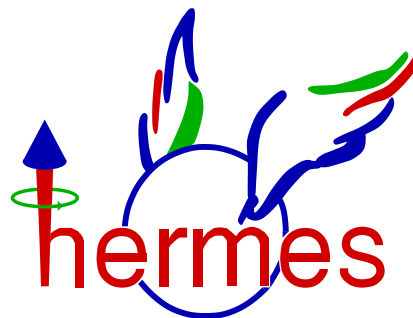

Exclusive hard processes at HERMES

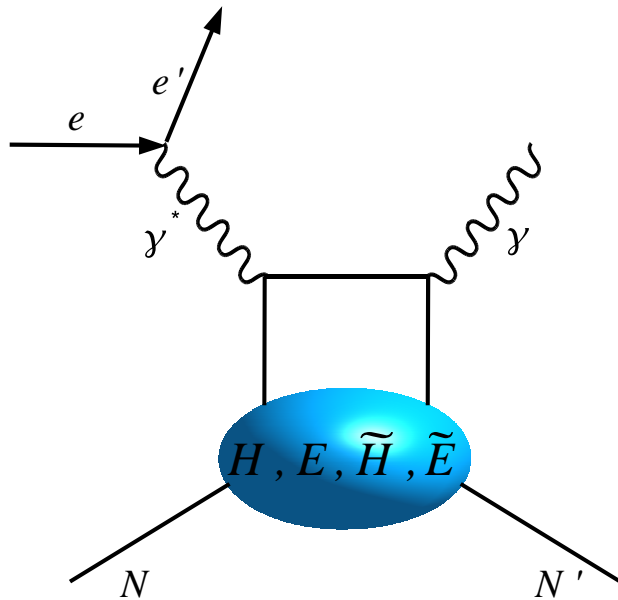
10th international workshop on hadron structure and spectroscopy Venice, Italy, 2010

Ami Rostomyan

(on behalf of the HERMES collaboration)



deeply virtual Compton scattering



$(\gamma^* \rightarrow \gamma): H, E, \tilde{H}, \tilde{E}$ (twist-2, chiral even)

\bullet H and \tilde{H} conserve the nucleon helicity

\bullet E and \tilde{E} describe the nucleon helicity flip

\bullet Ji relation

$$J_q = \frac{1}{2} \lim_{t \rightarrow 0} \int_{-1}^1 dx x [H_q(x, \xi, t) + E_q(x, \xi, t)]$$

$$= \frac{1}{2} \Delta \Sigma_q + L_q$$

why DVCS?

\bullet the cleanest probe of GPDs

\bullet theoretical accuracy at NNLO

\bullet no gluons in the LO

Compton form factors

\bullet convolutions of GPDs ($F : H, E, \tilde{H}, \tilde{E}$) and hard scattering functions

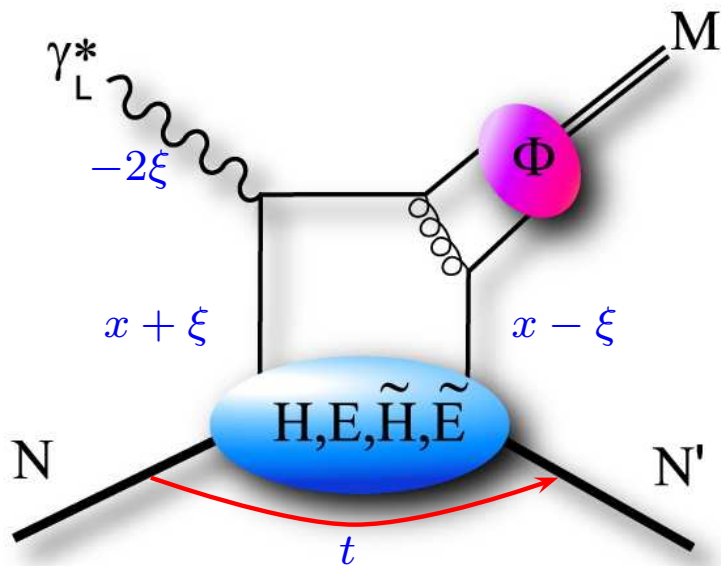
$$\mathcal{F}(\xi, t) = \sum_q \int_{-1}^1 dx C_q(\xi, x) F^q(x, \xi, t)$$

exclusive meson production

factorization in collinear approximation

-Collins, Frankfurt, Strikman (1997)-

$$\mathcal{A} \propto F(x, \xi, t; \mu^2) \otimes K(x, \xi, z; \log(Q^2/\mu^2)) \otimes \Phi(z; \mu^2)$$



at leading-twist: $H, E, \tilde{H}, \tilde{E}$

- H and \tilde{H} conserve the nucleon helicity

- E and \tilde{E} describe the nucleon helicity flip

quantum numbers of final state selects different GPDs

- vector mesons ($\gamma_L^* \rightarrow \rho_L, \omega_L, \phi_L$): H, E

- pseudoscalar mesons ($\gamma_L^* \rightarrow \pi, \eta$): \tilde{H}, \tilde{E}

factorization for σ_L (and ρ_L, ω_L, ϕ_L) only

- $\sigma_L - \sigma_T$ suppressed by $1/Q$

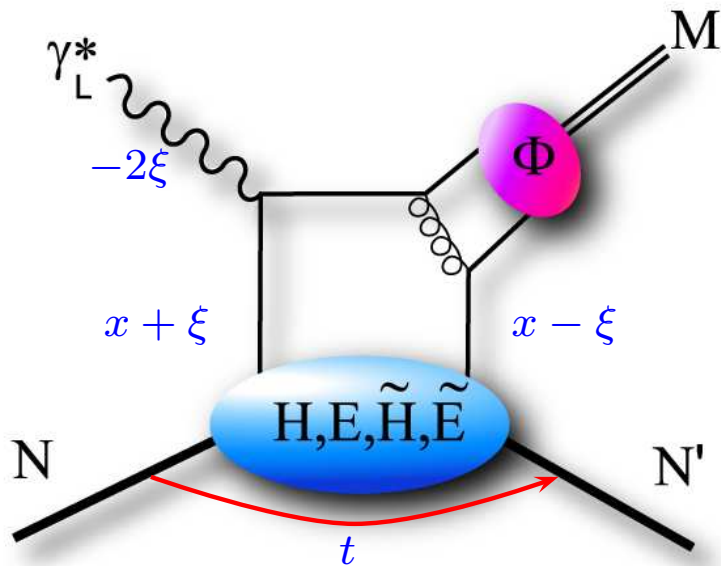
- σ_T suppressed by $1/Q^2$

exclusive meson production

modified perturbative approach

-Goloskokov, Kroll (2006)-

$$\mathcal{A} \propto F(x, \xi, t; \mu^2) \otimes K(x, \xi, z; \log(Q^2/\mu^2)) \otimes \Phi(z, k_{\perp}; \mu^2)$$



at leading-twist: $H, E, \tilde{H}, \tilde{E}$

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- $\sigma_L - \sigma_T$ suppressed by $1/Q$

- σ_T suppressed by $1/Q^2$

power corrections: k_{\perp} is not neglected

- regulate the singularity in the transverse amplitude

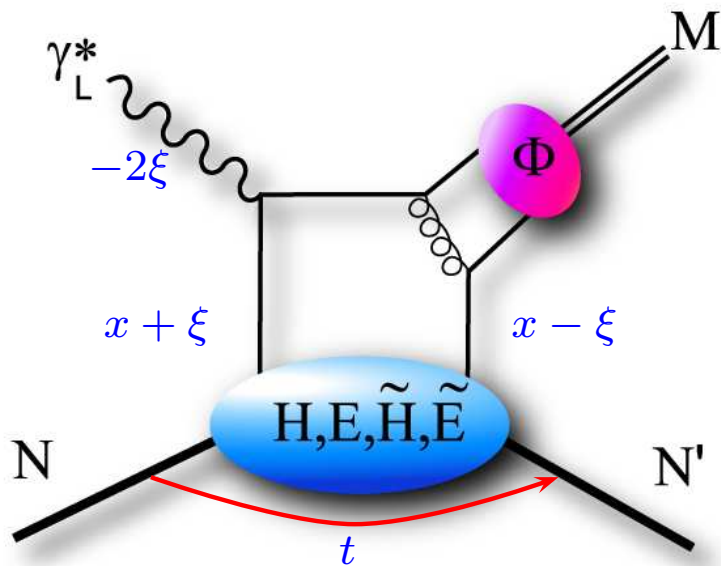
- $\gamma_T^* \rightarrow \rho_T^0$ transitions can be calculated (model dependent)

exclusive meson production

modified perturbative approach

-Goloskokov, Kroll (2006)-

$$A \propto F(x, \xi, t; \mu^2) \otimes K(x, \xi, z; \log(Q^2/\mu^2)) \otimes \Phi(z, k_{\perp}; \mu^2)$$



at leading-twist: $H, E, \tilde{H}, \tilde{E}$

- H and \tilde{H} conserve the nucleon helicity

- E and \tilde{E} describe the nucleon helicity flip

quantum numbers of final state selects different GPDs

- vector mesons ($\gamma_L^* \rightarrow \rho_L, \omega_L, \phi_L$): H, E

- pseudoscalar mesons ($\gamma_L^* \rightarrow \pi, \eta$): \tilde{H}, \tilde{E}

factorization for σ_L (and ρ_L, ω_L, ϕ_L) only

- $\sigma_L - \sigma_T$ suppressed by $1/Q$

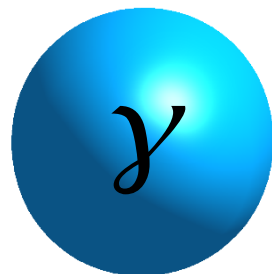
- σ_T suppressed by $1/Q^2$

power corrections: k_{\perp} is not neglected

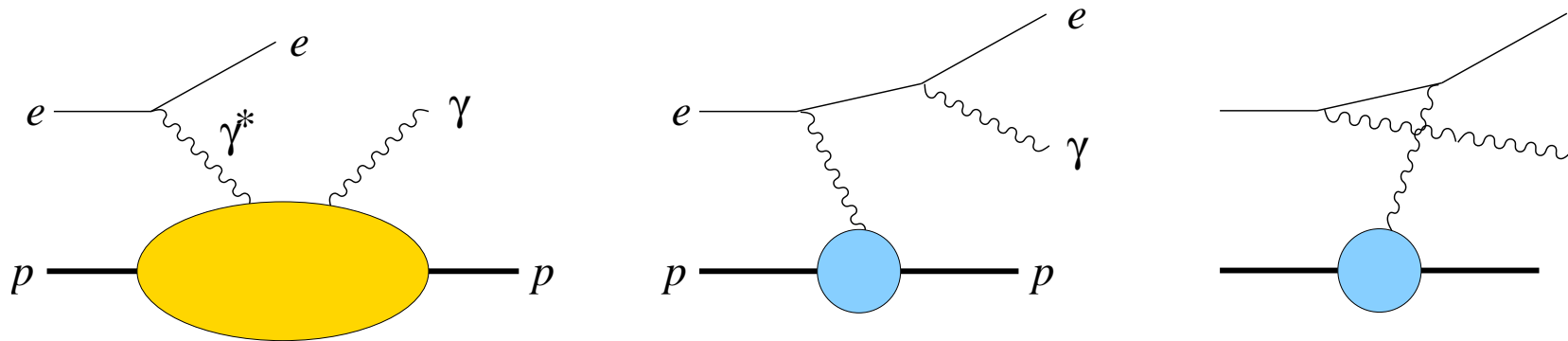
- $\gamma_T^* \rightarrow \rho_T^0$ transitions can be calculated (model dependent)

- ρ^0 : contributions from \tilde{H} and \tilde{E}

- π^+ : contributions from \tilde{H}_T



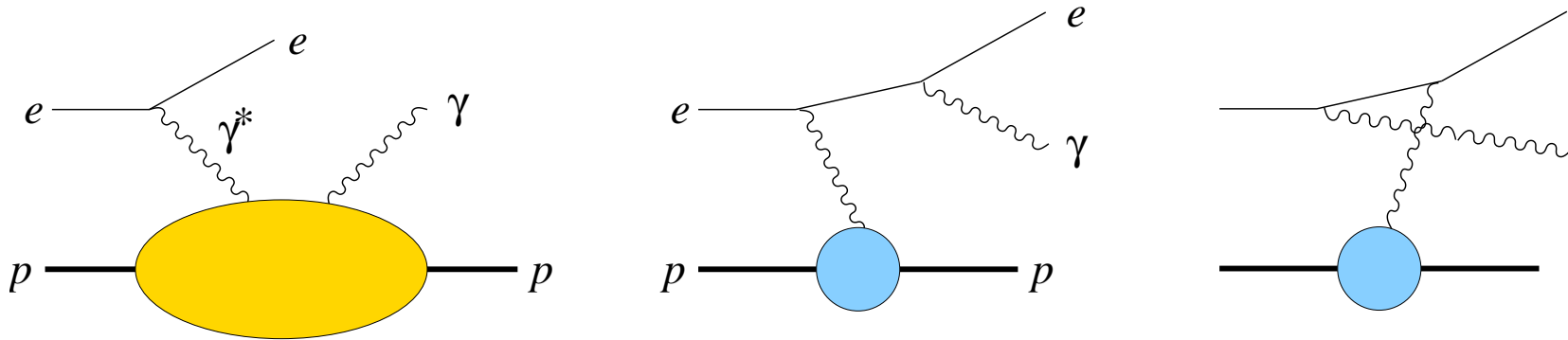
Deeply Virtual Compton Scattering (DVCS)



same initial and final states in DVCS and Bethe-Heitler \Rightarrow Interference!

$$\sigma_{ep} \propto |T_{BH}|^2 + |T_{DVCS}|^2 + \underbrace{T_{BH}T_{DVCS}^* + T_{BH}^*T_{DVCS}}_{\mathcal{I}}$$

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σ_{XY}

$$\sigma_{ep} \propto |T_{BH}|^2 + |T_{DVCS}|^2 + \underbrace{T_{BH}T_{DVCS}^* + T_{BH}^*T_{DVCS}}_{\mathcal{I}}$$

beam:
 P_l

target:
 $S_L S_T$

$$\begin{aligned} d\sigma \sim & d\sigma_{UU}^{BH} + e_l d\sigma_{UU}^I + d\sigma_{UU}^{DVCS} \\ & + e_l P_l d\sigma_{LU}^I + P_l d\sigma_{LU}^{DVCS} \\ & + e_l S_L d\sigma_{UL}^I + S_L d\sigma_{UL}^{DVCS} \\ & + e_l S_T d\sigma_{UT}^I + S_T d\sigma_{UT}^{DVCS} \\ & + P_l S_L d\sigma_{LL}^{BH} + e_l P_l S_L d\sigma_{LL}^I + P_l S_L d\sigma_{LL}^{DVCS} \\ & + P_l S_T d\sigma_{LT}^{BH} + e_l P_l S_T d\sigma_{LT}^I + P_l S_T d\sigma_{LT}^{DVCS} \end{aligned}$$

single spin terms: LU, UL, UT

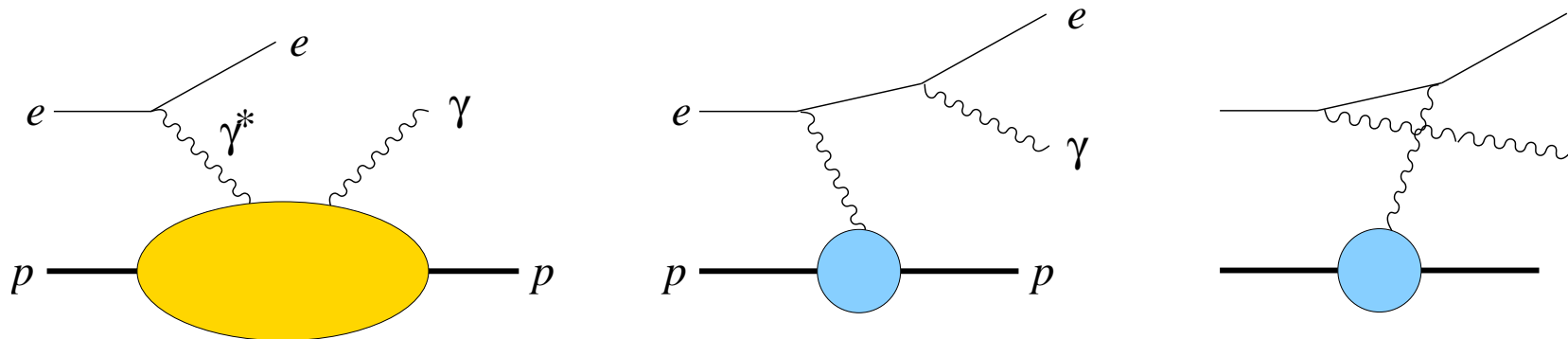
-  no pure Bethe-Heitler contribution
-  project imaginary parts of Compton form factors

unpolarized and double-spin terms:

UU, LL, LT

-  project real parts of Compton form factors

Deeply Virtual Compton Scattering (DVCS)



same initial and final states in DVCS and Bethe-Heitler \Rightarrow Interference!

