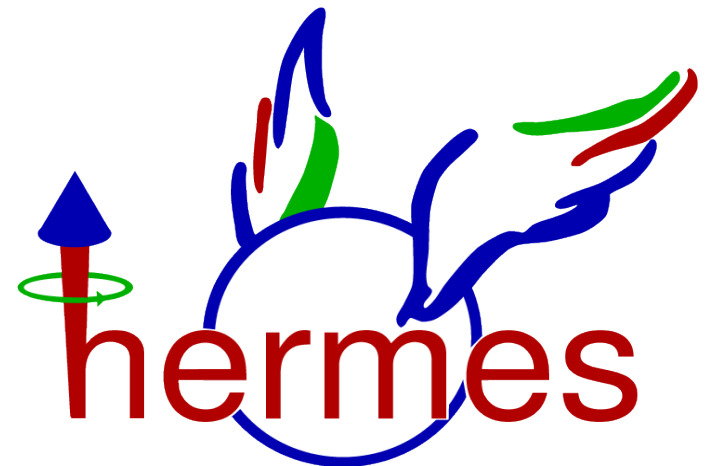


Overview of recent HERMES results

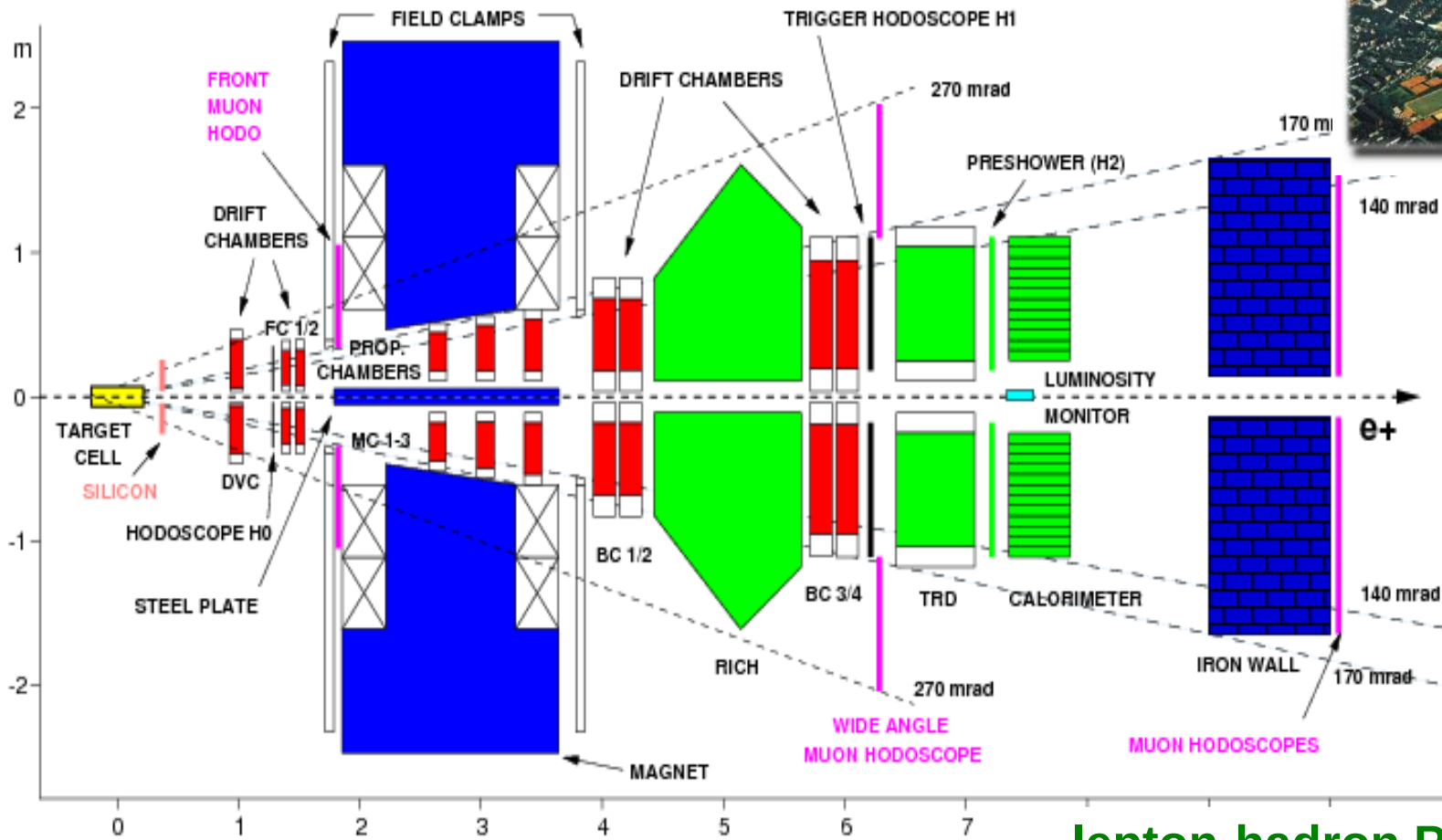
Charlotte Van Hulse, University of Ghent
on behalf of the HERMES collaboration



Overview

- strange quark distributions
- transverse structure of the nucleon
 - transverse momentum dependent distributions
 - transverse position:
generalized parton distributions and
deeply virtual Compton scattering

HERMES: HERA MEASUREMENT of SPIN



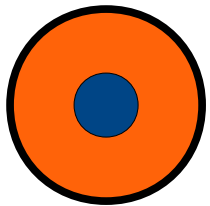
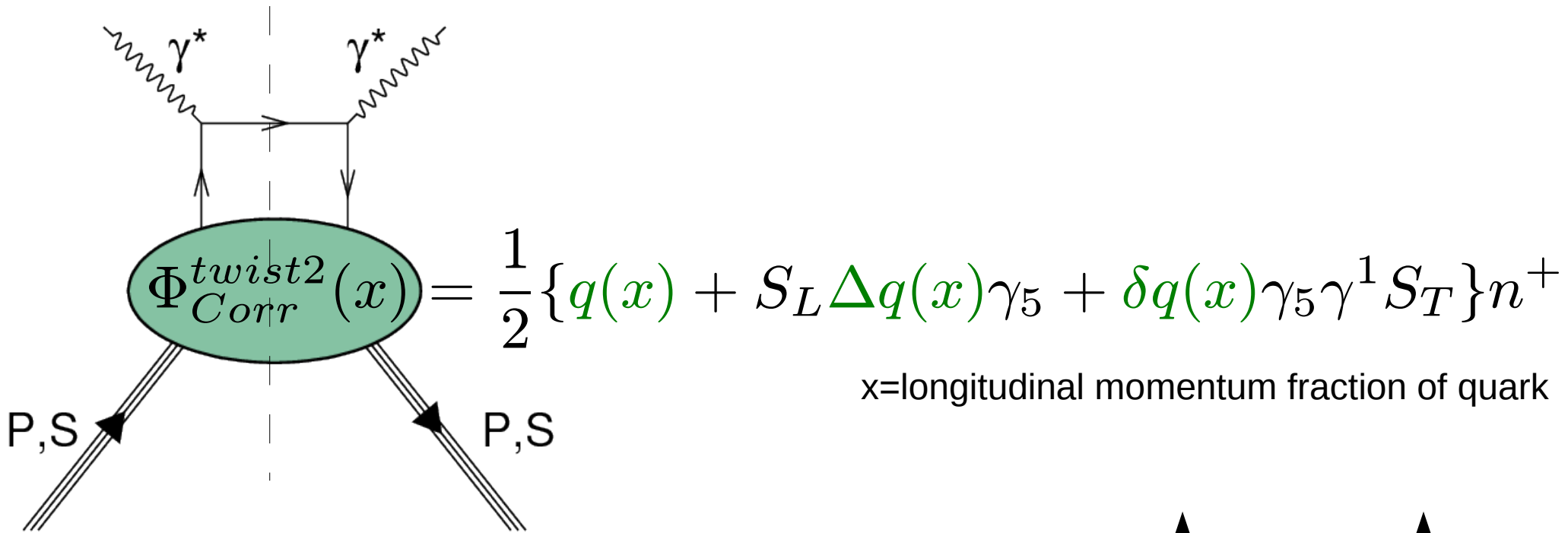
data taking from
1995
until
June, 30 2007

Beam
longitudinally pol.
 e^+ & e^-
 $E = 27.6 \text{ GeV}$

Gaseous internal target
longitudinally pol. H,D,He
transversely pol. H
unpol. H,D,Ne,Kr,..

lepton-hadron PID efficiency: ~98%
hadron PID: RICH 2-15 GeV/c
 $\delta E_\gamma / E_\gamma \cong 5\%$
 $\delta P / P < 2\%$
 $\Delta\theta < 1 \text{ mrad}$

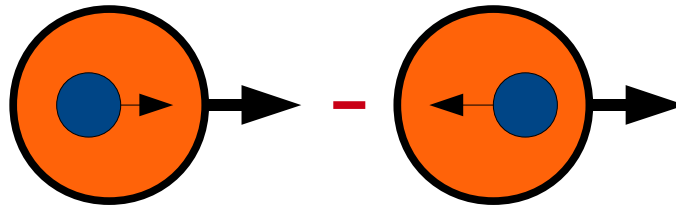
Probing the nucleon in DIS



$q(x)$

unpolarized nucleon
unpolarized quark

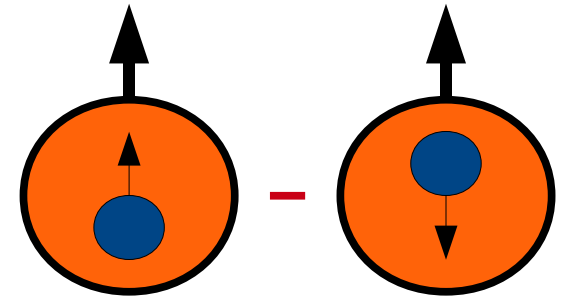
(also $f_1(x)$)



$\Delta q(x)$

longitudinally polarized nucleon
longitudinally polarized quark

(also $g_{1L}(x)$)



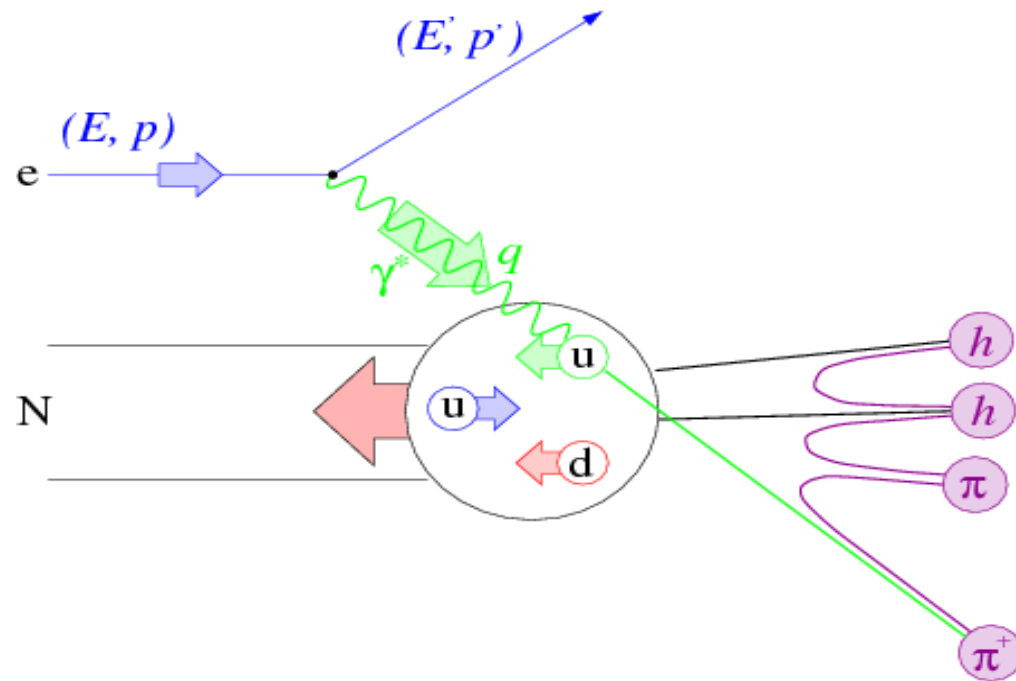
$\delta q(x)$

transversely polarized nucleon
transversely polarized quark

(also $h_{1T}(x)$)

How to access flavored quark distributions

Semi-inclusive deep-inelastic scattering (SIDIS)



$$Q^2 = -q^2$$

$$\nu \stackrel{lab}{=} E - E'$$

$$y \stackrel{lab}{=} \frac{\nu}{E}$$

$$x \stackrel{lab}{=} \frac{Q^2}{2M\nu}$$

$$z \stackrel{lab}{=} \frac{E_h}{\nu}$$

$$\sigma^{ep \rightarrow eh} = \sum_q DF^{p \rightarrow q}(x) \otimes \sigma^{eq \rightarrow eq} \otimes FF^{q \rightarrow h}(z)$$

Distribution Function (DF): distribution of quarks in nucleon

Fragmentation Function (FF): fragmentation of struck quark into final-state hadron

Strange quark distributions

Extraction of the strange quark distribution

- leading order extraction in α_s
- charged kaon production on (longitudinally pol.) deuteron:

$$e + d \rightarrow K^\pm + X$$

- strange quarks carry no isospin $\rightarrow s_p(x) = s_n(x)$
 $\Delta s_p(x) = \Delta s_n(x)$
- isoscalar target & $K^+ + K^- \rightarrow$ FF without isospin dependence
- hypothesis: isospin symmetry between p and n
charge-conjugation invariance of FF

