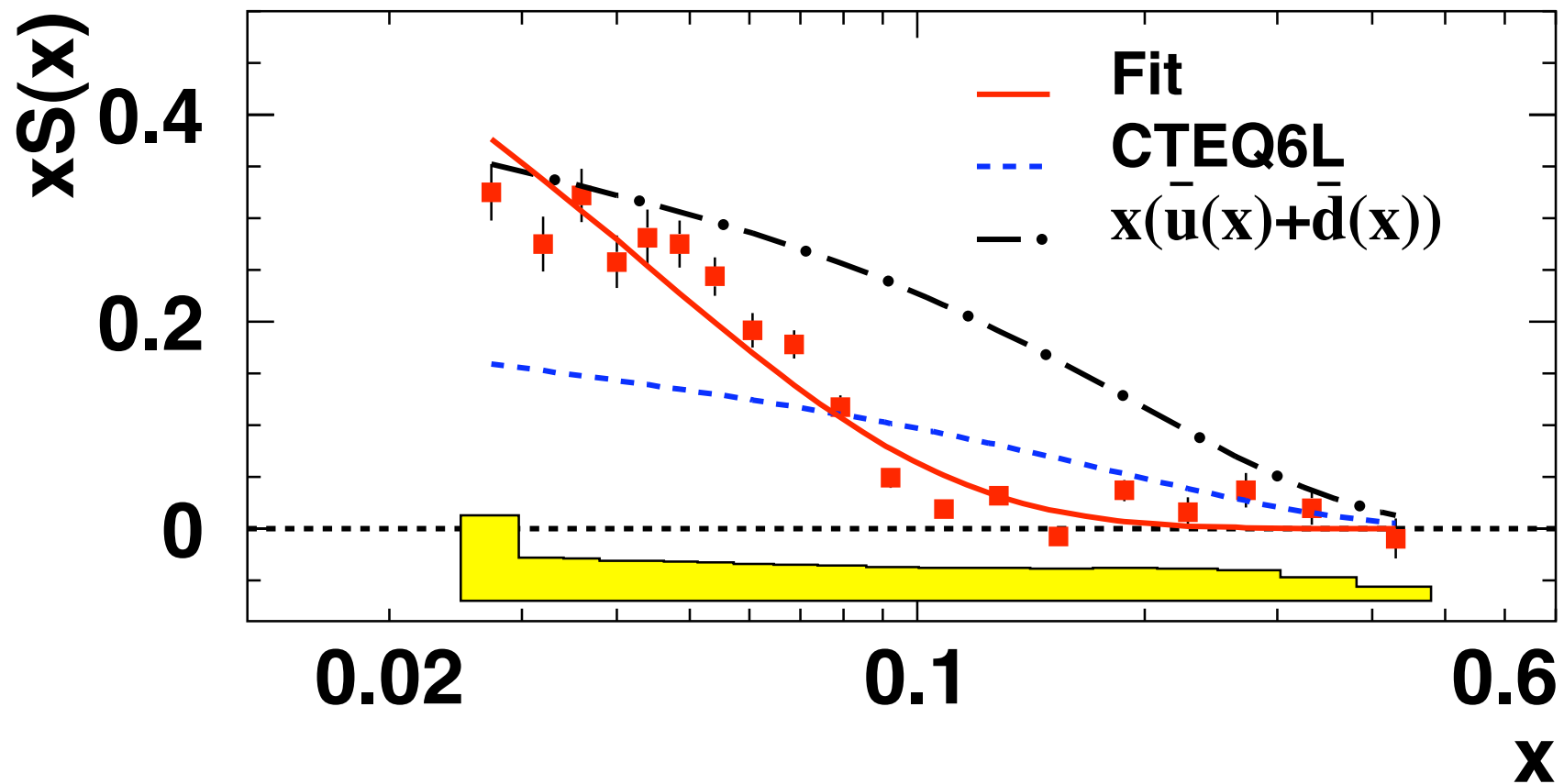
de Florian et al., PRD75, 114010 (2007):

$$\int_{0.2}^{0.8} D_Q^K(z) dz = 0.435 \pm 0.044$$

$$\frac{dN^K(x)}{dN^{DIS}(x)} = \frac{Q(x) \int D_Q^K(z) dz + S(x) \int D_S^K(z) dz}{5Q(x) + 2S(x)}$$