σ_{XY}

$$\sigma_{ep} \propto |\mathcal{T}_{BH}|^2 + |\mathcal{T}_{DVCS}|^2 + \underbrace{\mathcal{T}_{BH}\mathcal{T}_{DVCS}^* + \mathcal{T}_{BH}^*\mathcal{T}_{DVCS}}_{\mathcal{I}}$$

beam:
 P_L

target:
 $S_L S_T$

$$\begin{aligned} d\sigma \sim & d\sigma_{UU}^{BH} + e_l d\sigma_{UU}^I + d\sigma_{UU}^{DVCS} \\ & + e_l P_l d\sigma_{LU}^I + P_l d\sigma_{LU}^{DVCS} \\ & + e_l S_L d\sigma_{UL}^I + S_L d\sigma_{UL}^{DVCS} \\ & + e_l S_T d\sigma_{UT}^I + S_T d\sigma_{UT}^{DVCS} \\ & + P_l S_L d\sigma_{LL}^{BH} + e_l P_l S_L d\sigma_{LL}^I + P_l S_L d\sigma_{LL}^{DVCS} \\ & + P_l S_T d\sigma_{LT}^{BH} + e_l P_l S_T d\sigma_{LT}^I + P_l S_T d\sigma_{LT}^{DVCS} \end{aligned}$$


Bethe-Heitler contribution:

 calculated at QED

DVCS contribution:

 HERMES: $|\mathcal{T}_{DVCS}|^2 \ll |\mathcal{T}_{BH}|^2$

interference term:

 depend on a linear combination of Compton form factors

 access to GPD combinations through azimuthal asymmetries

express asymmetries in terms of Fourier coefficients

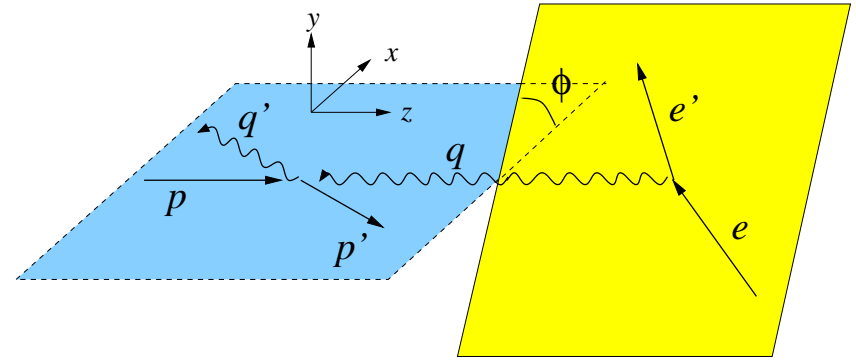
$$\sigma(\phi, P_\ell, e_\ell) = \sigma_{UU}(\phi) \times \left[1 + P_\ell A_{LU}^{DVCS}(\phi) + e_\ell P_\ell A_{LU}^I(\phi) + e_\ell A_C(\phi) \right]$$

Fourier expansion in azimuthal angle ϕ

$$|\tau_{BH}|^2 \propto \sum_{n=0}^2 c_n^{BH} \cos(n\phi)$$

$$|\tau_{DVCS}|^2 \propto \sum_{n=0}^2 c_n^{DVCS} \cos(n\phi) + P_\ell s_1^{DVCS} \sin \phi$$

$$I \propto \sum_{n=0}^3 c_n^I \cos(n\phi) + \sum_{n=1}^2 P_\ell s_n^I \sin(n\phi)$$



express asymmetries in terms of Fourier coefficients

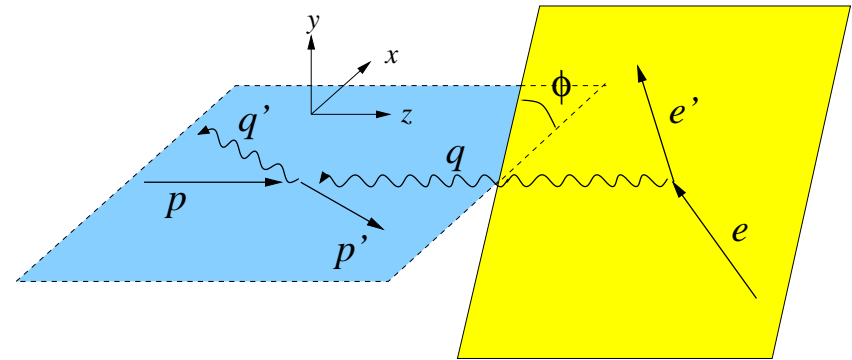
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$$c_1^I \propto F_1 \text{Re}\mathcal{H}$$

$$c_0^I \propto -\frac{-t}{Q} c_1^I$$

$$s_1^I \propto F_1 \text{Im}\mathcal{H}$$

express asymmetries in terms of Fourier coefficients

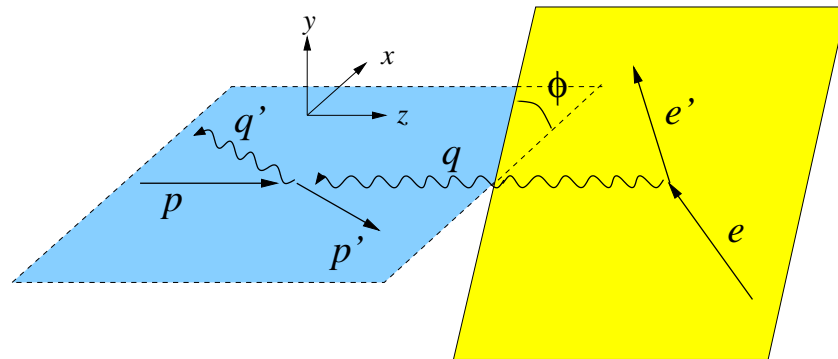
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$$I \propto \sum_{n=0}^3 c_n^I \cos(n\phi) + \sum_{n=1}^2 P_\ell s_n^I \sin(n\phi)$$



DVCS term:

azimuthal modulation	$\gamma^*(\mu) \rightarrow \gamma(\mu')$	relative order
constant	$+1 \rightarrow +1$	1
$\cos \phi, \sin \phi$	$0 \rightarrow +1$	$1/Q$
$\cos 2\phi, \sin 2\phi$	$-1 \rightarrow +1$	1 (gluon GPDs) $1/Q^2$ (quark GPDs)

$$c_1^I \propto F_1 \text{Re}\mathcal{H}$$

$$c_0^I \propto -\frac{-t}{Q} c_1^I$$

$$s_1^I \propto F_1 \text{Im}\mathcal{H}$$

express asymmetries in terms of Fourier coefficients

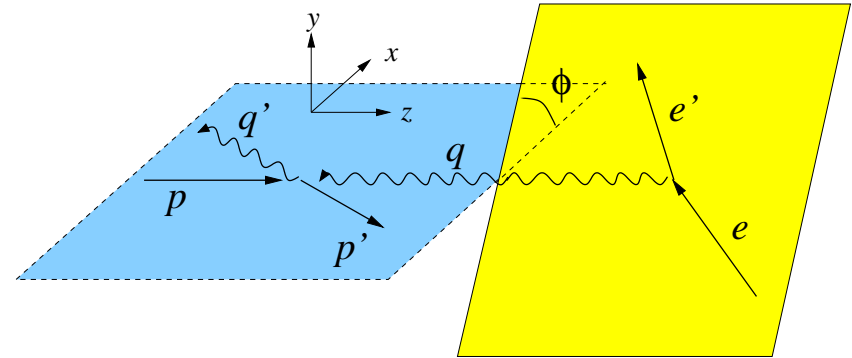
$$\sigma(\phi, P_\ell, e_\ell) = \sigma_{UU}(\phi) \times \left[1 + P_\ell A_{LU}^{DVCS}(\phi) + e_\ell P_\ell A_{LU}^I(\phi) + e_\ell A_C(\phi) \right]$$

Fourier expansion in azimuthal angle ϕ

$$|\tau_{BH}|^2 \propto \sum_{n=0}^2 c_n^{BH} \cos(n\phi)$$

$$|\tau_{DVCS}|^2 \propto \sum_{n=0}^2 c_n^{DVCS} \cos(n\phi) + P_\ell s_1^{DVCS} \sin \phi$$

$$I \propto \sum_{n=0}^3 c_n^I \cos(n\phi) + \sum_{n=1}^2 P_\ell s_n^I \sin(n\phi)$$



interference term:

azimuthal modulation	$\gamma^*(\mu) \rightarrow \gamma(\mu')$	relative order
constant	$+1 \rightarrow +1$	$1/Q$
$\cos \phi, \sin \phi$	$+1 \rightarrow +1$	1
$\cos 2\phi, \sin 2\phi$	$0 \rightarrow +1$	$1/Q$
$\cos 3\phi, \sin 3\phi$	$-1 \rightarrow +1$	$1/Q^2$ or α_s

$$c_1^I \propto F_1 \text{Re} \mathcal{H}$$

$$c_0^I \propto -\frac{t}{Q} c_1^I$$

$$s_1^I \propto F_1 \text{Im} \mathcal{H}$$

DVCS at HERMES (pre-recoil data)

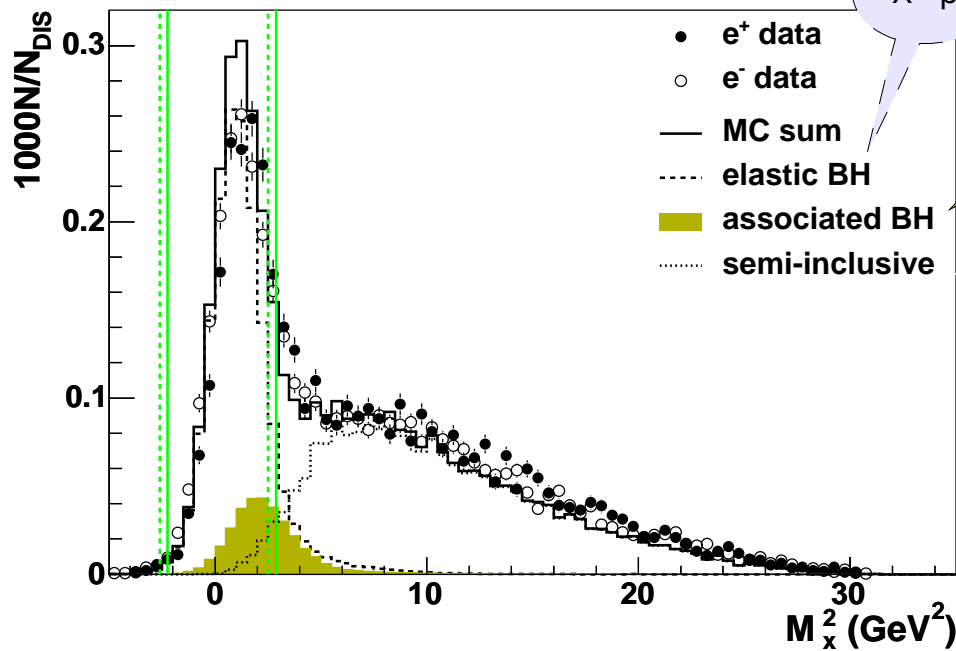
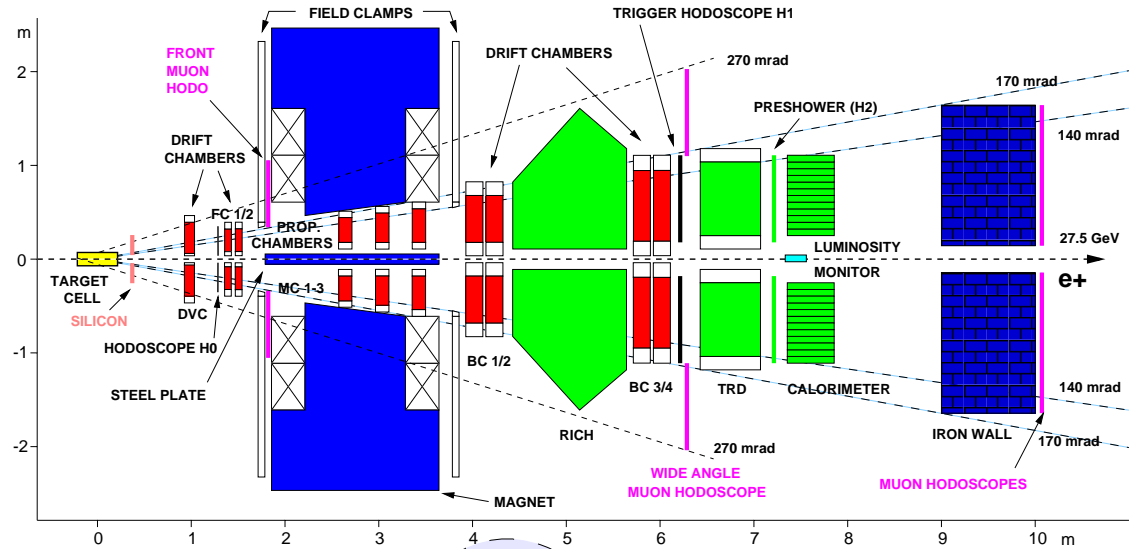
$$e + p \rightarrow e' + \gamma + p'$$



detected particles:
lepton and photon



missing mass technique for
 $ep \rightarrow e'\gamma X$:
 $M_X^2 = (p + e - e' - \gamma)^2$



$X=p$

Resonant excitation:
 $X=\Delta^+$

$X=\pi^0 + \dots$

unpolarized-target asymmetries

$$\sigma(\phi, P_\ell, e_\ell) = \sigma_{UU}(\phi) \times \left[1 + P_\ell \mathcal{A}_{LU}^{DVCS}(\phi) + e_\ell P_\ell \mathcal{A}_{LU}^I(\phi) + e_\ell \mathcal{A}_C(\phi) \right]$$

beam-helicity asymmetry (single charge):

$$\mathcal{A}_{LU}(\phi) \equiv \frac{d\sigma^{\rightarrow} - d\sigma^{\leftarrow}}{d\sigma^{\rightarrow} + d\sigma^{\leftarrow}}$$

- projects the imaginary part of τ_{DVCS}
- no separate access to s_1^{DVCS} and s_1^I

beam-helicity asymmetry (new approach):

- charge-difference beam-helicity asymmetry

$$\mathcal{A}_{LU}^I(\phi) \equiv \frac{(d\sigma^{+\rightarrow} - d\sigma^{+\leftarrow}) - (d\sigma^{-\rightarrow} - d\sigma^{-\leftarrow})}{(d\sigma^{+\rightarrow} + d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} + d\sigma^{-\leftarrow})}$$

- charge-averaged beam-helicity asymmetry

$$\mathcal{A}_{LU}^{DVCS}(\phi) \equiv \frac{(d\sigma^{+\rightarrow} - d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} - d\sigma^{-\leftarrow})}{(d\sigma^{+\rightarrow} + d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} + d\sigma^{-\leftarrow})}$$

- s_1^{DVCS} and s_1^I can be disentangled

beam-charge asymmetry:

$$\mathcal{A}_C(\phi) \equiv \frac{d\sigma^+ - d\sigma^-}{d\sigma^+ + d\sigma^-}$$

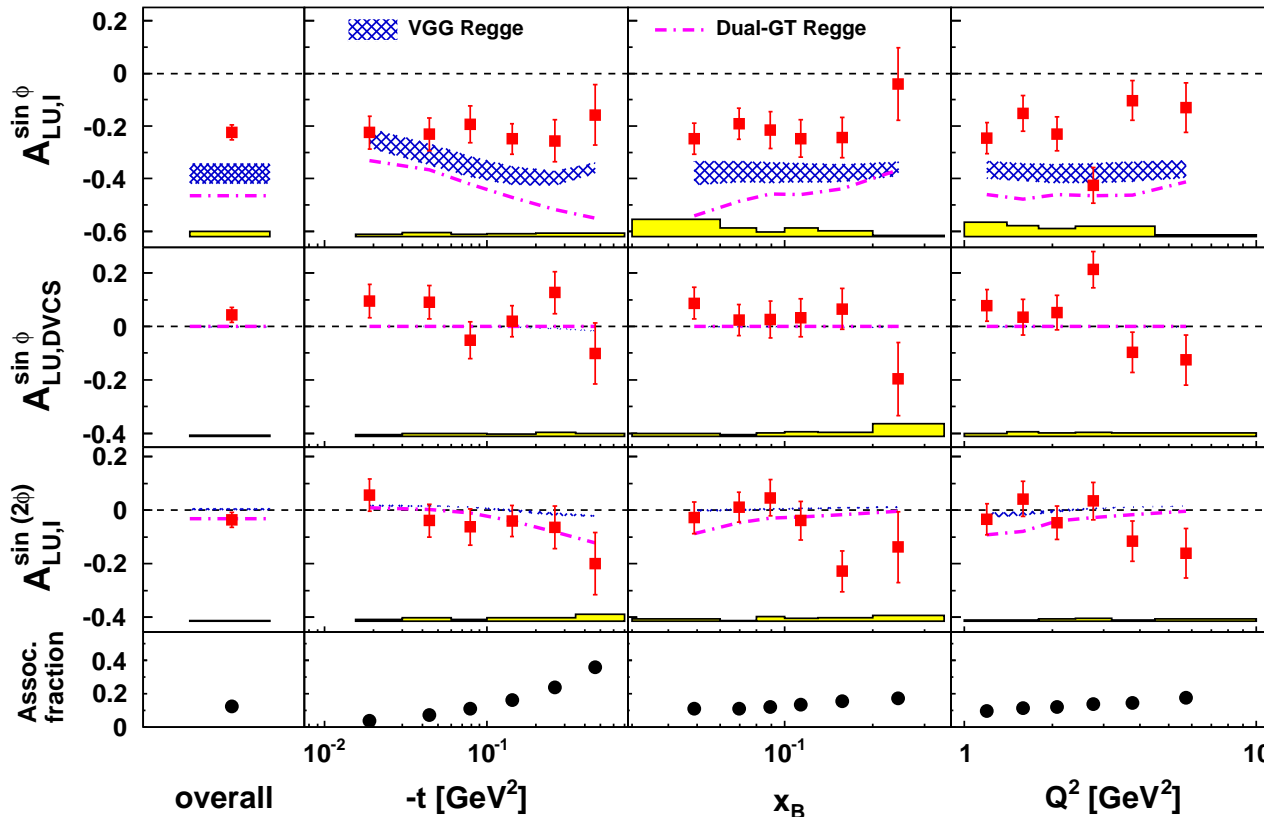
- projects the real part of τ_{DVCS}

beam helicity asymmetry

$$A_{LU}^I(\phi) = \sum_{n=1}^2 A_{LU,I}^{\sin(n\phi)} \sin(n\phi) \propto \sum_{n=1}^2 s_n^I \sin(n\phi)$$

$$A_{LU,DVCS}^{\sin\phi} \propto s_1^{\text{DVCS}} \sin\phi$$

-HERMES Collaboration: arXiv:0909.3587 (2009)-



$$A_{LU,I}^{\sin\phi}$$



twist-2:

$$\propto F_1 \text{Im}\mathcal{H}$$



large overall value



no kin. dependencies

$$A_{LU,DVCS}^{\sin\phi}, A_{LU,I}^{\sin 2\phi}$$



twist-3



overall value

compatible with 0



no kin. dependencies



overshoot the magnitude of $A_{LU,I}^{\sin\phi}$ by a factor of 2



describe the shape of kin dependencies on x_B and Q^2 , but not on t

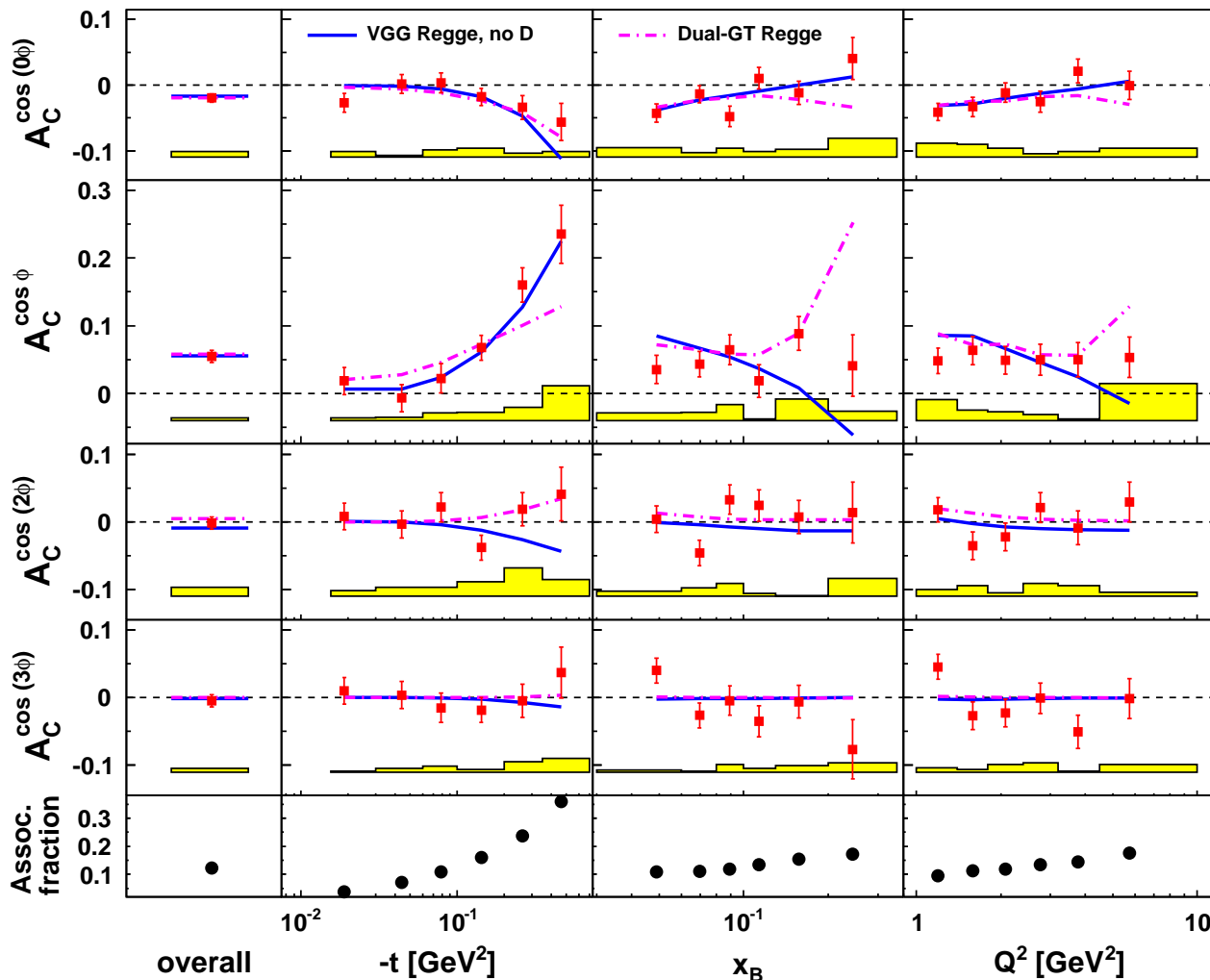


overestimation is not due to the associated production

beam charge asymmetry

$$A_C(\phi) = \sum_{n=0}^3 A_C^{\cos(n\phi)} \cos(n\phi) \propto \sum_{n=0}^3 c_n^I \cos(n\phi)$$

-HERMES Collaboration: arXiv:0909.3587 (2009)-



twist-2 GPDs: $A_C^{\cos \phi}$, $A_C^{\cos 0\phi}$

- strong t -dependence
- no x_B , Q^2 dependencies

$$A_C^{\cos \phi} \propto F_1 \text{Re}\mathcal{H}$$

$$A_C^{\cos 0\phi} \propto -\frac{t}{Q} A_C^{\cos \phi}$$

$A_C^{\cos(2\phi)} \approx 0$: twist-3 GPDs

$A_C^{\cos(3\phi)} \approx 0$: gluon helicity-flip GPDs

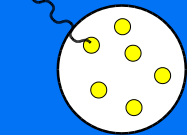
theoretical predictions:

- does not describe the beam-helicity data, but in good agreement with this data

unpolarized deuterium targets

coherent: $e^\pm d \rightarrow e^\pm d \gamma$

 DVCS



 Bethe-Heitler



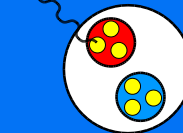
 target stays intact

 spin-1 targets described by 9 GPDs:

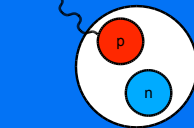
$$H_1^q, H_2^q, H_3^q, H_4^q, H_5^q, \tilde{H}_1^q, \tilde{H}_2^q, \tilde{H}_3^q, \tilde{H}_4^q$$

incoherent: $e^\pm d \rightarrow e^\pm pn \gamma$

 DVCS



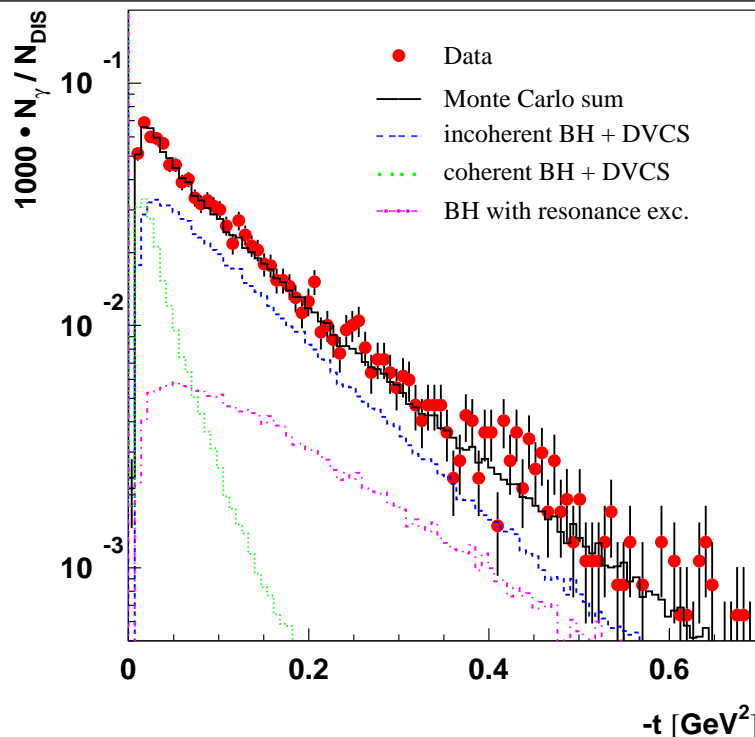
 Bethe-Heitler



 target brakes up

 spin- $\frac{1}{2}$ targets described by 4 GPDs:

$$H, E, \tilde{H}, \tilde{E}$$




coherent:

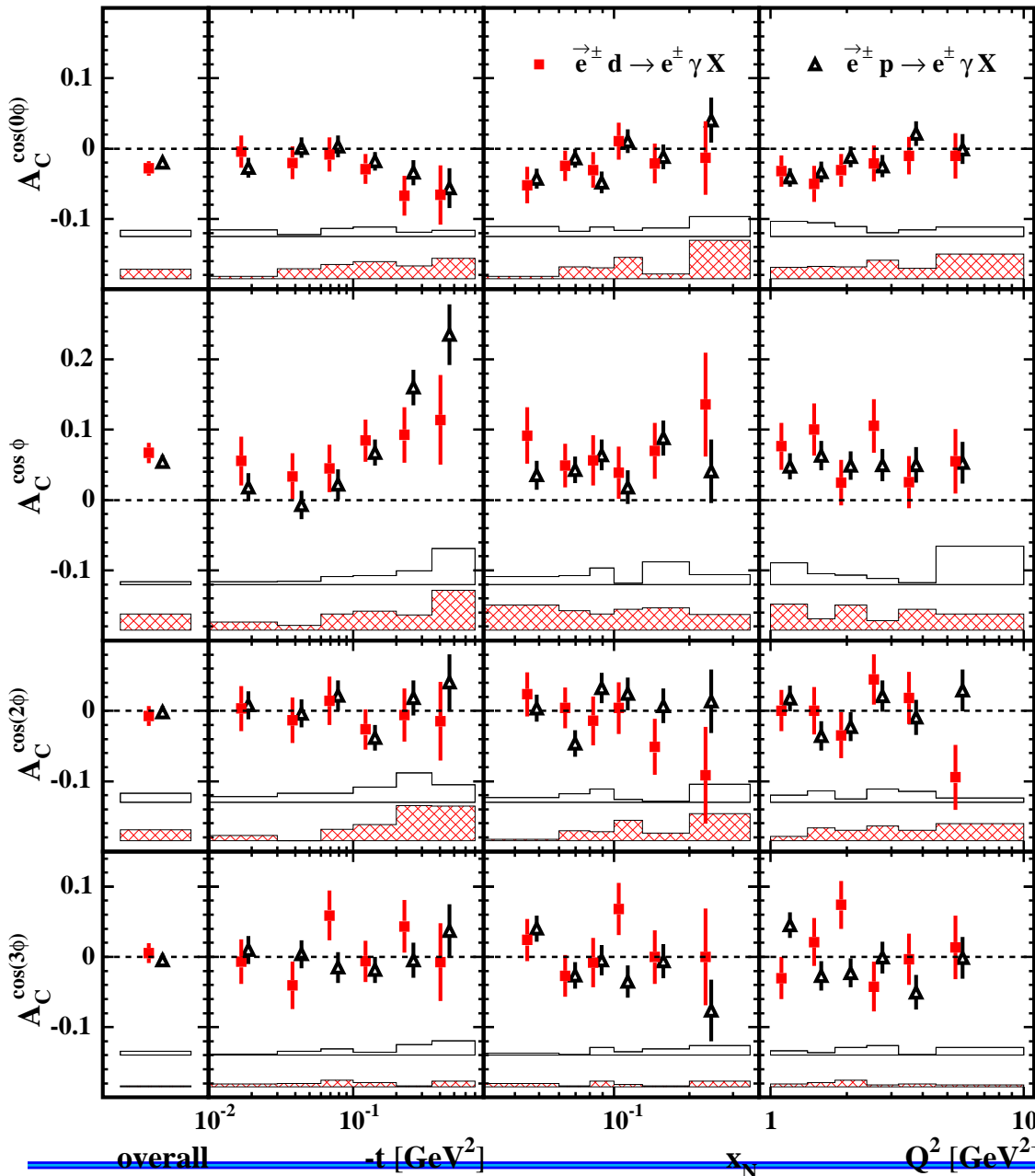
 contribution at small $-t$

incoherent:

 contribution at larger $-t$

 contribution from coherent $[0.06 : 0.7] \text{ GeV}^2$:
20%

beam-charge asymmetry



$$A_C(\phi) = \sum_{n=0}^3 A_C^{\cos(n\phi)} \cos(n\phi)$$

-HERMES Collaboration: arXiv:0911.0091 (2009)-

twist-2:

$$A_{C,coh}^{\cos \phi} \propto G_1 \text{Re}\mathcal{H}_1$$

$$A_{C,incoh}^{\cos \phi} \propto F_1 \text{Re}\mathcal{H}$$

$$A_C^{\cos 0\phi} \propto -\frac{t}{Q} A_C^{\cos \phi}$$

higher twist :

$$A_C^{\cos(2\phi)} \approx 0$$

$$A_C^{\cos(3\phi)} \approx 0$$

- d and p results consistent
- small values of $-t$:
differences due to coherent contribution
- larger values of $-t$:
differences due to neutron contribution

transversely polarized target

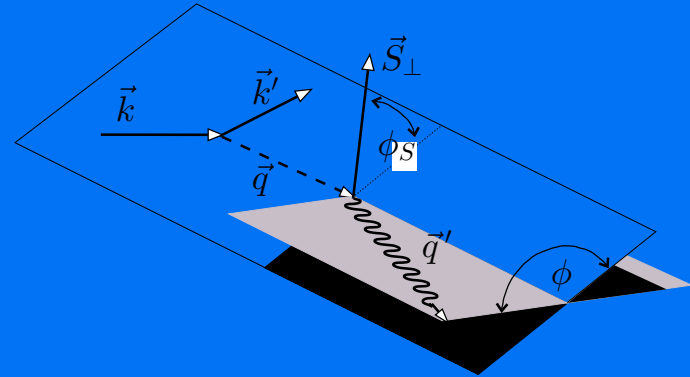
$$\sigma(\phi, P_\ell, S_T) = \sigma_{UU}(\phi) \times \left[1 + S_T \mathcal{A}_{UT}^{\text{DVCS}}(\phi, \phi_S) + S_T e_\ell \mathcal{A}_{UT}^{\text{I}}(\phi, \phi_S) + e_\ell \mathcal{A}_C(\phi) \right]$$

transverse target-spin asymmetry:

$$\mathcal{A}_{UT}(\phi, \phi_S) = \frac{1}{S_T} \cdot \frac{d\sigma^{\uparrow}(\phi, \phi_S) - d\sigma^{\downarrow}(\phi, \phi_S)}{d\sigma^{\uparrow}(\phi, \phi_S) + d\sigma^{\downarrow}(\phi, \phi_S)}$$

beam-charge asymmetry:

$$\mathcal{A}_C(\phi) \equiv \frac{d\sigma^+ - d\sigma^-}{d\sigma^+ + d\sigma^-}$$



$$\mathcal{A}_{UT}^{\text{DVCS}}(\phi, \phi_S) \equiv \frac{1}{S_T} \cdot \frac{d\sigma^{+\uparrow}(\phi, \phi_S) - d\sigma^{+\downarrow}(\phi, \phi_S) + d\sigma^{-\uparrow}(\phi, \phi_S) - d\sigma^{-\downarrow}(\phi, \phi_S)}{d\sigma^{+\uparrow}(\phi, \phi_S) + d\sigma^{+\downarrow}(\phi, \phi_S) + d\sigma^{-\uparrow}(\phi, \phi_S) + d\sigma^{-\downarrow}(\phi, \phi_S)}$$

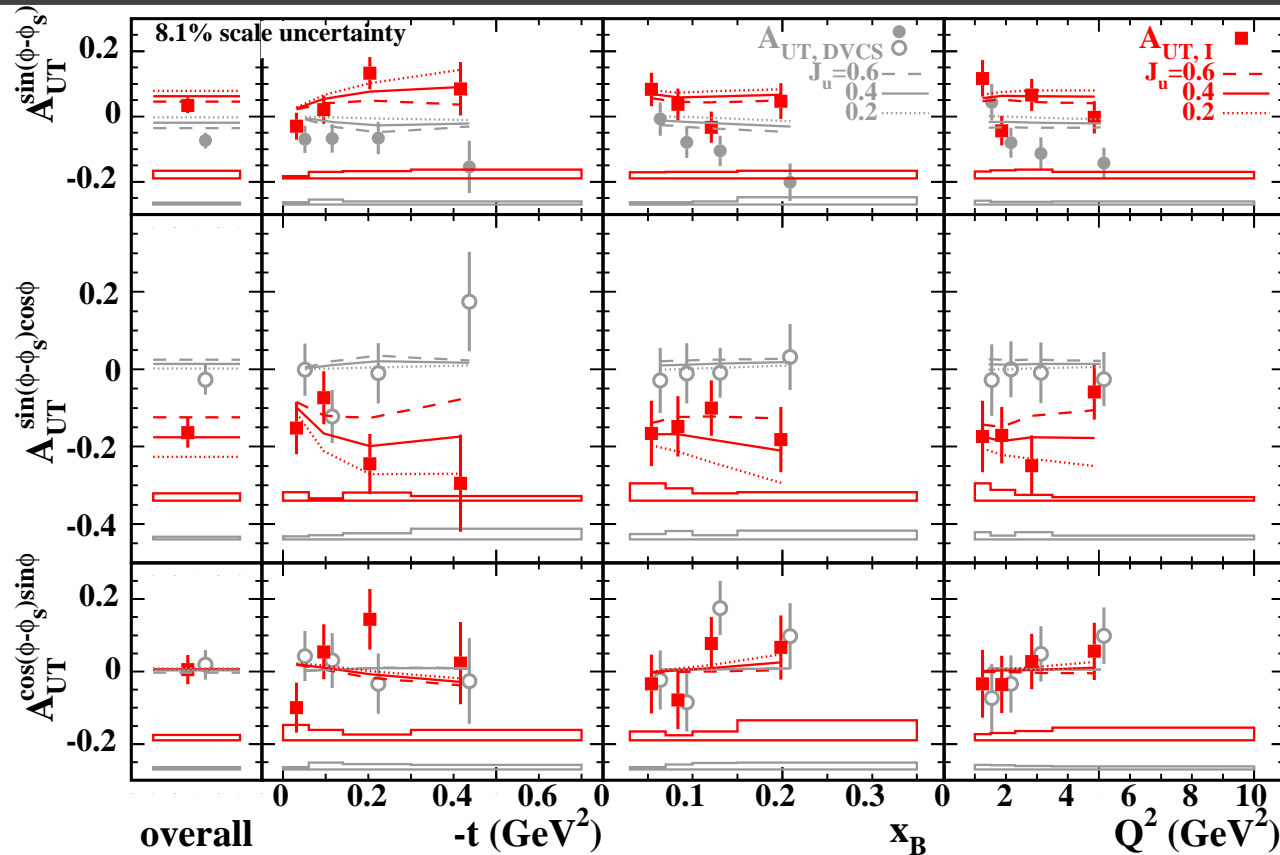
$$\mathcal{A}_{UT}^{\text{I}}(\phi, \phi_S) \equiv \frac{1}{S_T} \cdot \frac{d\sigma^{+\uparrow}(\phi, \phi_S) - d\sigma^{+\downarrow}(\phi, \phi_S) - d\sigma^{-\uparrow}(\phi, \phi_S) + d\sigma^{-\downarrow}(\phi, \phi_S)}{d\sigma^{+\uparrow}(\phi, \phi_S) + d\sigma^{+\downarrow}(\phi, \phi_S) + d\sigma^{-\uparrow}(\phi, \phi_S) + d\sigma^{-\downarrow}(\phi, \phi_S)}$$

separation of $s_i^{\text{DVCS}}, c_i^{\text{DVCS}}$ and $s_i^{\text{I}}, c_i^{\text{I}}$ terms with same harmonic signatures

