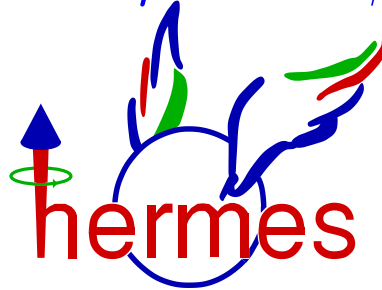
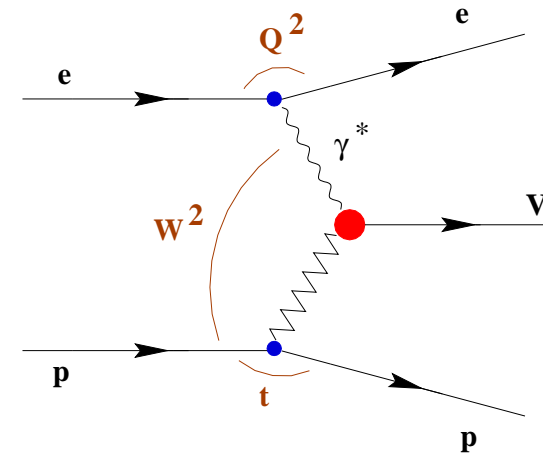


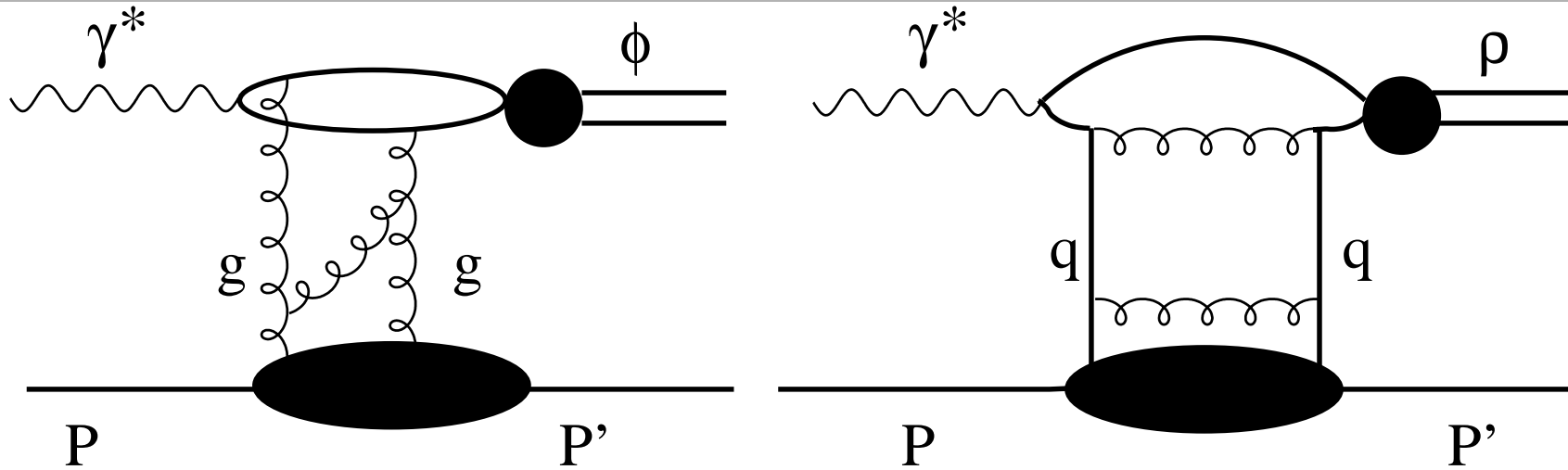
## New results on exclusive $\rho^0$ and $\phi$ meson production at



- Objectives: Generalized Parton Distributions
- HERMES Experiment
- Total and Longitudinal Cross Sections of  $\rho^0$  and  $\phi$
- $\rho^0$  and  $\phi$  Meson Spin Density Matrix Elements
  - Kinematic dependences
  - Longitudinal-to-Transverse Cross-Section Ratios
  - Hierarchy of Helicity Amplitudes
  - Unnatural Parity Exchange
- Summary



# Test of GPDs via Exclusive Vector Meson Production



## Properties of $\rho^0$ and $\phi$ meson data:

- different pQCD production mechanisms:
  - only two-gluon exchange for  $\phi$ ,
  - both two-gluon and quark exchanges for  $\rho^0$ $\implies$  GPDs as a flavor filter
- quark exchange mediated by
  - vector or scalar meson:  $\rho^0, \omega, a_2$   
(natural parity:  $J^P = 0^+, 1^-$ )  
 $\implies$  unpolarized GPDs:  $H, \tilde{H}$
  - pseudoscalar or axial meson:  $\pi, a_1, b_1$   
(unnatural parity  $J^P = 0^-, 1^+$ )  
 $\implies$  polarized GPDs:  $E, \tilde{E}$

## Experimental observables:

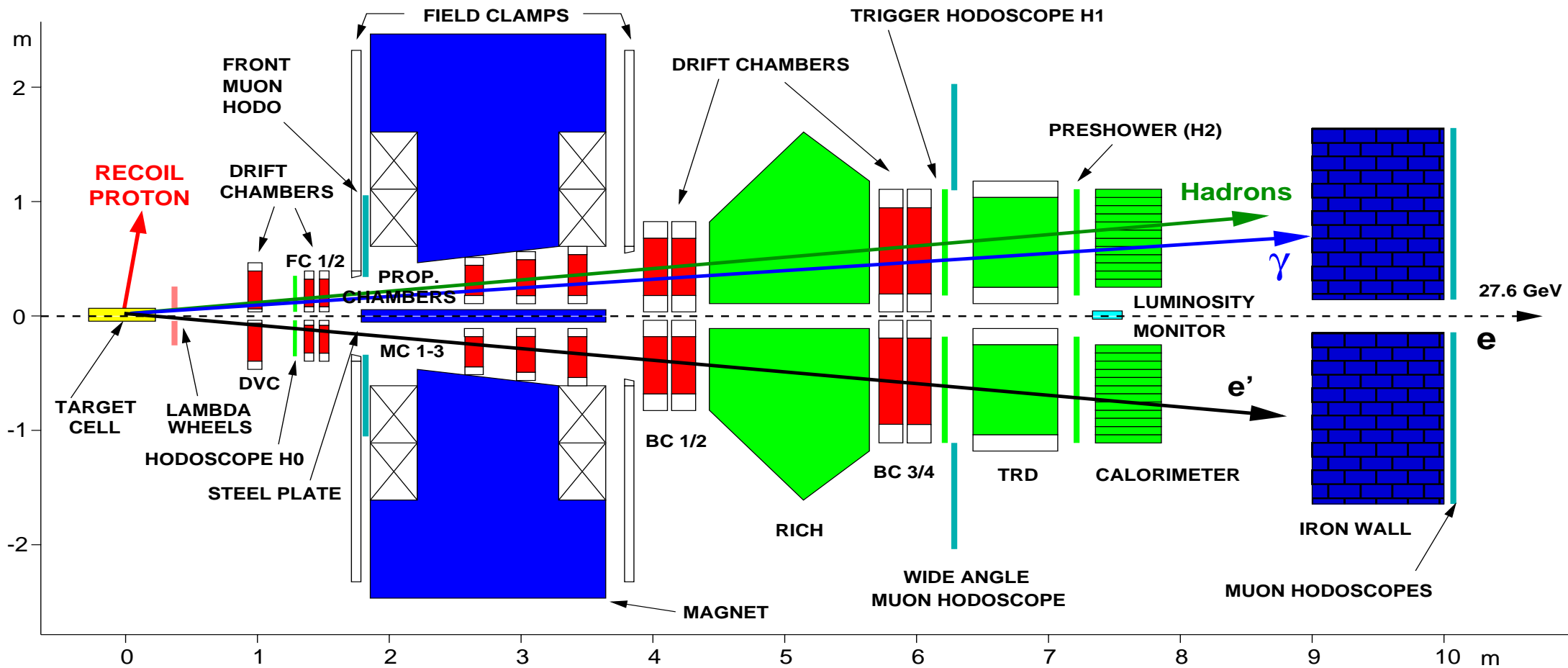
- total ( $\sigma_{tot}$ ) and longitudinal ( $\sigma_L$ ) cross sections:  

$$\sigma_L = \frac{R}{1+\epsilon R} \sigma_{tot}, \text{ where } R = \sigma_L / \sigma_T = \frac{r_{00}^{04}}{\epsilon(1-r_{00}^{04})}$$
- Spin Density Matrix Elements (SDMEs):  

$$r_{\lambda\rho\lambda'\rho'}^\alpha \sim \rho(V) = \frac{1}{2} T \rho(\gamma) T^+$$
 Vector meson spin-density matrix  $\rho(V)$  in terms of the photon matrix  $\rho(\gamma)$  and helicity amplitude  $T_{\lambda_V \lambda_\gamma}$
- SCHC: helicity of  $\gamma^* =$  helicity of  $\rho^0$ , any violation?
- Extracted from SDMEs Natural and Unnatural Parity Helicity Amplitudes

# HERMES Detector is Two Identical Halves of Forward Spectrometer

- Beam:  $P = 27.56 \text{ GeV}/c$ , 50...100 mA, longitudinal polarization  $\sim 55\%$ , accuracy of 2%
- Target:  $^1\text{H}$ ,  $^2\text{H}$  gases, integrated over polarization states



- Acceptance:  $40 < \Theta < 220 \text{ mrad}$ ,  $|\Theta_x| < 170 \text{ mrad}$ ,  $40 < |\Theta_y| < 140 \text{ mrad}$
- Resolution:  $\delta p/p \leq 1\%$ ,  $\delta\Theta \leq 0.6 \text{ mrad}$

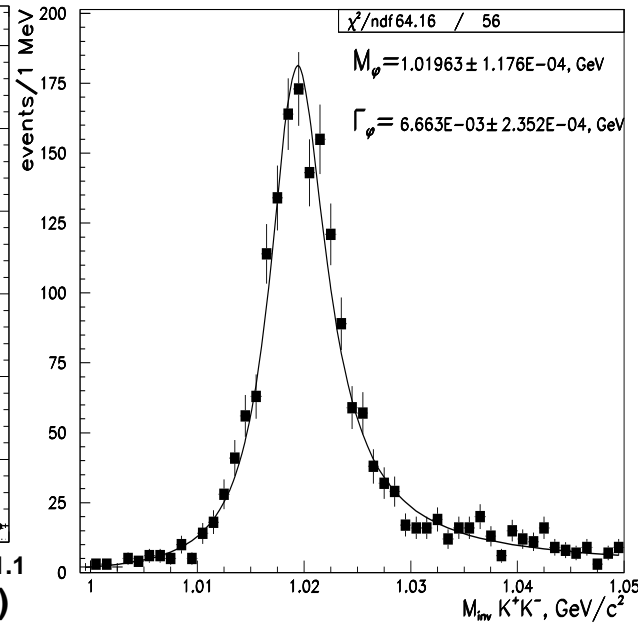
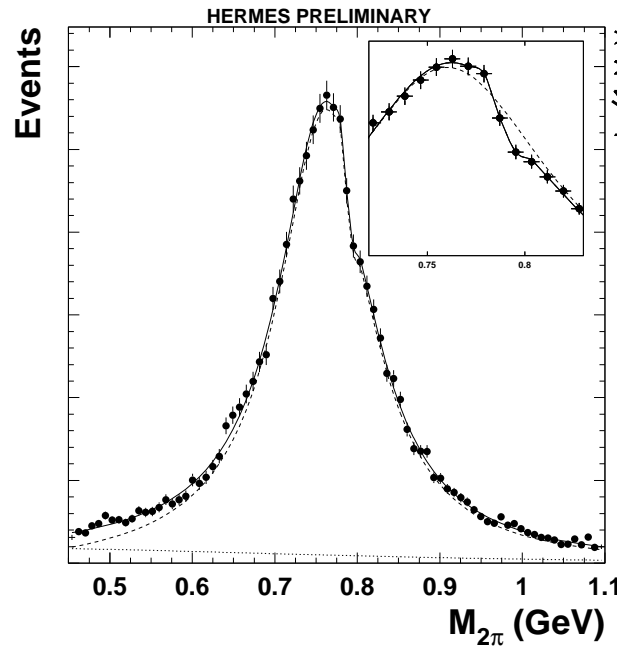
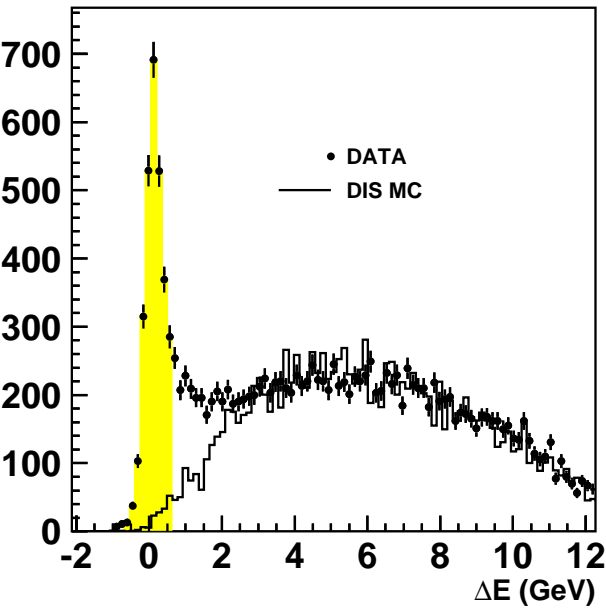
# Kinematics of exclusive $\rho^0$ and $\phi$ meson production

$$e+p \rightarrow e'+p'+\rho^0 \rightarrow \pi^+\pi^-$$

$$e+p \rightarrow e'+p'+\phi \rightarrow K^+K^-$$

Clean  $\rho^0$  exclusivity peak

$$\Delta E = \frac{M_X^2 - M_p^2}{2M_p}, \quad M_X^2 = (p+q-v)^2, \quad M_{inv} : \rho^0 \rightarrow \pi^+\pi^- \quad \phi \rightarrow K^+K^-$$