A. Airapetian et al., Phys. Lett. B **666**, 446-450 (2008)

Kaon multiplicities

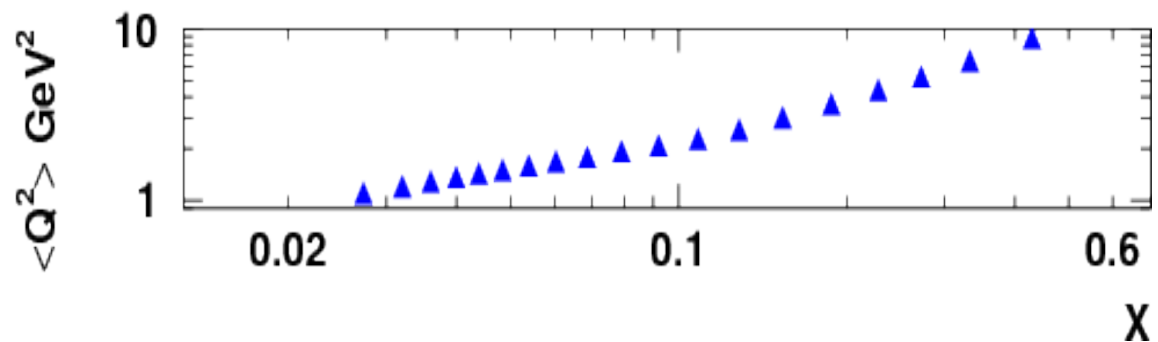
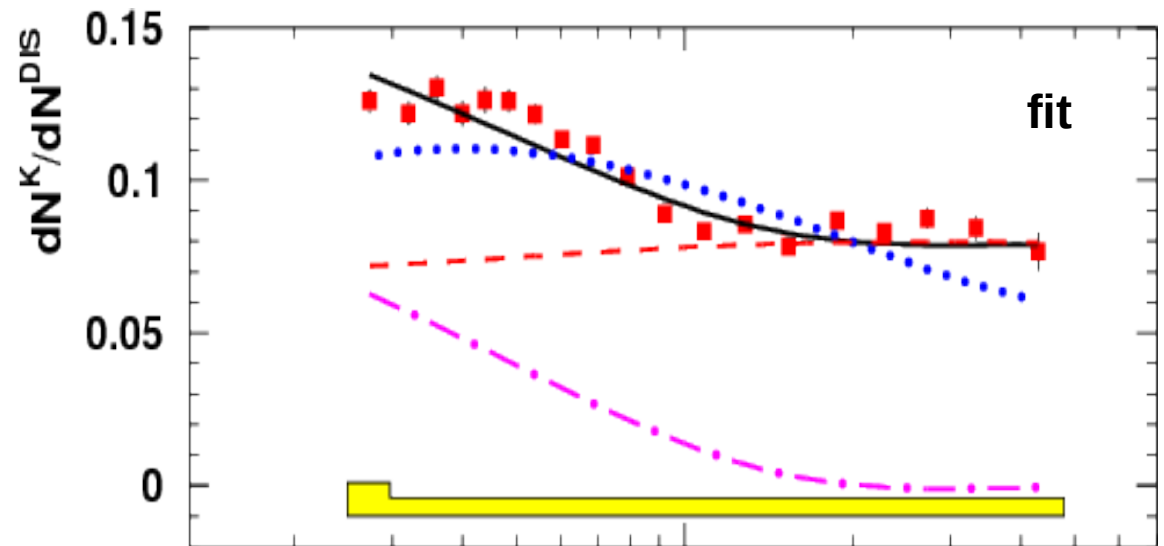
$$\frac{d^2 N^K(x)}{d^2 N^{DIS}(x)} = \frac{Q(x) \int_{0.2}^{0.8} \mathcal{D}_Q^K(z) dz + S(x) \int_{0.2}^{0.8} \mathcal{D}_S^K(z) dz}{5Q(x) + 2S(x)}$$

$$Q(x) \equiv u(x) + \bar{u}(x) + d(x) + \bar{d}(x)$$

$$S(x) \equiv s(x) + \bar{s}(x)$$

$$\mathcal{D}_Q^K(z) \equiv 4D_u^K(z) + D_d^K(z)$$

$$\mathcal{D}_S^K(z) \equiv 2D_s^K(z)$$



Kaon multiplicities

$$\frac{d^2 N^K(x)}{d^2 N^{DIS}(x)} = \frac{Q(x) \int_{0.2}^{0.8} \mathcal{D}_Q^K(z) dz + S(x) \int_{0.2}^{0.8} \mathcal{D}_S^K(z) dz}{5Q(x) + 2S(x)}$$

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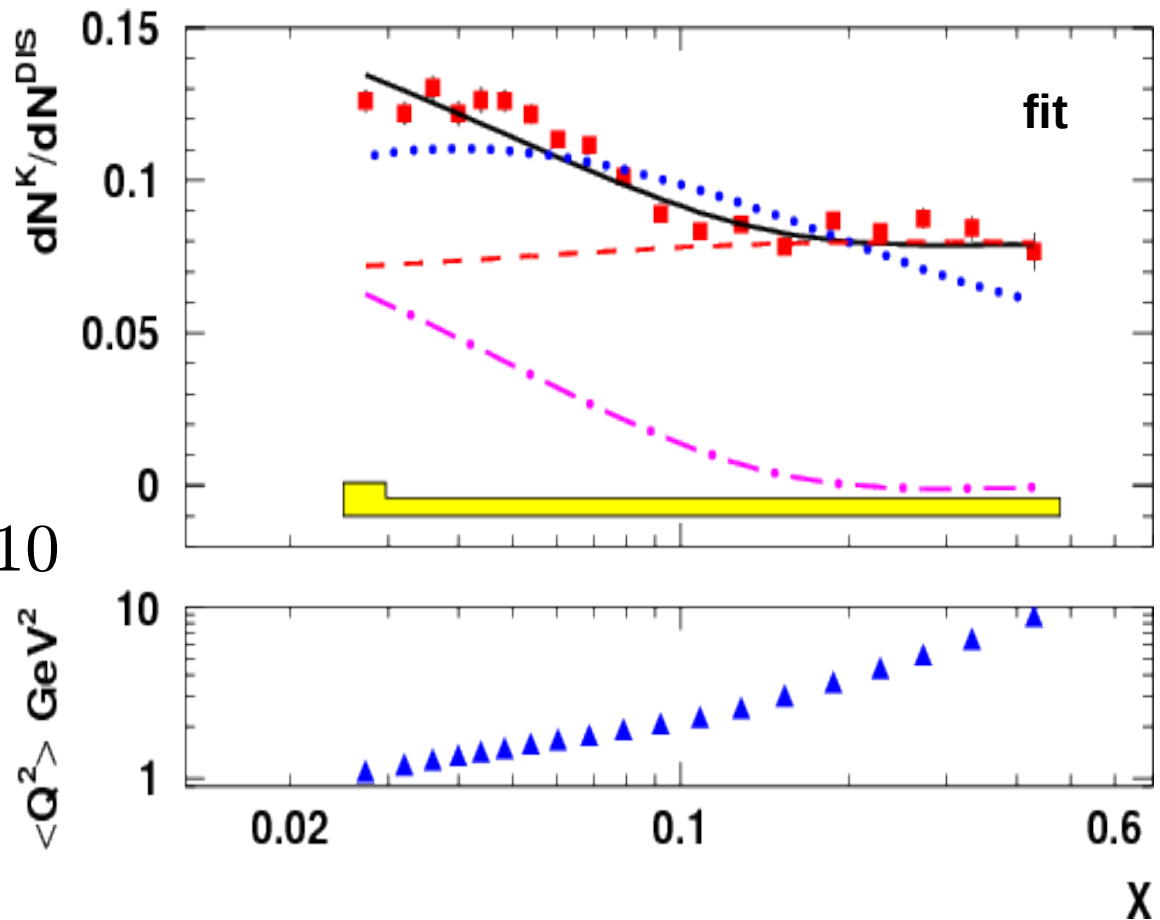
$$\mathcal{D}_Q^K(z) \equiv 4D_u^K(z) + D_d^K(z)$$

$$\mathcal{D}_S^K(z) \equiv 2D_s^K(z)$$

$S(x)=0$ for $x>0.15$

$Q(x)$ from CTEQ6L

$$\int_{0.2}^{0.8} \mathcal{D}_Q^K(z) dz = 0.398 \pm 0.010$$



Kaon multiplicities

$$\frac{d^2 N^K(x)}{d^2 N^{DIS}(x)} = \frac{Q(x) \int_{0.2}^{0.8} \mathcal{D}_Q^K(z) dz + S(x) \int_{0.2}^{0.8} \mathcal{D}_S^K(z) dz}{5Q(x) + 2S(x)}$$

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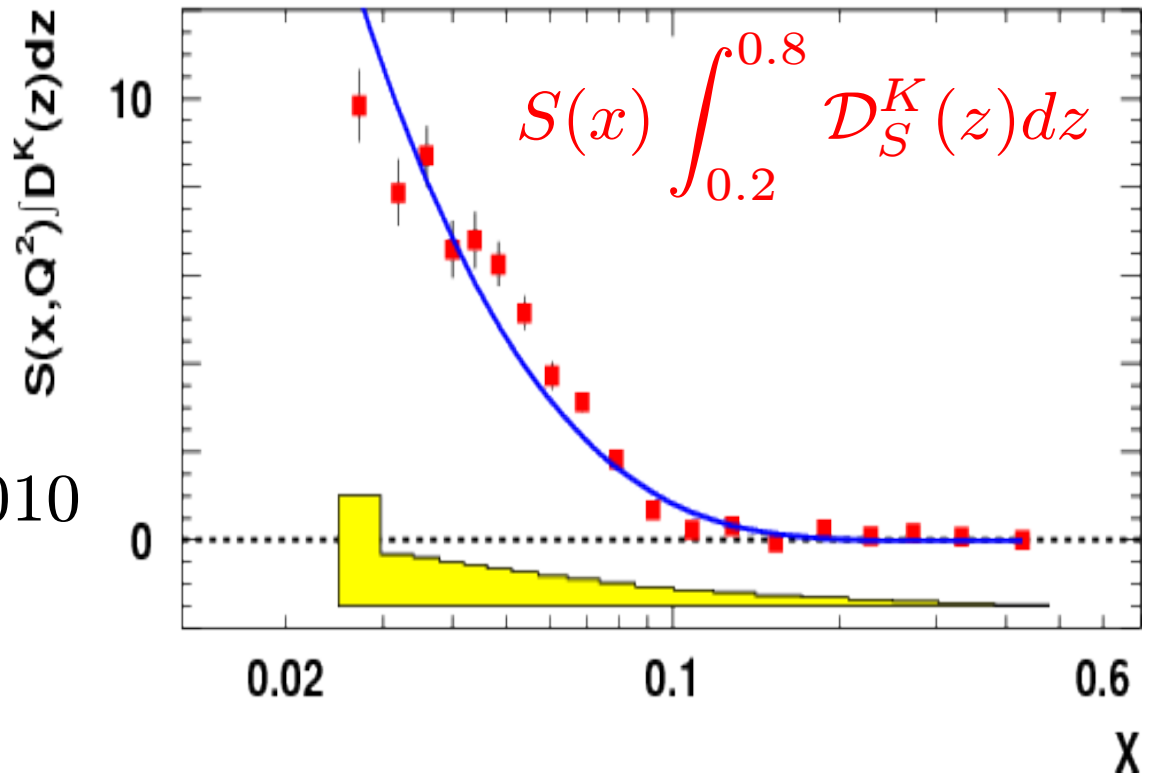
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$Q(x)$ from CTEQ6L

$$\int_{0.2}^{0.8} \mathcal{D}_Q^K(z) dz = 0.398 \pm 0.010$$

neglecting $2S(x)$

$$S(x) \int_{0.2}^{0.8} \mathcal{D}_S^K(z) dz$$

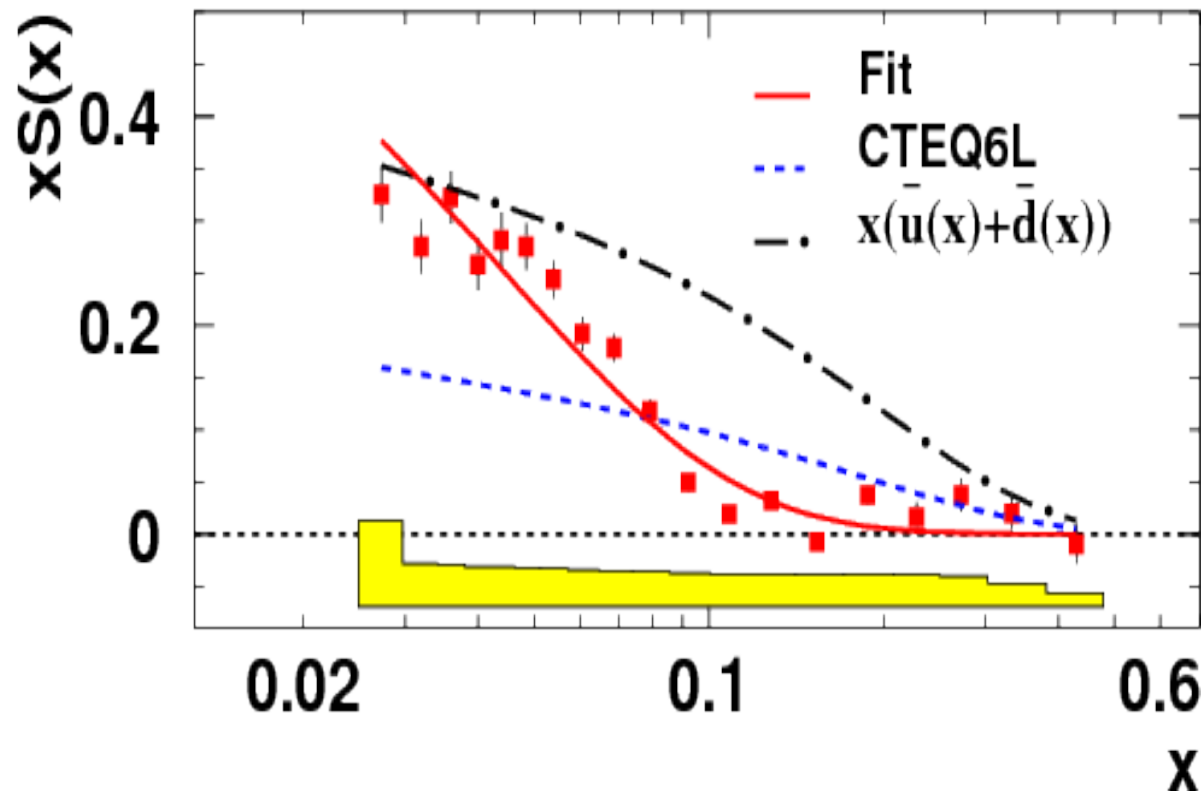
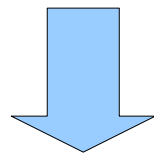


