

Highlights from HERMES

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(DESY)

for the  collaboration

Overview

- HERMES @ HERA
- Longitudinal nucleon structure
 - ▶ Spin-dependent structure function g_1
 - ▶ Strange quark distribution $s(x)$ and $\Delta s(x)$
- Transverse structure of the nucleon
 - ▶ Transversity and transverse momentum dependent distribution functions
- 3D picture of the nucleon
 - ▶ Accessing Generalized Parton Distributions (GPDs) via Deeply Virtual Compton Scattering (DVCS)

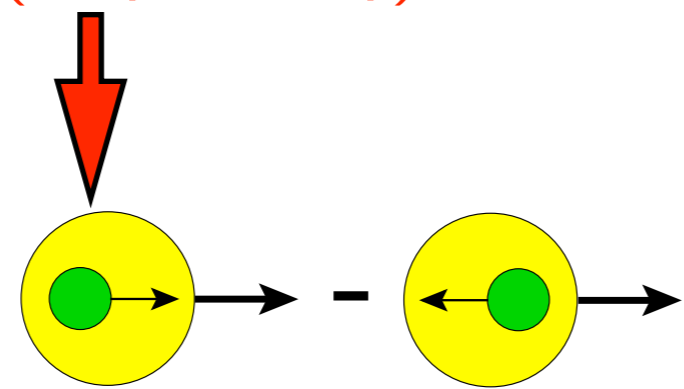
The Quest: Spin Structure of the Proton



$$\frac{1}{2} = \frac{1}{2} \Delta\Sigma + \Delta G + L_q + L_g$$

← quark spin
← gluon spin
← orbital angular momentum

$$\Delta\Sigma = \sum_{q=u,d,s} (\Delta q + \Delta \bar{q})$$



The Quest: Spin Structure of the Proton



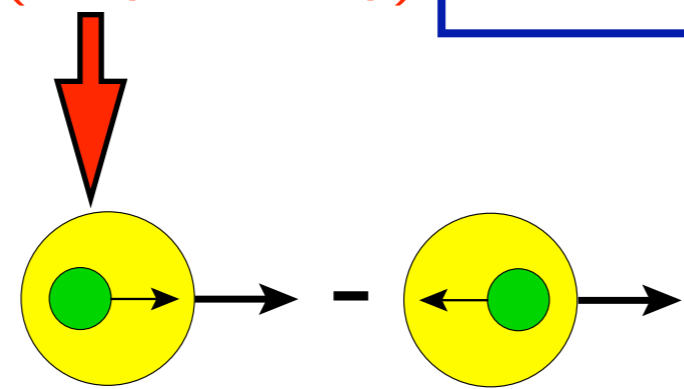
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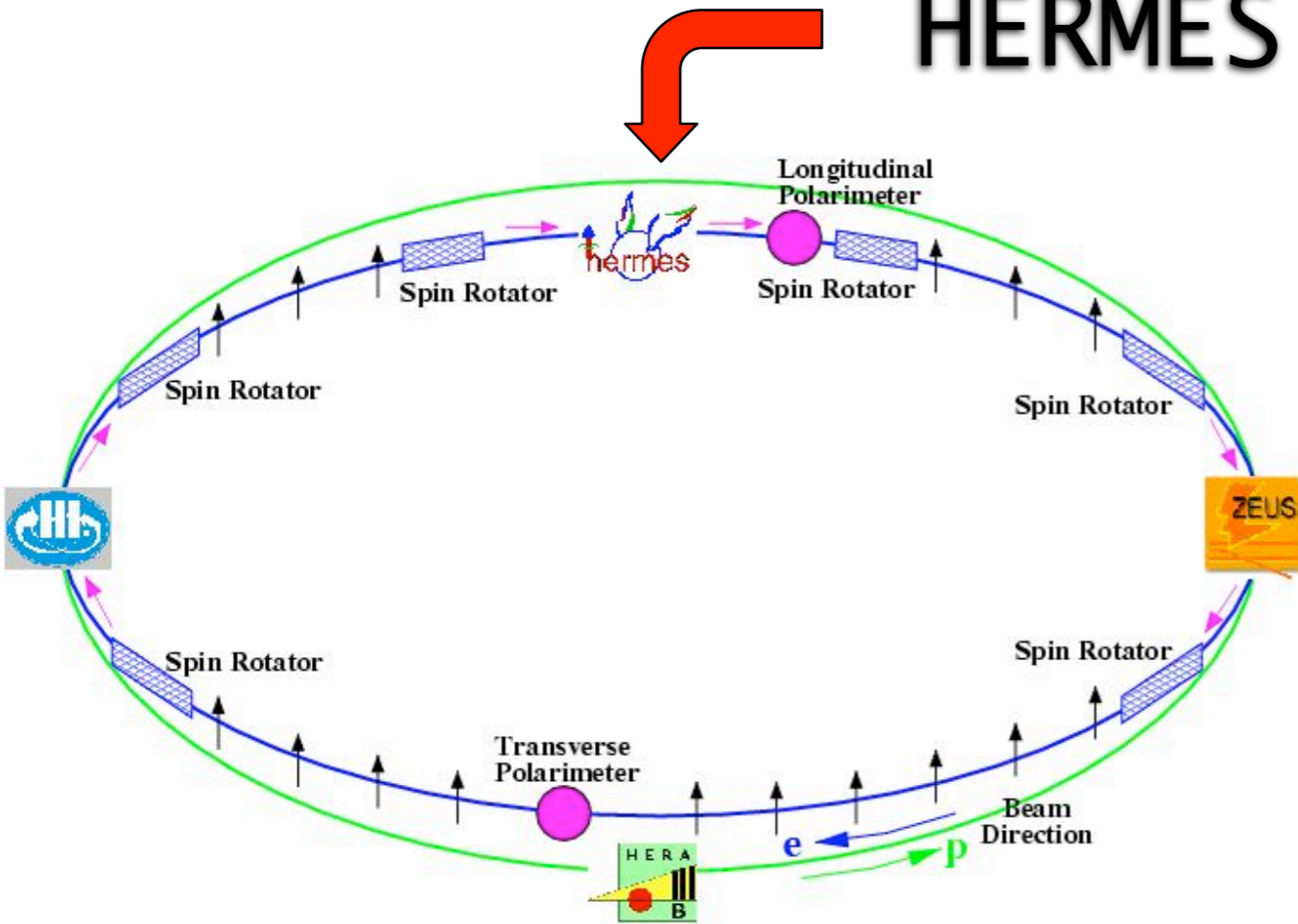
EMC (1988):

$$\Delta\Sigma = \sum_{q=u,d,s} (\Delta q + \Delta \bar{q})$$

$$= 0.120 \pm 0.094(\text{stat}) \pm 0.138(\text{syst})$$

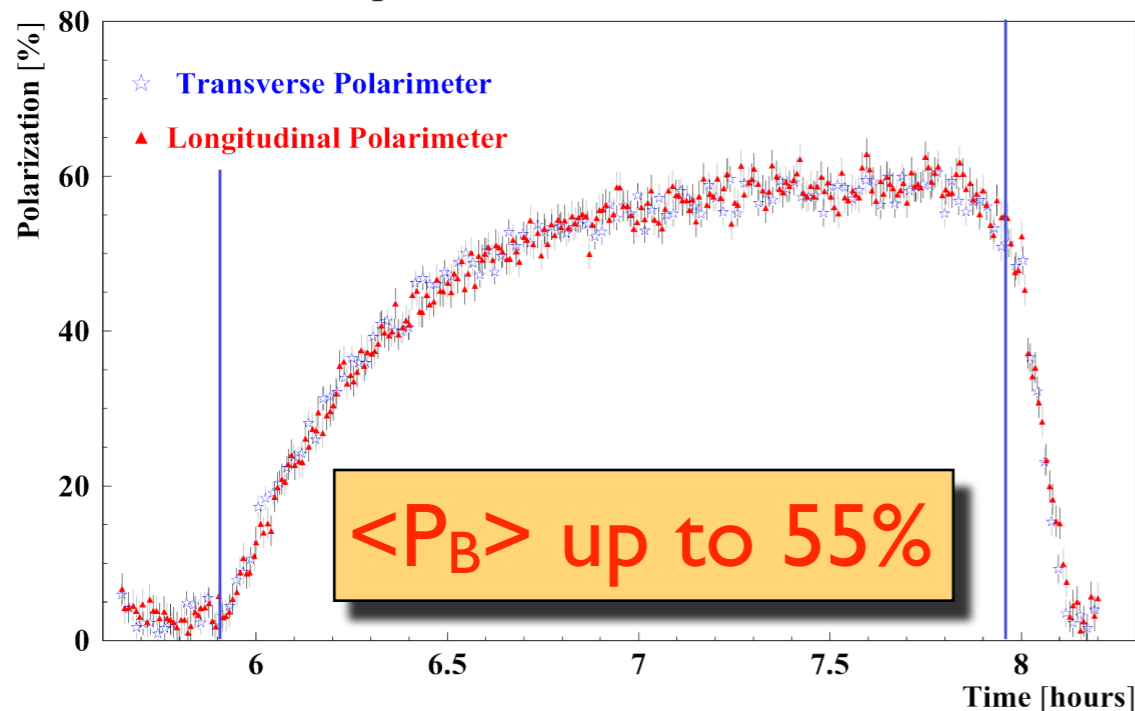


HERMES @ HERA



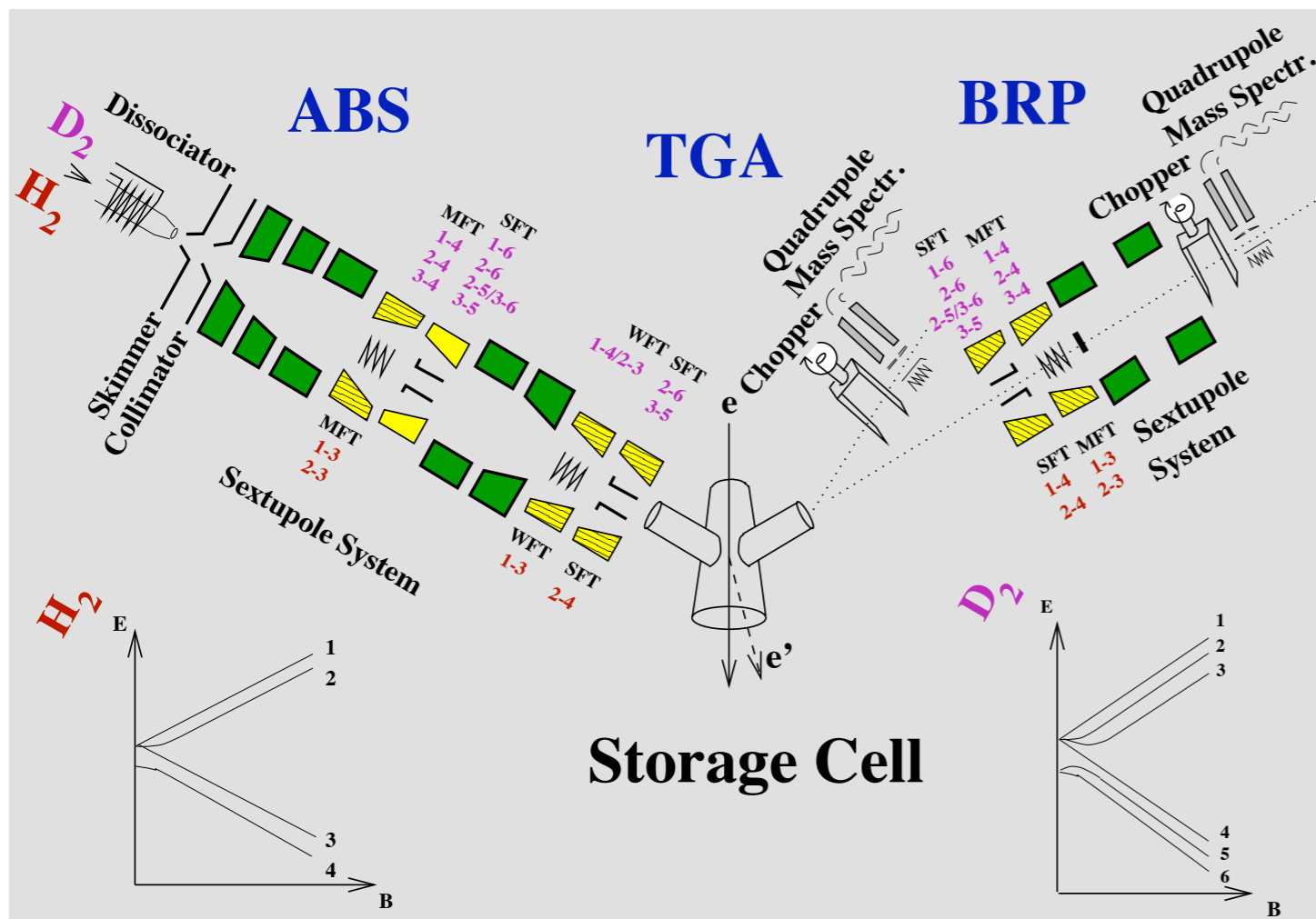
- **Fixed target** experiment
 ➔ only using HERA lepton (e^+/e^-) beam
- HERA lepton beam **self-polarizing**
 ➔ cross section asymmetry in synchrotron radiation emission leads to build-up of **transverse polarization** (Sokolov-Ternov effect)
- Spin-rotators ➔ **longitudinal polarization at HERMES** interaction region
- Beam polarization measured by two independent polarimeters

Comparison of rise time curves



The HERMES Target

Gaseous target in storage cell aligned with lepton beam

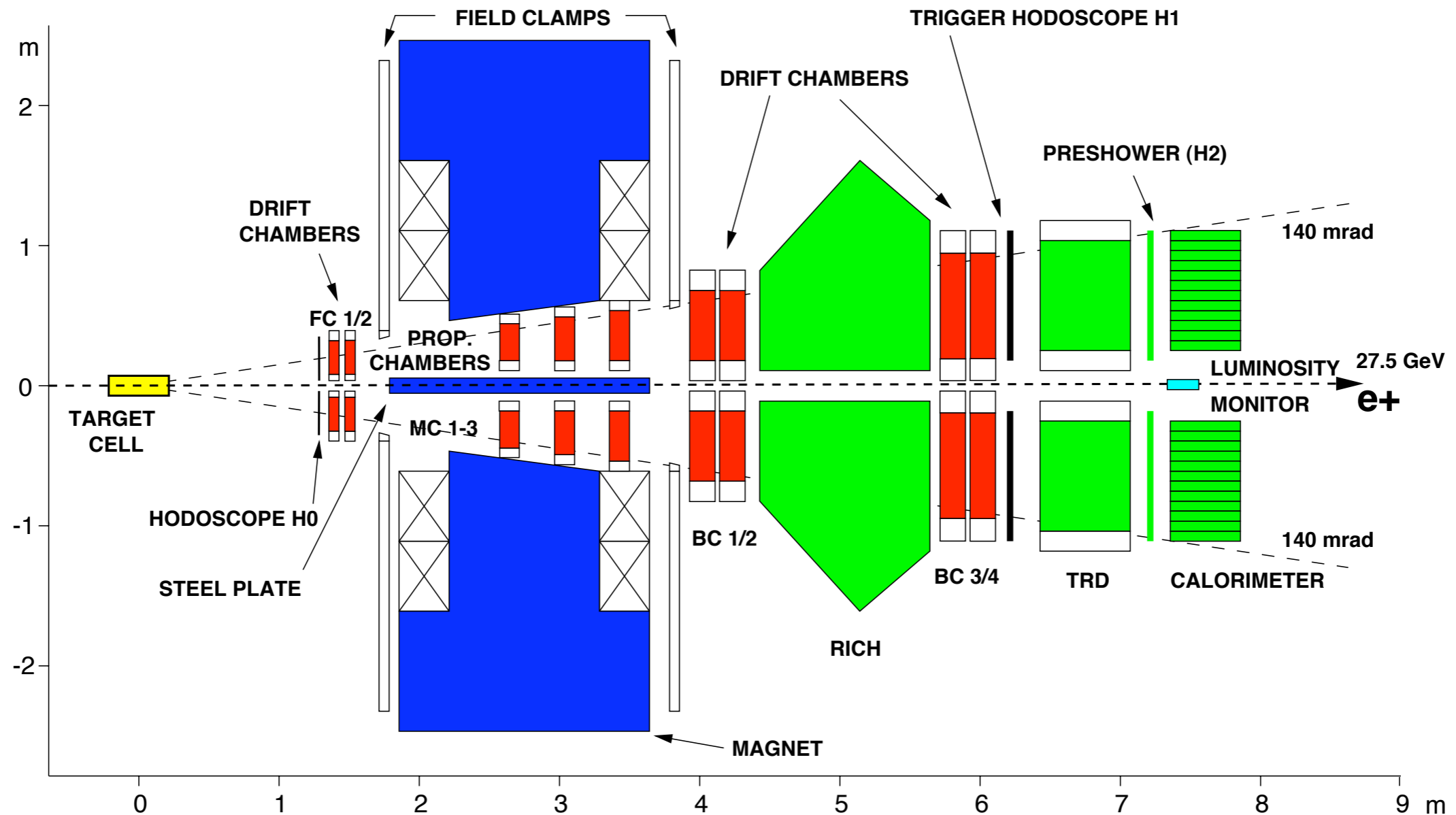


Features:

- Pure target (**no dilution**)
- **Unpolarized targets:**
variety of nuclear targets
 - ▶ H, D, He, Ne, Kr, ...
- **Polarized targets:**
 - ▶ Longitudinal pol. (≤ 2000)
H, D, He
 - ▶ Transverse pol. (2002-2005)
H
 - ▶ **Rapid reversal of polarization direction within 0.5s (every 90s)**

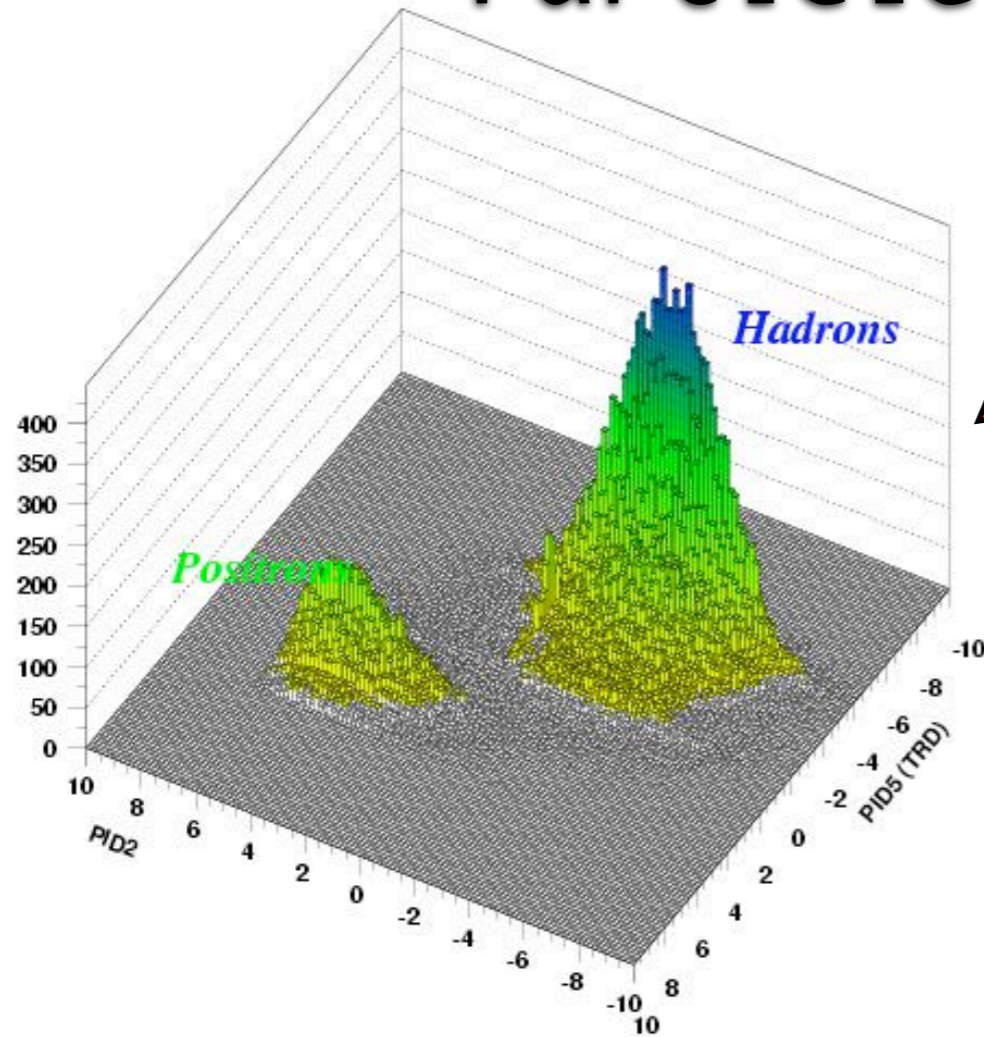
Polarization:
longitudinal: ~85%
transversal: ~75%

HERMES Spectrometer

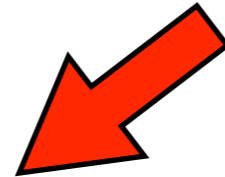


- Forward acceptance spectrometer: $40 \text{ mrad} \leq \Theta \leq 220 \text{ mrad}$
- Kinematic coverage: $0.02 \leq x_{Bj} \leq 0.8$ for $Q^2 > 1 \text{ GeV}^2$ and $W > 2 \text{ GeV}$
- Tracking: $\delta P/P = 0.7\% - 2.5\%$, $\delta\Theta \leq 1 \text{ mrad}$
- PID: TRD, Preshower, Calorimeter, Cherenkov (RICH after 1997)