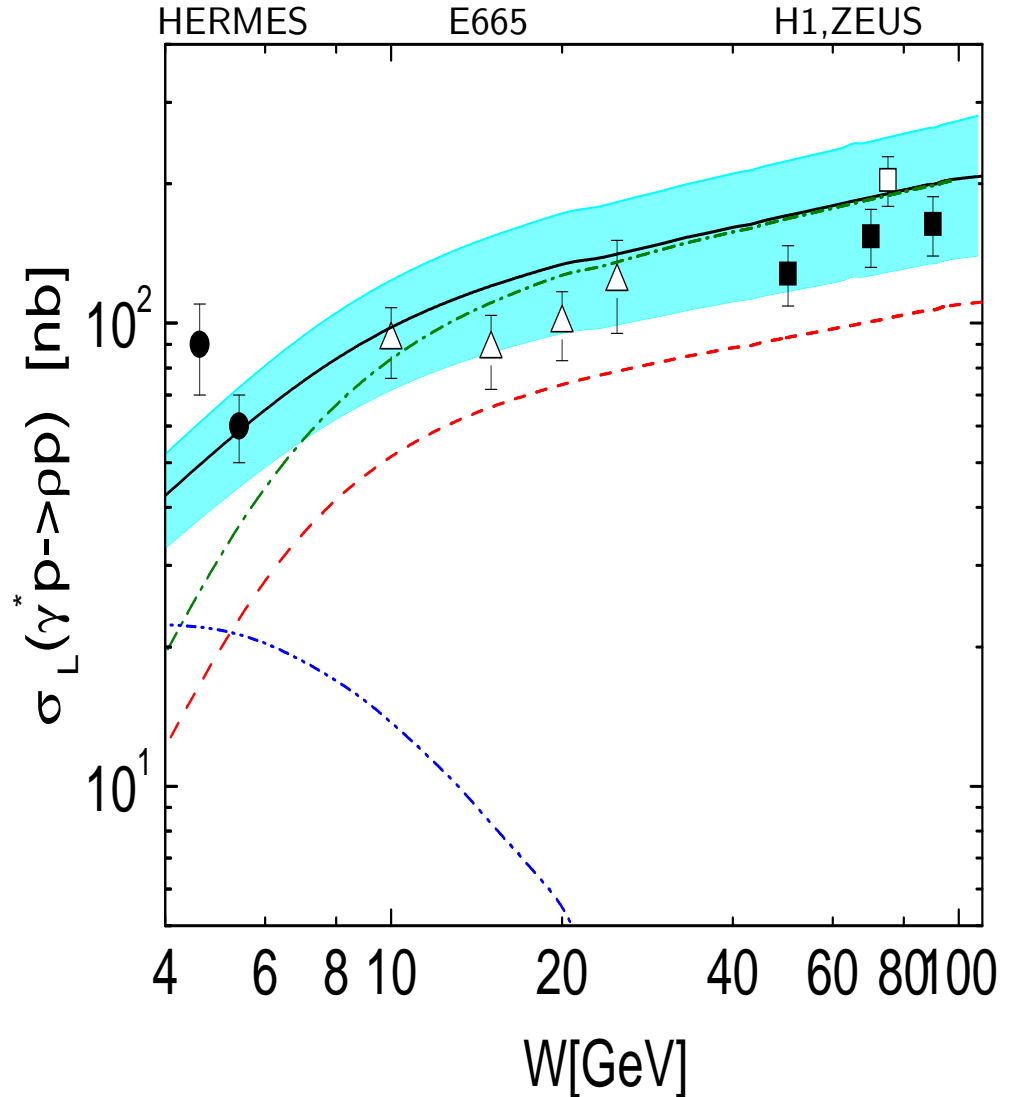
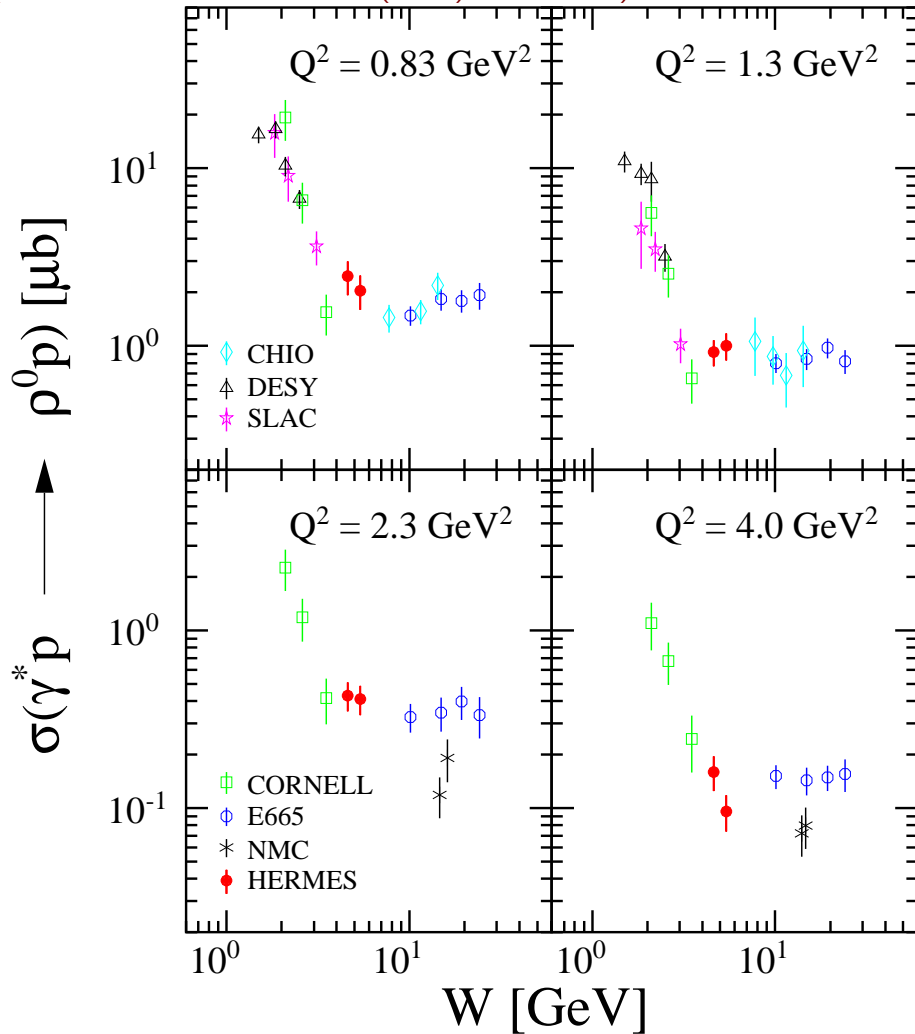
• Background is subtracted using MC (PYTHIA)

- $\nu = 5 \div 24 \text{ GeV}, \langle \nu \rangle = 13.3 \text{ GeV}, \quad Q^2 = 1.0 \div 5.0 \text{ GeV}^2, \langle Q^2 \rangle = 2.3 \text{ GeV}^2$
- $W = 3.0 \div 6.5 \text{ GeV}, \langle W \rangle = 4.9 \text{ GeV}, \quad x_{Bj} = 0.01 \div 0.35, \langle x_{Bj} \rangle = 0.07$

# $\rho^0$ Total and Longitudinal Cross Sections, and GK Model

(HERMES collab. EPJ C 17 (2000) 3, 389-398).

S.V.Goloskokov, P.Kroll hep-ph/0611290.



- HERMES data in the transition region
- which production mechanisms are involved?

two-gluon exchange, two-gluon+sea interference, quark exchange, sum

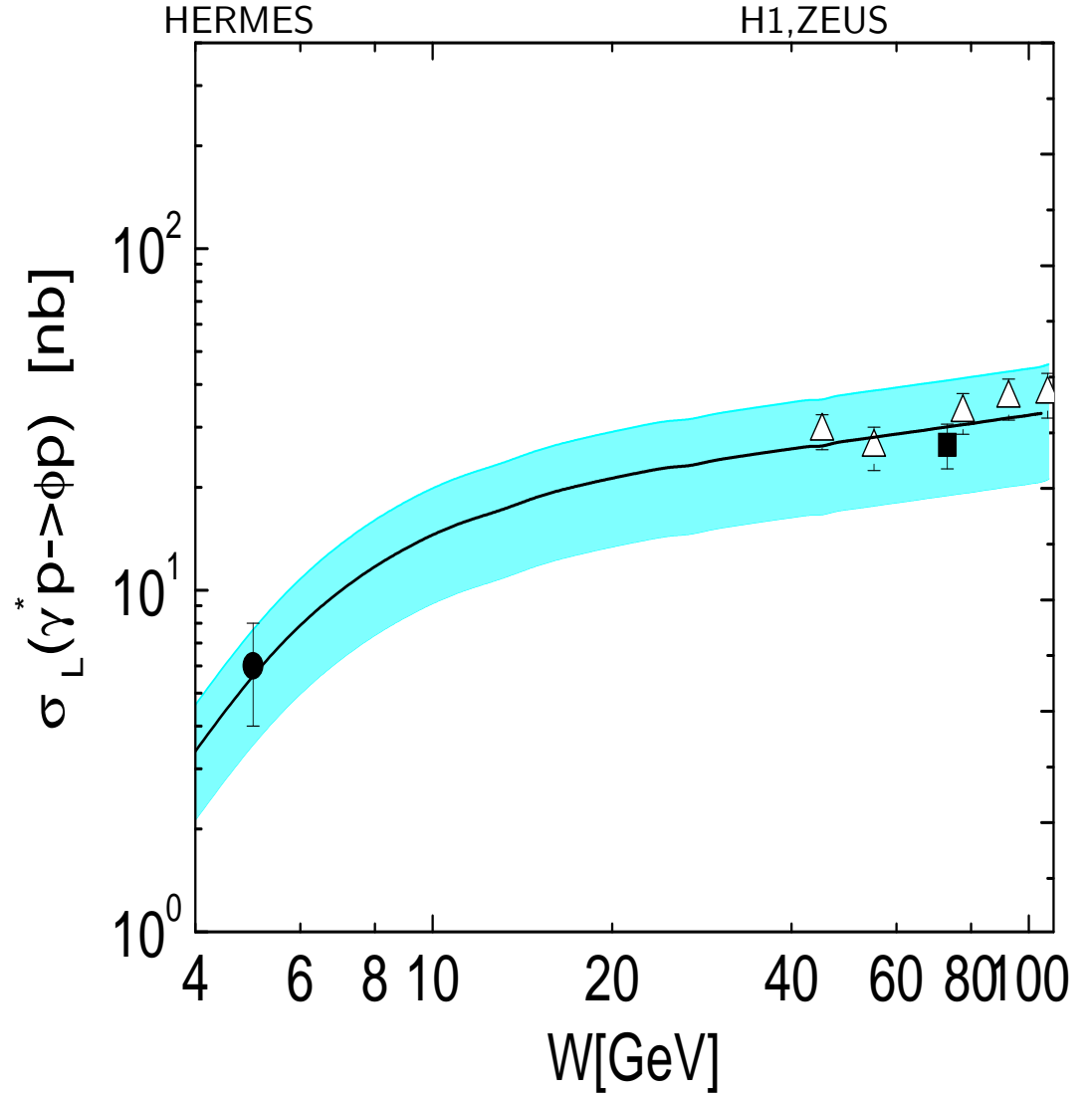
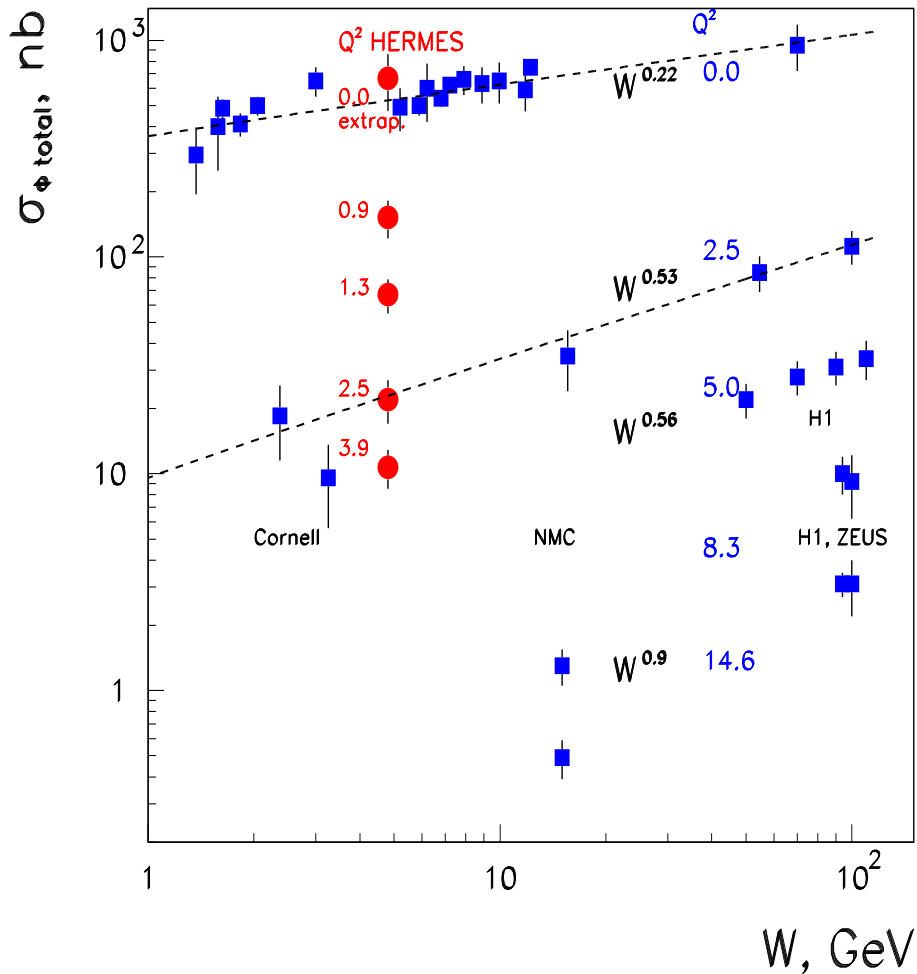
Band represents uncertainties in  $\sigma_L$  from Parton Distributions

⇒⇒ Quark exchange is important for HERMES, i.e. at  $W \leq 5$  GeV

# $\phi$ Total and Longitudinal Cross Sections, and GK model

S.V.Goloskokov, P.Kroll, Eur.Phys.J. C 42, 2005; hep-ph/0611290

PRELIMINARY



$\phi$ : two-gluon exchange only

Band represents uncertainties in  $\sigma_L$  from Parton Distributions

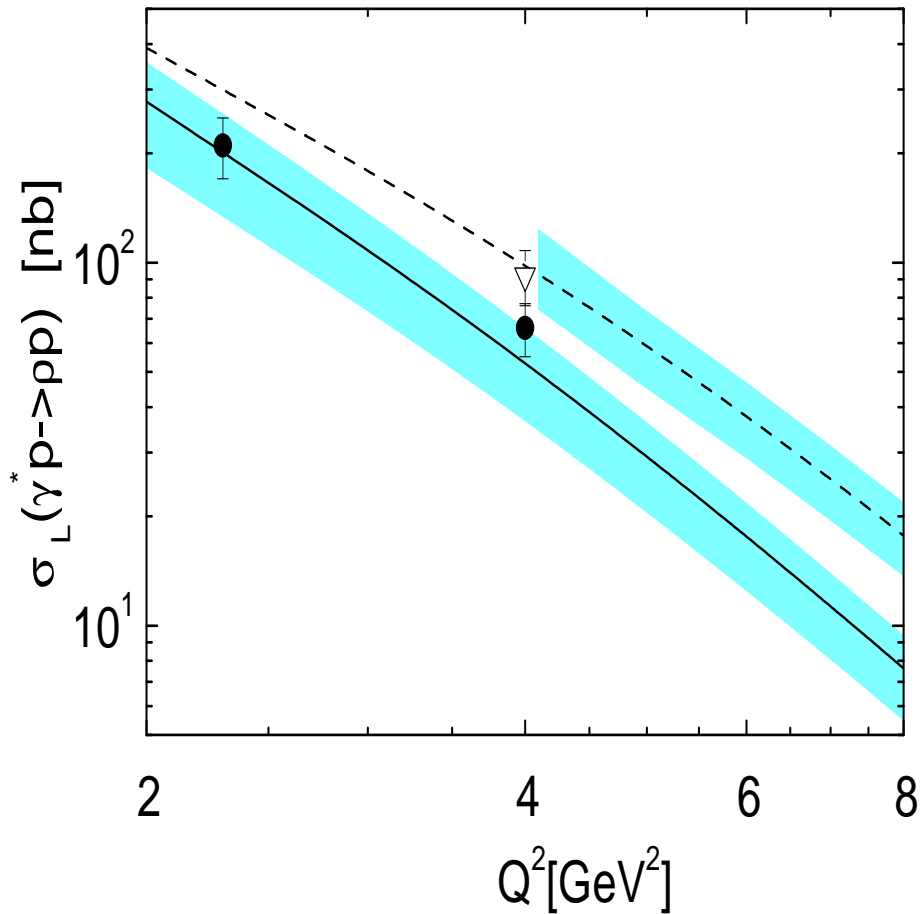
→  $W^{\delta_\phi(Q^2)}$  dependence over all  $W$

$\delta_\phi = 0.22$  at  $Q^2 = 0$ ,  $\delta_\phi = 0.53$  at  $Q^2 = 2.5 \text{ GeV}^2$

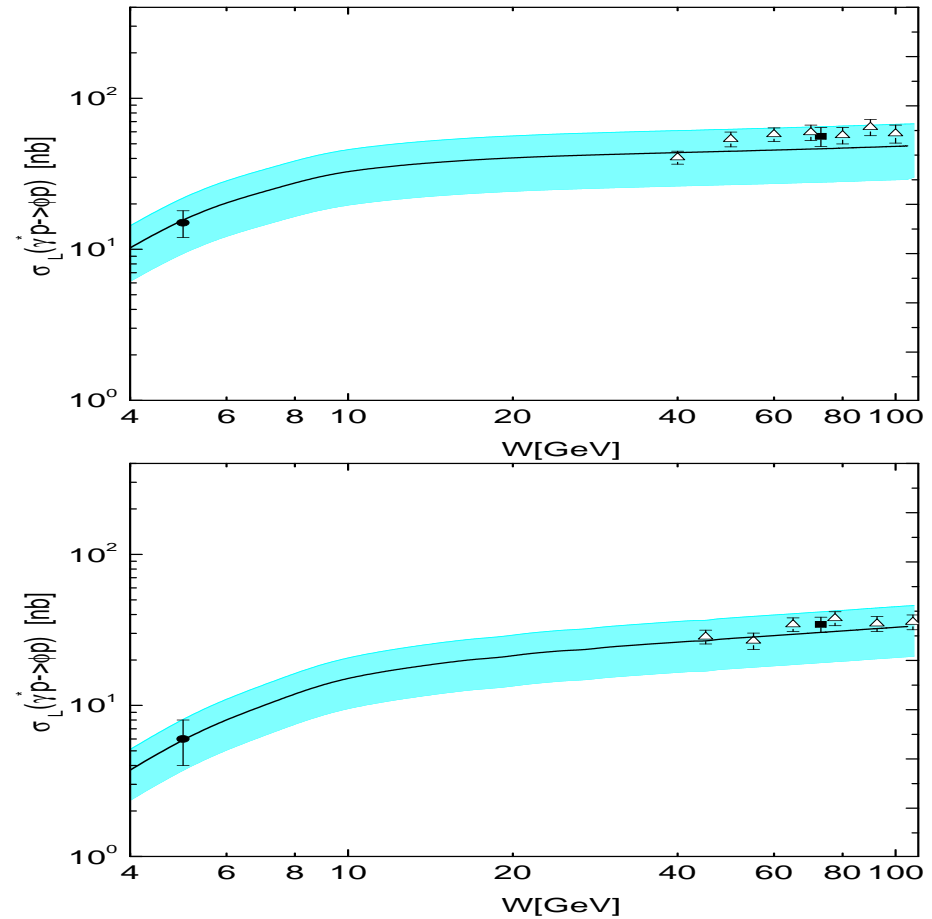
→ Two-gluon exchange is sufficient for  $\phi$