projects the imaginary part of τ_{DVCS}

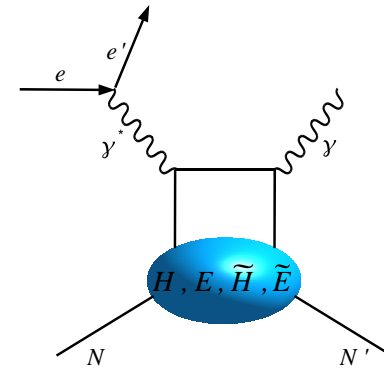
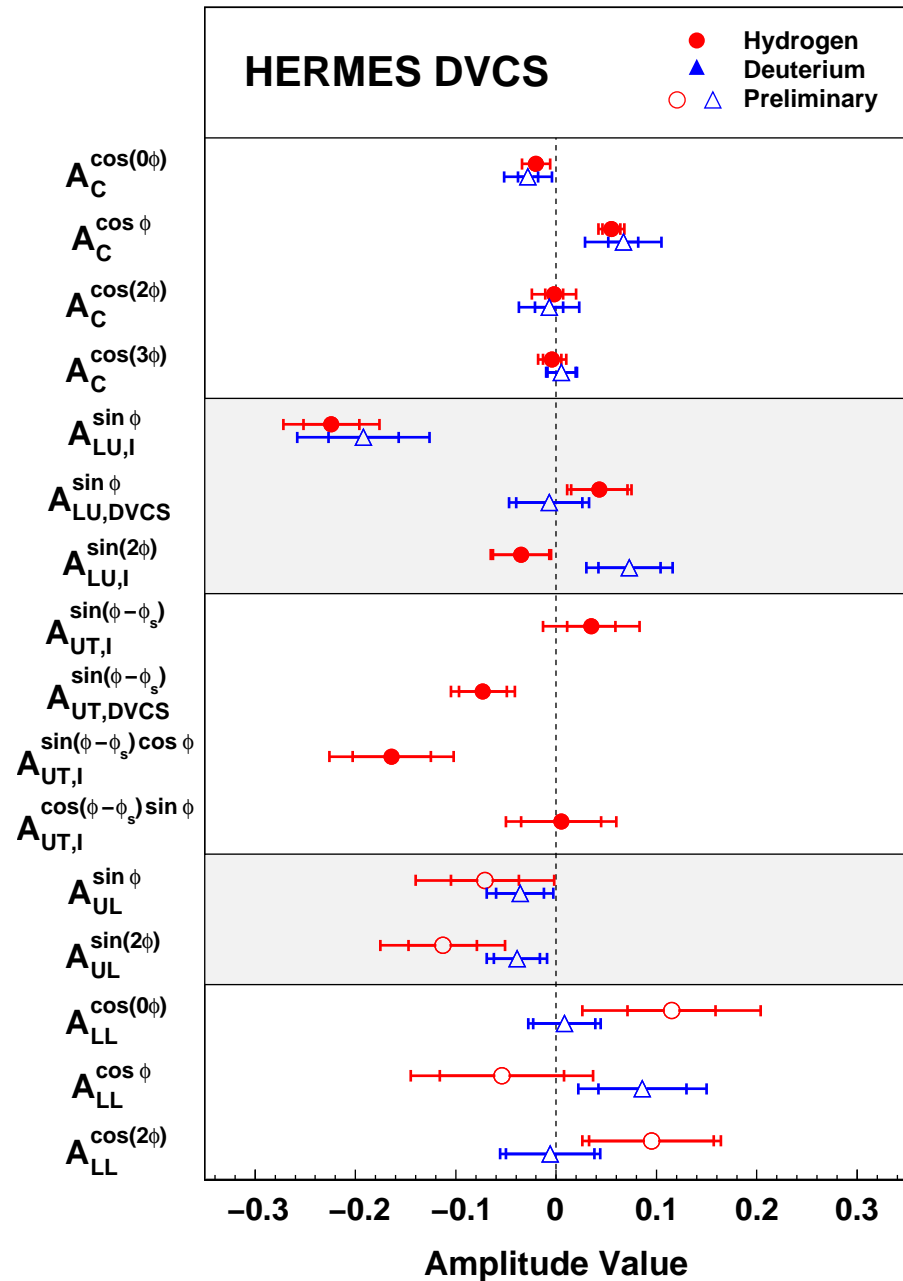
transverse target-spin asymmetry

$$\begin{aligned}
 A_{UT}(\phi, \phi_S) &\propto \text{Im}[F_2 \mathcal{H} - F_1 \mathcal{E}] \sin(\phi - \phi_S) \cos \phi + \text{Im}[F_2 \mathcal{H} - F_1 \mathcal{E}] \sin(\phi - \phi_S) \\
 &+ \text{Im}[\mathcal{H} \mathcal{E}^* - \mathcal{E} \mathcal{H}^* + \xi \tilde{\mathcal{E}} \tilde{\mathcal{H}}^* - \tilde{\mathcal{H}} \xi \tilde{\mathcal{E}}^*] \sin(\phi - \phi_S) + \dots
 \end{aligned}$$



- $A_{UT}^{\sin(\phi-\phi_S)\cos\phi}$ found much more sensitive to J_u than others
- insensitive to J_d , assumed $J_d = 0$ (supported by lattice QCD)
- with a good model, allows a model-dependent constraint

GPDs, DVCS and HERMES



beam-charge asymmetry:

$Re\mathcal{H}$

beam-helicity asymmetry:

$Im\mathcal{H}$

transverse target-spin asymmetry:

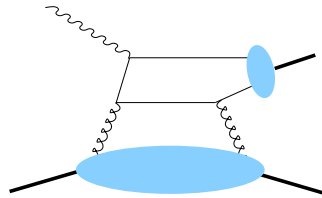
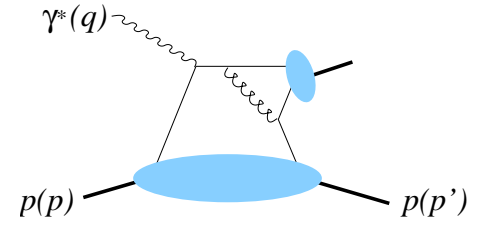
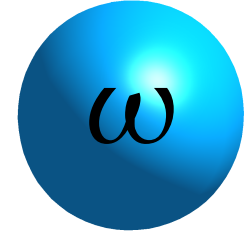
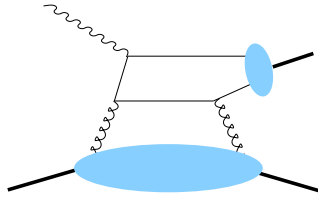
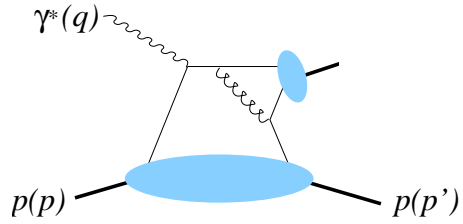
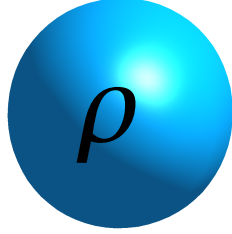
$Im(\mathcal{H}\mathcal{E})$

longitudinal target-spin asymmetry:

$Im\tilde{\mathcal{H}}$

double-spin asymmetry:

$Re\tilde{\mathcal{H}}$



vector meson polarization

🌀 γ^* and ρ^0, ϕ, ω have the same quantum numbers

■ helicity transfer $\gamma^* \rightarrow \rho^0, \phi, \omega$

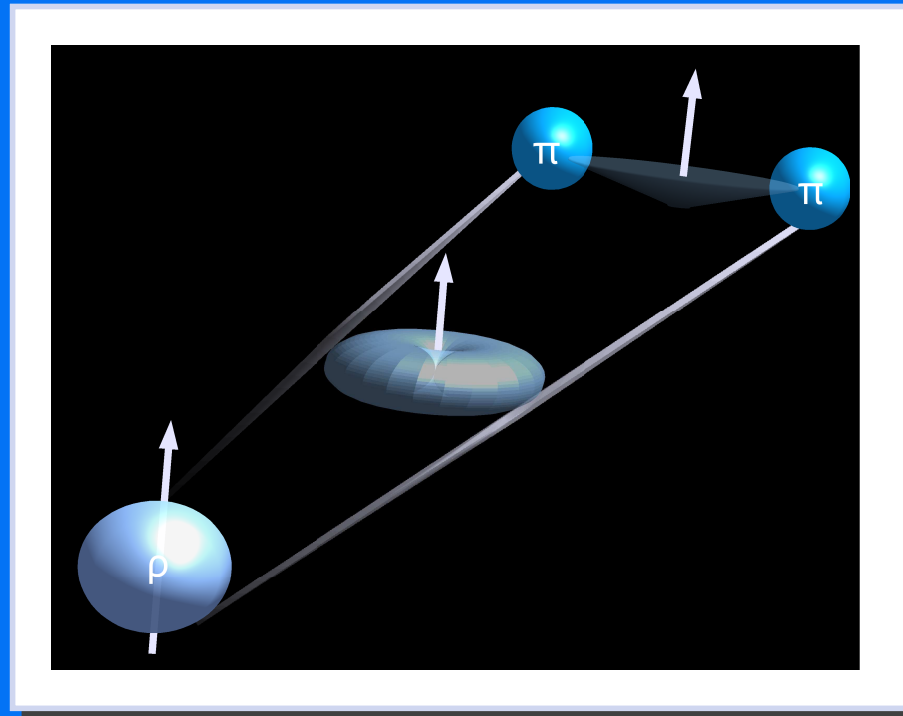
🌀 signature: ρ^0, ϕ, ω production angular distribution

🌀 the spin-state of the ρ^0, ϕ, ω is reflected in the orbital angular momentum of decay particles

■ ρ^0, ϕ, ω (in the rest frame): $J = L + S = 1$

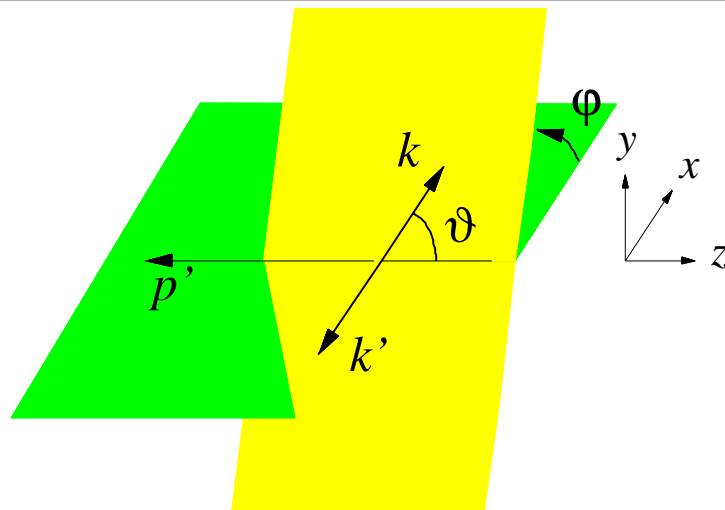
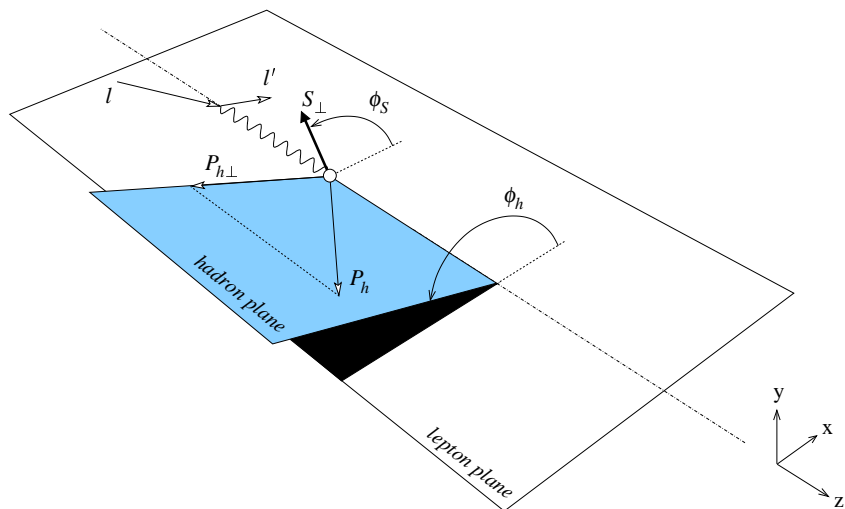
■ π, K : $S = 0, L = 1$

🌀 signature: decay angular distribution



vector meson cross section

$$\frac{d\sigma}{dx_B dQ^2 dt d\phi_s d\phi d\cos\vartheta d\varphi} \sim \frac{d\sigma}{dx_B dQ^2 dt} W(x_B, Q^2, t, \phi_s, \phi, \cos\vartheta, \varphi)$$

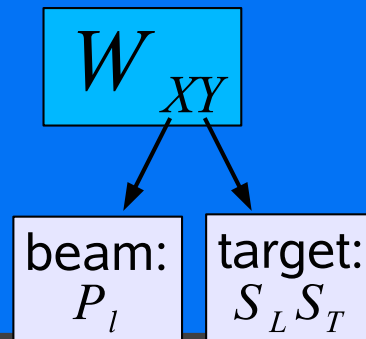


vector meson cross section

$$\frac{d\sigma}{dx_B dQ^2 dt d\phi_s d\phi d\cos\vartheta d\varphi} \sim \frac{d\sigma}{dx_B dQ^2 dt} W(x_B, Q^2, t, \phi_s, \phi, \cos\vartheta, \varphi)$$

production and decay angular distributions W decomposed:

$$W = W_{UU} + P_l W_{LU} + S_L W_{UL} + P_l S_L W_{LL} + S_T W_{UT} + P_l S_T W_{LT}$$



vector meson cross section

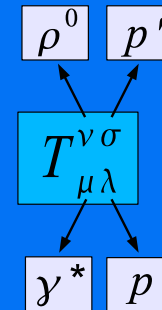
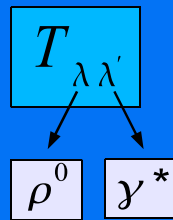
$$\frac{d\sigma}{dx_B dQ^2 dt d\phi_s d\phi d\cos\vartheta d\varphi} \sim \frac{d\sigma}{dx_B dQ^2 dt} W(x_B, Q^2, t, \phi_s, \phi, \cos\vartheta, \varphi)$$

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parametrized by helicity amplitudes $T_{\lambda\lambda'}$ or $T_{\mu\lambda}^{\nu\sigma}$:
 -Schilling, Wolf (1973)-

-Diehl notation (2007)-



vector meson cross section

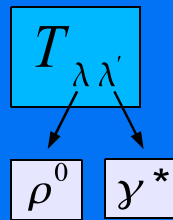
$$\frac{d\sigma}{dx_B dQ^2 dt d\phi_s d\phi d\cos\vartheta d\varphi} \sim \frac{d\sigma}{dx_B dQ^2 dt} W(x_B, Q^2, t, \phi_s, \phi, \cos\vartheta, \varphi)$$

production and decay angular distributions W decomposed:

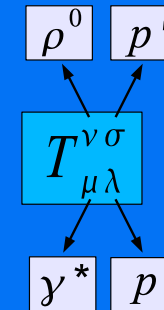
$$W = W_{UU} + P_L W_{LU} + S_L W_{UL} + P_L S_L W_{LL} + S_T W_{UT} + P_L S_T W_{LT}$$

parametrized by helicity amplitudes $T_{\lambda\lambda'}$ or $T_{\mu\lambda}^{\nu\sigma}$:

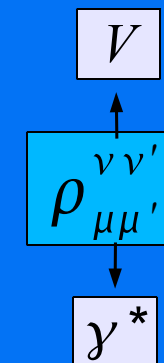
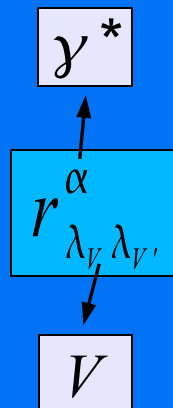
-Schilling, Wolf (1973)-



-Diehl notation (2007)-

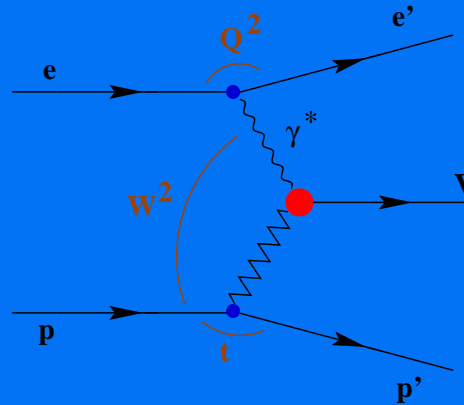


or alternatively by spin-density matrix elements (SDMEs):



(un)natural-parity exchange

Regge theory: the diffractive production of vector meson via an exchange of a particle



natural parity

■ $P = (-1)^J$: exchange of ρ, ω, f_2, a_2
or pomeron

■ $\propto M/W$


unnatural parity

■ $P = -(-1)^J$: exchange of π, a_1, b_1

■ $\propto (M/W)^2$

unnatural-parity exchange contribution is expected only at lower values of W

(un)natural-parity exchange

 Regge theory: the diffractive production of vector meson via an exchange of a particle

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 unnatural-parity exchange contribution is expected only at lower values of W

