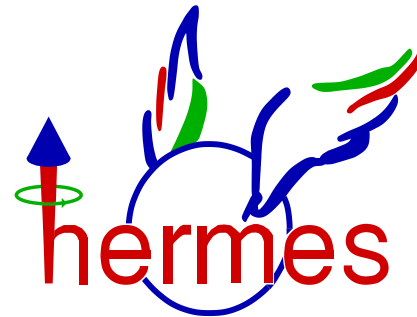

DVCS at HERMES

Orbital Angular Momentum of Partons in Hadrons, Trento, Italy, 2009

Ami Rostomyan

(on behalf of the HERMES collaboration)

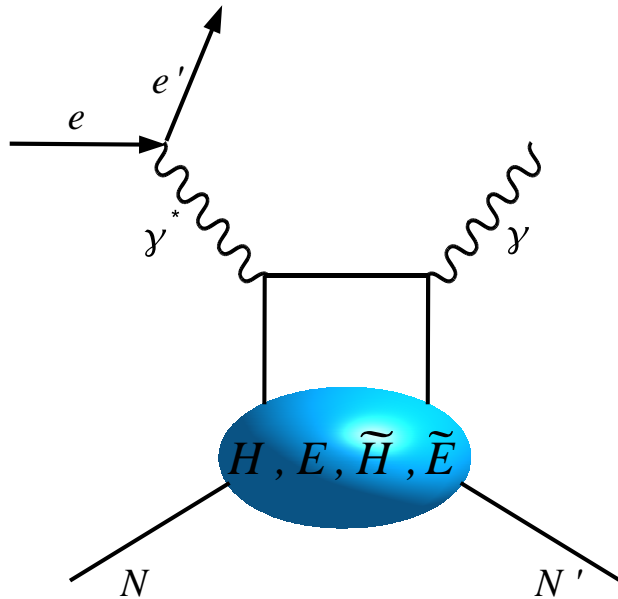


probing the orbital angular momentum

Generalised Parton Distributions (GPDs)

hard exclusive reactions

Deeply Virtual Compton Scattering (DVCS)



$(\gamma^* \rightarrow \gamma)$: $H, E, \tilde{H}, \tilde{E}$ (twist-2, chiral even)

H and \tilde{H} conserve the nucleon helicity

E and \tilde{E} describe the nucleon helicity flip

Ji relation

$$J_q = \frac{1}{2} \lim_{t \rightarrow 0} \int_{-1}^1 dx x [H_q(x, \xi, t) + E_q(x, \xi, t)]$$

$$= \frac{1}{2} \Delta \Sigma_q + L_q$$

why DVCS?

the cleanest probe of GPDs

theoretical accuracy at NNLO

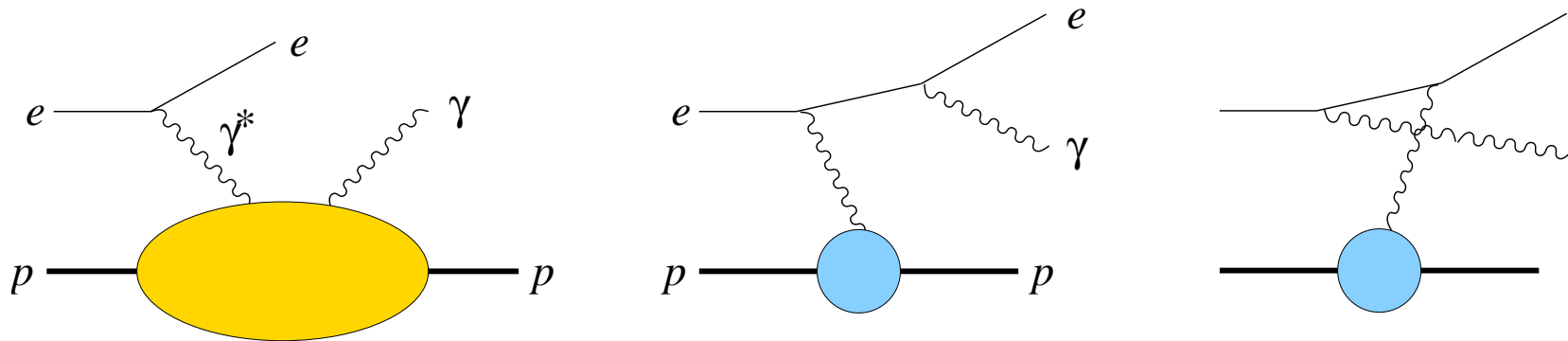
no gluons in the LO

Compton form factors

convolutions of GPDs ($F : H, E, \tilde{H}, \tilde{E}$) and hard scattering functions

$$\mathcal{F}(\xi, t) = \sum_q \int_{-1}^1 dx C_q(\xi, x) F^q(x, \xi, t)$$

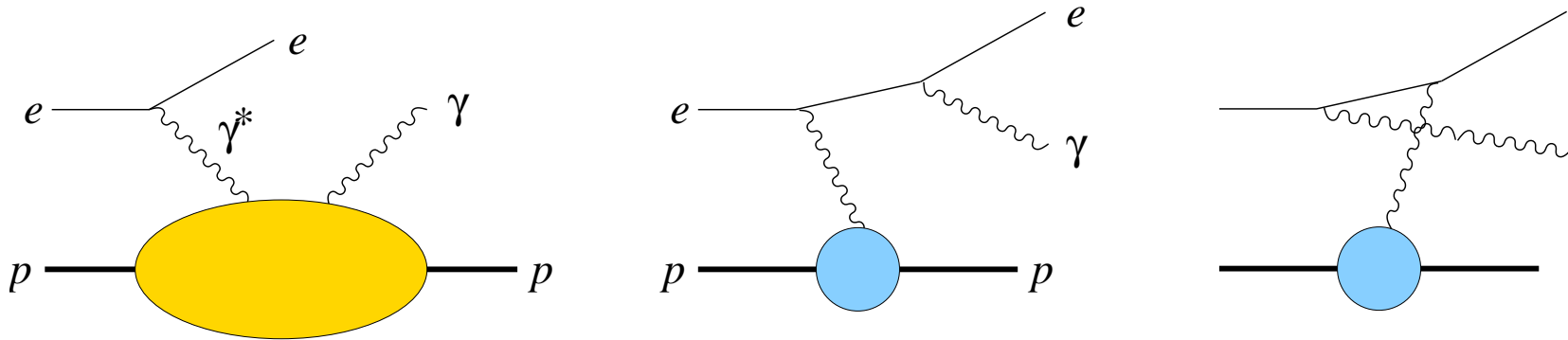
Deeply Virtual Compton Scattering (DVCS)



same initial and final states in DVCS and Bethe-Heitler \Rightarrow Interference!

$$\sigma_{ep} \propto |T_{BH}|^2 + |T_{DVCS}|^2 + \underbrace{T_{BH}T_{DVCS}^* + T_{BH}^*T_{DVCS}}_{\mathcal{I}}$$

Deeply Virtual Compton Scattering (DVCS)



same initial and final states in DVCS and Bethe-Heitler \Rightarrow Interference!

σ_{XY}

beam:
 P_l

target:
 $S_L S_T$

$$\sigma_{ep} \propto |T_{BH}|^2 + |T_{DVCS}|^2 + \underbrace{T_{BH} T_{DVCS}^* + T_{BH}^* T_{DVCS}}_{\mathcal{I}}$$

$$\begin{aligned} d\sigma \sim & d\sigma_{UU}^{BH} + e_l d\sigma_{UU}^I + d\sigma_{UU}^{DVCS} \\ & + e_l P_l d\sigma_{LU}^I + P_l d\sigma_{LU}^{DVCS} \\ & + e_l S_L d\sigma_{UL}^I + S_L d\sigma_{UL}^{DVCS} \\ & + e_l S_T d\sigma_{UT}^I + S_T d\sigma_{UT}^{DVCS} \\ & + P_l S_L d\sigma_{LL}^{BH} + e_l P_l S_L d\sigma_{LL}^I + P_l S_L d\sigma_{LL}^{DVCS} \\ & + P_l S_T d\sigma_{LT}^{BH} + e_l P_l S_T d\sigma_{LT}^I + P_l S_T d\sigma_{LT}^{DVCS} \end{aligned}$$

single spin terms: LU, UL, UT



no pure Bethe-Heitler contribution



project imaginary parts of Compton form factors

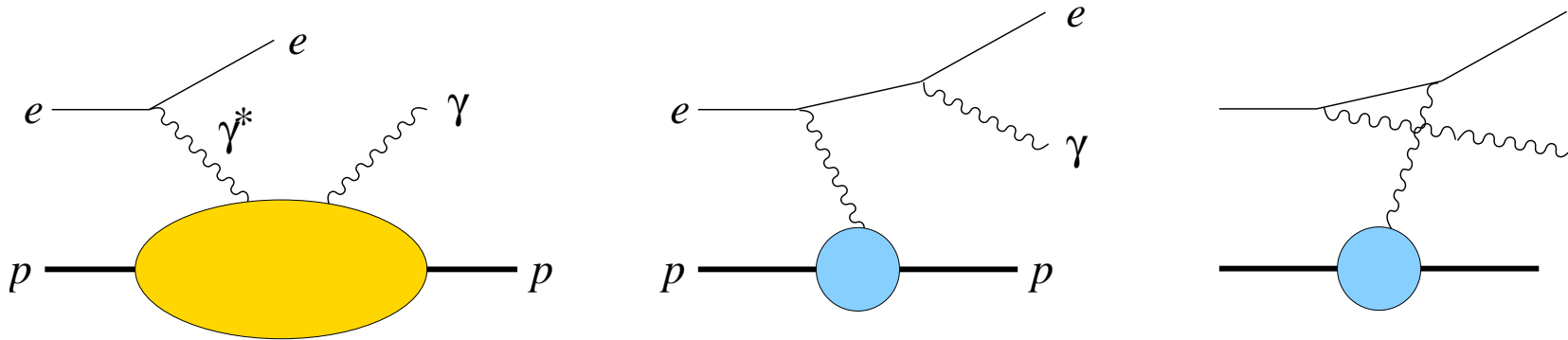
unpolarized and double-spin terms:

UU, LL, LT



project real parts of Compton form factors

Deeply Virtual Compton Scattering (DVCS)



same initial and final states in DVCS and Bethe-Heitler \Rightarrow Interference!