⇒ Good agreement of GK  $\sigma_L(W)$ -dependence

# $Q^2$ -dependence of $\sigma_L$ from GK model for $\rho^0$ and $\phi$ at HERMES



$W = 5$  GeV, black circles - HERMES



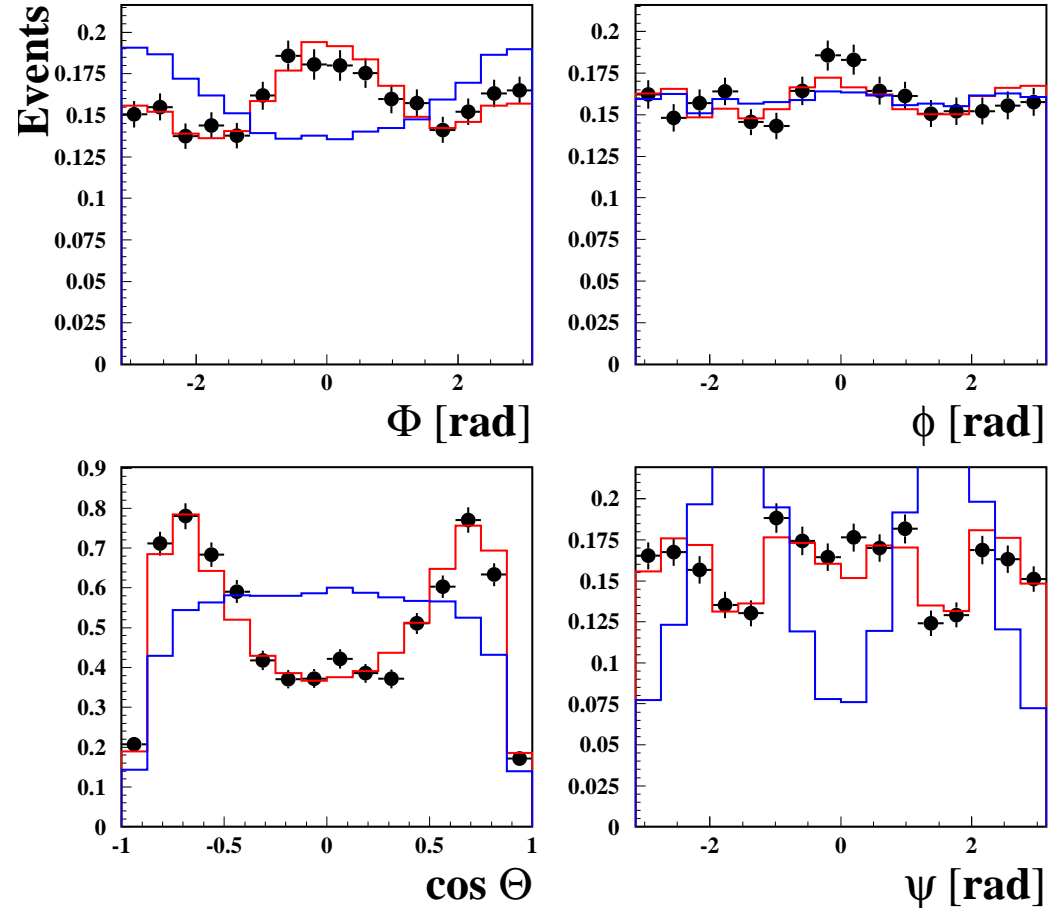
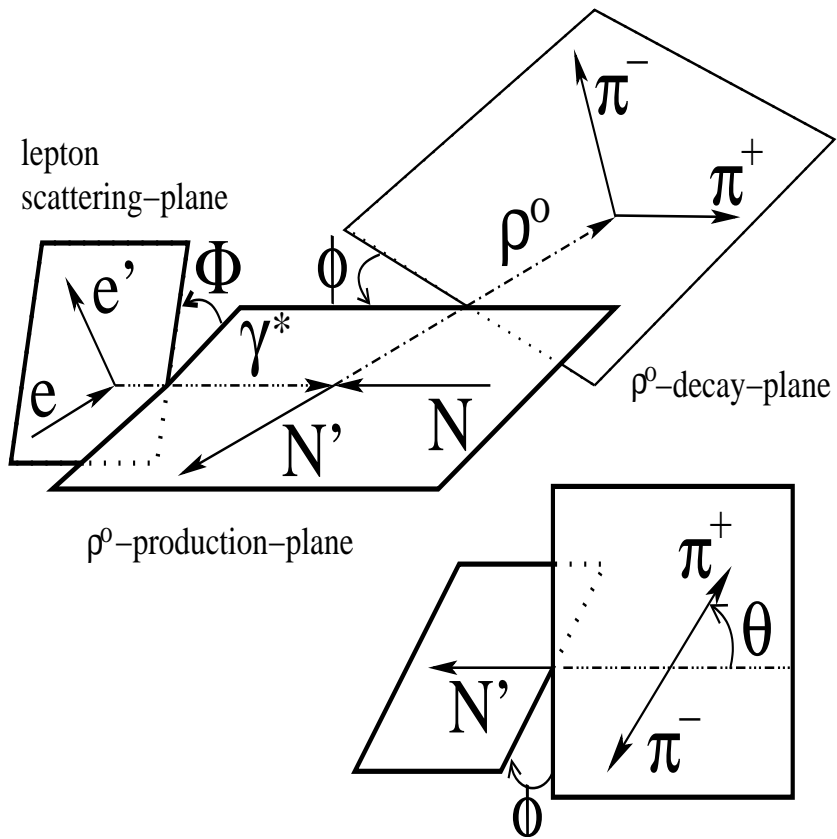
Top:  $Q^2 = 2.4$  GeV<sup>2</sup>

Bottom:  $Q^2 = 3.8$  GeV<sup>2</sup>

→ Full agreement of  $\sigma_L$  with HERMES data at  $Q^2 > 2.0$  GeV<sup>2</sup>  
 (Uncertainties of HERMES data are smaller than ones from the GK calculations)

⇒ **What's about  $\sigma_T$ ?**

# Fit of Angular Distributions Using Max. Likelihood Method in MINUIT



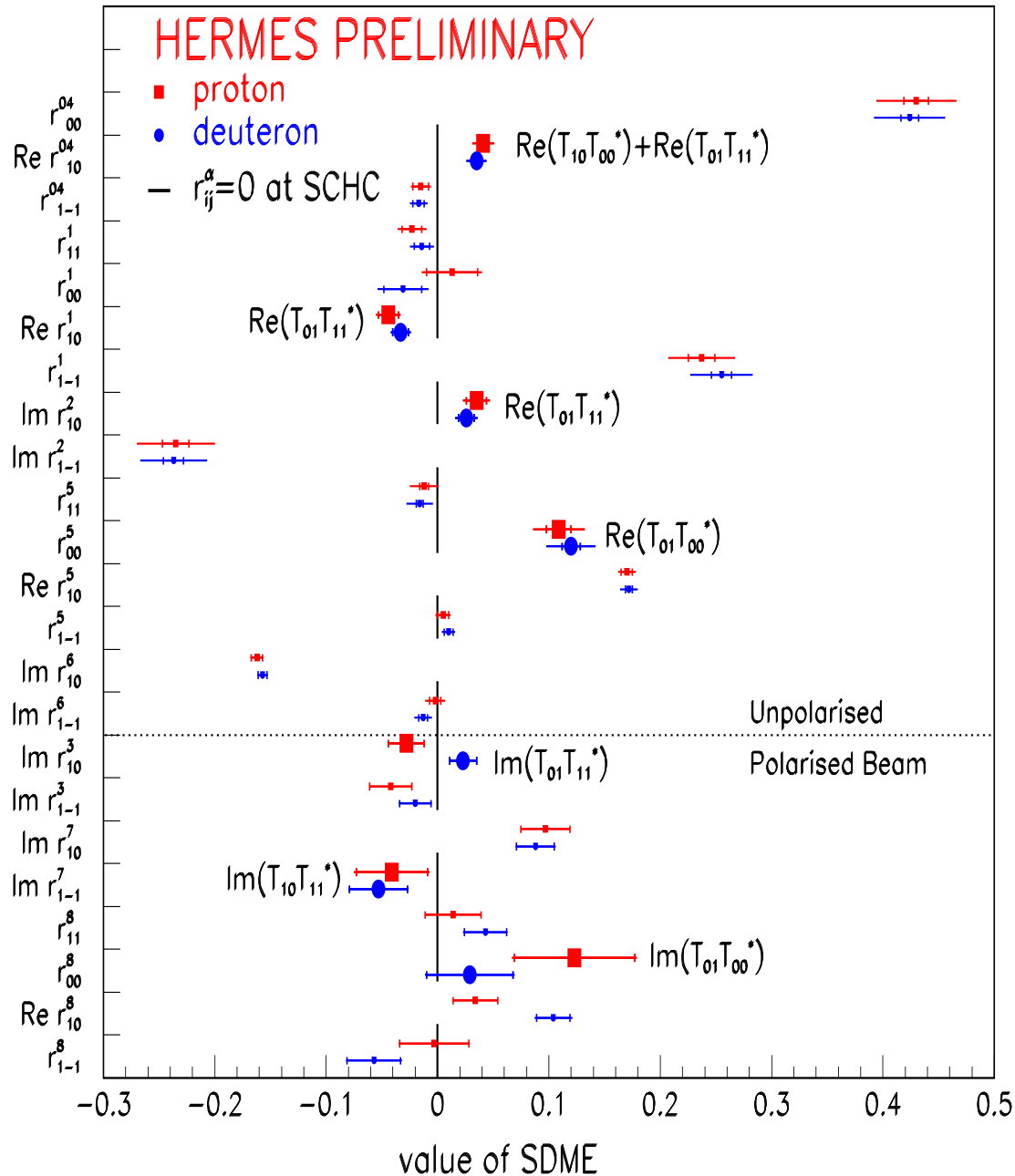
- Simulated Events: matrix of fully reconstructed MC events at initial uniform angular distribution
- Binned Maximum Likelihood Method:  $8 \times 8 \times 8$  bins of  $\cos(\Theta)$ ,  $\phi$ ,  $\Phi$ . Simultaneous fit of 23 SDMEs  $r_{ij}^\alpha = W(\Phi, \phi, \cos \Theta)$  for data with negative and positive beam helicity ( $\langle P_b \rangle = 53.5\%$ )

**$\Rightarrow$  Full agreement of fitted angular distributions with data**



# 23 Spin Density Matrix Elements $r_{\lambda\rho\lambda'\rho'}^\alpha$ from $\gamma^* + N \rightarrow \rho^0 + N'$

at  $0 < t' < 0.4 \text{ GeV}^2$  and  $1 < Q^2 < 5 \text{ GeV}^2$



- $\gamma^* + N \rightarrow \rho^0(\phi) + N'$  is perfect to study the spin structure of production mechanism:

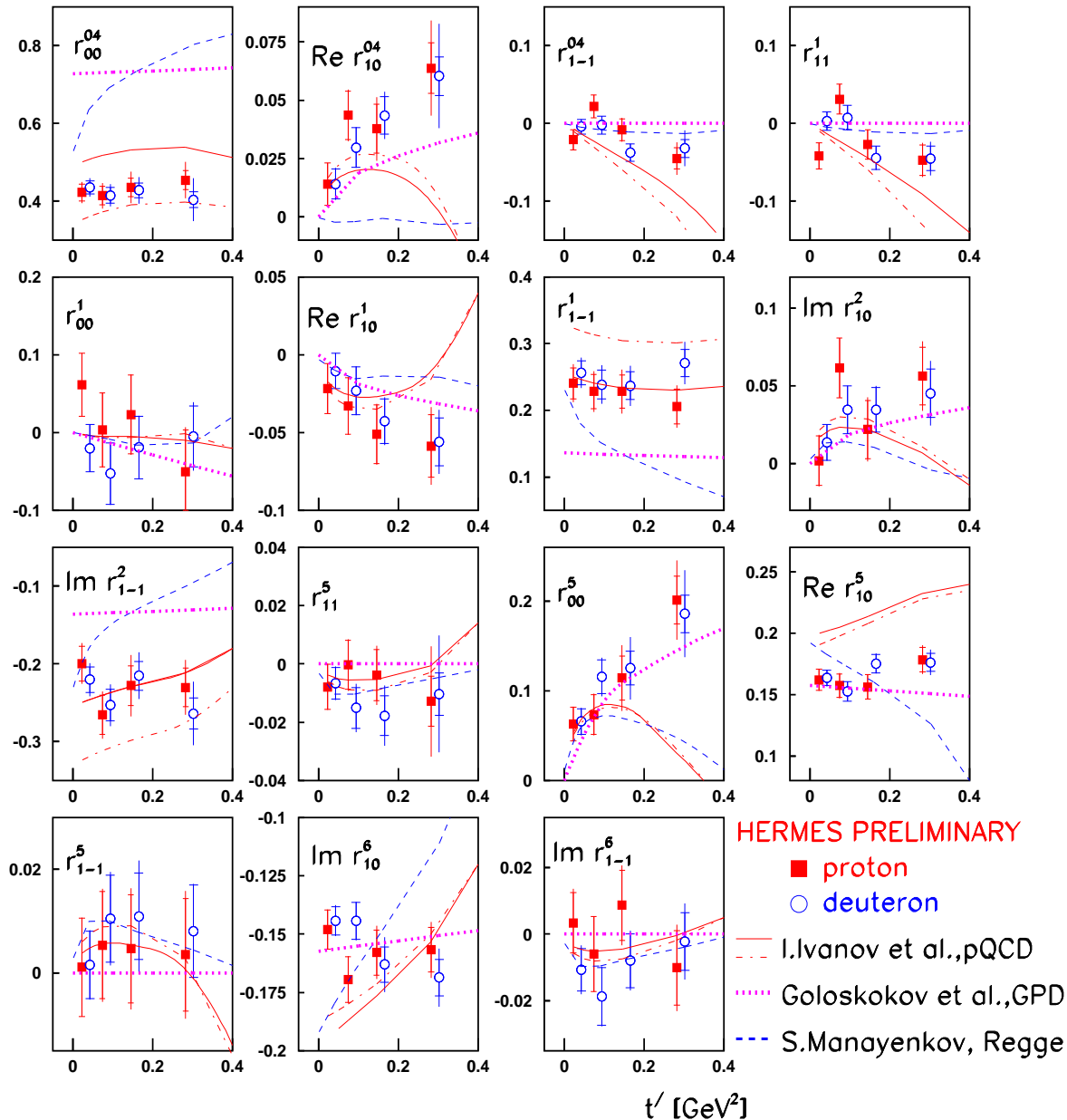
  - spin state of  $\gamma^*$  is known
  - $\rho^0 \rightarrow \pi^+ \pi^-$  decay is self-analysing
- SDMEs:  $r_{\lambda\rho\lambda'\rho'}^\alpha \sim \rho(V) = \frac{1}{2} T \rho(\gamma) T^+$  in terms of the photon matrix  $\rho(\gamma)$  and helicity amplitude  $T_{\lambda_V \lambda_\gamma}$

$\Rightarrow$  Beam-polarization dependent SDMEs, in a first time
- SCHC?