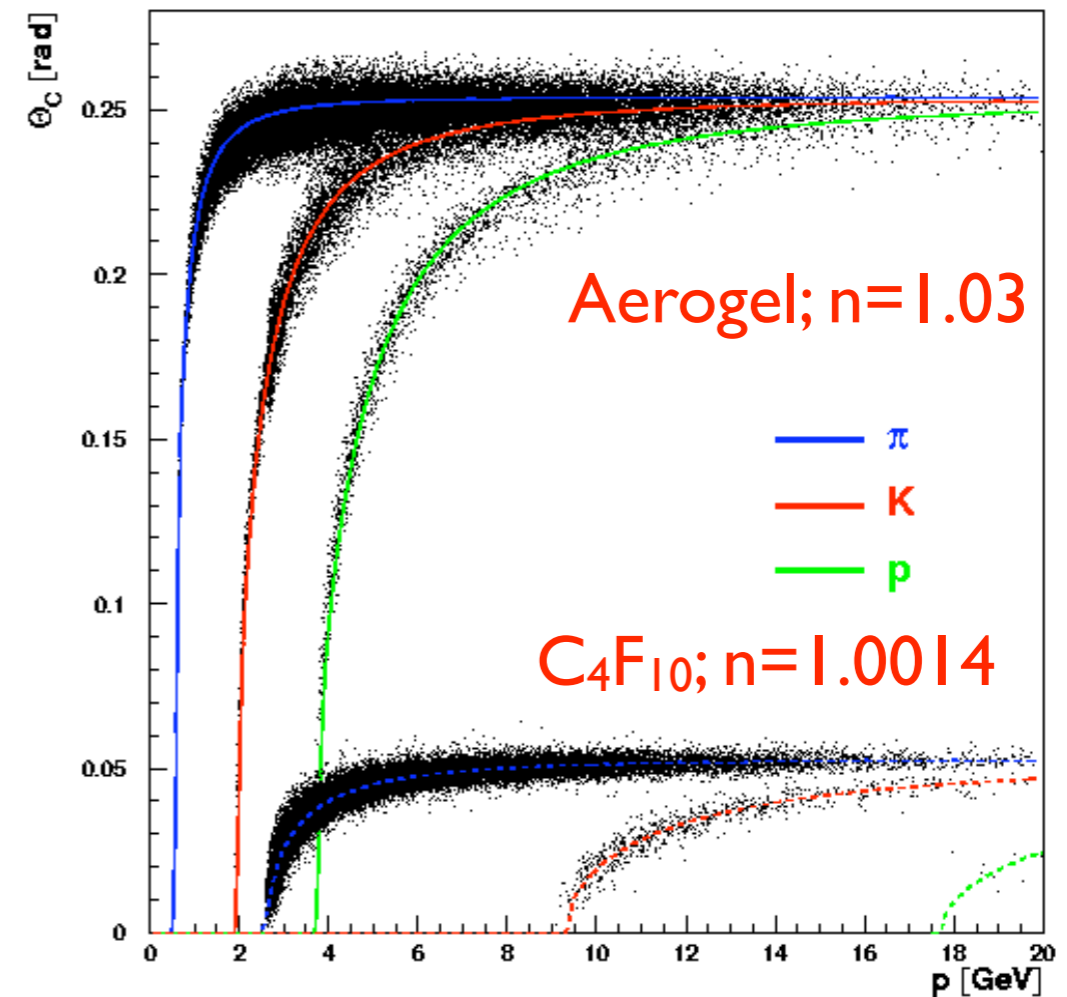
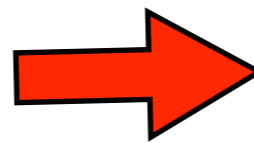
Particle Identification



excellent lepton/hadron separation



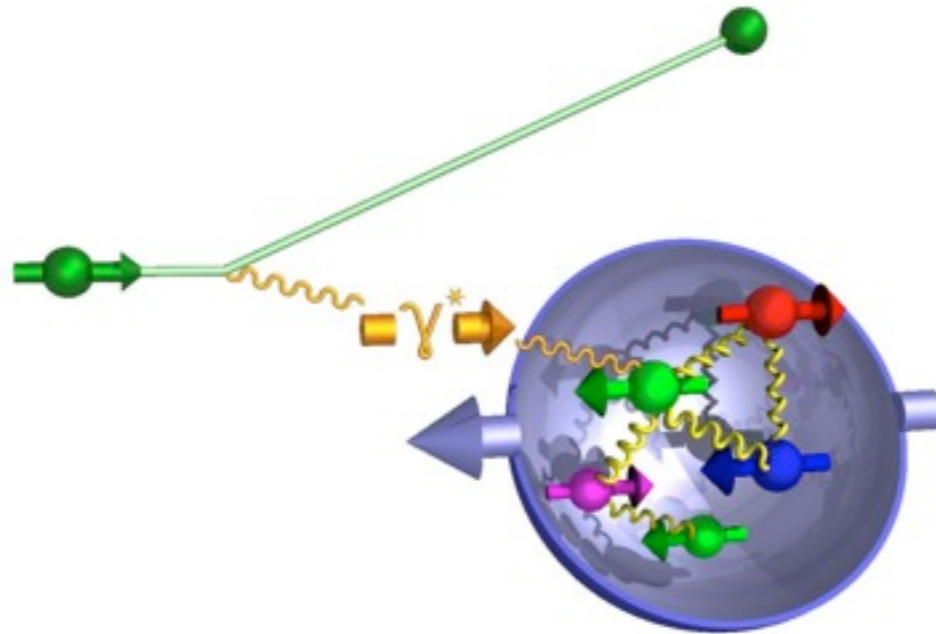
RICH: two radiators allow hadron separation between 2-15 GeV



The spin-dependent structure function g_1

g_1 : Inclusive DIS

HERA:
 e^\pm @ 27.6 GeV
 $P_B \sim 53\%$



long. pol. undiluted
 gas target:
 H ($P_z \sim 76\%, 85\%$)
 D ($P_z \sim 84\%$)

Cross section \rightarrow structure functions

{	F_1, F_2	unpol
	g_1, g_2	pol
	$b_1 \dots b_4$	pol (spin-1)

$$g_1(x, Q^2) = \frac{1}{2} \sum_q e_q^2 [\Delta q(x, Q^2) + \Delta \bar{q}(x, Q^2)]$$

in LO QCD

$$\Delta q = q_{\Rightarrow} - q_{\Leftarrow}$$

Measured Inclusive Asymmetries

$$P_{zz} = 0.83 \pm 0.03$$

$$A_{zz} \sim 0.01$$

$$\implies \frac{b_1^d}{F_1^d} = -\frac{3}{2} A_{zz}$$

(measured by HERMES)

$$\sigma = \sigma_{\text{unpol}} \left[1 + P_B P_z A_{\parallel} + \underbrace{\frac{1}{2} P_{zz} A_{zz}}_{\text{Deuterium}} \right]$$

measured DIS cross section

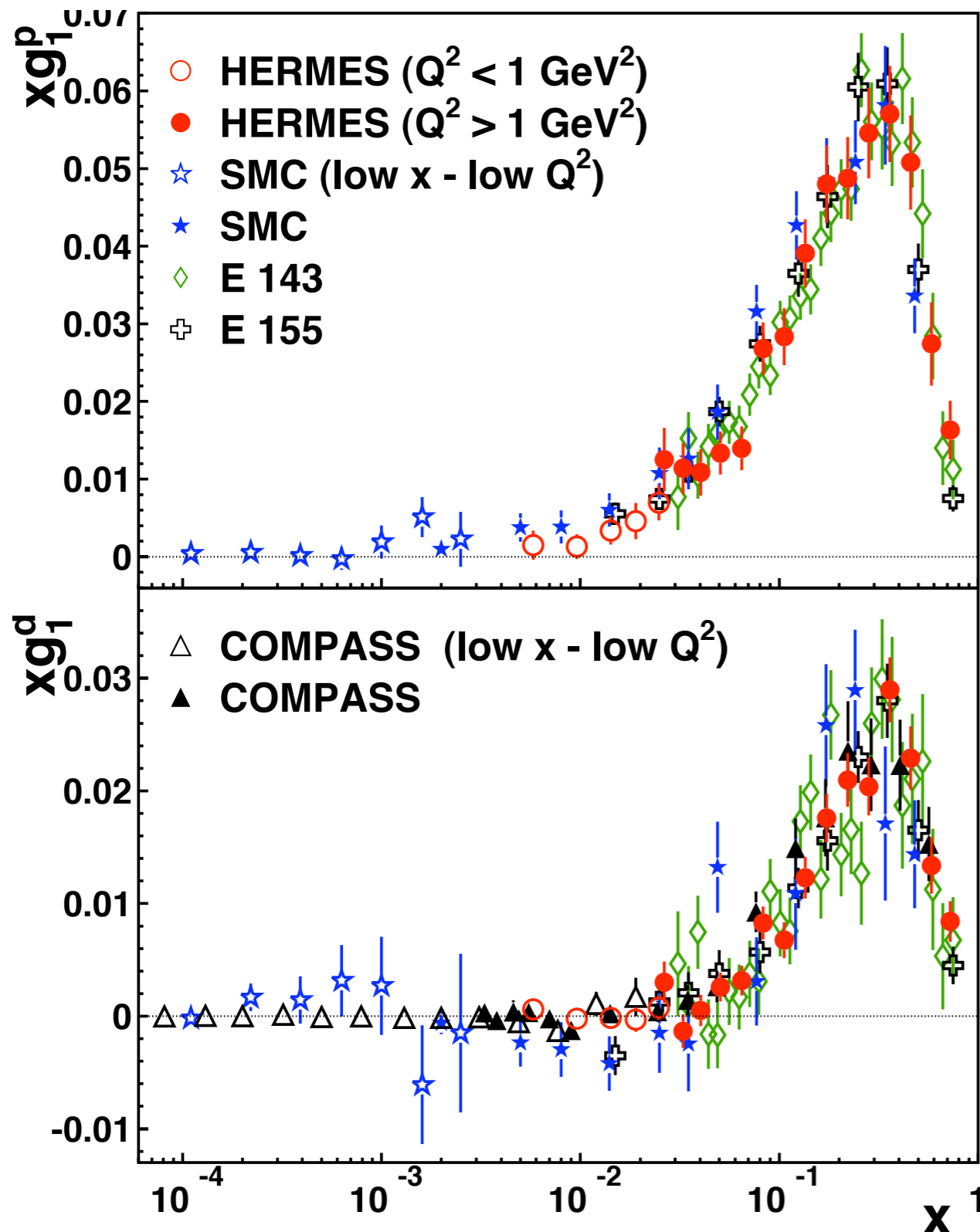
inclusive asymmetry:

$$A_{\parallel} = \frac{\sigma^{\leftarrow} - \sigma^{\rightarrow}}{\sigma^{\leftarrow} + \sigma^{\rightarrow}} = \frac{1}{P_B P_z} \cdot \frac{\frac{N^{\leftarrow}}{L^{\leftarrow}} - \frac{N^{\rightarrow}}{L^{\rightarrow}}}{\frac{N^{\leftarrow}}{L^{\leftarrow}} + \frac{N^{\rightarrow}}{L^{\rightarrow}}}$$

$$g_1(x, Q^2) = \frac{1}{1 - \frac{y}{2} - \frac{1}{4} y^2 \gamma} \left[\frac{Q^4}{8\pi\alpha^2 y} \frac{d^2\sigma_{\text{unpol}}}{dx dQ^2} A_{\parallel}(x, Q^2) + \frac{y}{2} \gamma^2 g_2(x, Q^2) \right]$$

kinematic factors
param.
meas.
kin. fac.
param.

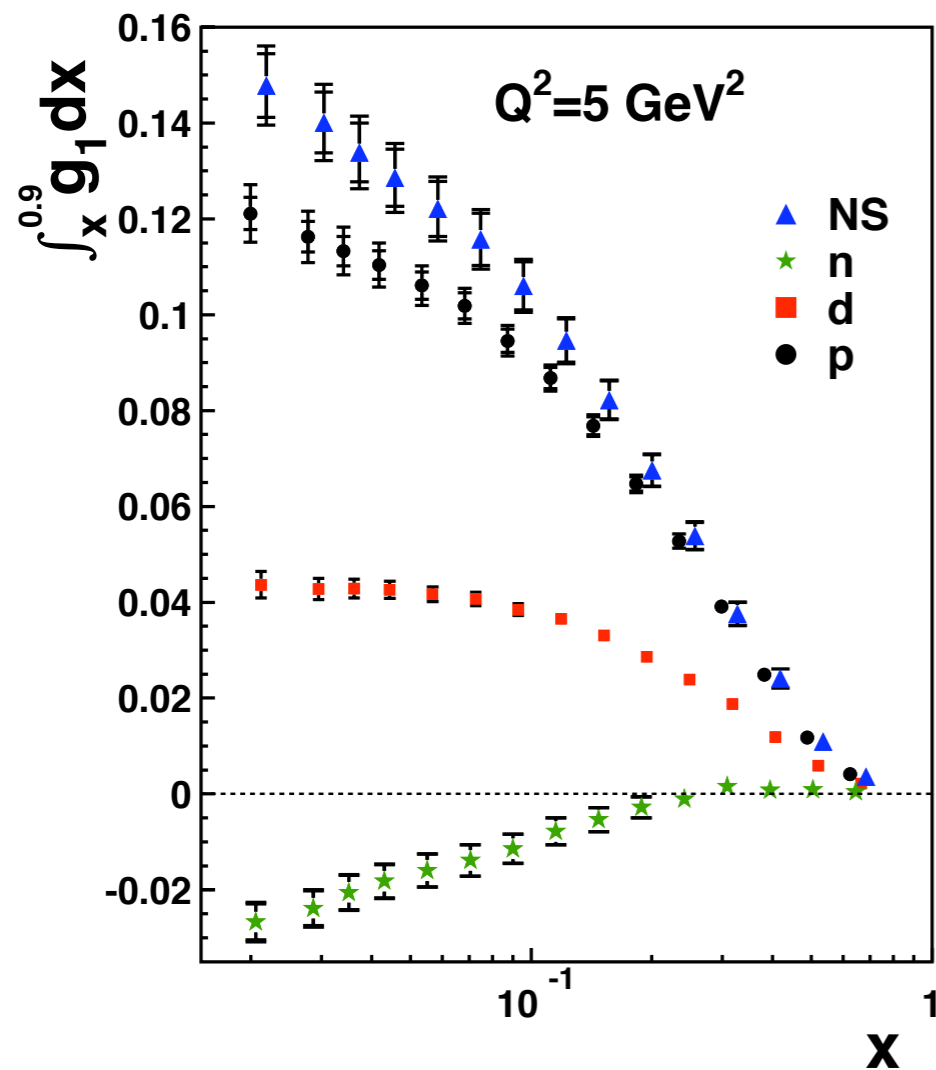
g_1 : Results for p and d



- Proton data:
 - ▶ Stat. precision comparable to previous data
- Deuteron data:
 - ▶ Most precise data in valence x region
- $\langle Q^2 \rangle$ lower compared to SMC/COMPASS
- HERMES points: **stat. and syst. errors added** in quadrature
 - ▶ **Stat. uncertainties** are **correlated** from **unfolding** of bin-to-bin migrations (shown are the diagonal elements of the cov. matrix)
 - ▶ **Syst. uncertainties** dominated by **target and beam polarization**

g_1 : Integrals

Phys. Rev. D 75
(2007) 012007



$$\Gamma_1^d = \int dx g_1^d$$

Assuming *saturation* in the deuteron integral:

→ Use only deuteron data!

$$\Gamma_1^d = \left(1 - \frac{3}{2}\omega_D\right) \frac{1}{36} \left[4a_0 \Delta C_S^{\overline{MS}} + a_8 \Delta C_{NS}^{\overline{MS}}\right]$$

$$a_0 \stackrel{\overline{MS}}{=} \Delta\Sigma$$

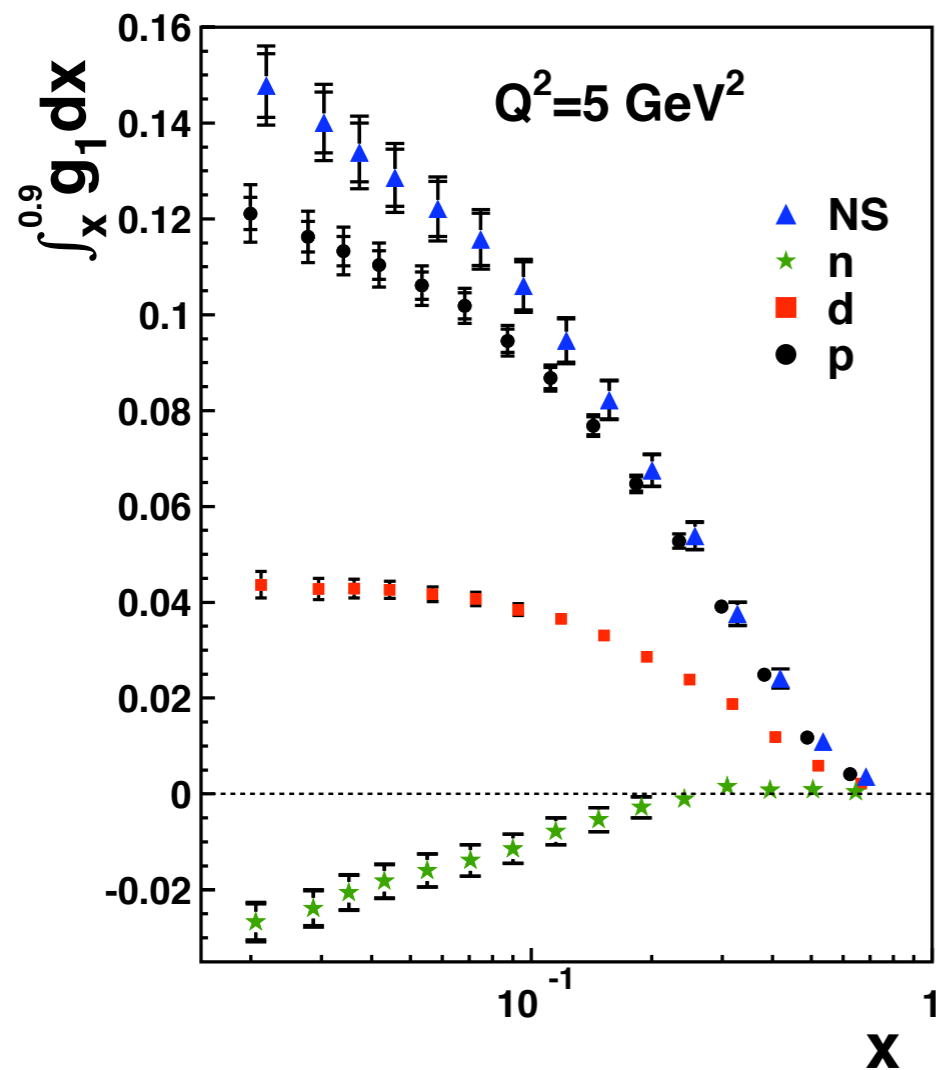
D-wave contribution to deuteron

in NNLO	central value	uncertainties		
		theor.	exp.	evol.
a_0	0.330	0.011	0.025	0.028
$\Delta u + \Delta \bar{u}$	0.842	0.004	0.008	0.009
$\Delta d + \Delta \bar{d}$	-0.427	0.004	0.008	0.009
$\Delta s + \Delta \bar{s}$	-0.085	0.013	0.008	0.009

$Q^2 = 5\text{GeV}^2$, NNLO in \overline{MS} scheme

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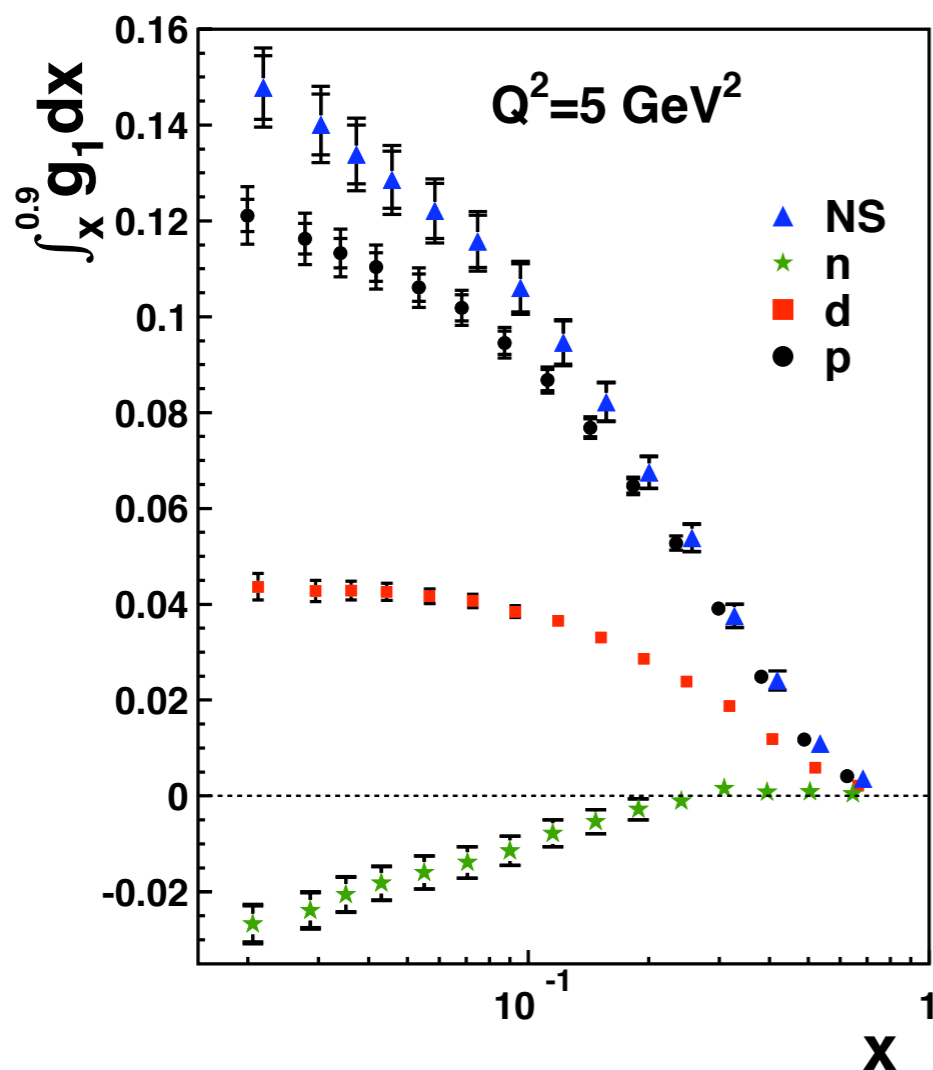
from hyperon beta decay
($a_8 = 0.586 \pm 0.031$)

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$$a_0 \stackrel{\overline{MS}}{=} \Delta\Sigma$$

$$\begin{aligned} \Delta u + \Delta \bar{u} &= \frac{1}{6} [2a_0 + a_8 + 3a_3] \\ \Delta d + \Delta \bar{d} &= \frac{1}{6} [2a_0 + a_8 - 3a_3] \\ \Delta s + \Delta \bar{s} &= \frac{1}{3} [a_0 - a_8] \end{aligned}$$

from hyperon beta decay
($a_8 = 0.586 \pm 0.031$)

from neutron beta decay
($a_3 = 1.269 \pm 0.003$)

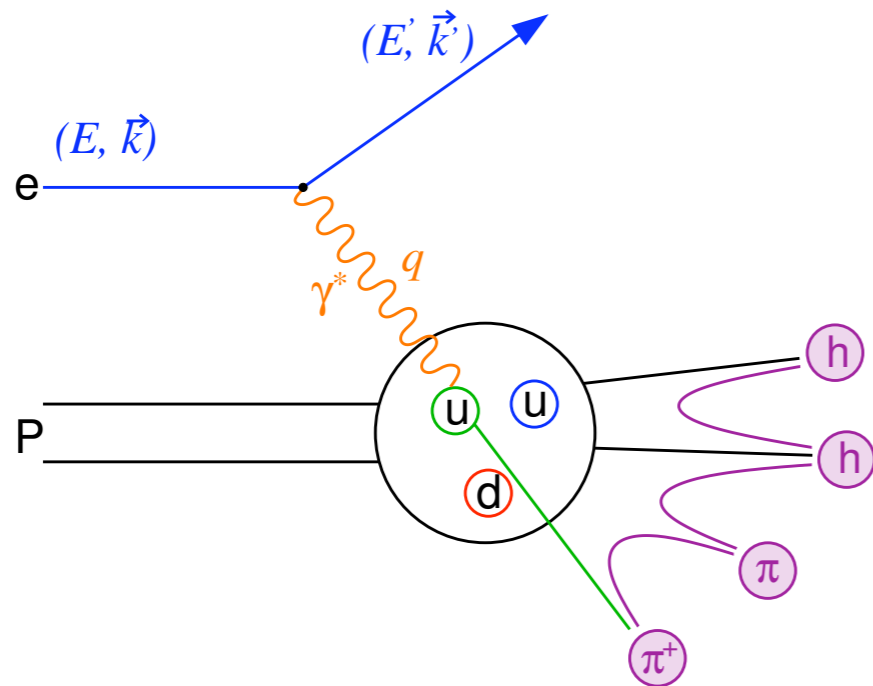
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$Q^2 = 5\text{GeV}^2$, NNLO in \overline{MS} scheme

Strange quark distributions

Semi-inclusive DIS

e^\pm @ 27.6 GeV (HERA)



Targets:

H: $\langle P_{\text{trans}} \rangle \sim 74 \pm 6\%$

D: $\langle P_{\text{long}} \rangle \sim 84.5 \pm 3.5\%$

Cross section contains **Distribution Functions** and **Fragmentation Functions**:

$$\sigma^{ep \rightarrow eh} \sim \sum_q DF^{p \rightarrow q} \otimes \sigma^{eq \rightarrow eq} \otimes FF^{q \rightarrow h}$$

DF: distribution of quarks in the nucleon

FF: fragmentation of (struck) quark into hadronic final state

Strange PDFs with isoscalar target

Assumptions:

- isospin symmetry between proton and neutron
- charge conjugation invariance in fragmentation