σ_{XY}

$$\sigma_{ep} \propto |\mathcal{T}_{BH}|^2 + |\mathcal{T}_{DVCS}|^2 + \underbrace{\mathcal{T}_{BH}\mathcal{T}_{DVCS}^* + \mathcal{T}_{BH}^*\mathcal{T}_{DVCS}}_{\mathcal{I}}$$

beam:
 P_L

target:
 $S_L S_T$

$$\begin{aligned} d\sigma \sim & d\sigma_{UU}^{BH} + e_l d\sigma_{UU}^I + d\sigma_{UU}^{DVCS} \\ & + e_l P_l d\sigma_{LU}^I + P_l d\sigma_{LU}^{DVCS} \\ & + e_l S_L d\sigma_{UL}^I + S_L d\sigma_{UL}^{DVCS} \\ & + e_l S_T d\sigma_{UT}^I + S_T d\sigma_{UT}^{DVCS} \\ & + P_l S_L d\sigma_{LL}^{BH} + e_l P_l S_L d\sigma_{LL}^I + P_l S_L d\sigma_{LL}^{DVCS} \\ & + P_l S_T d\sigma_{LT}^{BH} + e_l P_l S_T d\sigma_{LT}^I + P_l S_T d\sigma_{LT}^{DVCS} \end{aligned}$$


Bethe-Heitler contribution:

 calculated at QED

DVCS contribution:

 HERMES: $|\mathcal{T}_{DVCS}|^2 \ll |\mathcal{T}_{BH}|^2$

interference term:

 depend on a linear combination of Compton form factors

 access to GPD combinations through azimuthal asymmetries

express asymmetries in terms of Fourier coefficients

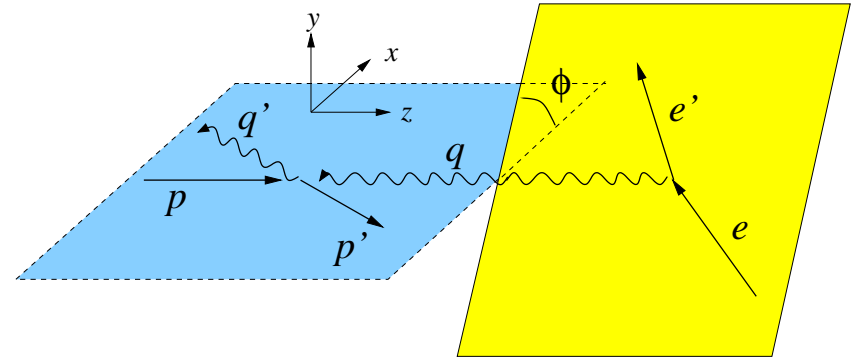
$$\sigma(\phi, P_\ell, e_\ell) = \sigma_{UU}(\phi) \times \left[1 + P_\ell A_{LU}^{DVCS}(\phi) + e_\ell P_\ell A_{LU}^I(\phi) + e_\ell A_C(\phi) \right]$$

Fourier expansion in azimuthal angle ϕ

$$|\tau_{BH}|^2 \propto \sum_{n=0}^2 c_n^{BH} \cos(n\phi)$$

$$|\tau_{DVCS}|^2 \propto \sum_{n=0}^2 c_n^{DVCS} \cos(n\phi) + P_\ell s_1^{DVCS} \sin \phi$$

$$I \propto \sum_{n=0}^3 c_n^I \cos(n\phi) + \sum_{n=1}^2 P_\ell s_n^I \sin(n\phi)$$



express asymmetries in terms of Fourier coefficients

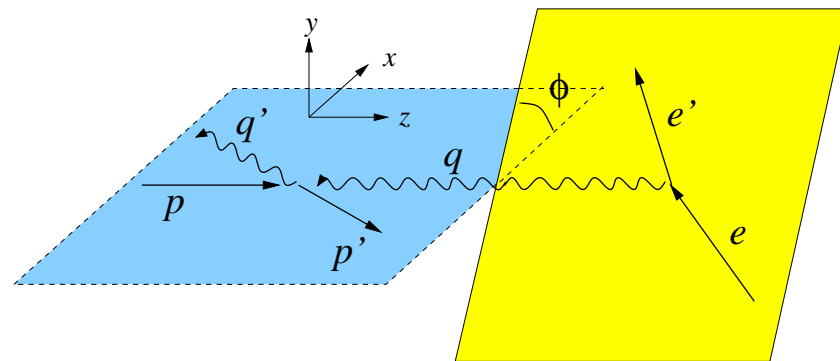
$$\sigma(\phi, P_\ell, e_\ell) = \sigma_{UU}(\phi) \times \left[1 + P_\ell A_{LU}^{DVCS}(\phi) + e_\ell P_\ell A_{LU}^I(\phi) + e_\ell A_C(\phi) \right]$$

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$$I \propto \sum_{n=0}^3 c_n^I \cos(n\phi) + \sum_{n=1}^2 P_\ell s_n^I \sin(n\phi)$$



$$c_1^I \propto F_1 \text{Re}\mathcal{H}$$

$$c_0^I \propto -\frac{-t}{Q} c_1^I$$

$$s_1^I \propto F_1 \text{Im}\mathcal{H}$$

express asymmetries in terms of Fourier coefficients

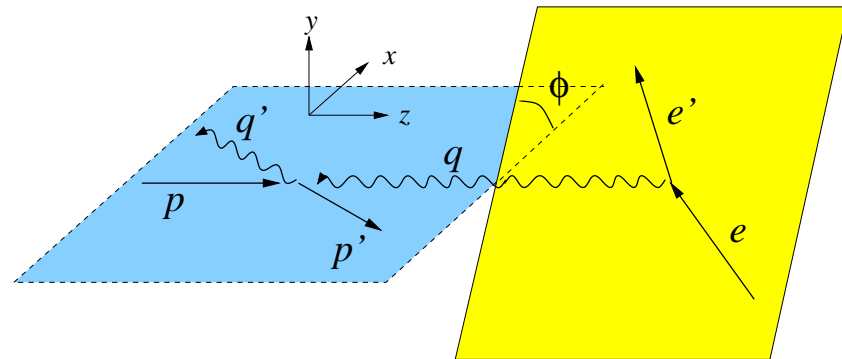
$$\sigma(\phi, P_\ell, e_\ell) = \sigma_{UU}(\phi) \times \left[1 + P_\ell A_{LU}^{DVCS}(\phi) + e_\ell P_\ell A_{LU}^I(\phi) + e_\ell A_C(\phi) \right]$$

Fourier expansion in azimuthal angle ϕ

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$$I \propto \sum_{n=0}^3 c_n^I \cos(n\phi) + \sum_{n=1}^2 P_\ell s_n^I \sin(n\phi)$$



DVCS term:

azimuthal modulation	$\gamma^*(\mu) \rightarrow \gamma(\mu')$	relative order
constant	$+1 \rightarrow +1$	1
$\cos \phi, \sin \phi$	$0 \rightarrow +1$	$1/Q$
$\cos 2\phi, \sin 2\phi$	$-1 \rightarrow +1$	1 (gluon GPDs) $1/Q^2$ (quark GPDs)

$$c_1^I \propto F_1 \text{Re}\mathcal{H}$$

$$c_0^I \propto -\frac{-t}{Q} c_1^I$$

$$s_1^I \propto F_1 \text{Im}\mathcal{H}$$

express asymmetries in terms of Fourier coefficients

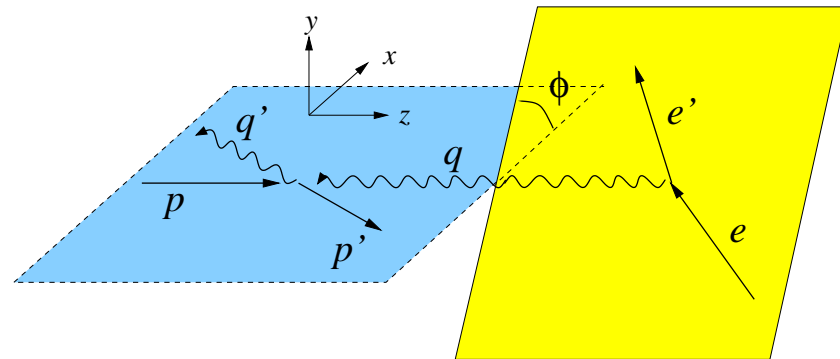
$$\sigma(\phi, P_\ell, e_\ell) = \sigma_{UU}(\phi) \times \left[1 + P_\ell A_{LU}^{DVCS}(\phi) + e_\ell P_\ell A_{LU}^I(\phi) + e_\ell A_C(\phi) \right]$$

