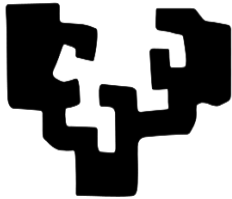


Hadronization studies at HERMES

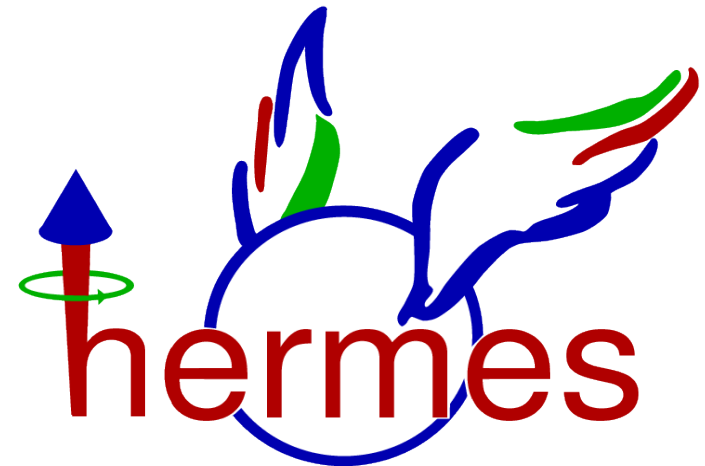
Charlotte Van Hulse,
University of the Basque Country – UPV/EHU

eman ta zabal zazu



Universidad
del País Vasco

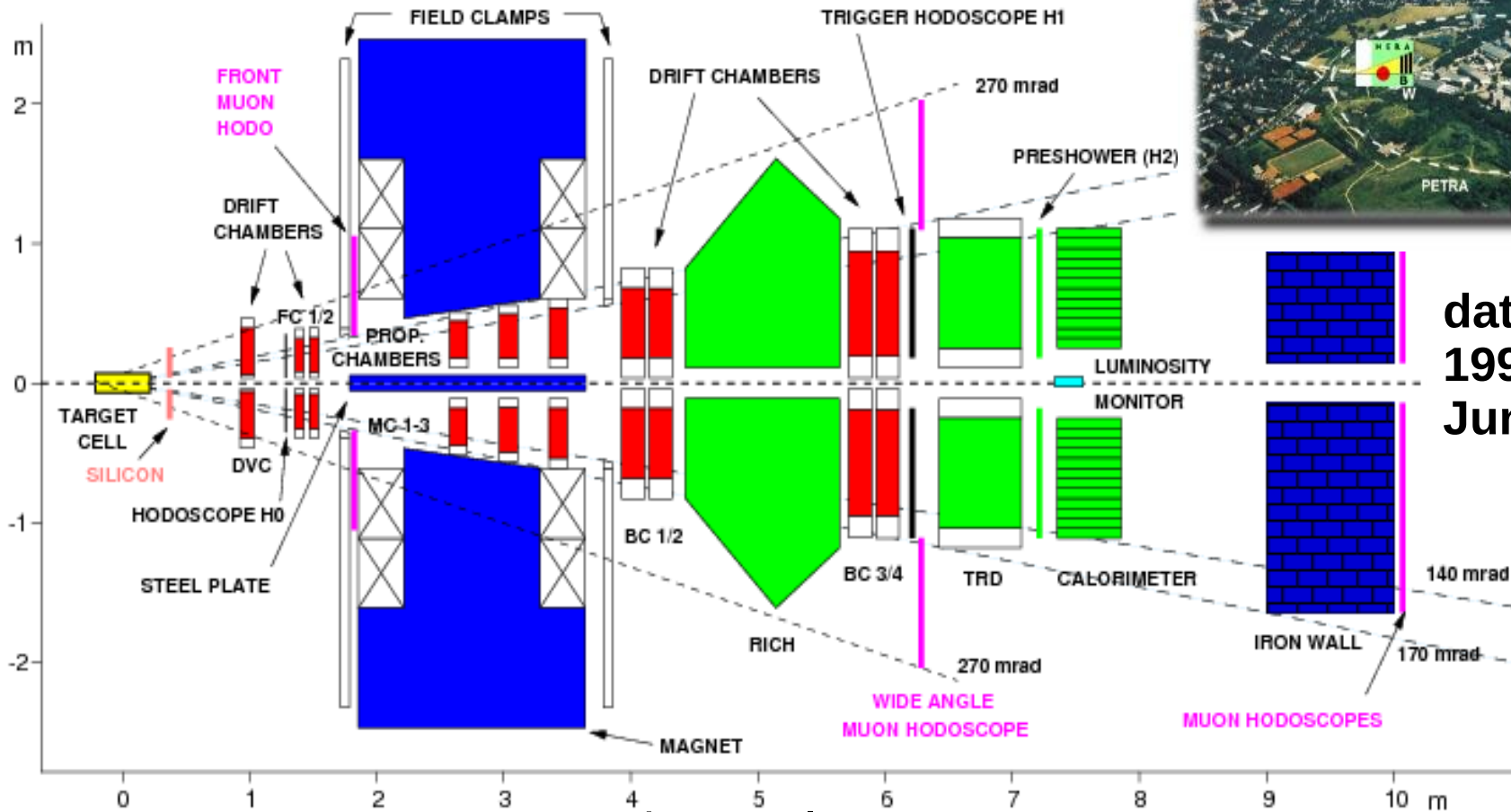
Euskal Herriko
Unibertsitatea



Outline

- the HERMES experiment
- π^\pm and K^\pm multiplicities on hydrogen and deuterium
- hadronization in nuclei
- Collins fragmentation function:
 - transversely polarized hydrogen target
 - unpolarized hydrogen/deuterium target
- dihadron fragmentation function

HERMES: HERA MEasurement of Spin



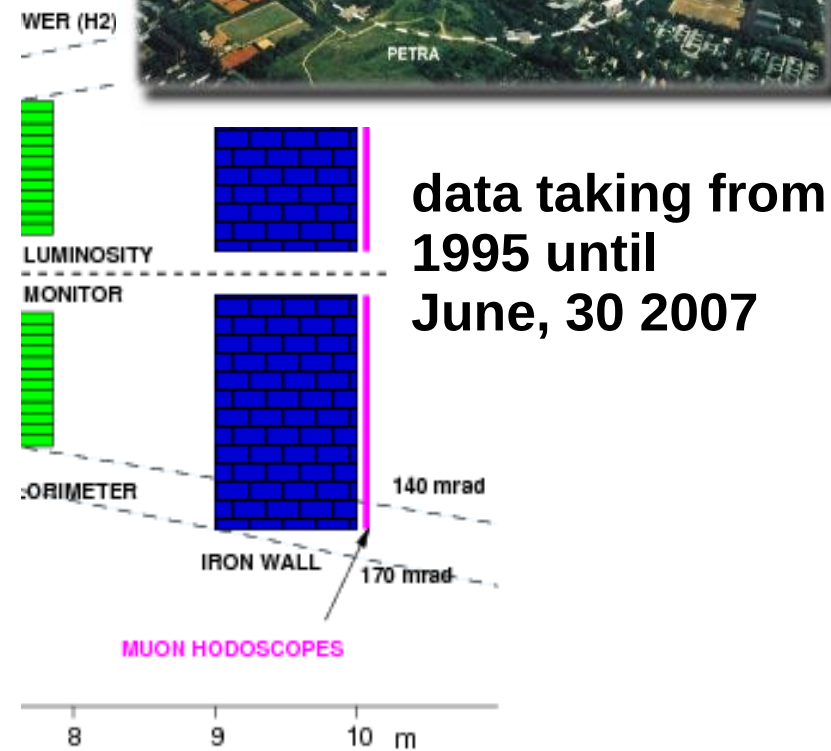
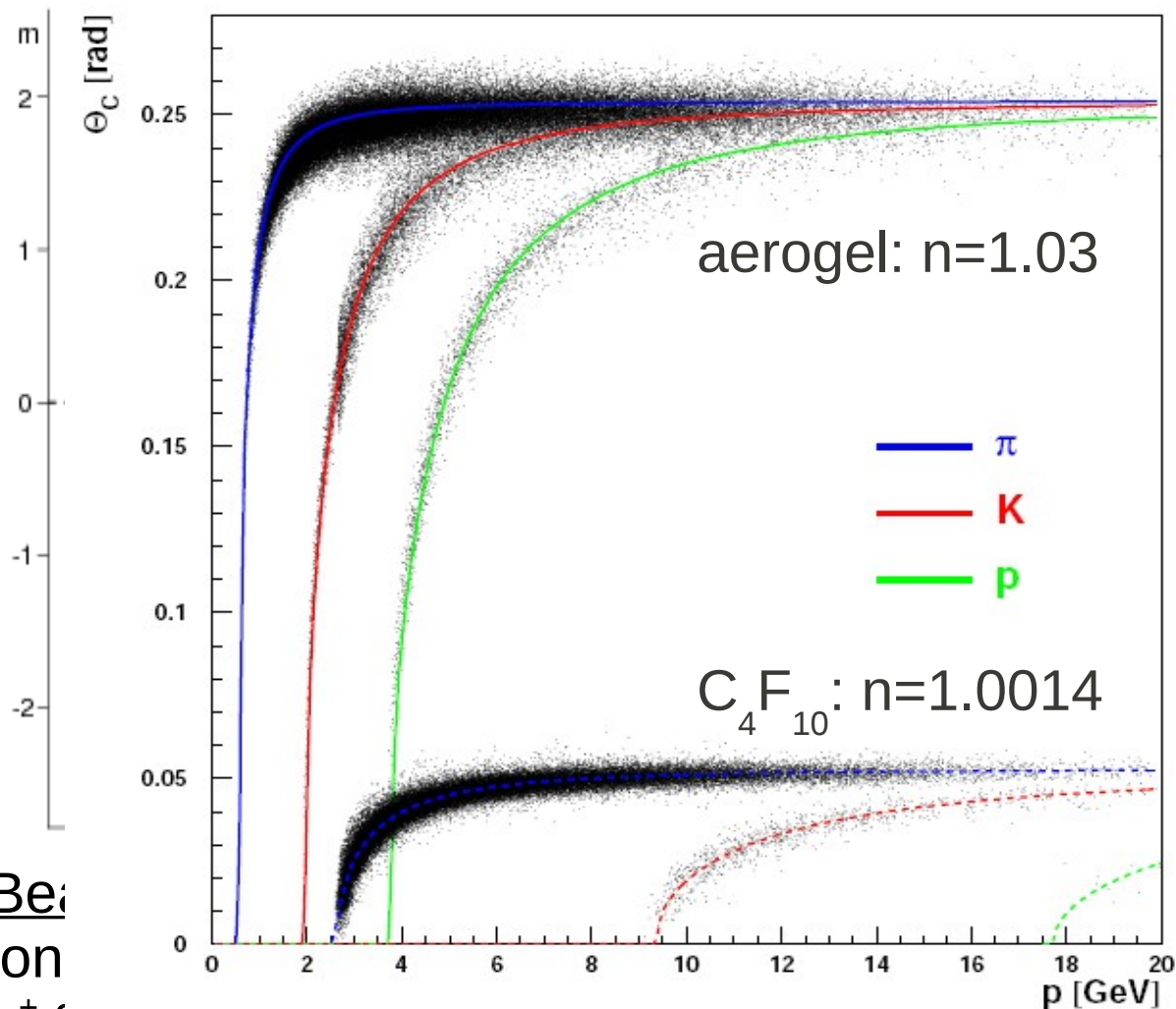
data taking from
1995 until
June, 30 2007

Beam
longitudinally pol.
 e^+ & e^-
 $E = 27.6$ GeV

Gaseous internal target
transversely pol. H (~75%)
unpol. H, D, He, Ne, Kr, Xe
longitudinally pol. H, D, He (~85%)

- lepton-hadron PID: high efficiency (>98%) & low contamination (<1%)
- hadron PID: RICH 2-15 GeV

HERMES: HERA MEasurement of Spin



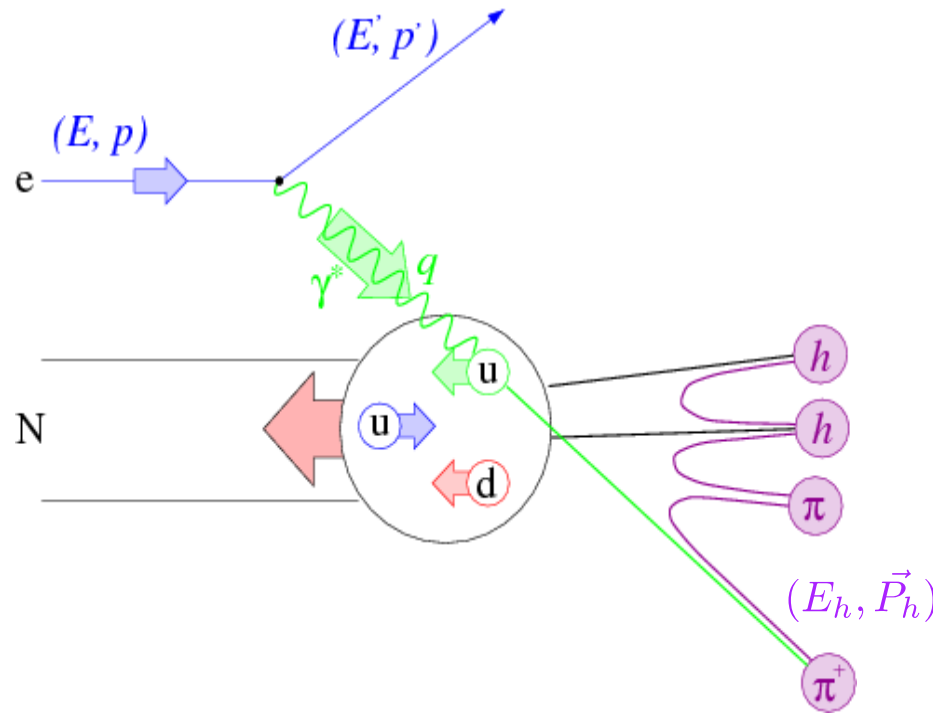
data taking from
 1995 until
 June, 30 2007

Be:
 Ion
 e^+ & e^-
 $E=27.6$ GeV

unpolar. H,D,He (~85%)
 longitudinally pol. H,D,He (~85%)

- lepton-hadron PID: high efficiency (>98%) & low contamination (<1%)
- hadron PID: RICH 2-15 GeV

Semi-inclusive deep-inelastic scattering



$$Q^2 = -q^2$$

$$\nu \stackrel{lab}{=} E - E'$$

$$W^2 = M_N^2 + 2M_N\nu - Q^2$$

$$y \stackrel{lab}{=} \frac{\nu}{E}$$

$$x_B \stackrel{lab}{=} \frac{Q^2}{2M_N\nu}$$

$$z \stackrel{lab}{=} \frac{E_h}{\nu}$$

$$\sigma^{ep \rightarrow eh} = \sum_q \mathcal{I} [DF^{p \rightarrow q}(x_B, p_T^2, Q^2) \otimes \sigma^{eq \rightarrow eq} \otimes FF^{q \rightarrow h}(z, k_T^2, Q^2)]$$

Distribution Function (DF): distribution of quarks in nucleon

Fragmentation Function (FF): fragmentation of struck quark into final-state hadron

p_T/k_T : transverse momentum of struck/fragmenting quark

Access to spin-independent fragmentation functions

Hadron multiplicities and fragmentation functions

$$M_n^h(x_B, Q^2, z, P_{h\perp}) = \frac{1}{d^2 N^{DIS}(x_B, Q^2)} \frac{d^4 N^h(x_B, Q^2, z, P_{h\perp})}{dz dP_{h\perp}}$$

$$= \frac{\sum_q e_q^2 \mathcal{I}[f_1^q(x_B, p_T^2, Q^2) \otimes \mathcal{W} D_1^q(z, k_T^2, Q^2)]}{\sum_q e_q^2 f_1^q(x_B, Q^2)}$$



collinear

QPM, leading twist, LO

$$M_n^h(x_B, Q^2, z) = \frac{\sum_q e_q^2 f_1^q(x_B, Q^2) D_1^q(z, Q^2)}{\sum_q e_q^2 f_1^q(x_B, Q^2)}$$

access to fragmentation function $D_1^q(z, (k_T^2), Q^2)$:

- probe fragmentation function complementary to e^+e^- and $p p^{(-)}$
- disentangle favored (e.g. $u \rightarrow \pi^+$) from unfavored fragmentation (e.g. $\bar{u} \rightarrow \pi^+$)