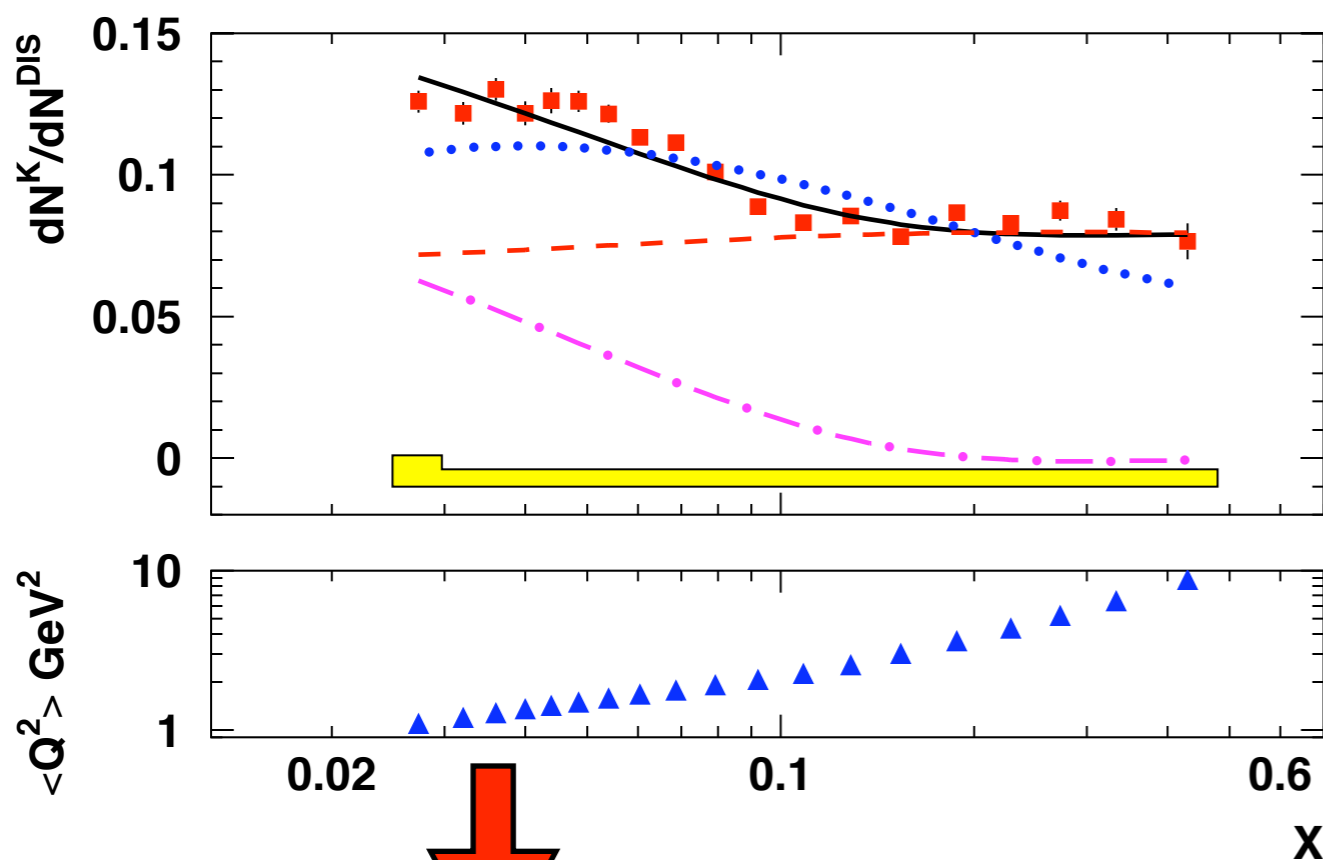
- strange quarks carry no isospin $\Rightarrow S(x)_{\text{Proton}} = S(x)_{\text{Neutron}}$
- deuteron target (isoscalar!):
fragmentation process in DIS can be described by isospin independent FFs
- Charged kaon multiplicity in LO:

$$\frac{dN^K(x)}{dN^{\text{DIS}}(x)} = \frac{Q(x) \int D_Q^K(z) dz + S(x) \int D_S^K(z) dz}{5Q(x) + 2S(x)}$$

$$Q(x) \equiv u(x) + \bar{u}(x) + d(x) + \bar{d}(x) \quad D_Q^K \equiv 4D_u^K(z) + D_d^K(z)$$

$$S(x) \equiv s(x) + \bar{s}(x) \quad D_S^K(z) \equiv 2D_s^K(z)$$

Fitting $dN^K(x)/dN^{\text{DIS}}(x)$



Assuming $S(x)=0$ for $x>0.15$:

$$\int_{0.2}^{0.8} D_Q^K(z) dz = 0.398 \pm 0.010$$

de Florian et al., PRD75, 114010 (2007):

$$\int_{0.2}^{0.8} D_Q^K(z) dz = 0.435 \pm 0.044$$

$$\frac{dN^K(x)}{dN^{\text{DIS}}(x)} = \frac{Q(x) \int D_Q^K(z) dz + S(x) \int D_S^K(z) dz}{5Q(x) + 2S(x)}$$

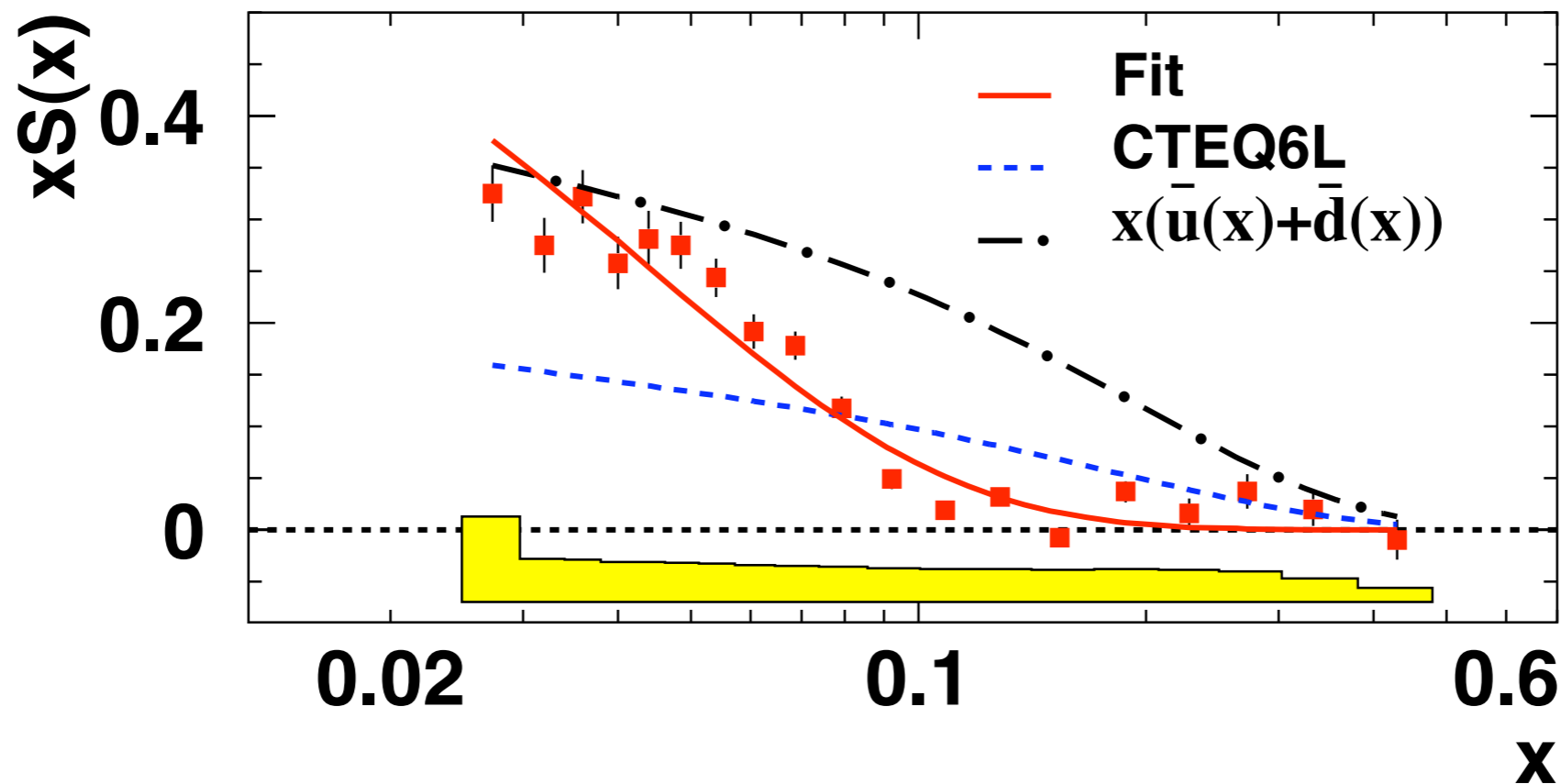
CTEQ6L

$S(x)$ at $Q^2=2.5 \text{ GeV}^2$

- $xS(x)$ obtained by evolution of data to $Q^2=2.5 \text{ GeV}^2$ using

$$\int_{0.2}^{0.8} D_S^K(z) dz = 1.27 \pm 0.13$$

de Florian et al., PRD75, 114010 (2007)

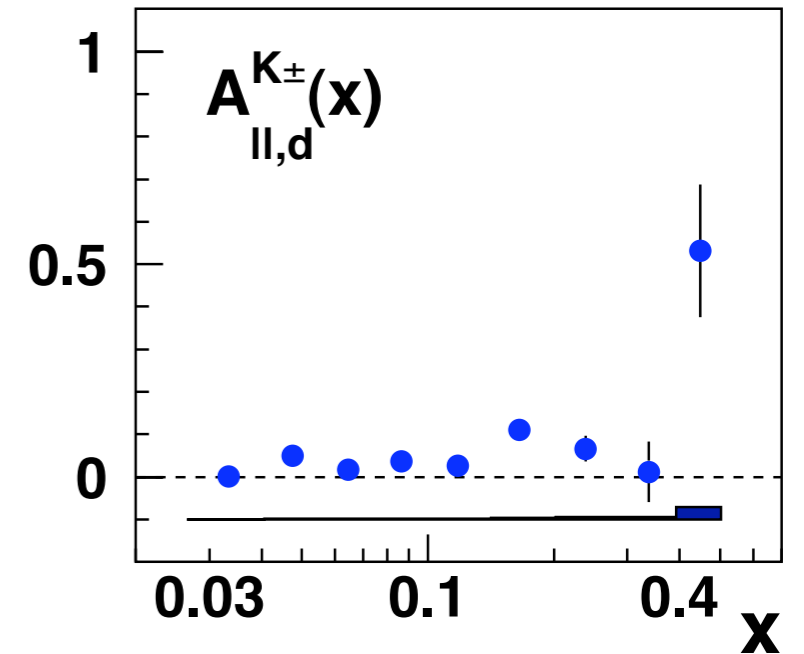
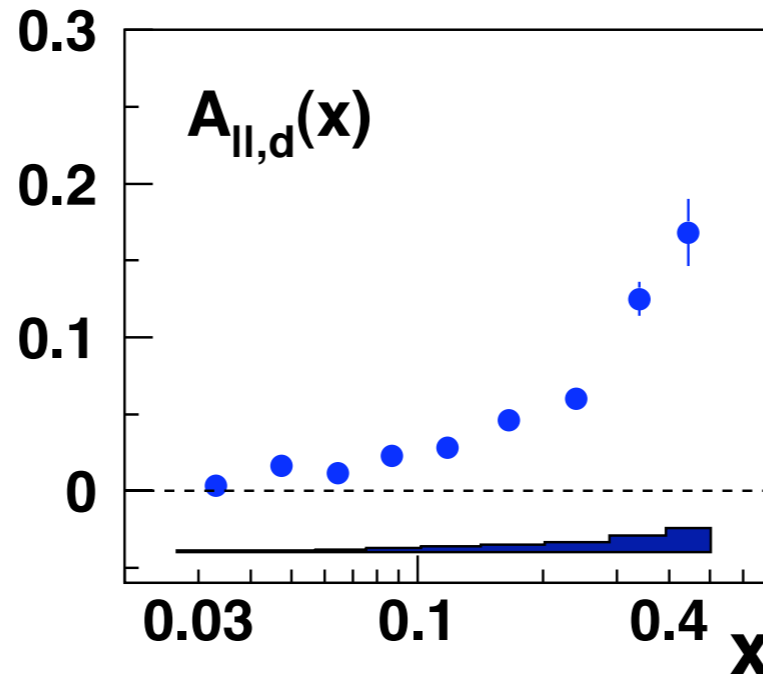


- Shape incompatible with CTEQ6L and with average of the isoscalar non-strange sea

Extraction of $\Delta Q(x)$ and $\Delta S(x)$

Double spin asymmetries from long. pol. deuteron target

$$A_{||}^{(h)} = \frac{\sigma^{\overleftarrow{=},(h)} - \sigma^{\overrightarrow{=},(h)}}{\sigma^{\overleftarrow{=},(h)} + \sigma^{\overrightarrow{=},(h)}}$$



$$A_{||,d}(x) \frac{d^2 N^{\text{DIS}}(x)}{dx dQ^2} = \mathcal{K}_{LL}(x, Q^2) [5\Delta Q(x) + 2\Delta S(x)]$$

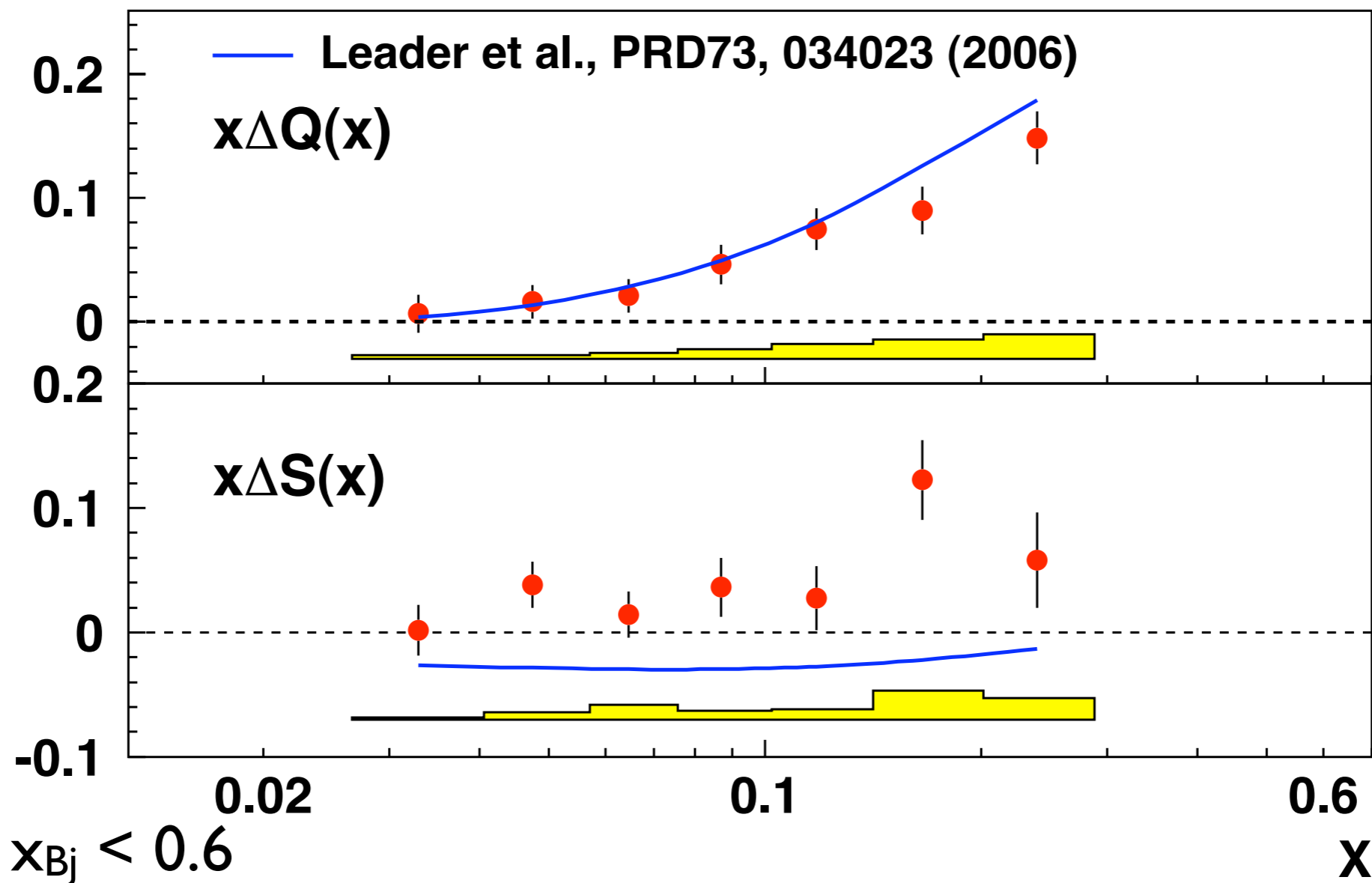
$$A_{||,d}^{\text{K}}(x) \frac{d^2 N^{\text{DIS}}(x)}{dx dQ^2} = \mathcal{K}_{LL}(x, Q^2) \left[\Delta Q(x) \int D_Q^{\text{K}}(z) dz + \Delta S(x) \int D_S^{\text{K}}(z) dz \right]$$

$$\Delta Q(x) = \Delta u(x) + \Delta \bar{u}(x) + \Delta d(x) + \Delta \bar{d}(x)$$

$$\Delta S(x) = \Delta s(x) + \Delta \bar{s}(x)$$

(from $S(X)$ extraction)

Helicity distributions at $Q^2=2.5 \text{ GeV}^2$



*Phys. Lett. B 666
(2008) 446*

- $0.02 < x_{Bj} < 0.6$
- $\Delta q_8 = \Delta Q - 2\Delta S$
- from hyperon decay constants (assuming SU(3) symmetry):
 $a_8 = 0.586 \pm 0.031 \simeq \Delta q_8$

Moments in measured range	
ΔQ	$0.359 \pm 0.026(\text{stat.}) \pm 0.018(\text{sys.})$
ΔS	$0.037 \pm 0.019(\text{stat.}) \pm 0.027(\text{sys.})$
Δq_8	$0.285 \pm 0.046(\text{stat.}) \pm 0.057(\text{sys.})$

Transverse Structure of the Nucleon

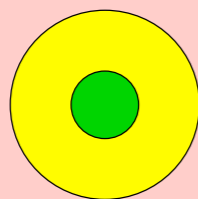
Distribution functions (I)

Leading twist:

3 DFs survive integration over transverse quark momenta

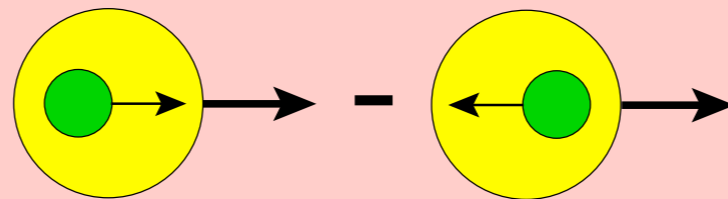
momentum distribution

$$q(x)$$



helicity distribution

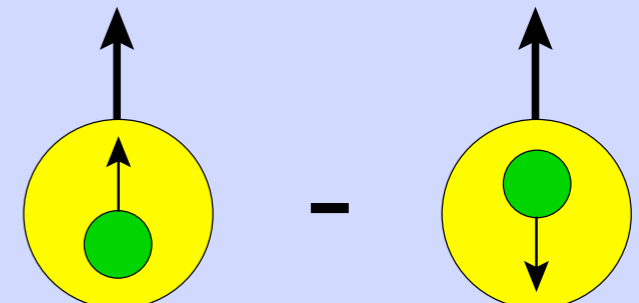
$$\Delta q(x)$$



helicity basis

transversity distribution

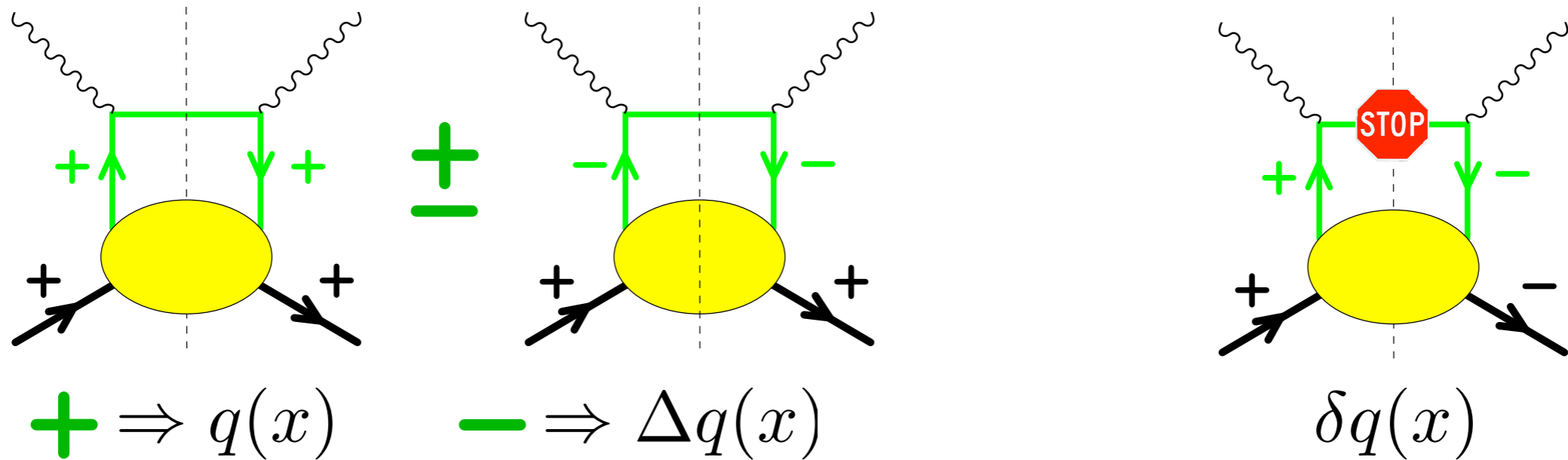
$$\delta q(x) = h_1^q(x)$$



basis of transv. spin eigenstates

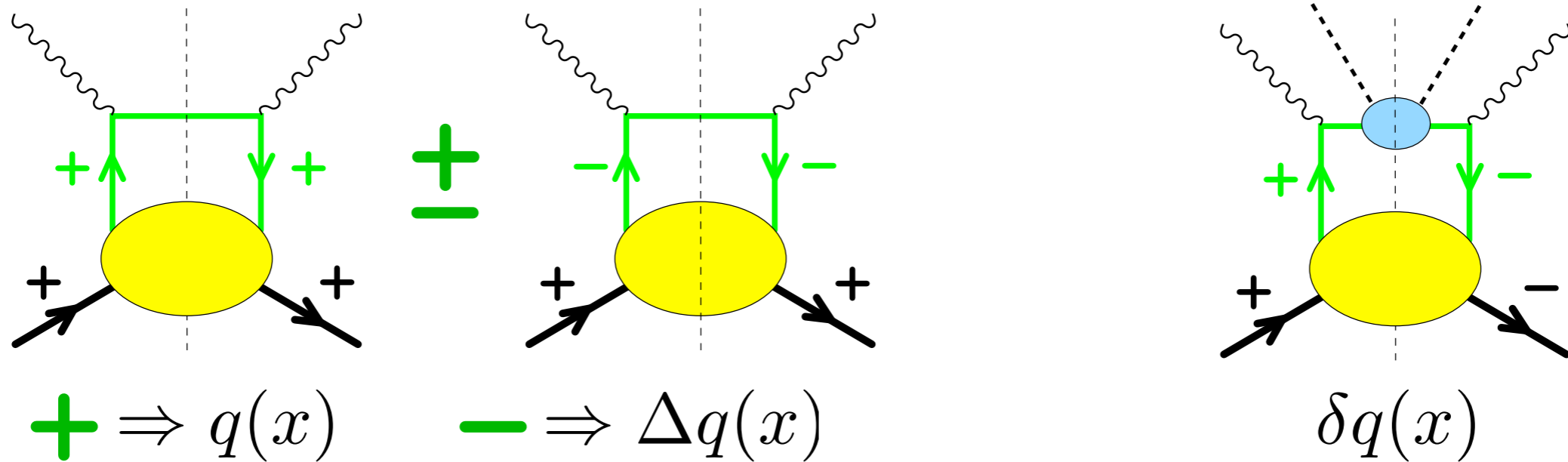
Transversity δq

- δq : helicity-flip of the quark \Rightarrow chiral-odd

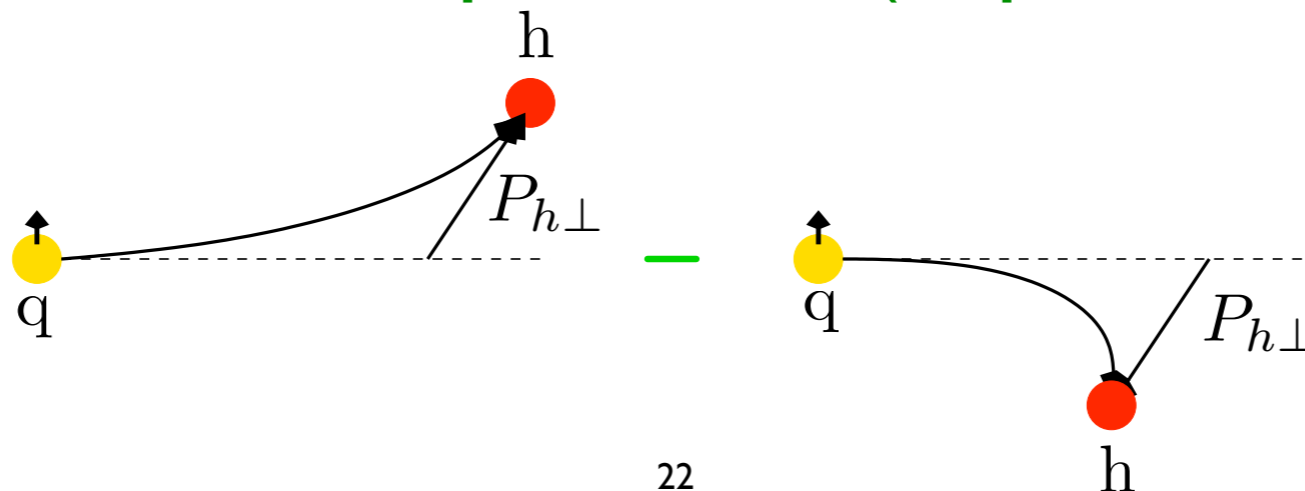


Transversity δq

- δq : helicity-flip of the quark \Rightarrow chiral-odd



- Collins-FF H_1^\perp describes **correlation** between **transverse polarisation of fragmenting quark** and the **transverse momentum $P_{h\perp}$ of the produced (unpolarised) hadron**