Fourier expansion in azimuthal angle ϕ

$$|\tau_{BH}|^2 \propto \sum_{n=0}^2 c_n^{BH} \cos(n\phi)$$

$$|\tau_{DVCS}|^2 \propto \sum_{n=0}^2 c_n^{DVCS} \cos(n\phi) + P_\ell s_1^{DVCS} \sin \phi$$

$$I \propto \sum_{n=0}^3 c_n^I \cos(n\phi) + \sum_{n=1}^2 P_\ell s_n^I \sin(n\phi)$$



interference term:

azimuthal modulation	$\gamma^*(\mu) \rightarrow \gamma(\mu')$	relative order
constant	+1 \rightarrow +1	1/Q
$\cos \phi, \sin \phi$	+1 \rightarrow +1	1
$\cos 2\phi, \sin 2\phi$	0 \rightarrow +1	1/Q
$\cos 3\phi, \sin 3\phi$	-1 \rightarrow +1	1/Q ² or α_s

$$c_1^I \propto F_1 \text{Re}\mathcal{H}$$

$$c_0^I \propto -\frac{t}{Q} c_1^I$$

$$s_1^I \propto F_1 \text{Im}\mathcal{H}$$

DVCS at HERMES (pre-recoil data)

$$e + p \rightarrow e' + \gamma + p'$$

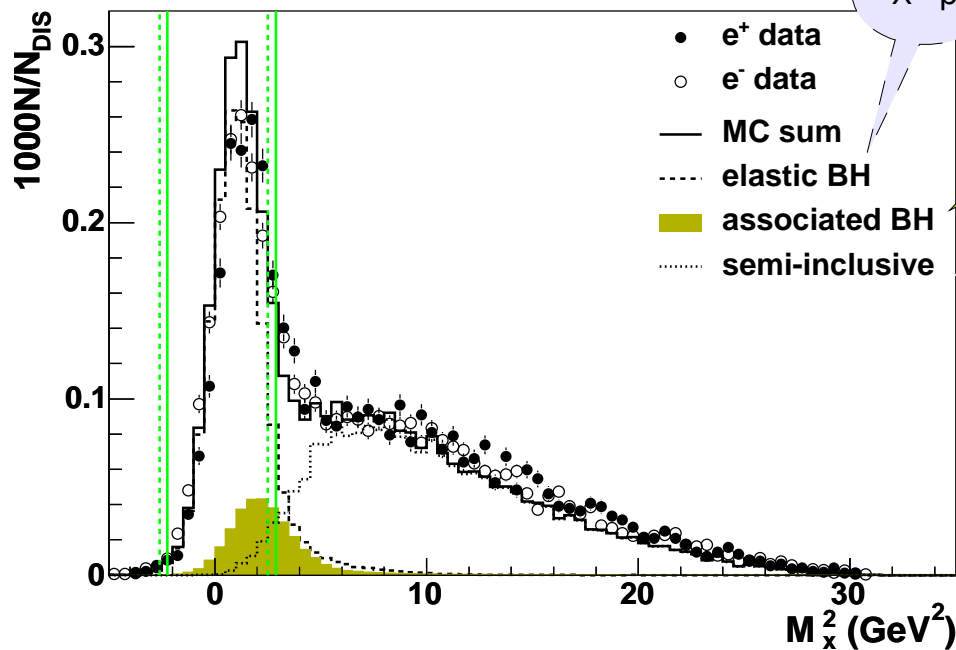
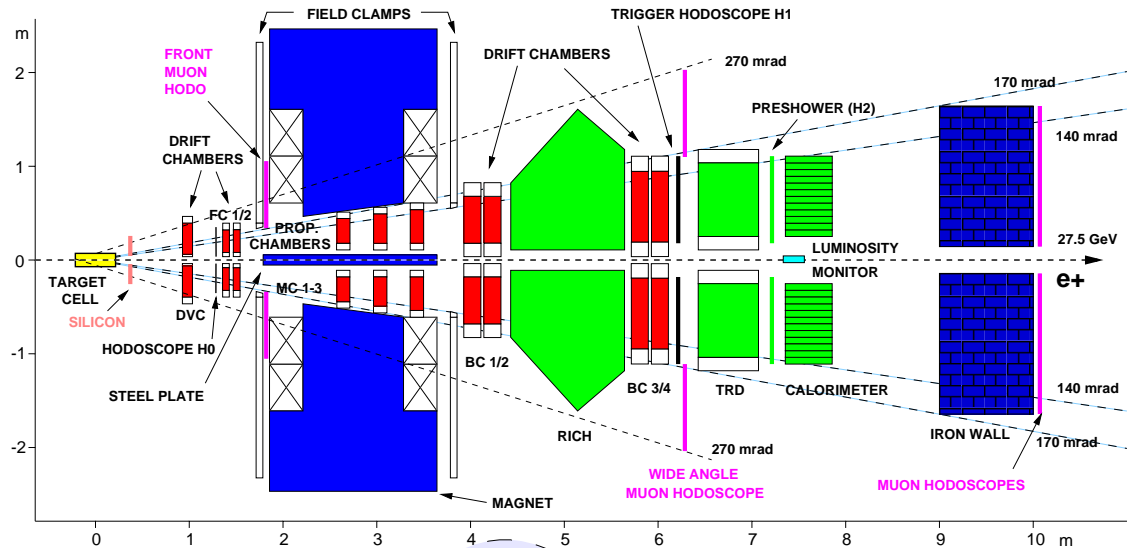


detected particles:
lepton and photon



missing mass technique for
 $ep \rightarrow e'\gamma X$:

$$M_X^2 = (p + e - e' - \gamma)^2$$



$X=p$

Resonant excitation:
 $X=\Delta^+$

$X=\pi^0 + \dots$

unpolarized-target asymmetries

$$\sigma(\phi, P_\ell, e_\ell) = \sigma_{UU}(\phi) \times \left[1 + P_\ell \mathcal{A}_{LU}^{DVCS}(\phi) + e_\ell P_\ell \mathcal{A}_{LU}^I(\phi) + e_\ell \mathcal{A}_C(\phi) \right]$$

beam-helicity asymmetry (single charge):

$$\mathcal{A}_{LU}(\phi) \equiv \frac{d\sigma^{\rightarrow} - d\sigma^{\leftarrow}}{d\sigma^{\rightarrow} + d\sigma^{\leftarrow}}$$

- projects the imaginary part of τ_{DVCS}
- no separate access to s_1^{DVCS} and s_1^I

beam-helicity asymmetry (new approach):

- charge-difference beam-helicity asymmetry

$$\mathcal{A}_{LU}^I(\phi) \equiv \frac{(d\sigma^{+\rightarrow} - d\sigma^{+\leftarrow}) - (d\sigma^{-\rightarrow} - d\sigma^{-\leftarrow})}{(d\sigma^{+\rightarrow} + d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} + d\sigma^{-\leftarrow})}$$

- charge-averaged beam-helicity asymmetry

$$\mathcal{A}_{LU}^{DVCS}(\phi) \equiv \frac{(d\sigma^{+\rightarrow} - d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} - d\sigma^{-\leftarrow})}{(d\sigma^{+\rightarrow} + d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} + d\sigma^{-\leftarrow})}$$

- s_1^{DVCS} and s_1^I can be disentangled

beam-charge asymmetry:

$$\mathcal{A}_C(\phi) \equiv \frac{d\sigma^+ - d\sigma^-}{d\sigma^+ + d\sigma^-}$$

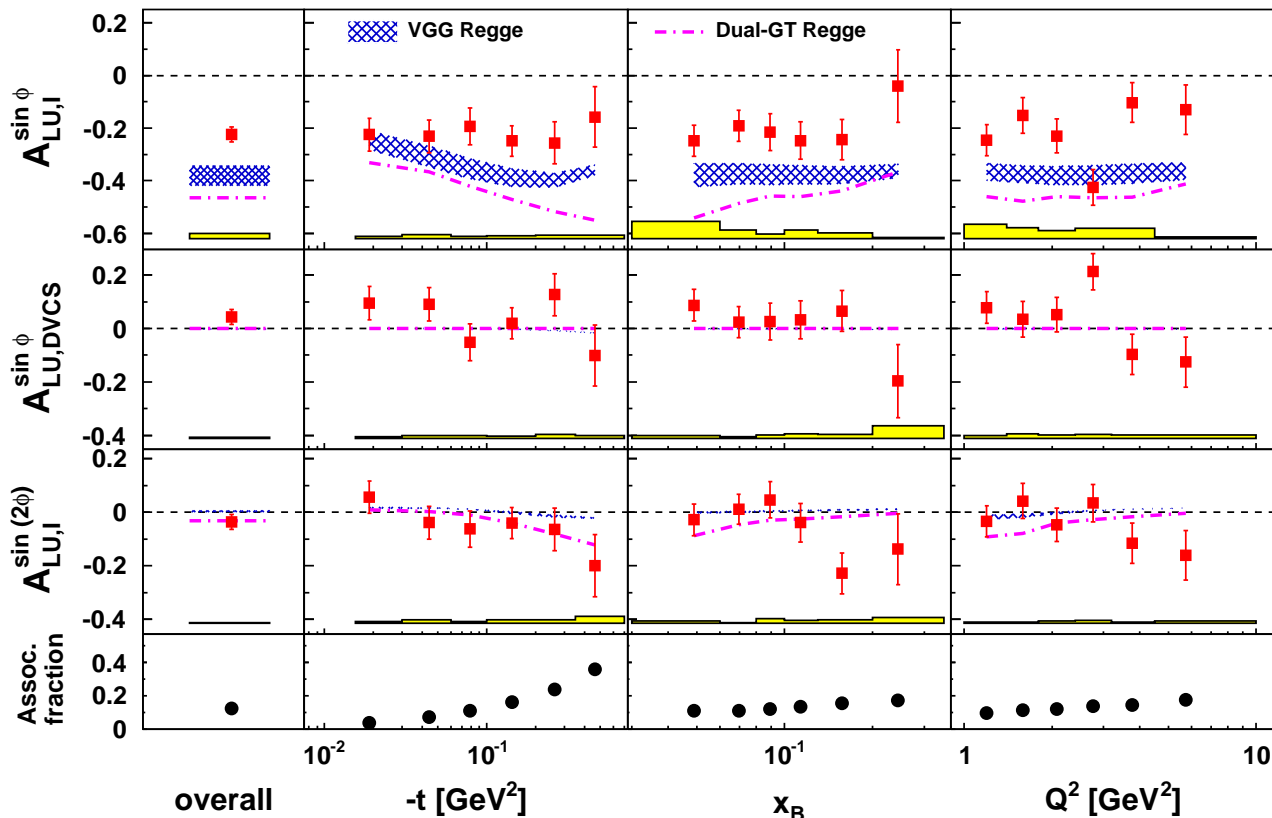
- projects the real part of τ_{DVCS}

beam helicity asymmetry

$$A_{LU}^I(\phi) = \sum_{n=1}^2 A_{LU,I}^{\sin(n\phi)} \sin(n\phi) \propto \sum_{n=1}^2 s_n^I \sin(n\phi)$$