Extraction of multiplicities

- charged pion and kaon multiplicities
- hydrogen and deuterium targets
- kinematic requirements:

$$Q^2 > 1 \text{ GeV}^2$$

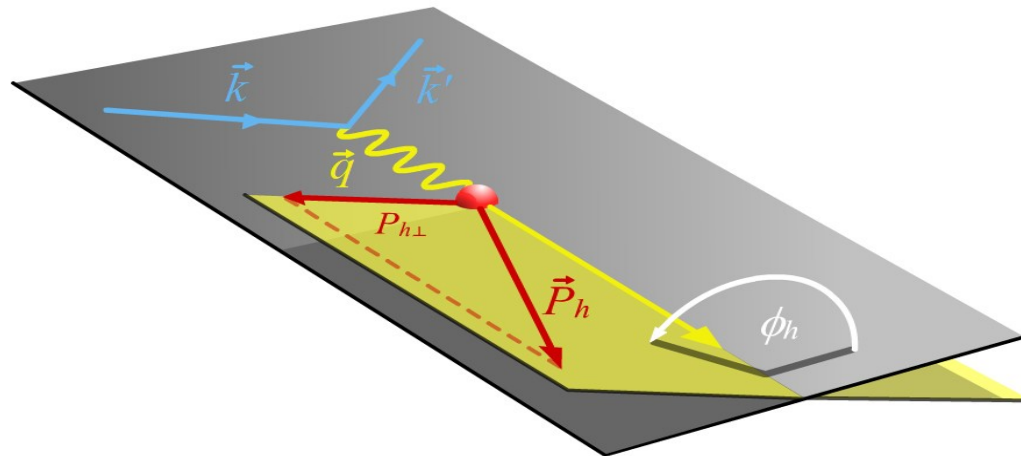
$$0.1 < y < 0.85$$

$$W^2 > 10 \text{ GeV}^2$$

$$2 \text{ GeV} < P_h < 15 \text{ GeV}$$

$$0.2 < z < 0.8$$

- 3D binning: $(x_B, z, P_{h\perp})$ and $(Q^2, z, P_{h\perp})$



Extraction of Born multiplicities

$$M_{Born}^h(j) = \frac{1}{n_{Born}^{DIS}(j)} \sum_i [S_h^{-1}](j, i) [M_{meas}^h(i) N_{meas}^{DIS}(i) - n^h(i, 0)]$$

smearing matrix from LEPTO+JETSET Monte-Carlo simulation

$$S_h(i, j) = \frac{n^h(i, j)}{n_{Born}^h(j)}$$

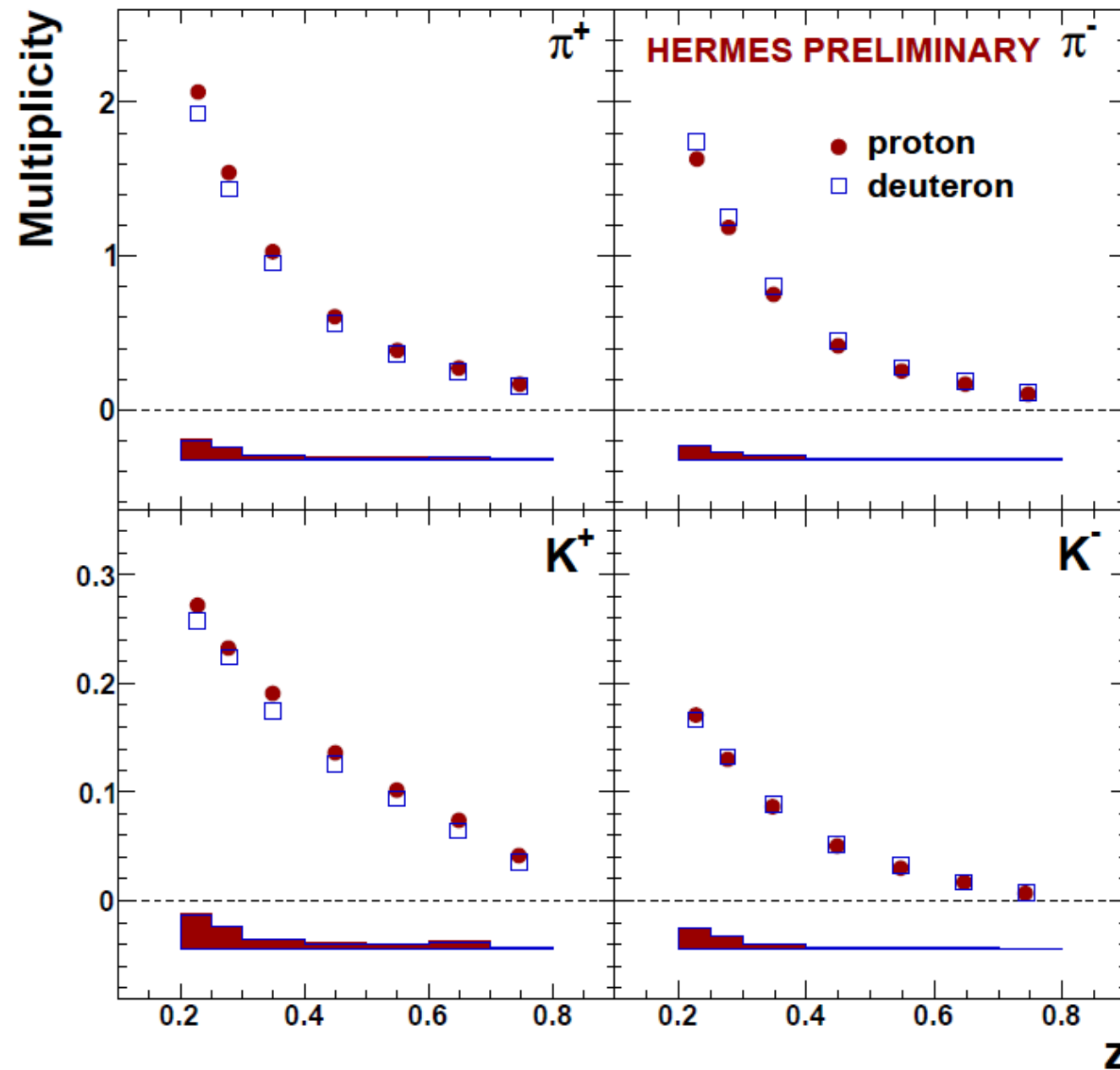
reconstructed
generated (Born)

accounts for

- QED radiative effects (RADGEN)
- limited geometric and kinematic acceptance of spectrometer
- detector resolution

$n^h(i, 0)$ migration of events outside acceptance into acceptance

Results projected in z

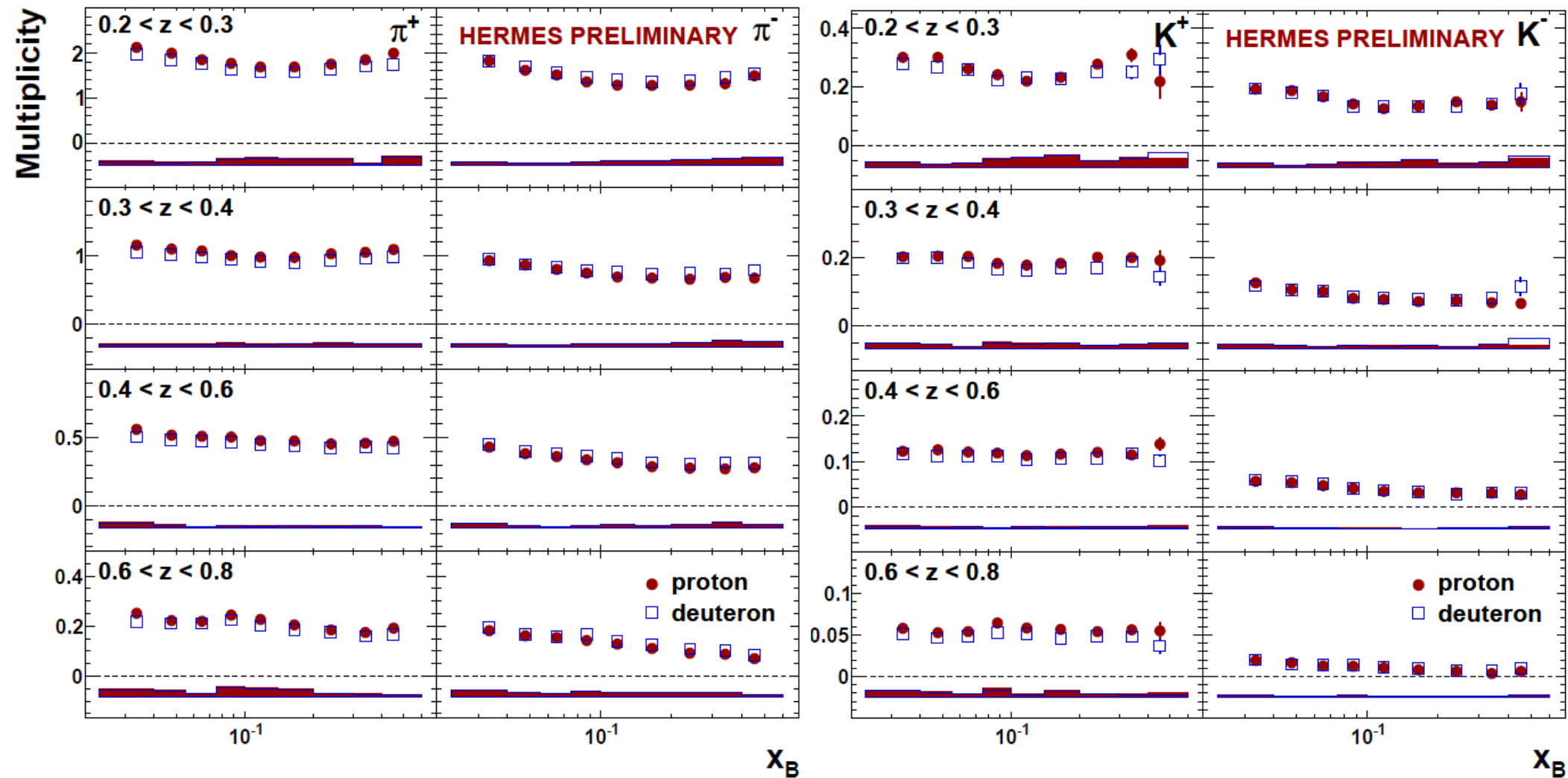


$$\frac{M_{p(d)}^{\pi^+}}{M_{p(d)}^{\pi^-}} = 1.2 - 2.6 (1.1 - 1.8)$$

$$\frac{M_{p(d)}^{K^+}}{M_{p(d)}^{K^-}} = 1.5 - 5.7 (1.3 - 4.6)$$

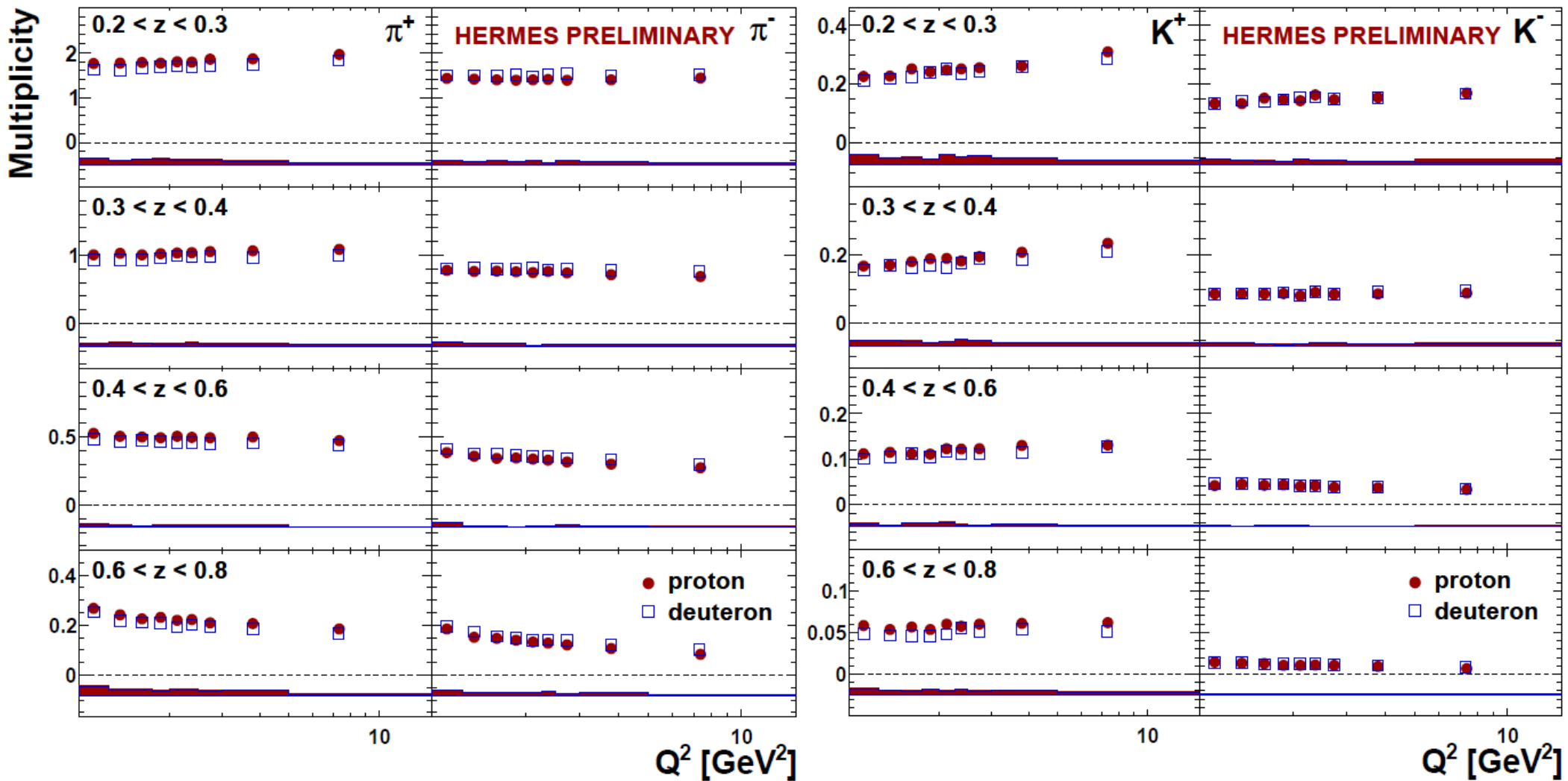
- multiplicities reflect nucleon valence-quark content (u-dominance)
- favored \leftrightarrow unfavored fragmentation