$\Rightarrow$  enlarged SDMEs violating SCHC ( $2 \div 5 \sigma$ ), indicating non-zero spin-flip amplitudes:  $T_{01}, T_{10}, T_{1-1}$
- $q\bar{q}$ -exchange with isospin 1 can be observed in case of difference between proton and deuteron data

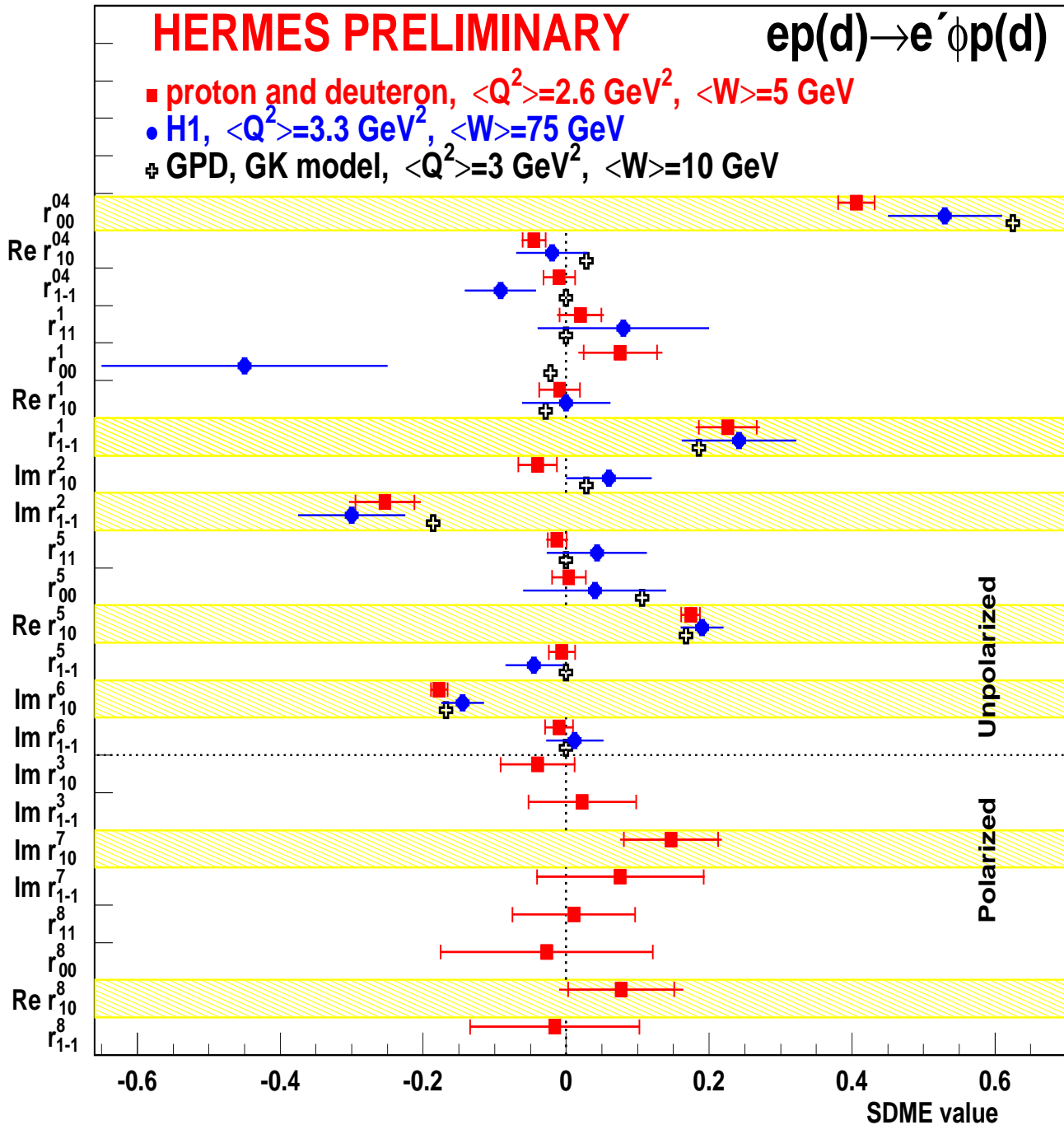
$\Rightarrow$  No significant difference between proton and deuteron

# $t'$ -Dependence of $\rho^0$ SDMEs Compared with Calculations



- GK model calculations done for  $Q^2 > 3.0 \text{ GeV}^2$  for two-gluon exchange only (S.V.Goloskokov and P.Kroll, Eur.Phys.J. C 42 (2005) 281)
- Incorporation of quark-exchange into GK model is under development
- Reasonable agreement for a majority of SDMEs (12 elements) at low  $t'$ :  $\text{Re } r_{10}^{04}, r_{00}^5 \dots$
- The most crucial disagreement with data for GK model:  $r_{00}^{04}, r_{1-1}^1, \text{Im}\{r_{1-1}^2\}$  connected with  $\sigma_L/\sigma_T$  ratio
- No model describes well all unpolarized SDMEs.

# $\phi$ Meson SDMEs Compared with Calculations and High Energy Data



- Note: GK model calculations done for  $Q^2 = 3.0 \text{ GeV}^2$  and two-gluon exchange

⇒ Reasonable agreement for a majority of SDMEs

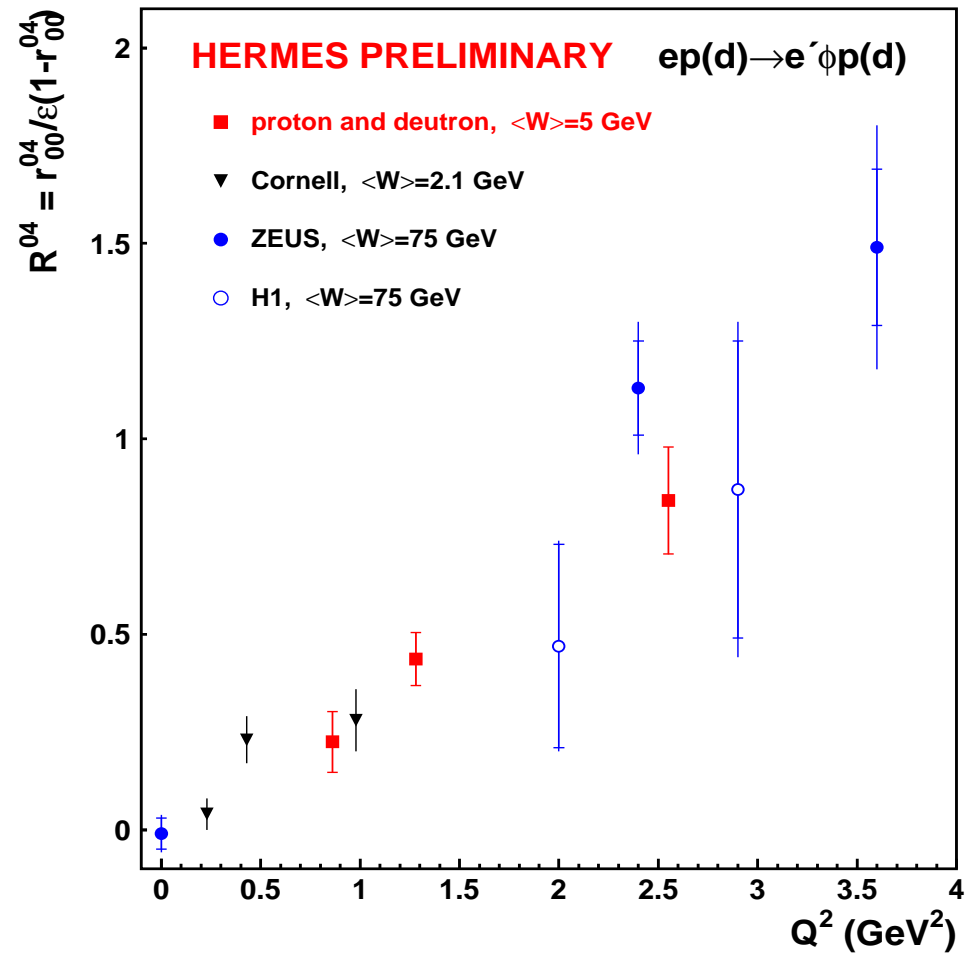
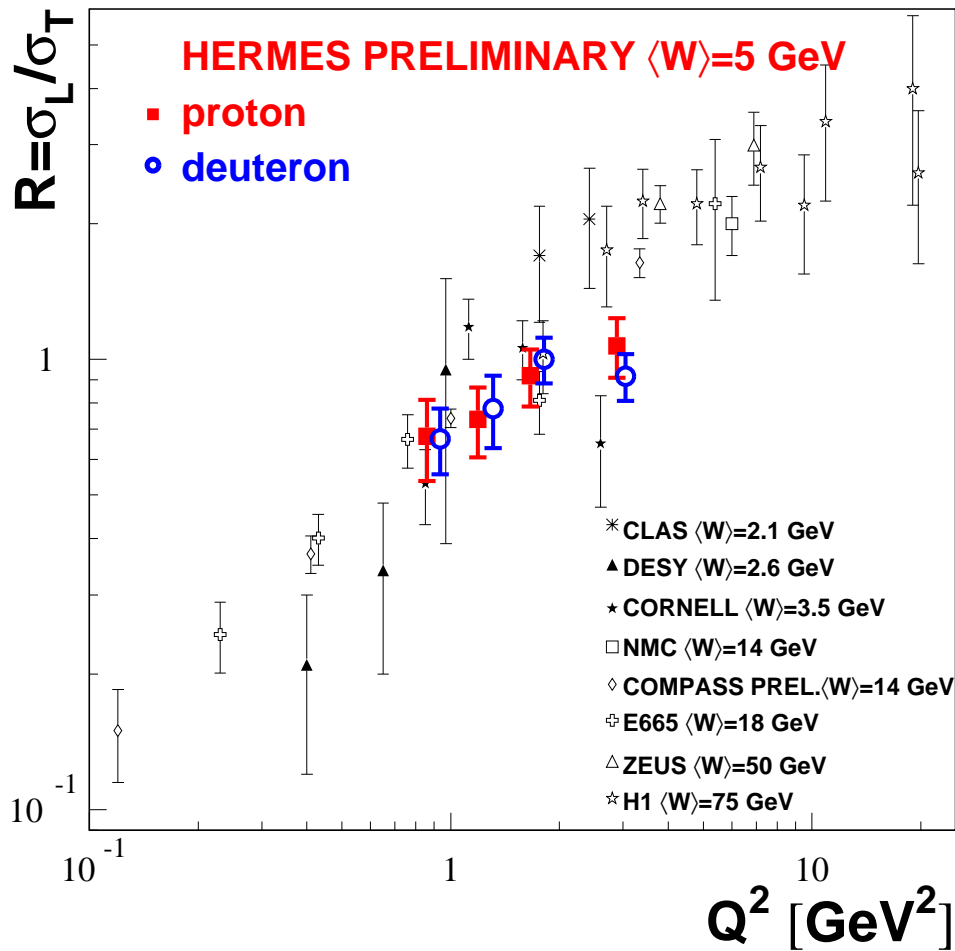
- Disagreement with data for GK Model:

- $r_{00}^{04} \rightarrow \sigma_L / \sigma_T$  ratio
- $r_{00}^5 \rightarrow$  SCHC in data, but not in the model

⇒ Further development of GK model

# $\rho^0$ and $\phi$ Longitudinal-to-Transverse Cross-Section Ratio $R^{04} = \frac{1}{\epsilon} \frac{r_{00}^{04}}{1-r_{00}^{04}}$ ,

where  $r_{00}^{04} = \sum\{\epsilon|T_{00}|^2 + |T_{01}|^2 + |U_{01}|^2\}/\sigma_{tot}$ ,  $\sigma_{tot} = \epsilon\sigma_L + \sigma_T$   
 $\sigma_T = \sum\{|T_{11}|^2 + |T_{01}|^2 + |T_{1-1}|^2 + |U_{11}|^2\}$ ,  $\sigma_L = \sum\{|T_{00}|^2 + 2|T_{10}|^2\}$



⇒ Due to the helicity-flip and unnatural parity amplitudes  $R^{04}$  depends on kinematic conditions, and is not identical to  $R \equiv |T_{00}|^2/|T_{11}|^2$  at SCHC and NPE dominance

⇒ HERMES  $\rho^0$  data are suggestive to  $R(W)$ -dependence

# SDMEs According to Hierarchy of Amplitudes without & with Helicity Flip: $\rho^0$ , $\phi$

- A,  $\gamma_L^* \rightarrow \rho_L^0$  and  $\gamma_T^* \rightarrow \rho_T^0$   
 $|T_{11}|^2 \propto 1 - r_{00}^{04} \propto r_{1-1}^1 \propto -Im\{r_{1-1}^2\}$

- B, Interference:  $\gamma_L^*, \rho_T^0$   
 $Re\{T_{00}T_{11}^*\} \propto Re\{r_{10}^5\} \propto -Im\{r_{10}^6\}$   
 $Im\{T_{11}T_{00}^*\} \propto Im\{r_{10}^7\} \propto Re\{r_{10}^8\}$

- C, Spin Flip:  $\gamma_T^* \rightarrow \rho_L^0$   
 $Re\{T_{11}T_{01}^*\} \propto Re\{r_{10}^{04}\} \propto Re\{r_{10}^1\} \propto Im\{r_{10}^2\}$   
 $Re\{T_{01}T_{00}^*\} \propto r_{00}^5$   
 $|T_{01}|^2 \propto r_{00}^1$   
 $Im\{T_{01}T_{11}^*\} \propto Im\{r_{10}^3\}$   
 $Im\{T_{01}T_{00}^*\} \propto r_{00}^8$

- D, Spin Flip:  $\gamma_L^* \rightarrow \rho_T^0$   
 $Re\{T_{10}T_{11}^*\} \propto r_{11}^5 \propto r_{1-1}^5 \propto Im\{r_{1-1}^6\}$   
 $Im\{T_{10}T_{11}^*\} \propto Im\{r_{1-1}^7\} \propto r_{11}^8 \propto r_{1-1}^8$

- E, Spin Flip:  $\gamma_T^* \rightarrow \rho_{-T}^0$   
 $Re\{T_{1-1}T_{11}^*\} \propto r_{1-1}^{04} \propto r_{11}^1$   
 $Im\{T_{1-1}T_{11}^*\} \propto Im\{r_{1-1}^3\}$

$$\begin{aligned} & 1 - r_{00}^{04} \\ & 2 r_{1-1}^1 \\ & -2 \operatorname{Im} r_{1-1}^2 \\ & 2\sqrt{2} \operatorname{Re} r_{10}^5 \\ & -2\sqrt{2} \operatorname{Im} r_{10}^6 \\ & 2\sqrt{2} \operatorname{Im} r_{10}^7 \\ & 2\sqrt{2} \operatorname{Re} r_{10}^8 \\ & 2 \operatorname{Re} r_{10}^{04} \\ & -2 \operatorname{Re} r_{10}^1 \\ & 2 \operatorname{Im} r_{10}^2 \\ & 1/\sqrt{2} r_{00}^5 \\ & -r_{00}^1 \\ & 2 \operatorname{Im} r_{10}^3 \\ & -1/\sqrt{2} r_{00}^8 \\ & \sqrt{2} r_{11}^5 \\ & -\sqrt{2} r_{1-1}^5 \\ & \sqrt{2} \operatorname{Im} r_{1-1}^6 \\ & -\sqrt{2} \operatorname{Im} r_{1-1}^7 \\ & \sqrt{2} r_{11}^8 \\ & -\sqrt{2} r_{1-1}^8 \\ & r_{1-1}^{04} \\ & r_{11}^1 \\ & \operatorname{Im} r_{1-1}^3 \end{aligned}$$

## HERMES PRELIMINARY

■  $\rho^0$  proton,  $\langle Q^2 \rangle = 1.9 \text{ GeV}^2$ ,  $\langle W \rangle = 5 \text{ GeV}$