$$A_{LU,DVCS}^{\sin\phi} \propto s_1^{\text{DVCS}} \sin\phi$$

-HERMES Collaboration: arXiv:0909.3587 (2009)-



$$A_{LU,I}^{\sin\phi}$$



twist-2:

$$\propto F_1 \text{Im}\mathcal{H}$$



large overall value



no kin. dependencies

$$A_{LU,DVCS}^{\sin\phi}, A_{LU,I}^{\sin 2\phi}$$



twist-3



overall value

compatible with 0



no kin. dependencies



overshoot the magnitude of $A_{LU,I}^{\sin\phi}$ by a factor of 2



describe the shape of kin dependencies on x_B and Q^2 , but not on t

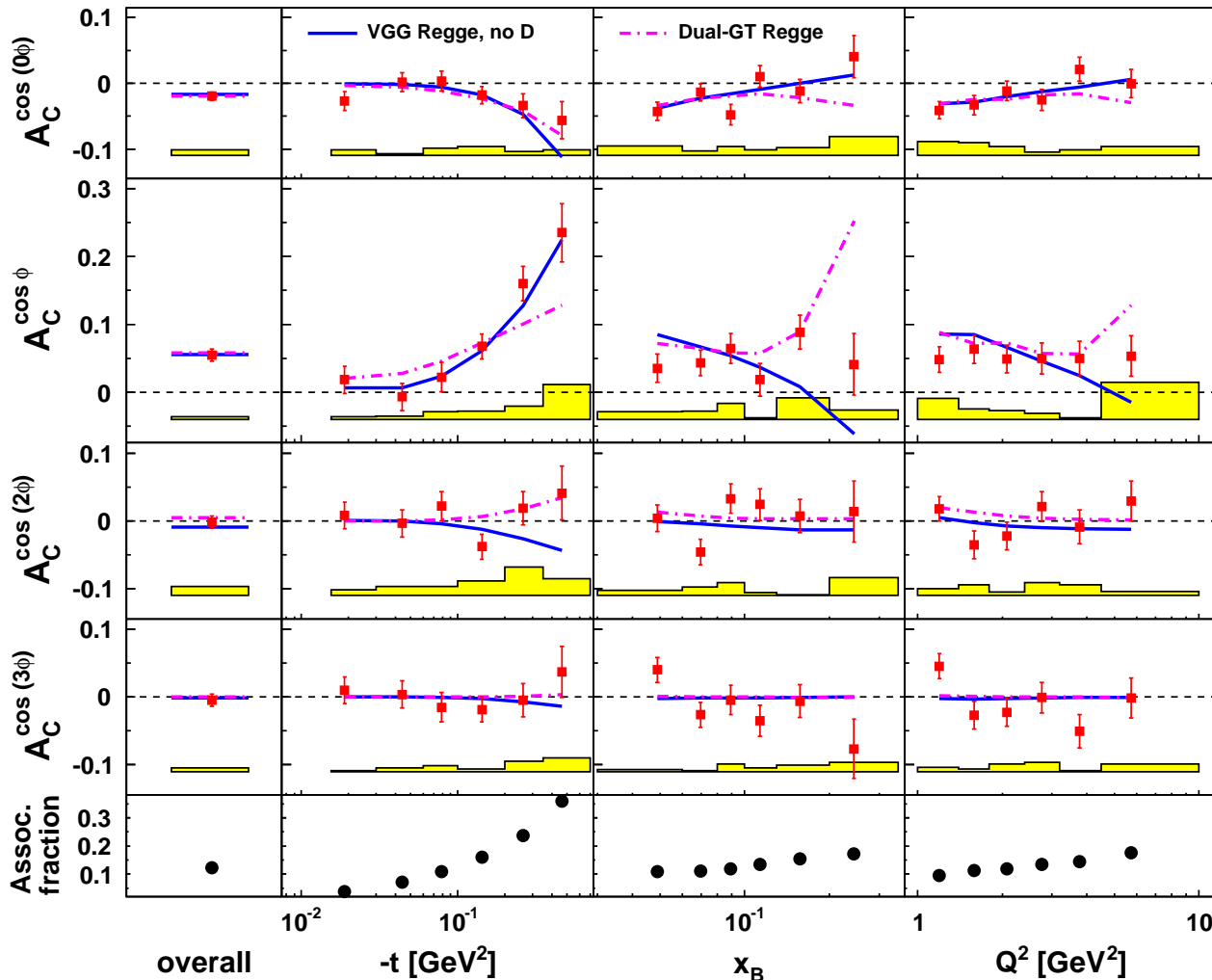


overestimation is not due to the associated production

beam charge asymmetry

$$A_C(\phi) = \sum_{n=0}^3 A_C^{\cos(n\phi)} \cos(n\phi) \propto \sum_{n=0}^3 c_n^I \cos(n\phi)$$

-HERMES Collaboration: arXiv:0909.3587 (2009)-



twist-2 $A_C^{\cos \phi}$, twist-3 $A_C^{\cos 0\phi}$

- strong t -dependence
- no x_B , Q^2 dependencies

$$A_C^{\cos \phi} \propto F_1 \text{Re}\mathcal{H}$$

$$A_C^{\cos 0\phi} \propto -\frac{t}{Q} A_C^{\cos \phi}$$

$A_C^{\cos(2\phi)} \approx 0$: twist-3 GPDs

$A_C^{\cos(3\phi)} \approx 0$: gluon helicity-flip GPDs

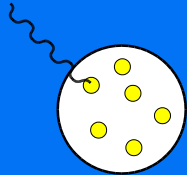
theoretical predictions:

- does not describe the beam-helicity data, but in good agreement with this data

unpolarized deuterium targets

coherent: $e^\pm d \rightarrow e^\pm d \gamma$

 DVCS



 Bethe-Heitler



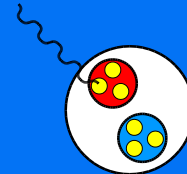
 target stays intact

 spin-1 targets described by 9 GPDs:

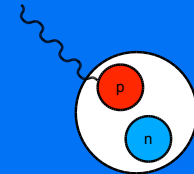
$$H_1^q, H_2^q, H_3^q, H_4^q, H_5^q, \tilde{H}_1^q, \tilde{H}_2^q, \tilde{H}_3^q, \tilde{H}_4^q$$

incoherent: $e^\pm d \rightarrow e^\pm pn \gamma$

 DVCS



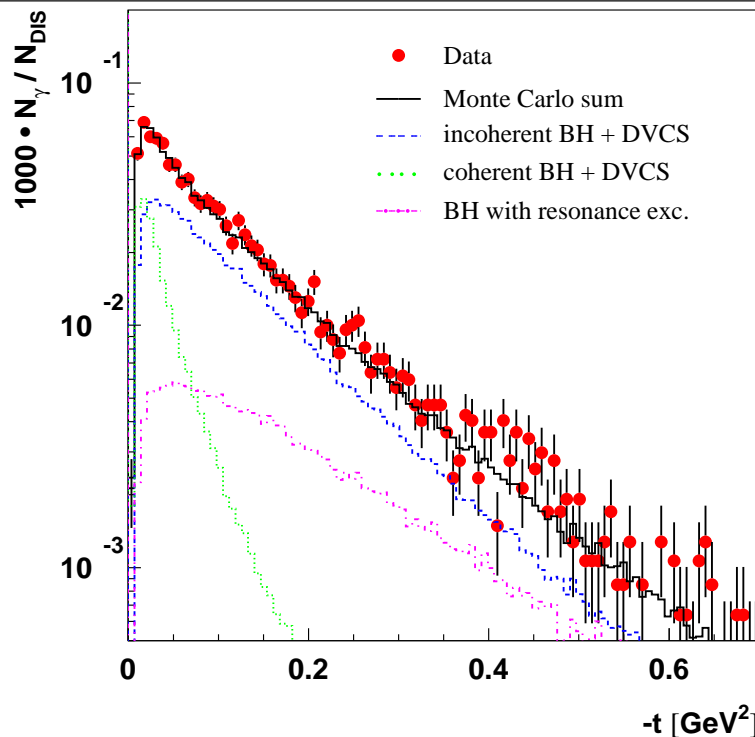
 Bethe-Heitler



 target brakes up

 spin- $\frac{1}{2}$ targets described by 4 GPDs:

$$H, E, \tilde{H}, \tilde{E}$$




coherent:

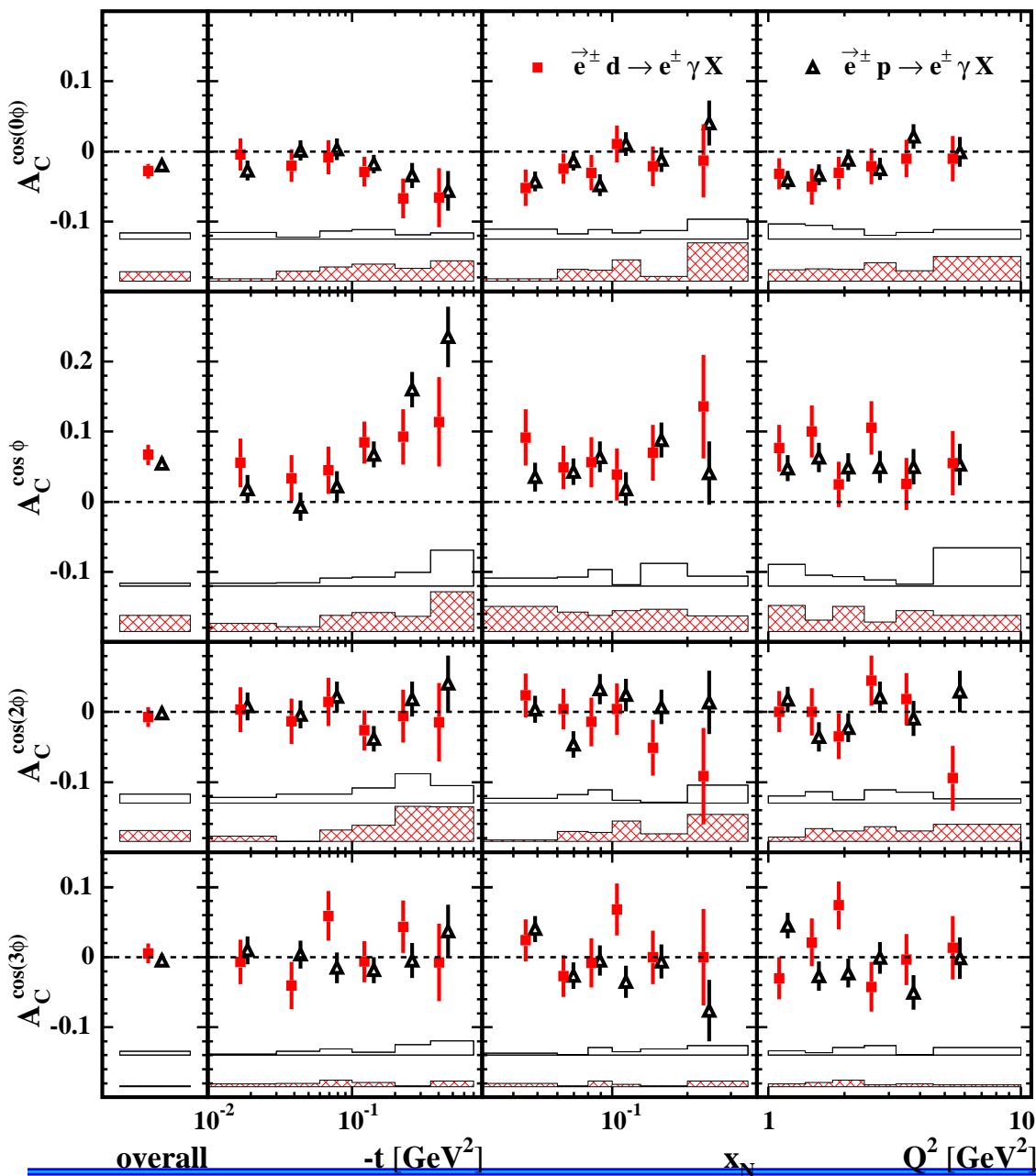
 contribution at small $-t$

incoherent:

 contribution at larger $-t$

 contribution from coherent $[0.06 : 0.7] \text{ GeV}^2$:
20%

beam-charge asymmetry



$$A_C(\phi) = \sum_{n=0}^3 A_C^{\cos(n\phi)} \cos(n\phi)$$

-HERMES Collaboration: arXiv:0911.0091 (2009)-

twist-2:

$$A_{C,coh}^{\cos \phi} \propto G_1 \text{Re}\mathcal{H}_1$$




$$A_{C,incoh}^{\cos \phi} \propto F_1 \text{Re}\mathcal{H}$$

higher twist :

$$A_C^{\cos 0\phi} \propto -\frac{t}{Q} A_C^{\cos \phi}$$

$$A_C^{\cos(2\phi)} \approx 0$$

$$A_C^{\cos(3\phi)} \approx 0$$

-  d and p results consistent
-  small values of $-t$: differences due to coherent contribution
-  larger values of $-t$: differences due to neutron contribution

longitudinal target polarization

$$\sigma(\phi, P_\ell, S_L) = \sigma_{UU}(\phi) \times [1 + P_\ell \mathcal{A}_{LU} + S_L \mathcal{A}_{UL}(\phi) + S_L P_\ell \mathcal{A}_{LL}(\phi)]$$

beam helicity asymmetry:

$$\mathcal{A}_{LU}(\phi) \equiv \frac{d\sigma^{\rightarrow} - d\sigma^{\leftarrow}}{d\sigma^{\rightarrow} + d\sigma^{\leftarrow}}$$

 projects the imaginary part of τ_{DVCS}

 no separate access to s_1^{DVCS} and s_1^I

longitudinal target-spin asymmetry:

$$\mathcal{A}_{UL}(\phi) \equiv \frac{(d\sigma^{\rightarrow\Rightarrow} + d\sigma^{\leftarrow\Rightarrow}) - (d\sigma^{\rightarrow\Leftarrow} + d\sigma^{\leftarrow\Leftarrow})}{(d\sigma^{\rightarrow\Rightarrow} + d\sigma^{\leftarrow\Rightarrow}) + (d\sigma^{\rightarrow\Leftarrow} + d\sigma^{\leftarrow\Leftarrow})}$$

 projects the imaginary part of τ_{DVCS}

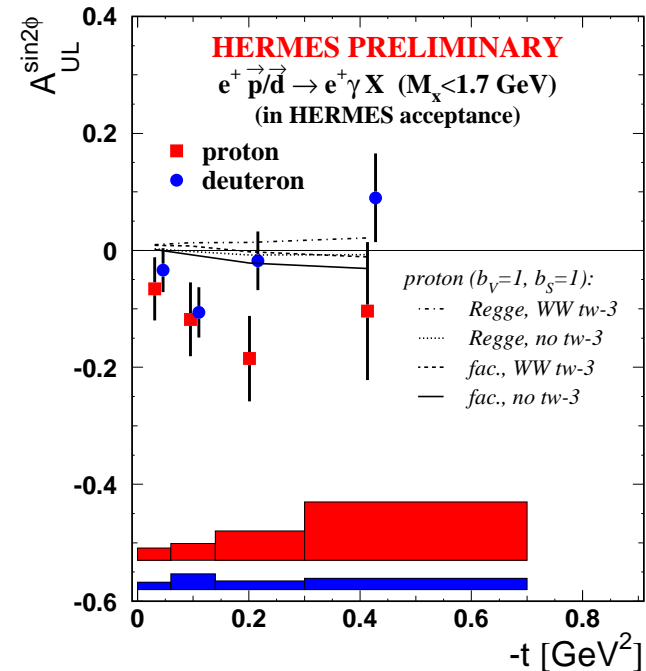
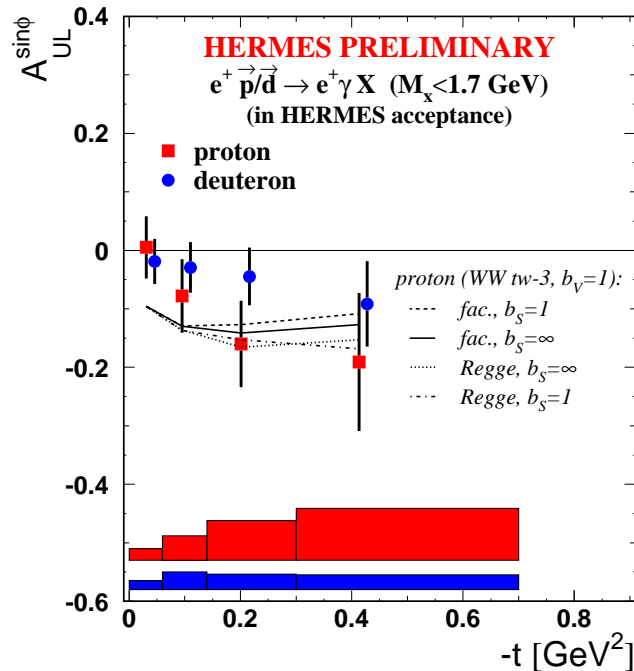
double-spin asymmetry:

$$\mathcal{A}_{LL}(\phi) \equiv \frac{(d\sigma^{\rightarrow\Rightarrow} + d\sigma^{\leftarrow\Leftarrow}) - (d\sigma^{\leftarrow\Rightarrow} + d\sigma^{\rightarrow\Leftarrow})}{(d\sigma^{\rightarrow\Rightarrow} + d\sigma^{\leftarrow\Leftarrow}) + (d\sigma^{\leftarrow\Rightarrow} + d\sigma^{\rightarrow\Leftarrow})}$$

 projects the real part of τ_{DVCS}

longitudinal target-spin asymmetry

$$A_{UL}(\phi) = \sum_{n=1}^2 A_{UL}^{\sin(n\phi)} \sin(n\phi) \propto \sum_{n=1}^2 s_n^I, s_n^{\text{DVCS}}$$