Distribution functions (II)

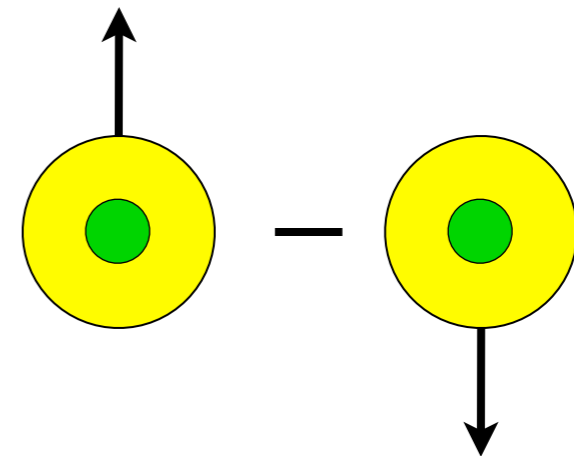
5 other sets of distribution functions exist which do not survive integration over transverse momentum



‘unintegrated’ or ‘transverse momentum dependent’ distributions (TMDs)

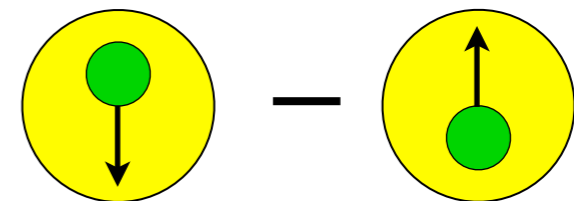
Sivers function:

correlates quark’s transverse momentum with transverse nucleon spin



Boer-Mulders function:

correlates quark’s transverse momentum with transverse quark spin

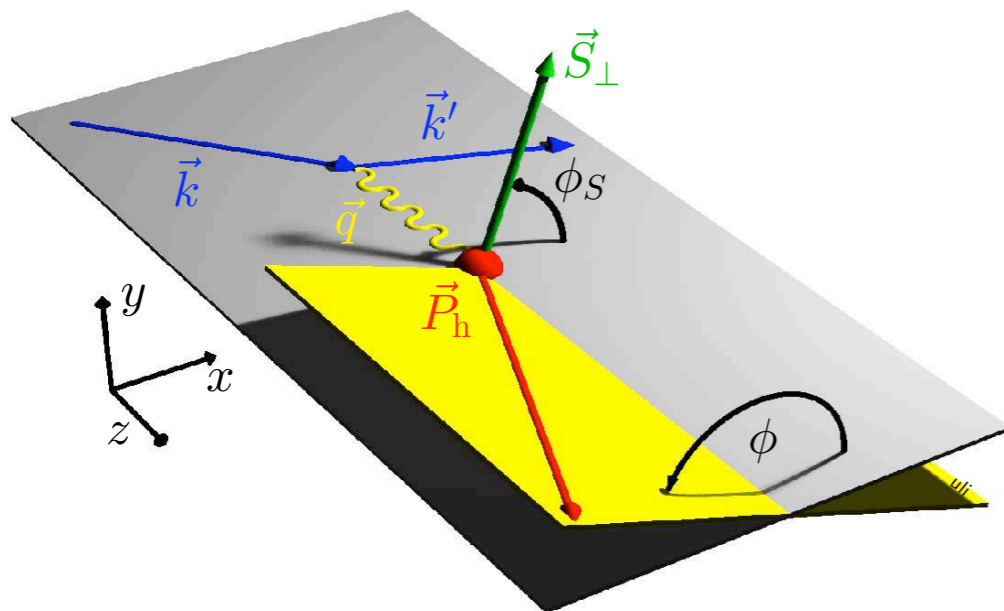


non-zero Sivers and Boer-Mulders functions require non-vanishing orbital angular momentum in nucleon wave function!

1-Hadron Production ($ep \rightarrow ehX$)

$$\begin{aligned}
 d\sigma = & d\sigma_{UU}^0 + \cos 2\phi d\sigma_{UU}^1 + \frac{1}{Q} \cos \phi d\sigma_{UU}^2 + \lambda_e \frac{1}{Q} \sin \phi d\sigma_{LU}^3 \\
 & + S_L \left\{ \sin 2\phi d\sigma_{UL}^4 + \frac{1}{Q} \sin \phi d\sigma_{UL}^5 + \lambda_e \left[d\sigma_{LL}^6 + \frac{1}{Q} \cos \phi d\sigma_{LL}^7 \right] \right\} \\
 & + S_T \left\{ \sin(\phi - \phi_S) d\sigma_{UT}^8 + \sin(\phi + \phi_S) d\sigma_{UT}^9 + \sin(3\phi - \phi_S) \sigma_{UT}^{10} \right. \\
 & \quad \left. + \frac{1}{Q} (\sin(2\phi - \phi_S) d\sigma_{UT}^{11} + \sin \phi_S d\sigma_{UT}^{12}) \right. \\
 & \quad \left. + \lambda_e \left[\cos(\phi - \phi_S) d\sigma_{LT}^{13} + \frac{1}{Q} (\cos \phi_S d\sigma_{LT}^{14} + \cos(2\phi - \phi_S) d\sigma_{LT}^{15}) \right] \right\}
 \end{aligned}$$

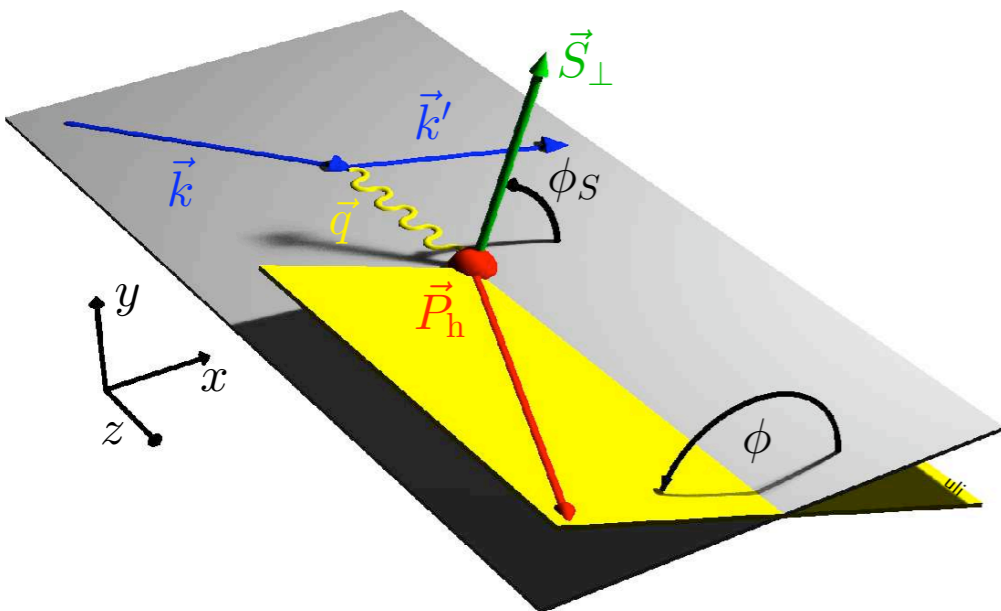
σ X Y
 Beam Target
 Polarization



1-Hadron Production ($ep \rightarrow ehX$)

$$\begin{aligned}
 d\sigma = & d\sigma_{UU}^0 + \boxed{\cos 2\phi d\sigma_{UU}^1} \leftarrow \text{Boer-Mulders-DF} \otimes \text{Collins-FF} \\
 & + S_L \left\{ \sin 2\phi d\sigma_{UL}^4 + \frac{1}{Q} \sin \phi d\sigma_{UL}^5 + \lambda_e \left[d\sigma_{LL}^6 + \frac{1}{Q} \cos \phi d\sigma_{LL}^7 \right] \right\} \\
 & + S_T \left\{ \boxed{\sin(\phi - \phi_S) d\sigma_{UT}^8} + \boxed{\sin(\phi + \phi_S) d\sigma_{UT}^9} + \sin(3\phi - \phi_S) \sigma_{UT}^{10} \right. \\
 & \quad \left. + \frac{1}{Q} (\sin 2\phi - \phi_S) d\sigma_{UT}^{11} + \sin \phi_S d\sigma_{UT}^{12} \right. \\
 & \quad \left. + \lambda_e \left[\cos(\phi - \phi_S) d\sigma_{LT}^{13} + \frac{1}{Q} (\cos \phi_S d\sigma_{LT}^{14} + \cos(2\phi - \phi_S) d\sigma_{LT}^{15}) \right] \right\}
 \end{aligned}$$

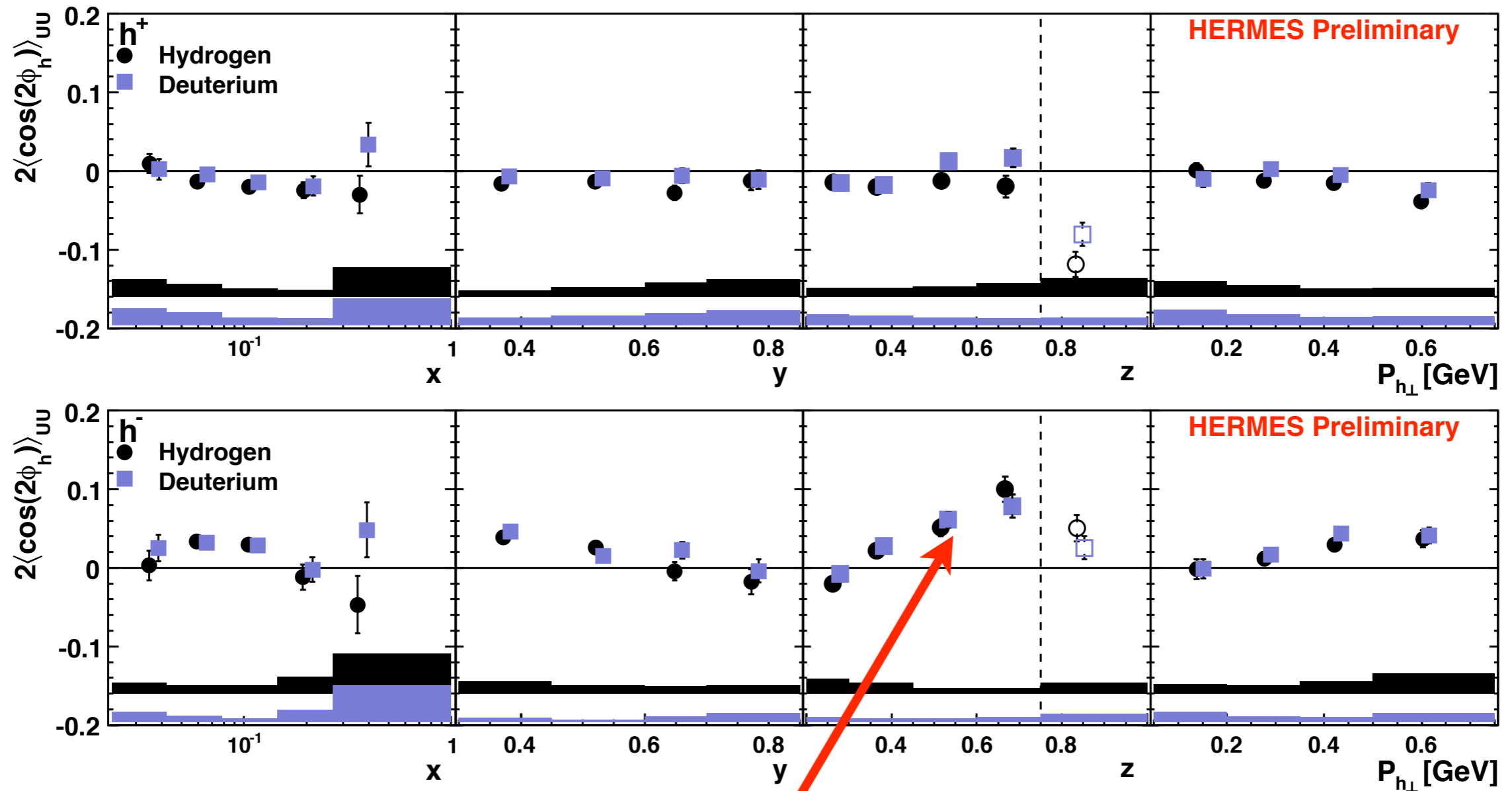
σ X Y
 Beam Target
 Polarization



Boer-Mulders Amplitudes

Extraction challenging: azimuthal moments also possible due to e.g. acceptance effects

➔ Fully differential analysis, unfolding in 5D (z, y, z, p_{hT}, ϕ)



Evidence of transversely polarized quarks in unpolarized nucleons!

Azimuthal Single-Spin Asymmetries

Measurement of cross-section asymmetries depending on the azimuthal angles ϕ and ϕ_S

$$A_{UT}(\phi, \phi_S, \dots) = \frac{1}{S_{\perp}} \frac{\sigma^{\uparrow} - \sigma^{\downarrow}}{\sigma^{\uparrow} + \sigma^{\downarrow}}$$

Collins Amplitude

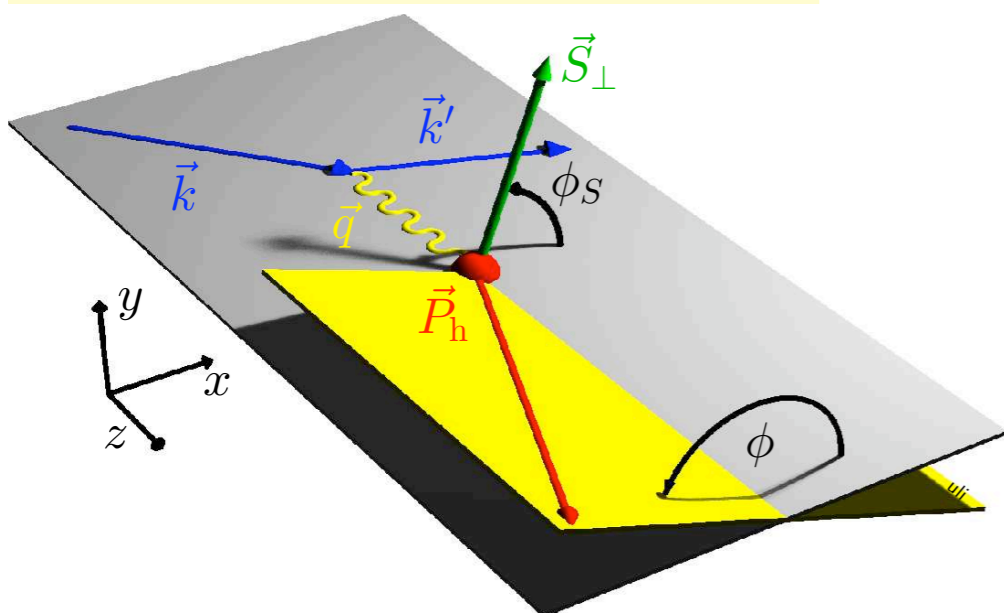
$$\sim \dots \sin(\phi + \phi_S) \frac{\sum_q e_q^2 \mathcal{I} \left[\dots \delta q(x, \vec{p}_T^2) \cdot H_1^{\perp q}(z, \vec{k}_T^2) \right]}{\sum_q e_q^2 q(x) \cdot D_1^q(z)}$$

Sivers Amplitude

$$+ \dots \sin(\phi - \phi_S) \frac{\sum_q e_q^2 \mathcal{I} \left[\dots f_{1T}^{\perp q}(x, \vec{p}_T^2) \cdot D_1^q(z, \vec{k}_T^2) \right]}{\sum_q e_q^2 q(x) \cdot D_1^q(z)}$$

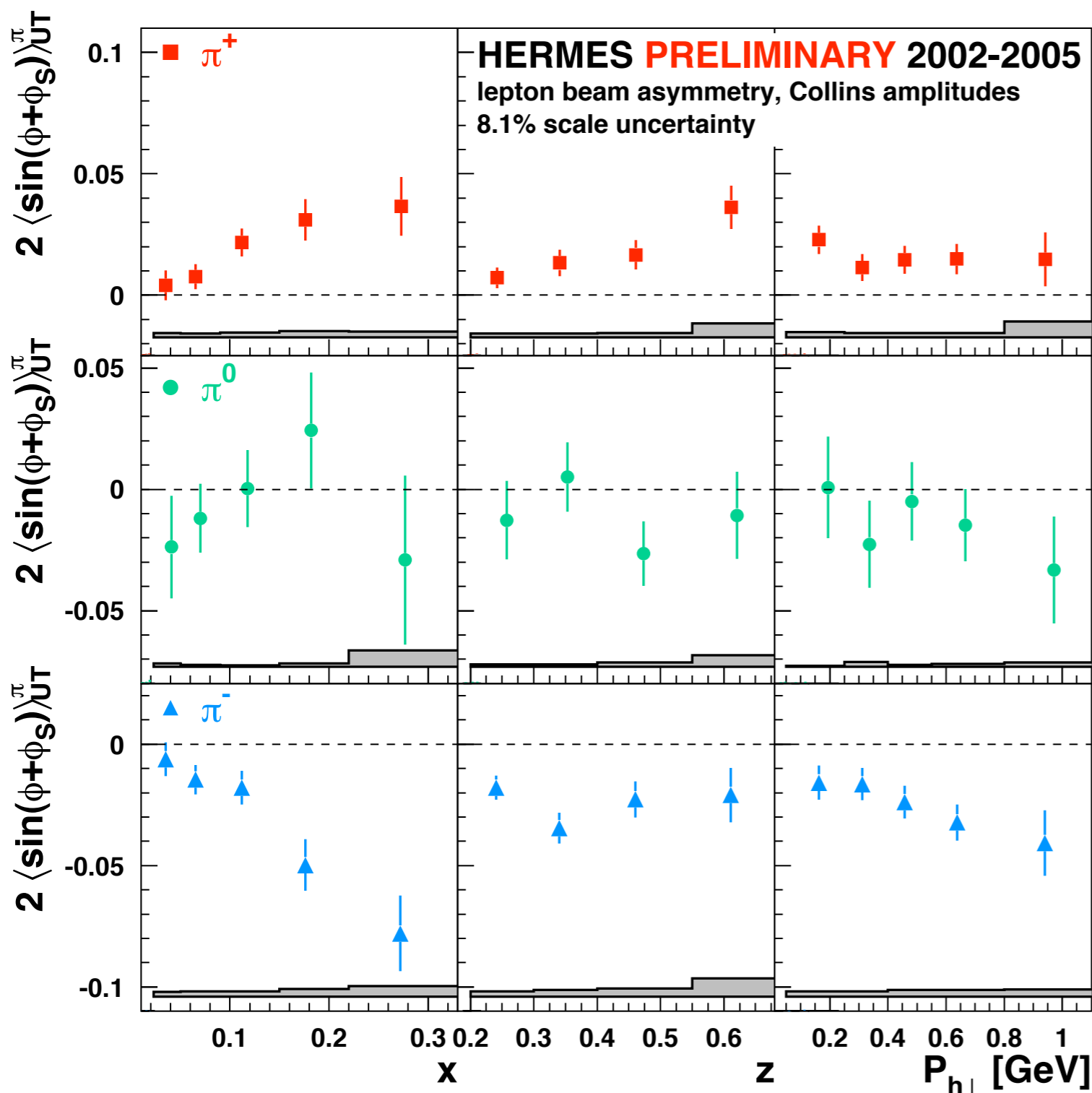
...