●  $\phi$  proton and deuteron

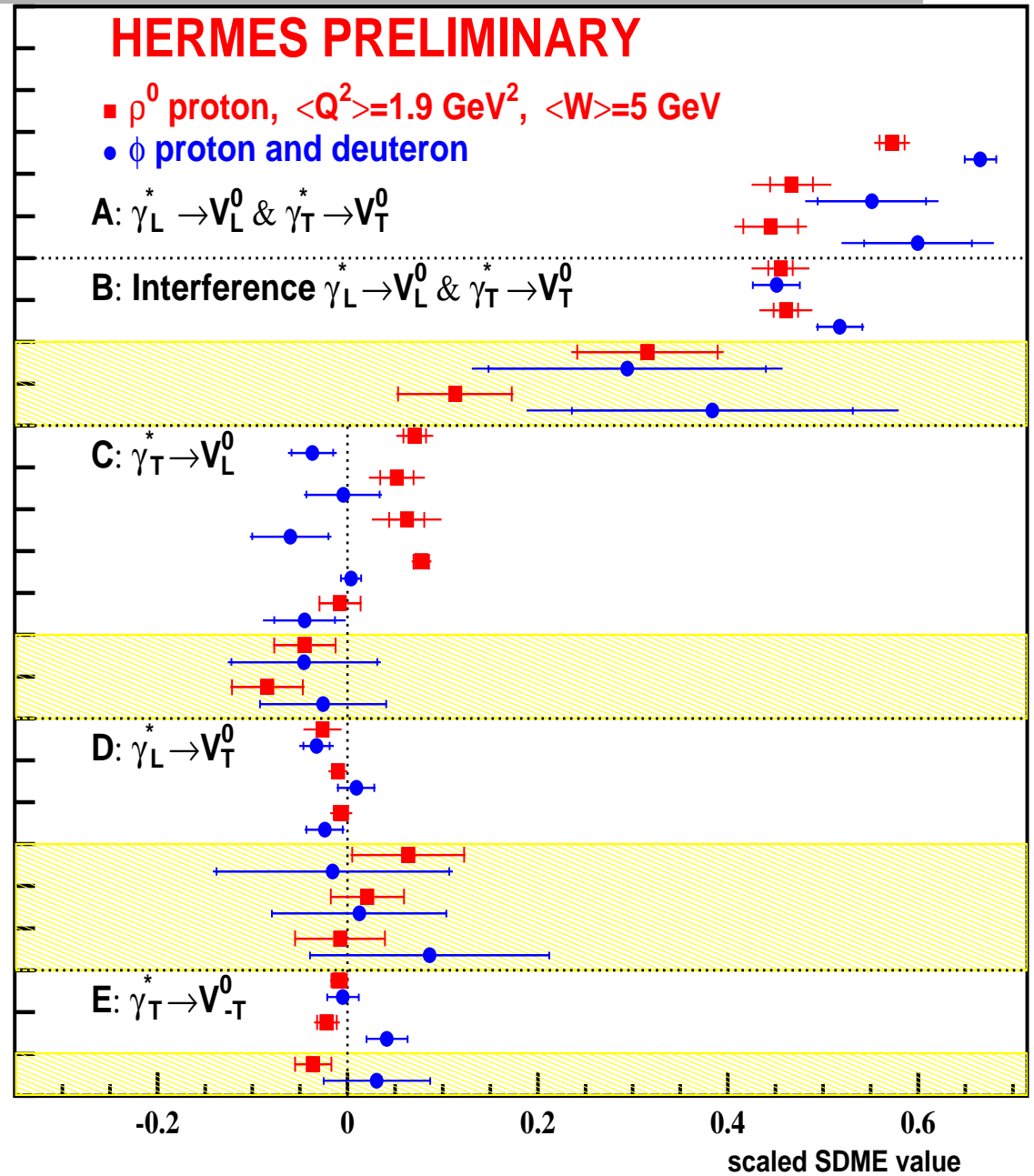
A:  $\gamma_L^* \rightarrow V_L^0$  &  $\gamma_T^* \rightarrow V_T^0$

B: Interference  $\gamma_L^* \rightarrow V_L^0$  &  $\gamma_T^* \rightarrow V_T^0$

C:  $\gamma_T^* \rightarrow V_L^0$

D:  $\gamma_L^* \rightarrow V_T^0$

E:  $\gamma_T^* \rightarrow V_{-T}^0$

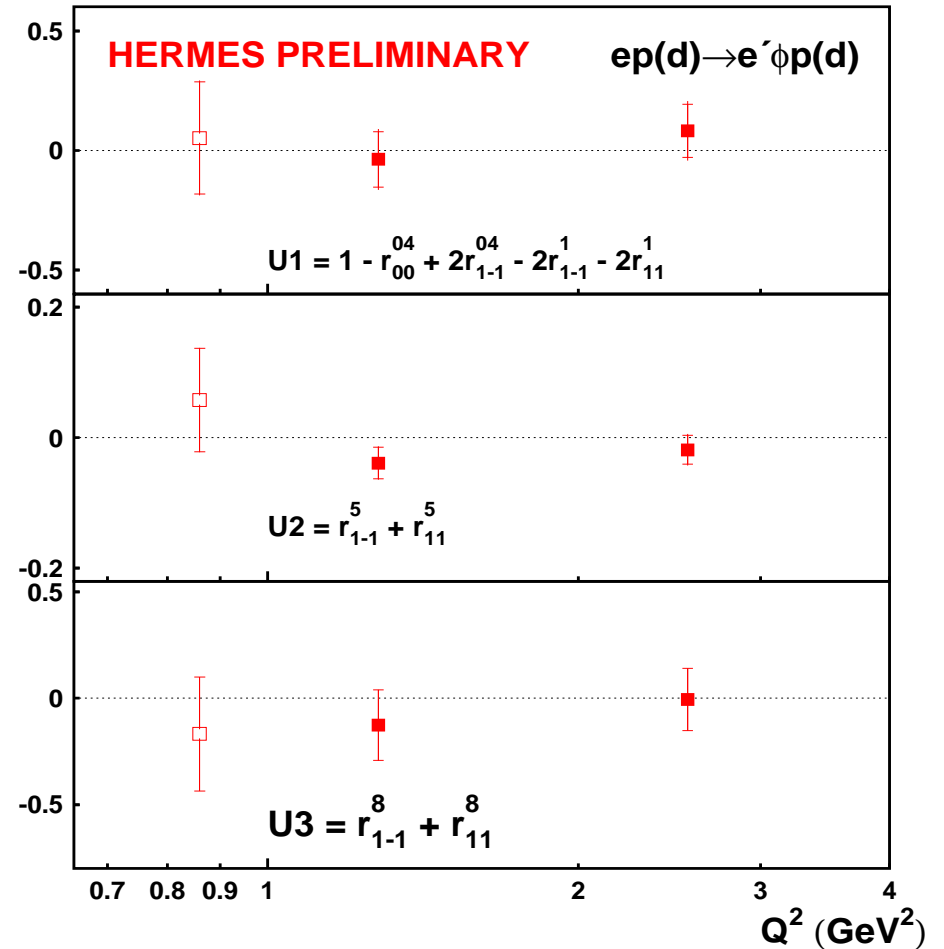
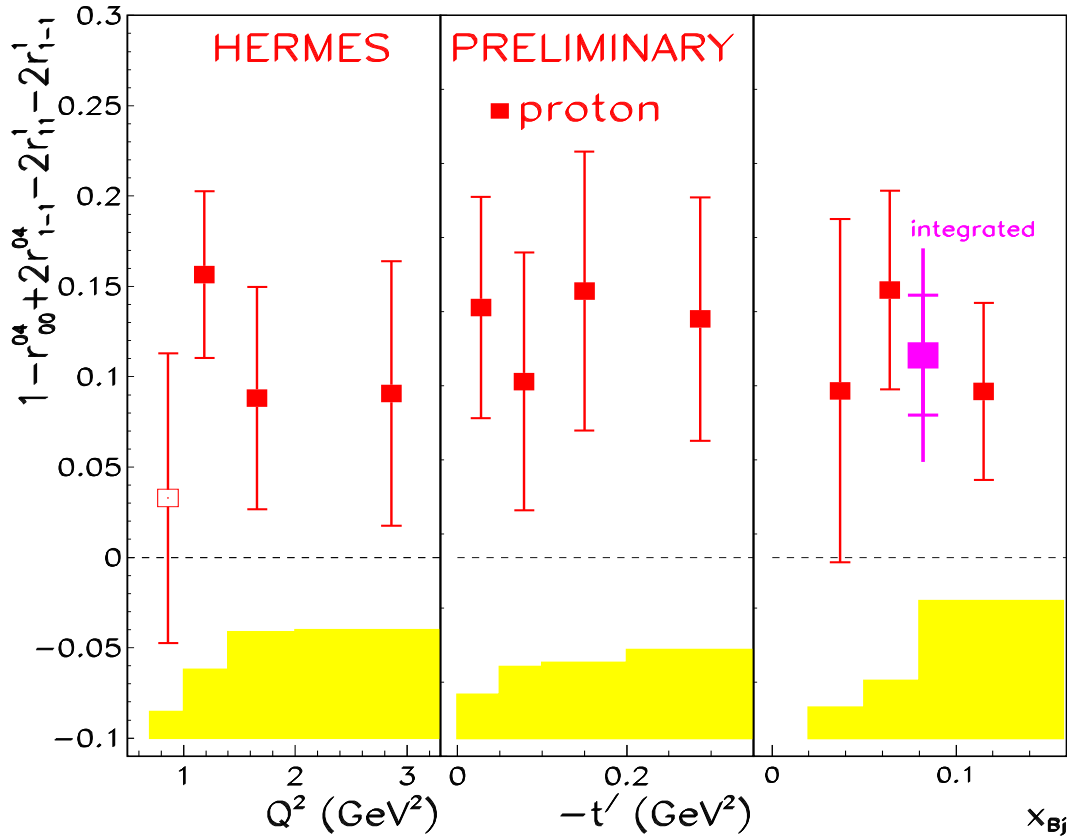


⇒ **Hierarchy of  $\rho^0$  amplitudes:**  $|T_{00}| \sim |T_{11}| \gg |T_{01}| > |T_{10}| \gtrsim |T_{1-1}|$ , ( $0 \rightarrow L, 1 \rightarrow T$ )

⇒  $\phi$  meson SDMEs are consistent with SCHC,  $|T_{00}| \sim |T_{11}|$

# Observation of Unnatural-parity-exchange (UPE) in $\rho^0$ Leptoproduction

- Natural-parity exchange: interaction is mediated by a particle of 'natural' parity: vector or scalar meson:  $J^P = 0^+, 1^-$  e.g.  $\rho^0, \omega, a_2$
- Unnatural parity exchange is mediated by pseudoscalar or axial meson:  $J^P = 0^-, 1^+$ , e.g.  $\pi, a_1, b_1$
- UPE amplitudes correspond to the contributions of polarized GPDs:  $E, \tilde{E}$



$\Rightarrow$  no UPE for  $\phi$  meson production

p:  $U1 = 2|U_{11}|^2 = 0.132 \pm 0.026_{st} \pm 0.053_{syst}$

d:  $U1 = 0.094 \pm 0.020_{st} \pm 0.044_{syst}$

$U2 \propto |U_{10}|^2 = 0, U3 \propto |U_{01}|^2 = 0$

$\Rightarrow$  Indication on hierarchy of  $\rho^0$  UPE amplitudes:  $|U_{11}| \gg |U_{10}| \sim |U_{01}|$

## Summary

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- $\rho$  data:
  - Longitudinal cross section well described by GPD models
  - Incorporation of *quark-exchange* mechanism for calculation of 15 beam-polarization-independent SDMEs in GK model is under way
  - Further tuning of GK model for transversal cross section
  - $R \equiv \sigma_L/\sigma_T$  ratio is suggestive to  $W$ -dependence
  - Hierarchy of (un)natural helicity transfer amplitudes is established
- $\phi$  meson data:
  - Total and Longitudinal cross section consistent with *two-gluon* exchange
  - SCHC dominance
  - Further tuning of GK model for transversal cross section
  - $R \equiv \sigma_L/\sigma_T$  is consistent with world data
  - Natural-parity-exchange dominance

...Target-polarization dependent SDMEs are under analysis

**More data from 2006-2007 will be available**

**BACKUP SLIDES !!!**

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# Equations for Unpolarized SDMEs from Helicity Transfer Amplitudes

$$D = \epsilon N_L + N_T$$

$$N_T = \sum^* \{|T_{11}^N|^2 + |T_{01}^N|^2 + |T_{1-1}^N|^2 + |T_{11}^U|^2 + |T_{01}^U|^2 + |T_{1-1}^U|^2\}$$

$$N_L = \sum^* \{|T_{00}|^2 + 2|T_{10}^N|^2 + 2|T_{10}^U|^2\}$$

$$r_{00}^{04} = \sum^* \{\epsilon |T_{00}|^2 + |T_{01}^N|^2 + |T_{01}^U|^2\} / D$$

$$\Re\{r_{10}^{04}\} = \sum^* \Re\{\epsilon T_{10}^N T_{00}^* + \frac{1}{2} T_{01}^N (T_{11}^N - T_{1-1}^N)^* + \frac{1}{2} T_{01}^U (T_{11}^U + T_{1-1}^U)^*\} / D$$

$$r_{1-1}^{04} = \sum^* \Re\{-\epsilon |T_{10}^N|^2 + \epsilon |T_{10}^U|^2 + T_{1-1}^N (T_{11}^N)^* - T_{1-1}^U (T_{11}^U)^*\} / D$$

$$r_{11}^1 = \sum^* \Re\{T_{1-1}^N (T_{11}^N)^* + T_{1-1}^U (T_{11}^U)^*\} / D$$

$$r_{00}^1 = \sum^* \{-|T_{01}^N|^2 + |T_{01}^U|^2\} / D$$

$$\Re\{r_{10}^1\} = \frac{1}{2} \sum^* \Re\{-T_{01}^N (T_{11}^N - T_{1-1}^N)^* + T_{01}^U (T_{11}^U + T_{1-1}^U)^*\} / D$$

$$r_{1-1}^1 = \frac{1}{2} \sum^* \{|T_{11}^N|^2 + |T_{1-1}^N|^2 - |T_{11}^U|^2 - |T_{1-1}^U|^2\} / D \sim |T_{11}^N|^2 - |T_{11}^U|^2$$

$$\Im\{r_{1-1}^2\} = \frac{1}{2} \sum^* \{-|T_{11}^N|^2 + |T_{1-1}^N|^2 + |T_{11}^U|^2 - |T_{1-1}^U|^2\} / D \sim -|T_{11}^N|^2 + |T_{11}^U|^2$$

$$\Im\{r_{10}^2\} = \frac{1}{2} \sum^* \Re\{T_{01}^N (T_{11}^N + T_{1-1}^N)^* - T_{01}^U (T_{11}^U - T_{1-1}^U)^*\} / D$$

$$r_{11}^5 = \frac{1}{\sqrt{2}} \sum^* \Re\{T_{10}^N (T_{11}^N - T_{1-1}^N)^* + T_{10}^U (T_{11}^U - T_{1-1}^U)^*\} / D$$

$$r_{00}^5 = \sqrt{2} \sum^* \Re\{T_{01}^N T_{00}^*\} / D \quad \Re r_{10}^5 = \frac{1}{\sqrt{8}} \sum^* \Re\{2T_{10}^N (T_{01}^N)^* + (T_{11}^N - T_{1-1}^N) T_{00}^*\} / D$$

$$r_{1-1}^5 = \frac{1}{\sqrt{2}} \sum^* \Re\{-T_{10}^N (T_{11}^N - T_{1-1}^N)^* + T_{10}^U (T_{11}^U - T_{1-1}^U)^*\} / D$$

→  $T_{11}^U$  decreases  $r_{1-1}^1$  and increases  $\Im\{r_{1-1}^2\}$  No other SDMEs contain  $T_{11}^U$  in the numerator

→ can be checked with SDMEs!

