

# Recent results from HERMES

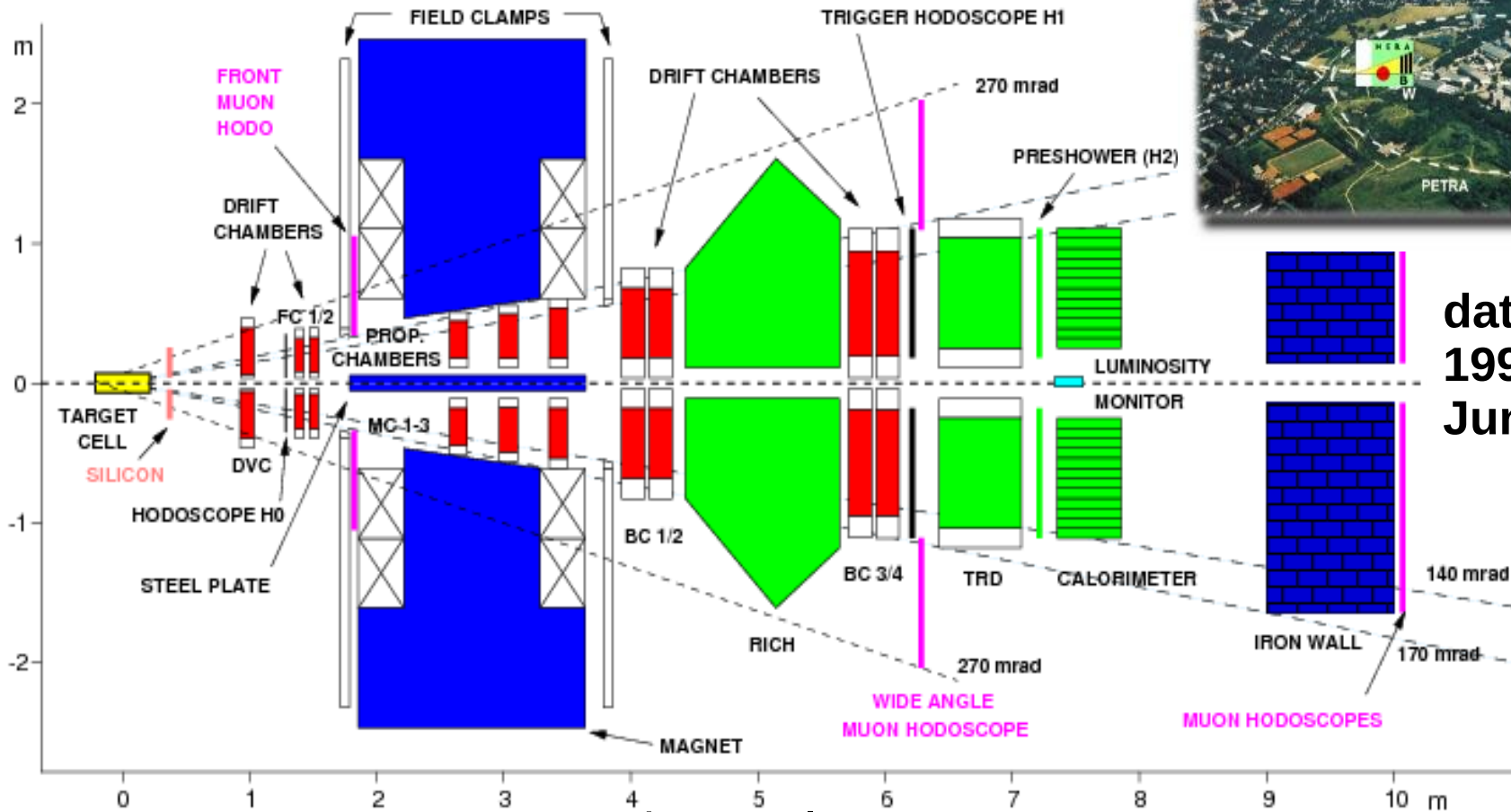
Charlotte Van Hulse, on behalf of the HERMES collaboration  
University of the Basque Country – UPV/EHU



# Outline

- the HERMES experiment
- the proton in 3D: Generalized parton distributions
- Single-helicity asymmetries in DVCS
  - complete data set, through missing mass reconstruction
  - kinematically complete event reconstruction
- the proton in 3D: transverse-momentum-dependent parton distributions
- single-spin asymmetries in SIDIS off transversely polarized protons
  - Sivers distribution function
  - transversity and Collins fragmentation function
- spin-independent non-collinear cross section
  - Boer-Mulders-Collins amplitude

# HERMES: HERA MEasurement of Spin



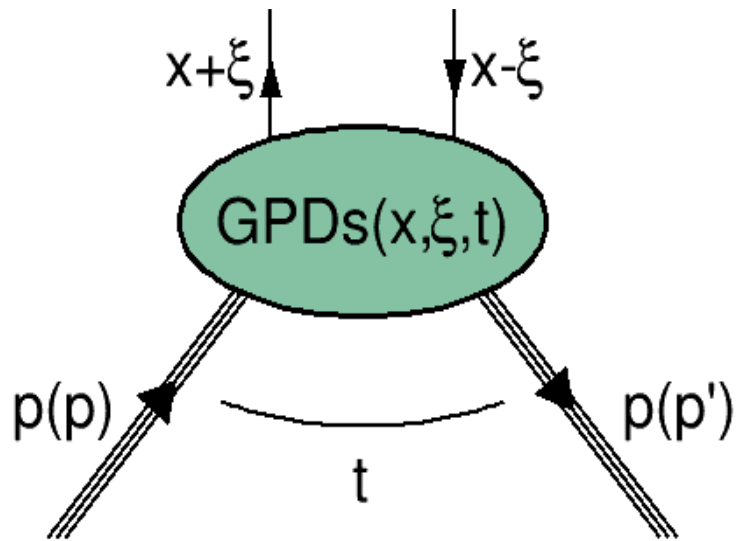
data taking from  
1995 until  
June, 30 2007

Beam  
longitudinally pol.  
 $e^+$  &  $e^-$   
 $E = 27.6$  GeV

Gaseous internal target  
transversely pol. H (~75%)  
unpol. H, D, He, Ne, Kr, Xe  
longitudinally pol. H, D, He (~85%)

- lepton-hadron PID: high efficiency (>98%) & low contamination (<1%)
- hadron PID: RICH 2-15 GeV

# Generalized Parton Distributions (GPDs)



- $x$ =average longitudinal momentum fraction
- $2\xi$ =average longitudinal momentum transfer
- $t$ = squared momentum transfer to nucleon