Results projected in z and x_B



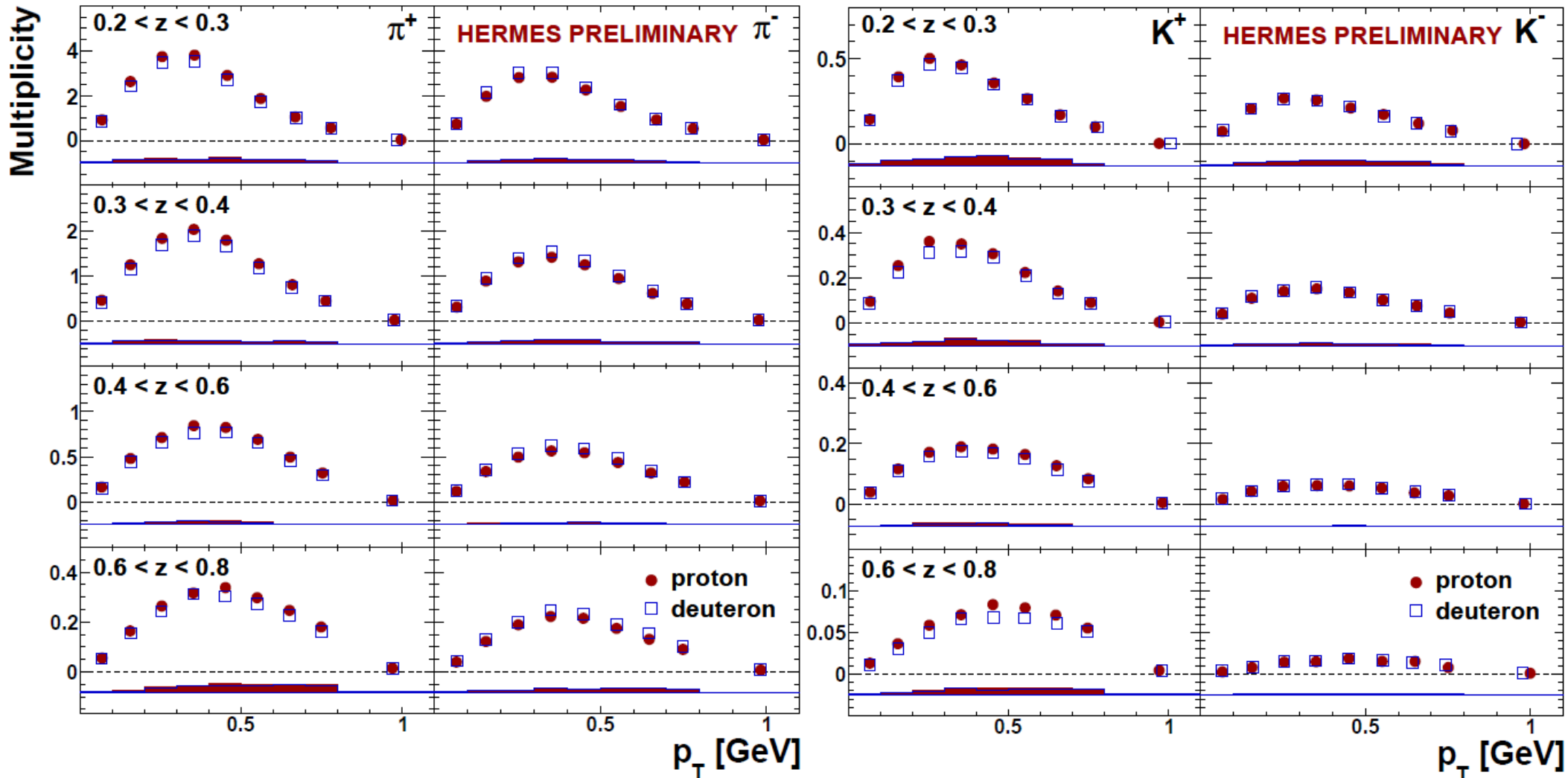
- no strong dependence on x_B

Results projected in z and Q^2



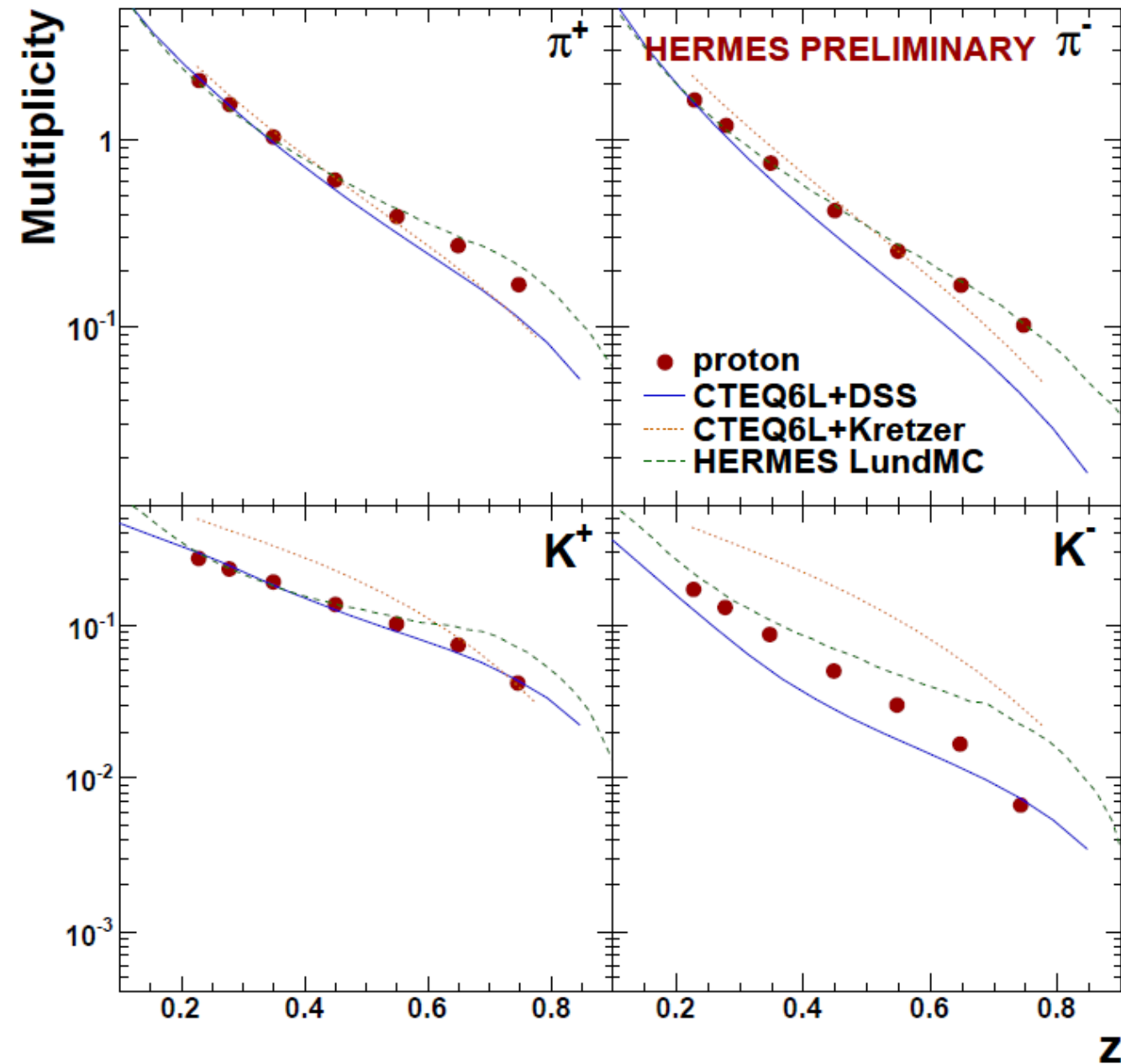
- strong correlation x_B and Q^2

Results projected in z and $P_{h\perp}$



- $P_{h\perp}$ ($=p_T$ on figures): - transverse intrinsic struck-quark momentum
- transverse momentum from fragmentation process
- K^- : broader distribution

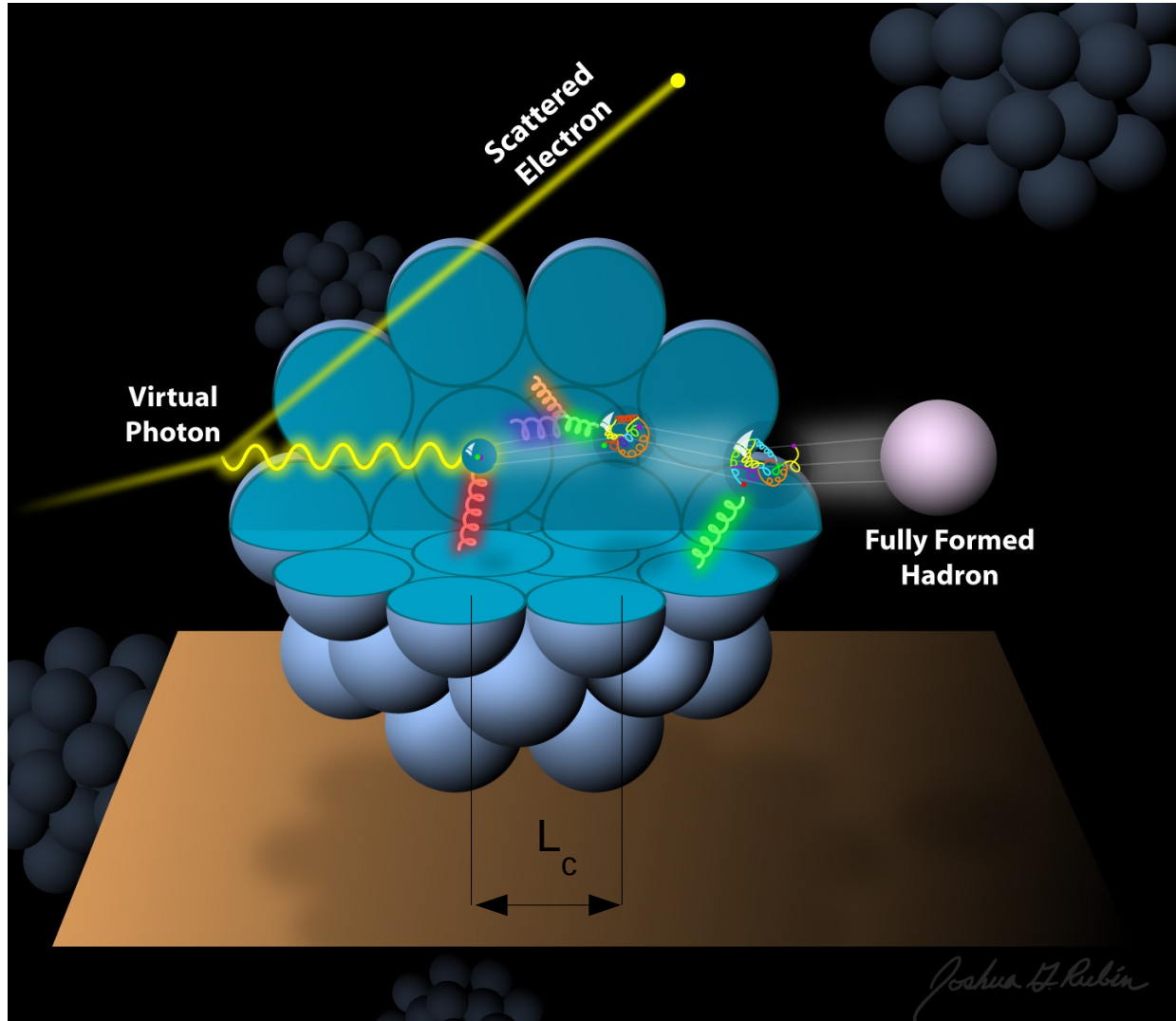
Comparison with models



- LO in α_S
- CTEQ6L PDFs
JHEP **0602** (2006) 032
- DSS FFs
Phys. Rev. D**75** (2007) 114010
- Kretzer FFs
Phys. Rev. D**62** (2000) 054001

Hadronization in nuclei

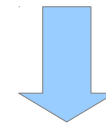
Probing space-time evolution of hadronization



- parton and nuclear medium:
- PDFs modified by nuclear medium
 - gluon radiation and rescattering

- (pre-)hadron and nuclear medium:
- rescattering
 - absorption

- differences predicted for partonic and (pre-)hadronic interactions
- change from partonic to hadronic interactions = $f(L_c / \text{nucleon size})$



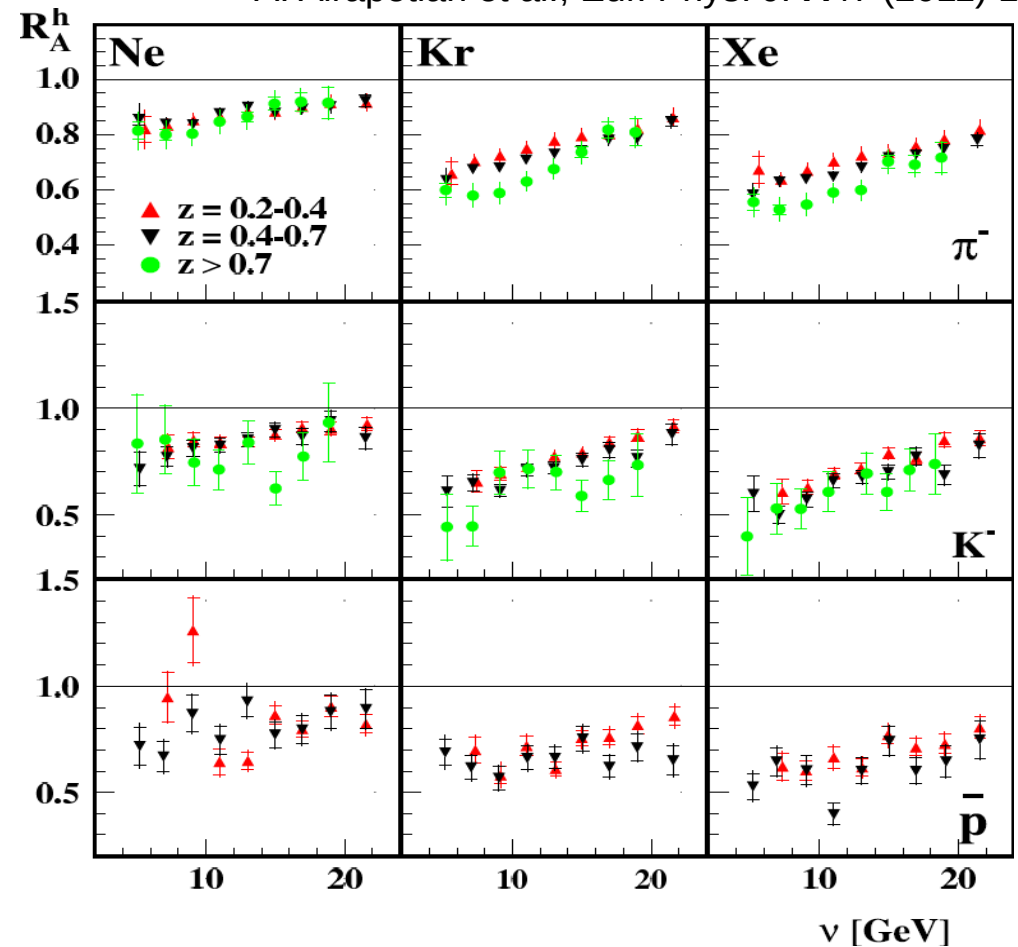
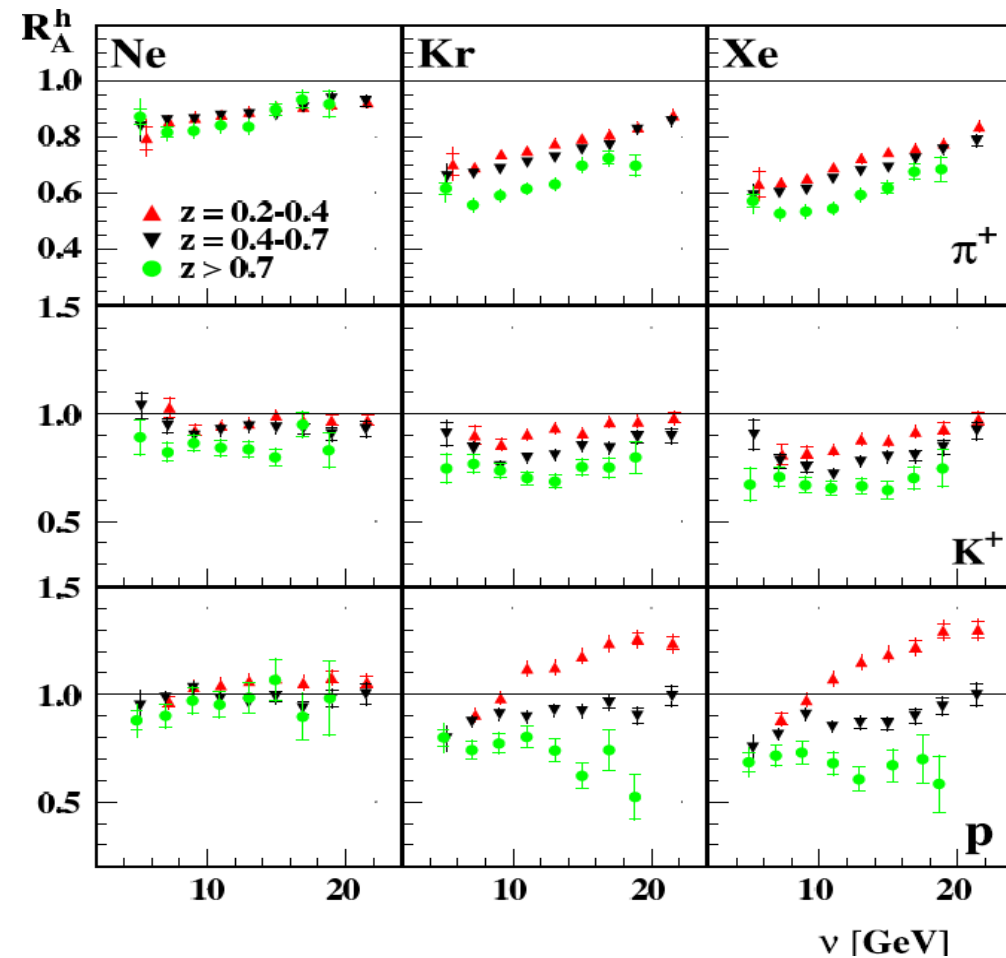
hadron multiplicity ratios from heavier targets and deuterium
→ space-time evolution of hadron formation

Extraction of multiplicity ratios

- nuclear targets: Ne, Kr, Xe compared to D
- ratio \implies approximate cancellation of
 - QED radiative effects (RADGEN)
 - limited geometric and kinematic acceptance of spectrometer
 - detector resolution
- multi-dimensional extraction:
 - v for slices of z
 - z for slices of v
 - $P_{h\perp}^2$ for slices of z
 - z for slices of $P_{h\perp}^2$

Results in ν for slices of z

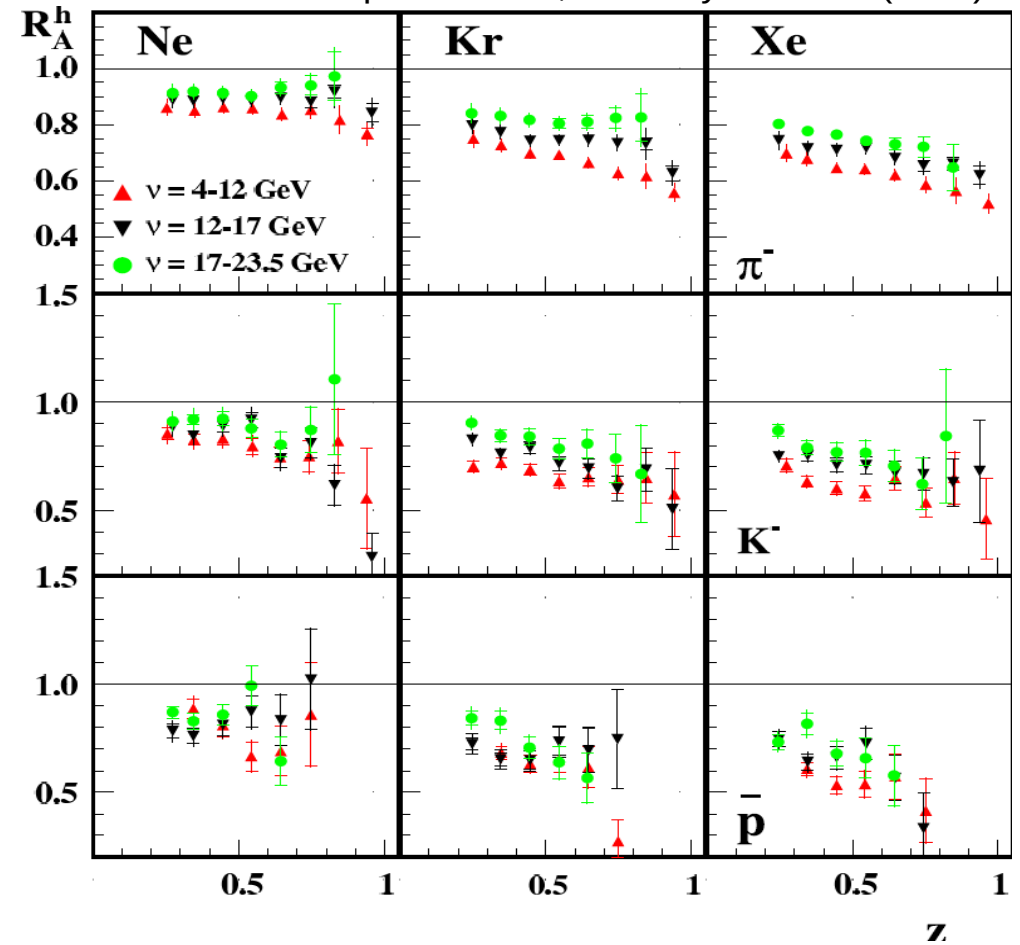
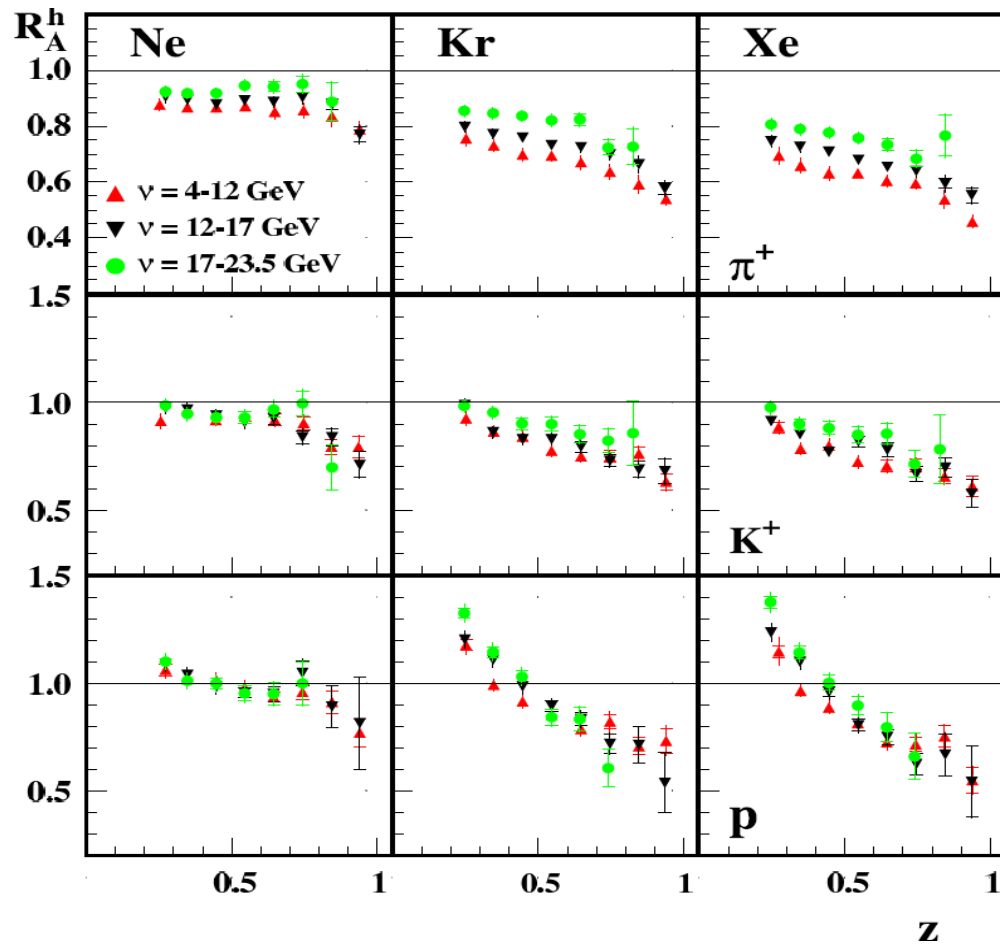
A. Airapetian et al., Eur. Phys. J. A47 (2011) 113