 GPD formalism: generalized to characterize the symmetry properties of amplitudes under the helicity reversal of the γ^* and ρ^0


natural parity

■ related to GPDs H and E

unnatural parity

■ related to GPDs \tilde{H} and \tilde{E}

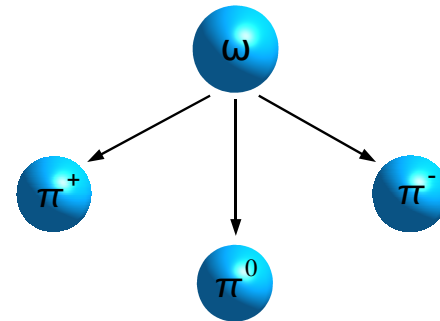
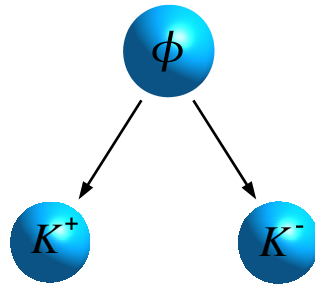
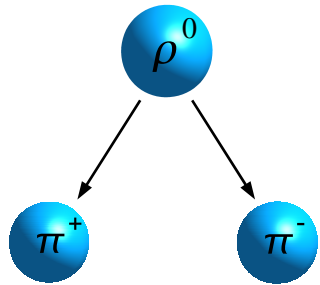
pomeron exchange \Rightarrow gluon exchange

 only **NPE**

reggeon exchange \Rightarrow quark exchange

 **NPE** and **UPE**

exclusive vector meson sample



- no recoil proton detection

- elastic scattering:

$$\Delta E = \frac{M_x^2 - M^2}{2M} \approx 0$$

- only little energy transferred to the target

$$t = (\mathbf{q} - \mathbf{v})^2$$

- transverse four-momentum transfer is used

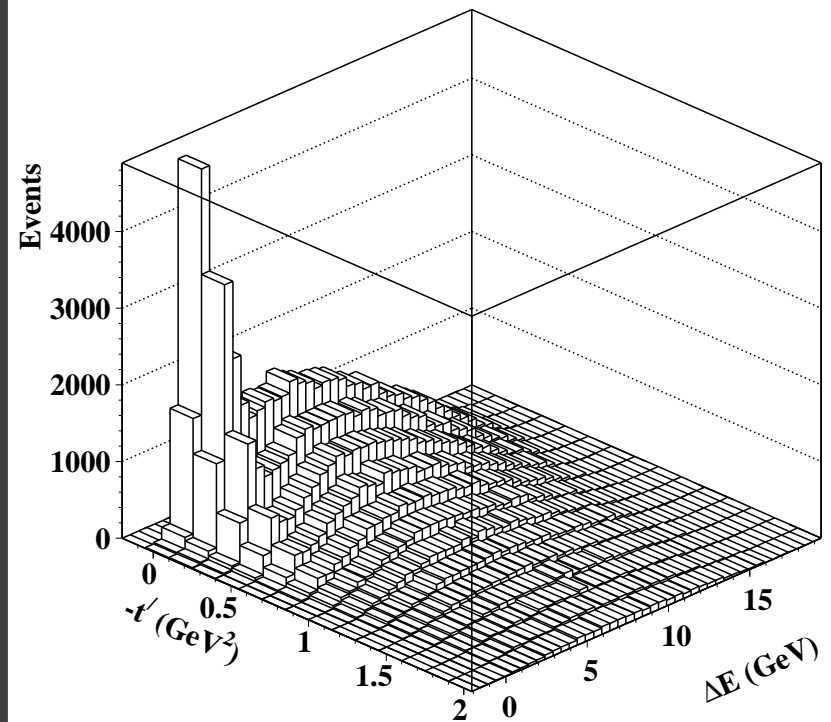
$$t' = t - t_0$$

- main contribution at small values of ΔE and t'

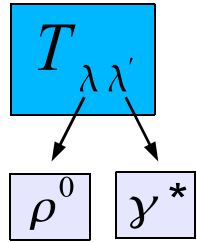
- non-exclusive events:

$$\Delta E > 0$$

- SIDIS background estimated by PYTHIA MC



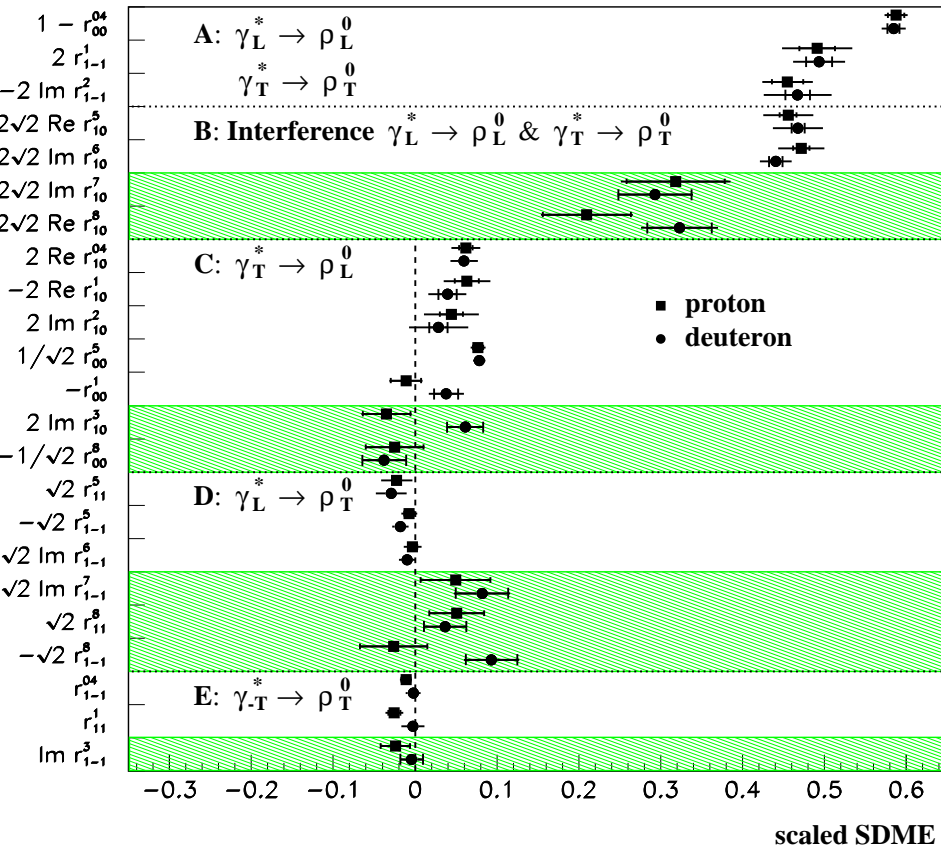
ρ^0 : unpolarized & beam-polarized SDMEs



SDMEs shown according to hierarchy of NPE helicity amplitudes:

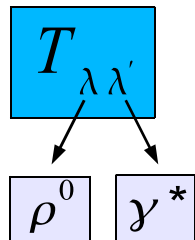
$$|T_{00}|^2 \sim |T_{11}|^2 \gg |T_{01}|^2 > |T_{10}|^2 \sim |T_{-11}|^2$$

-HERMES Collaboration: arXiv:0901.0701 (2009)-



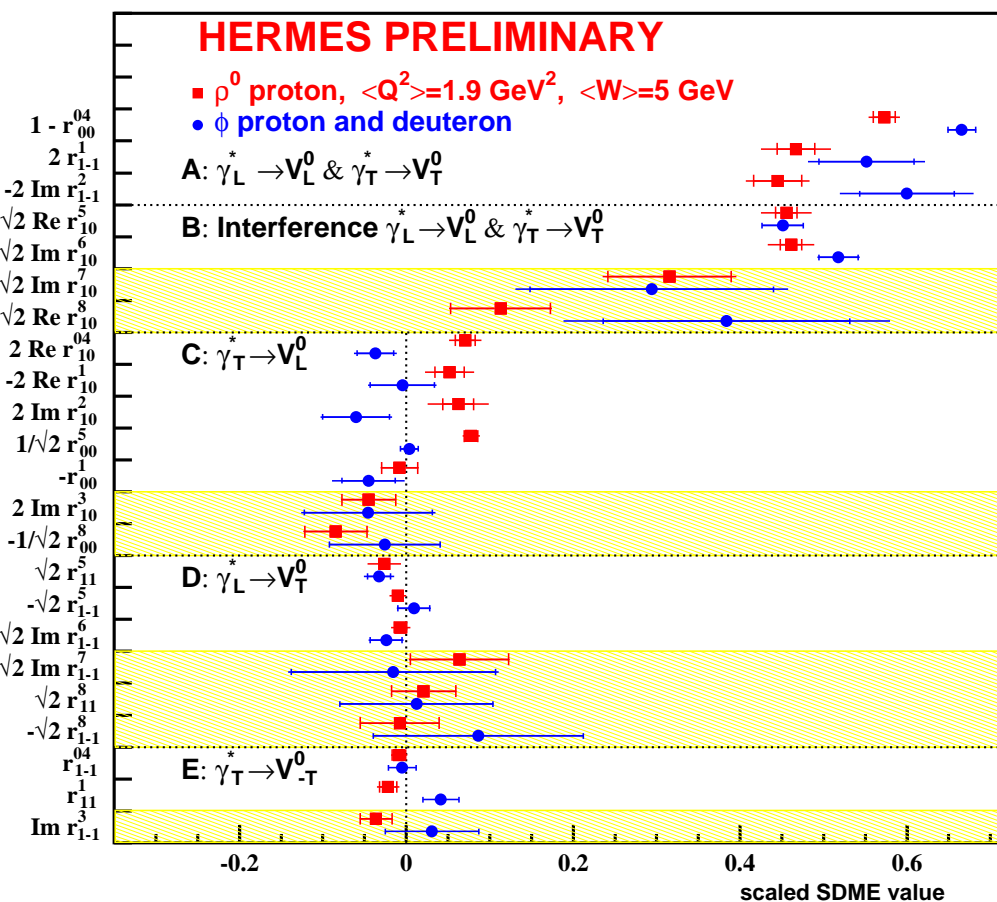
- unpolarized SDMEs: W_{UU}
- beam-polarized SDMEs: W_{UL}
- hierarchy confirmed experimentally
- proton and deuteron data consistent
- s -channel helicity conservation:
 - (ρ^0 conserves the helicity of γ^*)
 - significant $\gamma_L^* \rightarrow \rho_L^0$ and $\gamma_T^* \rightarrow \rho_T^0$
 - a substantial interference
- s -channel helicity violation
 - (vertical line corresponds to SCHC)
 - significant $\gamma_T^* \rightarrow \rho_L^0$
 - smaller $\gamma_L^* \rightarrow \rho_T^0$ and $\gamma_{-T}^* \rightarrow \rho_T^0$
 - 2 – 10 σ level violation

$\rho^0 - \phi$: comparison



SDMEs shown according to hierarchy of NPE helicity amplitudes:

$$|T_{00}|^2 \sim |T_{11}|^2 \gg |T_{01}|^2 > |T_{10}|^2 \sim |T_{-11}|^2$$



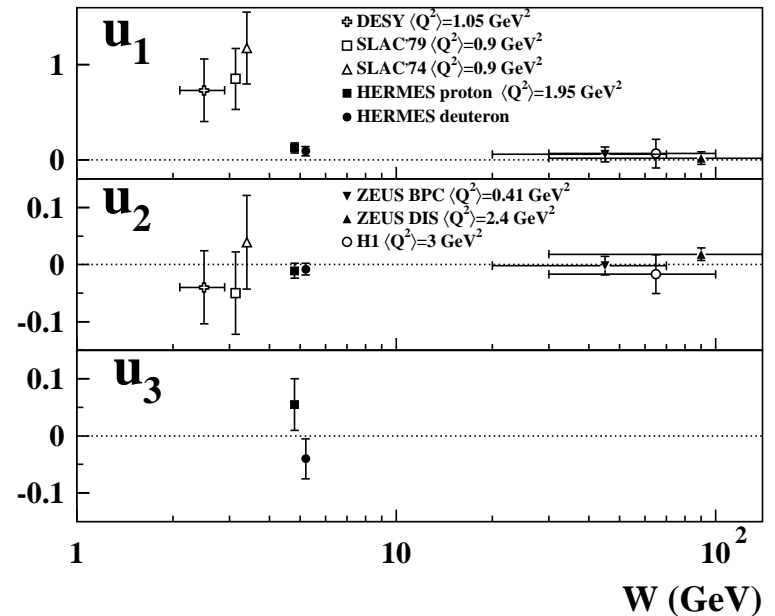
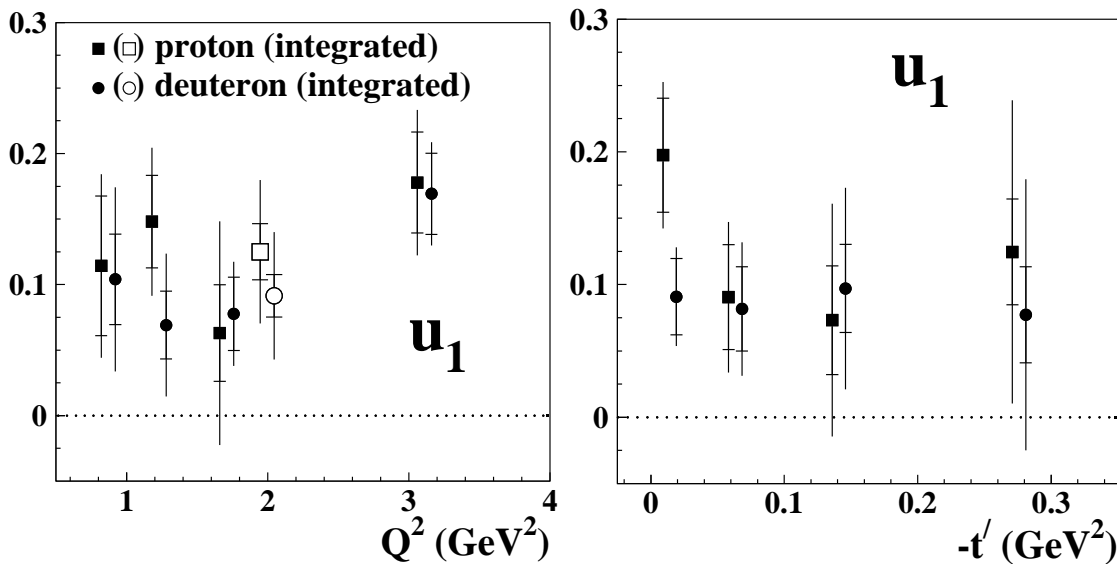
- unpolarized SDMEs: W_{UU}
- beam-polarized SDMEs: W_{UL}
- polarized SDMEs have been measured by HERMES for the first time
- no statistically significant difference between proton and deuteron
- no s-channel helicity violation
- hierarchy of amplitudes:
 $T_{00} \sim T_{11}$
 $T_{01} \approx T_{10} \approx T_{-11} \approx 0$

ρ^0 : observation of unnatural-parity exchange

 UPE contributions measured from SDMEs: *-HERMES Collaboration: arXiv:0901.0701 (2009)-*

$$u_1 = 1 - r_{00}^{04} + 2r_{1-1}^{04} - 2r_{11}^1 - 2r_{1-1}^1, \quad u_2 = r_{11}^5 + r_{1-1}^5, \quad u_3 = r_{11}^8 + r_{1-1}^8$$

 the combinations of SDMEs expected to be the zero in case of NPE dominance



UPE contribution is W -dependent



proton:

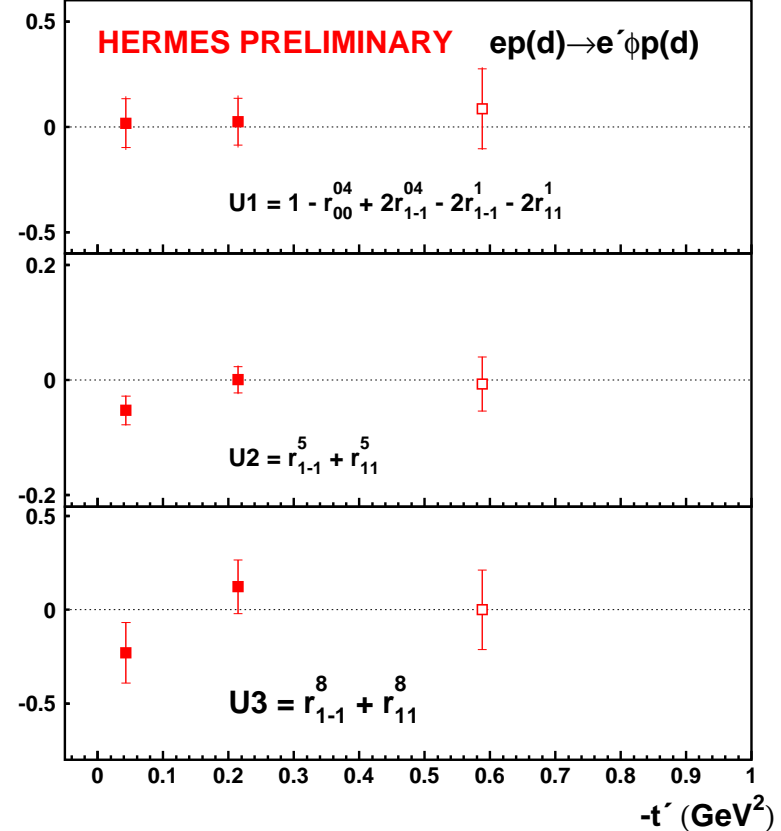
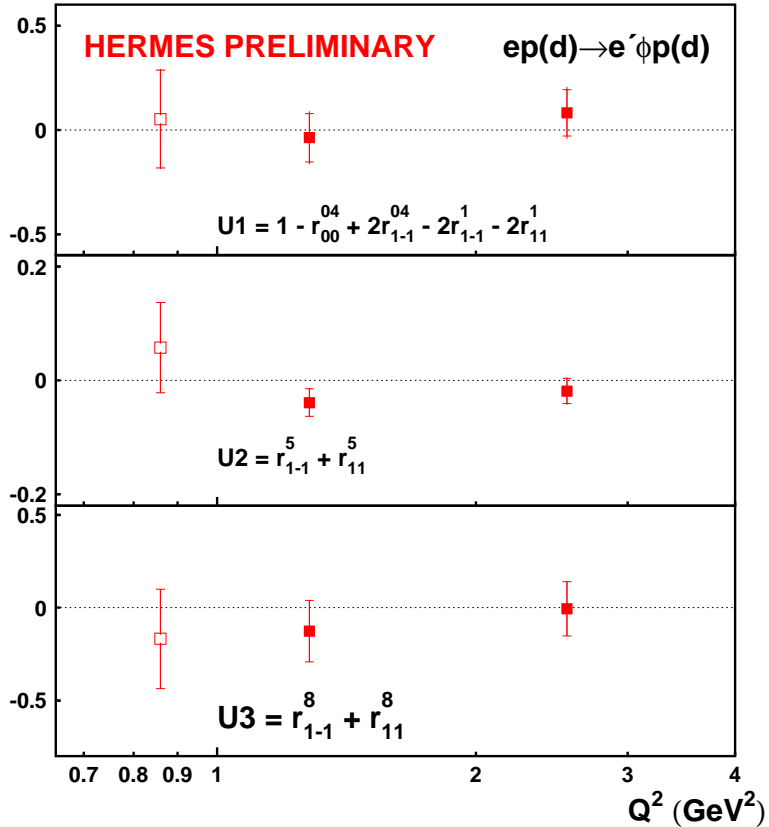
$$u_1 = 0.125 \pm 0.021_{stat} \pm 0.050_{sys}$$







deuteron:

$$u_1 = 0.091 \pm 0.016_{stat} \pm 0.046_{sys}$$

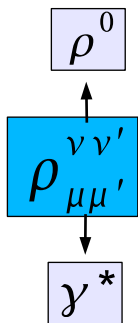
ϕ : observation of unnatural-parity exchange