Spin-independent strange quark distribution

- evolution of data to $Q^2=2.5 \text{ GeV}^2$ (CTEQ6L)

- $\int_{0.2}^{0.8} \mathcal{D}_S^K(z) dz = 1.27 \pm 0.13$

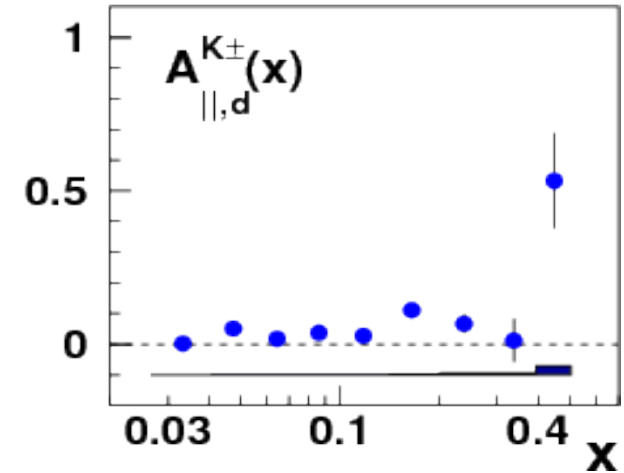
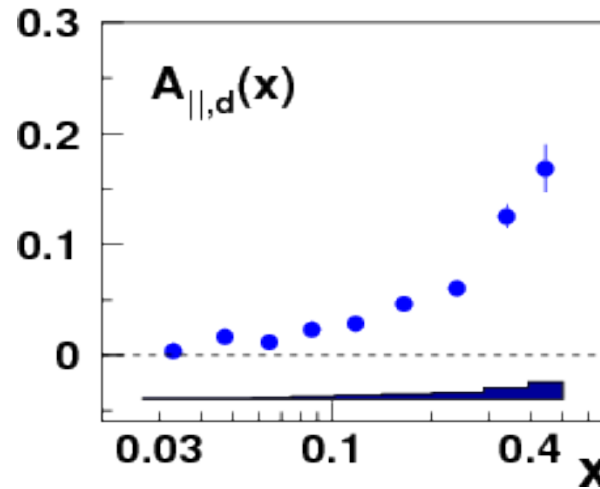
D. de Florian et al., PRD75, 114010



- discrepancy with CTEQ6L
- $S(x)$ not an average of isoscalar non-strange sea $S(x)$ towards lower x -values

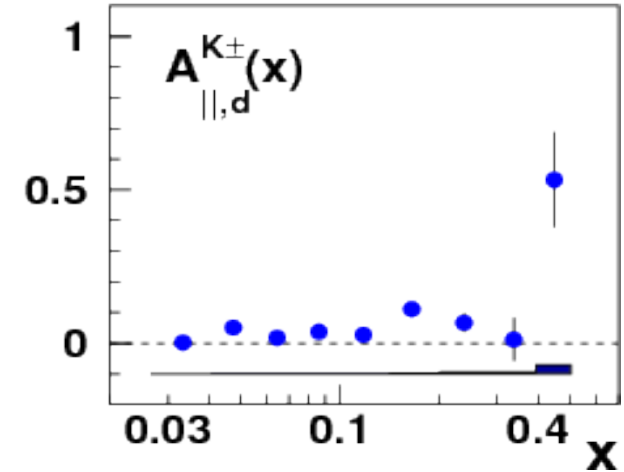
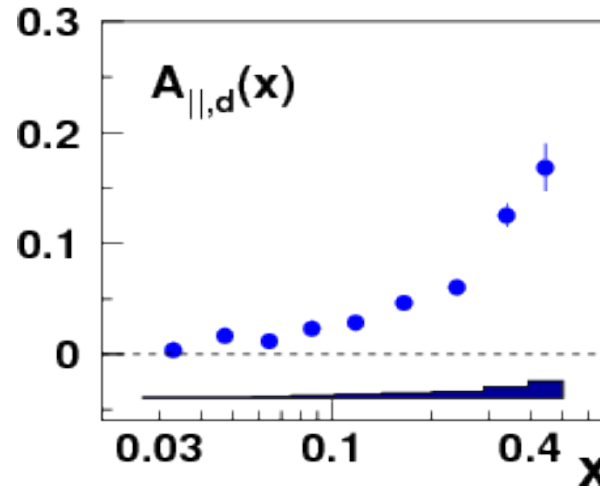
Double spin asymmetry from longitudinally polarized deuterons

$$A_{\parallel}^{(h)} = \frac{\sigma^{\leftarrow, (h)} - \sigma^{\rightarrow, (h)}}{\sigma^{\leftarrow, (h)} + \sigma^{\rightarrow, (h)}}$$



Double spin asymmetry from longitudinally polarized deuterons

$$A_{\parallel}^{(h)} = \frac{\sigma^{\leftarrow, (h)} - \sigma^{\rightarrow, (h)}}{\sigma^{\leftarrow, (h)} + \sigma^{\rightarrow, (h)}}$$



$$A_{\parallel, d}(x) \frac{d^2 N^{DIS}(x)}{dx dQ^2} = \mathcal{K}_{\mathcal{L}\mathcal{L}}(x, Q^2) [5\Delta Q(x) + 2\Delta S(x)]$$

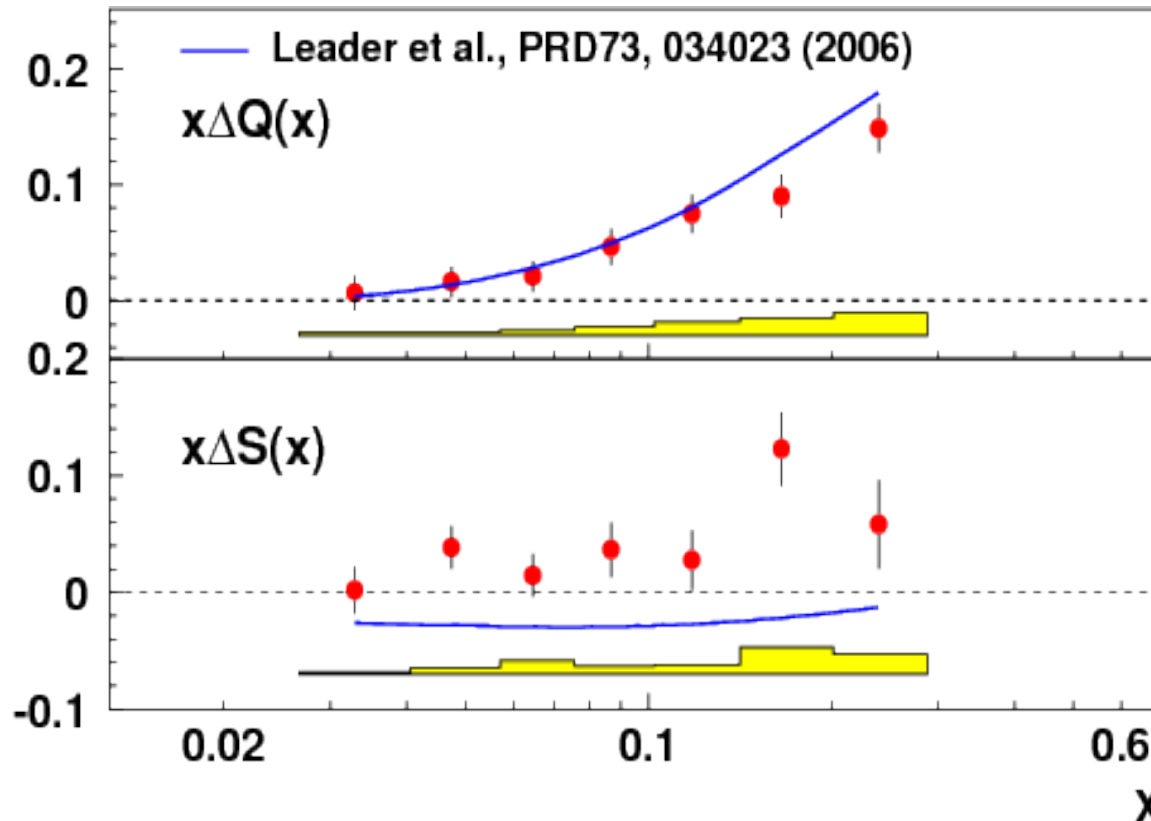
$$A_{\parallel, d}^{K^{\pm}}(x) \frac{d^2 N^K(x)}{dx dQ^2} = \mathcal{K}_{\mathcal{L}\mathcal{L}}(x, Q^2) \left[\Delta Q(x) \int_{0.2}^{0.8} \mathcal{D}_Q^K(z) dz + \Delta S(x) \int_{0.2}^{0.8} \mathcal{D}_S^K(z) dz \right]$$

$$\Delta Q(x) \equiv \Delta u(x) + \Delta \bar{u}(x) + \Delta d(x) + \Delta \bar{d}(x)$$

$$\Delta S(x) \equiv \Delta s(x) + \Delta \bar{s}(x)$$

$$\int_{0.2}^{0.8} \mathcal{D}_Q^K(z) dz, \int_{0.2}^{0.8} \mathcal{D}_S^K(z) dz \quad \text{from } S(x) \text{ extraction}$$

Helicity distribution @ $Q^2=2.5 \text{ GeV}^2$



- ΔQ and ΔS in agreement with previous HERMES results

- $\Delta q_8 = \int [\Delta Q(x) - 2\Delta S(x)] dx$ for $x: 0.02 \rightarrow 0.6$
 $= 0.285 \pm 0.046(\text{stat.}) \pm 0.057(\text{sys.})$

\neq

- Δq_8 from hyperon decay, assuming SU(3) symmetry ($x: 0 \rightarrow 1$)
 $= 0.586 \pm 0.031$

SU(3) symmetry violation \longleftrightarrow large contribution from $x < 0.02$ region

Transverse structure of the nucleon

Transverse structure of the nucleon

transverse momentum
dependent distributions

Transverse structure of the nucleon

transverse momentum
dependent distributions

transverse position:
generalized parton
distributions

Transverse momentum dependent distributions (TMDs)

$$\sigma^{ep \rightarrow eh} = \sum_q \mathcal{I} [DF^{p \rightarrow q}(x, k_T^2) \otimes \sigma^{eq \rightarrow eq} \otimes FF^{q \rightarrow h}(z, p_T^2)]$$

k_T / p_T = transverse momentum of struck/fragmenting quark

$\mathcal{I}[\dots]$ = convolution integral over k_T and p_T

Transverse momentum dependent distributions (TMDs)

$$\sigma^{ep \rightarrow eh} = \sum_q \mathcal{I} [DF^{p \rightarrow q}(x, k_T^2) \otimes \sigma^{eq \rightarrow eq} \otimes FF^{q \rightarrow h}(z, p_T^2)]$$

Distribution functions

q leading twist

Fragmentation functions

$f_1 = \text{yellow circle with blue center}$

$g_{1L} = \text{yellow circle with blue center and right arrow} - \text{yellow circle with blue center and left arrow}$

$h_{1T} = \text{yellow circle with blue center and up arrow} - \text{yellow circle with blue center and down arrow}$

$f_{1T}^\perp = \text{yellow circle with blue center and up arrow} - \text{yellow circle with blue center and down arrow}$