→  $T_{10}^U, T_{01}^U, T_{1-1}^U$  omitted in the fit function

# Equations for Polarized SDMEs from Helicity Transfer Amplitudes

---

$$\begin{aligned}
\Im r_{10}^6 &= \frac{1}{\sqrt{8}} \sum^* \Re \{ 2T_{10}^U (T_{01}^U)^* - (T_{11}^N + T_{1-1}^N) T_{00}^* \} / D \\
\Im r_{1-1}^6 &= \frac{1}{\sqrt{2}} \sum^* \Re \{ T_{10}^N (T_{11}^N + T_{1-1}^N)^* - T_{10}^U (T_{11}^U + T_{1-1}^U)^* \} / D \\
\Im r_{10}^3 &= -\frac{1}{2} \sum^* \Im \{ T_{01}^N (T_{11}^N + T_{1-1}^N)^* + T_{01}^U (T_{11}^U - T_{1-1}^U)^* \} / D \\
\Im r_{1-1}^3 &= -\sum^* \Im \{ T_{1-1}^N (T_{11}^N)^* - T_{1-1}^U (T_{11}^U)^* \} / D \\
\Im r_{10}^7 &= \frac{1}{\sqrt{8}} \sum^* \Im \{ 2T_{10}^U (T_{01}^U)^* + (T_{11}^N + T_{1-1}^N) T_{00}^* \} / D \\
\Im r_{1-1}^7 &= \frac{1}{\sqrt{2}} \sum^* \Im \{ T_{10}^N (T_{11}^N + T_{1-1}^N)^* - T_{10}^U (T_{11}^U + T_{1-1}^U)^* \} / D \\
r_{11}^8 &= -\frac{1}{\sqrt{2}} \sum^* \Im \{ T_{10}^N (T_{11}^N - T_{1-1}^N)^* + T_{10}^U (T_{11}^U - T_{1-1}^U)^* \} / D \\
r_{00}^8 &= \sqrt{2} \sum^* \Im \{ T_{01}^N T_{00}^* \} / D \\
\Re r_{10}^8 &= \frac{1}{\sqrt{8}} \sum^* \Im \{ -2T_{10}^N (T_{01}^N)^* + (T_{11}^N - T_{1-1}^N) T_{00}^* \} / D \\
r_{1-1}^8 &= \frac{1}{\sqrt{2}} \sum^* \Im \{ T_{10}^N (T_{11}^N - T_{1-1}^N)^* - T_{10}^U (T_{11}^U - T_{1-1}^U)^* \} / D
\end{aligned}$$

# Function for the Fit of 23 SDME $r_{ij}^\alpha$

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$$W(\cos \Theta, \phi, \Phi) = W^{unpol} + W^{long.pol},$$

$$W^{unpol}(\cos \Theta, \phi, \Phi) = \frac{3}{8\pi^2} \left[ \frac{1}{2}(1 - r_{00}^{04}) + \frac{1}{2}(3r_{00}^{04} - 1) \cos^2 \Theta - \sqrt{2}\text{Re}\{r_{10}^{04}\} \sin 2\Theta \cos \phi - r_{1-1}^{04} \sin^2 \Theta \cos 2\phi \right.$$

$$- \epsilon \cos 2\Phi \left( r_{11}^1 \sin^2 \Theta + r_{00}^1 \cos^2 \Theta - \sqrt{2}\text{Re}\{r_{10}^1\} \sin 2\Theta \cos \phi - r_{1-1}^1 \sin^2 \Theta \cos 2\phi \right)$$

$$- \epsilon \sin 2\Phi \left( \sqrt{2}\text{Im}\{r_{10}^2\} \sin 2\Theta \sin \phi + \text{Im}\{r_{1-1}^2\} \sin^2 \Theta \sin 2\phi \right)$$

$$+ \sqrt{2\epsilon(1 + \epsilon)} \cos \Phi \left( r_{11}^5 \sin^2 \Theta + r_{00}^5 \cos^2 \Theta - \sqrt{2}\text{Re}\{r_{10}^5\} \sin 2\Theta \cos \phi - r_{1-1}^5 \sin^2 \Theta \cos 2\phi \right)$$

$$+ \sqrt{2\epsilon(1 + \epsilon)} \sin \Phi \left( \sqrt{2}\text{Im}\{r_{10}^6\} \sin 2\Theta \sin \phi + \text{Im}\{r_{1-1}^6\} \sin^2 \Theta \sin 2\phi \right) \left. \right],$$

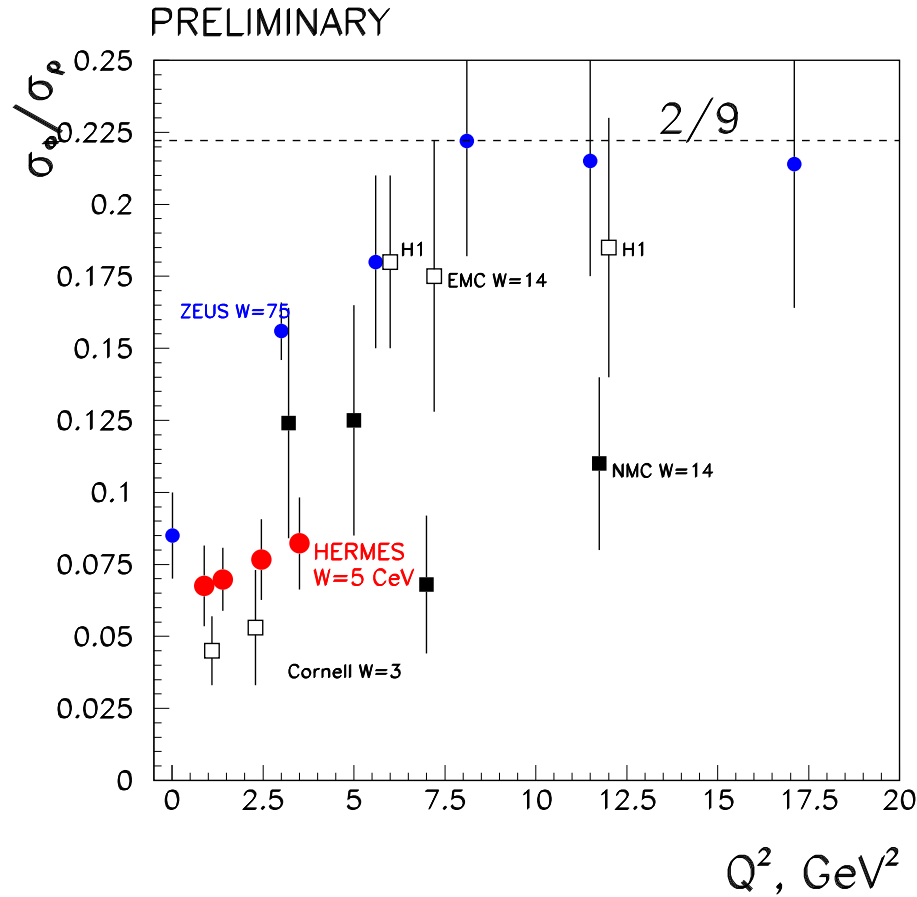
$$W^{long.pol.}(\cos \Theta, \phi, \Phi) = \frac{3}{8\pi^2} P_{beam} \left[ \sqrt{1 - \epsilon^2} \left( \sqrt{2}\text{Im}\{r_{10}^3\} \sin 2\Theta \sin \phi + \text{Im}\{r_{1-1}^3\} \sin^2 \Theta \sin 2\phi \right) \right.$$

$$+ \sqrt{2\epsilon(1 - \epsilon)} \cos \Phi \left( \sqrt{2}\text{Im}\{r_{10}^7\} \sin 2\Theta \sin \phi + \text{Im}\{r_{1-1}^7\} \sin^2 \Theta \sin 2\phi \right)$$

$$+ \sqrt{2\epsilon(1 - \epsilon)} \sin \Phi \left( r_{11}^8 \sin^2 \Theta + r_{00}^8 \cos^2 \Theta - \sqrt{2}\text{Re}\{r_{10}^8\} \sin 2\Theta \cos \phi - r_{1-1}^8 \sin^2 \Theta \cos 2\phi \right) \left. \right]$$

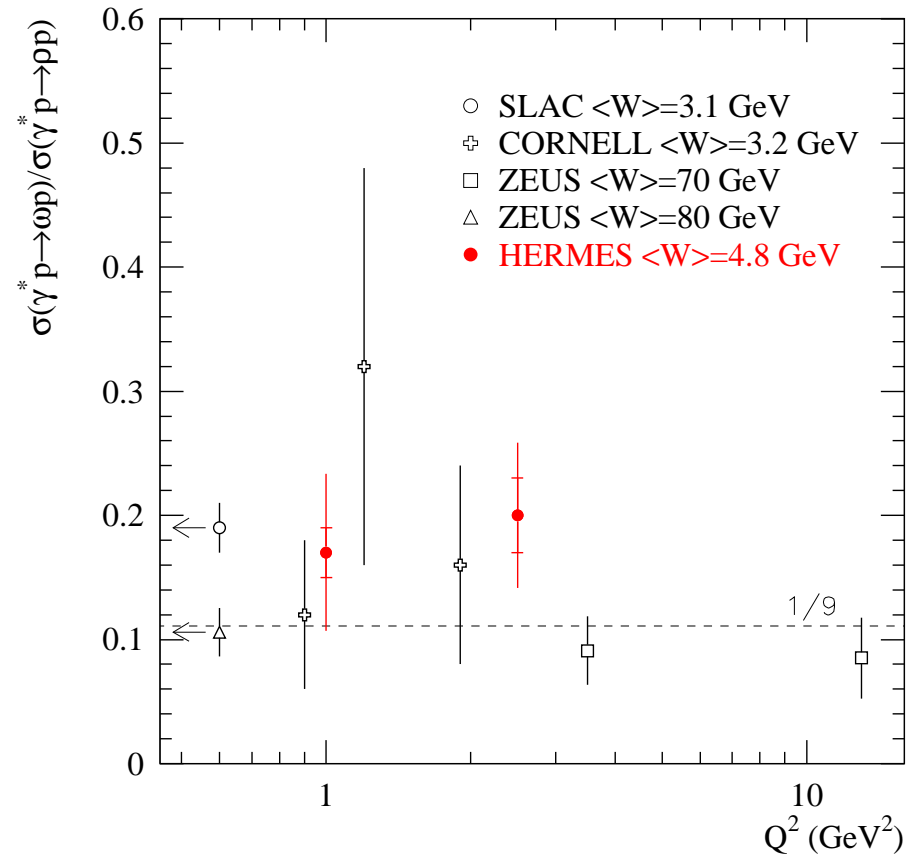
# Cross Section Ratios: $\sigma_\phi/\sigma_{\rho^0}$ , $\sigma_\omega/\sigma_{\rho^0}$

Asymptotic SU(4) pQCD predicts:  $\rho^0 : \omega : \phi : J/\Psi = 9 : 1 : 2 : 8$



→  $W$ -dependence at  $Q^2 = 2.5 \sim 4 \text{ GeV}^2$

→ Substantial two-gluon contribution for  $\rho^0$   
(M.Diehl and A.V.Vinnikov Phys.Lett. **B609** (2005) 286)



→  $W$ -dependence of  $\sigma_\omega/\sigma_{\rho^0}$

→ VGG model:  $\sigma_L^\omega/\sigma_L^{\rho^0} \sim 0.2$

# $\rho^0/\phi$ ratio of $\sigma_L$ from GK model

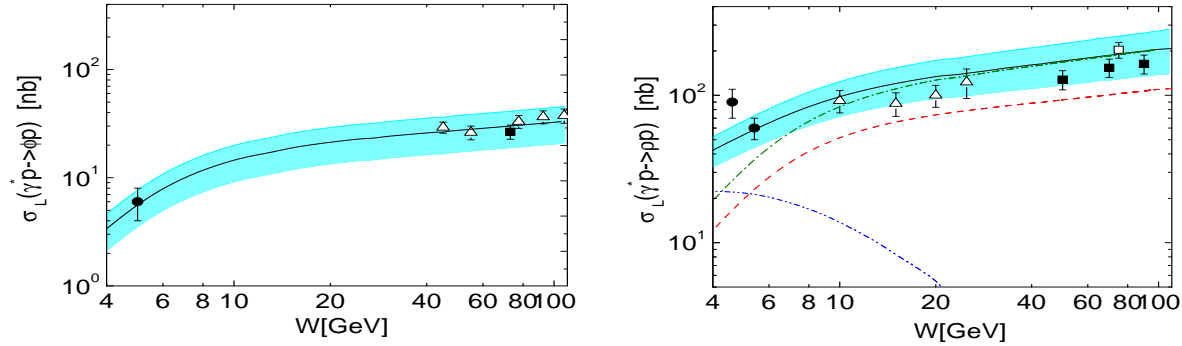


Figure 11: The longitudinal cross section for  $\phi$  (left) and  $\rho$  (right) electroproduction versus  $W$  at  $Q^2 = 3.8 \text{ GeV}^2$  and  $4 \text{ GeV}^2$ , respectively. The handbag predictions are evaluated from the interval  $-t' \leq 0.5 \text{ GeV}^2$ . Data for  $\phi$  production are taken from HERMES [41] (solid circle), ZEUS [13] (open triangles) and H1 [37] (solid square). The data for  $\rho$  production are taken from HERMES [42] (solid circles), E665 [43] (open triangles), ZEUS [12] (open square) and H1 [11] (solid square). The dashed (dash-dotted, dash-dot-dotted) line represents the gluon (gluon + sea, (gluon + sea)-valence interference plus valence quark) contribution. For other notations cf. Fig. 7.

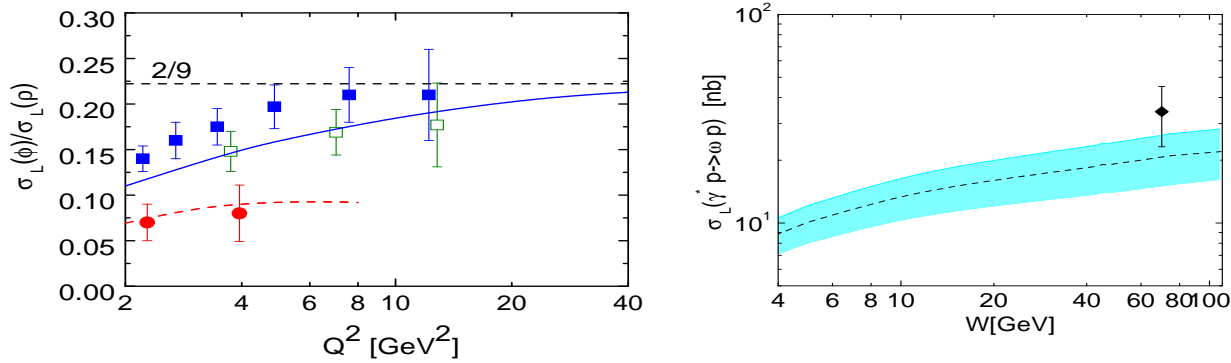
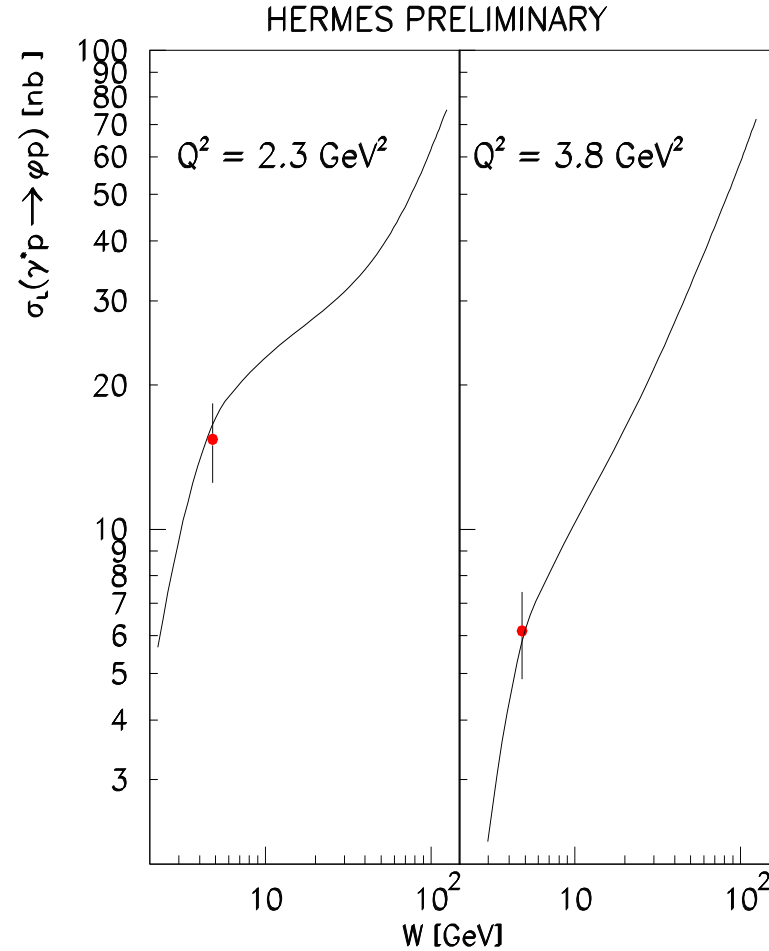
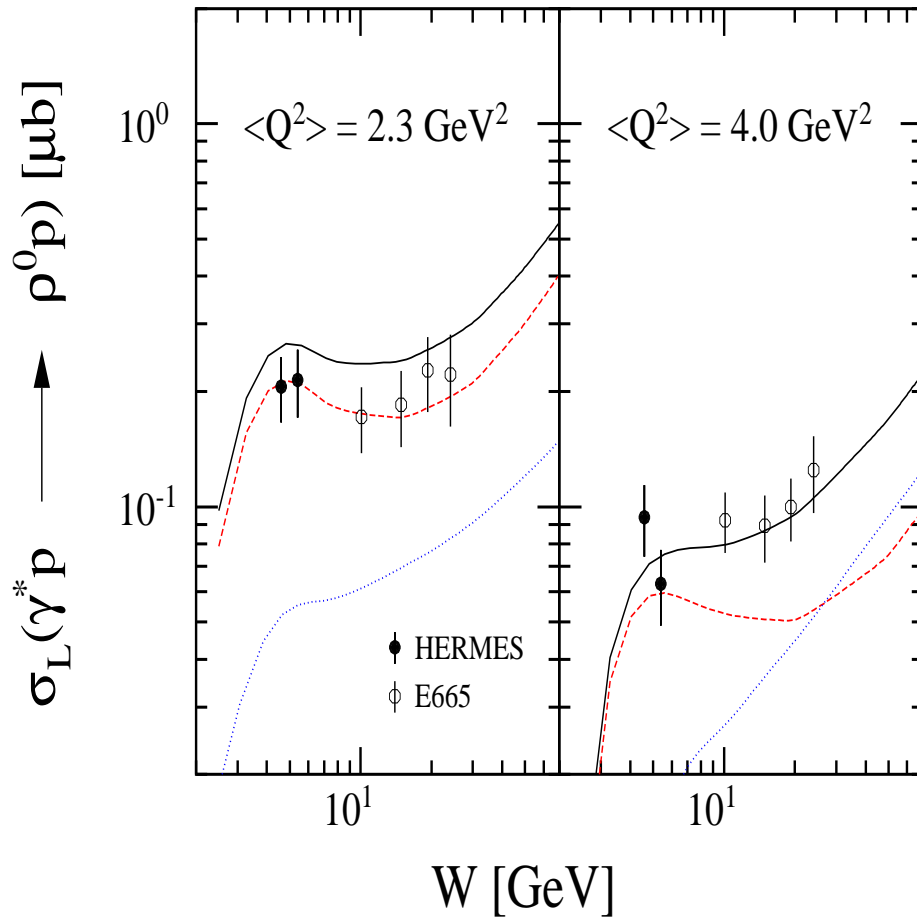


Figure 12: Left: The ratio of the longitudinal cross sections for  $\phi$  and  $\rho$  production. Data are taken from H1 [11, 37] (solid squares), ZEUS [12, 13] (open squares) and HERMES [41, 42] (solid circles). The solid (dashed) line represents the handbag predictions at  $W = 75(5) \text{ GeV}$ . Right: Predictions for  $\omega$  electroproduction versus  $W$  at  $Q^2 = 3.5 \text{ GeV}^2$ . For comparison the full cross section for  $\omega$  production, measured by ZEUS [49], is also shown (solid diamond).