CTEQ6L

$S(x)$ at $Q^2_0=2.5 \text{ GeV}^2$



- $xS(x)$ obtained by evolution of data to $Q^2_0=2.5 \text{ GeV}^2$ using

$$\int_{0.2}^{0.8} D_S^K(z) dz = 1.27 \pm 0.13$$

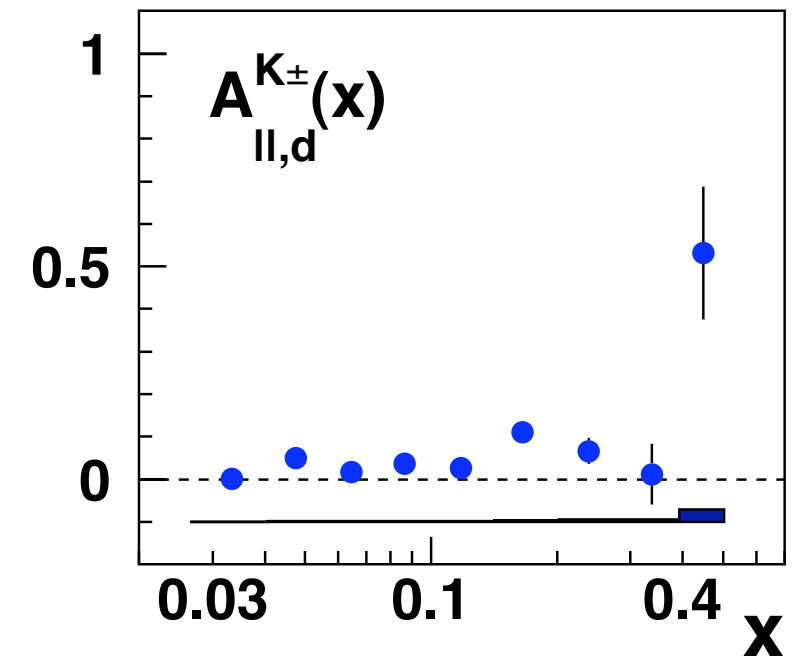
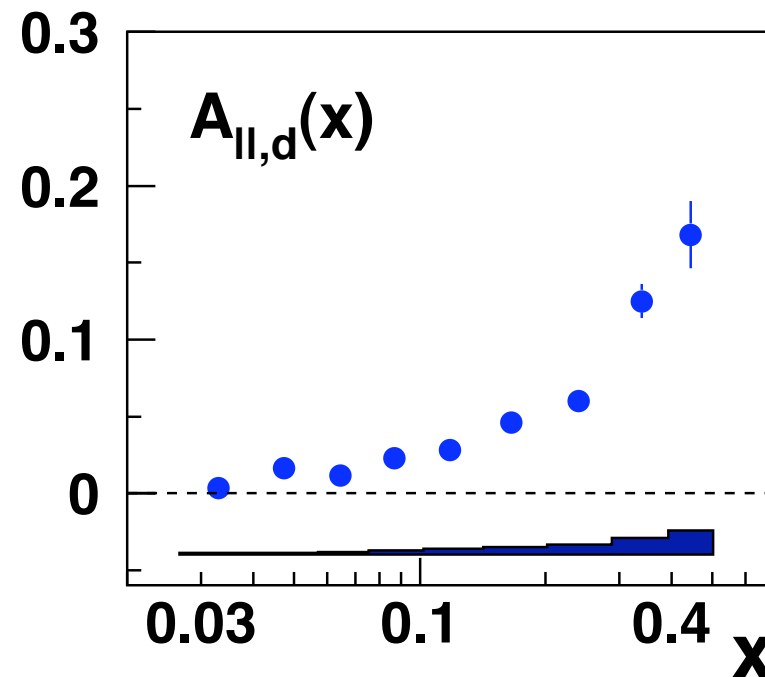
de Florian et al., PRD75, 114010 (2007)

- Shape incompatible with CTEQ6L and with average of the isoscalar nonstrange sea

Extraction of $\Delta Q(x)$ and $\Delta S(x)$

Double spin
asymmetries from long.
pol. deuteron target

$$A_{||}^{(h)} = \frac{\sigma^{\overleftarrow{e},(h)} - \sigma^{\overrightarrow{e},(h)}}{\sigma^{\overleftarrow{e},(h)} + \sigma^{\overrightarrow{e},(h)}}$$