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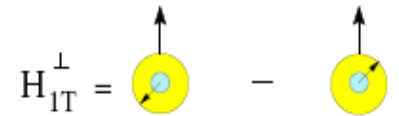
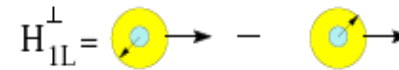
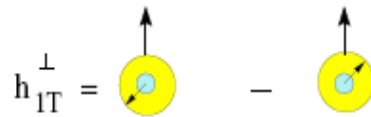
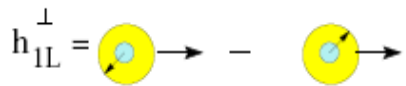
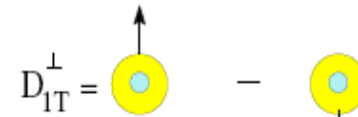
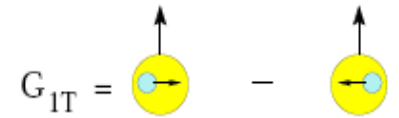
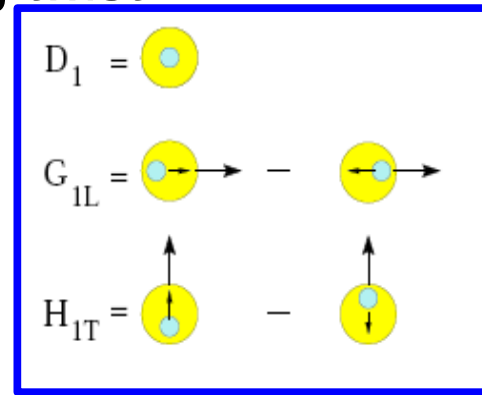
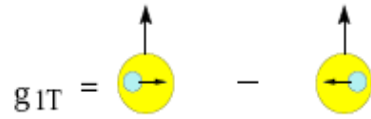
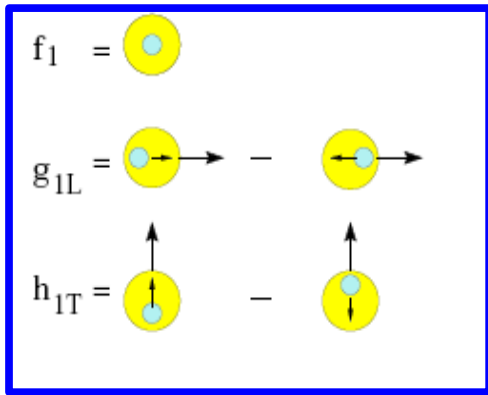
Transverse momentum dependent distributions (TMDs)

$$\sigma^{ep \rightarrow eh} = \sum_q \mathcal{I} [DF^{p \rightarrow q}(x, k_T^2) \otimes \sigma^{eq \rightarrow eq} \otimes FF^{q \rightarrow h}(z, p_T^2)]$$

Distribution functions

q leading twist

Fragmentation functions



only distributions that survive integration over transverse momentum

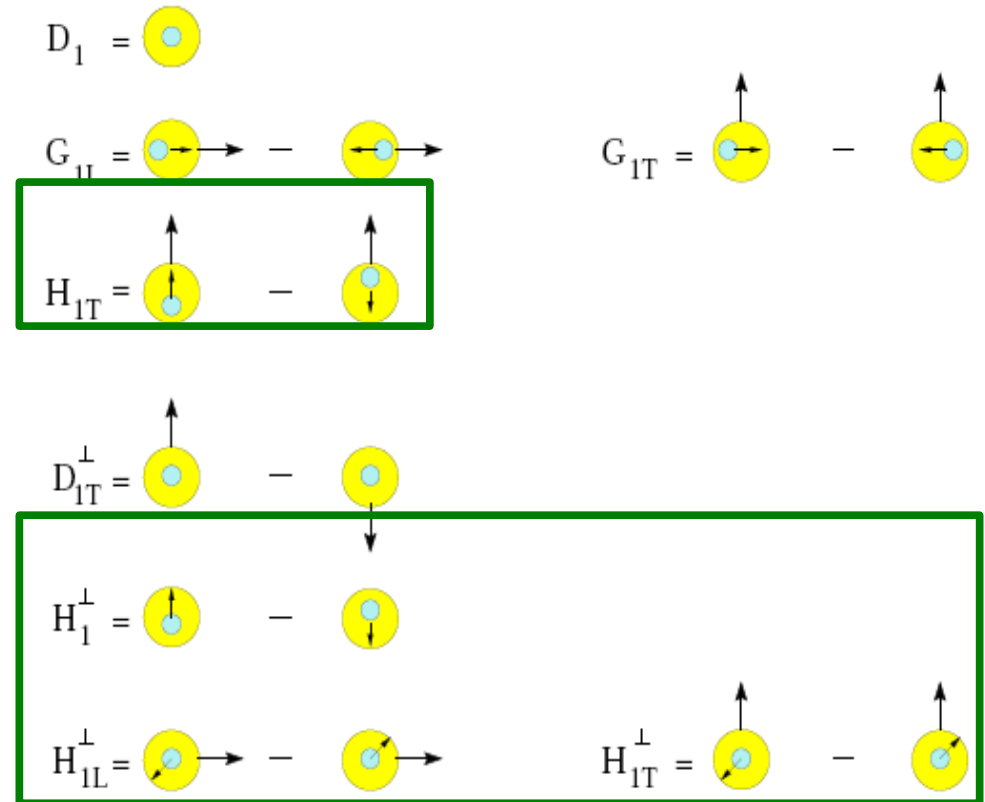
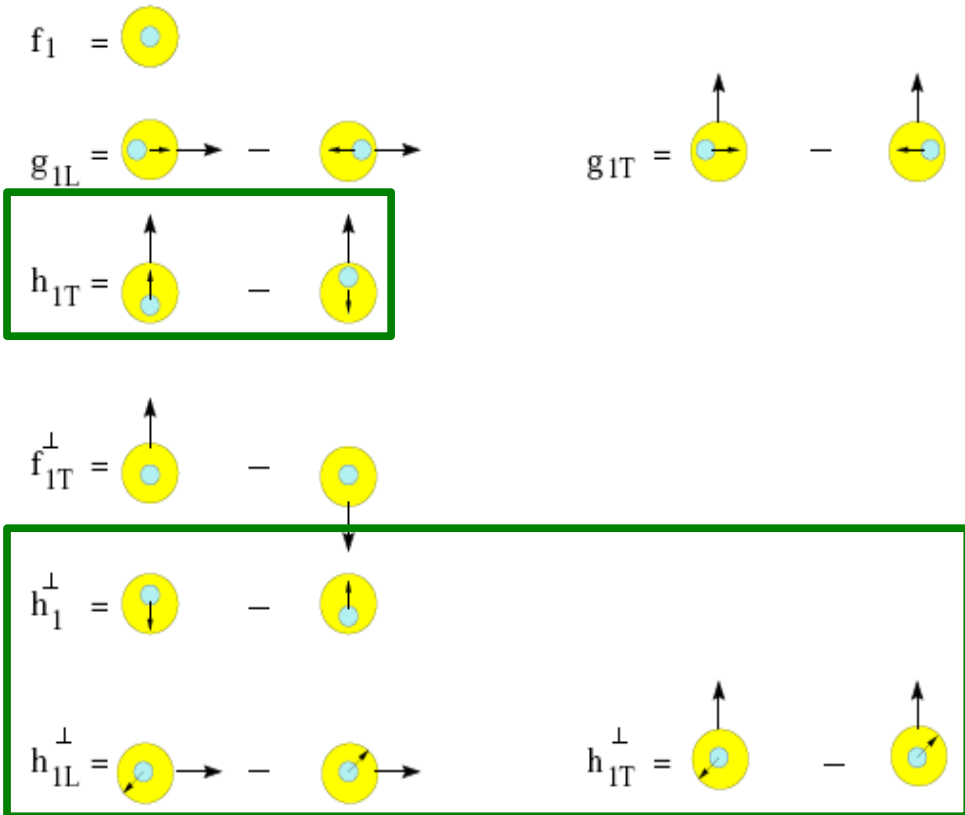
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Distribution functions

q leading twist

Fragmentation functions



Chiral odd: involve helicity flip of quark
appear in pairs in cross section

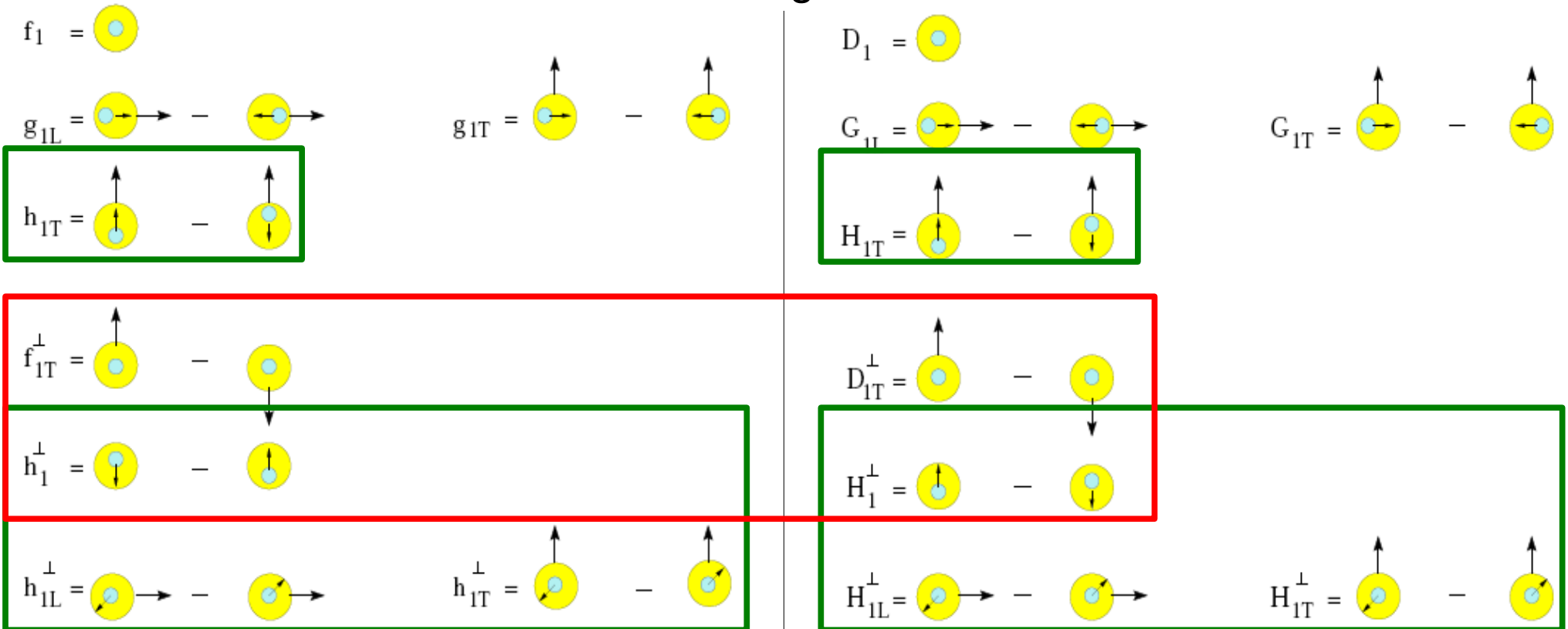
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Distribution functions

q leading twist

Fragmentation functions



Chiral odd: involve helicity flip of transversally polarized quark
appear in pairs in cross section

T-odd : appear in pairs in spin-independent x-section & double spin asymmetries
single in Single Spin Asymmetries (SSAs)

Transverse momentum dependent distributions (TMDs)

$$\sigma^{ep \rightarrow eh} = \sum_q \mathcal{I} [DF^{p \rightarrow q}(x, k_T^2) \otimes \sigma^{eq \rightarrow eq} \otimes FF^{q \rightarrow h}(z, p_T^2)]$$

Distribution functions

q leading twist

Fragmentation functions

$f_1 = \text{[diagram]}$

$g_{1L} = \text{[diagram]}$

$h_{1T} = \text{[diagram]}$

transversity

$f_{1T}^\perp = \text{[diagram]}$

$h_1^\perp = \text{[diagram]}$

$h_{1L}^\perp = \text{[diagram]}$

$g_{1T} = \text{[diagram]}$

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Distribution functions

q leading twist

Fragmentation functions

$f_1 = \text{[diagram: yellow circle with blue dot]}$

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transversity

$f_{1T}^\perp = \text{[diagram: two yellow circles with blue dots and vertical arrows pointing up and down, separated by a minus sign, enclosed in a red box]}$

Sivers

$h_1^\perp = \text{[diagram: two yellow circles with blue dots and vertical arrows pointing down and up, separated by a minus sign, enclosed in a green box]}$

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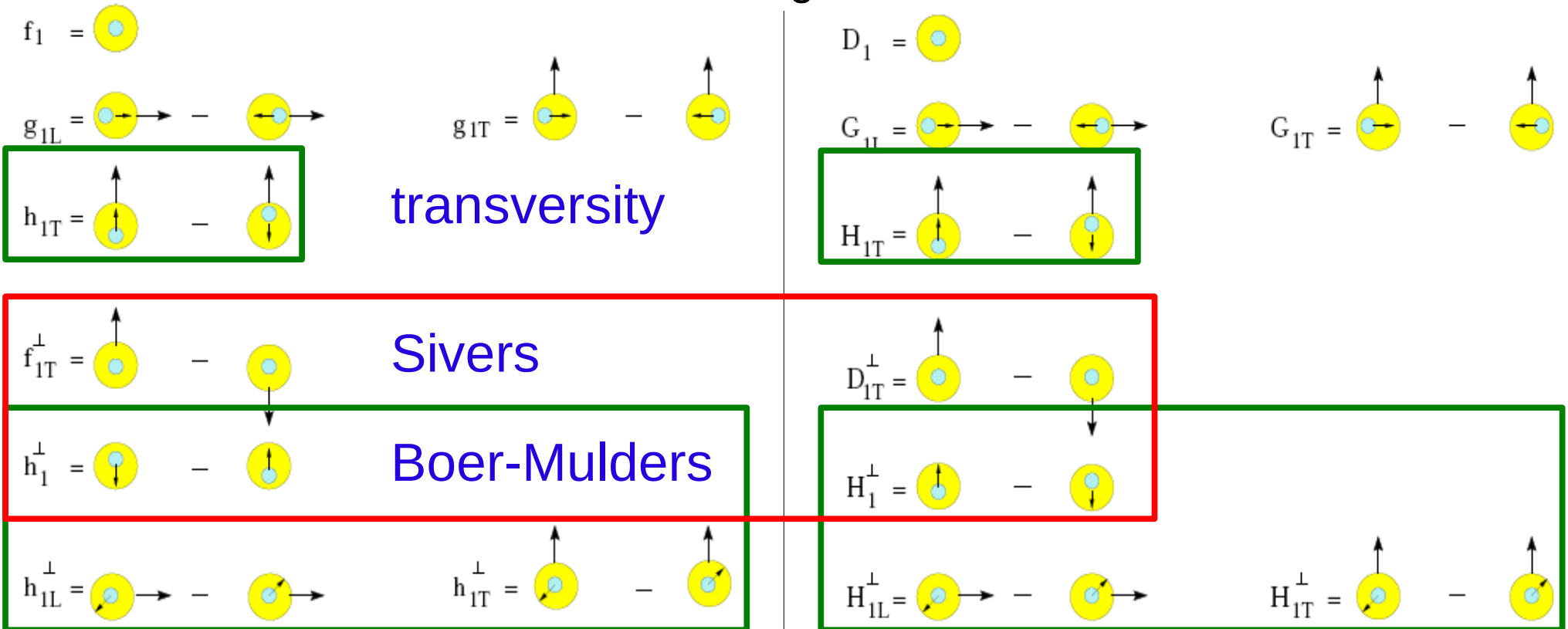
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Distribution functions

q leading twist

Fragmentation functions



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Transverse momentum dependent distributions (TMDs)