- R_A^h decreases with increasing A (except for protons)
- π^\pm & K^- : R_A^h increases with increasing ν
- K^+ : R_A^h increases with increasing ν , but different behavior
- p : $R_A^h > 1$ at low z

Results in z for slices of ν

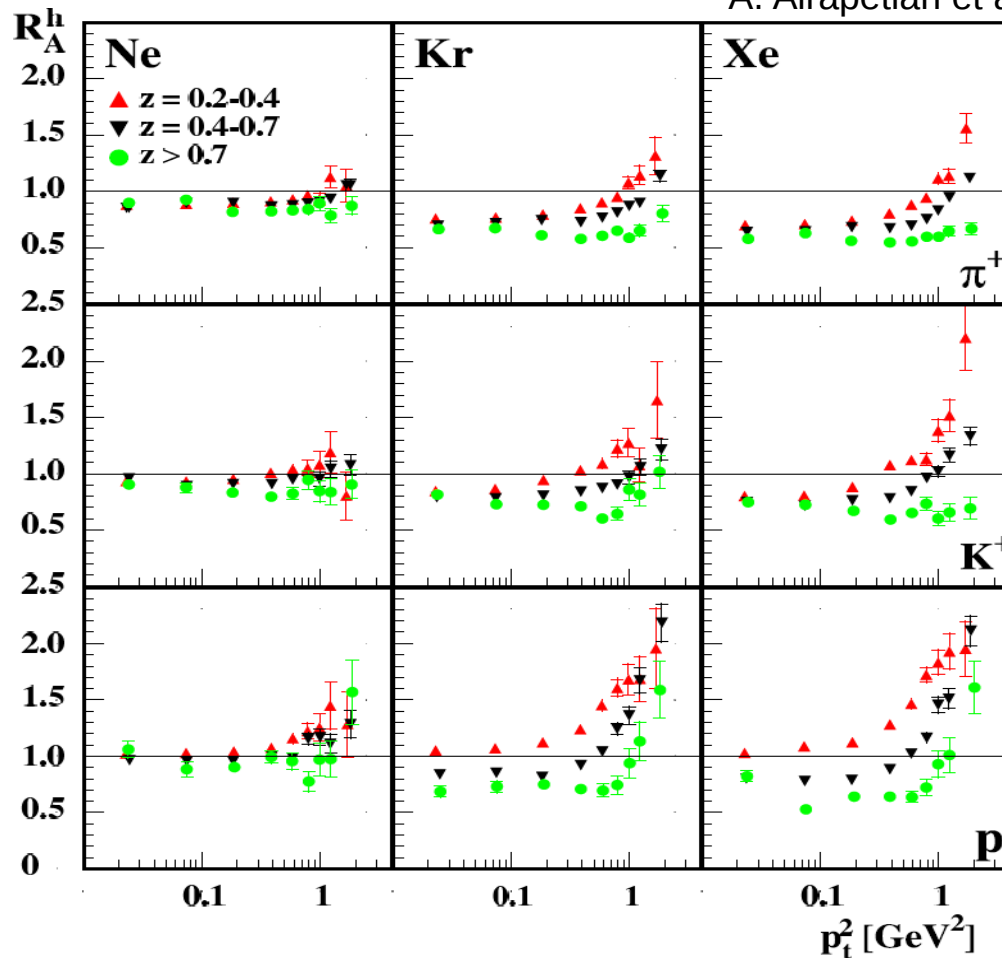
A. Airapetian et al., Eur. Phys. J. A47 (2011) 113



- R_A^h decreases with increasing z
- effect increases with increasing A
- p : $R_A^h > 1$ at low z
- K^+ : $R_A^h \approx 1$ at low z

Results in $P_{h\perp}^2$ for slices of z

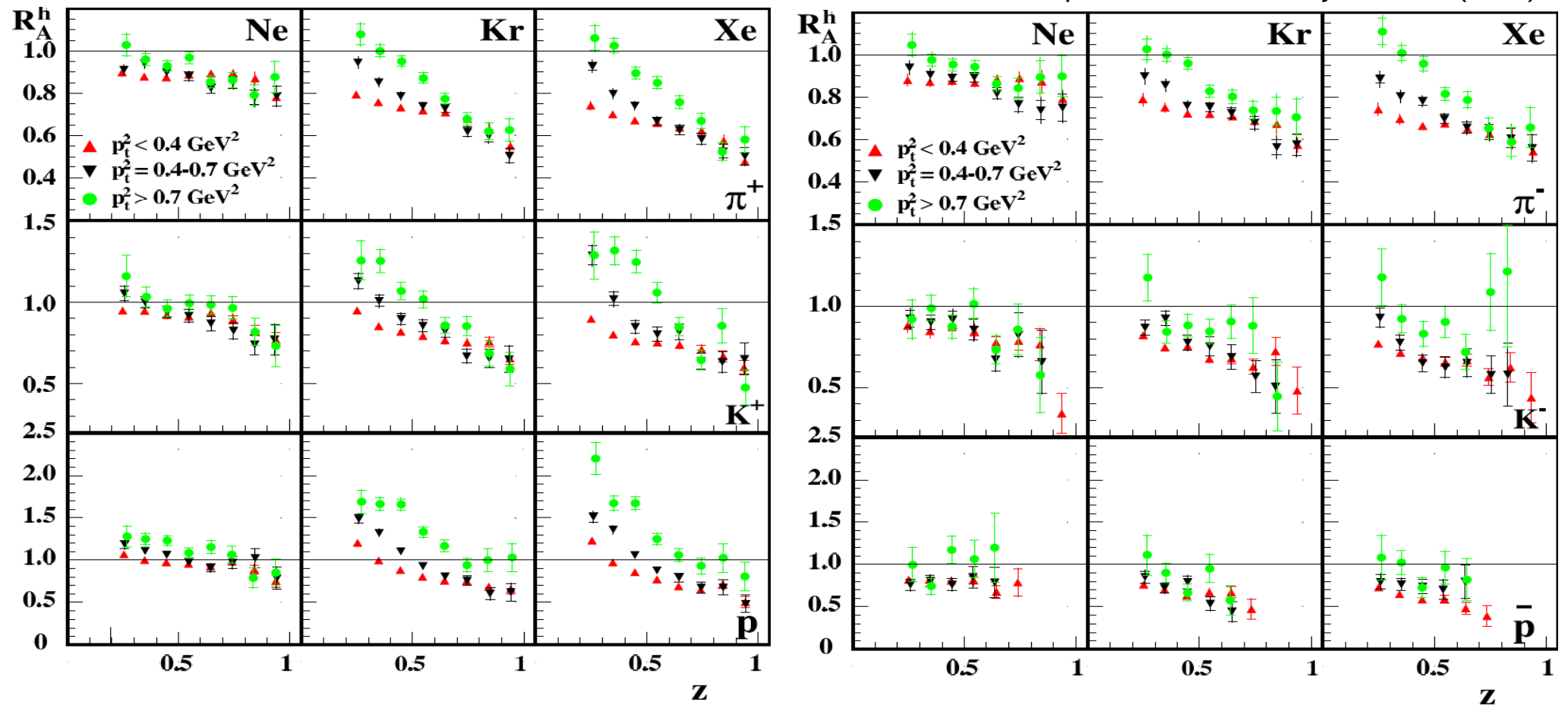
A. Airapetian et al., Eur. Phys. J. A47 (2011) 113



- R_A^h increases strongly with increasing $P_{h\perp}^2$ (Cronin effect)
- except at large z for π^+ and K^+

Results in z for slices of $P_{h\perp}^2$

A. Airapetian et al., Eur. Phys. J. A47 (2011) 113

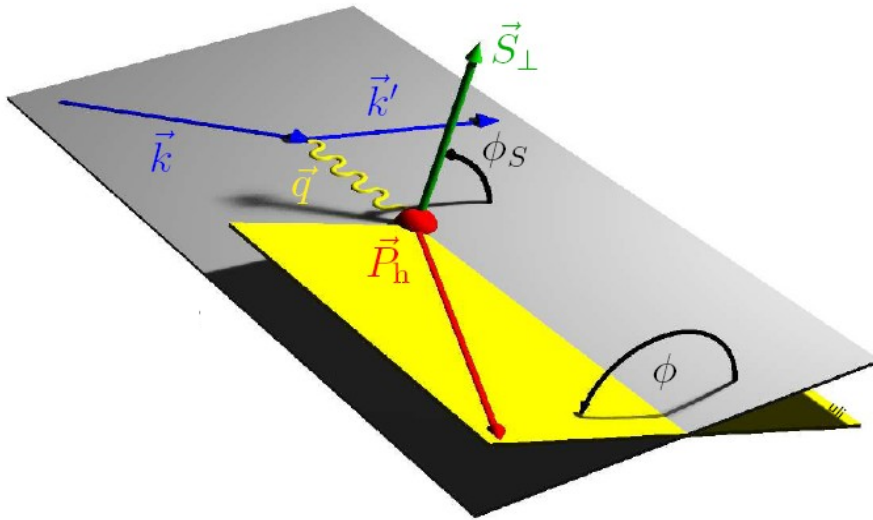


- decrease of R_A^h with increasing z stronger at large $P_{h\perp}^2$ and A
- no Cronin effect at large z
- p : R_A^h at low z larger for large $P_{h\perp}^2$

Access to Collins fragmentation function

Semi-inclusive deep-inelastic single-hadron production

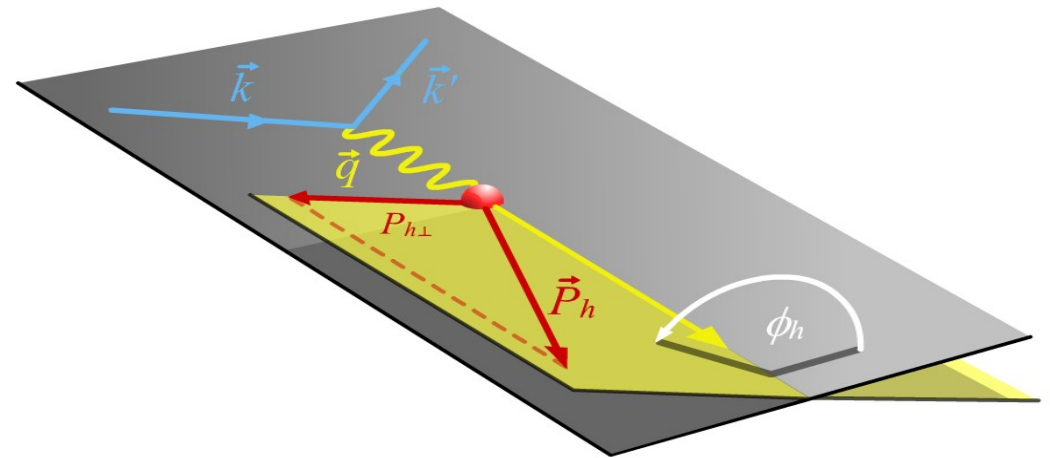
transverse target-spin
asymmetry:



$$\sim \sin(\phi + \phi_S) \sum_q e_q^2 \mathcal{I}[h_{1T}^q \otimes \mathcal{W}_1 H_1^{\perp,q}]$$

$H_1^{\perp,q}$: Collins fragmentation function

spin-independent
semi-inclusive cross section:

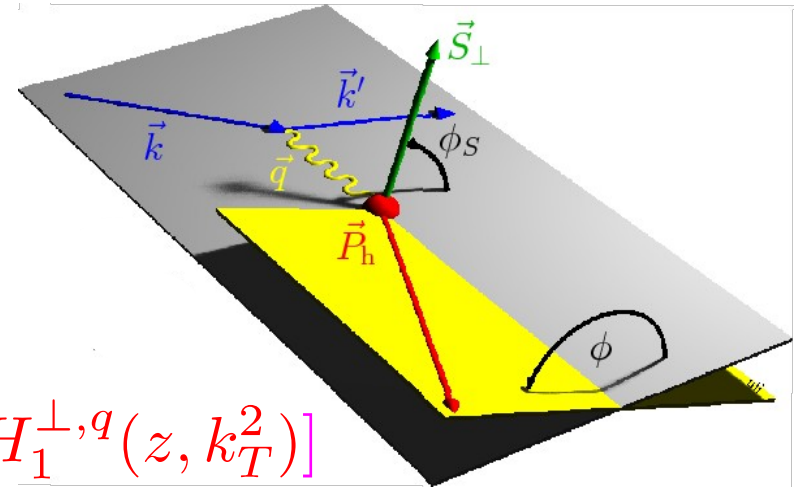


$$\begin{aligned} &\sim \cos(2\phi_h) \sum_q e_q^2 \mathcal{I}[-h_1^{\perp,q} \otimes \mathcal{W}_2 H_1^{\perp,q}] \\ &+ \cos(\phi_h) \sum_q e_q^2 \mathcal{I}[-f_1^q \otimes \mathcal{W}_3 D_1^q \\ &\quad - h_1^{\perp,q} \otimes \mathcal{W}_4 H_1^{\perp,q} + \dots] \end{aligned}$$

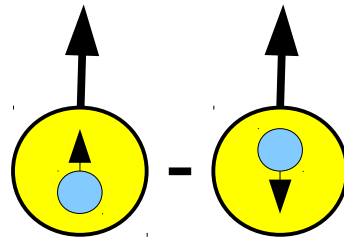
Single-Spin Asymmetry

$$A_{UT} = \frac{1}{\langle |S_T| \rangle} \frac{N^\uparrow(\phi, \phi_S) - N^\downarrow(\phi, \phi_S)}{N^\uparrow(\phi, \phi_S) + N^\downarrow(\phi, \phi_S)}$$

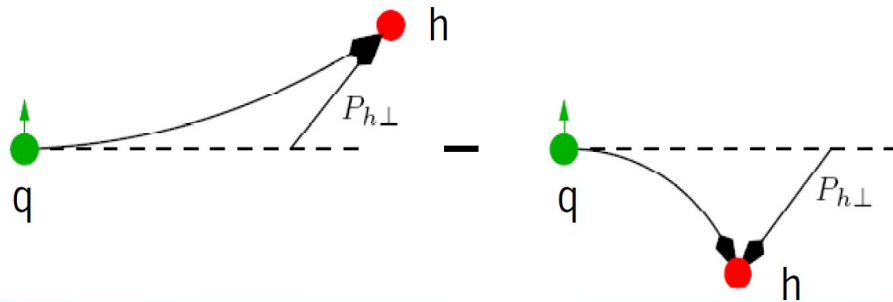
$$\sim \sin(\phi + \phi_S) \sum_q e_q^2 \mathcal{I} \left[\frac{\vec{k}_T \cdot \hat{P}_{h\perp}}{M_h} h_{1T}^q(x, p_T^2) \otimes H_1^{\perp,q}(z, k_T^2) \right]$$



$h_{1T}^q(x, p_T^2)$: transversity



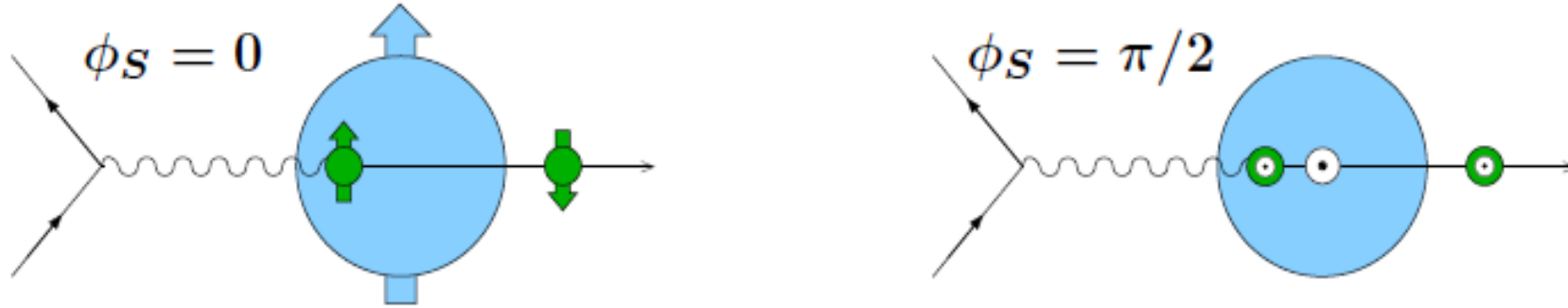
$H_1^{\perp,q}(z, k_T^2)$: Collins fragmentation function