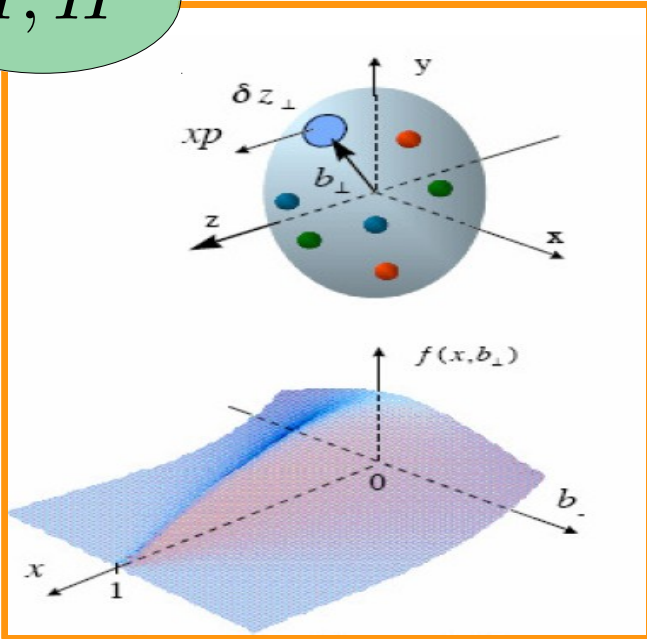
Four quark helicity-conserving GPDs at twist-2

$H^q(x, \xi, t)$	$E^q(x, \xi, t)$	spin independent
$\tilde{H}^q(x, \xi, t)$	$\tilde{E}^q(x, \xi, t)$	spin dependent
proton helicity non-flip	proton helicity flip	

# Generalized Parton Distributions (GPDs)

$H, \tilde{H}$

unpolarized nucleon



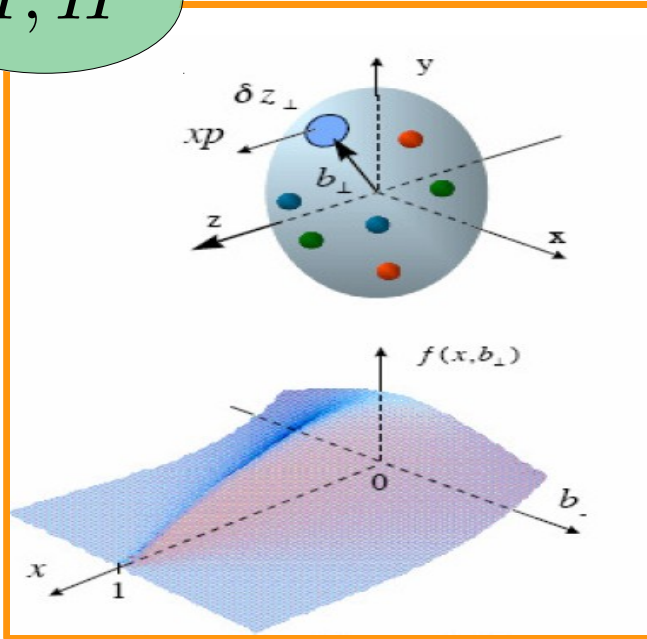
helicity-(in)dependent probability distribution  
of quarks as a function of their longitudinal  
fractional momentum and transverse position

M. Burkardt, Phys. Rev. D **62** (2000) 071503

# Generalized Parton Distributions (GPDs)

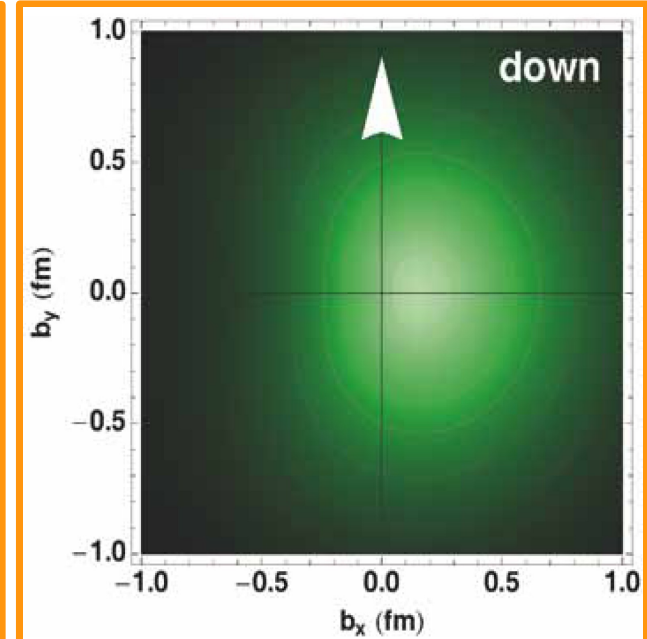
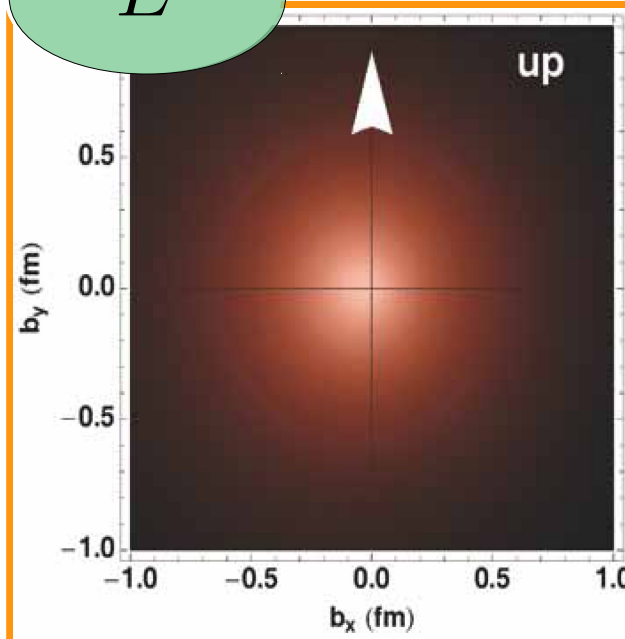
$H, \tilde{H}$

unpolarized nucleon



$E$

transversely polarized nucleon



pictures taken from A. Bacchetta and M. Contalbrigo, *Il Nuovo Saggiatore* **28** (2012) 1-2

helicity-(in)dependent probability distribution of quarks as a function of their longitudinal fractional momentum and transverse position