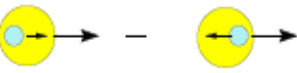
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Distribution functions

q leading twist


Fragmentation functions

$f_1 =$ 

$g_{1L} =$ 

$h_{1T} =$ 

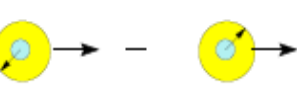
transversity

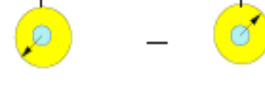
$f_{1T}^\perp =$ 


Sivers

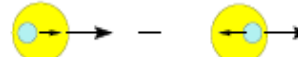
$h_1^\perp =$ 


Boer-Mulders


$h_{1L}^\perp =$ 


$h_{1T}^\perp =$ 


$D_1 =$ 

$G_{1L} =$ 

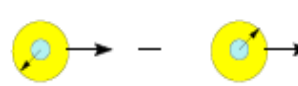
$H_{1T} =$ 

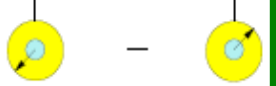
$G_{1T} =$ 

$D_{1T}^\perp =$ 

$H_1^\perp =$ 

Collins

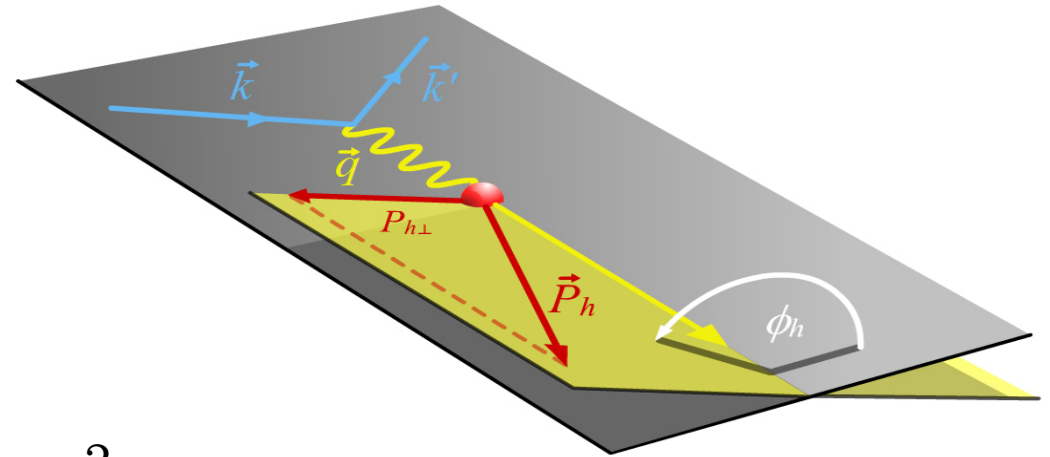
$H_{1L}^\perp =$ 

$H_{1T}^\perp =$ 

Chiral odd: involve helicity flip of transversally polarized quark
appear in pairs in cross section

T-odd : appear in pairs in spin-independent x-section & double spin asymmetries
single in Single Spin Asymmetries (SSAs)

Spin-independent SIDIS cross section

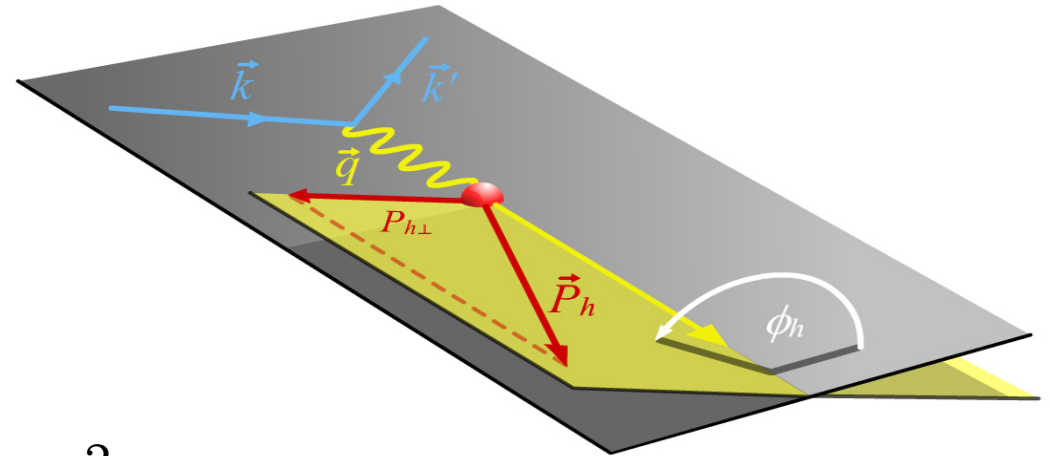


Non-collinear cross section

$$\frac{d\sigma}{dx dy dz dP_{h\perp}^2 d\phi_h} = \frac{\alpha^2}{xyQ^2} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ A(y) F_{UU,T} + B(y) F_{UU,L} \right. \\ \left. + C(y) \cos \phi_h F_{UU}^{\cos \phi_h} + B(y) \cos 2\phi_h F_{UU}^{\cos 2\phi_h} \right\}$$

$$\gamma = \frac{2Mx}{Q}, \quad F = F(x, Q, z, \vec{P}_{h\perp})$$

Spin-independent SIDIS cross section



Non-collinear cross section

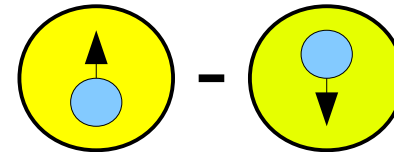
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leading twist term

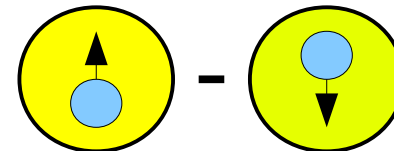
$$\gamma = \frac{2Mx}{Q}, \quad F = F(x, Q, z, \vec{P}_{h\perp})$$

$$F_{UU}^{\cos 2\phi_h} = \mathcal{I} \left[- \frac{2(\hat{P}_{h\perp} \cdot \vec{k}_T)(\hat{P}_{h\perp} \cdot \vec{p}_T) - \vec{k}_T \cdot \vec{p}_T}{M_h M} h_1^\perp H_1^\perp \right]$$

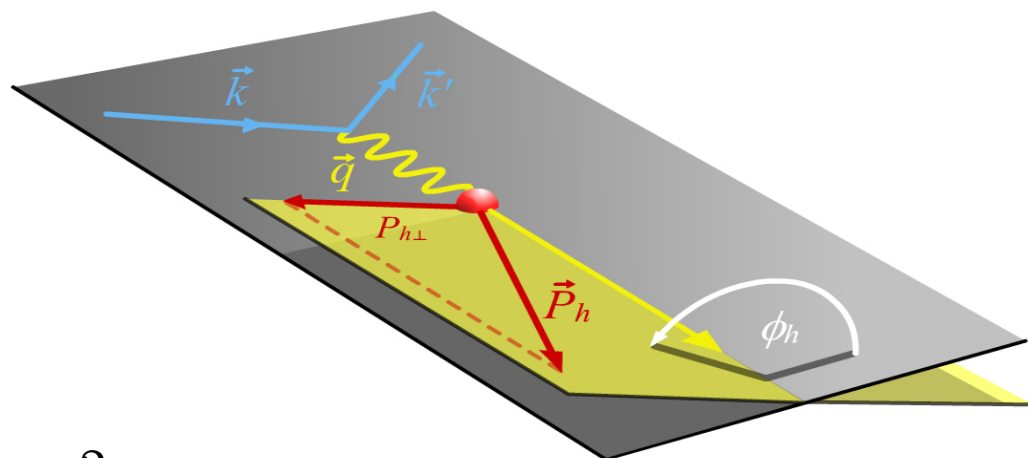
h_1^\perp = Boer-Mulders distribution function



H_1^\perp = Collins fragmentation function



Spin-independent SIDIS cross section



Non-collinear cross section

$$\frac{d\sigma}{dx dy dz dP_{h\perp}^2 d\phi_h} = \frac{\alpha^2}{xyQ^2} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ A(y) F_{UU,T} + B(y) F_{UU,L} \right. \\ \left. + C(y) \cos \phi_h F_{UU}^{\cos \phi_h} + B(y) \cos 2\phi_h F_{UU}^{\cos 2\phi_h} \right\}$$

sub-leading twist term

$$\gamma = \frac{2Mx}{Q}, \quad F = F(x, Q, z, \vec{P}_{h\perp})$$

$$F_{UU}^{\cos \phi_h} = \frac{2M}{Q} \mathcal{I} \left[-\frac{\hat{P}_{h\perp} \cdot \vec{k}_T}{M} f_1 D_1 - \frac{\hat{P}_{h\perp} \cdot \vec{p}_T}{M_h} \frac{k_T^2}{M^2} h_1^\perp H_1^\perp + \dots \right]$$

Cahn effect

quark-gluon-quark correlations


Extraction of the cosine moments

$$\langle \cos(n\phi_h) \rangle \stackrel{th.}{=} \frac{\int d\phi_h \cos(n\phi_h) \sigma_{UU}(x, y, z, P_{h\perp}^2, \phi_h)}{\int d\phi_h \sigma_{UU}(x, y, z, P_{h\perp}^2, \phi_h)}$$

\updownarrow

$$\langle \cos(n\phi_h) \rangle \stackrel{exp.}{=} \frac{\int d\phi_h \cos(n\phi_h) \epsilon_{acc}(\phi_h) \epsilon_{rad}(\phi_h) \sigma_{UU}(x, y, z, P_{h\perp}^2, \phi_h)}{\int d\phi_h \epsilon_{acc}(\phi_h) \epsilon_{rad}(\phi_h) \sigma_{UU}(x, y, z, P_{h\perp}^2, \phi_h)}$$

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Extraction is challenging!

Azimuthal modulations also possible due to

- detector geometrical acceptance
- higher-order QED effects

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fully differential analysis needed
unfolding procedure with 400 x 12 bins *

BINNING

400 kinematic bins x 12 ϕ -bins

Variable	Bin limits						#
x	0.023	0.042	0.078	0.145	0.27	1	5
y	0.3	0.45	0.6	0.7	0.85		4
z	0.2	0.3	0.45	0.6	0.75	1	5
P_{hT}	0.05	0.2	0.35	0.5	0.75		4

(*)see F. Giordano,
Proceedings of Transversity 2008 Workshop,
May 28-31 2008, Ferrara, Italy,
to be published by World Scientific

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$$\langle \cos(n\phi_h) \rangle \Big|_{\text{bin } i} \approx \frac{\int d\phi_h \cos(n\phi_h) \sigma_{UU}(x, y, z, P_{h\perp}^2, \phi_h) \Big|_{\text{bin } i}}{\int d\phi_h \sigma_{UU}(x, y, z, P_{h\perp}^2, \phi_h) \Big|_{\text{bin } i}}$$

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Extraction of the cosine moments

$$\langle \cos(n\phi_h) \rangle \stackrel{th.}{=} \frac{\int d\phi_h \cos(n\phi_h) \sigma_{UU}(x, y, z, P_{h\perp}^2, \phi_h)}{\int d\phi_h \sigma_{UU}(x, y, z, P_{h\perp}^2, \phi_h)}$$

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Extraction is challenging!
 Azimuthal modulations also possible due to

- detector geometrical acceptance
- higher-order QED effects

fully differential analysis needed
 unfolding procedure with 400 x 12 bins *

BINNING
 kinematic bins x 12 ϕ -bins

Variable	Bin limits						#
x	0.023	0.042	0.078	0.145	0.27	1	5
y	0.3	0.45	0.6	0.7	0.85		4
z	0.2	0.3	0.45	0.6	0.75	1	5
P_{hT}	0.05	0.2	0.35	0.5	0.75		4