Collins fragmentation function: Artru model

X. Artru et al. , Z. Phys. C73 (1997) 527

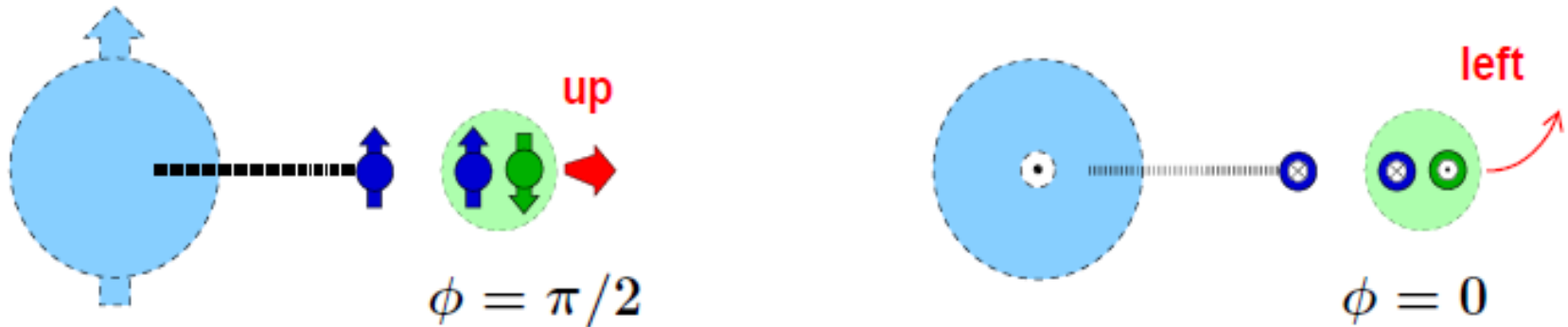
polarisation component in lepton scattering plane reversed by photoabsorption:



string break, quark-antiquark pair with vacuum numbers:

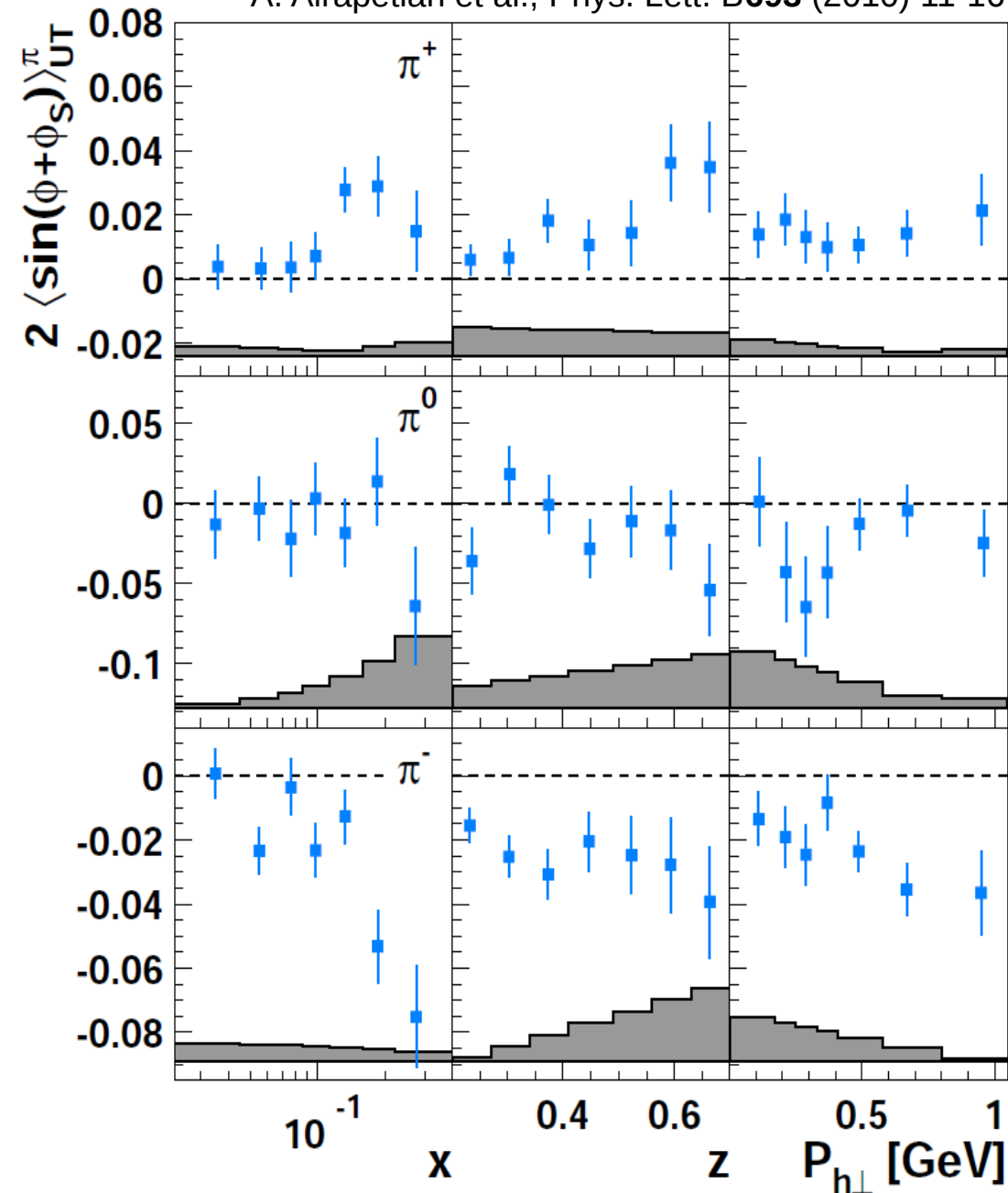


orbital angular momentum creates transverse momentum:



Collins amplitudes for pions

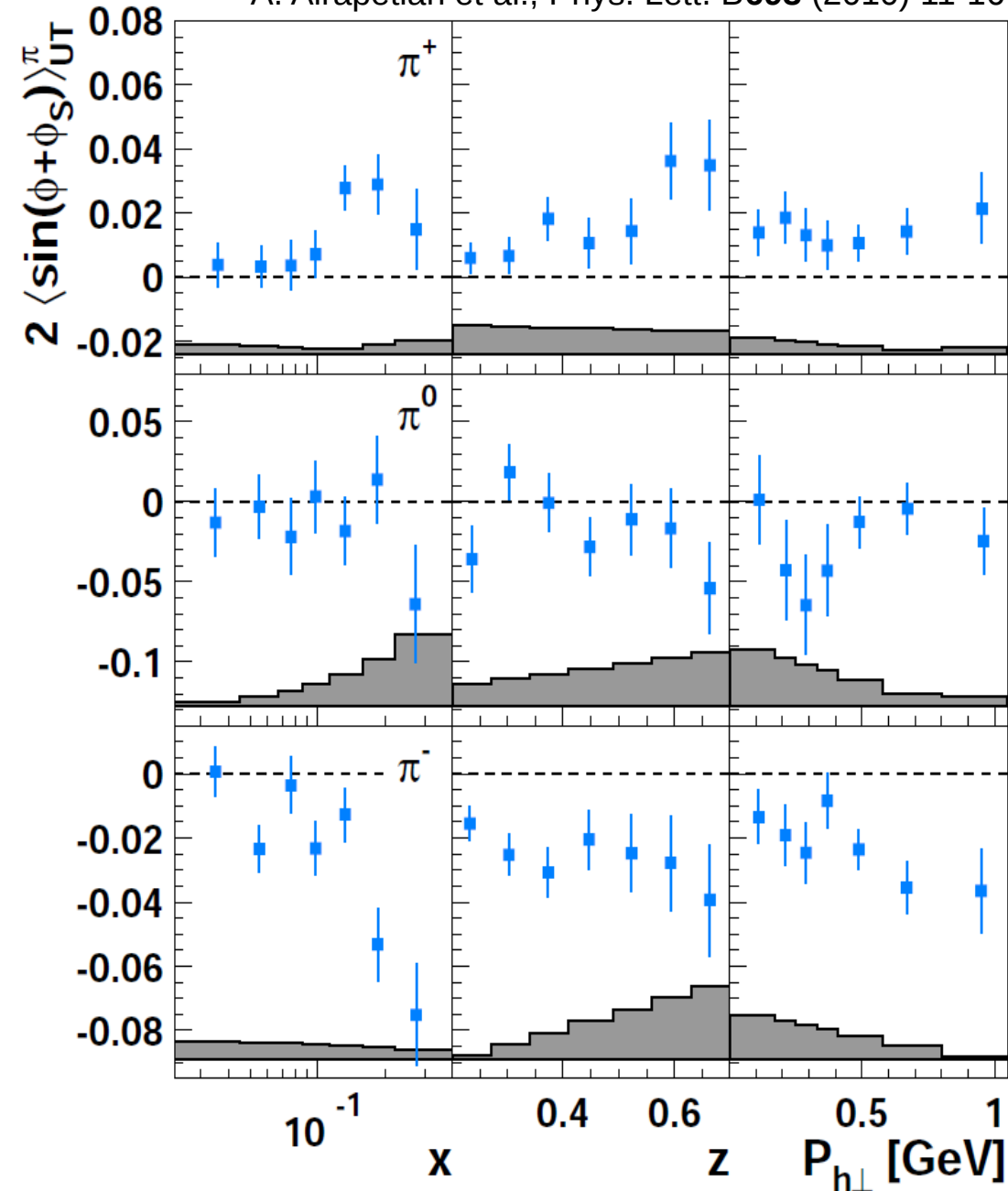
A. Airapetian et al., Phys. Lett. B**693** (2010) 11-16



- π^\pm increasing with z
 - positive for π^+
 - large & negative for π^-
- $$H_1^{\perp, fav} \approx -H_1^{\perp, unfav}$$
- isospin symmetry fulfilled

Collins amplitudes for pions

A. Airapetian et al., Phys. Lett. B**693** (2010) 11-16

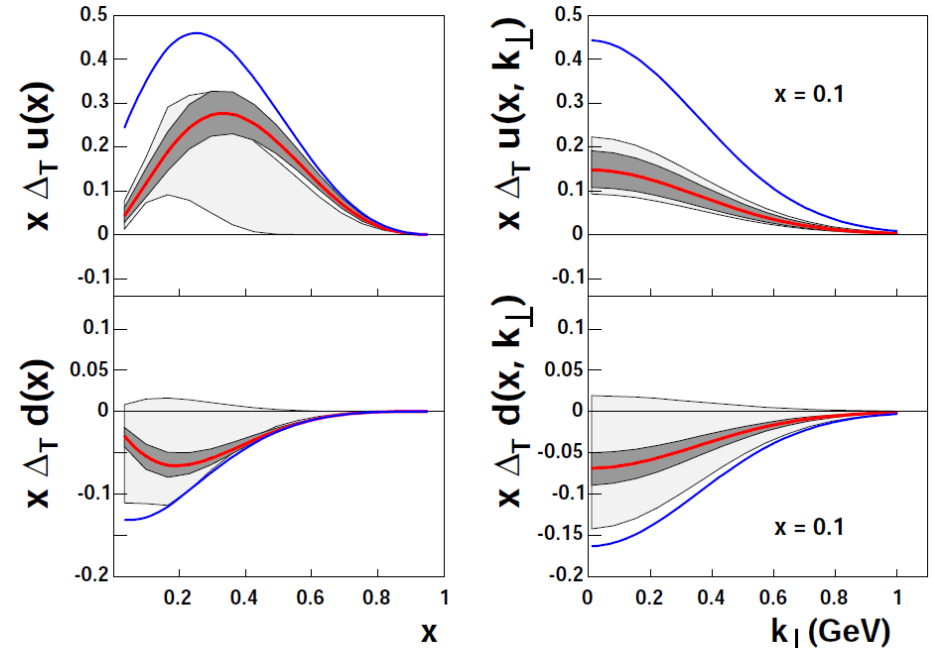


- π^\pm increasing with z
- positive for π^+
- large & negative for π^-

$$H_1^{\perp, fav} \approx -H_1^{\perp, unfav}$$

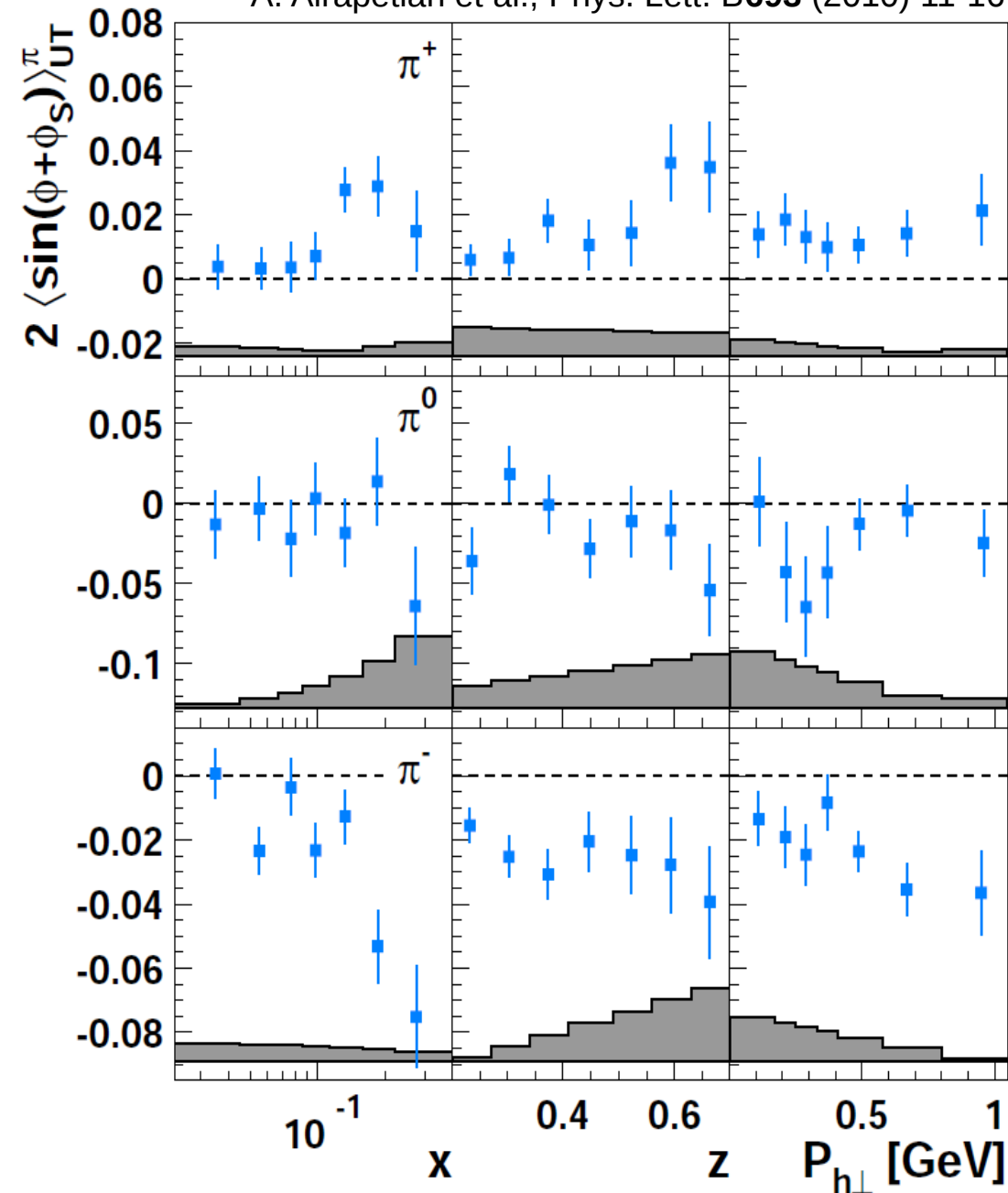
- isospin symmetry fulfilled
- data from BELLE, COMPASS & HERMES \longrightarrow extraction of h_{1T}^q