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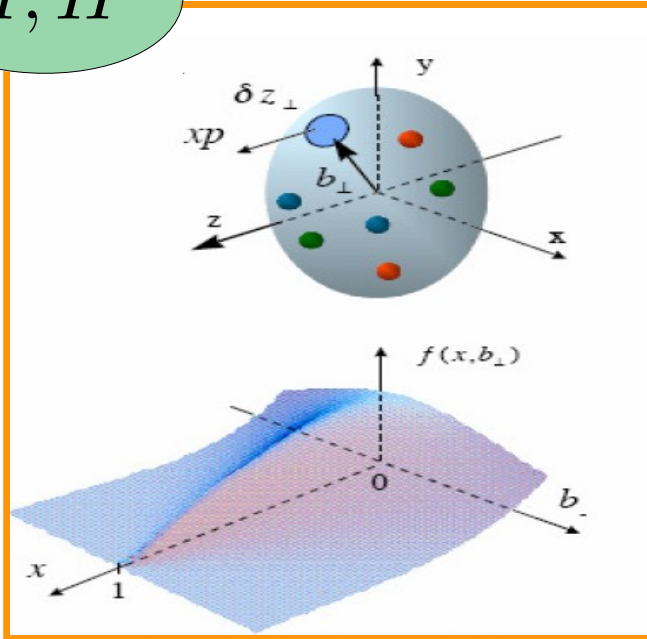
distortion of quark probability distribution compared to unpolarized nucleon

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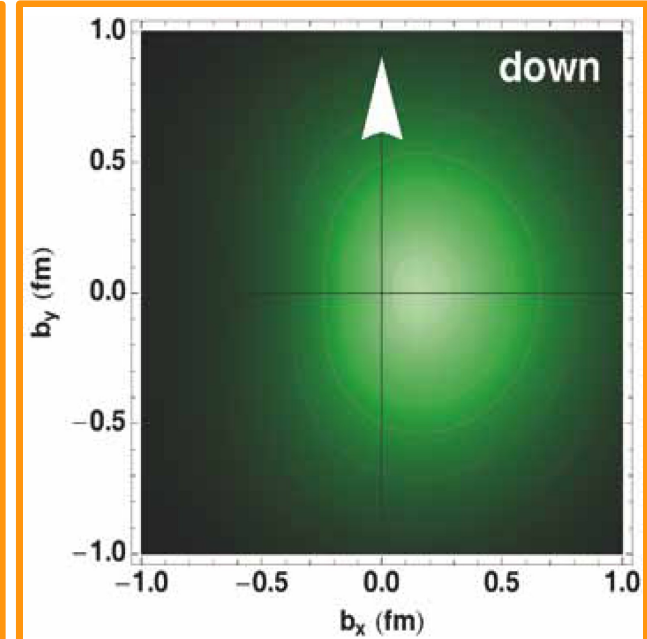
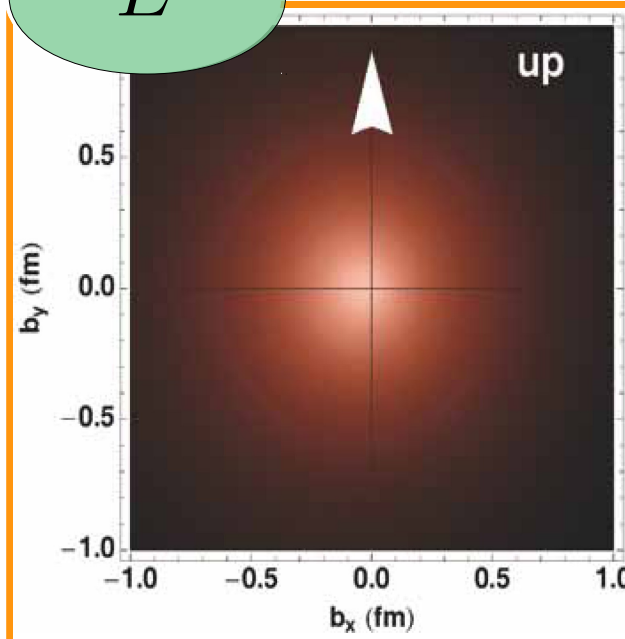
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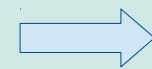
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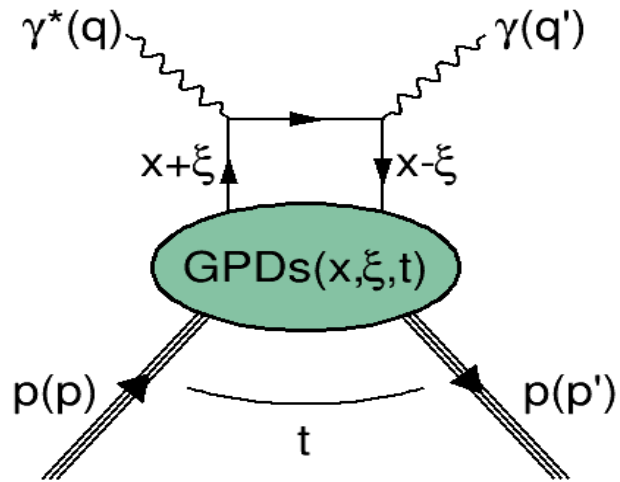
$$J^q = \lim_{t \rightarrow 0} \frac{1}{2} \int_{-1}^1 dx x [H^q(x, \xi, t) + E^q(x, \xi, t)]$$