-  $u_1 = 0.02 \pm 0.07_{stat} \pm 0.16_{sys}$
-  $u_2 = -0.03 \pm 0.01_{stat} \pm 0.03_{sys}$
-  $u_3 = -0.05 \pm 0.12_{stat} \pm 0.07_{sys}$
-  no signal of unnatural-parity exchange

expected since dominant contribution to the production is from two gluon exchange

'transverse' SDMEs: $n_{\mu\mu'}^{\nu\nu'}$ and $s_{\mu\mu'}^{\nu\nu'}$



-HERMES Collaboration: arXiv:0906.5160 (2009)-

transverse SDMEs: W_{UT}

measured for the first time

average kinematics:

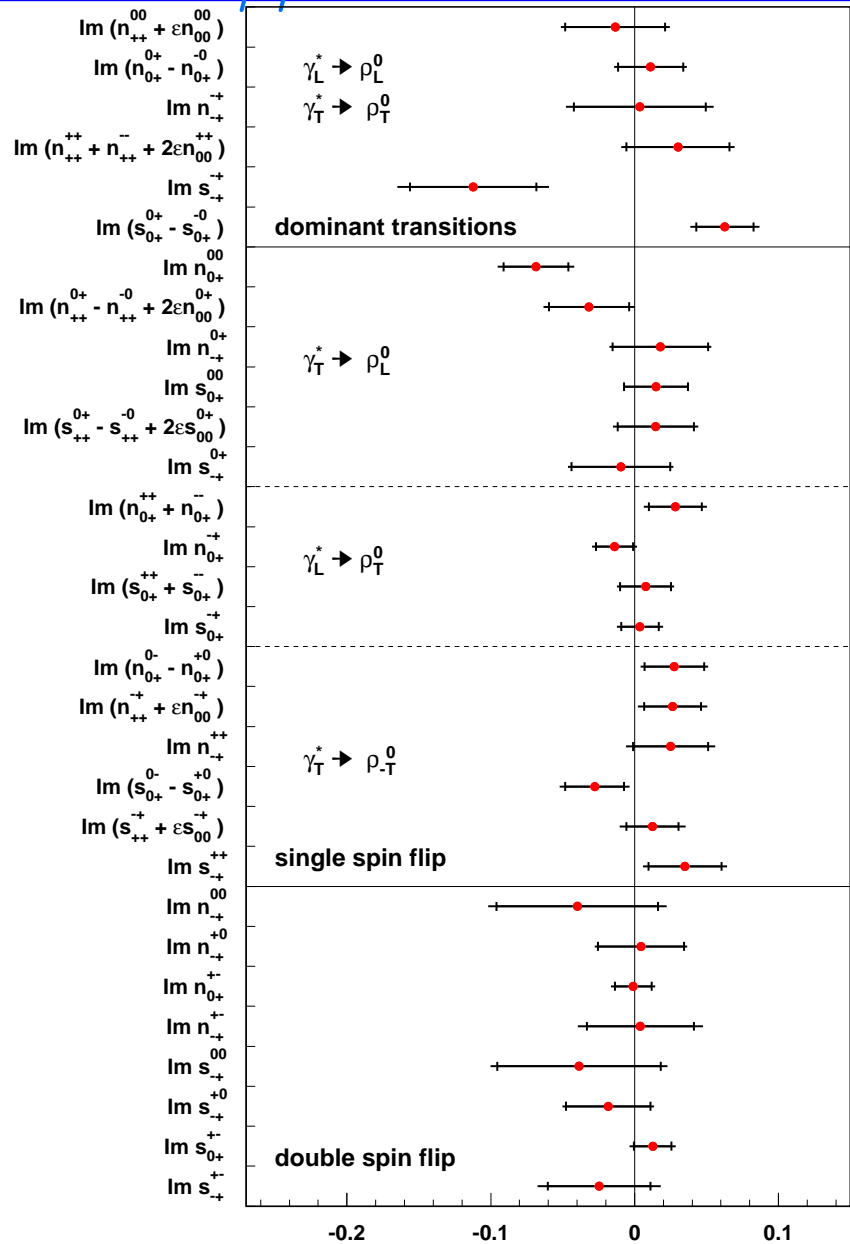
$$\langle -t' \rangle = 0.13 \text{ GeV}^2$$

$$\langle x_B \rangle = 0.09$$

$$\langle Q^2 \rangle = 2.0 \text{ GeV}^2$$

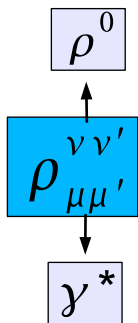
related to the proton helicity-flip amplitude

suppressed by a factor $\sqrt{-t}/2M_p$






SDME values

'transverse' SDMEs: $n_{\mu\mu'}^{\nu\nu'}$ and $s_{\mu\mu'}^{\nu\nu'}$



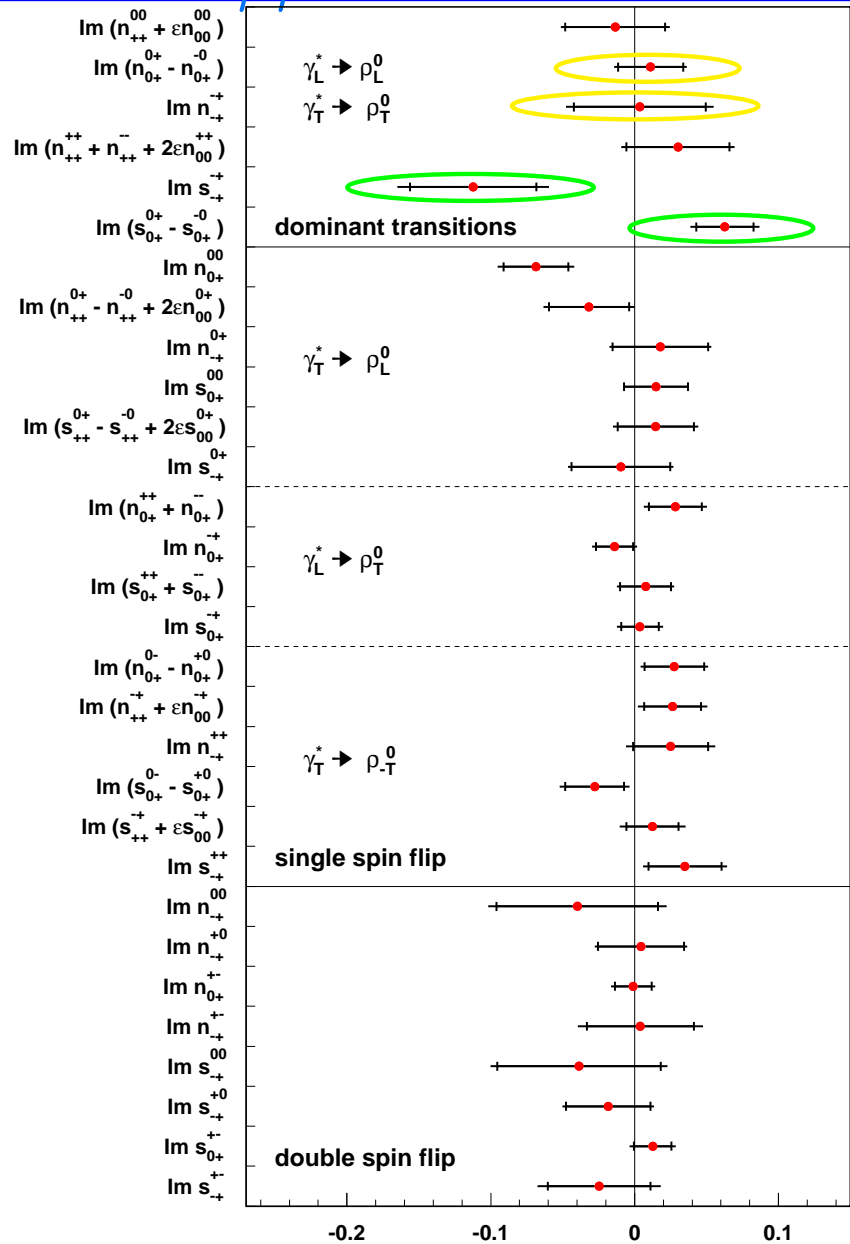
-HERMES Collaboration: arXiv:0906.5160 (2009)-

$$\gamma_L^* \rightarrow \rho_L^0 \text{ and } \gamma_T^* \rightarrow \rho_T^0$$

-  $\text{Im } s_{-+}^{\pm}$ and $\text{Im}(s_{0+}^{0+} - s_{0+}^{-0})$: deviate from 0 by 2.5σ
-  expected $s_{\mu\mu'}^{\nu\nu'} < n_{\mu\mu'}^{\nu\nu'}$ (if identical indices)
-  s_{-+}^{\pm} and $\text{Im } s_{0+}^{\pm}$ involve

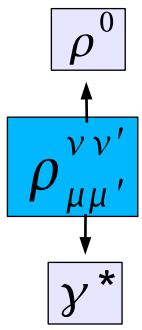
-Manaenkov (2008)-

-  the biggest NPE amplitudes N_{-+}^{\pm} or N_{0+}^{0+}
-  the biggest UPE amplitude U_{+-}^{\pm}
-  signal for unnatural-parity exchange
-  related to GPDs \tilde{H} and \tilde{E}






SDME values

'transverse' SDMEs: $n_{\mu\mu'}^{\nu\nu'}$ and $s_{\mu\mu'}^{\nu\nu'}$







-HERMES Collaboration: arXiv:0906.5160 (2009)-

$$\gamma_L^* \rightarrow \rho_L^0 \text{ and } \gamma_T^* \rightarrow \rho_T^0$$

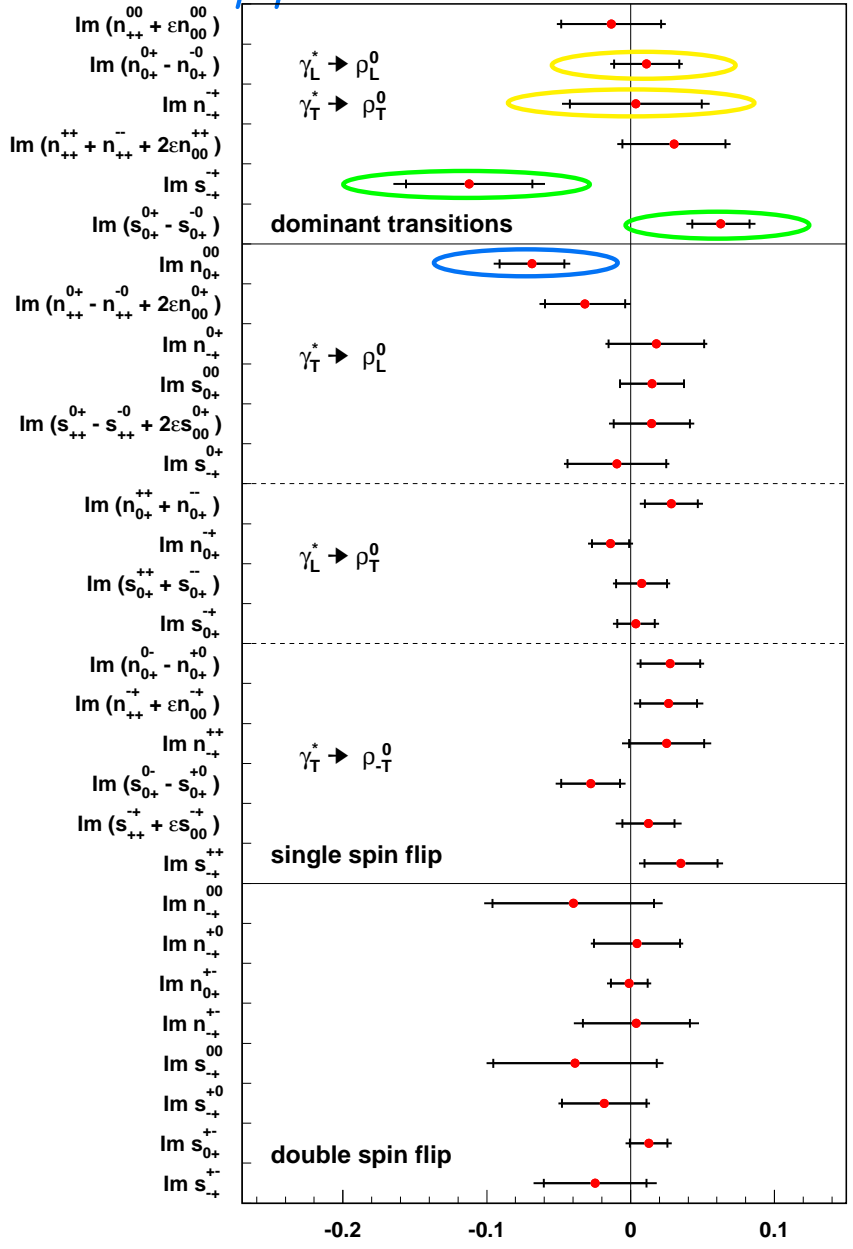
-  $\text{Im } s_{-+}^-$ and $\text{Im}(s_{0+}^{0+} - s_{0+}^{-0})$: deviate from 0 by 2.5σ
-  expected $s_{\mu\mu'}^{\nu\nu'} < n_{\mu\mu'}^{\nu\nu'}$ (if identical indices)
-  s_{-+}^- and $\text{Im } s_{0+}^{0+}$ involve

-Manaenkov (2008)-

-  the biggest NPE amplitudes N_{-+}^{-0} or N_{0+}^{0+}
-  the biggest UPE amplitude U_{+-}^{++}
-  signal for unnatural-parity exchange
-  related to GPDs \tilde{H} and \tilde{E}

$$\gamma_T^* \rightarrow \rho_L^0$$

-  $\text{Im } n_{0+}^{00}$: 2.5σ deviation from 0



SDME values



ρ^0 : transverse target-spin asymmetry

- theoretically at leading order in $1/Q$
($\gamma_L^* \rightarrow \rho_L^0$):

$$A_{UT}^{\sin(\phi-\phi_s)} = \frac{\text{Im } n_{00}^{00}}{u_{00}^{00}}$$

- asymmetry in terms of GPDs

$$A_{UT}^{\sin(\phi-\phi_s)} \propto \frac{E}{H} \propto \frac{E^q + E^g}{H^q + H^g}$$

- experimentally:

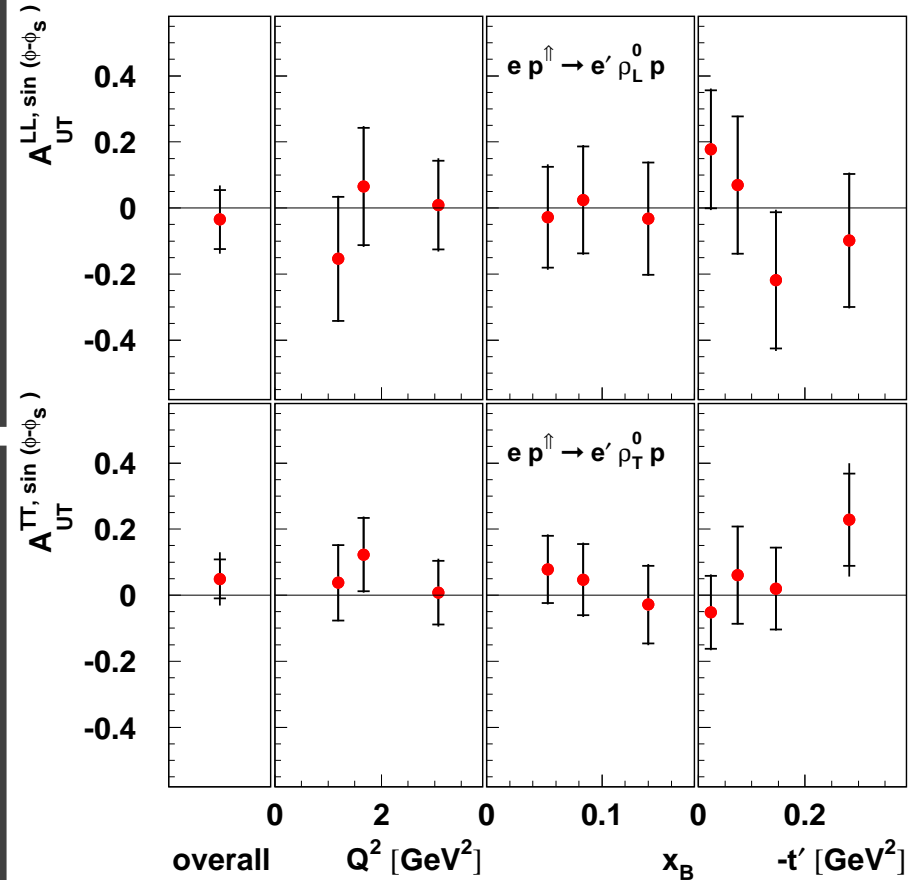
$$A_{UT}^{\gamma^*}(\phi, \phi_s) = \frac{\text{Im}(n_{++}^{00} + \epsilon n_{00}^{00})}{u_{++}^{00} + \epsilon u_{00}^{00}}$$

- u_{++}^{00} and n_{++}^{00} are expected to be negligible

- similarly, $\gamma_T^* \rightarrow \rho_T^0$:

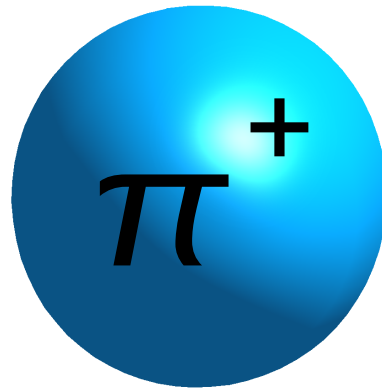
$$A_{UT}^{\gamma^*}(\phi, \phi_s) = \frac{\text{Im}(n_{++}^{++} + n_{++}^{--} + 2\epsilon n_{00}^{++})}{u_{++}^{++} + u_{++}^{--} + 2\epsilon u_{00}^{++}}$$