Anselmino et al., arXiv: 0807.0173



Collins amplitudes for pions

A. Airapetian et al., Phys. Lett. B**693** (2010) 11-16

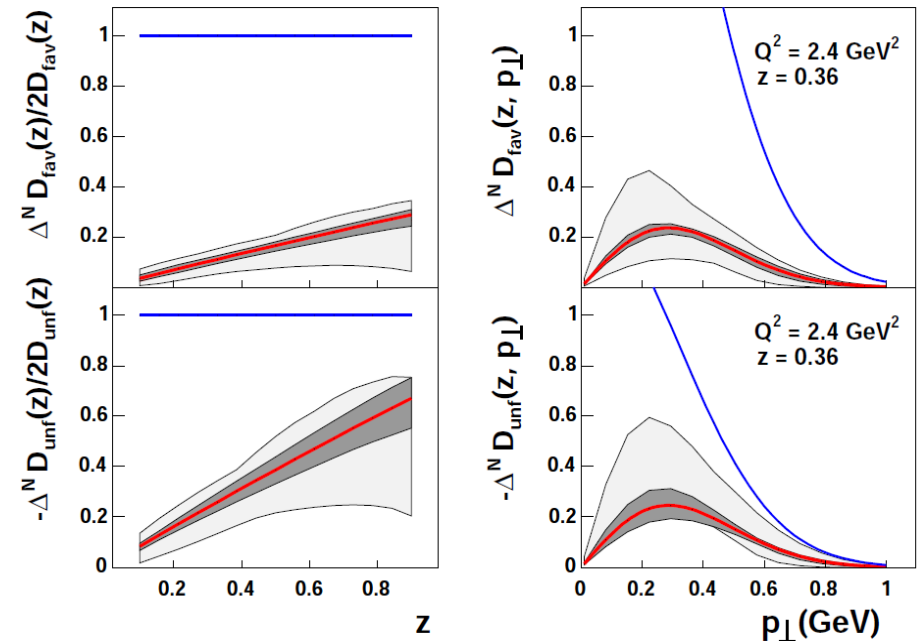


- π^{\pm} increasing with z
- positive for π^+
- large & negative for π^-

$$H_1^{\perp, fav} \approx -H_1^{\perp, unfav}$$

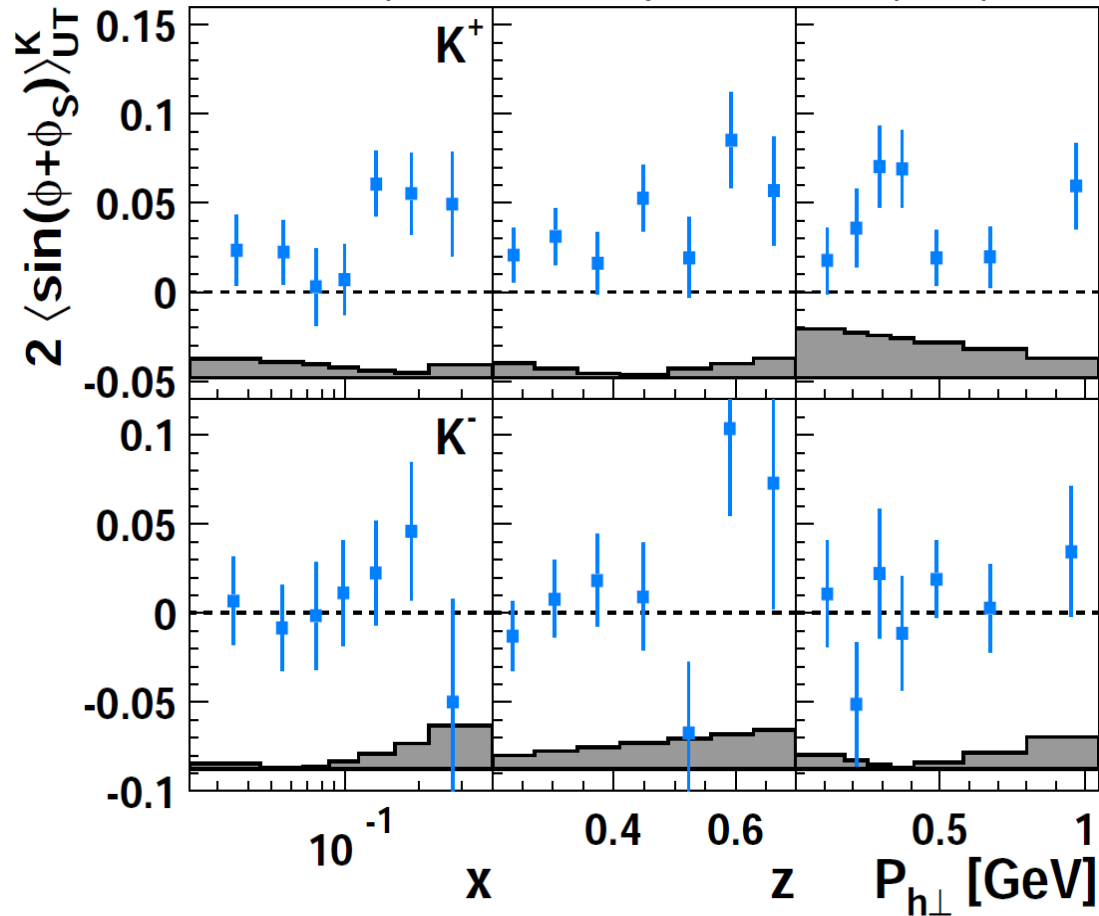
- isospin symmetry fulfilled
- data from BELLE, COMPASS & HERMES \longrightarrow extraction of H_1^{\perp}

Anselmino et al., arXiv: 0807.0173



Collins amplitudes for kaons

A. Airapetian et al., Phys. Lett. B**693** (2010) 11-16

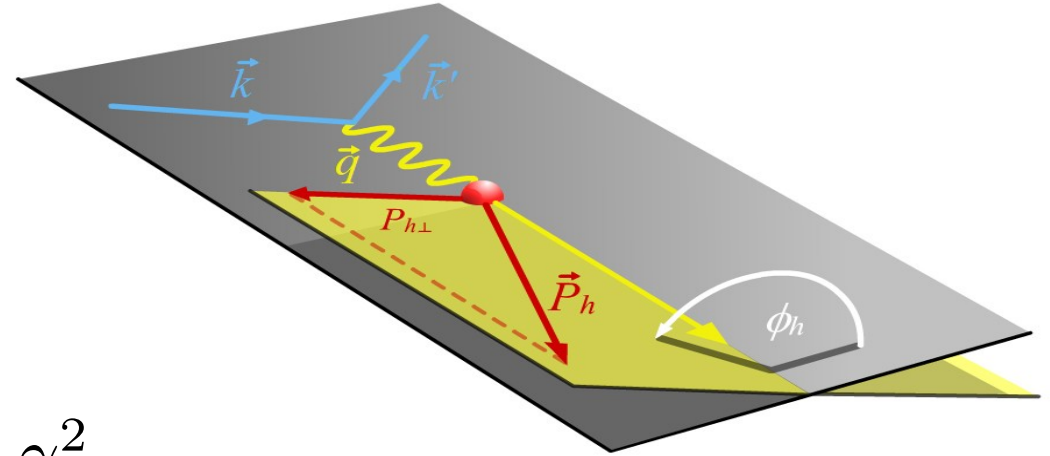


- K^+ : increasing with z
- positive for K^+ & larger than for π^+
 - role of s-quark
 - u-dominance $\xrightarrow{?}$

$$H_1^{\perp, u \rightarrow K^+} > H_1^{\perp, u \rightarrow \pi^+}$$

- $K^- \approx 0$, \neq from π^-
 K^- is pure sea object:
 sea-quark transversity expected to be small

Spin-independent semi-inclusive DIS cross section

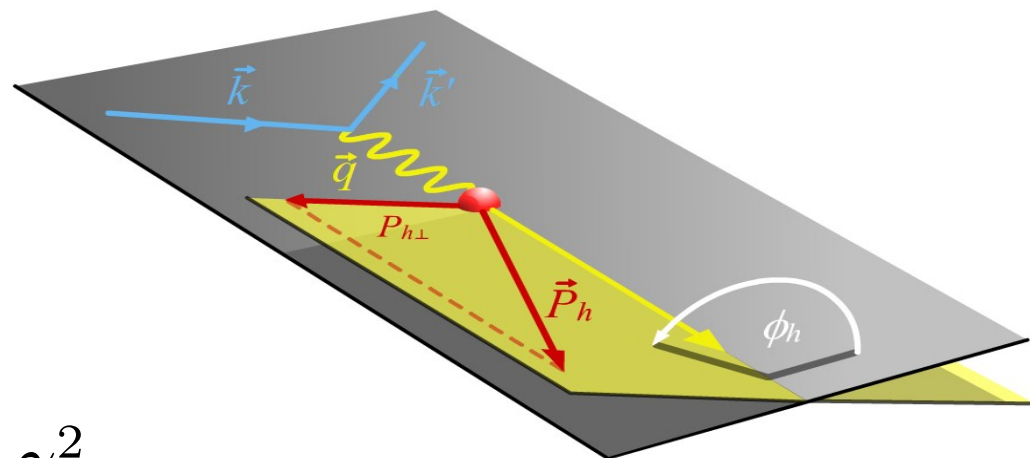


Non-collinear cross section

$$\frac{d\sigma}{dx dy dz dP_{h\perp}^2 d\phi_h} = \frac{\alpha^2}{xyQ^2} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ A(y) F_{UU,T} + B(y) F_{UU,L} \right. \\ \left. + C(y) \cos \phi_h F_{UU}^{\cos \phi_h} + B(y) \cos 2\phi_h F_{UU}^{\cos 2\phi_h} \right\}$$

$$\gamma = \frac{2Mx}{Q}, \quad F = F(x, Q, z, \vec{P}_{h\perp})$$

Spin-independent semi-inclusive DIS cross section



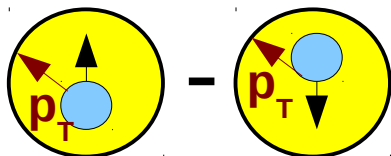
Non-collinear cross section

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$$\gamma = \frac{2Mx}{Q}, \quad F = F(x, Q, z, \vec{P}_{h\perp})$$

leading twist

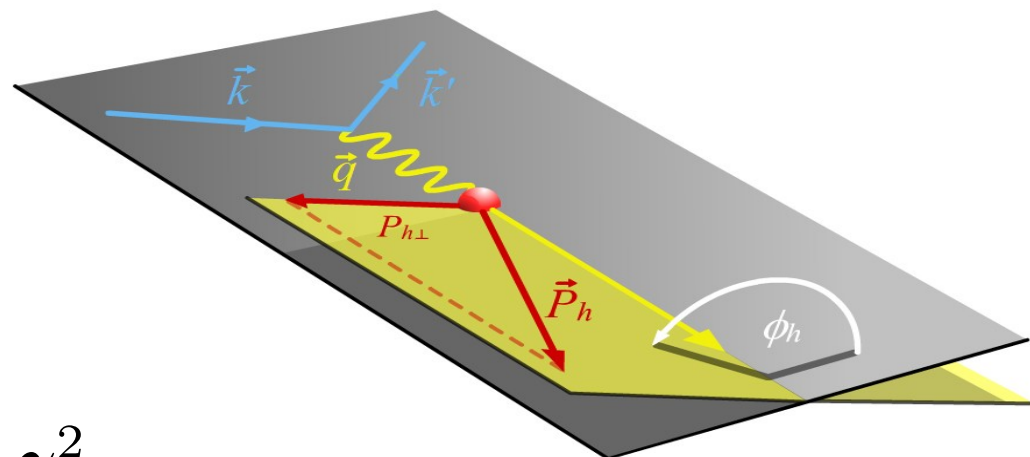
$$F_{UU}^{\cos 2\phi_h} = \mathcal{I} \left[- \frac{2(\hat{P}_{h\perp} \cdot \vec{p}_T)(\hat{P}_{h\perp} \cdot \vec{k}_T) - \vec{p}_T \cdot \vec{k}_T}{M_h M} h_1^\perp H_1^\perp \right]$$



Boer-Mulders DF

Collins FF

Spin-independent semi-inclusive DIS cross section



Non-collinear cross section

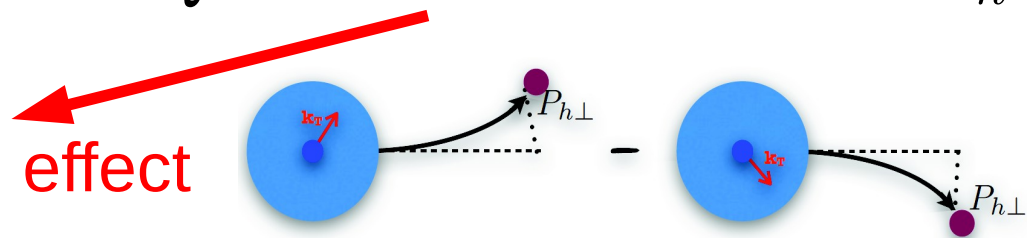
$$\frac{d\sigma}{dx dy dz dP_{h\perp}^2 d\phi_h} = \frac{\alpha^2}{xyQ^2} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ A(y) F_{UU,T} + B(y) F_{UU,L} \right. \\ \left. + C(y) \cos \phi_h F_{UU}^{\cos \phi_h} + B(y) \cos 2\phi_h F_{UU}^{\cos 2\phi_h} \right\}$$

$$\gamma = \frac{2Mx}{Q}, \quad F = F(x, Q, z, \vec{P}_{h\perp})$$

sub-leading twist

$$F_{UU}^{\cos \phi_h} = \frac{2M}{Q} \mathcal{I} \left[-\frac{\hat{P}_{h\perp} \cdot \vec{p}_T}{M} f_1 D_1 - \frac{\hat{P}_{h\perp} \cdot \vec{k}_T}{M_h} \frac{p_T^2}{M^2} h_1^\perp H_1^\perp + \dots \right]$$

Cahn effect



quark-gluon-quark correlations

Extraction of the cosine moments

$$\langle \cos(n\phi_h) \rangle \stackrel{th.}{=} \frac{\int d\phi_h \cos(n\phi_h) \sigma_{UU}(\omega, \phi_h)}{\int d\phi_h \sigma_{UU}(\omega, \phi_h)} \quad \omega = (x, y, z, P_{h\perp}^2)$$

$$\langle \cos(n\phi_h) \rangle \stackrel{exp.}{=} \frac{\int d\phi_h \cos(n\phi_h) \epsilon_{acc}(\omega, \phi_h) \epsilon_{rad}(\omega, \phi_h) \sigma_{UU}(\omega, \phi_h)}{\int d\phi_h \epsilon_{acc}(\omega, \phi_h) \epsilon_{rad}(\omega, \phi_h) \sigma_{UU}(\omega, \phi_h)}$$

Extraction of the cosine moments

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extraction is challenging!

azimuthal modulations also possible due to

- detector geometrical acceptance
- higher-order QED effects

Extraction of the cosine moments

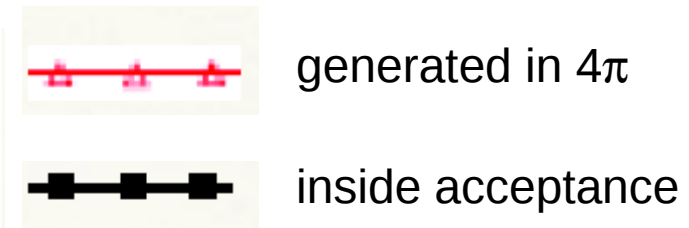
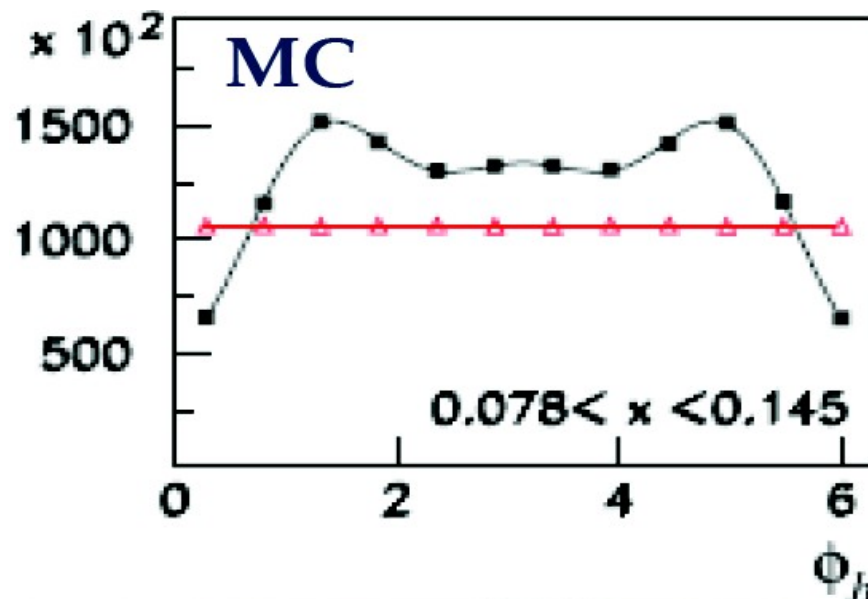
$$\langle \cos(n\phi_h) \rangle \stackrel{th.}{=} \frac{\int d\phi_h \cos(n\phi_h) \sigma_{UU}(\omega, \phi_h)}{\int d\phi_h \sigma_{UU}(\omega, \phi_h)} \quad \omega = (x, y, z, P_{h\perp}^2)$$

$$\langle \cos(n\phi_h) \rangle \stackrel{exp.}{=} \frac{\int d\phi_h \cos(n\phi_h) \epsilon_{acc}(\omega, \phi_h) \epsilon_{rad}(\omega, \phi_h) \sigma_{UU}(\omega, \phi_h)}{\int d\phi_h \epsilon_{acc}(\omega, \phi_h) \epsilon_{rad}(\omega, \phi_h) \sigma_{UU}(\omega, \phi_h)}$$

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- detector geometrical acceptance
- higher-order QED effects



Extraction of the cosine moments

$$\langle \cos(n\phi_h) \rangle \stackrel{th.}{=} \frac{\int d\phi_h \cos(n\phi_h) \sigma_{UU}(\omega, \phi_h)}{\int d\phi_h \sigma_{UU}(\omega, \phi_h)} \quad \omega = (x, y, z, P_{h\perp}^2)$$

$$\langle \cos(n\phi_h) \rangle \stackrel{exp.}{=} \frac{\int d\phi_h \cos(n\phi_h) \epsilon_{acc}(\omega, \phi_h) \epsilon_{rad}(\omega, \phi_h) \sigma_{UU}(\omega, \phi_h)}{\int d\phi_h \epsilon_{acc}(\omega, \phi_h) \epsilon_{rad}(\omega, \phi_h) \sigma_{UU}(\omega, \phi_h)}$$

extraction is challenging!

azimuthal modulations also possible due to

- detector geometrical acceptance
- higher-order QED effects



fully differential analysis needed
unfolding procedure with 400 x 12 bins

BINNING

400 kinematic bins x 12 ϕ -bins

| Variable | Bin limits | | | | | | # |
|----------|------------|-------|-------|-------|------|---|---|
| x | 0.023 | 0.042 | 0.078 | 0.145 | 0.27 | 1 | 5 |
| y | 0.3 | 0.45 | 0.6 | 0.7 | 0.85 | | 4 |
| z | 0.2 | 0.3 | 0.45 | 0.6 | 0.75 | 1 | 5 |
| P_{hT} | 0.05 | 0.2 | 0.35 | 0.5 | 0.75 | | 4 |