quark orbital angular momentum

X. Ji, Phys. Rev. Lett. **78** (1997) 610

# Deeply virtual Compton scattering



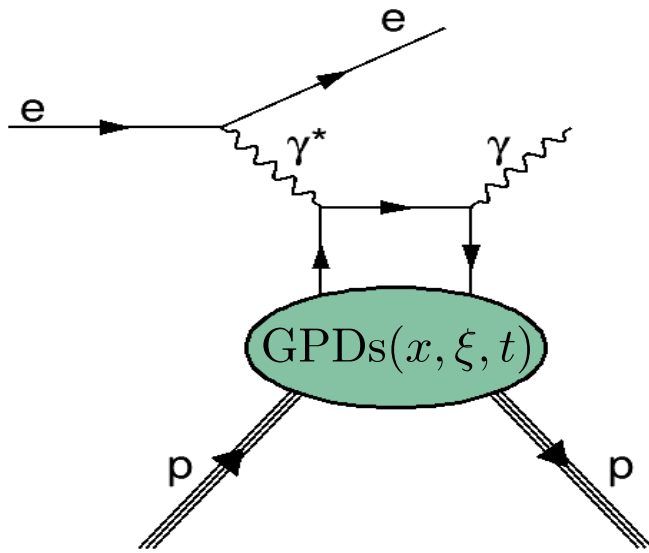
$$Q^2 \equiv -q^2$$

$$x_B \equiv \frac{Q^2}{2pq}$$

$$\xi \approx \frac{x_B}{2 - x_B}$$

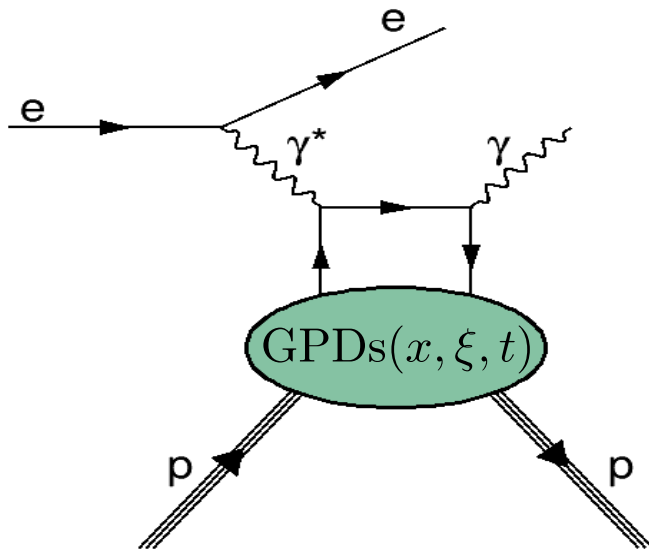


# Exclusive lepto-production of real photons

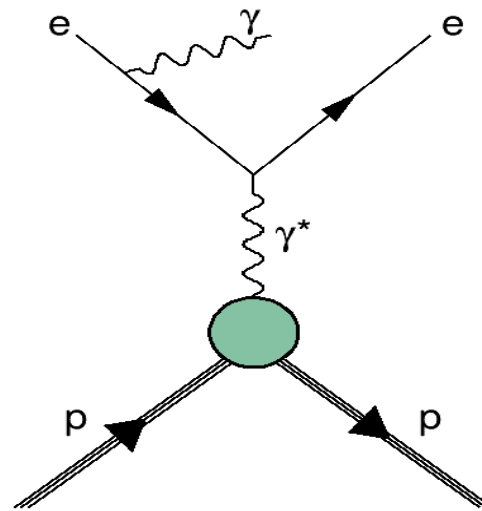


DVCS

# Exclusive lepto-production of real photons



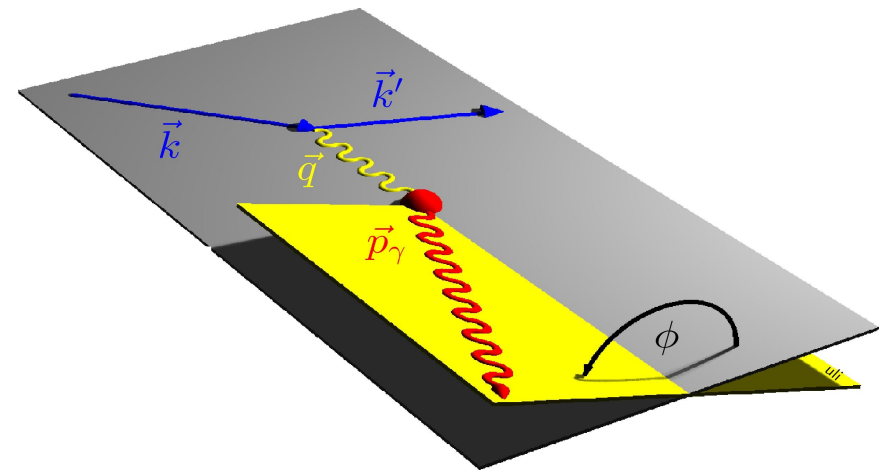
DVCS



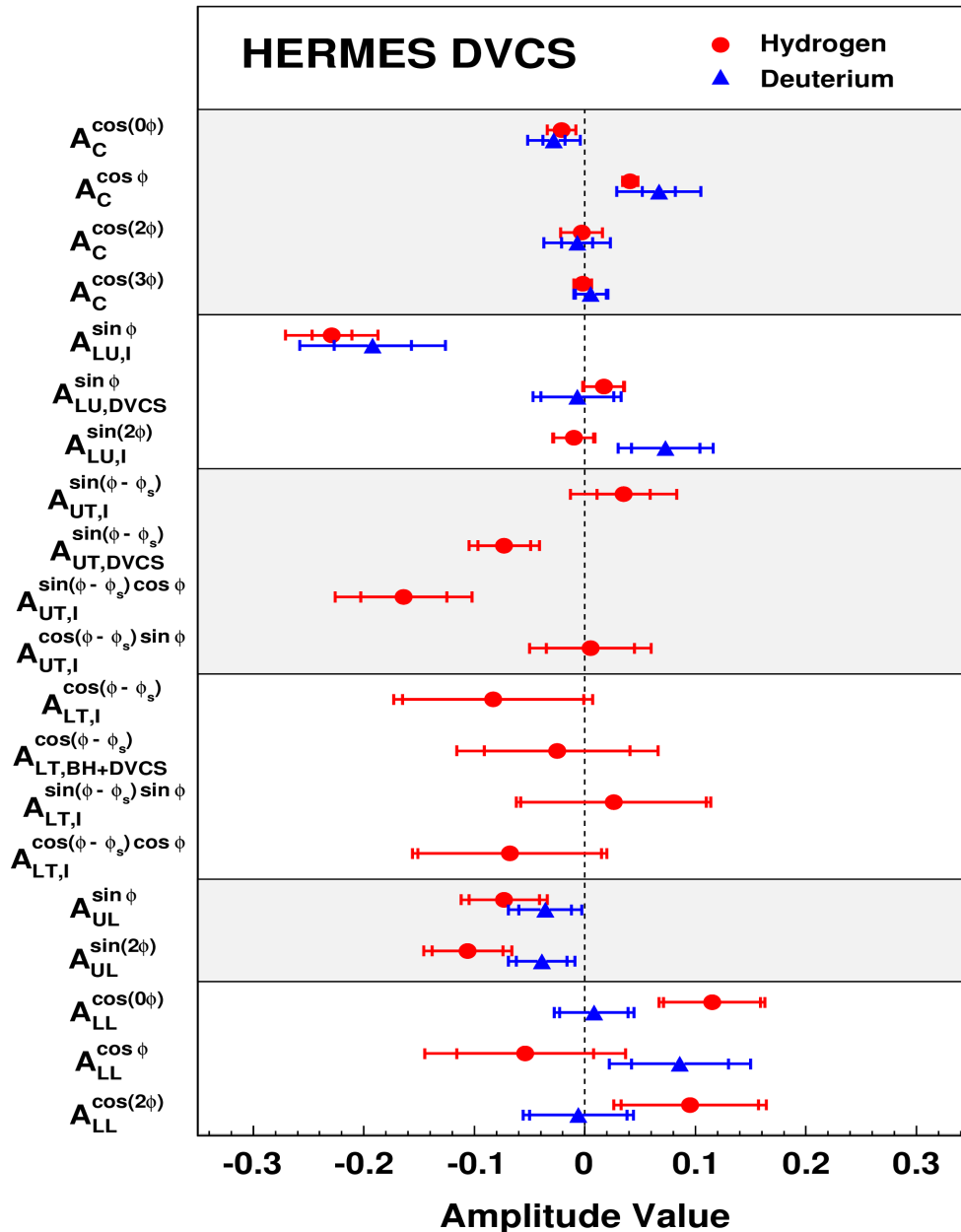
Bethe-Heitler

$$d\sigma \propto |\tau_{BH}|^2 + |\tau_{DVCS}|^2 + \tau_{BH} \tau_{DVCS}^* + \tau_{DVCS} \tau_{BH}^*$$