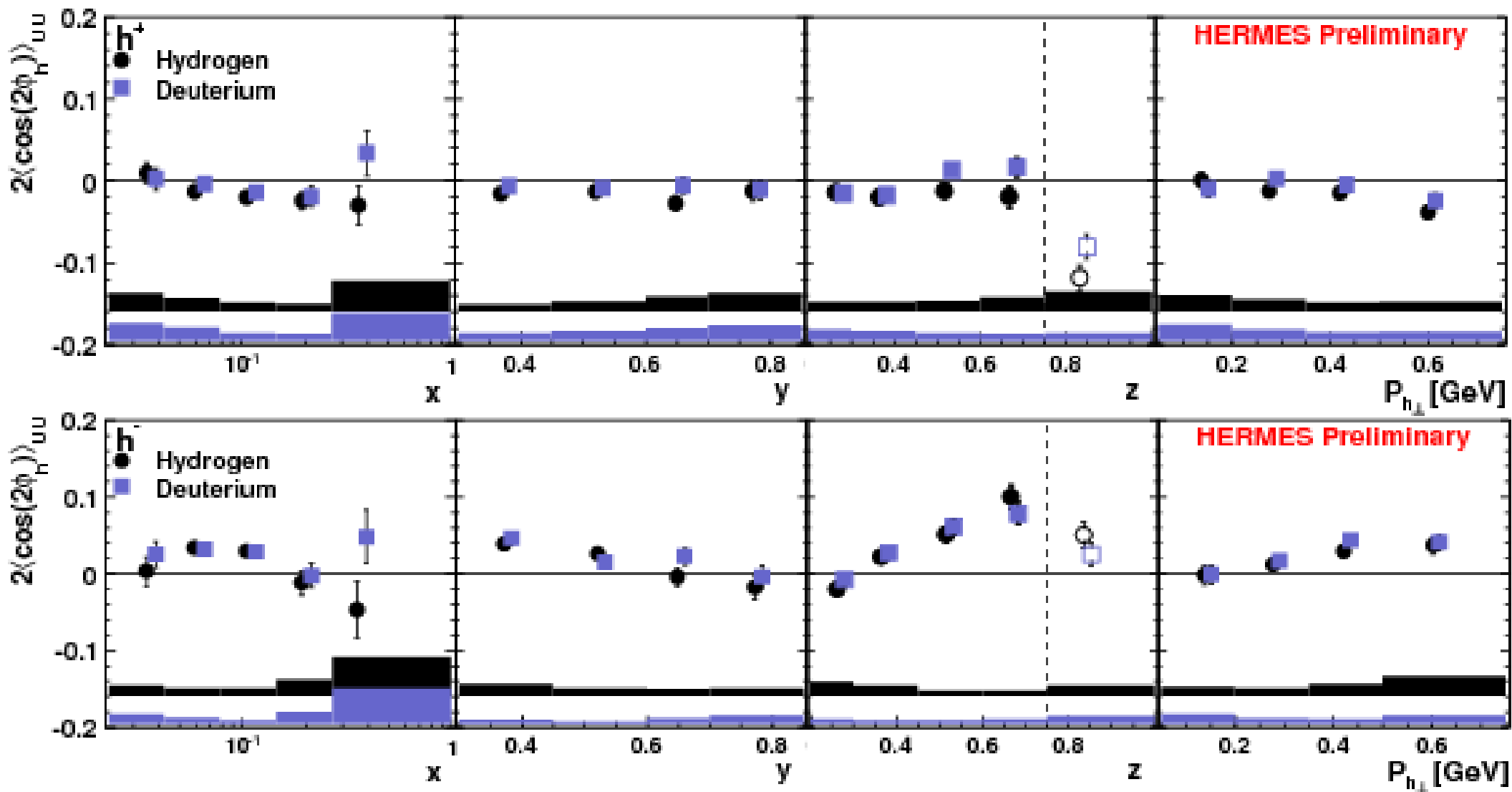
more on unfolding, see F. Giordano (HK81)

unfolding

$$\langle \cos(n\phi_h) \rangle \Big|_{\text{bin } i} \approx \frac{\int d\phi_h \cos(n\phi_h) \sigma_{UU}(x, y, z, P_{h\perp}^2, \phi_h) \Big|_{\text{bin } i}}{\int d\phi_h \sigma_{UU}(x, y, z, P_{h\perp}^2, \phi_h) \Big|_{\text{bin } i}}$$

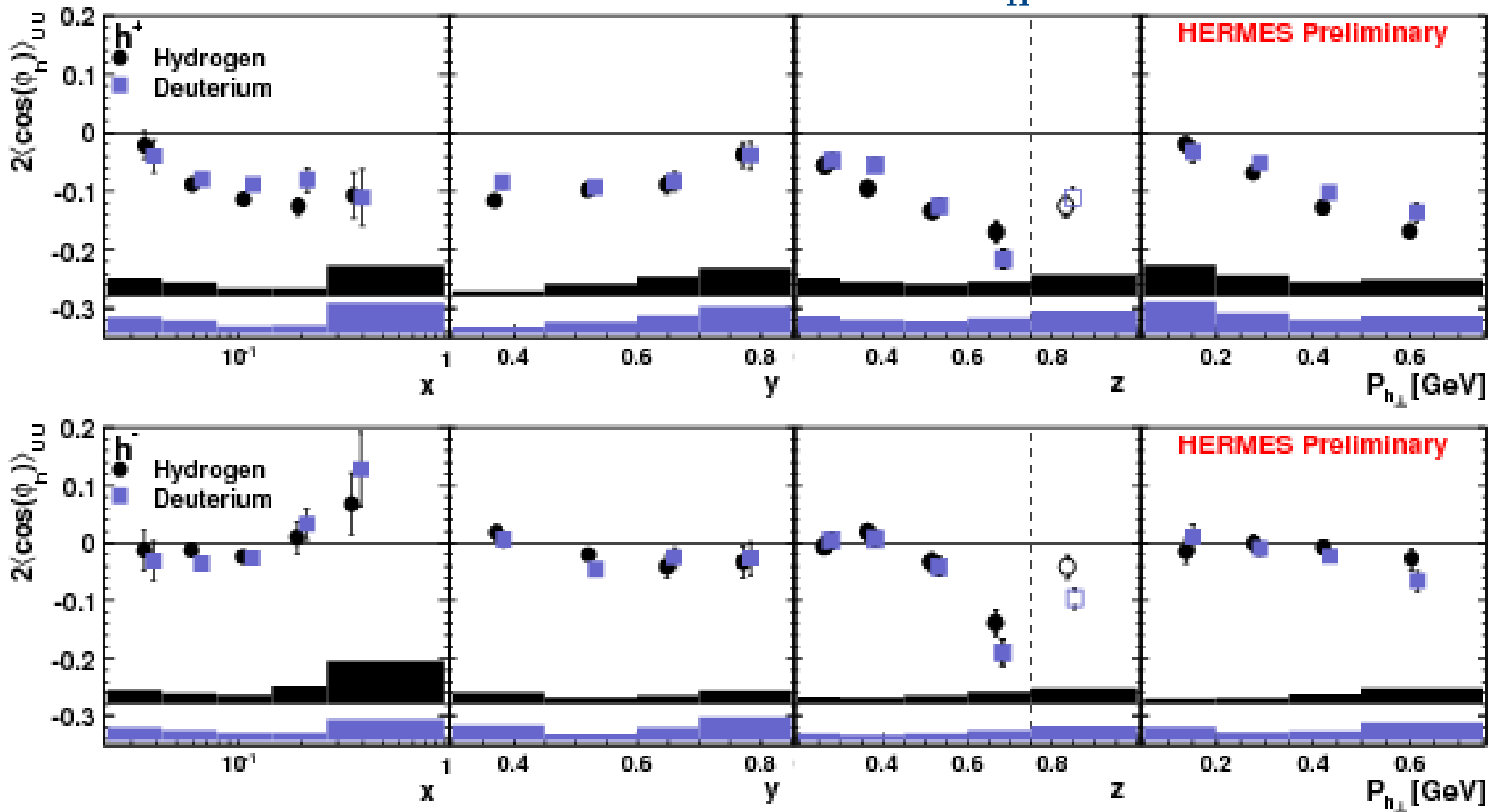
(*)see F. Giordano,
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Results for $\langle \cos 2\phi_h \rangle$



- evidence for transversely polarized quarks in unpolarized nucleon!
- h^+ and h^- : opposite sign in agreement with models

Results for $\langle \cos \phi_h \rangle$



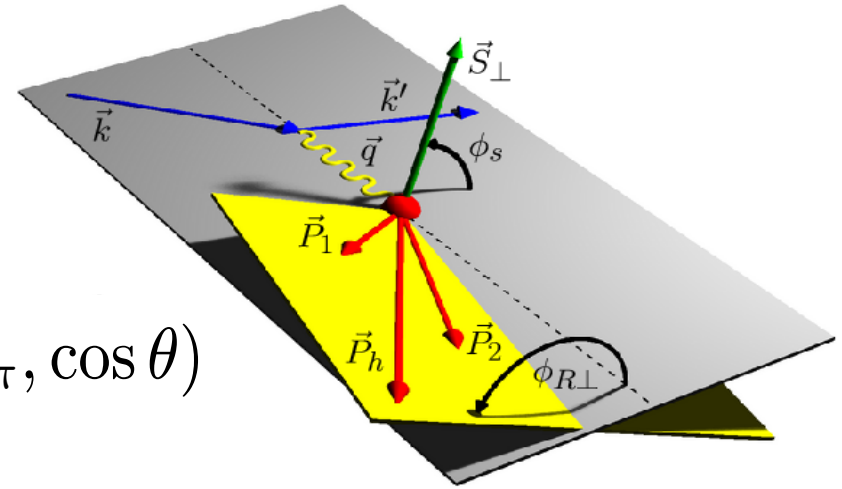
- predictions for Cahn effect: negative for h^+ and h^-
- \rightarrow also other effects have to be taken into account

Single Spin Asymmetries

$$A_{UT} = \frac{1}{\langle |S_T| \rangle} \frac{N^\uparrow(\phi, \phi_S) - N^\downarrow(\phi, \phi_S)}{N^\uparrow(\phi, \phi_S) + N^\downarrow(\phi, \phi_S)}$$

2-hadron production

$$\sim \sin(\phi_{R\perp} + \phi_S) \sum_q e_q^2 h_{1T}^q(x) H_1^{\perp,q}(z, M_{\pi\pi}, \cos\theta)$$



h_{1T} : transversity

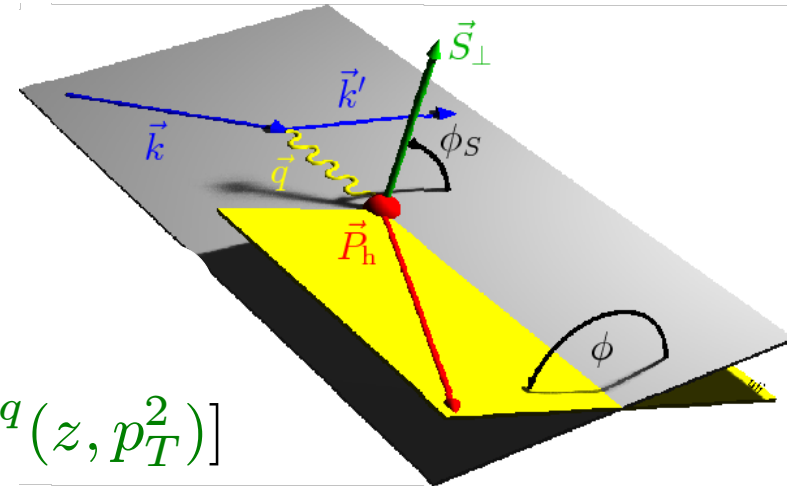
H_1^\perp : Collins fragmentation function

f_{1T}^\perp : Sivers distribution function

1-hadron production

$$\sim \sin(\phi + \phi_S) \sum_q e_q \mathcal{I} \left[\frac{\vec{p}_T \cdot \hat{P}_{h\perp}}{M_h} h_{1T}^q(x, k_T^2) \otimes H_1^{\perp,q}(z, p_T^2) \right]$$

$$+ \sin(\phi - \phi_S) \sum_q e_q \mathcal{I} \left[\frac{\vec{k}_T \cdot \hat{P}_{h\perp}}{M_h} f_{1T}^{\perp,q}(x, k_T^2) \otimes D_1^q(z, p_T^2) \right]$$