# $\rho^0$ and $\phi$ Longitudinal Cross Sections, and VGG Model

first approach: GPD calculations of M.Vanderhaeghen, P.A.M. Guichon, M. Guidal, Phys.Rev.Let. **80** 5064, (1998); Phys.Rev.D **60** 094017 (1999)



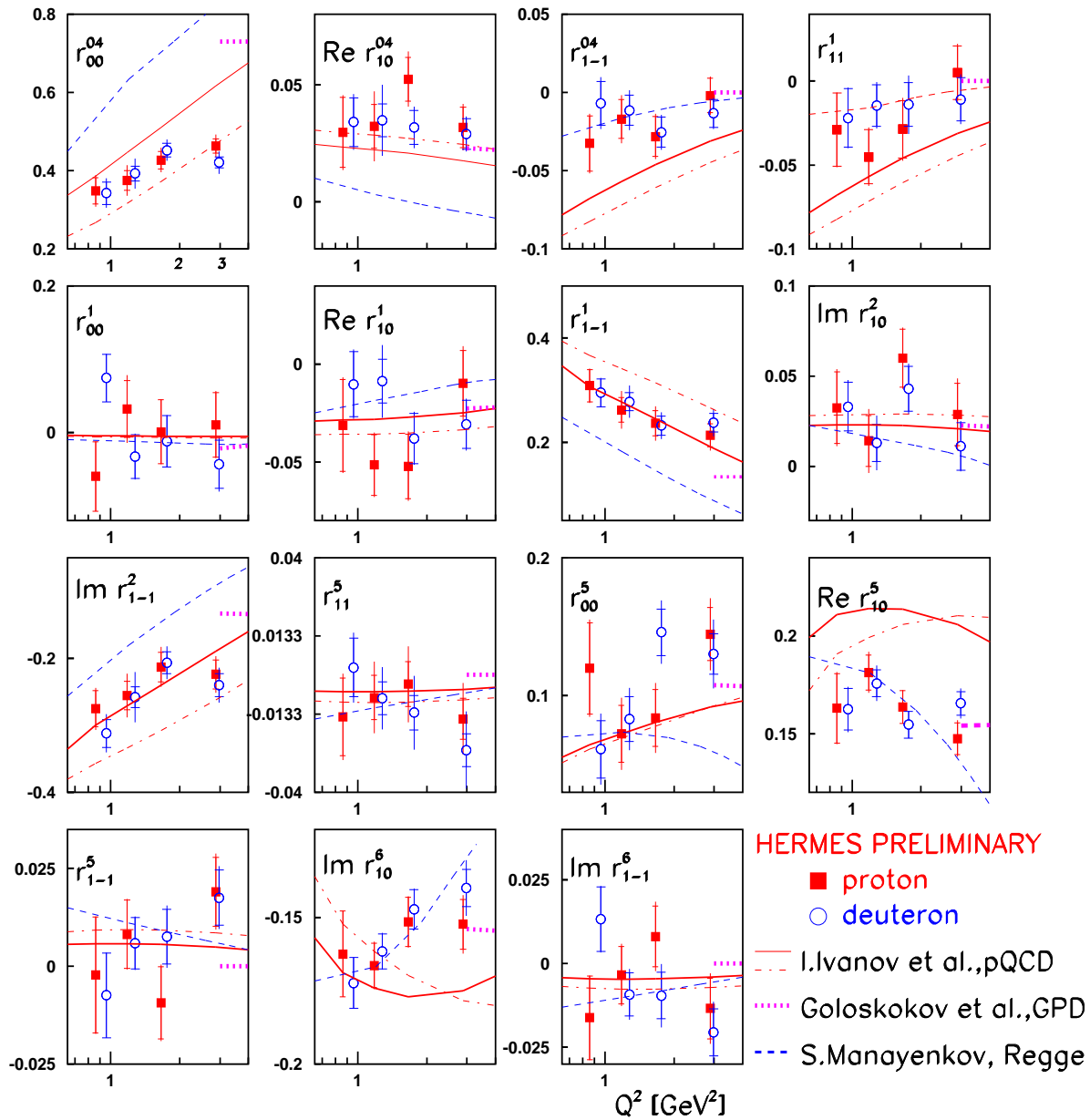
2-gluon exchange, quark exchange, sum of both,

two-gluon exchange for  $\phi$

→ Domination of quark exchange for  $\rho^0$  and two-gluon for  $\phi$  from VGG model

...since BARYONS'04:

# $Q^2$ -Dependence of SDMEs Compared with Calculations



Reasonable agreement for a majority of SDMEs of 12 elements.

To be compared with calculations, for example:

(S.V.Goloskokov and P.Kroll, Eur.Phys.J. C **42** (2005) 281)

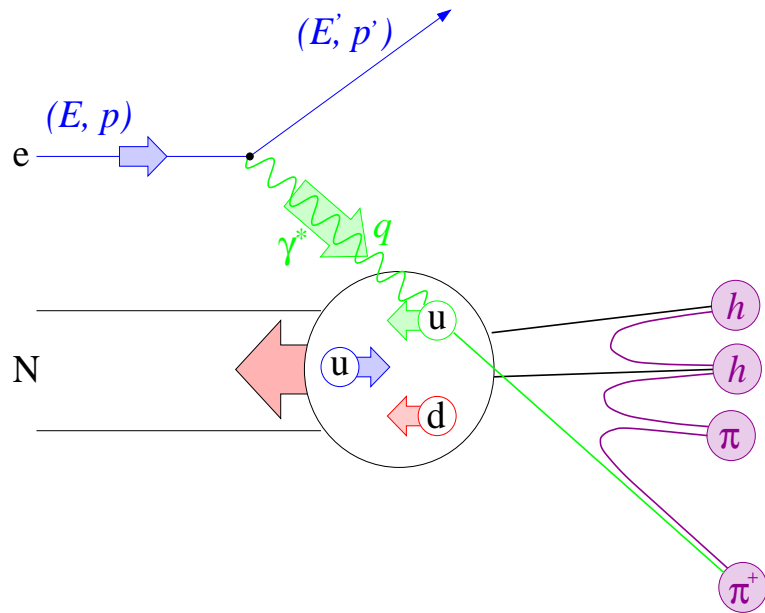
$$T_{01} \sim T \rightarrow L : \quad \mathcal{H}^V \propto \frac{\sqrt{-t}}{Q}$$

$$T_{11} \sim T \rightarrow T : \quad \mathcal{H}^V \propto \frac{\langle k_{\perp}^2 \rangle^{1/2}}{Q}$$

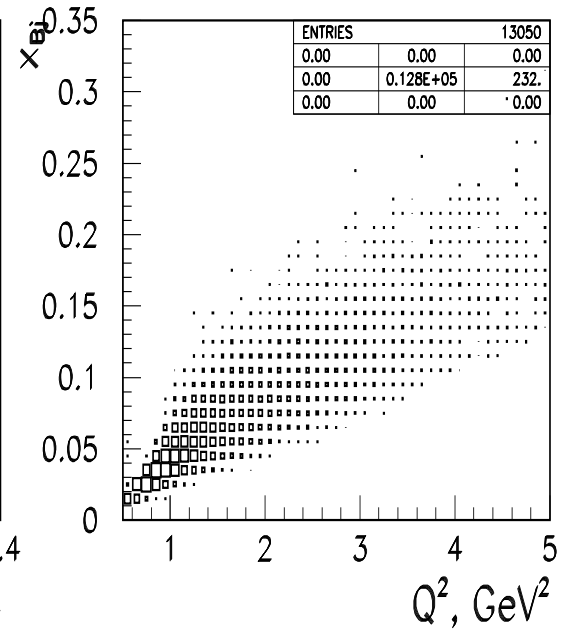
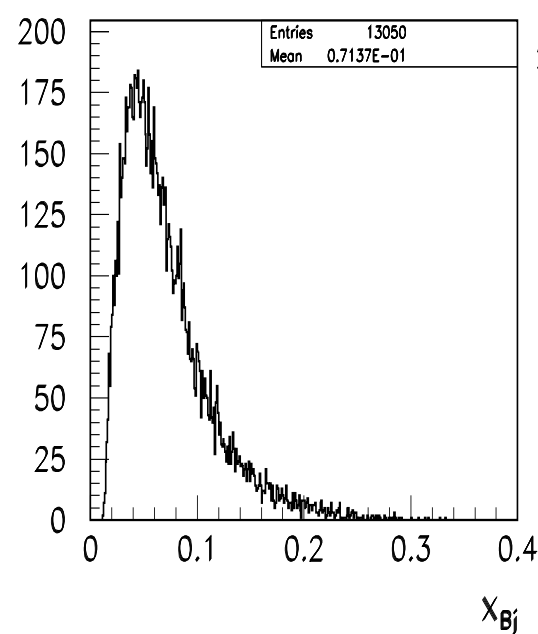
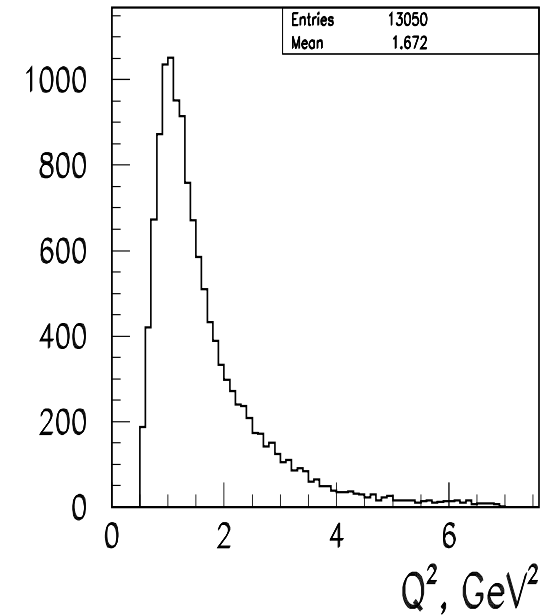
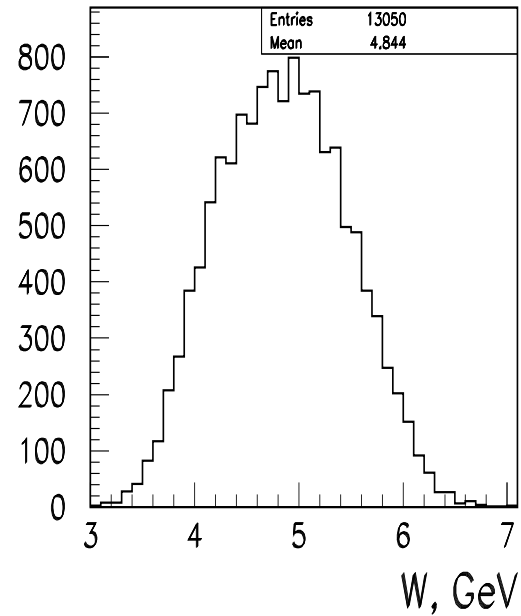
$$T_{10} \sim L \rightarrow T : \quad \mathcal{H}^V \propto \frac{\sqrt{-t} \langle k_{\perp}^2 \rangle^{1/2}}{Q}$$

$$T_{1-1} \sim T \rightarrow -T : \quad \mathcal{H}^V \propto \frac{-t \langle k_{\perp}^2 \rangle^{1/2}}{Q^2}$$

# Deep Inelastic Scattering: Important Variables and Kinematic Distributions



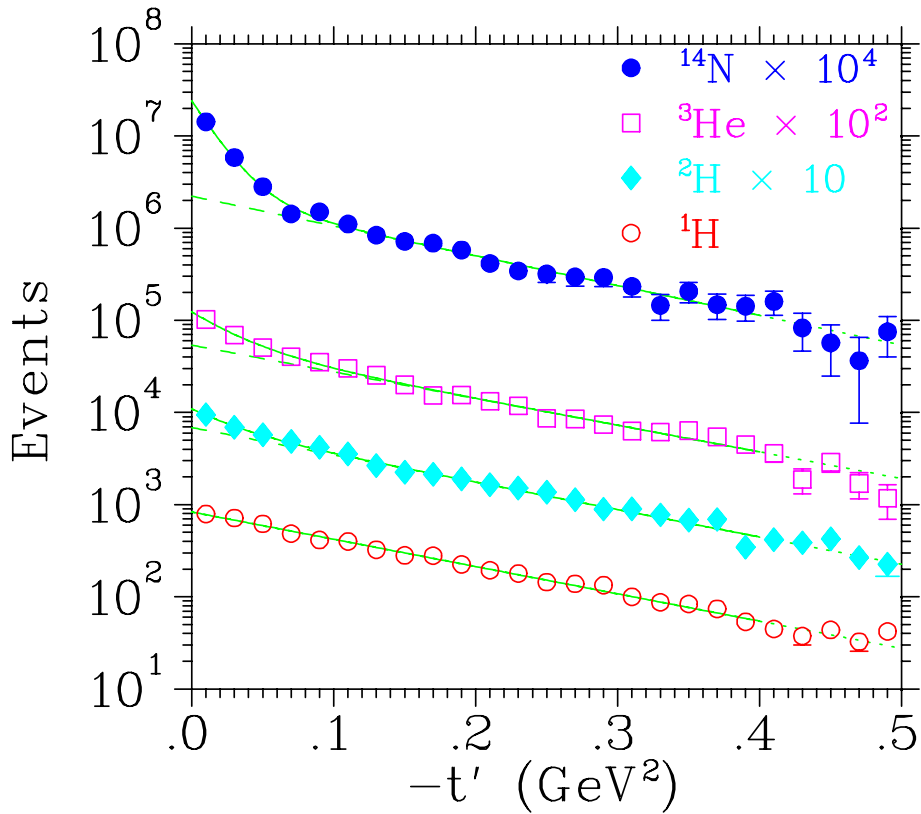
- $Q^2 \stackrel{lab}{=} 4EE' \sin^2(\Theta/2)$
- $\nu \stackrel{lab}{=} E - E'$
- $x_{Bj} \stackrel{lab}{=} Q^2/2M\nu$
- $W^2 \stackrel{lab}{=} M^2 + 2M\nu - Q^2$