$\mathcal{I} [\dots]$ convolution integral over initial (\mathbf{p}_T) and final (\mathbf{k}_T) quark transverse momenta



Collins Amplitudes for Pions

$$A_C \propto \delta q \otimes H_1^\perp$$



- positive amplitudes for π^+
- large negative π^- amplitude

$$u \rightarrow \pi^+ \Rightarrow H_1^{\perp, \text{fav}}$$

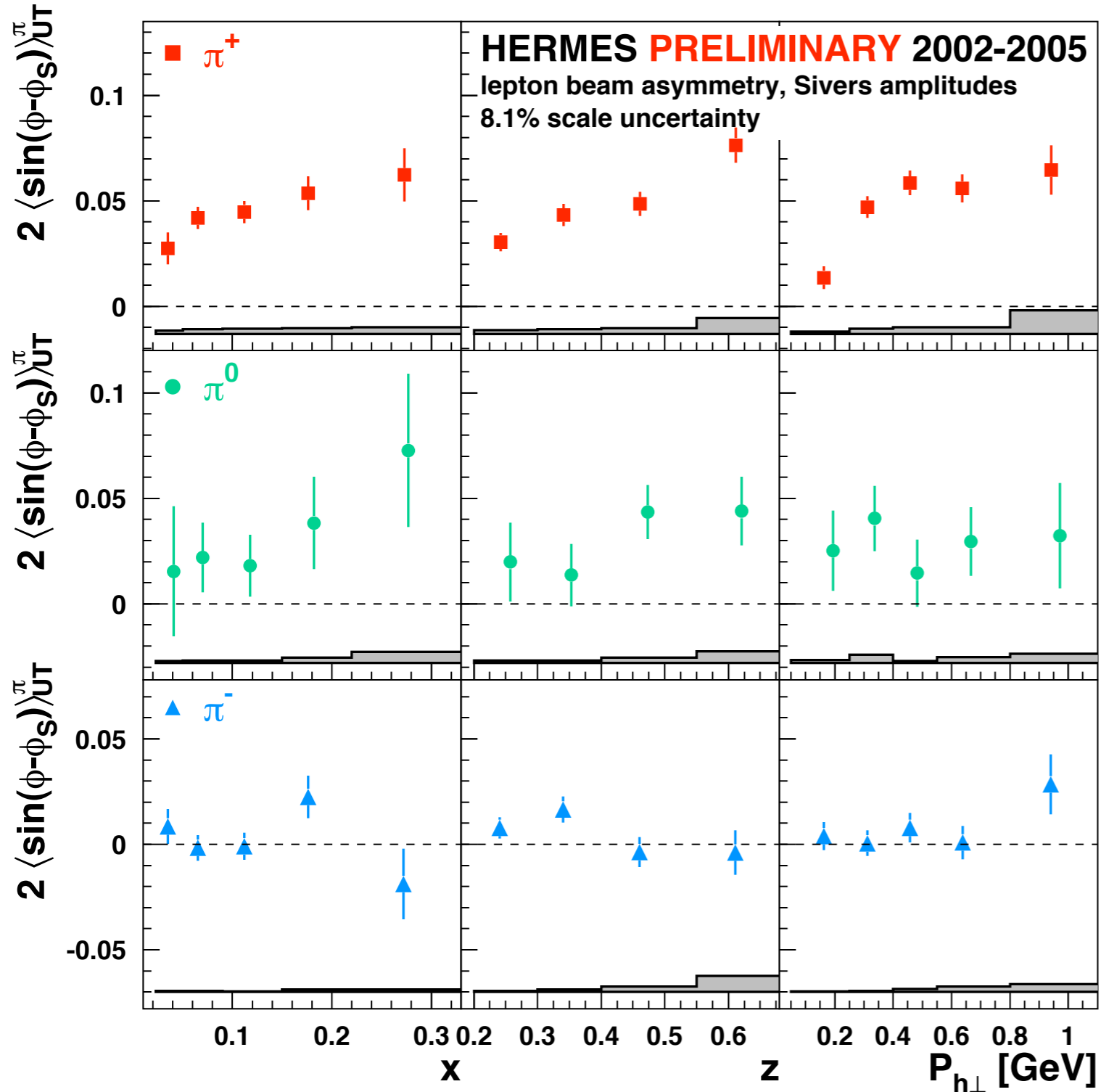
$$u \rightarrow \pi^- \Rightarrow H_1^{\perp, \text{unfav}}$$

$$\Rightarrow H_1^{\perp, \text{fav}} \approx -H_1^{\perp, \text{unfav}}$$

- isospin symmetry in π -fragmentation is fulfilled
- information from another process on Collins FF (BELLE) allows extraction of δq (eg. Anselmino et. al. Phys.Rev.D75:054032,2007)

Sivers Amplitudes for Pions

$$A_S \propto f_{1T}^\perp \otimes D_1^q$$

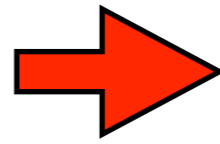


- significantly positive for π^+
- implies non-zero orbital angular momentum of quarks
- consistent with zero for π^-
- isospin symmetry of π -mesons fulfilled

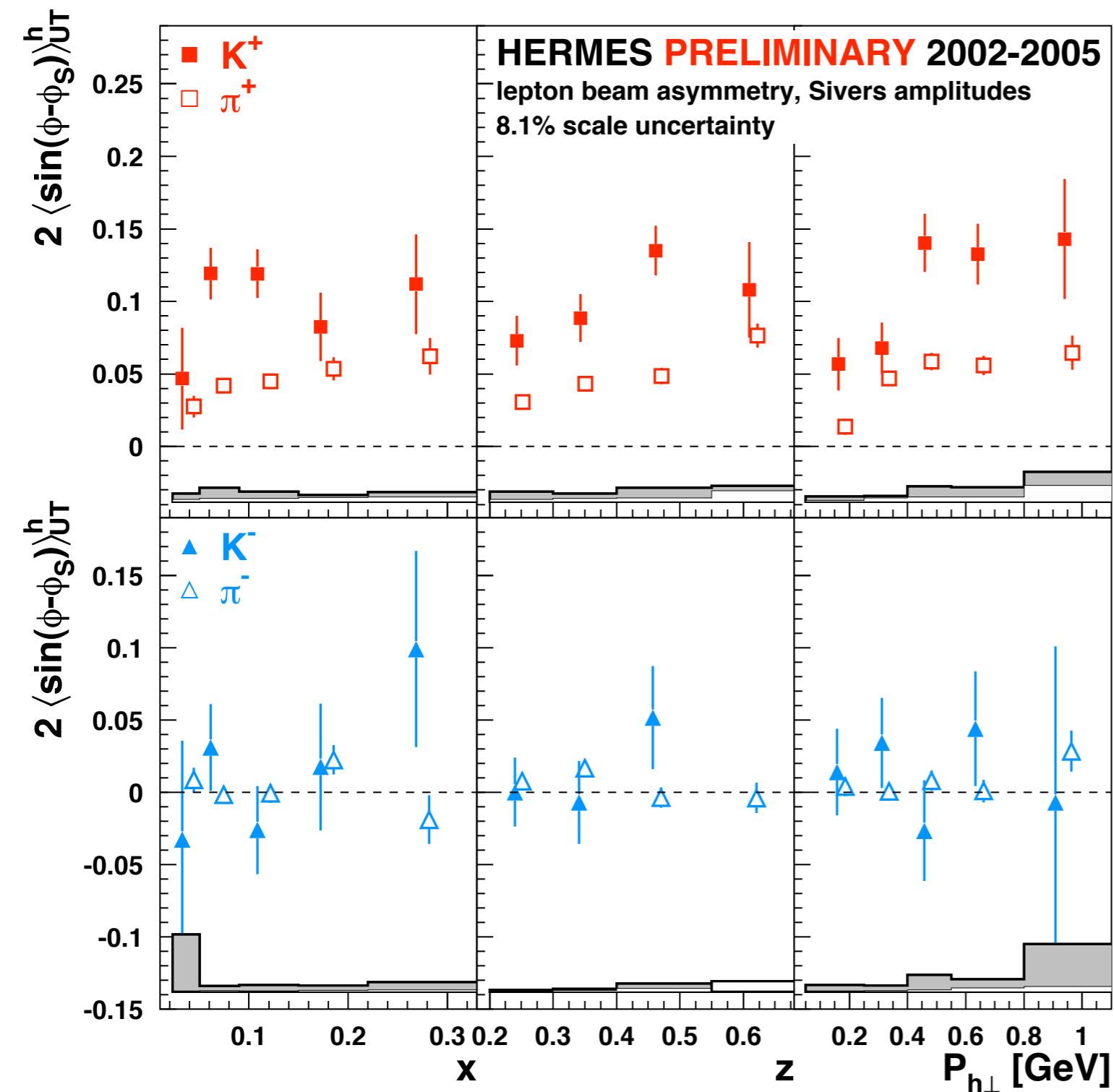
Sivers Amplitudes for Kaons

$$A_S \propto f_{1T}^\perp \otimes D_1^q$$

- significantly positive for K^+
- implies non-zero orbital angular momentum of quarks
- consistent with zero for K^-
- K^+ amplitude larger than π^+ amplitude

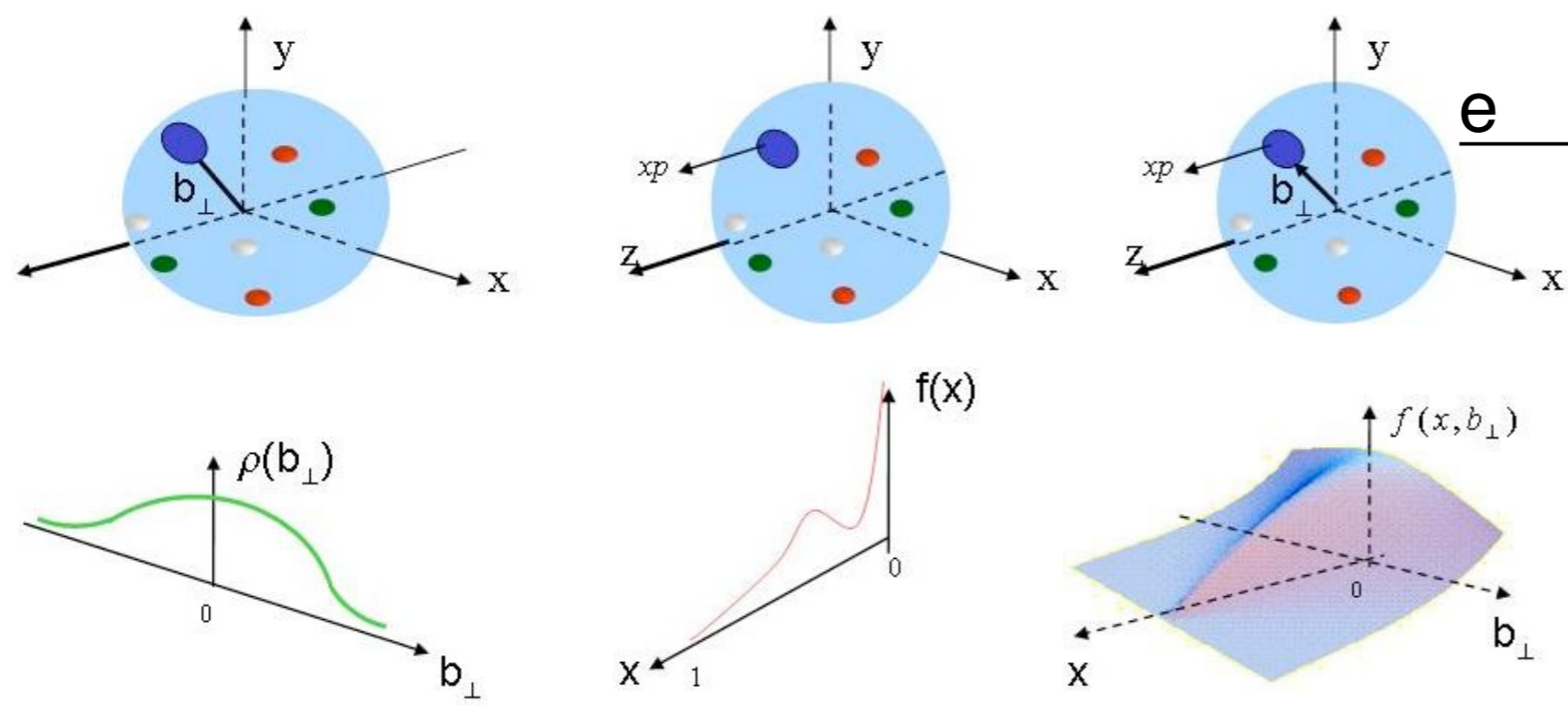

 sea quark contribution to Sivers mechanism may be important

$$\pi^+ = |u\bar{d}\rangle \quad K^+ = |u\bar{s}\rangle$$



Accessing Generalized Parton Distribution Functions (GPDs) via Deeply Virtual Compton Scattering (DVCS)

Probing GPDs in Exclusive Reactions



Form factors

Parton Distribution Functions

GPDs

Transverse distribution of quarks in space coordinates

Quark longitudinal momentum fraction distribution in the nucleon

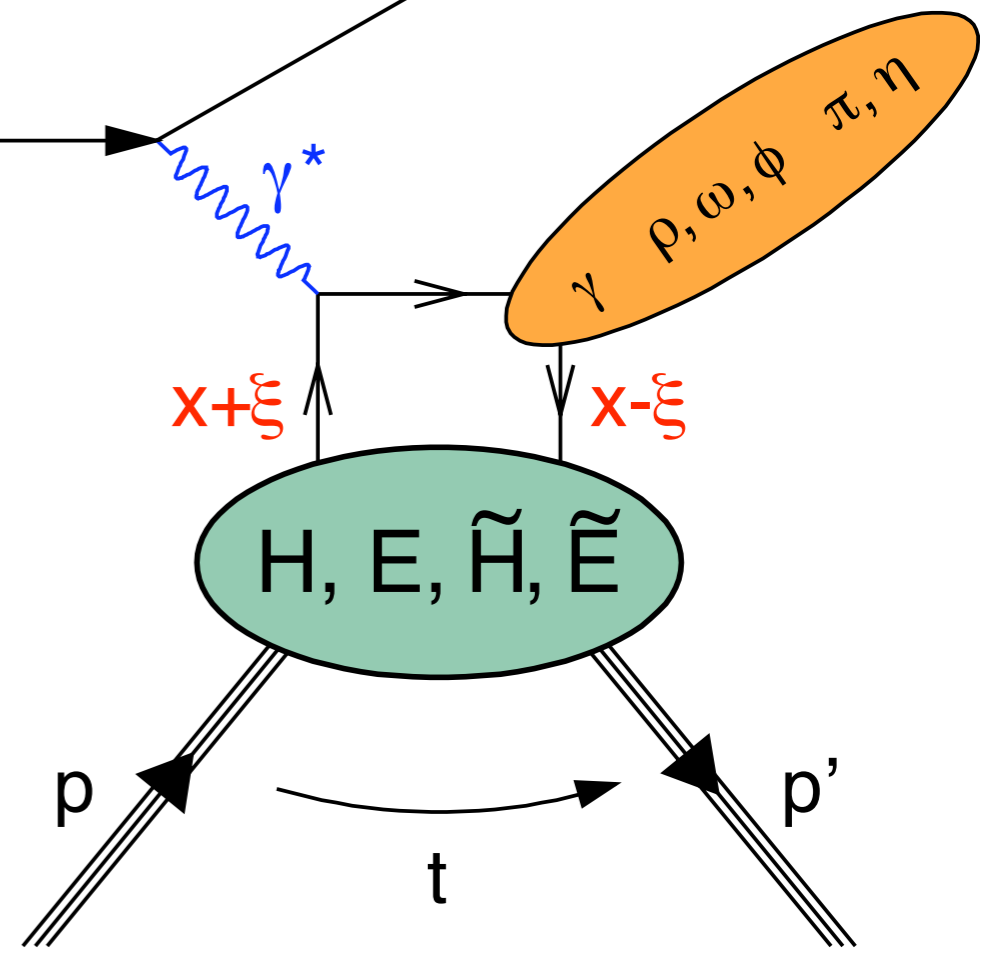
Correlation between transverse position and longitudinal momentum fraction of quark in the nucleon

$$\int dx H^q(x, \xi, t) = F_1^q(t)$$

$$\int dx E^q(x, \xi, t) = F_2^q(t)$$

$$H^q(x, \xi = 0, t = 0) = q(x)$$

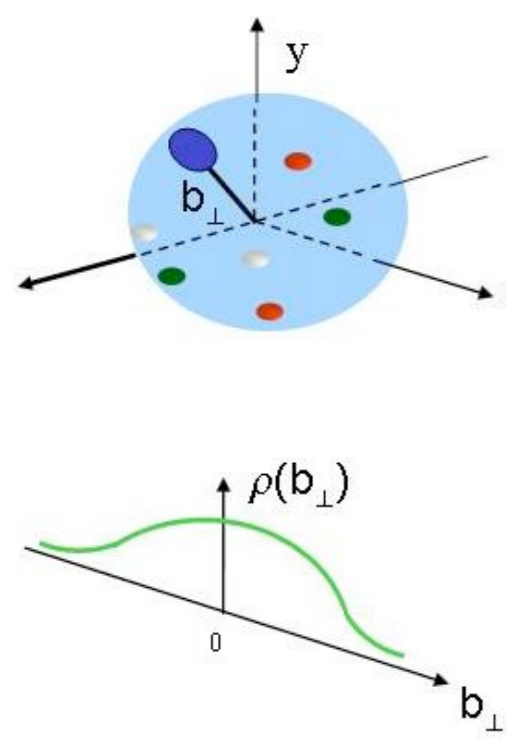
$$\tilde{H}^q(x, \xi = 0, t = 0) = \Delta q(x)$$



	unpolarized	polarized
no nucleon hel. flip	H	\tilde{H}
nucleon hel. flip	E	\tilde{E}

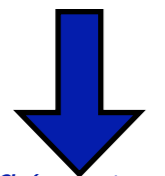
(+ 4 more chiral-odd functions)

Probing GPDs in Exclusive Reactions



Form factors

Transverse distribution of quarks in space coordinates



$$\int dx H^q(x, \xi, t) = F_1^q(t)$$

$$\int dx E^q(x, \xi, t) = F_2^q(t)$$



momentum fraction distribution in the nucleon



$$H^q(x, \xi = 0, t = 0) = q(x)$$

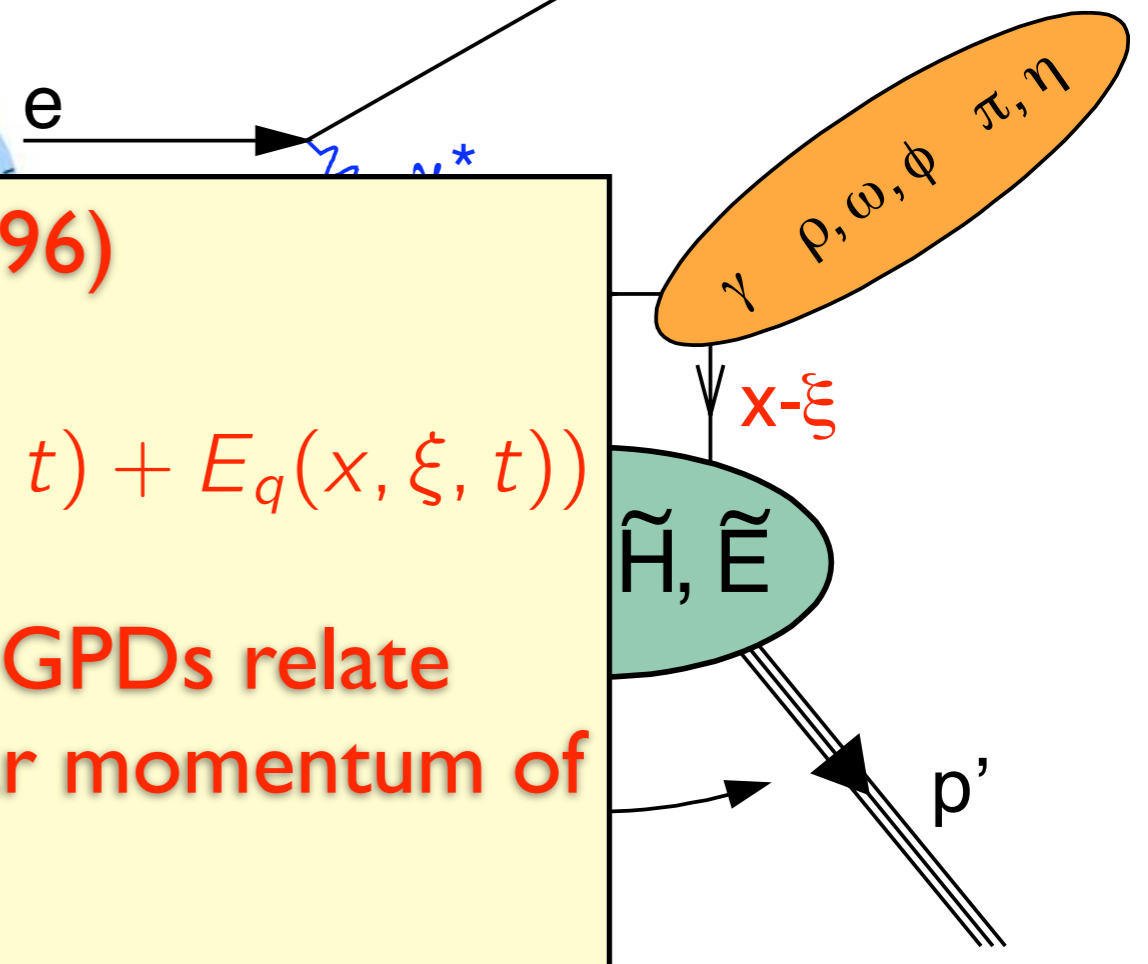
$$\tilde{H}^q(x, \xi = 0, t = 0) = \Delta q(x)$$

longitudinal momentum fraction of quark in the nucleon

Ji relation (1996)

$$J_q = \lim_{t \rightarrow 0} \int_{-1}^1 dx x (H_q(x, \xi, t) + E_q(x, \xi, t))$$