Single Spin Asymmetries

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h_{1T} : transversity

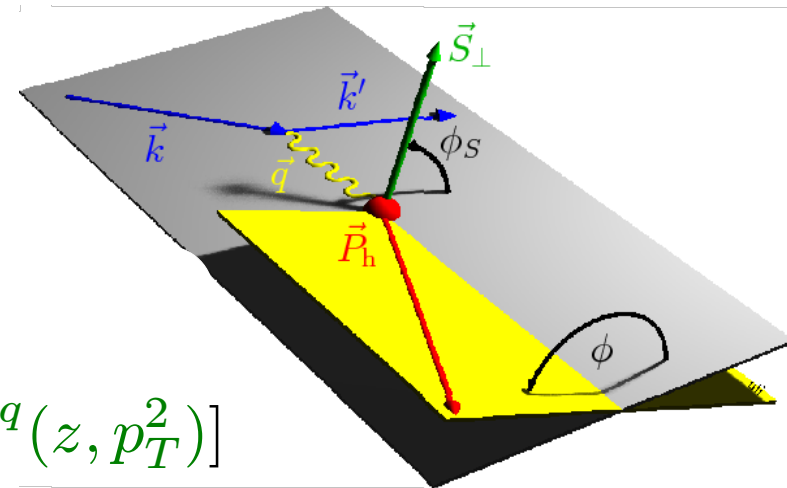
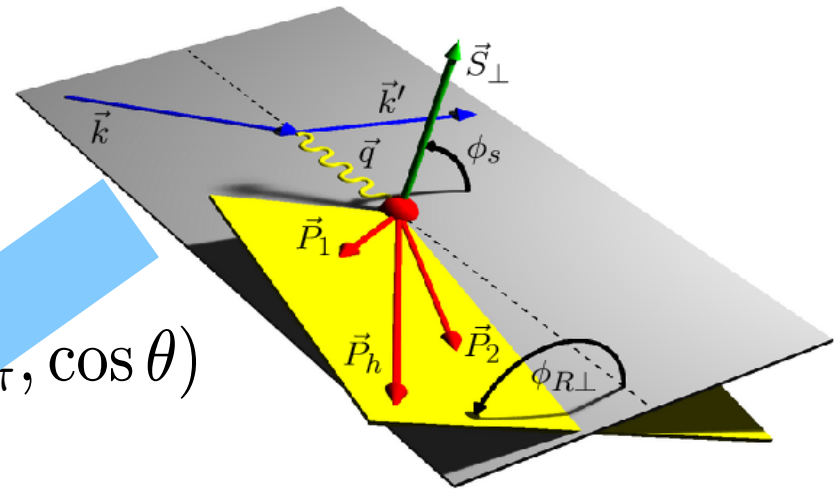
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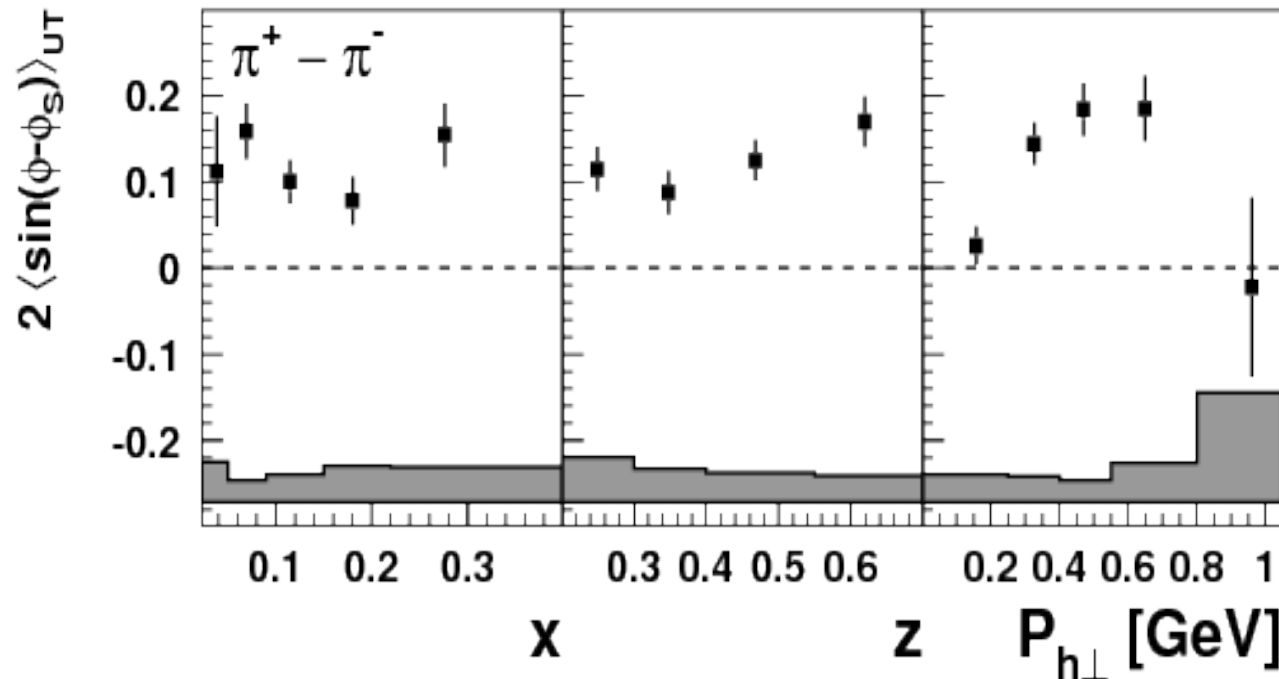
see talk by M. Dieffenthaler

Sivers distribution for valence quarks

$$A_{UT}^{\pi^+ - \pi^-} = \frac{1}{\langle |S_T| \rangle} \frac{(\sigma_{U\uparrow}^{\pi^+} - \sigma_{U\uparrow}^{\pi^-}) - (\sigma_{U\downarrow}^{\pi^+} - \sigma_{U\downarrow}^{\pi^-})}{(\sigma_{U\uparrow}^{\pi^+} - \sigma_{U\uparrow}^{\pi^-}) + (\sigma_{U\downarrow}^{\pi^+} - \sigma_{U\downarrow}^{\pi^-})}$$

$$\longrightarrow \langle \sin(\phi - \phi_S) \rangle_{UT}^{\pi^+ - \pi^-} = - \frac{4f_{1T}^{\perp, u_v} - f_{1T}^{\perp, d_v}}{4f_1^{u_v} - f_1^{d_v}}$$

HERMES PRELIMINARY 2002-2005
lepton beam amplitudes, 8.1% scale uncertainty



- Sivers distribution for d-valence \gg u-valence
or
- Sivers distribution for u-valence is large & < 0
(more likely)

Generalized parton distributions
and
Deeply virtual Compton scattering

Spin decomposition of the nucleon

X. Ji, *Phys. Rev. Lett.* **78**, 610-613 (1997)

$$\frac{1}{2} = \sum_q J^q + J^g = \frac{1}{2} \Delta\Sigma + \sum_q L^q + J^g$$

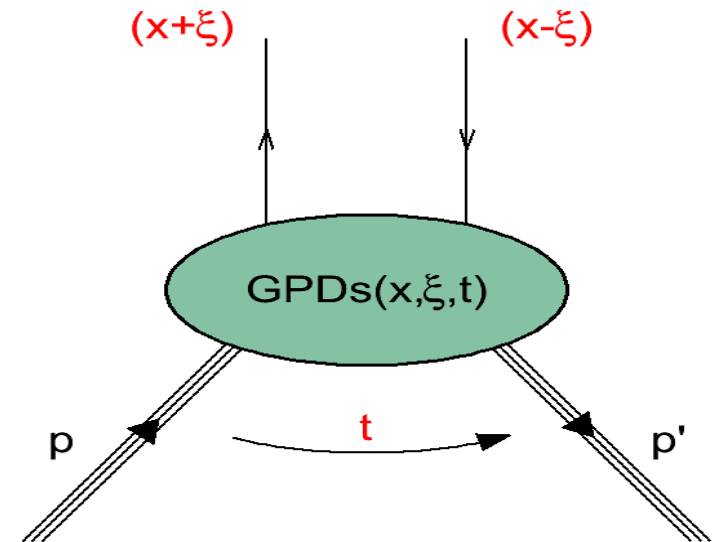
$$J^q = \lim_{t \rightarrow 0} \frac{1}{2} \int_{-1}^1 dx x [H^q(x, \xi, t) + E^q(x, \xi, t)]$$

possibility to access quark orbital angular momentum

Generalized Parton Distributions (GPDs)

- 4 twist-2 quark helicity conserving GPDs:

$$H^q, \tilde{H}^q, E^q, \tilde{E}^q$$



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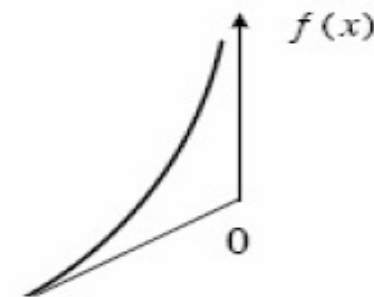
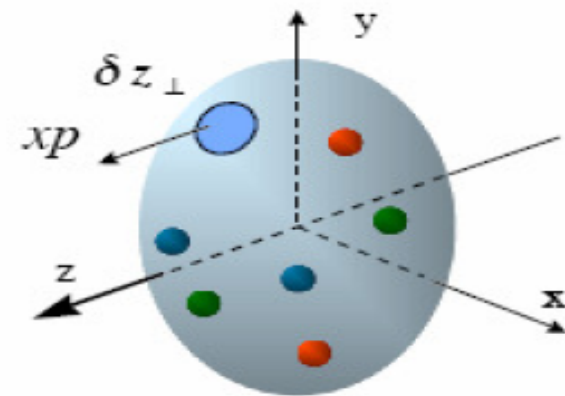
- 4 twist-2 quark helicity conserving GPDs:

$$H^q, \tilde{H}^q, E^q, \tilde{E}^q$$

- forward limit \rightarrow parton distribution functions

$$H^q(x, 0, 0) = q(x)$$

$$\tilde{H}^q(x, 0, 0) = \Delta q(x)$$



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X. Ji, *Phys. Rev. Lett.* **78**, 610-613 (1997)

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Generalized Parton Distributions (GPDs)

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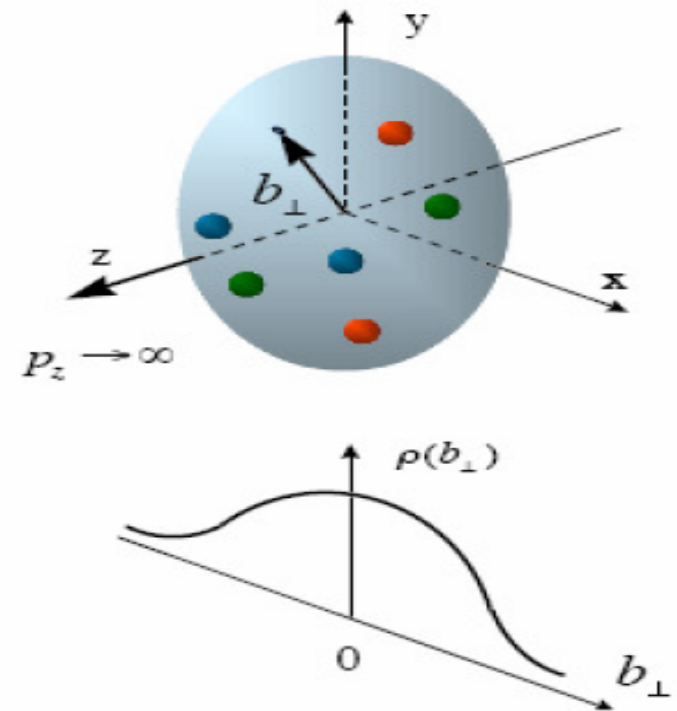
$$H^q, \tilde{H}^q, E^q, \tilde{E}^q$$

- forward limit \rightarrow parton distribution functions

- moments \rightarrow form factors

$$\int_{-1}^1 dx H^q(x, \xi, t) = F_1^q(t)$$

■
■
■



Spin decomposition of the nucleon

X. Ji, *Phys. Rev. Lett.* **78**, 610-613 (1997)

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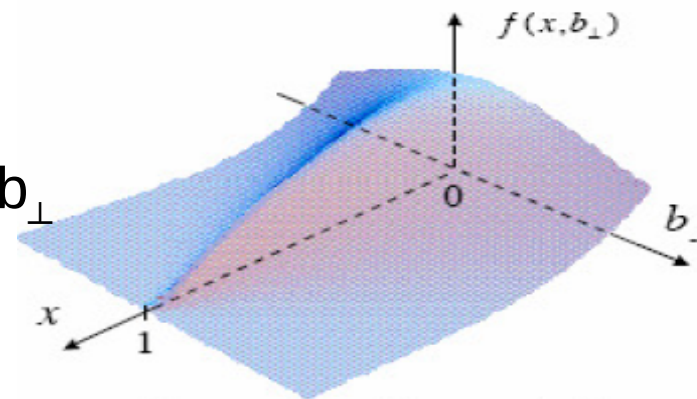
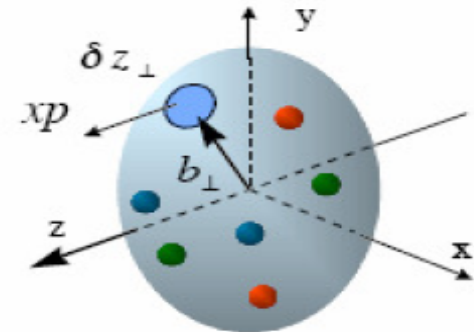
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Generalized Parton Distributions (GPDs)

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- moments \rightarrow form factors
- probability to find quark with longitudinal momentum fraction x at transverse location b_\perp



Spin decomposition of the nucleon

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$$\frac{1}{2} = \sum_q J^q + J^g = \frac{1}{2} \Delta\Sigma + \sum_q L^q + J^g$$

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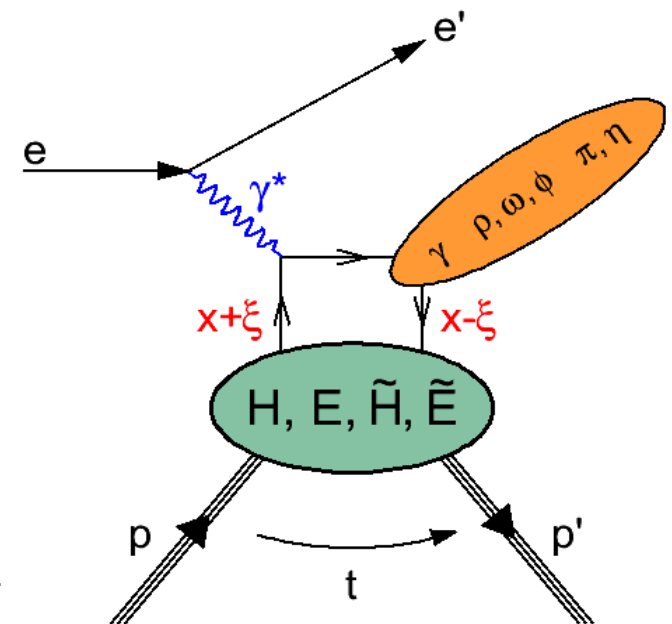
→ possibility to access quark orbital angular momentum

Generalized Parton Distributions (GPDs)

- 4 twist-2 quark helicity conserving GPDs:

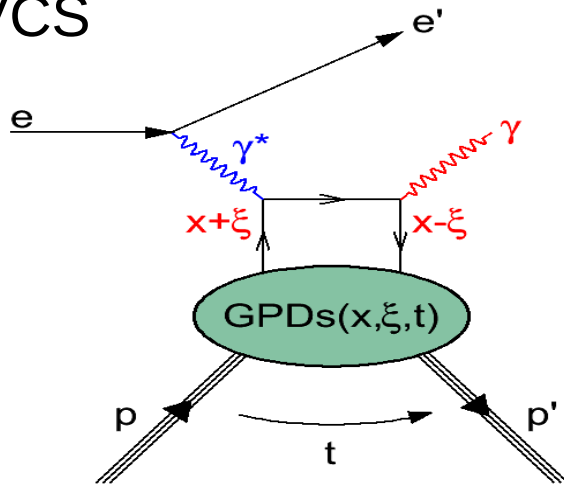
$$H^q, \tilde{H}^q, E^q, \tilde{E}^q$$

- forward limit → parton distribution functions
- moments → form factors
- probability to find quark with longitudinal momentum fraction x at transverse location b_{\perp}
- access via exclusive meson production and deeply virtual Compton scattering