Extraction of the cosine moments

$$\langle \cos(n\phi_h) \rangle \stackrel{th.}{=} \frac{\int d\phi_h \cos(n\phi_h) \sigma_{UU}(\omega, \phi_h)}{\int d\phi_h \sigma_{UU}(\omega, \phi_h)} \quad \omega = (x, y, z, P_{h\perp}^2)$$

$$\langle \cos(n\phi_h) \rangle \stackrel{exp.}{=} \frac{\int d\phi_h \cos(n\phi_h) \epsilon_{acc}(\omega, \phi_h) \epsilon_{rad}(\omega, \phi_h) \sigma_{UU}(\omega, \phi_h)}{\int d\phi_h \epsilon_{acc}(\omega, \phi_h) \epsilon_{rad}(\omega, \phi_h) \sigma_{UU}(\omega, \phi_h)}$$

extraction is challenging!

azimuthal modulations also possible due to

- detector geometrical acceptance
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unfolding

fully differential analysis needed
unfolding procedure with 400 x 12 bins

$$\langle \cos(n\phi_h) \rangle \approx \left. \frac{\int d\phi_h \cos(n\phi_h) \sigma_{UU}(\omega, \phi_h)}{\int d\phi_h \sigma_{UU}(\omega, \phi_h)} \right|_{\text{bin } i}$$

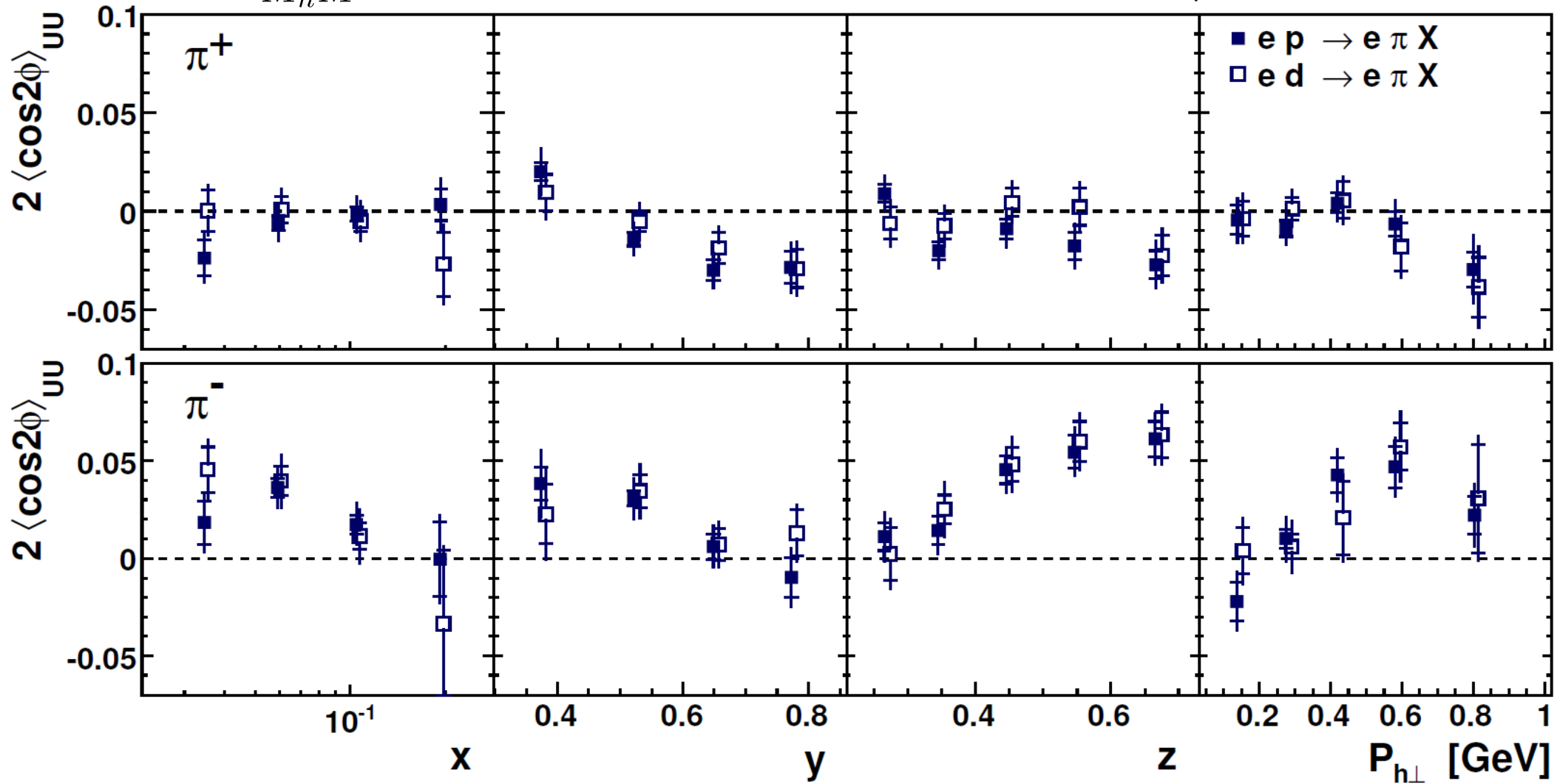
BINNING
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Results for $\langle \cos 2\phi_h \rangle$: pions

$$\mathcal{I} \left[-\frac{2(\hat{P}_{h\perp} \cdot \vec{p}_T)(\hat{P}_{h\perp} \cdot \vec{k}_T) - \vec{p}_T \cdot \vec{k}_T}{M_h M} h_1^\perp H_1^\perp \right]$$

A. Airapetian et al., arXiv:1204.4161

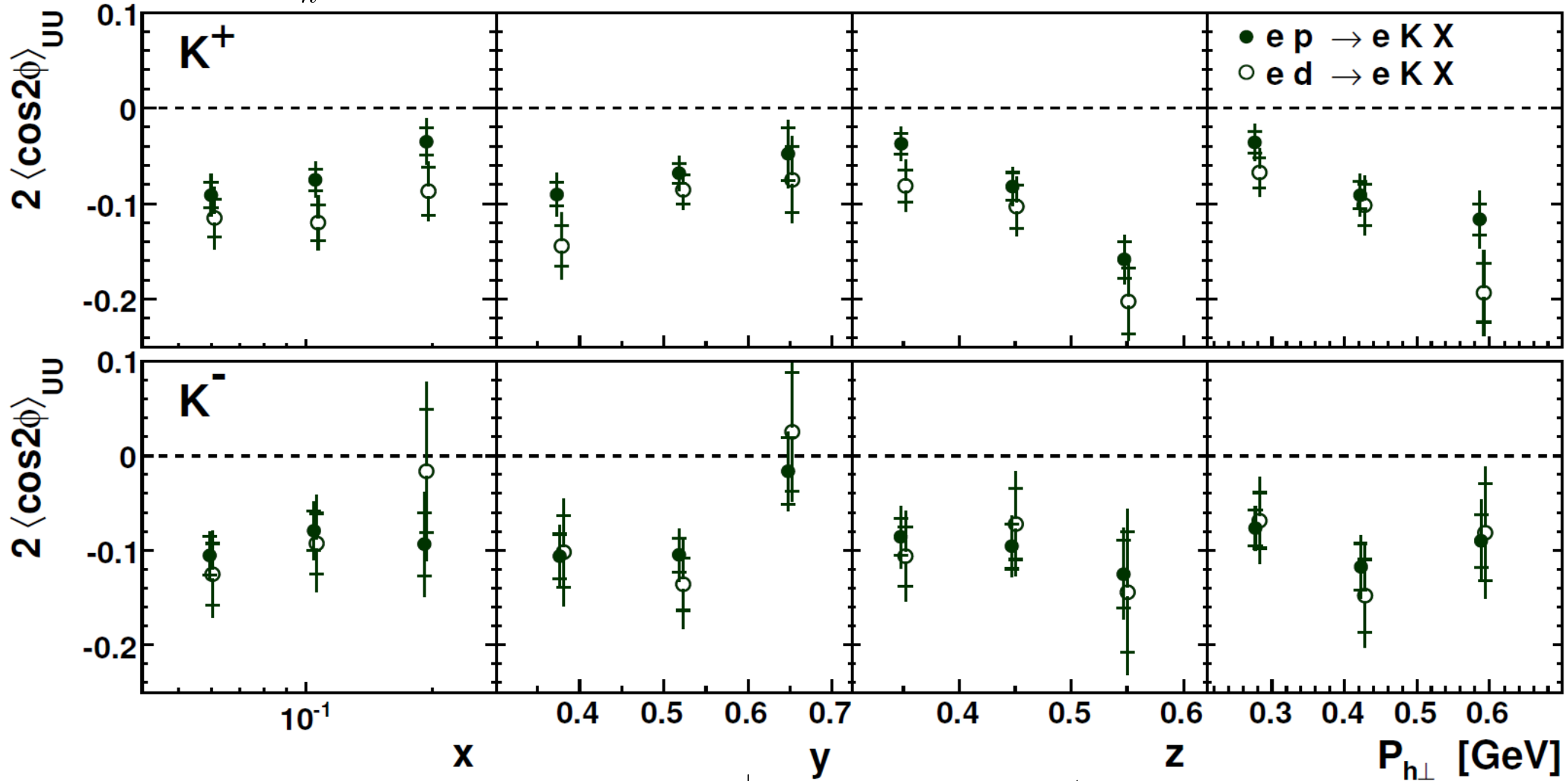


- H-D comparison: $h_1^{\perp,u} \approx h_1^{\perp,d}$
- $\pi^- > 0 \longleftrightarrow \pi^+ \leq 0$: $H_1^{\perp, fav} \approx -H_1^{\perp, unfav}$

Results for $\langle \cos 2\phi_h \rangle$: kaons

$$\mathcal{I} \left[-\frac{2(\hat{P}_{h\perp} \cdot \vec{p}_T)(\hat{P}_{h\perp} \cdot \vec{k}_T) - \vec{p}_T \cdot \vec{k}_T}{M_h M} h_1^\perp H_1^\perp \right]$$

A. Airapetian et al., arXiv:1204.4161

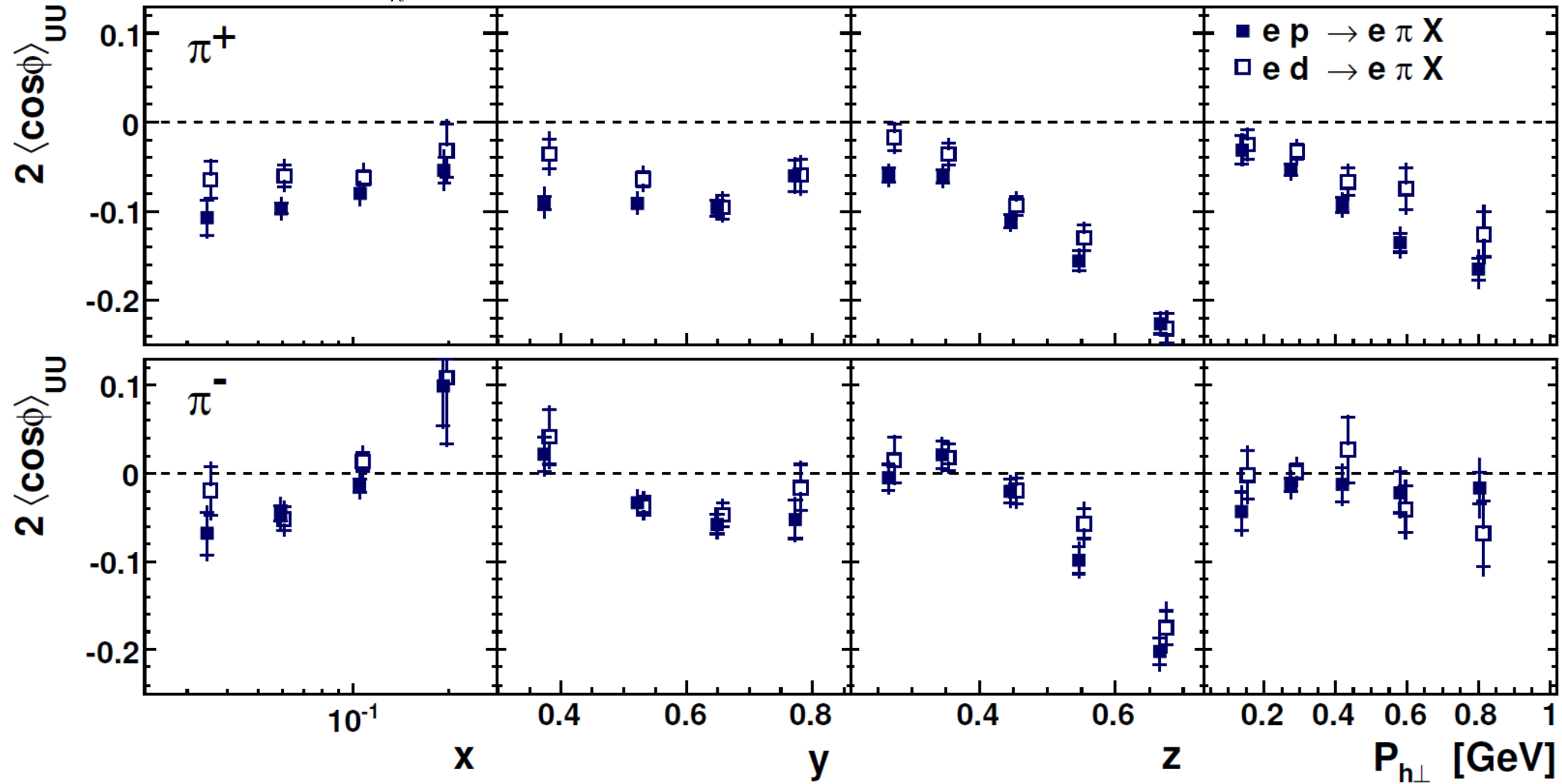


- $K^+ < 0$: - Artru model: $\text{sign } H_1^\perp, u \rightarrow K^+ = \text{sign } H_1^\perp, u \rightarrow \pi^+$
- $K^- \approx K^+$: - u-dominance $\xrightarrow{?} H_1^\perp, u \rightarrow K^+ \approx H_1^\perp, u \rightarrow K^-$
- role of sea-quarks

Results for $\langle \cos \phi_h \rangle$: pions

$$\mathcal{I}\left[-\frac{\hat{P}_{h\perp}\cdot\vec{p}_T}{M}f_1D_1 - \frac{\hat{P}_{h\perp}\cdot\vec{k}_T}{M_h}\frac{p_T^2}{M^2}h_1^\perp H_1^\perp + \dots\right]$$

A. Airapetian et al., arXiv:1204.4161

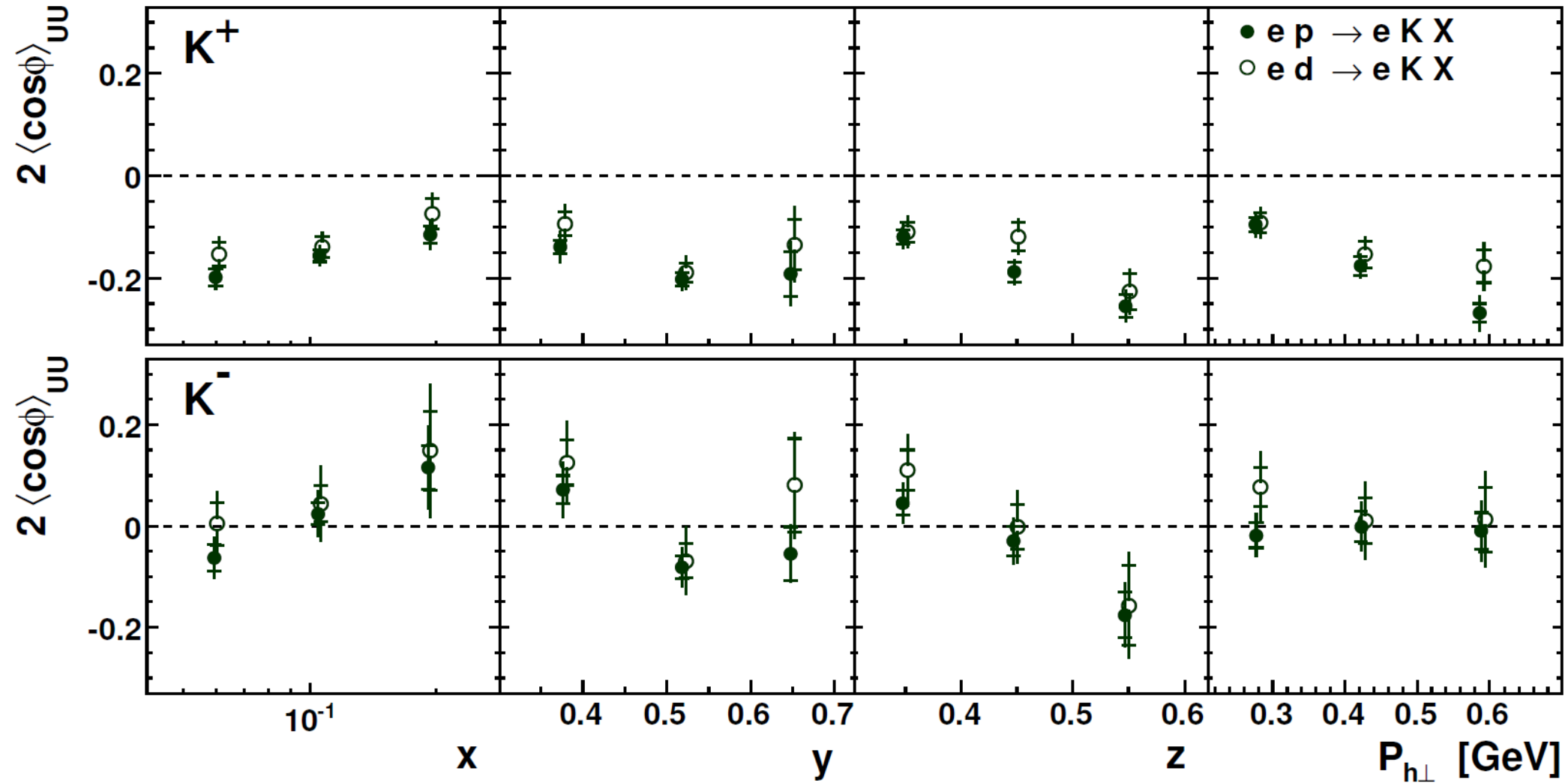


- H-D comparison: weak flavor dependence
- magnitude increases with z
- π^+ : magnitude increases with $P_{h\perp}$