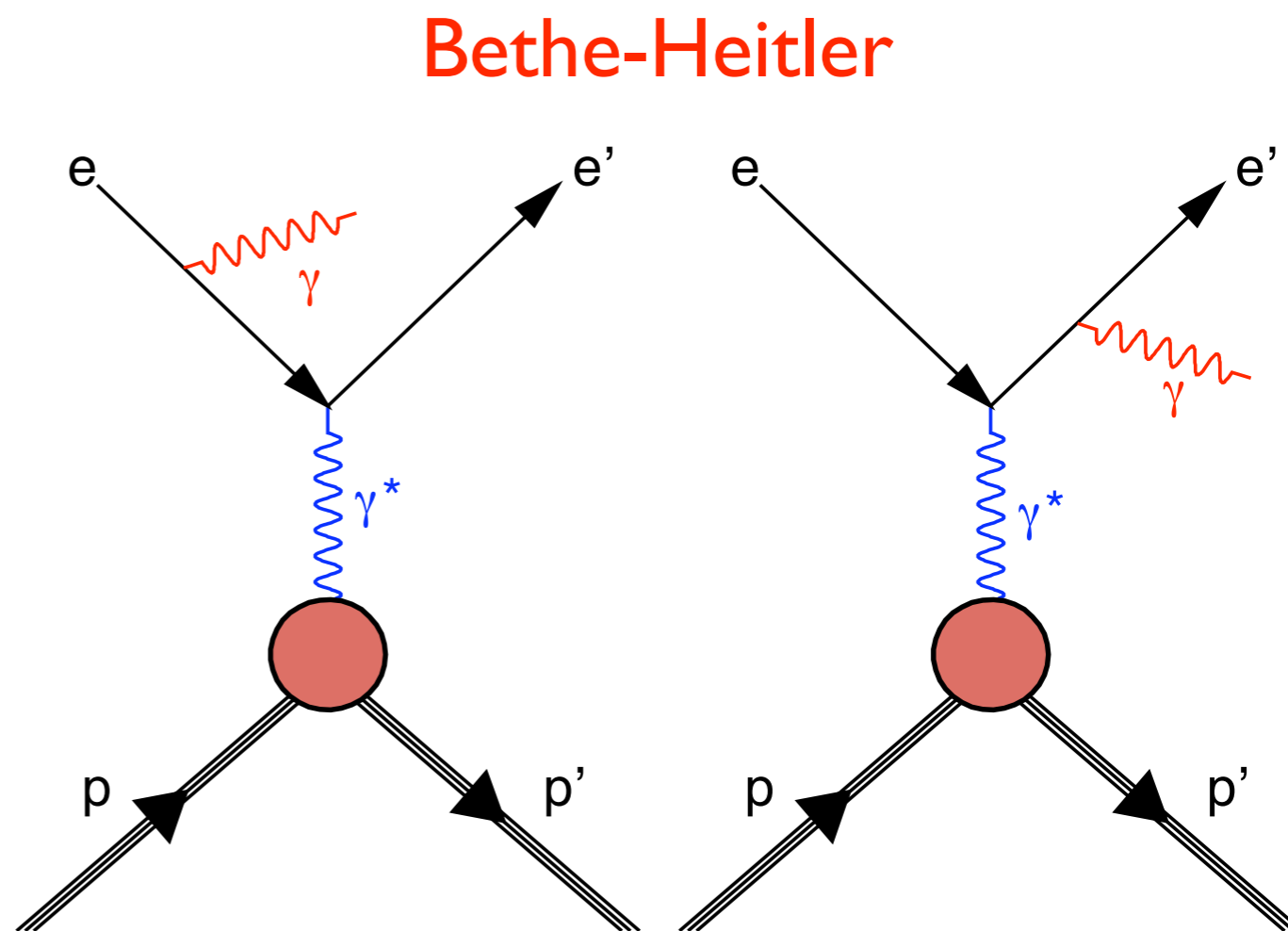
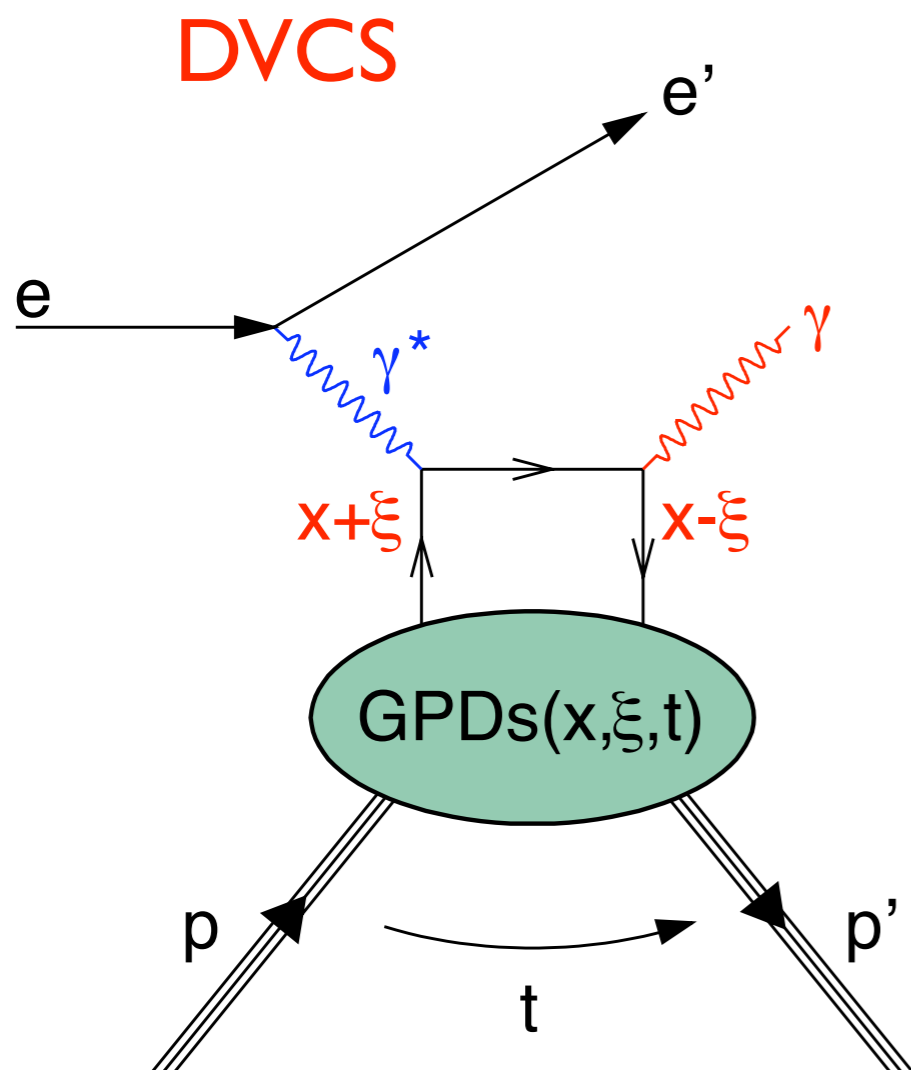
→ Moments of certain GPDs relate directly to the total angular momentum of quarks



	unpolarized	polarized
no nucleon hel. flip	H	\tilde{H}
nucleon hel. flip	E	\tilde{E}

(+ 4 more chiral-odd functions)

DVCS/Bethe-Heitler Interference

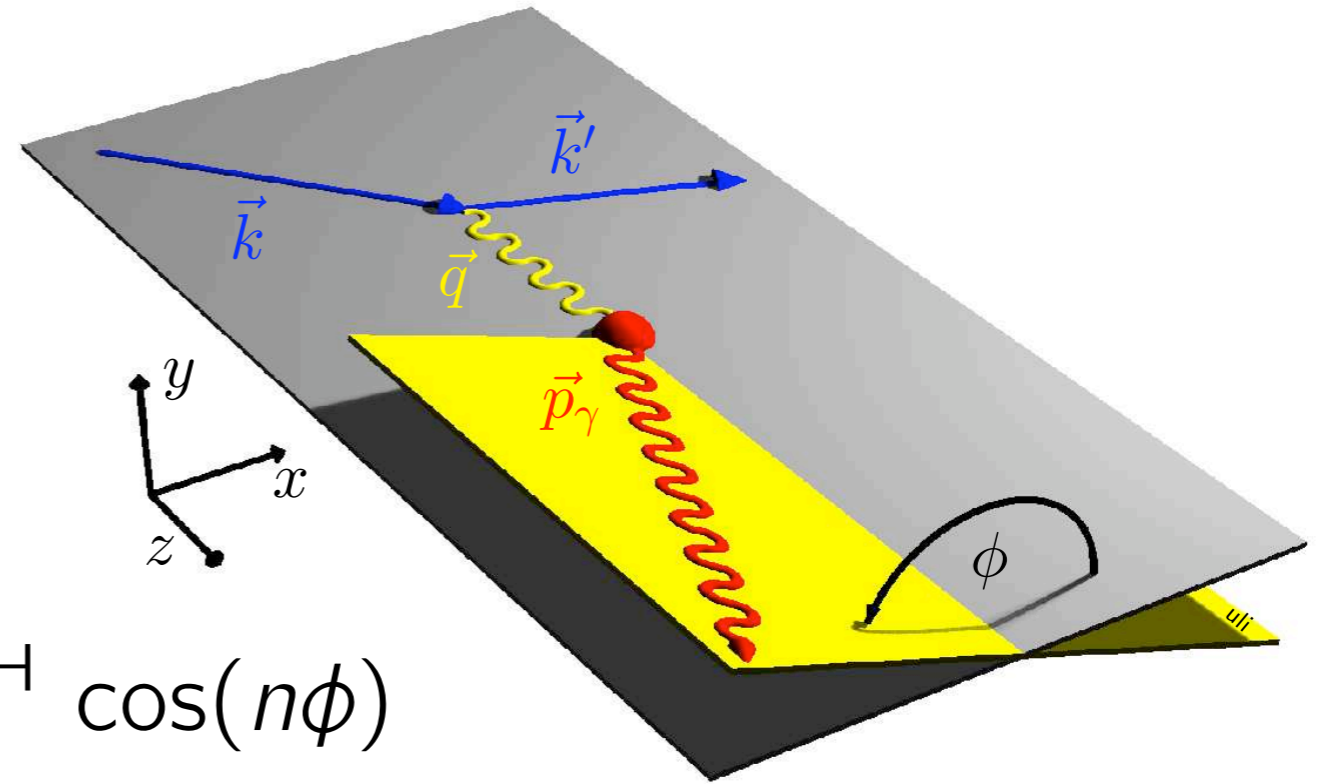


$$\frac{d^4\sigma}{dQ^2 dx_B dt d\phi} = \frac{y^2}{32(2\pi)^4 \sqrt{1 + \frac{4M^2 x_B^2}{Q^2}}} (|\mathcal{T}_{\text{DVCS}}|^2 + |\mathcal{T}_{\text{BH}}|^2 + \mathcal{I})$$

Azimuthal Dependences in DVCS

Fourier expansion for Φ :

- beam polarization P_B
- beam charge C_B
- unpolarized target



$$|\mathcal{T}_{\text{BH}}|^2 = \frac{K_{\text{BH}}}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \sum_{n=0}^2 c_n^{\text{BH}} \cos(n\phi)$$

$$|\mathcal{T}_{\text{DVCS}}|^2 = K_{\text{DVCS}} \left[\sum_{n=0}^2 c_n^{\text{DVCS}} \cos(n\phi) + P_B \sum_{n=1}^1 s_n^{\text{DVCS}} \sin(n\phi) \right]$$

$$\mathcal{I} = \frac{C_B K_{\mathcal{I}}}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \left[\sum_{n=0}^3 c_n^{\mathcal{I}} \cos(n\phi) + P_B \sum_{n=1}^2 s_n^{\mathcal{I}} \sin(n\phi) \right]$$

Azimuthal Asymmetries in DVCS

Cross section:

$$\sigma(\phi, \phi_S, P_B, C_B, P_T) = \sigma_{UU}(\phi) \cdot \left[1 + P_B \mathcal{A}_{LU}^{\text{DVCS}}(\phi) + C_B P_B \mathcal{A}_{LU}^{\mathcal{I}}(\phi) + C_B \mathcal{A}_C(\phi) \right. \\ \left. + P_T \mathcal{A}_{UT}^{\text{DVCS}}(\phi, \phi_S) + C_B P_T \mathcal{A}_{UT}^{\mathcal{I}}(\phi, \phi_S) \right]$$

Azimuthal asymmetries:

- Beam-charge asymmetry $\mathcal{A}_C(\Phi)$:

$$d\sigma(e^+, \phi) - d\sigma(e^-, \phi) \propto \text{Re}[F_1 \mathcal{H}] \cdot \cos \phi$$

- Beam-helicity asymmetry $\mathcal{A}_{LU}^{\mathcal{I}}(\Phi)$:

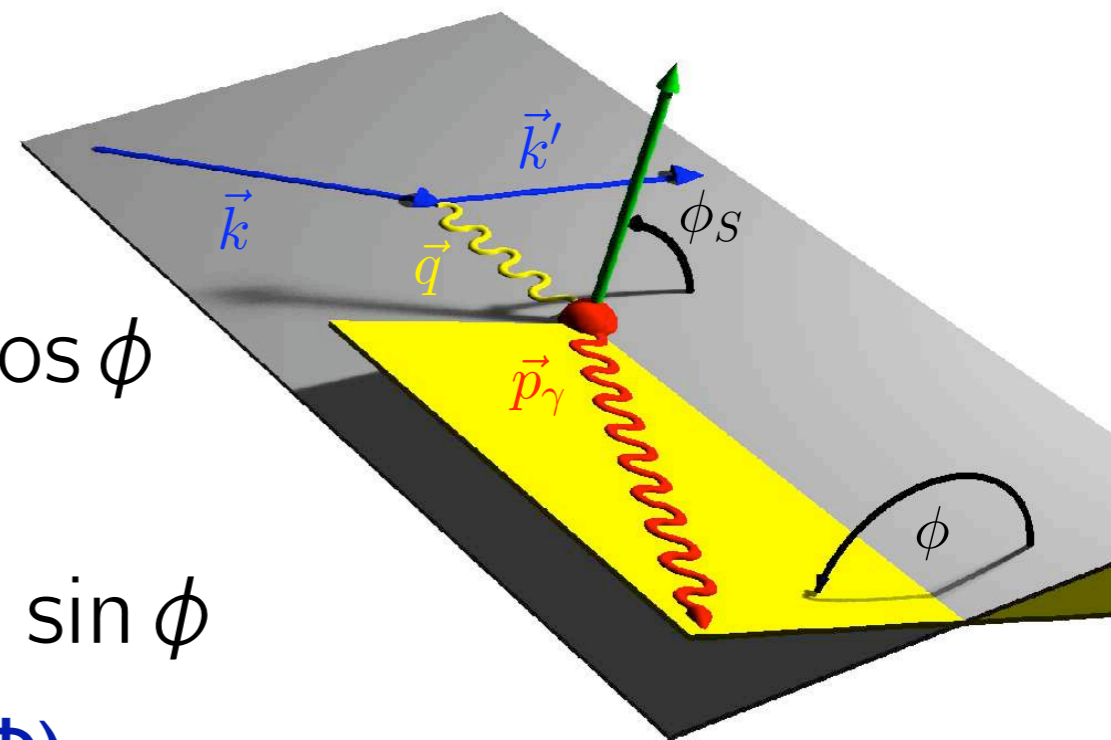
$$d\sigma(e^{\rightarrow}, \phi) - d\sigma(e^{\leftarrow}, \phi) \propto \text{Im}[F_1 \mathcal{H}] \cdot \sin \phi$$

- Transverse target-spin asymmetry $\mathcal{A}_{UT}^{\mathcal{I}}(\Phi)$:

$$d\sigma(\phi, \phi_S) - d\sigma(\phi, \phi_S + \pi) \propto \text{Im}[F_2 \mathcal{H} - F_1 \mathcal{E}] \cdot \sin(\phi - \phi_S) \cos \phi \\ + \text{Im}[F_2 \tilde{\mathcal{H}} - F_1 \xi \tilde{\mathcal{E}}] \cdot \cos(\phi - \phi_S) \sin \phi$$

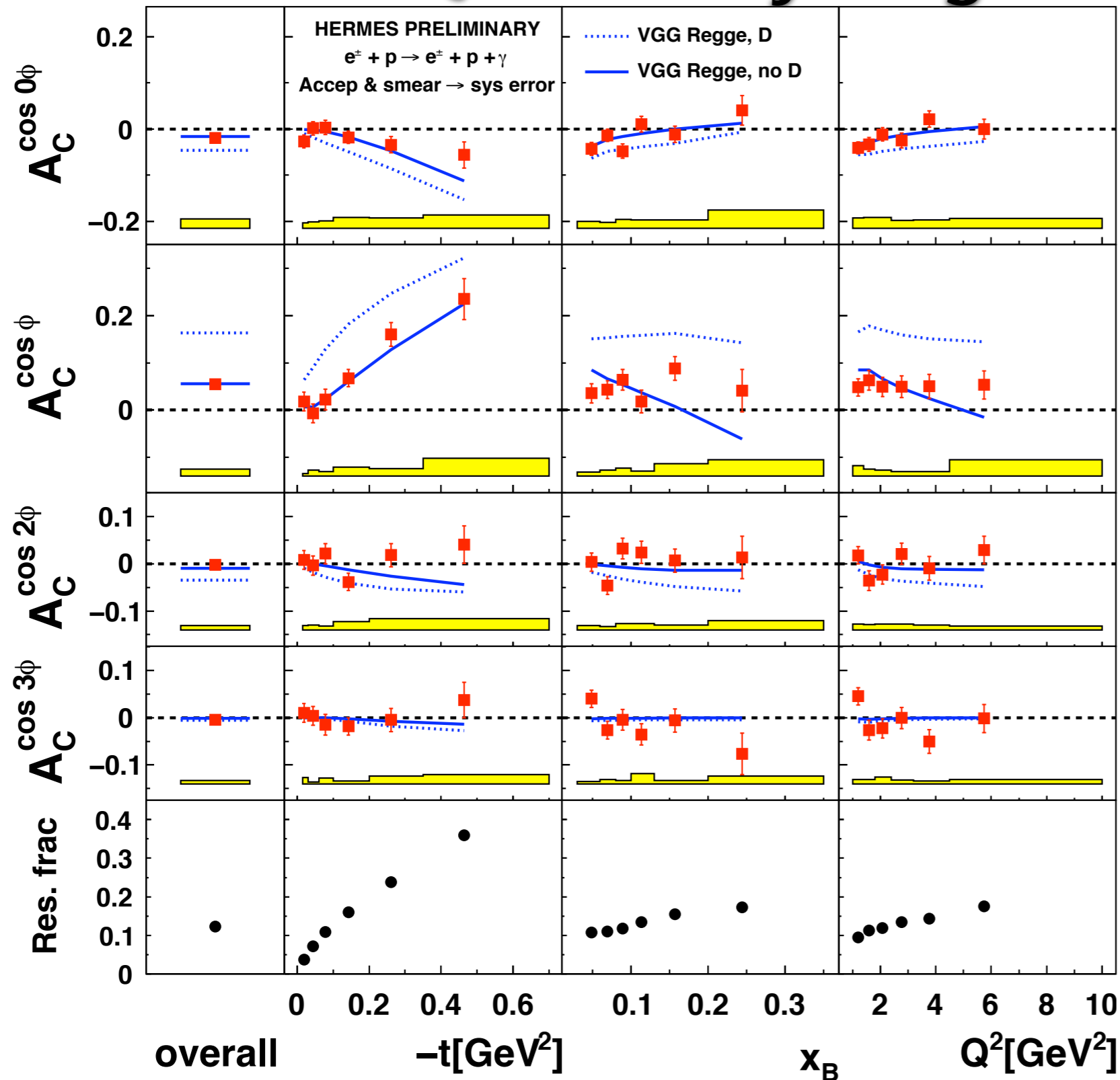
(F_1, F_2 are the Dirac and Pauli form factors)

($\mathcal{H}, \mathcal{E} \dots$ Compton form factors involving GPDs H, E, \dots)



A_C on a hydrogen target

All data
1996-2005



constant term

$$\propto -A_C^{\cos \phi}$$

$$\propto \text{Re}[F_1 \mathcal{H}]$$

[higher twist]

[gluon leading twist]

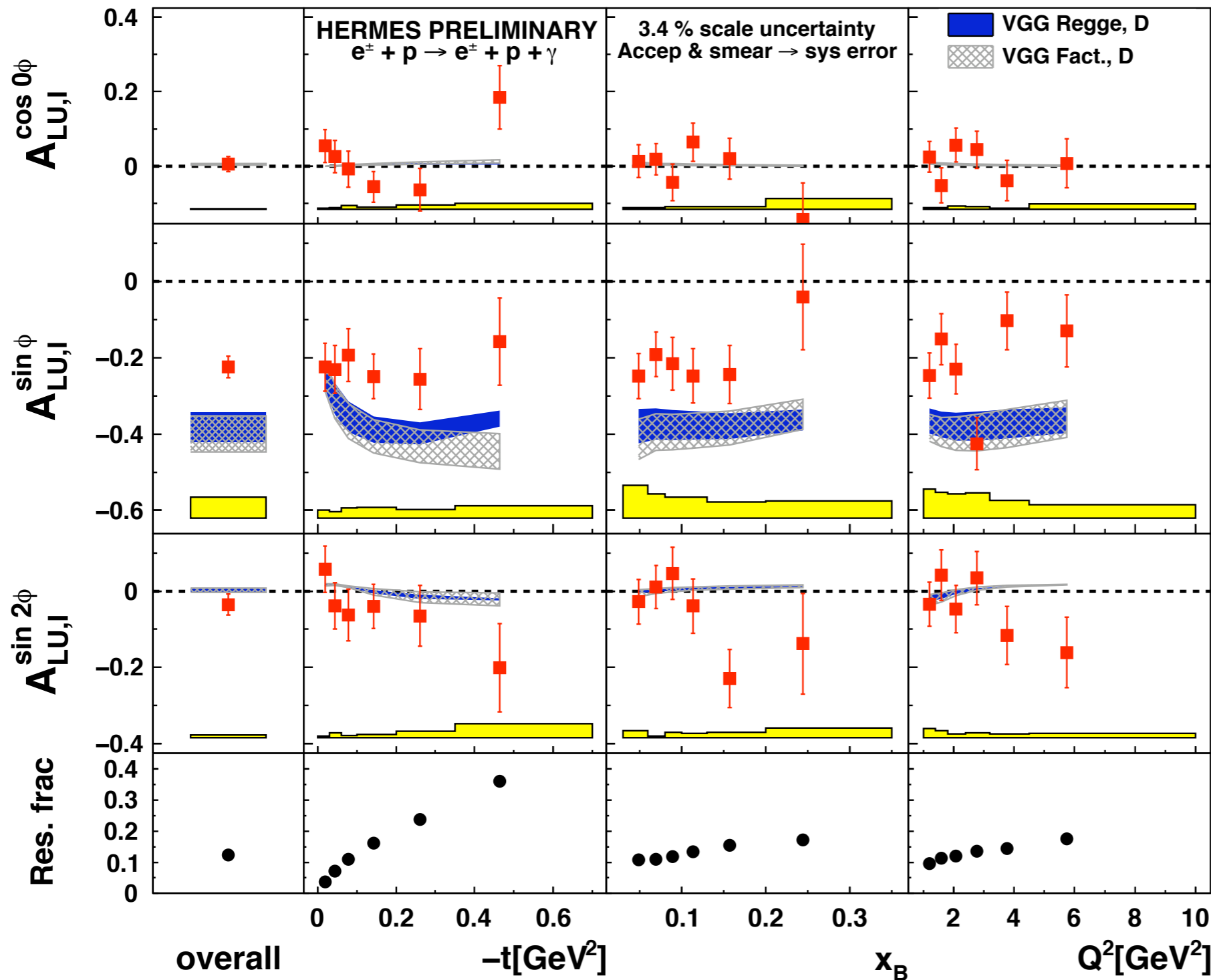
Resonant fraction:

$$ep \rightarrow e\Delta^+ \gamma$$

GPD model: VGG Phys. Rev. D60 (1999) 094017 & Prog. Nucl. Phys. 47 (2001) 401

A_{LU}^I on a hydrogen target

All data
1996-2005



$$\propto \text{Im}[F_1 \mathcal{H}]$$

[higher twist]

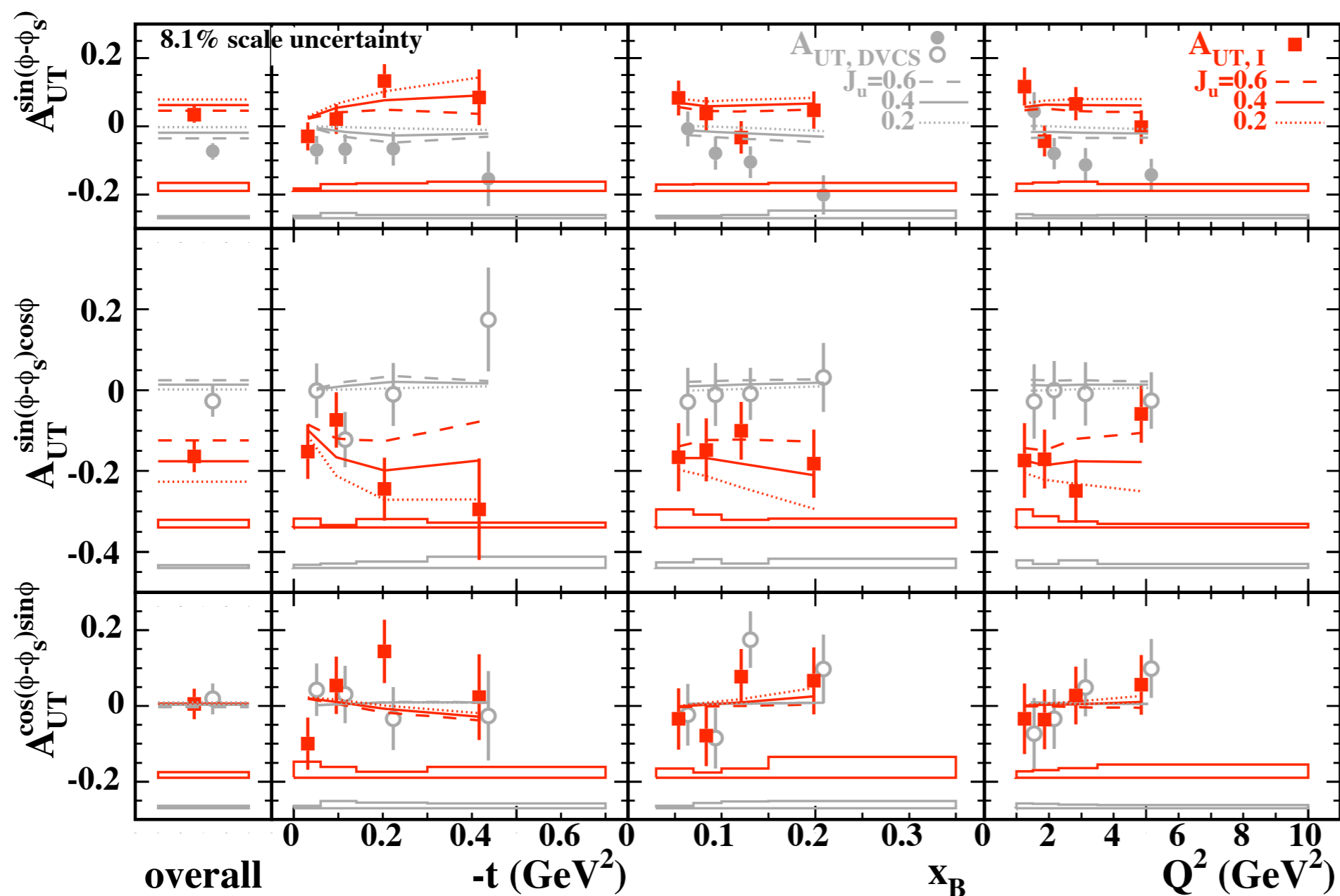
Resonant fraction:

$$ep \rightarrow e\Delta^+ \gamma$$

GPD model: VGG Phys. Rev. D60 (1999) 094017 & Prog. Nucl. Phys. 47 (2001) 401

A_{UT}^I on a hydrogen target

JHEP06
(2008) 066



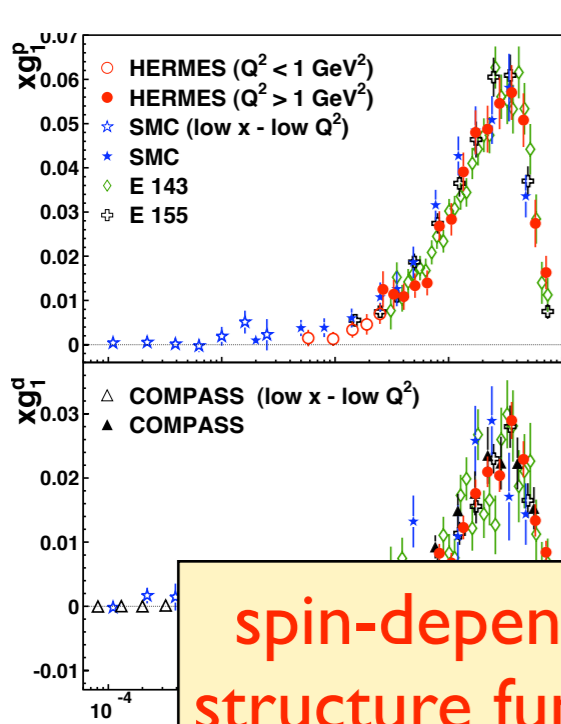
$$\propto -A_{UT}^{\sin(\phi-\phi_S)} \cos \phi$$