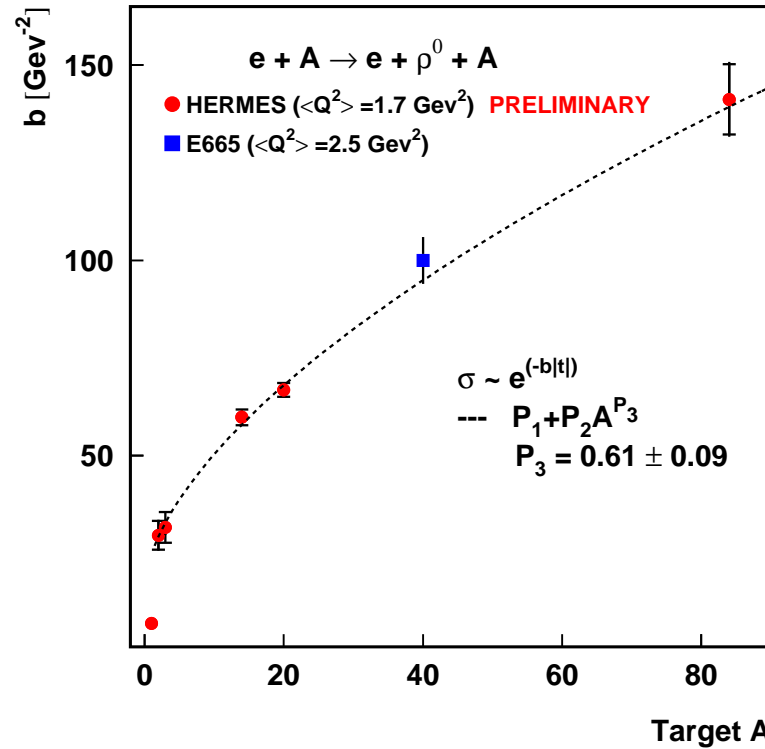


# Coherent and Incoherent $\rho^0$ Production

HERMES collab., Phys.Lett.B 513 (2001) 301-310; Eur.Phys.J. C 29, 171 - 179 (2003)



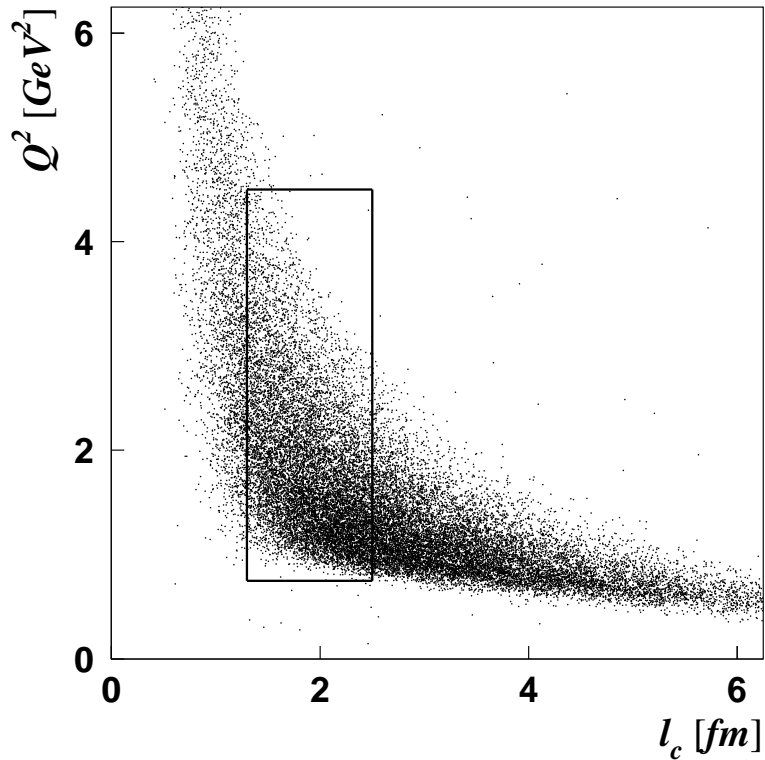
At  $-t \lesssim 0.045 \text{ GeV}^2$  coherent  $\rho^0$  dominates  
 at  $-t \gtrsim 0.1 \text{ GeV}^2$  incoherent.



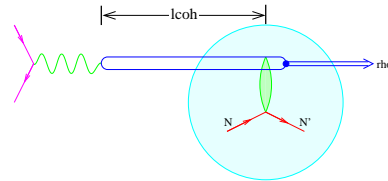
$b_{(coh)} \approx r_A^2/3$  is in agreement with world data  
 of nuclear size measurements

(H.Alvensleben et al, Phys.Rev.Let. 24,792 (1970)).

# Kinematics of exclusive $\rho^0$ matches dimension of Nuclei



- radius of the nucleus:  $r_{14N} \simeq 2.5$  fm
- coherence length: distance traversed by  $qq$



$$l_c = \frac{2 \cdot \nu}{Q^2 + m_V^2} = 0.6 \div 8 \text{ fm},$$

$$\langle l_c \rangle = 2.7 \text{ fm}$$

- transverse size of the  $qq$  wave packet  
 $r_{q\bar{q}} \sim 1 / \langle Q^2 \rangle \simeq 0.4 \text{ fm} < r_p = 1 \text{ fm}$
- formation length: distance needed for  $qq$  to develop into hadron:

$$l_{form} = \frac{2 \cdot \nu}{m_{V'}^2 - m_V^2} = 1.3 \div 6.3 \text{ fm}$$

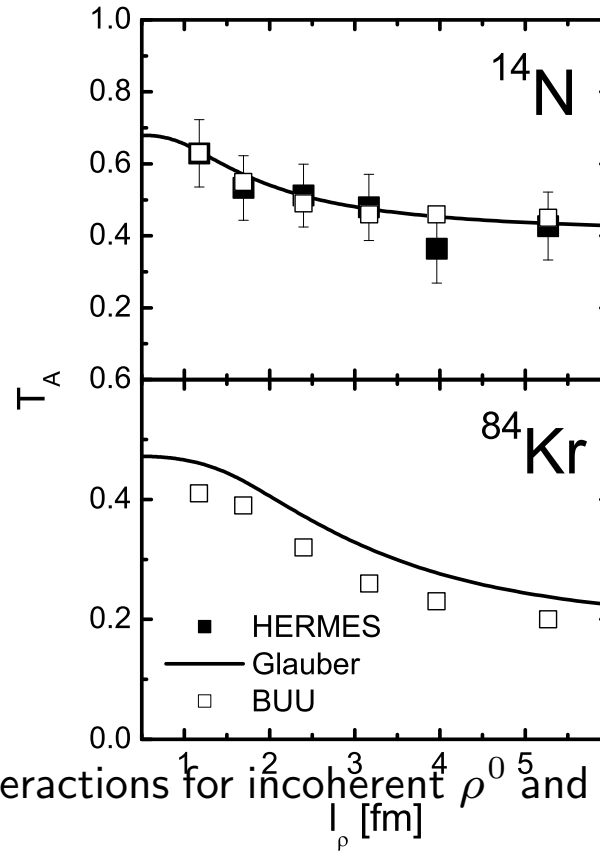
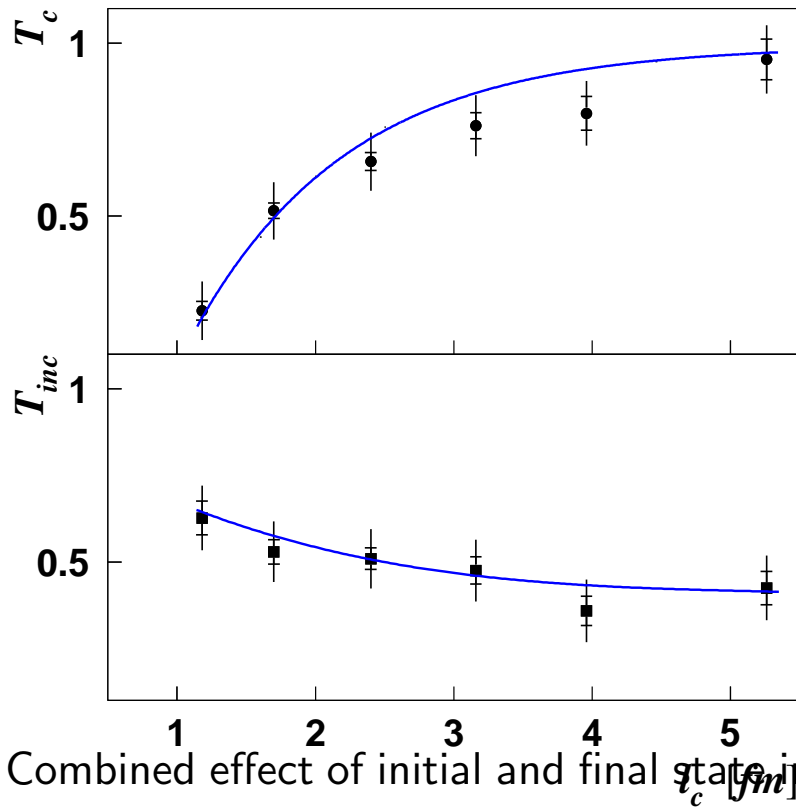
$$\langle l_{form} \rangle = 3.47 \text{ fm}$$

→  $\rho^0$  absorption at  $l_c \gtrsim r_{14N}$   
 → 2-dimensional analysis of  $Q^2$ ,  $l_c$  dependences

# Coherent Length Effect

(HERMES collab., Phys.Rev.Let., **90**, 5, 2003)

$$T_{c/inc}(l_c) = \frac{\sigma_{Ac/inc}}{A\sigma_H} = \frac{N_{Ac/inc} \cdot L_H}{A \cdot N_H \cdot L_A}, \quad A = {}^{14}\text{N}$$

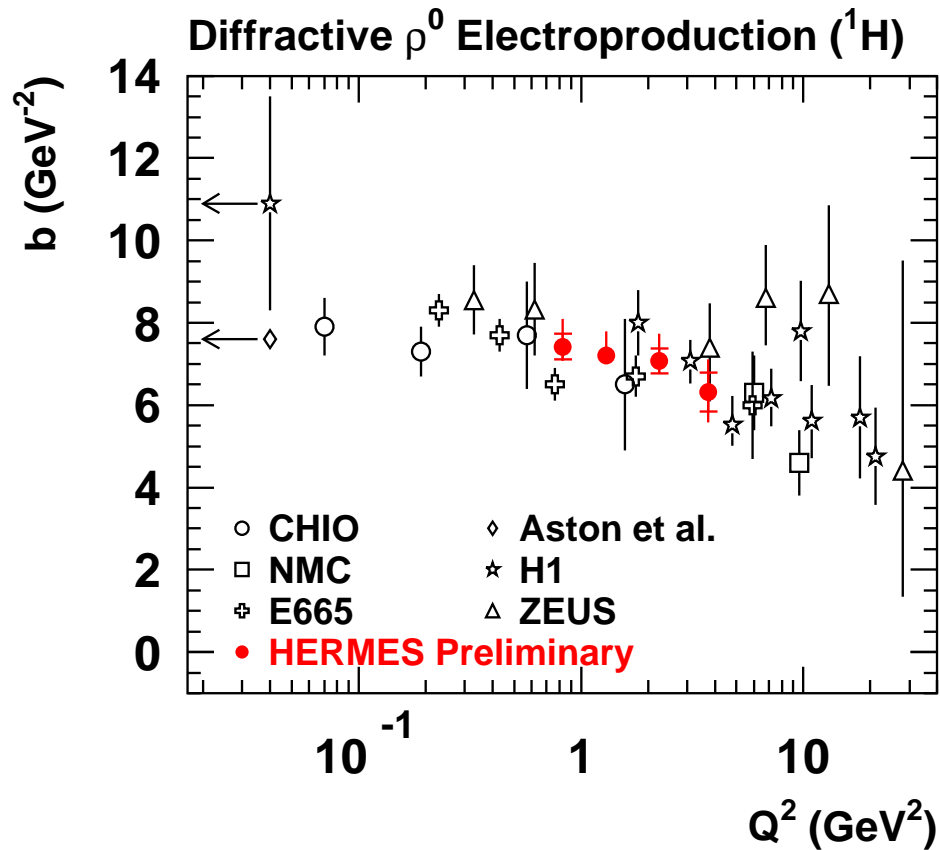


Combined effect of initial and final state interactions for incoherent  $\rho^0$  and additional effect of nuclear

formfactor for coherent  $\rho^0$ . Agreement with calculations (blue curves, left panel) based on CT approach (B.Z. Kopeliovich et al, Phys.Rev. C, **65**, 035201, 2002).

Calculations for incoherent production of semi-classical transport model without CT presented on right panel. (T.Falter, W.Cassing, K.Gallmeister and U.Mosel, nucl-th/0309057).

# $b(Q^2)$ 'Photon Shrinkage' a Prerequisite for Color Transparency



→ Size of virtual photon controlled via  $Q^2$

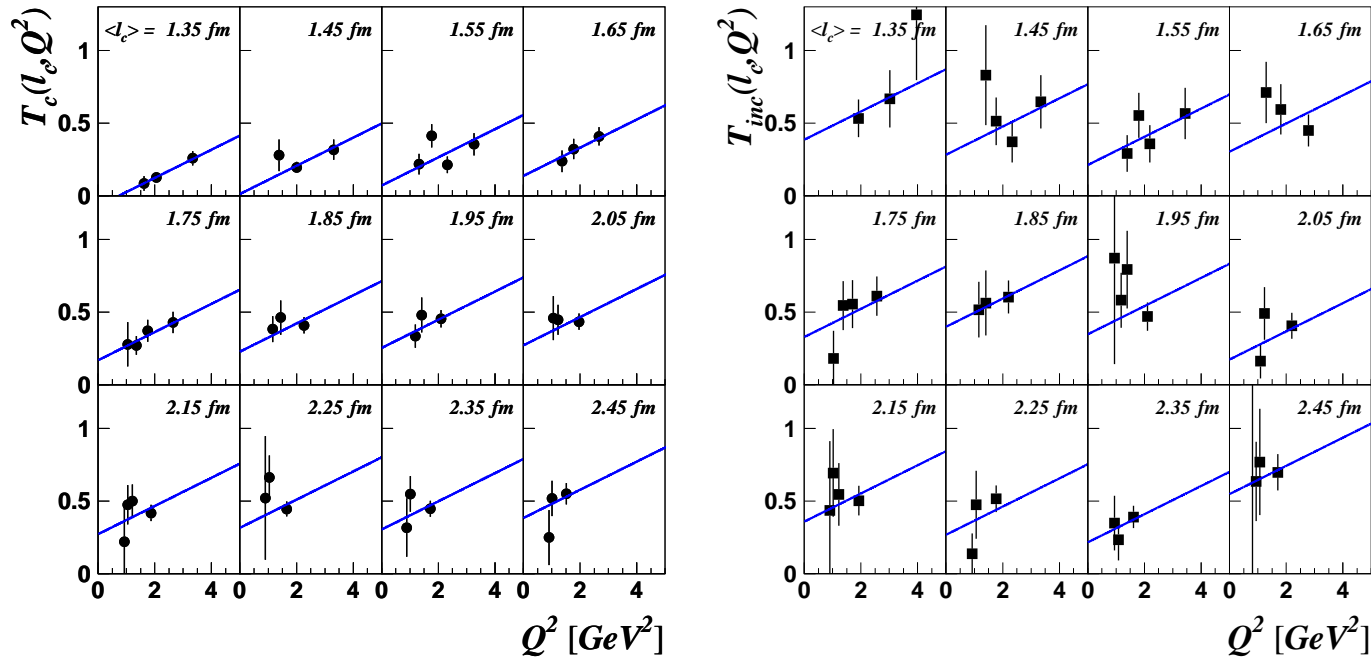
→ No strong  $W$ -dependence

# Color Transparency Effect

(HERMES collab., Phys.Rev.Let.,**90**,5,052501,2003) The QCD factorization theorem rigorously not possible without the onset of the color transparency:

→  $r(qq)$  decreases with the increase of  $Q^2$  →  $Tr^A(Q^2, l_{coh}) = \sigma_{(in)coh}^A / \sigma^H$  grows with  $Q^2$

At fixed  $l_{coh}$ :



data	Slope of $Q^2$ -dependence, $\text{GeV}^{-2}$	Prediction, $\text{GeV}^{-2}$
N incoh.	$0.089 \pm 0.046_{st} \pm 0.020_{syst}$	0.060
N coh.	$0.070 \pm 0.027_{st} \pm 0.017_{syst}$	0.048
N combined	$0.074 \pm 0.023$	0.058

Agreement with theoretical calculations where positive slope of  $Q^2$ -dependence was derived from the onset of the color transparency effect (B.Z. Kopeliovich et al, Phys.Rev. C, **65**, 035201, 2002)