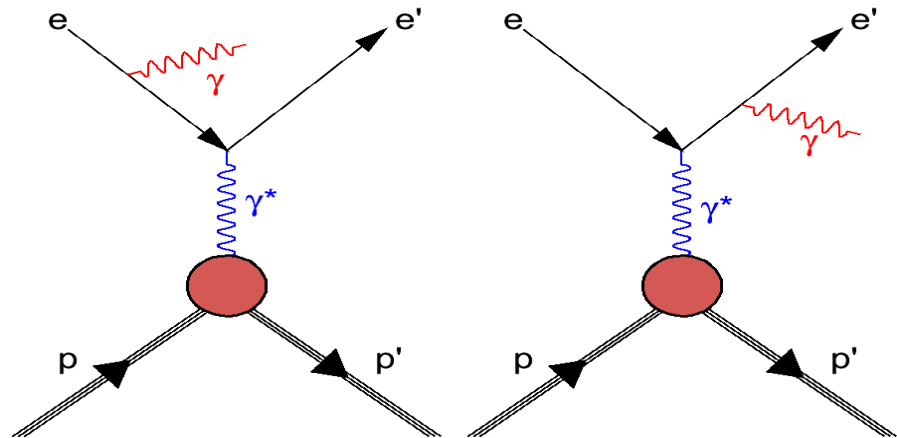


Deeply virtual Compton scattering

DVCS



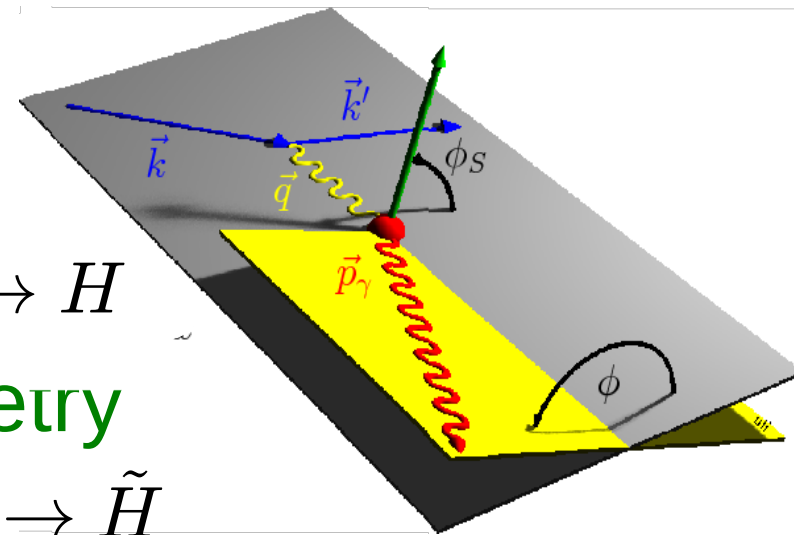
Bethe-Heitler



$$d\sigma \sim |T_{DVCS}|^2 + |T_{BH}|^2 + \underbrace{T_{BH}T_{DVCS}^* + T_{BH}^*T_{DVCS}}_{\text{interference term}}$$

- theoretically cleanest process to access GPDs
- DVCS and BH: indistinguishable \rightarrow interference
- $T_{BH} \gg T_{DVCS}$
- T_{BH} : calculable (form factors)
- access interference term by measuring azimuthal asymmetries

Azimuthal asymmetries



- **Beam-spin asymmetry**

$$d\sigma(\vec{e}, \phi) - d\sigma(\overleftarrow{e}, \phi) \sim \Im[F_1 \mathcal{H}] \sin \phi \rightarrow H$$

- **Longitudinal target-spin asymmetry**

$$d\sigma(\vec{P}, \phi) - d\sigma(\overleftarrow{P}, \phi) \sim \Im[F_1 \tilde{\mathcal{H}}] \sin \phi \rightarrow \tilde{H}$$

- **Beam-charge asymmetry**

$$d\sigma(e^+, \phi) - d\sigma(e^-, \phi) \sim \Re[F_1 \mathcal{H}] \cos \phi \rightarrow H$$

- **Transverse target-spin asymmetry**

$$d\sigma(\phi, \phi_S) - d\sigma(\phi, \phi_S + \pi) \sim$$

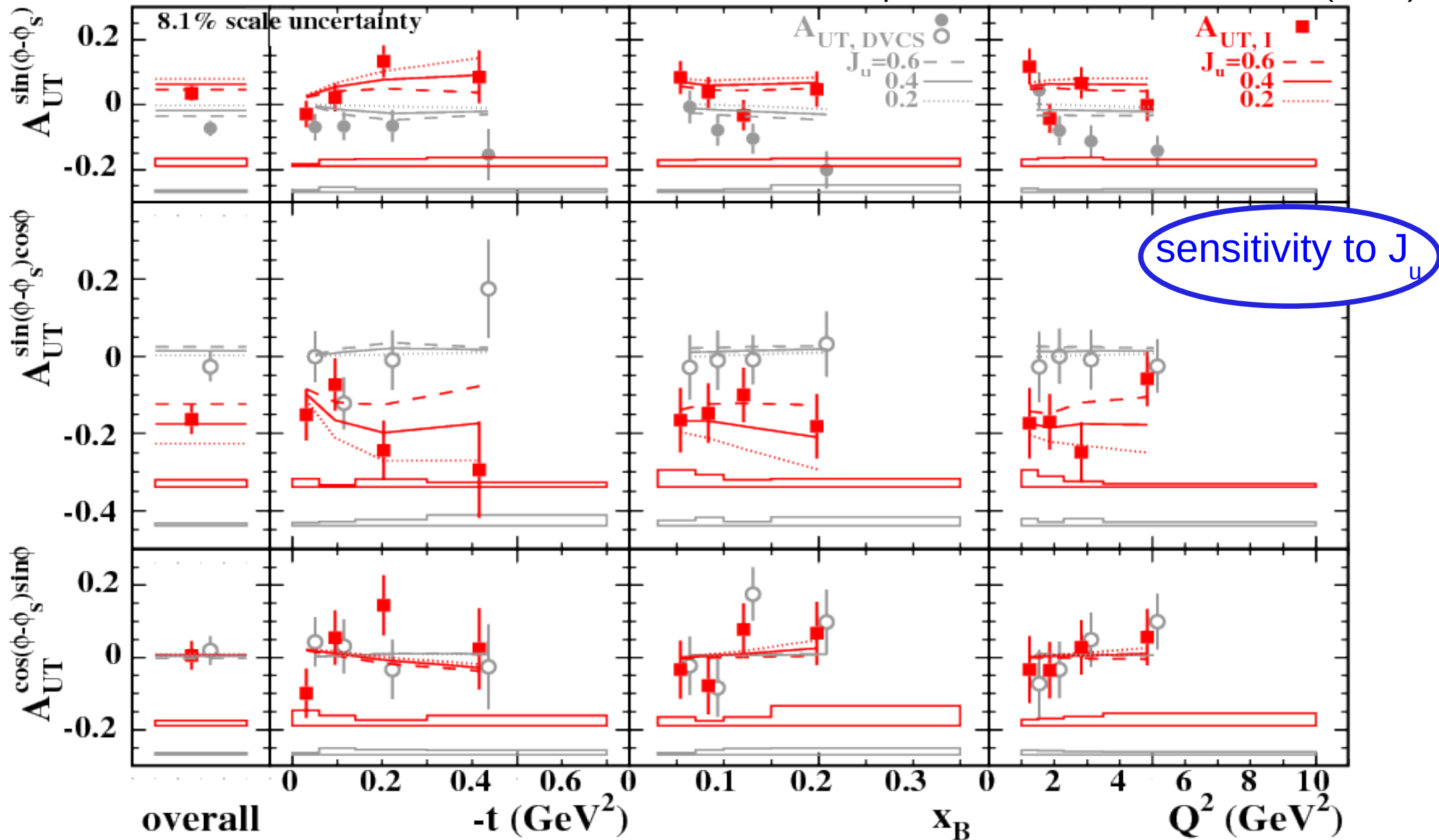
$$\Im[F_2 \mathcal{H} - F_1 \mathcal{E}] \sin(\phi - \phi_S) \cos \phi \quad \longrightarrow \quad \text{only access to } E!$$

$$\Im[F_2 \tilde{\mathcal{H}} - F_1 \xi \tilde{\mathcal{E}}] \cos(\phi - \phi_S) \sin \phi$$

$\mathcal{H}, \mathcal{E}, \tilde{\mathcal{H}}, \tilde{\mathcal{E}}$: Compton form factors

Transverse target-spin asymmetry

A. Airapetian et al., JHEP **0806**, 066 (2008)

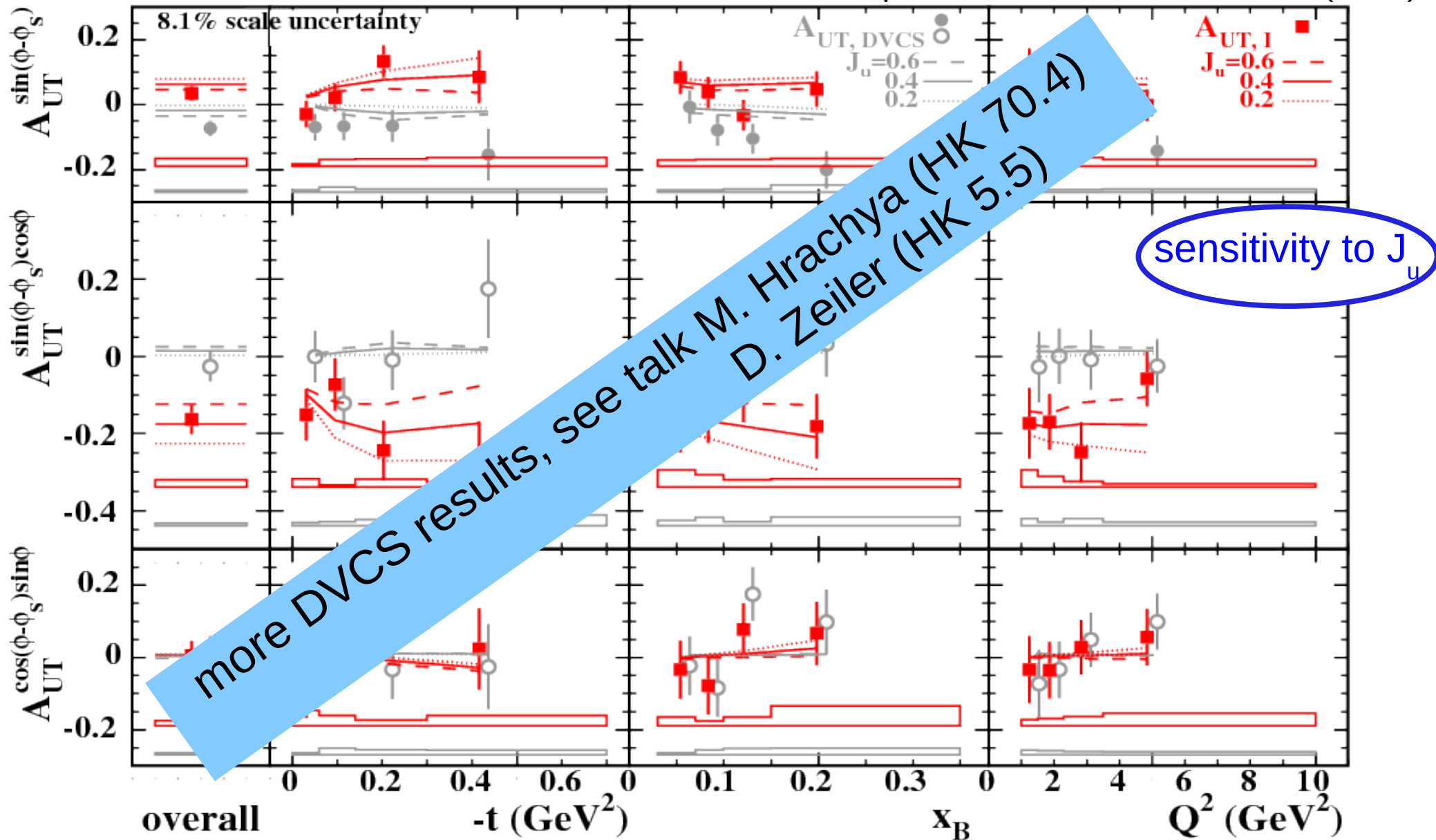


VGG model: Phys. Rev. D60, 094017 (1999)

Prog. Part. Nucl. Phys. 47, 401 (2001)

Transverse target-spin asymmetry

A. Airapetian et al., JHEP **0806**, 066 (2008)



VGG model: Phys. Rev. D60, 094017 (1999)

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Summary

- strange quark distributions
 - SU(3) symmetry appears to be violated
 - $S(x)$ much softer than light isoscalar
 - $\Delta S(x)$ consistent with 0
- accounting for transverse momentum of parton \rightarrow
azimuthal dependence of unpolarized cross-section
Boer-Mulders effect: non zero!
- Sivers distribution for valence quarks:
likely, large and negative for u_v
- generalized parton distributions \rightarrow
access to quark orbital angular momentum:
transverse target-spin asymmetry sensitive to J_u