-HERMES Collaboration: arXiv:0906.5160 (2009)-



compatible with 0 overall value:

$$A_{UT}^{\rho_L^0, \sin(\phi-\phi_s)} = -0.033 \pm 0.058$$



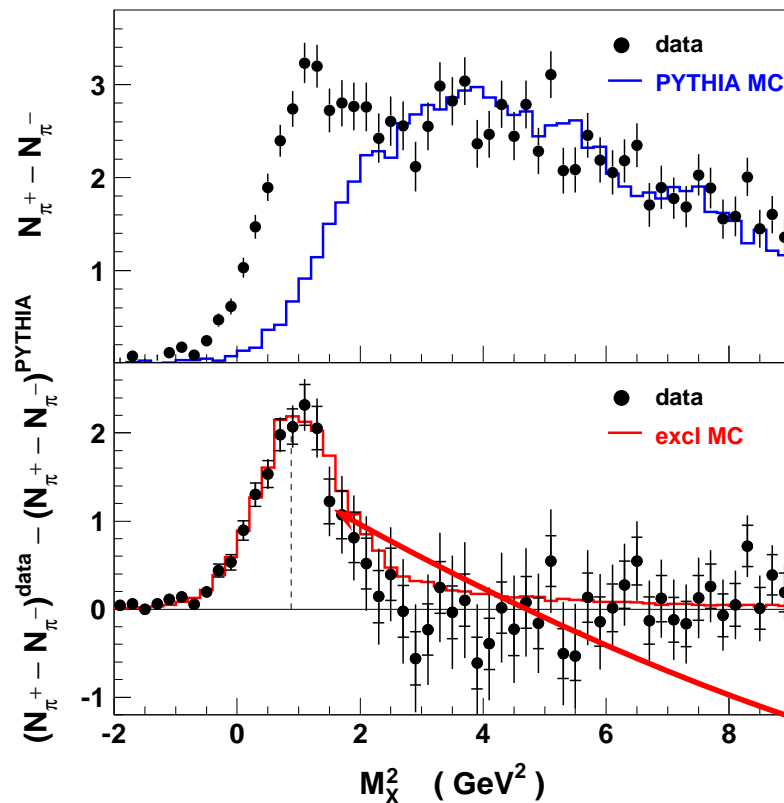
exclusive π^+ production: $ep \rightarrow e'\pi^+(n)$

- no recoil nucleon detection
- select exclusive π^+ reaction through the missing mass technique:

$$M_x^2 = (P_e + P_p - P_{e'} - P_{\pi^+})^2$$

$$N^{excl} = (\pi^+ - \pi^-)_{data} - (\pi^+ - \pi^-)^{MC}$$

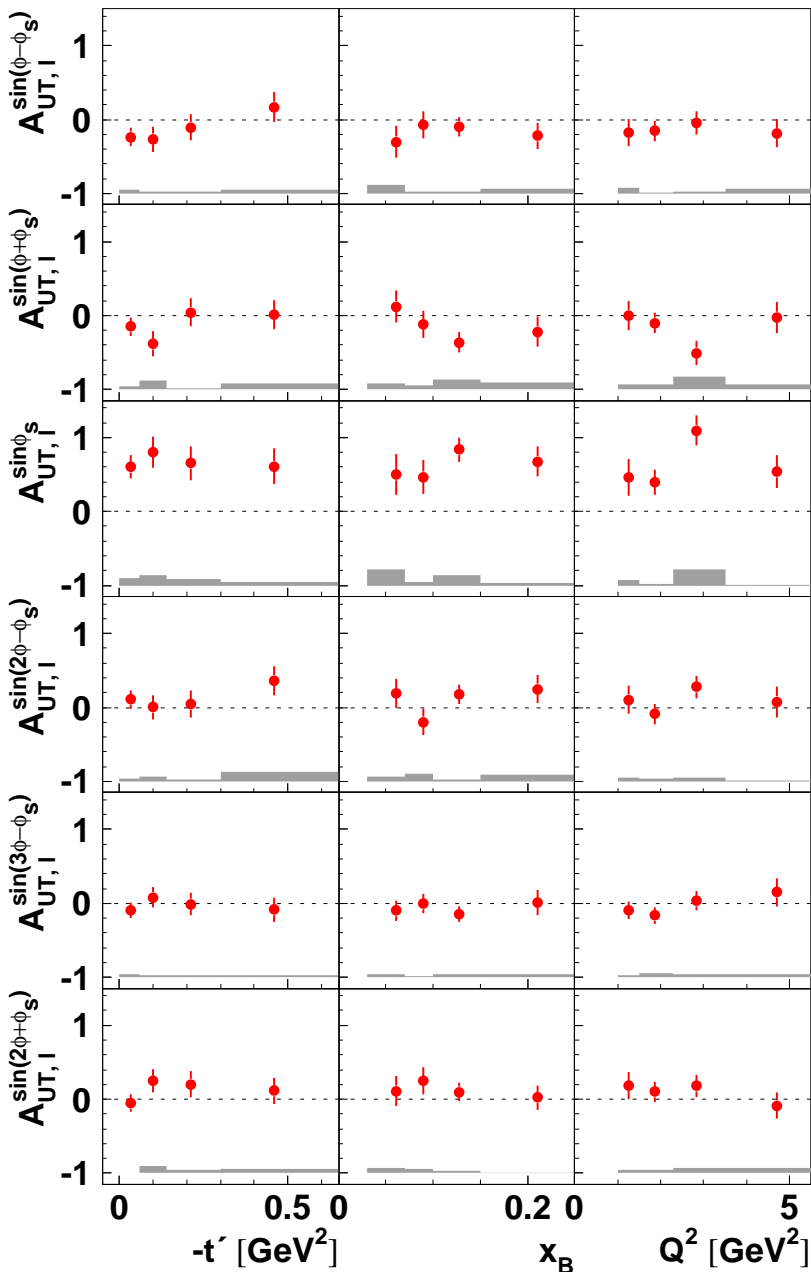
-HERMES collaboration arXiv:0707.0222 (2007)-



π^+	exclusive π^+	VM_{π^+}	SIDIS
π^-		VM_{π^-}	SIDIS

- $\pi^+ - \pi^-$ yield difference was used to subtract the non exclusive background
- exclusive peak centered at the nucleon mass
- exclusive MC based on GPD model

kinematic dependences of $A_{UT}^{\pi^+}$



-HERMES Collaboration: arXiv:0907.2596 (2009)-



6 azimuthal moments extracted according to

-Diehl, Sapeta (2005)-



average kinematics:

$$\langle -t' \rangle = 0.18 \text{ GeV}^2$$

$$\langle x_B \rangle = 0.13$$

$$\langle Q^2 \rangle = 2.38 \text{ GeV}^2$$



no γ_L^*/γ_T^* separation



small overall value for leading asymmetry

amplitude $A_{UT}^{\sin(\phi - \phi_s)}$



unexpected large overall value for asymmetry

amplitude $A_{UT}^{\sin \phi_s}$



other moments: consistent with 0

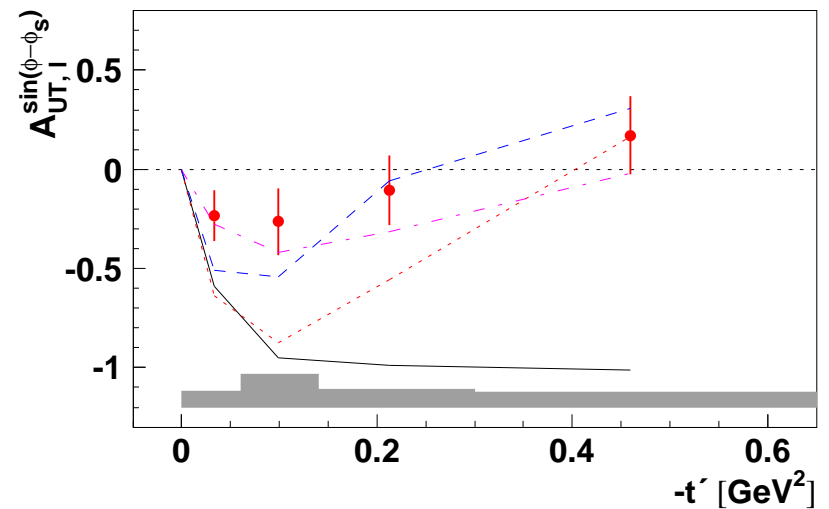


evidence of contributions from transversely polarized photons

theoretical interpretation of $A_{UT}^{\pi^+}$

leading azimuthal amplitude $A_{UT}^{\sin(\phi-\phi_s)}$

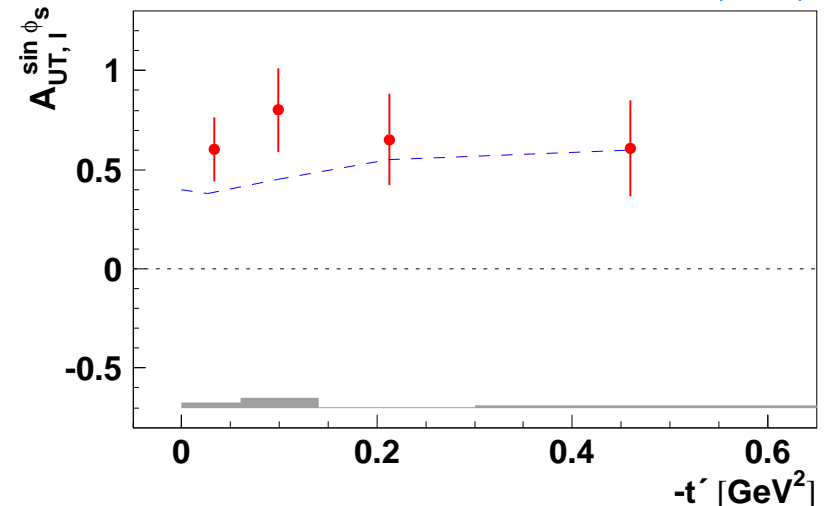
- not large asymmetry with possible sign change
- theoretical expectation: $A_{UT}^{\sin(\phi-\phi_s)} \propto \sqrt{-t'}$
- large negative asymmetry -Frankfurt et al. (2001)-
-Belitsky, Muller (2001)-
- are the differences due to γ_T^* ?
-Goloskokov, Kroll (2009)-
-Bechler, Muller (2009)-



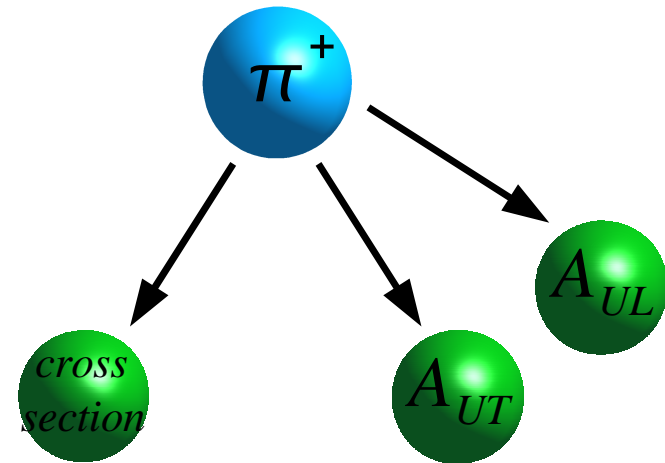
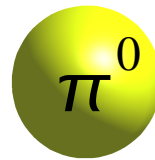
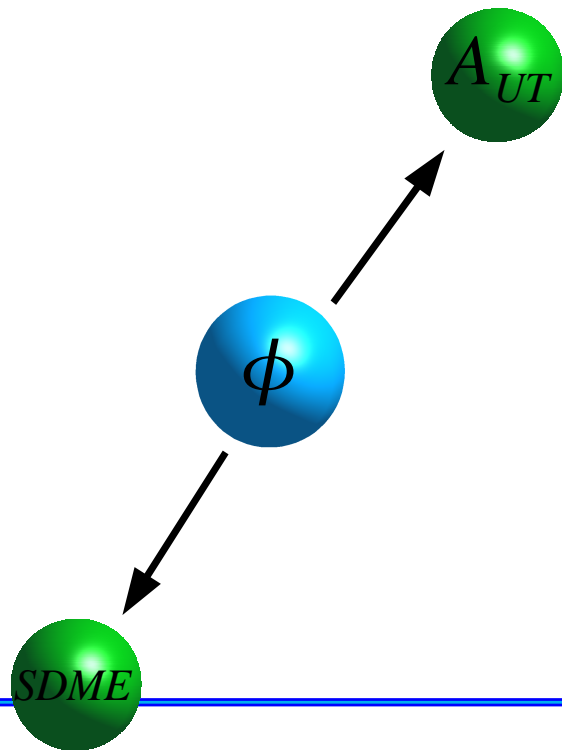
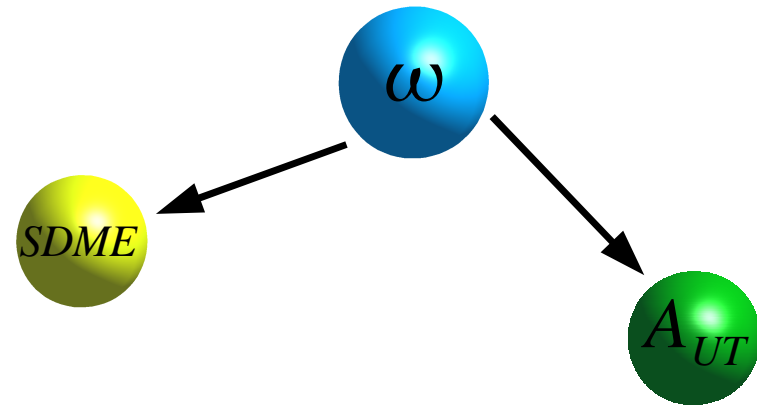
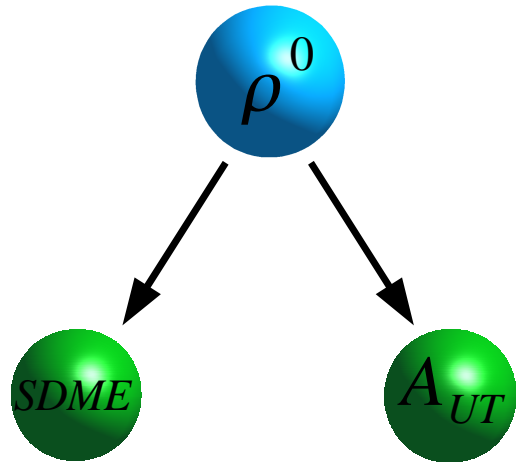
azimuthal amplitude $A_{UT}^{\sin \phi_s}$

- no turnover towards 0 for $t' \rightarrow 0$
- milde t -dependence
- can be explained only by γ_L^*/γ_T^* interference
- predictions $A_{UT}^{\sin \phi_s} \approx const$
- non-vanishing model predictions: contribution from H_T

-Goloskokov, Kroll (2009)-



GPDs, Meson Production and HERMES



backup slides

transverse target-spin asymmetry

$$\begin{aligned}\mathcal{A}_{UT}^{\text{DVCS}}(\phi, \phi_S) &= \sum_{n=0}^2 A_{UT, \text{DVCS}}^{\sin(\phi - \phi_S) \cos(n\phi)} \sin(\phi - \phi_S) \cos(n\phi) \\ &+ \sum_{n=1}^2 A_{UT, \text{DVCS}}^{\cos(\phi - \phi_S) \sin(n\phi)} \cos(\phi - \phi_S) \sin(n\phi) \\ \mathcal{A}_{UT}^{\text{I}}(\phi, \phi_S) &= \sum_{n=0}^2 A_{UT, \text{I}}^{\sin(\phi - \phi_S) \cos(n\phi)} \sin(\phi - \phi_S) \cos(n\phi) \\ &+ \sum_{n=1}^2 A_{UT, \text{I}}^{\cos(\phi - \phi_S) \sin(n\phi)} \cos(\phi - \phi_S) \sin(n\phi)\end{aligned}$$

longitudinal target polarization

$$\sigma(\phi, P_\ell, S_L) = \sigma_{UU}(\phi) \times [1 + P_\ell \mathcal{A}_{LU} + S_L \mathcal{A}_{UL}(\phi) + S_L P_\ell \mathcal{A}_{LL}(\phi)]$$

beam helicity asymmetry:

$$\mathcal{A}_{LU}(\phi) \equiv \frac{d\sigma^{\rightarrow} - d\sigma^{\leftarrow}}{d\sigma^{\rightarrow} + d\sigma^{\leftarrow}}$$

 projects the imaginary part of τ_{DVCS}

 no separate access to s_1^{DVCS} and s_1^I

longitudinal target-spin asymmetry:

$$\mathcal{A}_{UL}(\phi) \equiv \frac{(d\sigma^{\rightarrow\Rightarrow} + d\sigma^{\leftarrow\Rightarrow}) - (d\sigma^{\rightarrow\Leftarrow} + d\sigma^{\leftarrow\Leftarrow})}{(d\sigma^{\rightarrow\Rightarrow} + d\sigma^{\leftarrow\Rightarrow}) + (d\sigma^{\rightarrow\Leftarrow} + d\sigma^{\leftarrow\Leftarrow})}$$

 projects the imaginary part of τ_{DVCS}

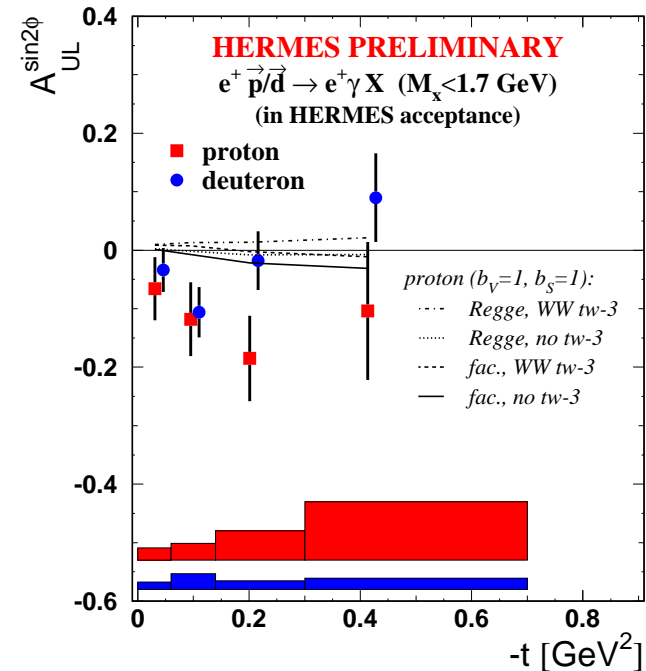
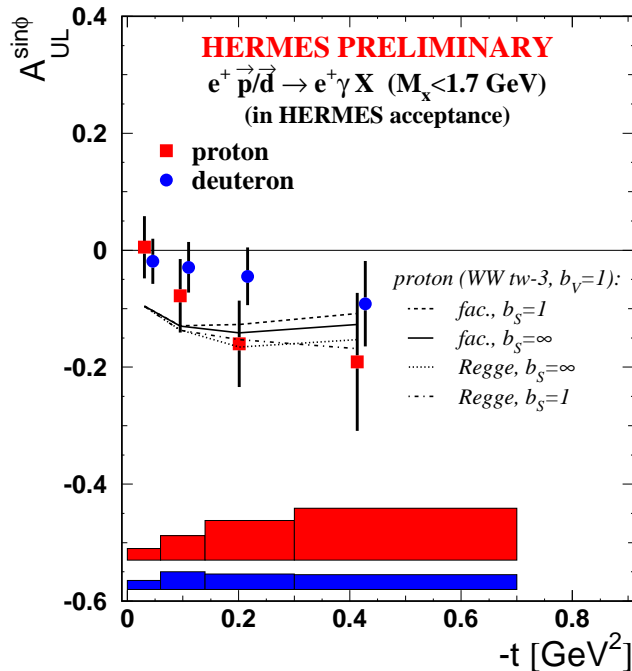
double-spin asymmetry:

$$\mathcal{A}_{LL}(\phi) \equiv \frac{(d\sigma^{\rightarrow\Rightarrow} + d\sigma^{\leftarrow\Leftarrow}) - (d\sigma^{\leftarrow\Rightarrow} + d\sigma^{\rightarrow\Leftarrow})}{(d\sigma^{\rightarrow\Rightarrow} + d\sigma^{\leftarrow\Leftarrow}) + (d\sigma^{\leftarrow\Rightarrow} + d\sigma^{\rightarrow\Leftarrow})}$$

 projects the real part of τ_{DVCS}

longitudinal target-spin asymmetry

$$A_{UL}(\phi) = \sum_{n=1}^2 A_{UL}^{\sin(n\phi)} \sin(n\phi) \propto \sum_{n=1}^2 s_n^I, s_n^{\text{DVCS}}$$