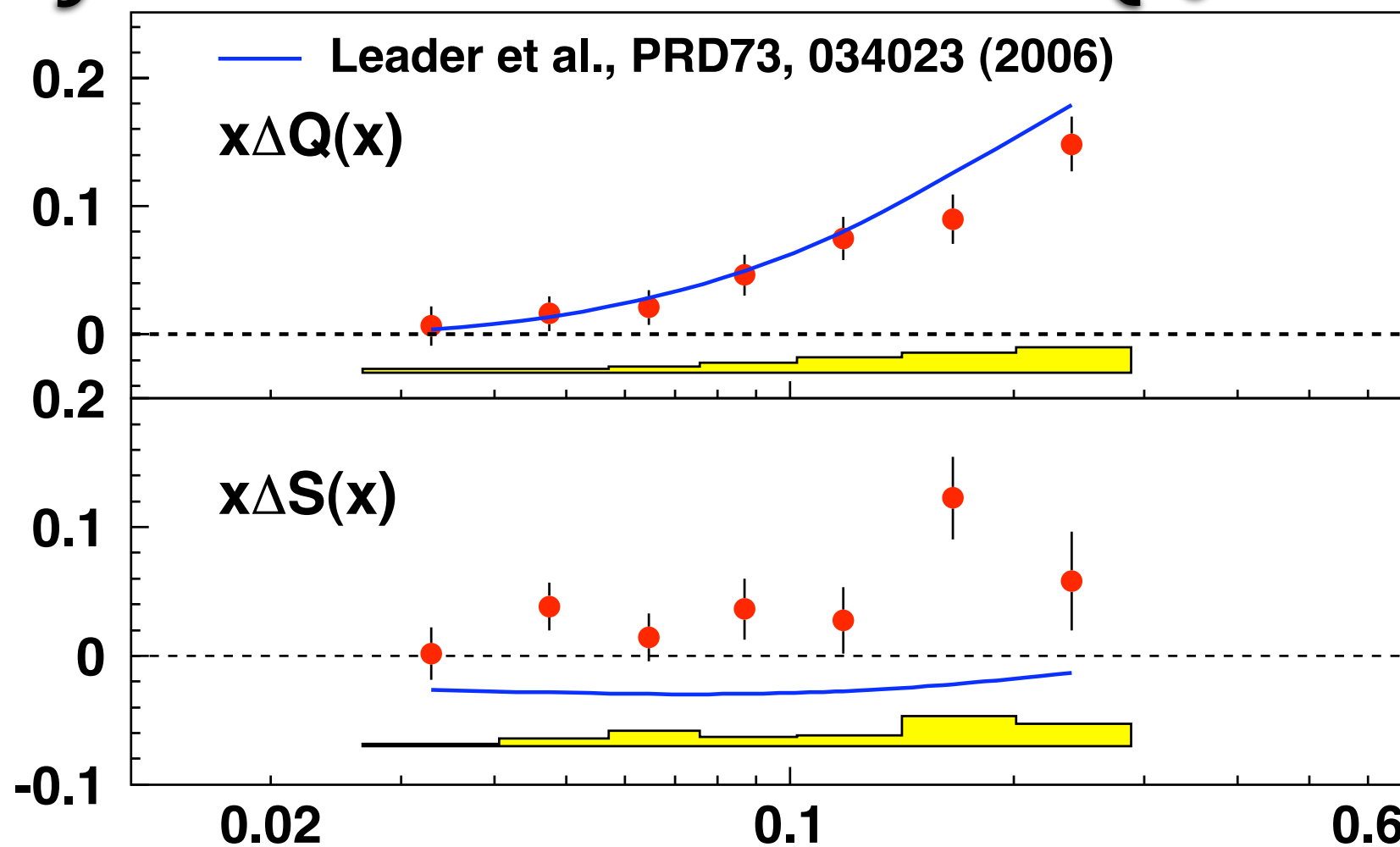
$$A_{||,d}(x) \frac{d^2 N^{\text{DIS}}(x)}{dx dQ^2} = \mathcal{K}_{LL}(x, Q^2) [5\Delta Q(x) + 2\Delta S(x)]$$

$$A_{||,d}^{\text{K}}(x) \frac{d^2 N^{\text{K}}(x)}{dx dQ^2} = \mathcal{K}_{LL}(x, Q^2) \left[\Delta Q(x) \int D_Q^{\text{K}}(z) dz + \Delta S(x) \int D_S^{\text{K}}(z) dz \right]$$

$$\Delta Q(x) = \Delta u(x) + \Delta \bar{u}(x) + \Delta d(x) + \Delta \bar{d}(x)$$

$$\Delta S(x) = \Delta s(x) + \Delta \bar{s}(x)$$

Helicity distributions at $Q^2_0=2.5 \text{ GeV}^2$



- $0.02 < x_{Bj} < 0.6$
- $\Delta q_8 = \Delta Q - 2\Delta S$
- from hyperon decay constants (assuming SU(3) symmetry):