- $|\tau_{BH}|$  : calculable (form factors)
- $|\tau_{BH}| \gg |\tau_{DVCS}|$  at HERMES
- interference term:  
through azimuthal asymmetries



# DVCS at HERMES



beam-charge asymmetry  
 JHEP **07** (2012) 32  
 Nucl. Phys. B 829 (2010) 1

beam-helicity asymmetry  
 JHEP **07** (2012) 32  
 Nucl. Phys. B 829 (2010) 1

transverse target-spin asymmetry  
 JHEP **06** (2008) 066

double spin (LT) asymmetry  
 Phys. Lett. B **704** (2011) 15

longitudinal target-spin asymmetry  
 JHEP **06** (2010) 019  
 Nucl. Phys. B 842 (2011) 265

double spin (LL) asymmetry  
 JHEP **06** (2010) 019  
 Nucl. Phys. B 842 (2011) 265

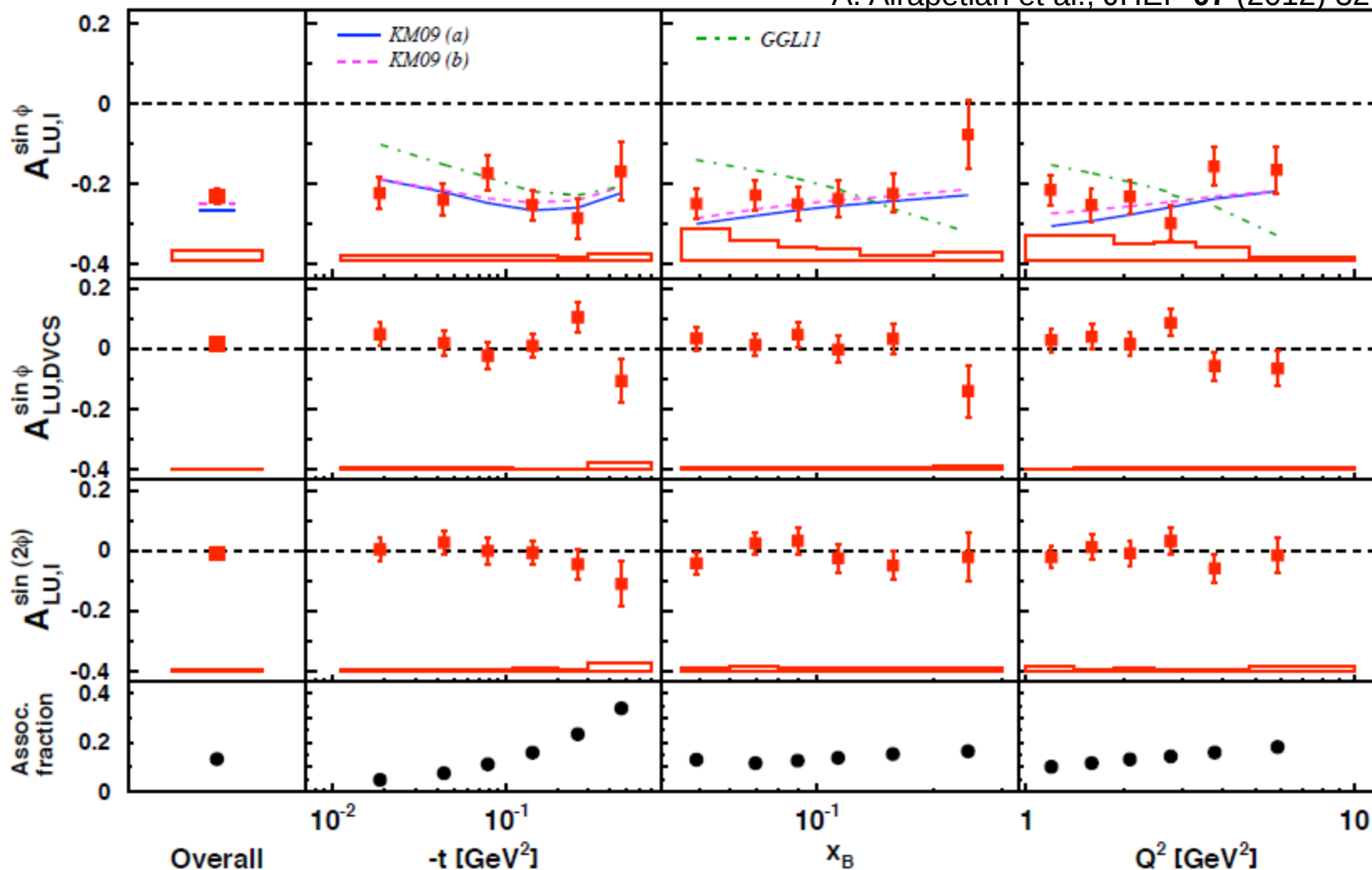
GPD  $H$

GPD  $E$

GPD  $\tilde{H}$

# Charged-separated beam-helicity asymmetry

A. Airapetian et al., JHEP 07 (2012) 32

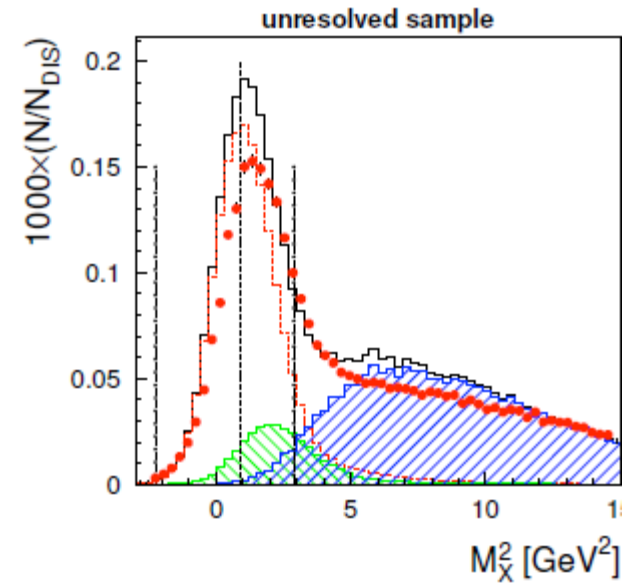
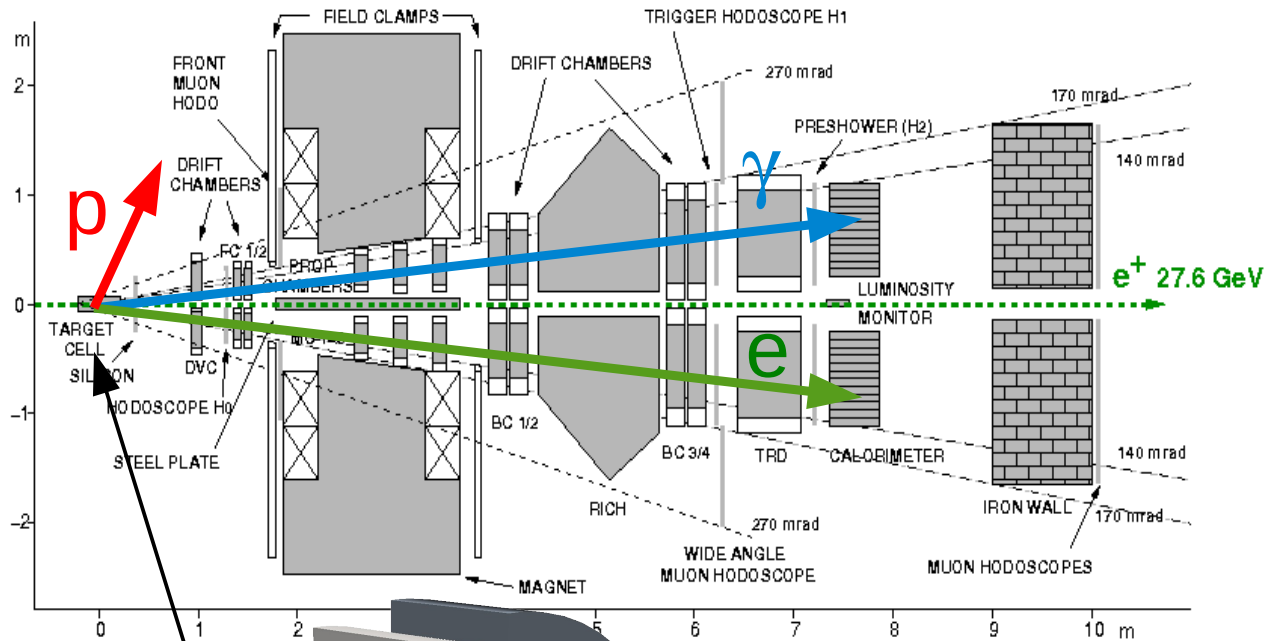


KM09: Nucl. Phys. B  
**841** (2010) 1:  
 fit to HERMES, ZEUS,  
 H1 data  
 Fit to HERMES, ZEUS,  
 H1, Jefferson Lab  
 data

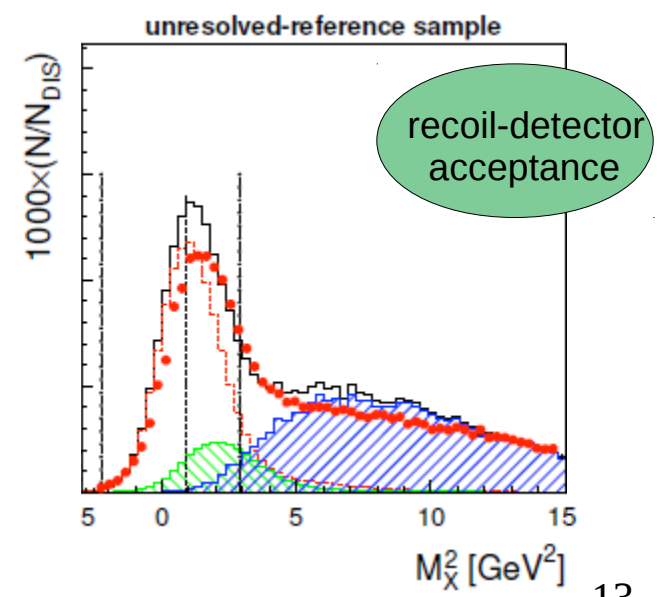
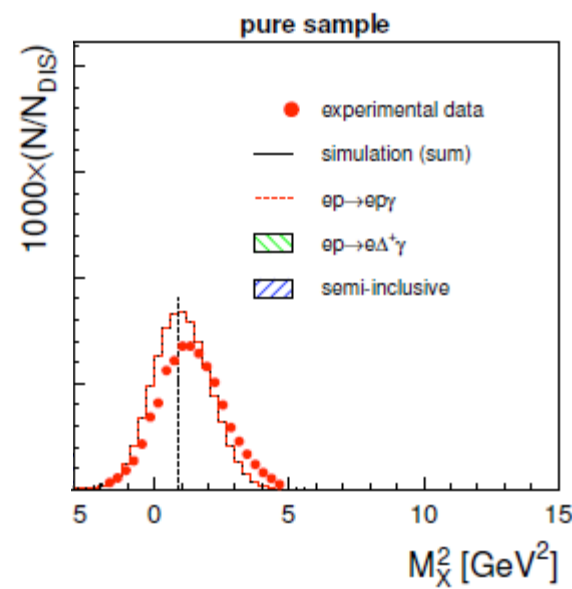
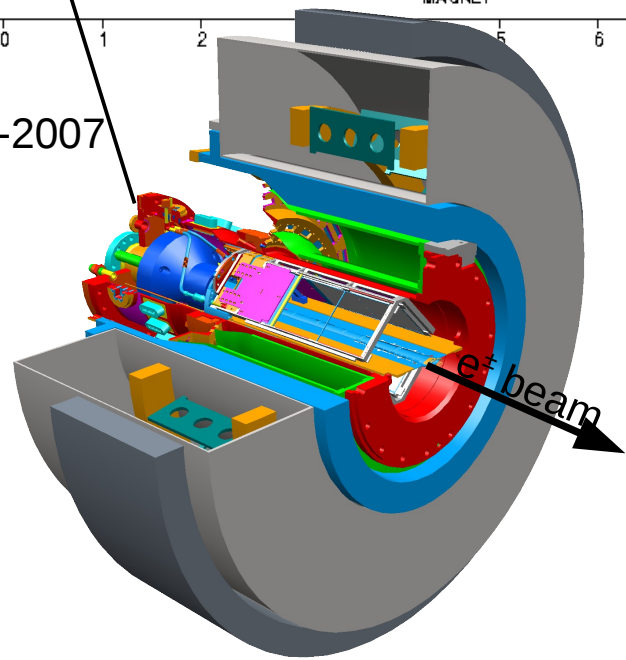
GGL11: Phys. Rev. D  
**84** (2011) 034007