● s_1^I : twist-2

$$A_{UL}^{\sin\phi} \propto s_1^I \propto F_1 \text{Im}\tilde{\mathcal{H}}$$

● s_1^{DVCS} : twist-3

model in good agreement with data

unexpected large value

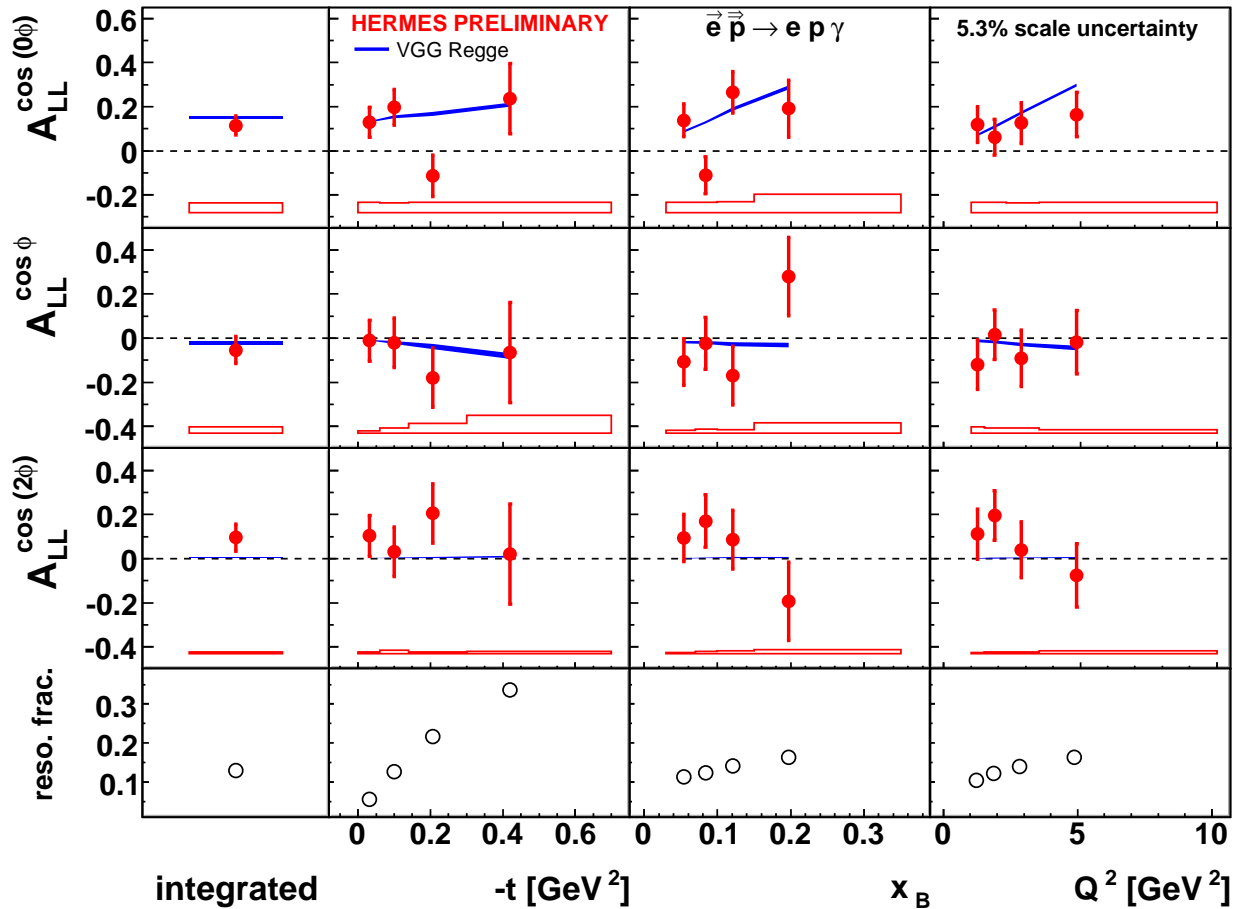
● s_2^I : quark twist-3 or gluon twist-2

● s_2^{DVCS} : twist-4

model does not describe the data

double-spin asymmetry

$$A_{LL}(\phi) \propto \sum_0^2 A_{LL}^{\cos(n\phi)} \cos(n\phi) \propto \sum_{n=0}^2 c_n^I, c_n^{\text{DVCS}}$$



twist-2: $\propto F_1 \text{Re}\tilde{\mathcal{H}}$

$$A_{LL}^{\cos 0\phi} \propto \begin{cases} c_0^{\text{DVCS}} \\ c_0^I \end{cases}$$



twist-2 / twist-3:

$$A_{LL}^{\cos \phi} \propto \begin{cases} c_1^{\text{DVCS}} \\ c_1^I \end{cases}$$

twist-3:

$$A_{LL}^{\cos 2\phi} \propto \begin{cases} c_2^I \end{cases}$$

model predictions:

-  the same model, as for BCA and BHA
-  in good agreement with data

ρ^0 : observation of unnatural-parity exchange

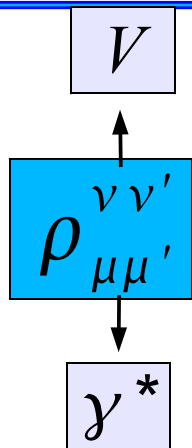
☉ UPE contributions measured from SDMEs:

$$u_1 = 1 - r_{00}^{04} + 2r_{1-1}^{04} - 2r_{11}^1 - 2r_{1-1}^1, \quad u_2 = r_{11}^5 + r_{1-1}^5, \quad u_3 = r_{11}^8 + r_{1-1}^8$$

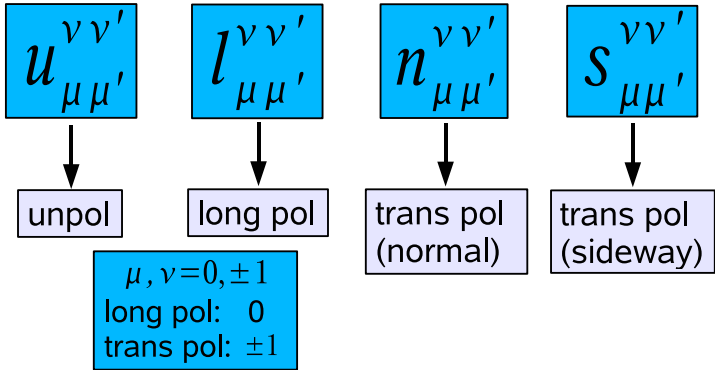
☉ UPE contributions expressed through amplitudes:

$$u_1 \propto \epsilon |U_{10}|^2 + 2|U_{11} + U_{1-1}|^2, \quad u_2 + iu_3 \propto (U_{11} + U_{1-1}) * U_{10}$$

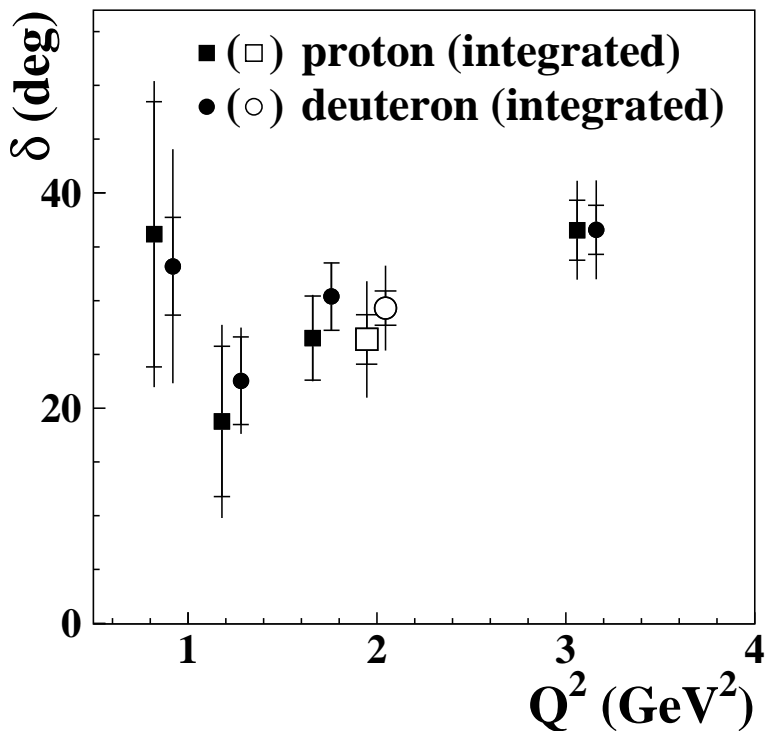
☉ the combinations of SDMEs expected to be the zero in case of NPE dominance:



$$\rho_{\mu\mu',\lambda\lambda'}^{\nu\nu'} \propto \sum_{\sigma} T_{\mu\lambda}^{\nu\sigma} (T_{\mu'\lambda'}^{\nu'\sigma})^*$$



ρ^0 : phase difference δ between T_{00} and T_{11}



-HERMES Collaboration: arXiv:0901.0701 (2009)-

 $|\delta|$ obtained from unpolarized SDMEs:

$$\cos \delta = \frac{2\sqrt{\epsilon}(\Re r_{10}^5 - \Im r_{10}^6)}{\sqrt{r_{00}^{04}(1 - r_{00}^{04} + r_{1-1}^1 - \Im r_{1-1}^2)}}$$

 sign of δ obtained from polarized SDMEs:
(for the first time)

$$\sin \delta = \frac{2\sqrt{\epsilon}(\Re r_{10}^8 - \Im r_{10}^7)}{\sqrt{r_{00}^{04}(1 - r_{00}^{04} + r_{1-1}^1 - \Im r_{1-1}^2)}}$$

 results on δ (in degrees):

 proton: $|\delta| = 26.4 \pm 2.3_{stat} \pm 4.9_{sys}$; $\delta = 30.6 \pm 5.0_{stat} \pm 2.4_{sys}$

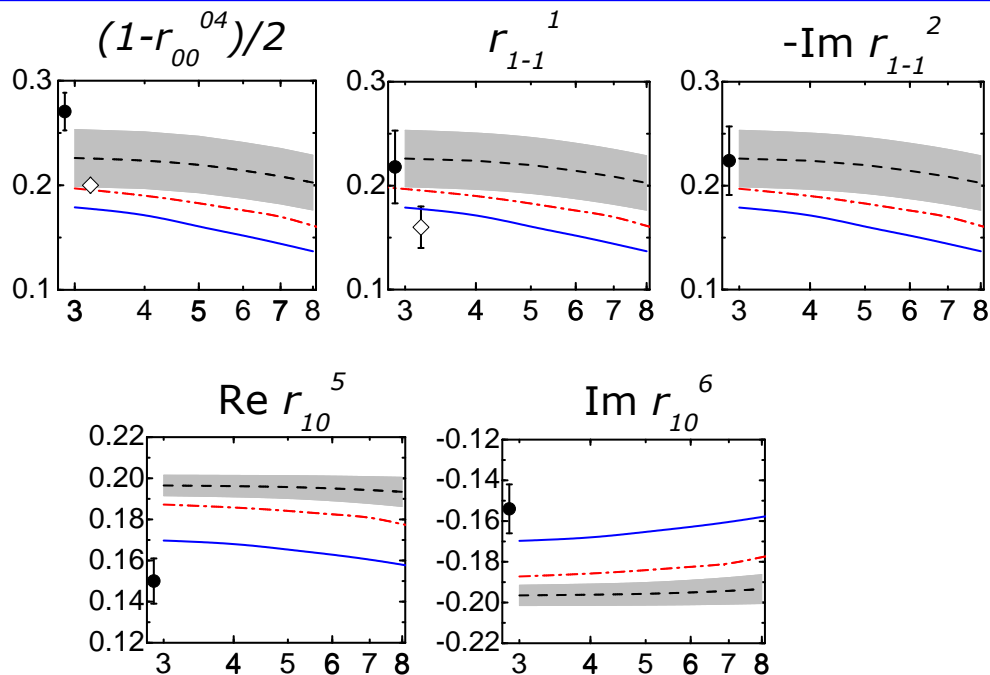
 deuteron: $|\delta| = 29.3 \pm 1.6_{stat} \pm 3.6_{sys}$; $\delta = 36.3 \pm 3.9_{stat} \pm 1.7_{sys}$

 values are consistent

 with each other

 with H1 results: $|\delta| = 21.5 \pm 4.3_{stat} \pm 5.3_{sys}$

comparison with a GPD model



-Goloskokov, Kroll (2007)-
 Q^2 -dependence calculated for 3 different W values:

$W = 5$ GeV (HERMES)

$W = 10$ GeV (COMPASS)

$W = 90$ GeV (H1, ZEUS)

$\gamma_L^* \rightarrow \rho_L^0$ and $\gamma_T^* \rightarrow \rho_T^0$

$1 - r_{00}^{04} \propto r_{1-1}^1 \propto -\Im r_{1-1}^2 \propto T_{11}$

describe data for various W -ranges

interference of $\gamma_L^* \rightarrow \rho_L^0$ and $\gamma_T^* \rightarrow \rho_T^0$

$r_{10}^5 \propto -\Im r_{10}^6 \propto T_{00}$ and T_{11} interference

model does not describe the data

model uses phase difference $\delta = 3.1$ degree between T_{00} and T_{11}

HERMES result: $\delta \approx 30$ degree

ρ^0 : comparison with GPD models

asymmetry in terms of GPDs

$$A_{UT}^{\sin(\phi-\phi_s)} \propto \frac{E}{H} \propto \frac{E^q + E^g}{H^q + H^g}$$

- Ellinghaus, Nowak, Vinnikov, Ye (2004)-

parametrization for H^q , $H^{\bar{q}}$, H^g

E^q is related to the total angular momenta J^u and J^d

▣ predictions for $J^d = 0$

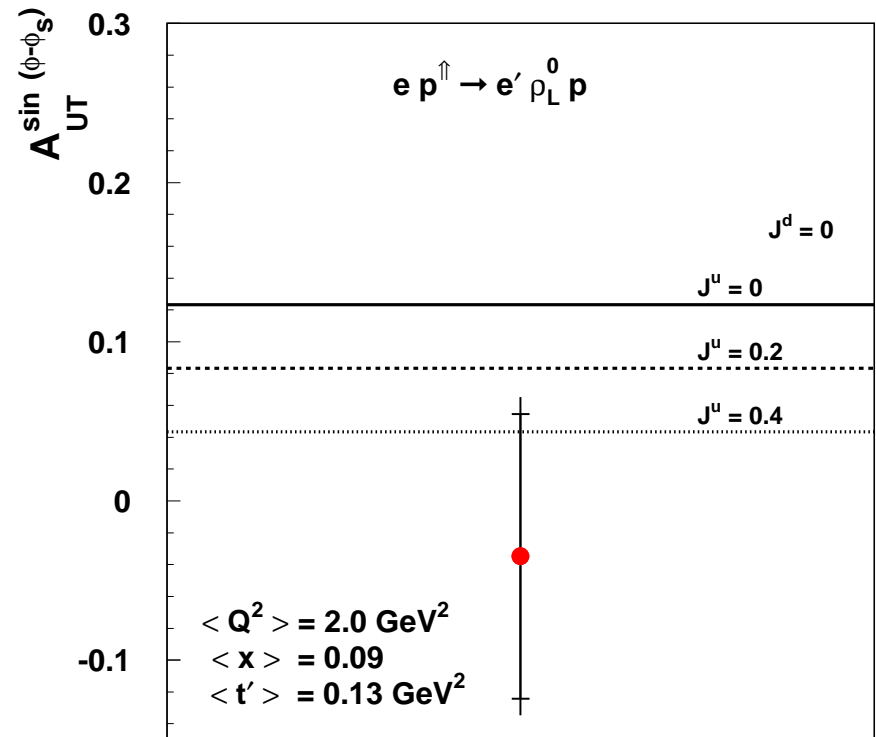
$E^{\bar{q}}$ and E^g are neglected

data favors positive J^u

▣ statistics too low to reliably determine the value of J^u and its uncertainty

within the statistical uncertainty in agreement with theoretical calculations

▣ indication of small E^g and $E^{\bar{q}}$?



overall

other GPD model calculations

- Goeke, Polyakov, Vanderhaeghen (1999)-

-Goloskokov, Kroll (2007)-

-Diehl, Kugler (2008)-

ω : transverse target-spin asymmetry

- 6 azimuthal moments extracted using integrated angular distributions

- due to low statistics no ω_L/ω_T separation

- predictions for large asymmetry

$$A_{UT}^{\sin(\phi-\phi_s)} \approx -0.10$$

- indication of negative $\sin(\phi - \phi_s)$ amplitude

$$A_{UT}^{\sin(\phi-\phi_s)} = -0.22 \pm 0.16_{stat} \pm 0.11_{sys}$$

- no contradiction with ρ^0 predictions

$$A_{UT}^{\rho^0, \sin(\phi-\phi_s)} \propto \Im \left\{ \frac{2E^u + E^d}{2H^u + H^d + Hg} \right\}$$

$$A_{UT}^{\omega, \sin(\phi-\phi_s)} \propto \Im \left\{ \frac{2E^u - E^d}{2H^u - H^d} \right\}$$