$$\Delta q_8 = \int_0^1 \Delta q_8(x) dx = 0.586 \pm 0.031$$

Moments in measured range

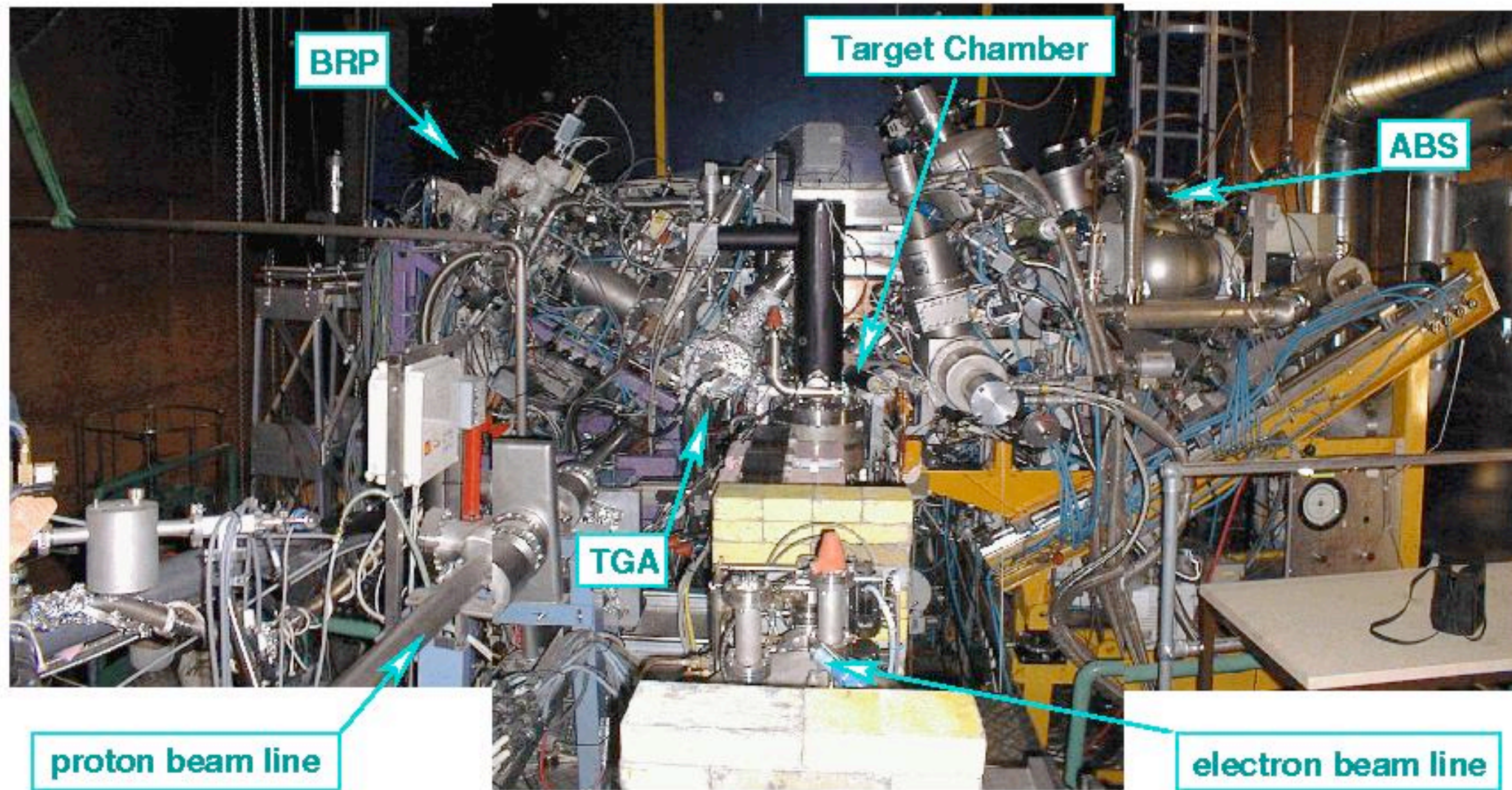
ΔQ	$0.359 \pm 0.026(\text{stat.}) \pm 0.018(\text{sys.})$
ΔS	$0.037 \pm 0.019(\text{stat.}) \pm 0.027(\text{sys.})$
Δq_8	$0.285 \pm 0.046(\text{stat.}) \pm 0.057(\text{sys.})$