- Substantial magnitude
- Little kin. dependence

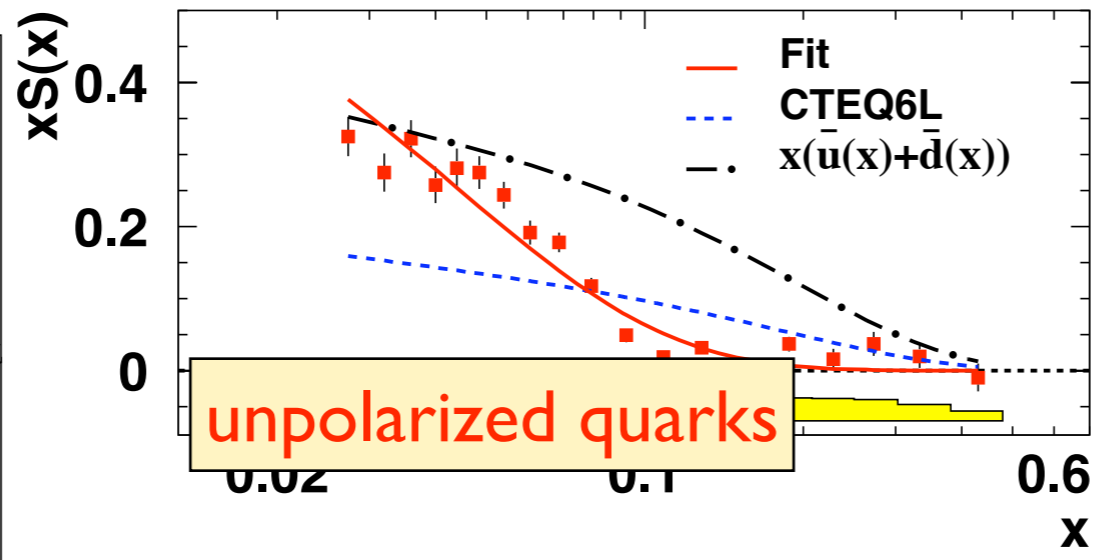
$$\propto \text{Im}[F_2 \mathcal{H} - F_1 \mathcal{E}]$$

$$\propto \text{Im}[F_2 \tilde{\mathcal{H}} - F_1 \xi \tilde{\mathcal{E}}]$$

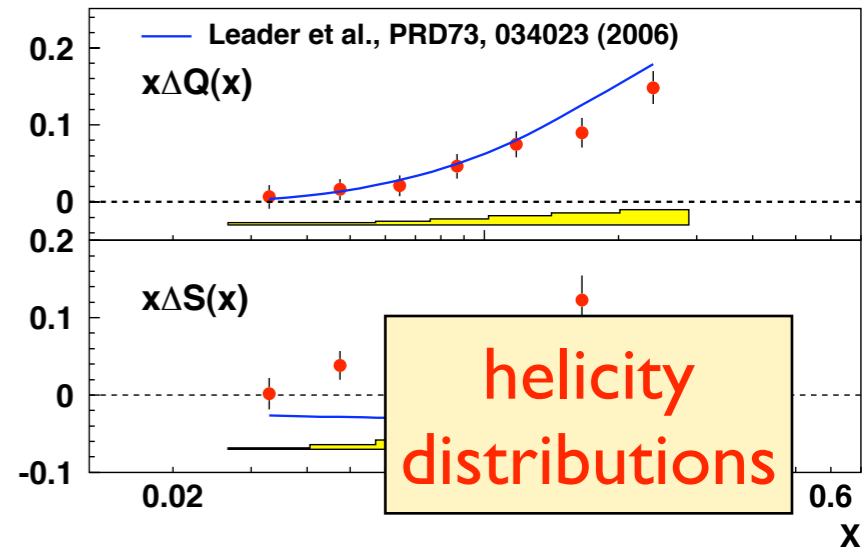
GPD model: VGG Phys. Rev. D60 (1999) 094017 & Prog. Nucl. Phys. 47 (2001) 401



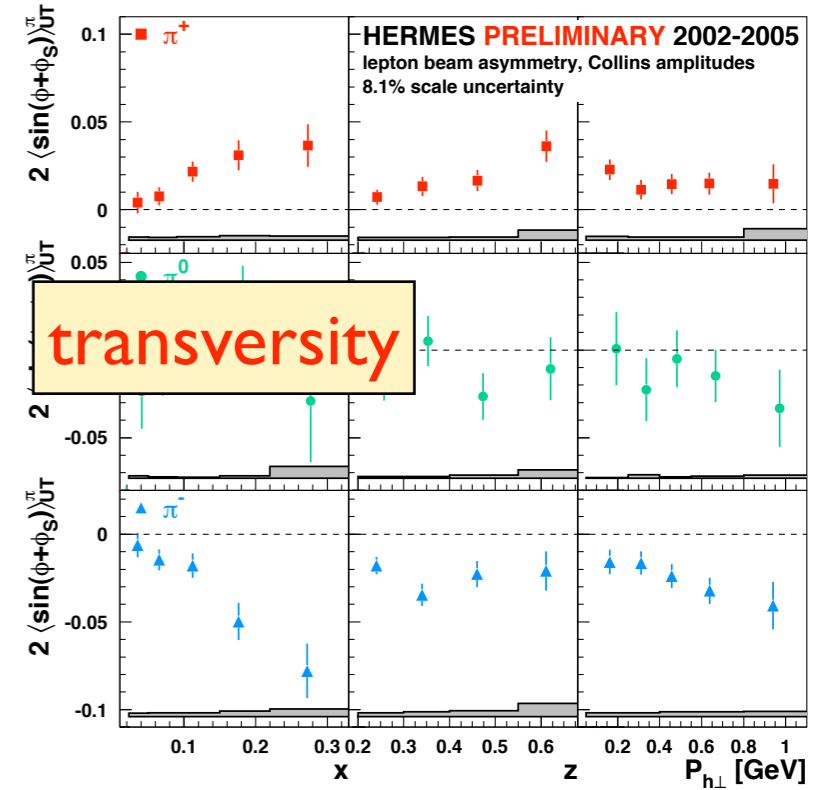
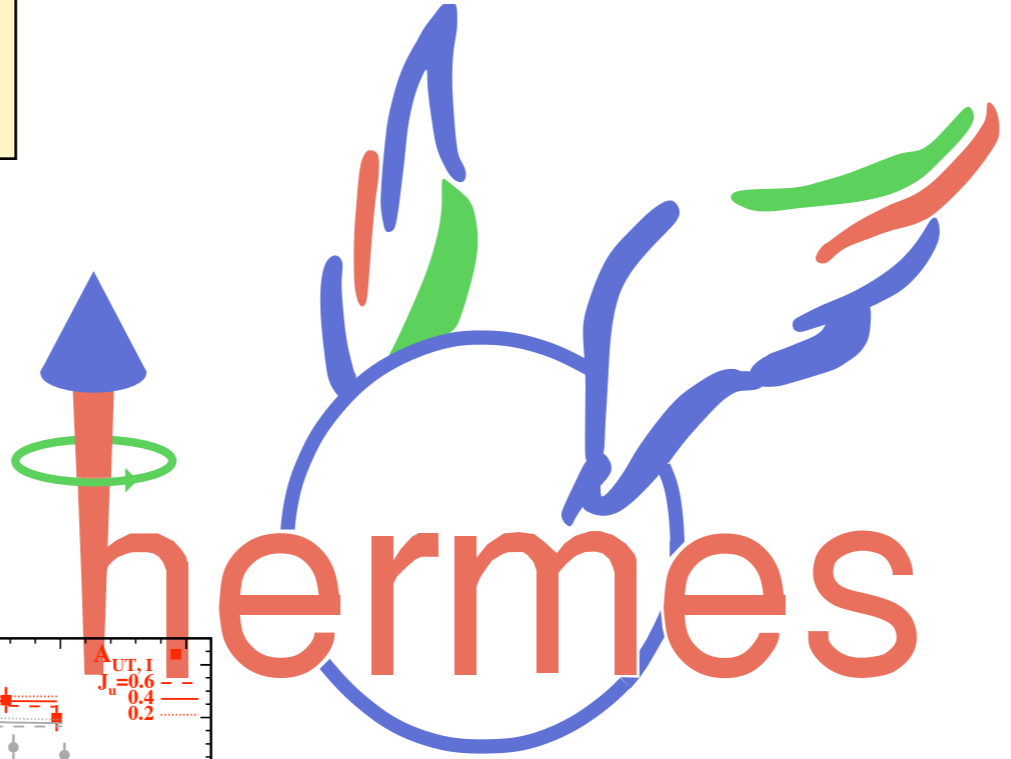
spin-dependent structure function



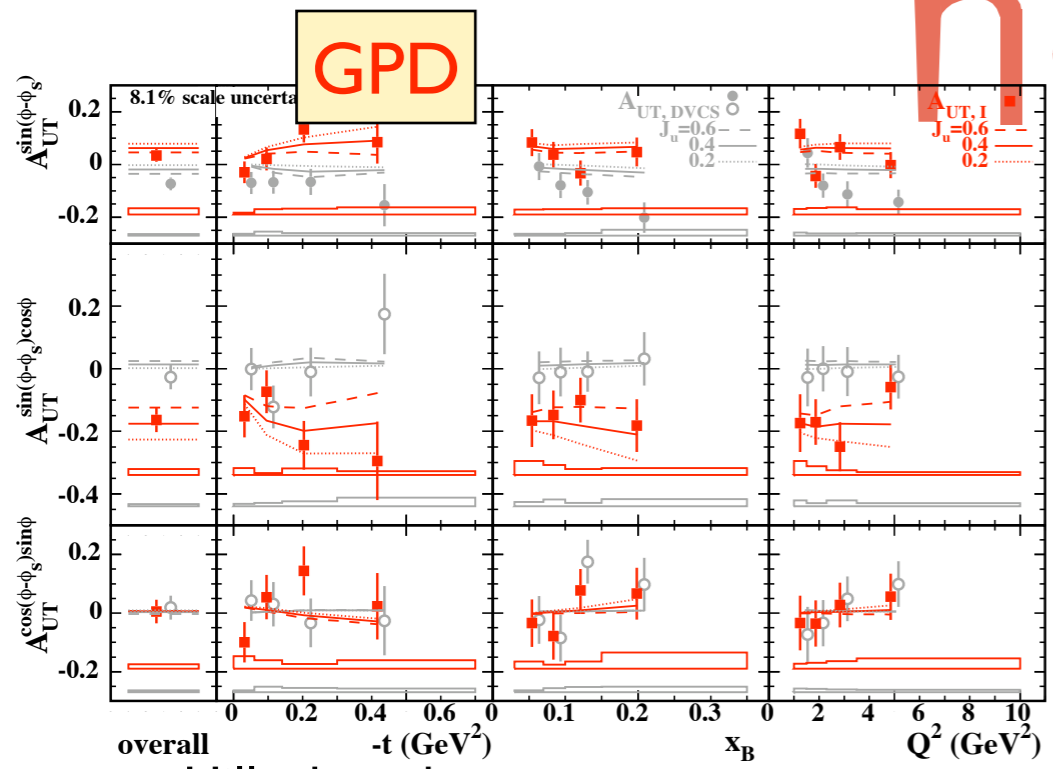
unpolarized quarks



helicity distributions

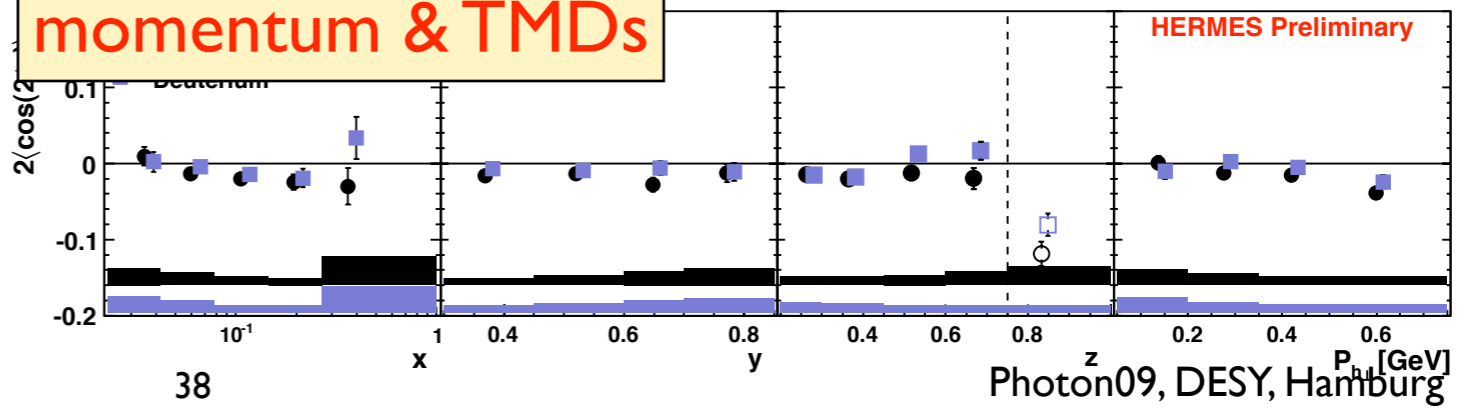


transversity



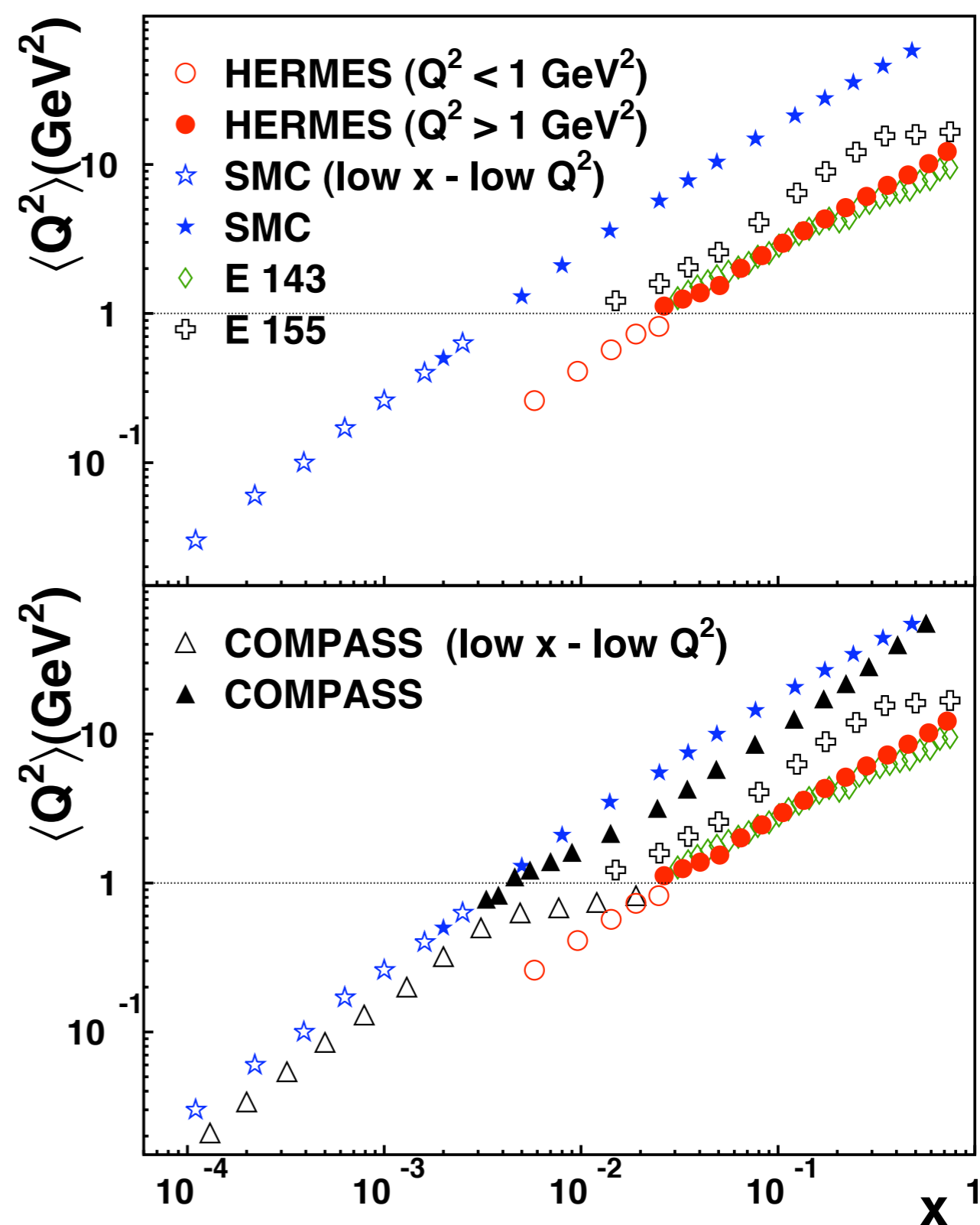
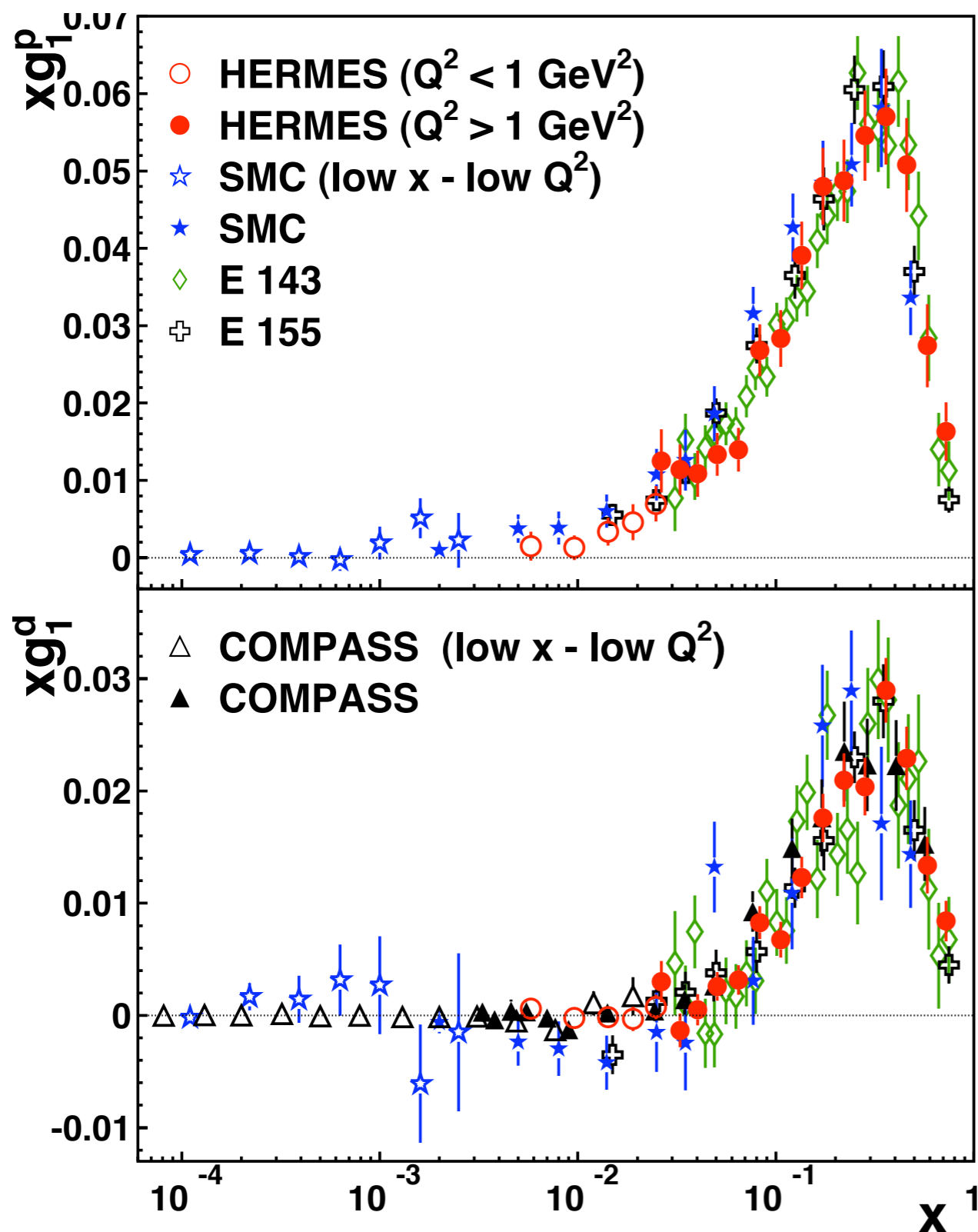
GPD