● s_1^I : twist-2

$$A_{UL}^{\sin \phi} \propto s_1^I \propto F_1 \text{Im} \tilde{\mathcal{H}}$$

● s_1^{DVCS} : twist-3

model in good agreement with data

unexpected large value

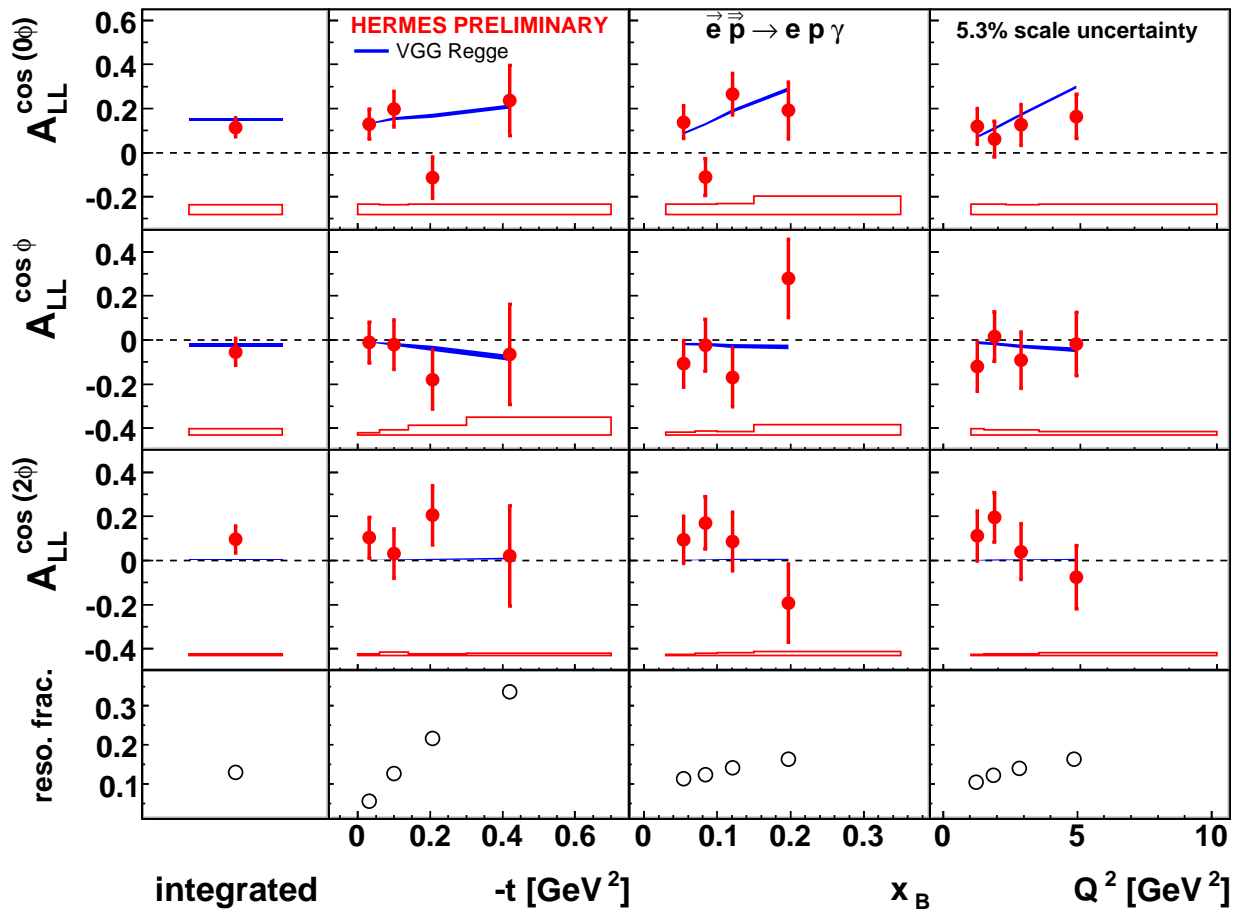
● s_2^I : quark twist-3 or gluon twist-2

● s_2^{DVCS} : twist-4

model does not describe the data

double-spin asymmetry

$$A_{LL}(\phi) \propto \sum_0^2 A_{LL}^{\cos(n\phi)} \cos(n\phi) \propto \sum_{n=0}^2 c_n^I, c_n^{\text{DVCS}}$$



twist-2: $\propto F_1 \text{Re}\tilde{\mathcal{H}}$

$$A_{LL}^{\cos 0\phi} \propto \begin{cases} c_0^{\text{DVCS}} \\ c_0^I \end{cases}$$



twist-2 / twist-3:

$$A_{LL}^{\cos \phi} \propto \begin{cases} c_1^{\text{DVCS}} \\ c_1^I \end{cases}$$

twist-3:

$$A_{LL}^{\cos 2\phi} \propto c_2^I$$

model predictions:

-  the same model, as for BCA and BHA
-  in good agreement with data

transversely polarized target

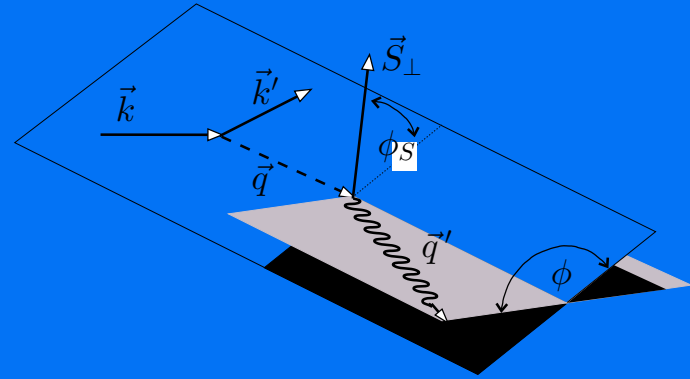
$$\sigma(\phi, P_\ell, S_T) = \sigma_{UU}(\phi) \times \left[1 + S_T \mathcal{A}_{UT}^{\text{DVCS}}(\phi, \phi_S) + S_T e_\ell \mathcal{A}_{UT}^{\text{I}}(\phi, \phi_S) + e_\ell \mathcal{A}_C(\phi) \right]$$

transverse target-spin asymmetry:

$$\mathcal{A}_{UT}(\phi, \phi_S) = \frac{1}{S_T} \cdot \frac{d\sigma^{\uparrow}(\phi, \phi_S) - d\sigma^{\downarrow}(\phi, \phi_S)}{d\sigma^{\uparrow}(\phi, \phi_S) + d\sigma^{\downarrow}(\phi, \phi_S)}$$

beam-charge asymmetry:

$$\mathcal{A}_C(\phi) \equiv \frac{d\sigma^+ - d\sigma^-}{d\sigma^+ + d\sigma^-}$$



$$\mathcal{A}_{UT}^{\text{DVCS}}(\phi, \phi_S) \equiv \frac{1}{S_T} \cdot \frac{d\sigma^{+\uparrow}(\phi, \phi_S) - d\sigma^{+\downarrow}(\phi, \phi_S) + d\sigma^{-\uparrow}(\phi, \phi_S) - d\sigma^{-\downarrow}(\phi, \phi_S)}{d\sigma^{+\uparrow}(\phi, \phi_S) + d\sigma^{+\downarrow}(\phi, \phi_S) + d\sigma^{-\uparrow}(\phi, \phi_S) + d\sigma^{-\downarrow}(\phi, \phi_S)}$$

$$\mathcal{A}_{UT}^{\text{I}}(\phi, \phi_S) \equiv \frac{1}{S_T} \cdot \frac{d\sigma^{+\uparrow}(\phi, \phi_S) - d\sigma^{+\downarrow}(\phi, \phi_S) - d\sigma^{-\uparrow}(\phi, \phi_S) + d\sigma^{-\downarrow}(\phi, \phi_S)}{d\sigma^{+\uparrow}(\phi, \phi_S) + d\sigma^{+\downarrow}(\phi, \phi_S) + d\sigma^{-\uparrow}(\phi, \phi_S) + d\sigma^{-\downarrow}(\phi, \phi_S)}$$

separation of s_i^{DVCS} , c_i^{DVCS} and s_i^{I} , c_i^{I} terms with same harmonic signatures

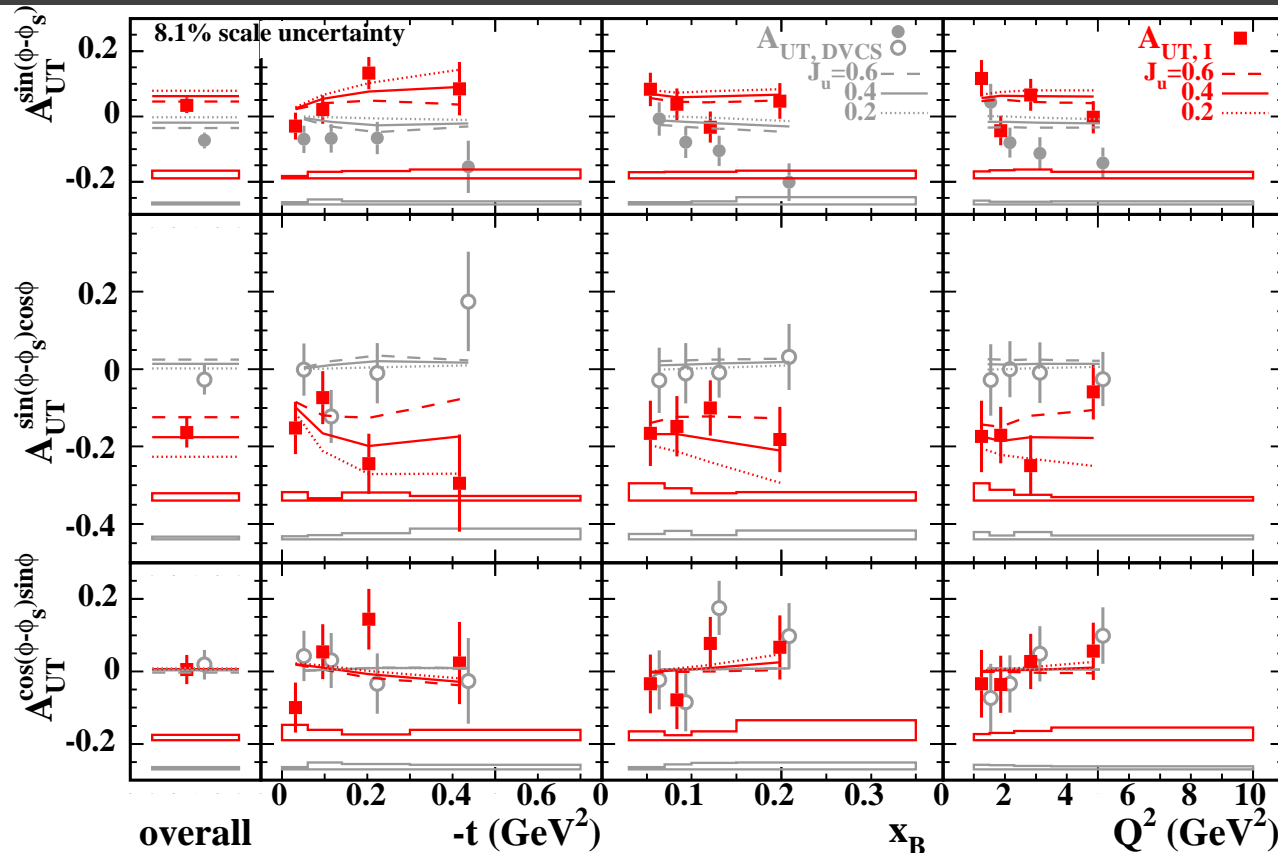
projects the imaginary part of τ_{DVCS}

transverse target-spin asymmetry

$$\begin{aligned}\mathcal{A}_{UT}^{\text{DVCS}}(\phi, \phi_S) &= \sum_{n=0}^2 A_{UT, \text{DVCS}}^{\sin(\phi - \phi_S) \cos(n\phi)} \sin(\phi - \phi_S) \cos(n\phi) \\ &+ \sum_{n=1}^2 A_{UT, \text{DVCS}}^{\cos(\phi - \phi_S) \sin(n\phi)} \cos(\phi - \phi_S) \sin(n\phi) \\ \mathcal{A}_{UT}^{\text{I}}(\phi, \phi_S) &= \sum_{n=0}^2 A_{UT, \text{I}}^{\sin(\phi - \phi_S) \cos(n\phi)} \sin(\phi - \phi_S) \cos(n\phi) \\ &+ \sum_{n=1}^2 A_{UT, \text{I}}^{\cos(\phi - \phi_S) \sin(n\phi)} \cos(\phi - \phi_S) \sin(n\phi)\end{aligned}$$