Conclusions

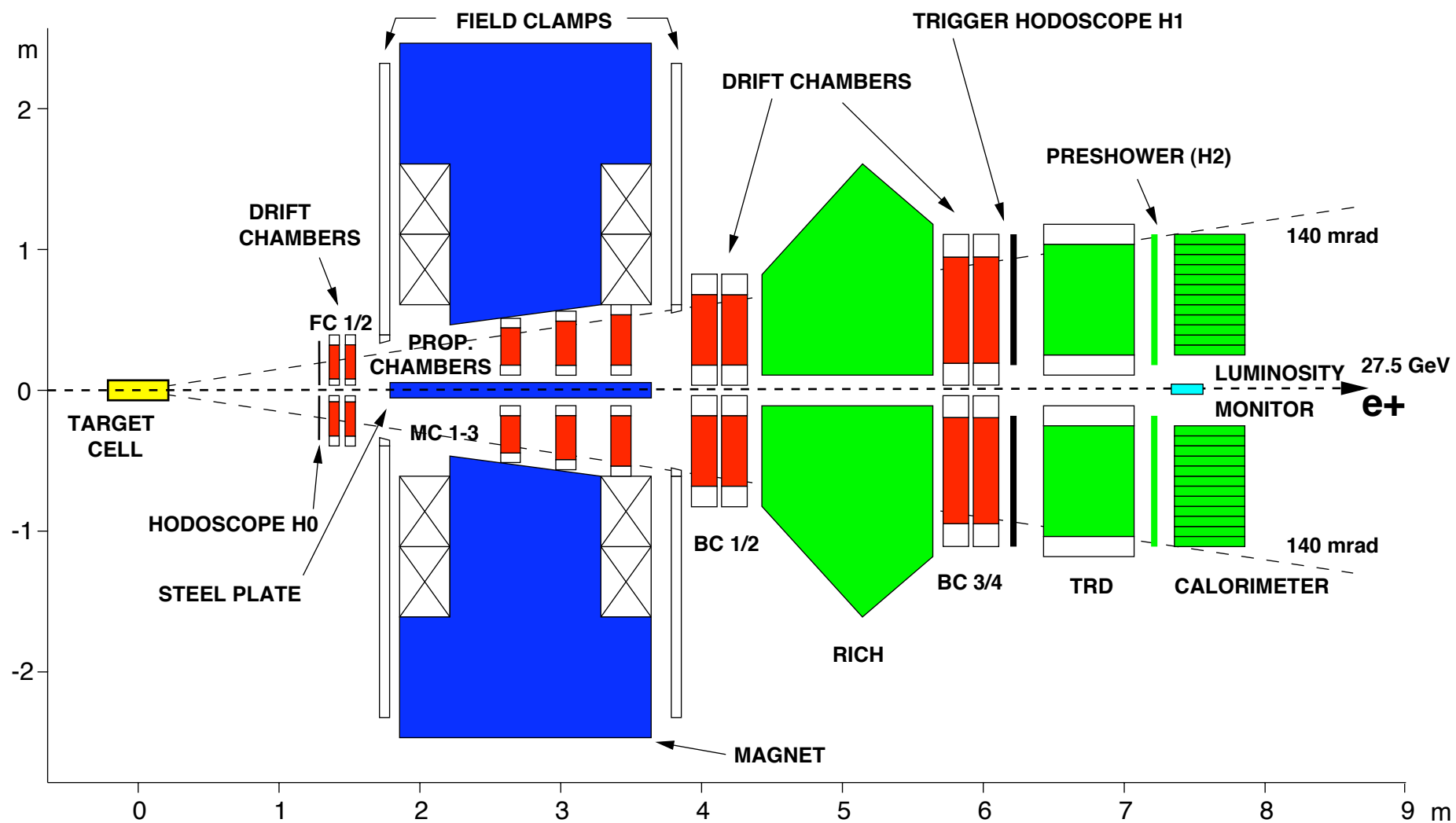
- (most) precise data on a transversely polarized hydrogen target
- significant Collins amplitudes for π -mesons
 - ⇒ enables quantitative extraction of transversity distribution
- significant Sivers amplitudes for π^+ and K^+
 - ⇒ clear (and first) evidence of naive-T-odd parton distribution
 - ⇒ enables quantitative extraction of the Sivers function
- Shape of $S(x)$ is much softer than the isoscalar sea
- SU(3) symmetry seems to be violated by strange quark PDFs
- s quark helicity densities consistent with 0

Additional slides

The transversely pol target



The HERMES Experiment



Internal gas target: pol. : He, H, D

unpol: H₂, D₂, He, N₂, Ne, Kr, Xe

Particle ID: TRD, Preshower, Calorimeter, Cerenkov (until 1997), RICH (since 1998)

Reconstruction: $\Delta p/p < 2\%$, $\Delta\theta < 1$ mrad