orbital angular momentum & TMDs

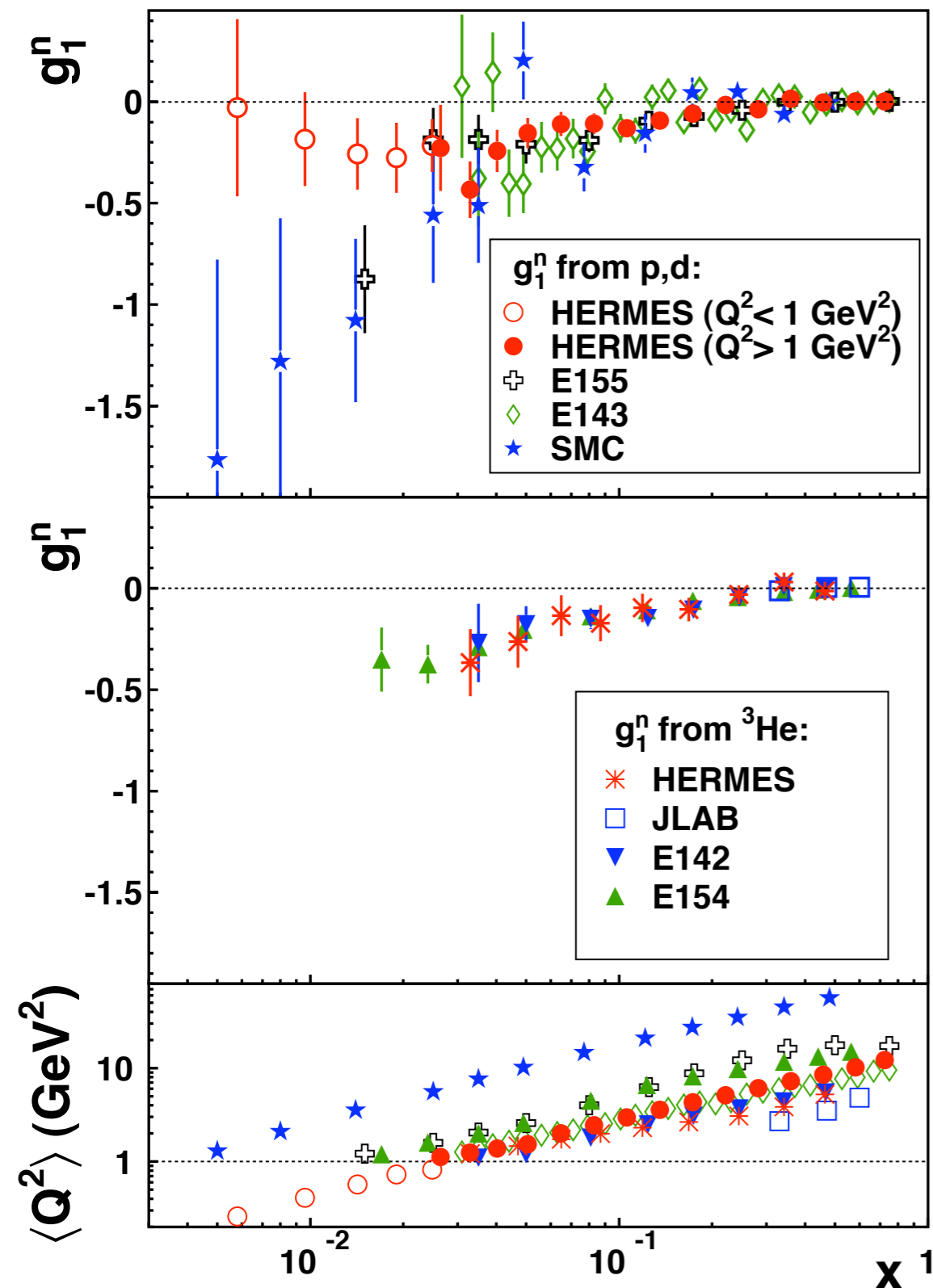


Backup

g_1 : Results for p and d



g_1 : Neutron results



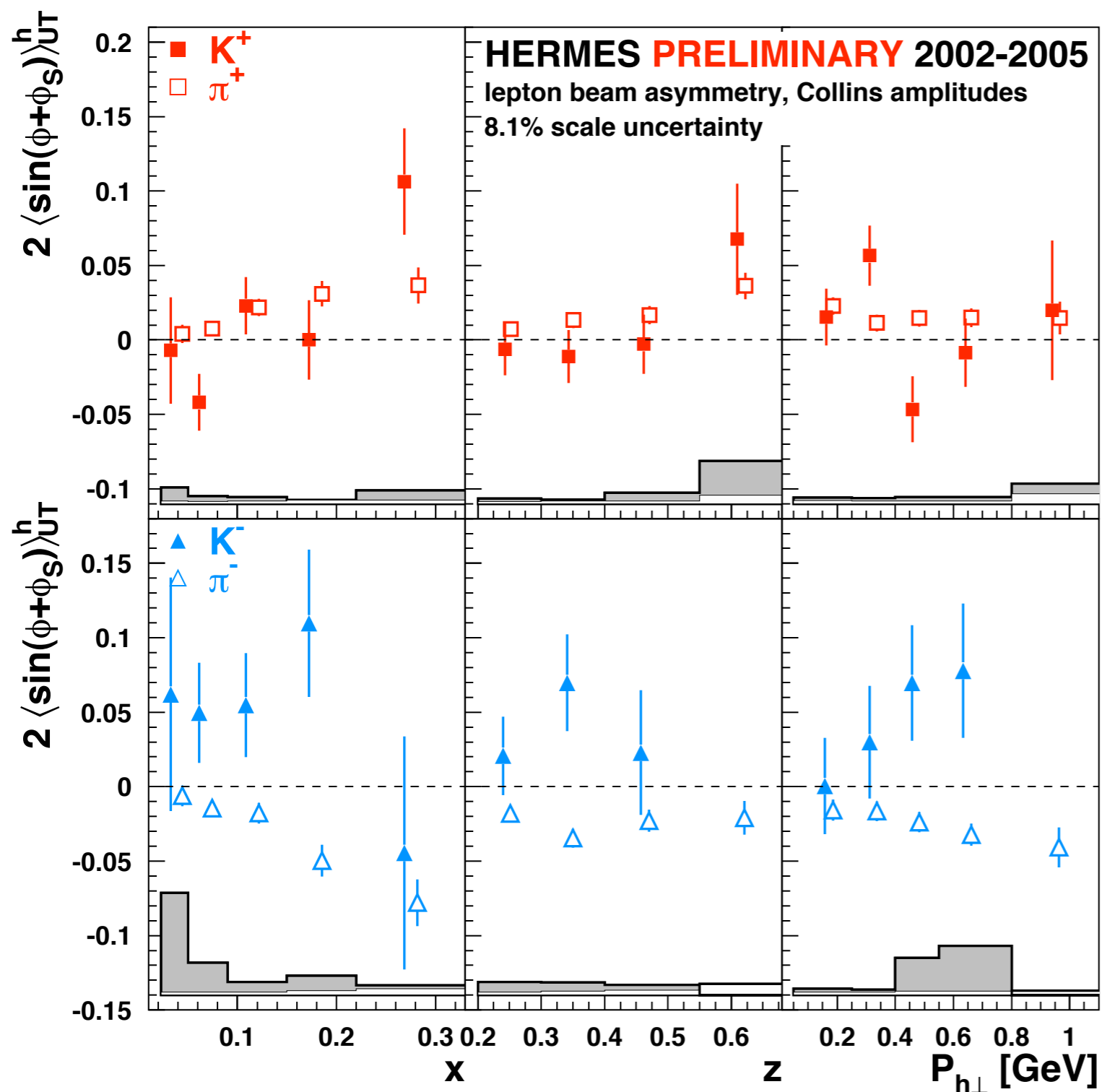
$$g_1^n = \frac{2}{1 - \frac{3}{2}\omega_D} \cdot g_1^d - g_1^p$$

$$\omega_D = 0.05 \pm 0.01$$

- g_1^n negative everywhere except at very high x
- Low- Q^2 data tends to zero at low x
 - ▶ Contrary to SMC data at higher Q^2

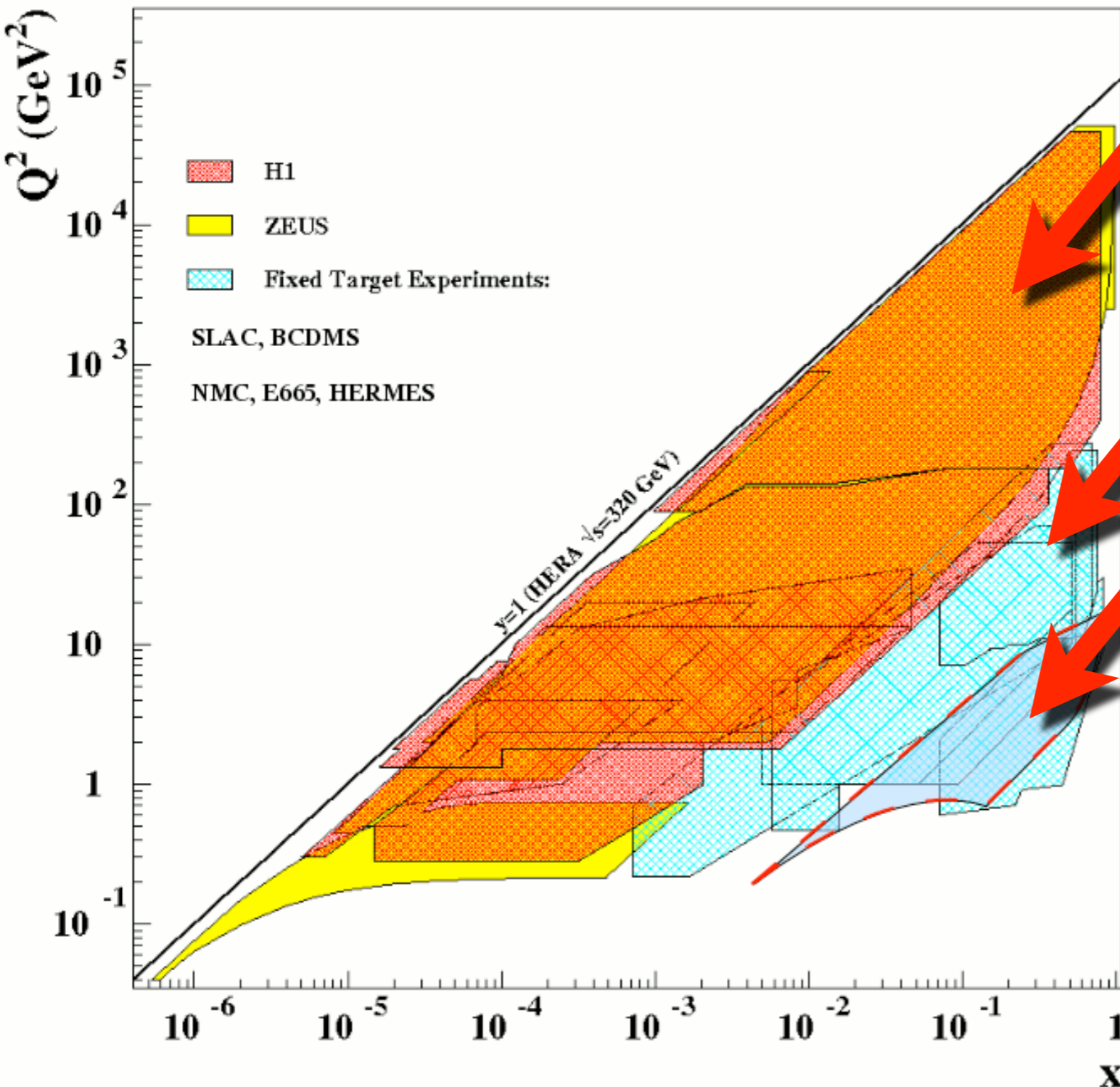
Collins Amplitudes for Kaons

$$A_C \propto \delta q \otimes H_1^\perp$$



- no significant non-zero Collins amplitudes for both K^+ and K^-
- Collins amplitudes for K^+ are within statistical accuracy consistent with π^+
- Collins fragmentation function for kaons unknown
- Sea quark transversity expected to be small

Why measuring inclusive DIS cross sections at HERMES?



Collider experiments

Fixed target experiments

HERMES

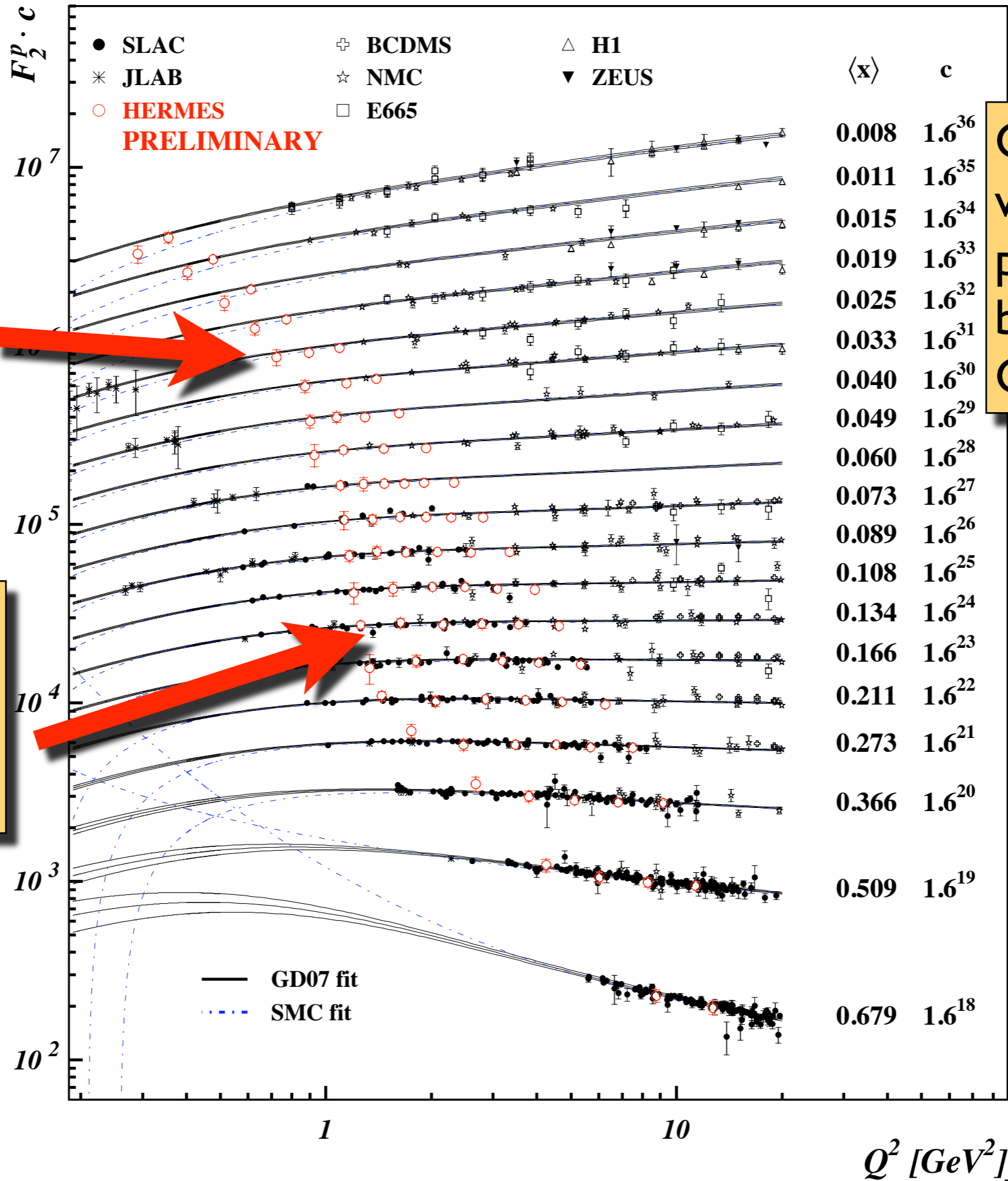
- complementary kinematic coverage compared to colliders
- higher statistics compared to other fixed target experiments:
 - ▶ HERMES: 58 million DIS (P+D)
 - ▶ NMC: 9 million DIS (P+D)

F_2^p

Proton

New region covered by HERMES

Agreement with world data in the overlap region



$\langle x \rangle$	c
0.008	1.6^{36}
0.011	1.6^{35}
0.015	1.6^{34}
0.019	1.6^{33}
0.025	1.6^{32}
0.033	1.6^{31}
0.040	1.6^{30}
0.049	1.6^{29}
0.060	1.6^{28}
0.073	1.6^{27}
0.089	1.6^{26}
0.108	1.6^{25}
0.134	1.6^{24}
0.166	1.6^{23}
0.211	1.6^{22}
0.273	1.6^{21}
0.366	1.6^{20}
0.509	1.6^{19}
0.679	1.6^{18}

Comparison with parameterization by SMC and GD07

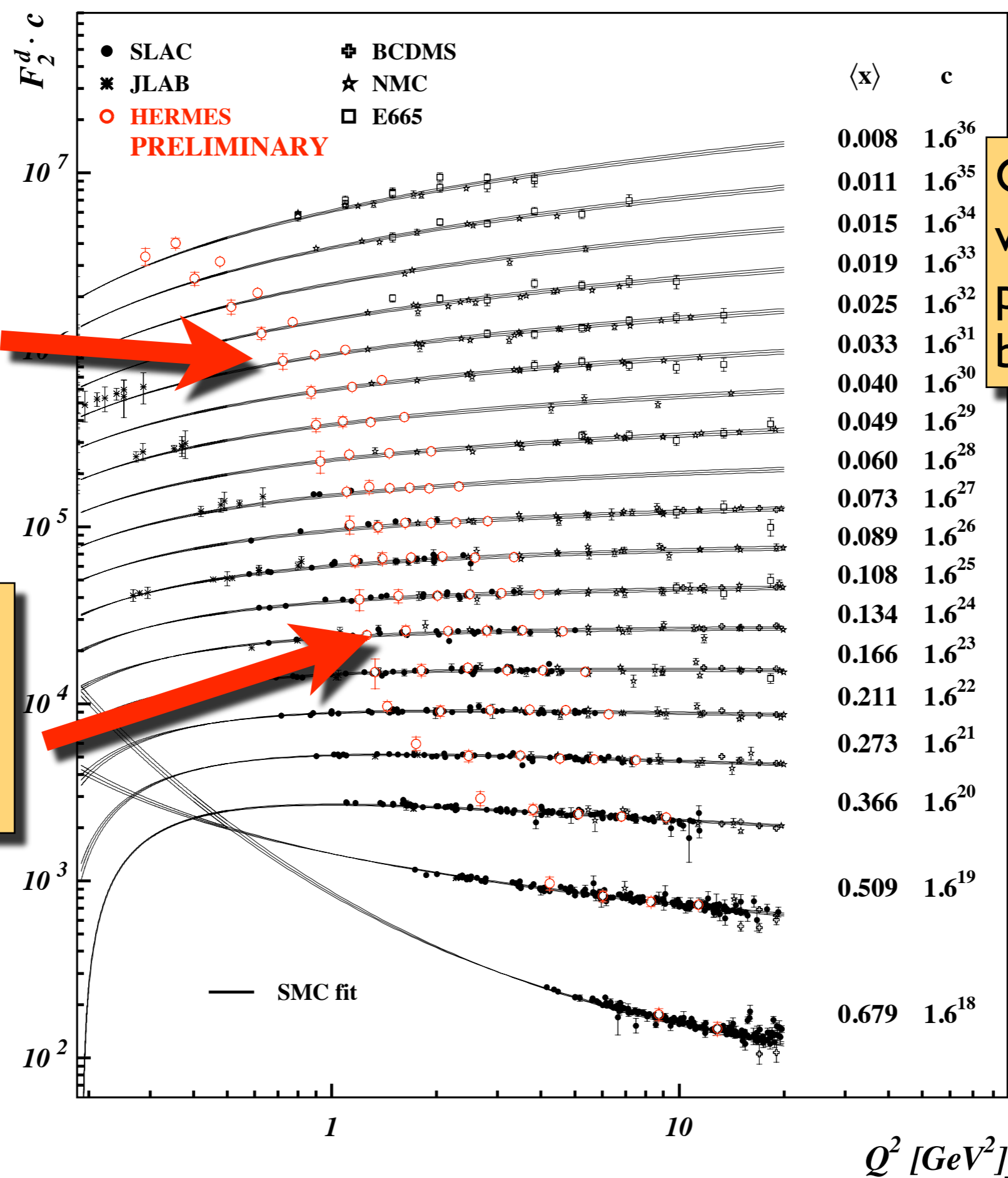
GD07: hep-ph0708.3196
 SMC: Phys. Rev. D, Vol. 58, 112001

F_2^D

Deuteron

New region covered by HERMES

Agreement with world data in the overlap region

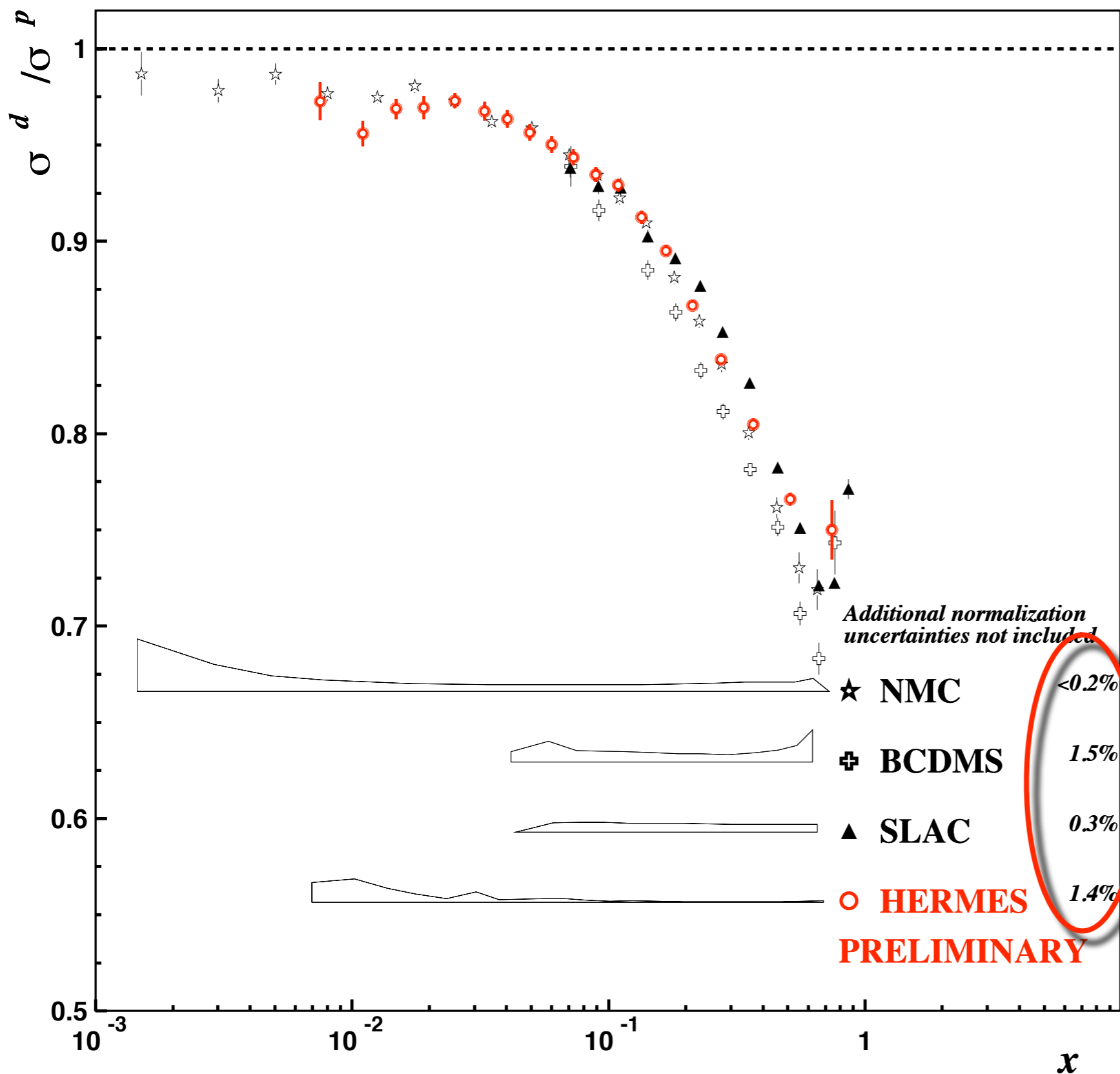


$\langle x \rangle$	c
0.008	1.6^{36}
0.011	1.6^{35}
0.015	1.6^{34}
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0.211	1.6^{22}
0.273	1.6^{21}
0.366	1.6^{20}
0.509	1.6^{19}
0.679	1.6^{18}

Comparison with parameterization by SMC

SMC: Phys. Rev. D, Vol. 58, I12001

World data on σ^d/σ^p



Many systematic errors common to proton and deuteron cross sections cancel in ratio

Normalization uncertainties