- data collected from 1996-2007 (74% of data from 2006-2007)
- additional 3.2% scale uncertainty from beam polarization

# DVCS event selection

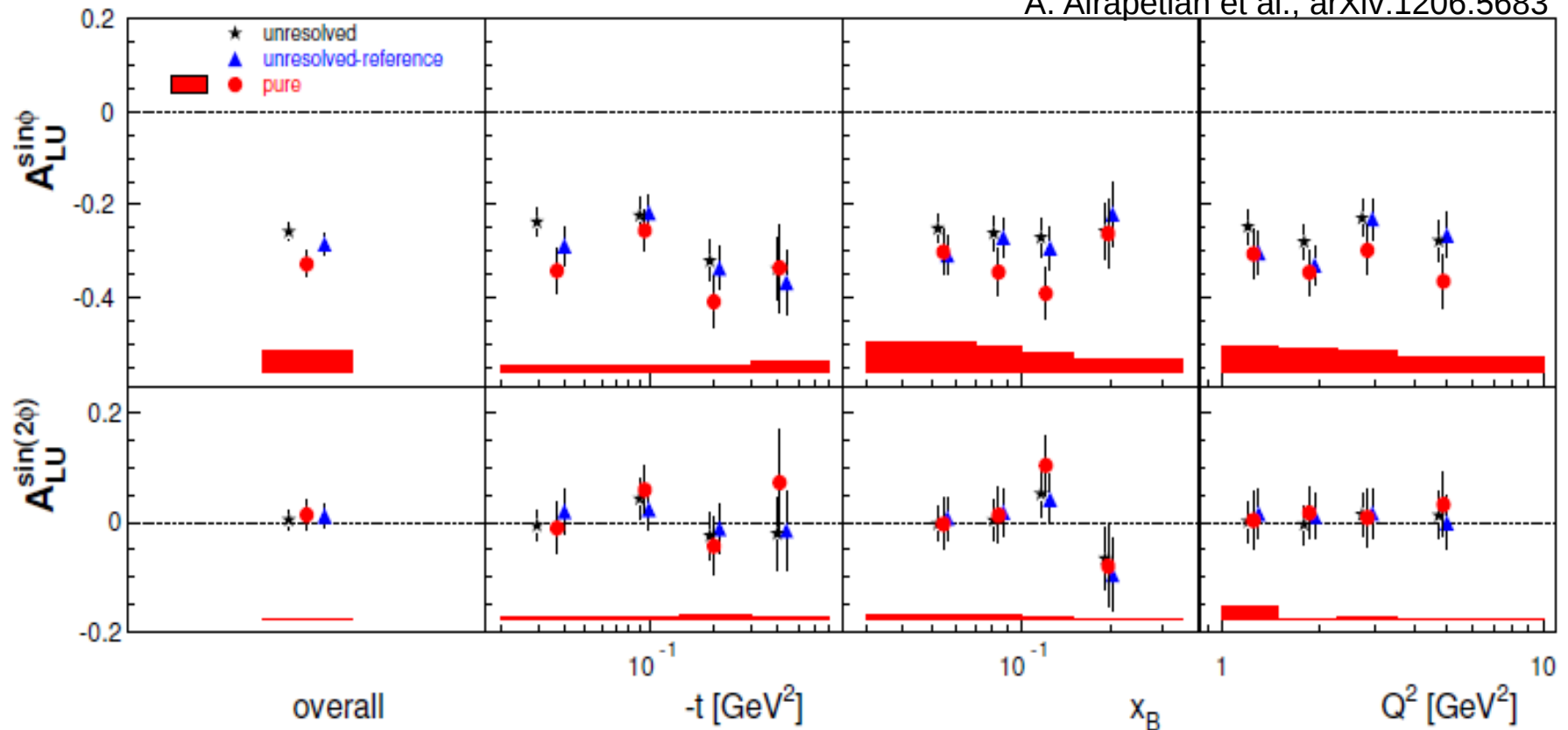


2006-2007



# Beam-helicity asymmetry

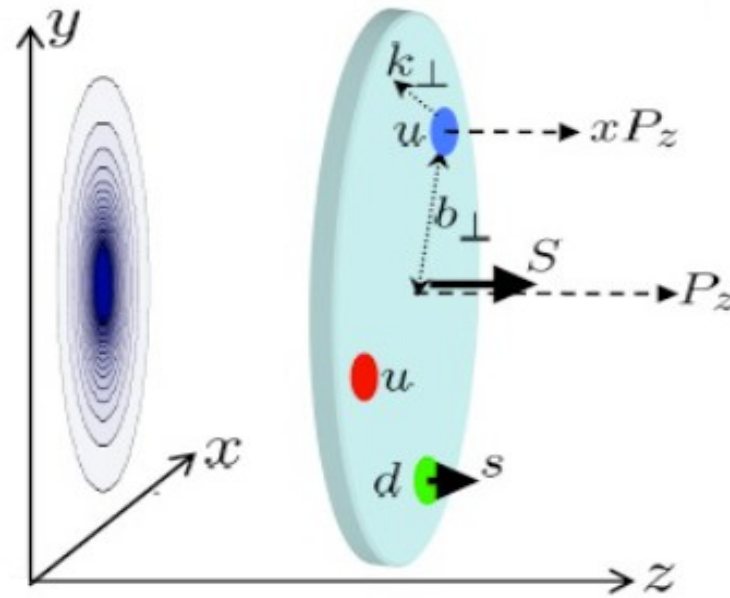
A. Airapetian et al., arXiv:1206.5683



- additional 1.96 % scale uncertainty from beam polarization

Generalized parton distributions

$$\int d^2\vec{k}_T W(x, \vec{k}_T, b_\perp) = \text{GPDs } (x, \xi, t)$$

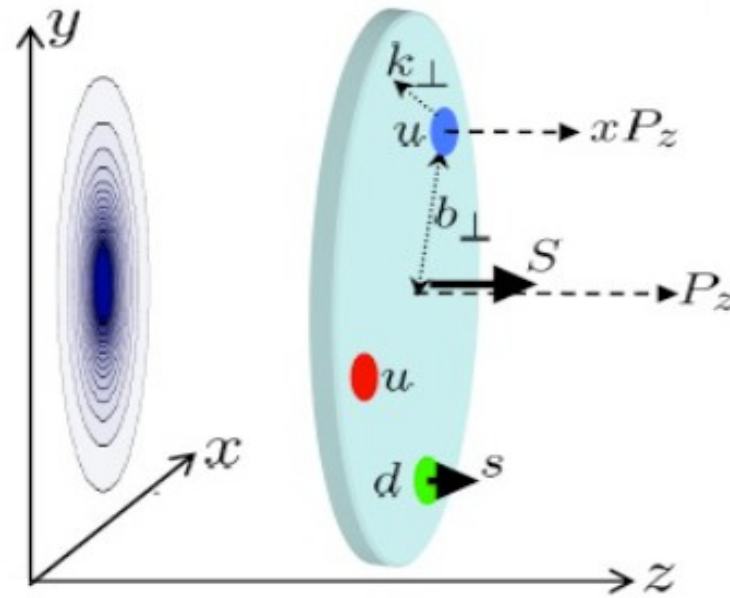


$$W(x, \vec{k}_T, \vec{b}_\perp)$$

Generalized parton distributions

$$\int d^2\vec{k}_T W(x, \vec{k}_T, \vec{b}_\perp) = \text{GPDs } (x, \xi, t)$$





$$W(x, \vec{k}_T, \vec{b}_\perp)$$

Generalized parton distributions

$$\int d^2\vec{k}_T W(x, \vec{k}_T, \vec{b}_\perp) = \text{GPDs } (x, \xi, t)$$

Transverse-momentum-dependent  
parton distribution functions

$$\int d^2\vec{b}_\perp W(x, \vec{k}_T, \vec{b}_\perp) = \text{TMD PDFs } (x, \vec{k}_T)$$

# Transverse momentum dependent distributions (TMDs)

Distribution functions

leading twist

$$f_1 = \text{yellow circle with blue center}$$

$$g_{1L} = \text{yellow circle with blue center and right arrow} - \text{yellow circle with blue center and left arrow}$$

$$h_{1T} = \text{yellow circle with blue center and up arrow} - \text{yellow circle with blue center and down arrow}$$

$$f_{1T}^\perp = \text{yellow circle with blue center and up arrow} - \text{yellow circle with blue center and down arrow}$$