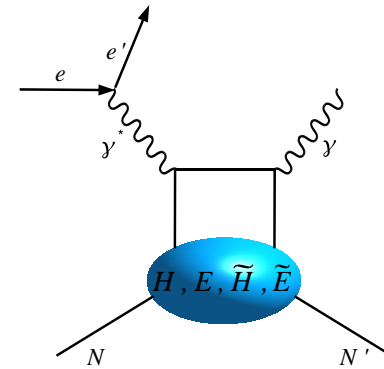
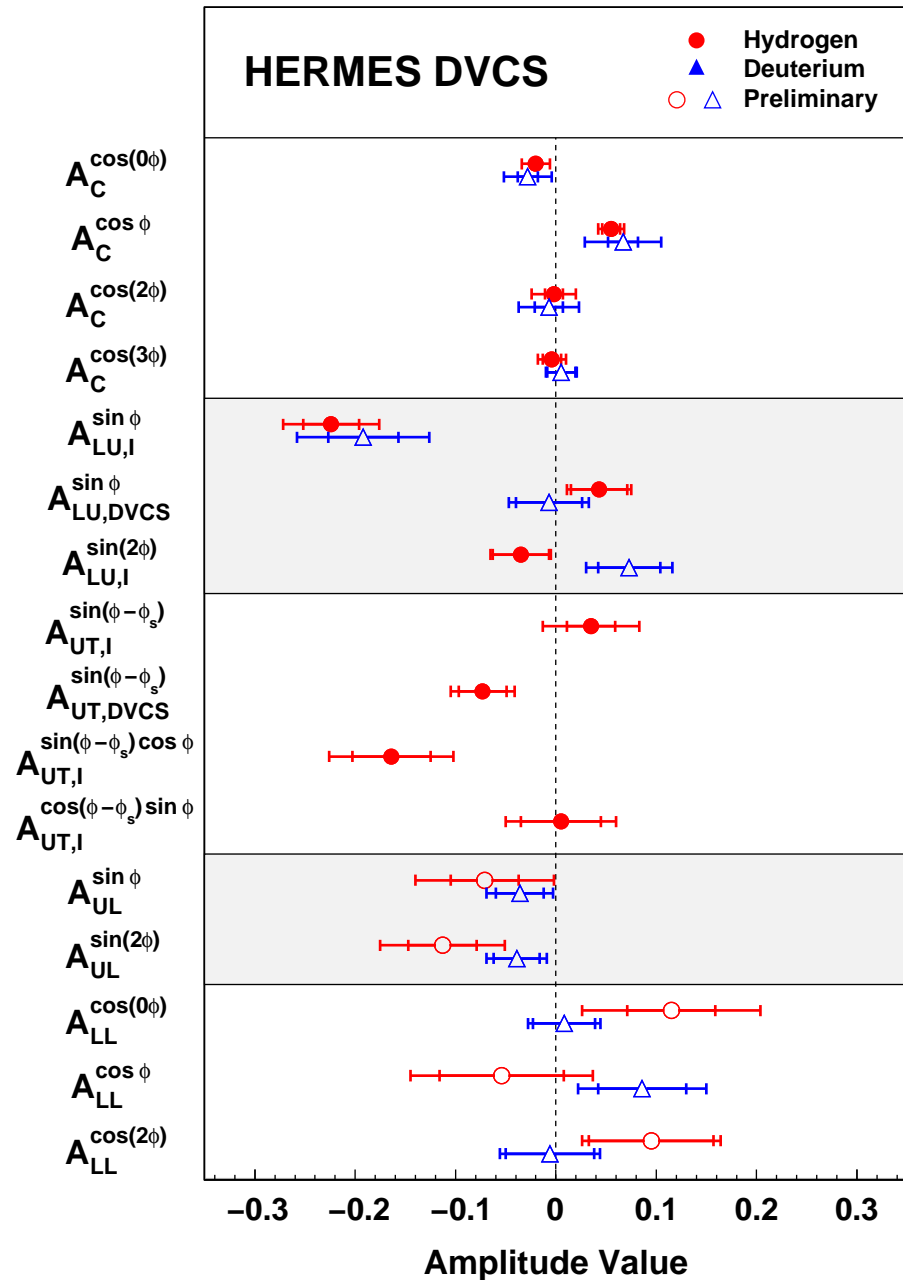
transverse target-spin asymmetry

$$A_{UT}(\phi, \phi_S) \propto \text{Im}[F_2\mathcal{H} - F_1\mathcal{E}] \sin(\phi - \phi_S) \cos \phi + \text{Im}[F_2\mathcal{H} - F_1\mathcal{E}] \sin(\phi - \phi_S) \\ + \text{Im}[\mathcal{H}\mathcal{E}^* - \mathcal{E}\mathcal{H}^* + \xi\tilde{\mathcal{E}}\tilde{\mathcal{H}}^* - \tilde{\mathcal{H}}\xi\tilde{\mathcal{E}}^*] \sin(\phi - \phi_S) + \dots$$



- $A_{UT}^{\sin(\phi - \phi_S) \cos \phi}$ found much more sensitive to J_u than others
- insensitive to J_d , assumed $J_d = 0$ (supported by lattice QCD)
- with a good model, allows a model-dependent constraint

Summary



beam-charge asymmetry:

 $\text{Re}\mathcal{H}$

beam-helicity asymmetry:

 $\text{Im}\mathcal{H}$

transverse target-spin asymmetry:

 $\text{Im}(\mathcal{H}\mathcal{E})$

longitudinal target-spin asymmetry:

 $\text{Im}\tilde{\mathcal{H}}$

double-spin asymmetry:

 $\text{Re}\tilde{\mathcal{H}}$

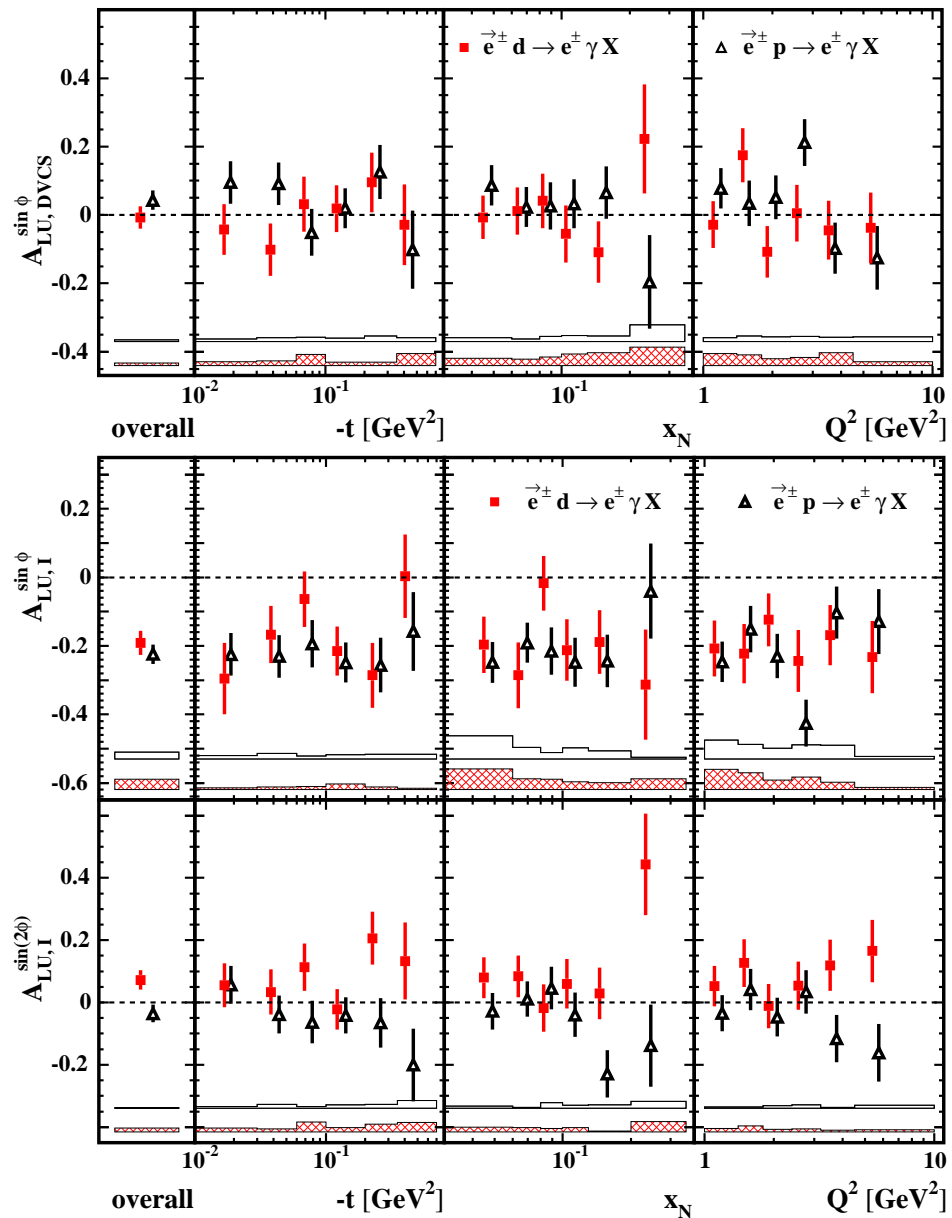
backup slides

beam helicity asymmetry

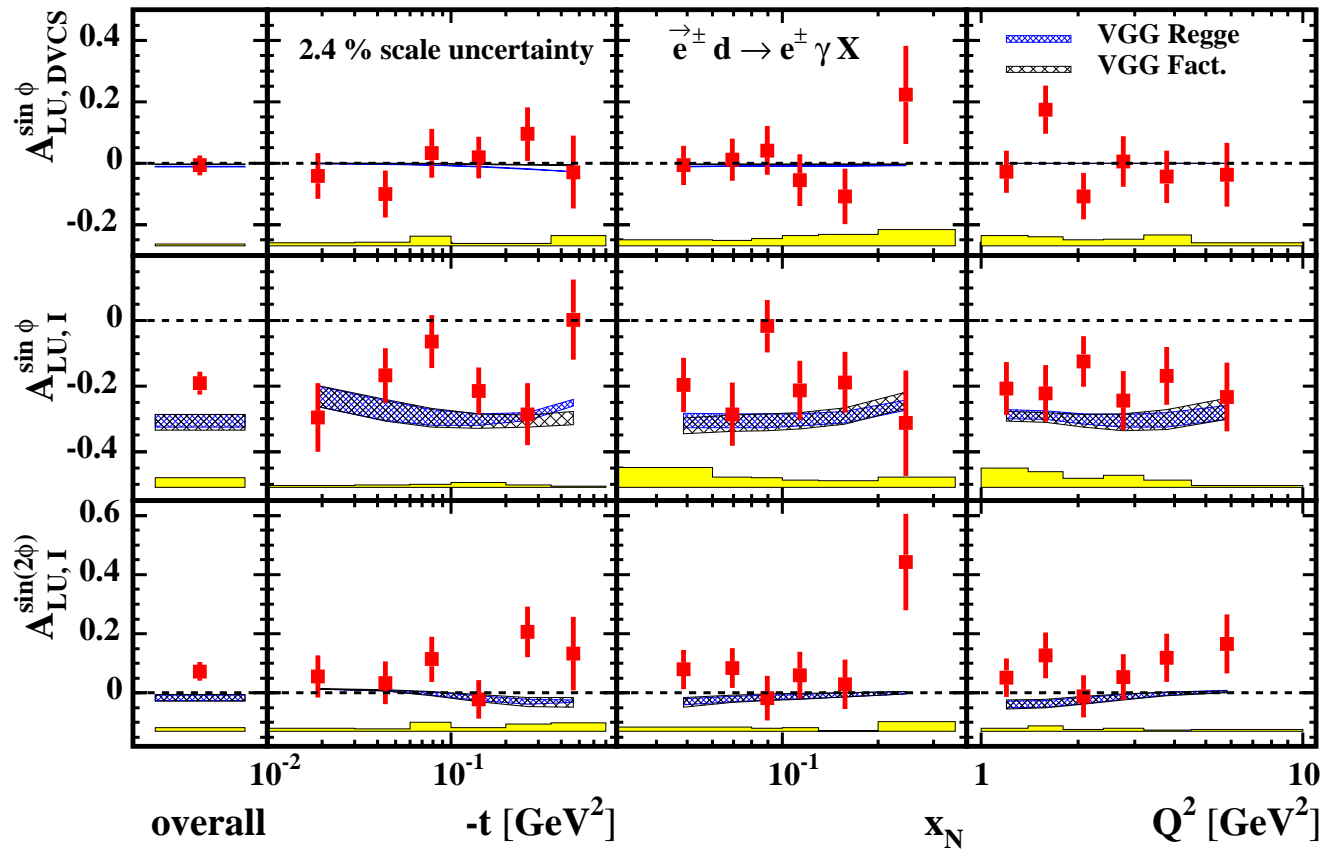
$$\begin{aligned}
 A_{LU}(\phi) &\equiv \frac{d\sigma^{\rightarrow} - d\sigma^{\leftarrow}}{d\sigma^{\rightarrow} + d\sigma^{\leftarrow}} \\
 &= \frac{-e_{\ell} \frac{K_I}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \left[\sum_{n=1}^2 s_n^I \sin(n\phi) \right] + \frac{1}{Q^2} s_1^{\text{DVCS}} \sin \phi}{\frac{1}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \left[K_{\text{BH}} \sum_{n=0}^2 c_n^{\text{BH}} \cos(n\phi) - e_{\ell} K_I \sum_{n=0}^3 c_n^I \cos(n\phi) \right] + \frac{1}{Q^2} \sum_{n=0}^2 c_n^{\text{DVCS}} \cos(n\phi)}.
 \end{aligned}
 \tag{1}$$

$$\begin{aligned}
 A_{LU}^I(\phi) &\equiv \frac{(d\sigma^{+\rightarrow} - d\sigma^{+\leftarrow}) - (d\sigma^{-\rightarrow} - d\sigma^{-\leftarrow})}{(d\sigma^{+\rightarrow} + d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} + d\sigma^{-\leftarrow})} \\
 &= \frac{-\frac{K_I}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \left[\sum_{n=1}^2 s_n^I \sin(n\phi) \right]}{\frac{K_{\text{BH}}}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \sum_{n=0}^2 c_n^{\text{BH}} \cos(n\phi) + \frac{1}{Q^2} \sum_{n=0}^2 c_n^{\text{DVCS}} \cos(n\phi)},
 \end{aligned}
 \tag{2}$$

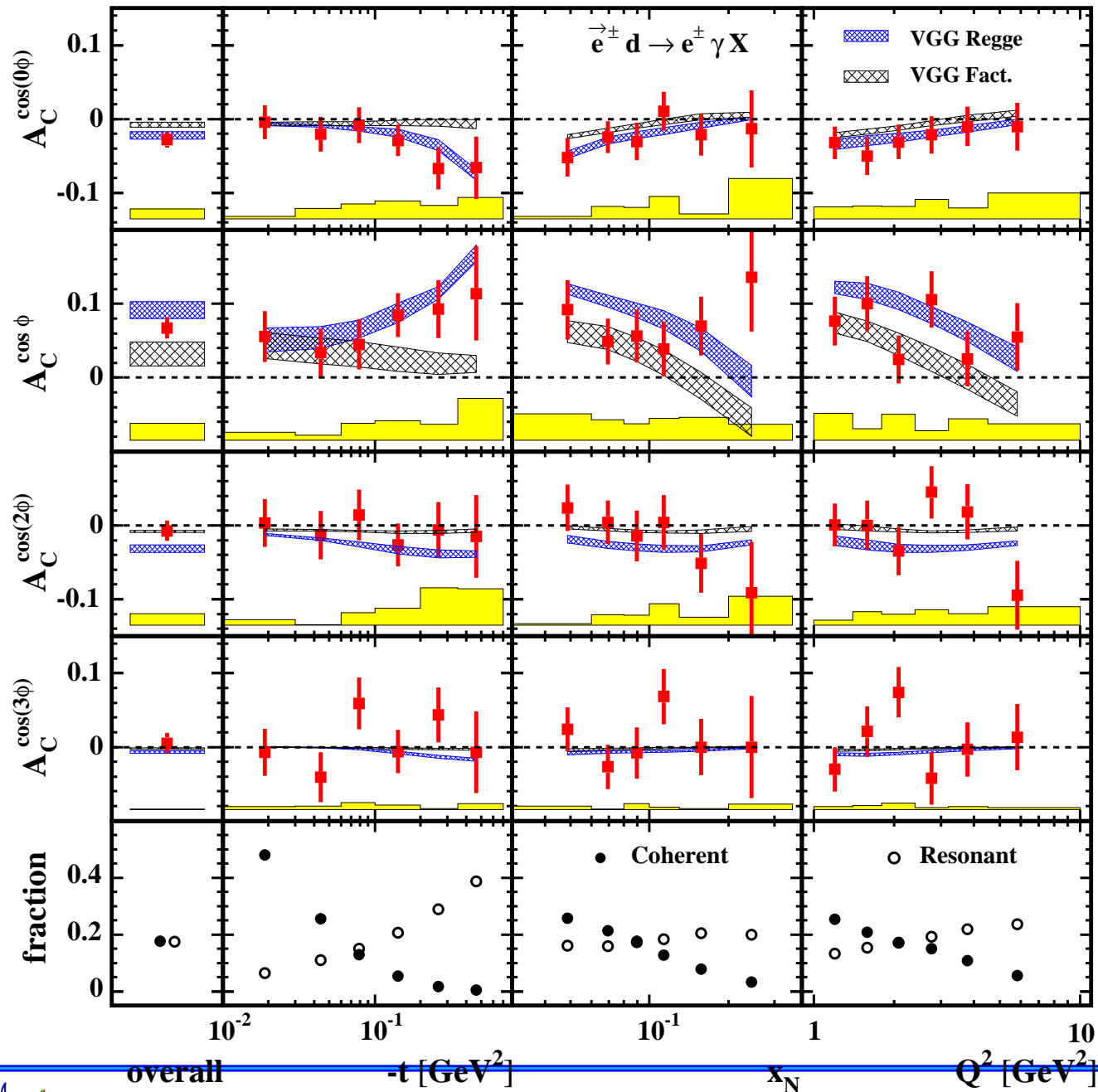
beam-helicity asymmetry



beam-helicity asymmetry



beam-helicity asymmetry



nuclear targets: He, N, Ne, Kr, Xe