Results for $\langle \cos \phi_h \rangle$: kaons

$$\mathcal{I}\left[-\frac{\hat{P}_{h\perp} \cdot \vec{p}_T}{M} f_1 D_1 - \frac{\hat{P}_{h\perp} \cdot \vec{k}_T}{M_h} \frac{p_T^2}{M^2} h_1^\perp H_1^\perp + \dots\right]$$

A. Airapetian et al., arXiv:1204.4161

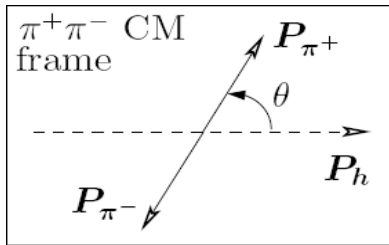


- $K^+ < 0$, larger in magnitude than π^+
- $K^- \approx 0$

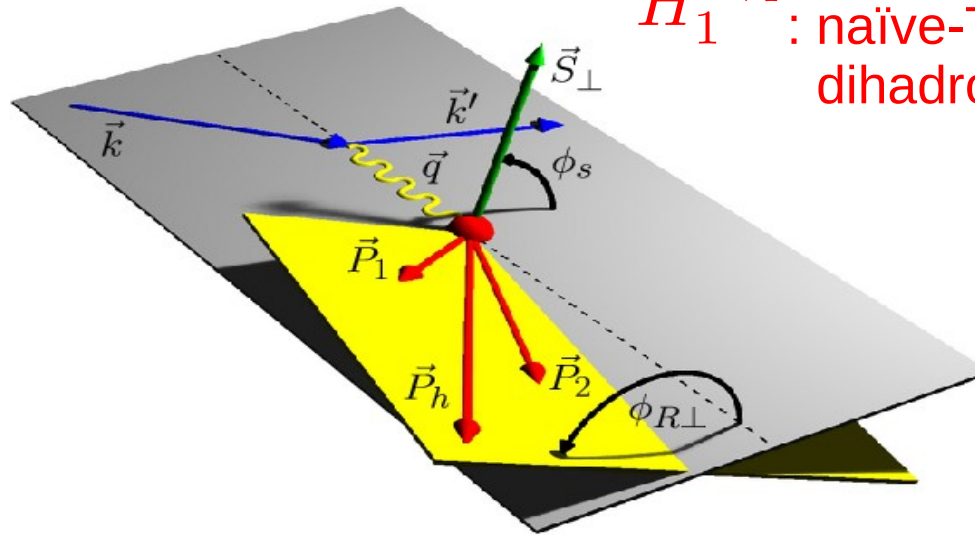
Access to dihadron fragmentation function

Single-spin asymmetry: $\pi^+\pi^-$ production

$$\sigma_{UT} \sim \sin(\phi_{R\perp} + \phi_S) \sum_q e_q^2 h_1^q(x) H_1^{\triangleleft,q}(z, M_{\pi\pi}, \theta)$$



$H_1^{\triangleleft,q}$: naïve-T-odd and chiral-odd dihadron fragmentation function



$$\vec{R} = \frac{1}{2}(\vec{P}_1 - \vec{P}_2)$$

$$\vec{P}_h = \vec{P}_1 + \vec{P}_2$$

$$\vec{R}_T = \vec{R} - (\vec{R} \cdot \hat{P}_h) \hat{P}_h$$

- independent method to probe transversity: transverse spin of fragmenting quark transferred to relative orbital angular momentum of hadron pair
- integration over hadron momenta \rightarrow direct product but
- more complex cross section (9 variables)
- less statistics

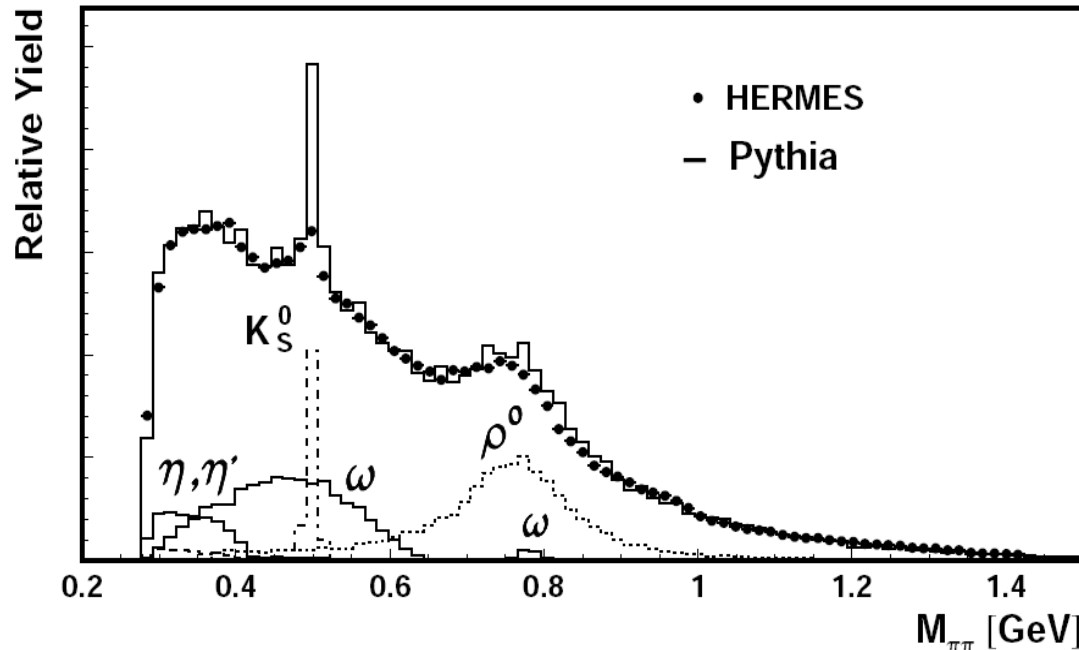
Extraction of $\pi^+\pi^-$ asymmetry

$$A_{UT} \sim \sin(\phi_{R\perp} + \phi_S) \sin \theta \frac{\sum_q e_q^2 h_{1T}^q(x) H_1^{\triangleleft,q}(z, M_{\pi\pi}, \cos \theta)}{\sum_q e_q^2 f_1^q(x) D_1^q(z, M_{\pi\pi}, \cos \theta)}$$

- Legendre expansion ($M_{\pi\pi} < 1.5$ GeV):

$$H_1^{\triangleleft} = H_1^{\triangleleft,sp} + H_1^{\triangleleft,pp} \cos \theta$$

$$D_1 = D_1 + D_1^{sp} \cos \theta + D_1^{pp} \frac{1}{4} (3 \cos^2 \theta - 1)$$



Extraction of $\pi^+\pi^-$ asymmetry

- Legendre expansion ($M_{\pi\pi} < 1.5$ GeV):

$$H_1^\angle = H_1^{\angle,sp} + H_1^{\angle,pp} \cos \theta$$

$$D_1 = D_1 + D_1^{sp} \cos \theta + D_1^{pp} \frac{1}{4} (3 \cos^2 \theta - 1)$$

- symmetrization around $\theta = \pi/2$

$$\cancel{H_1^{\angle,pp} \cos \theta} \quad \text{and} \quad \cancel{D_1^{sp} \cos \theta}$$

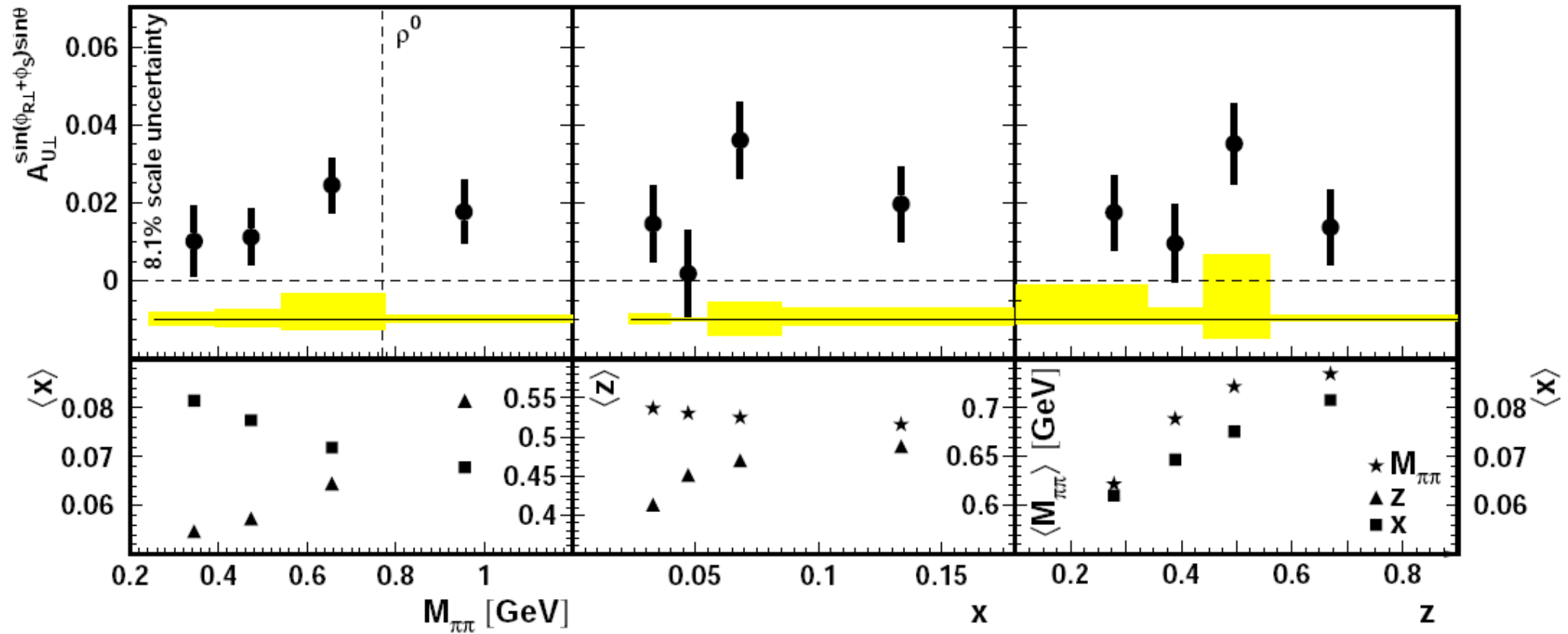


$$\frac{a}{1 + \frac{b}{4} (3 \cos^2 \theta - 1)} \sin(\phi_{R\perp} + \phi_S) \sin \theta$$

$$a \equiv A_{U\perp}^{\sin(\phi_{R\perp} + \phi_S) \sin \theta} \sim \frac{\sum_q e_q^2 h_{1T}(x) H_1^{\angle,sp}(z, M_{\pi\pi})}{\sum_q e_q^2 f_1(x) D_1(z, M_{\pi\pi})}$$

Final HERMES results

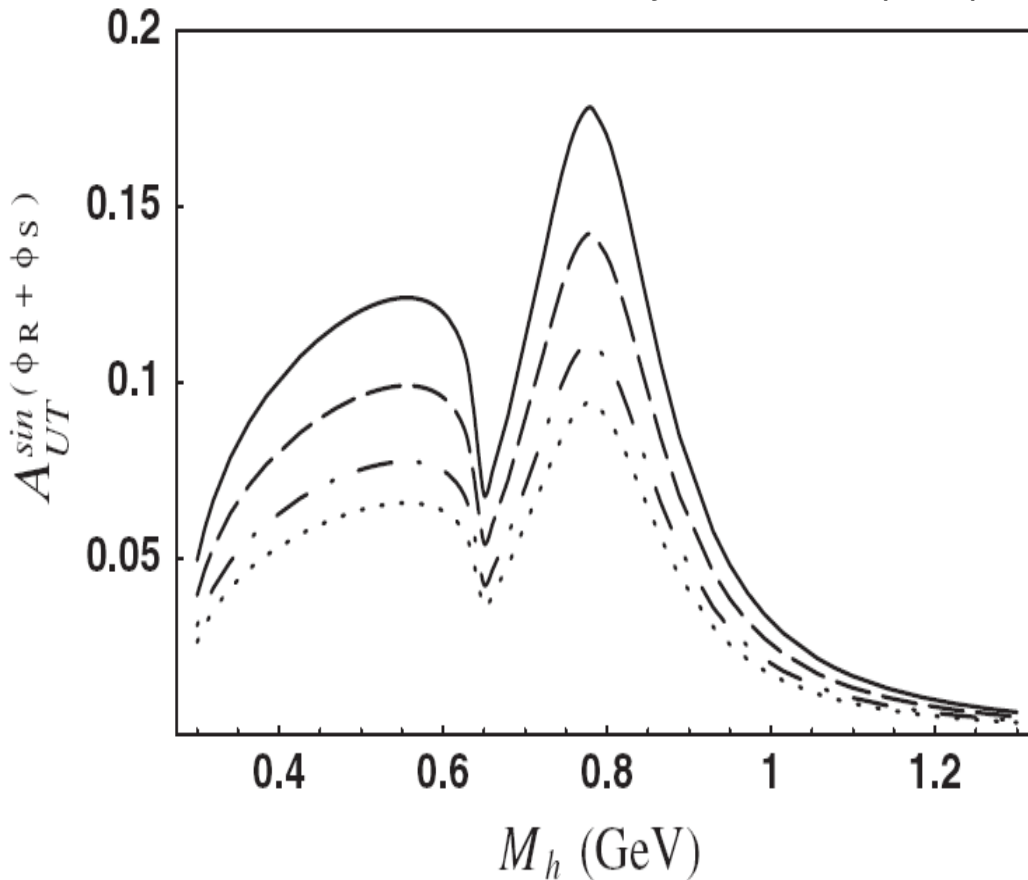
A. Airapetian et al., JHEP 0806 (2008) 017



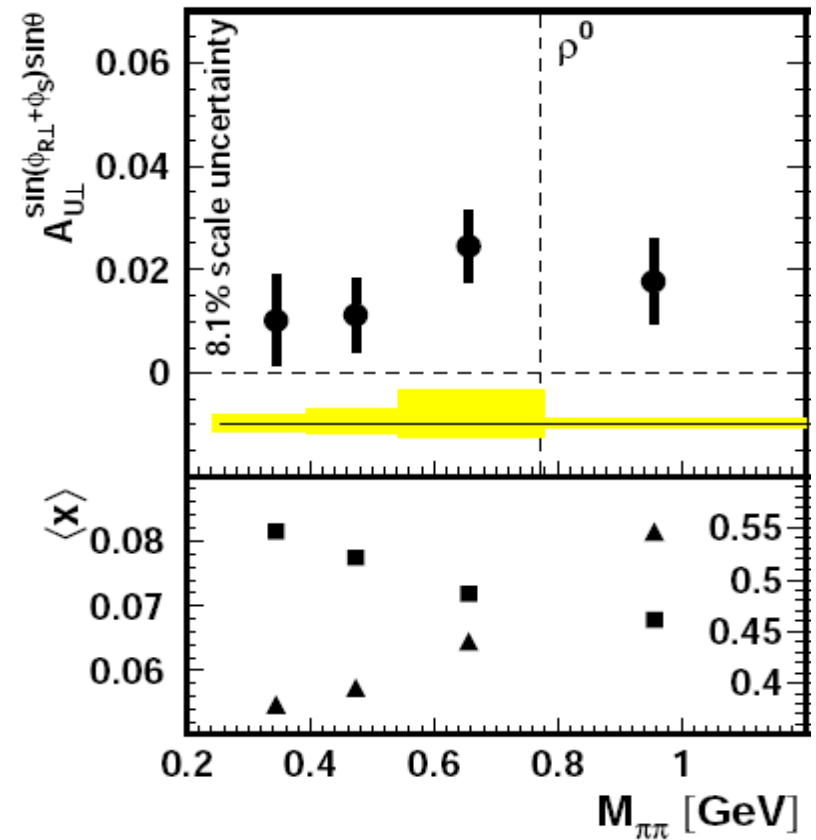
- first evidence for non-zero T-odd and chiral-odd dihadron fragmentation function

Comparison with model

A. Bacchetta, M. Radici, Phys. Rev. D74 (2006) 114007



A. Airapetian et al., JHEP 0806 (2008) 017



- no sign change around ρ^0 mass (\longleftrightarrow Jaffe model), confirmed by BELLE and COMPASS data

Summary

- π^\pm and K^\pm multiplicities on hydrogen and deuterium:
 - 3-dimensional extraction
 - support notion of favored fragmentation
- hadronization in nuclei:
 - 2-dimensional extraction
 - contribute to increased understanding of fragmentation process
- SIDIS single-hadron production on transv. pol. H and unpol. H and D:
 - pions: opposite sign for favored and unfavored u-quark Collins fragmentation function
 - kaons: large signal for single-spin asymmetry (K^+) and $\cos(2\phi)$ (K^+ and K^-)
 - substantial s-quark Collins fragmentation function?
- dihadron fragmentation function:
 - sizeable signal observed —►
 - contribute to increased understanding of transverse-spin effects

Backup

Multiplicities projected in z: VM contribution