$$h_1^\perp = \text{yellow circle with blue center and down arrow} - \text{yellow circle with blue center and up arrow}$$

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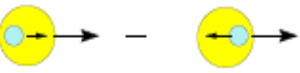
$$\sigma^{ep \rightarrow eh} = \sum_q \mathcal{I} [DF^{p \rightarrow q}(x, k_T^2) \sigma^{eq \rightarrow eq} FF^{q \rightarrow h}(z, p_T^2)]$$


Distribution functions


$q$   
leading twist

Fragmentation functions

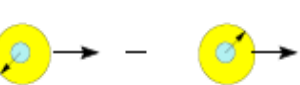
$f_1 =$  


$g_{1L} =$  


$h_{1T} =$  


$f_{1T}^\perp =$  

$h_1^\perp =$  


$h_{1L}^\perp =$  


$g_{1T} =$  

$h_{1T}^\perp =$  

$D_1 =$  


$G_{1L} =$  


$H_{1T} =$  

$D_{1T}^\perp =$  

$H_1^\perp =$  

$H_{1L}^\perp =$  

$G_{1T} =$  

$H_{1T}^\perp =$  

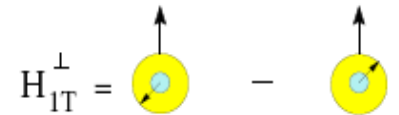
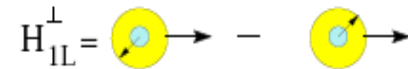
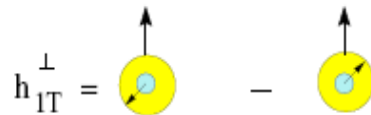
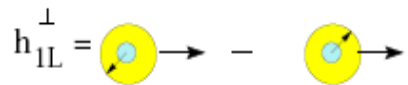
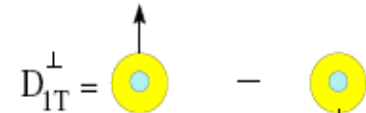
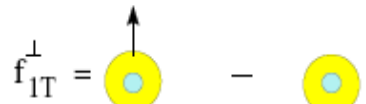
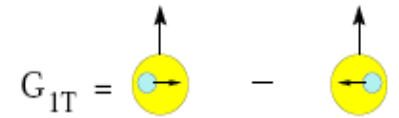
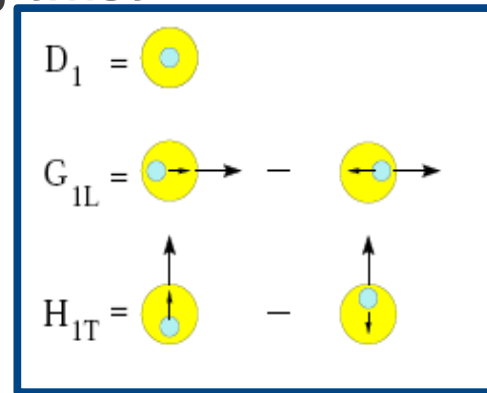
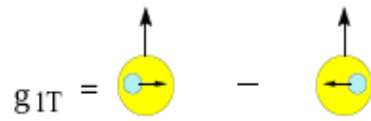
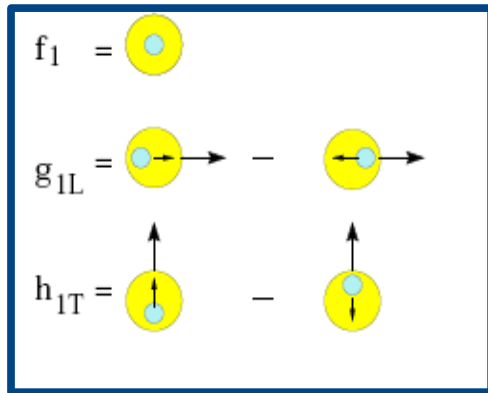
# Transverse momentum dependent distributions (TMDs)

$$\sigma^{ep \rightarrow eh} = \sum_q \mathcal{I} [DF^{p \rightarrow q}(x, k_T^2) \sigma^{eq \rightarrow eq} FF^{q \rightarrow h}(z, p_T^2)]$$

Distribution functions

$q$   
leading twist

Fragmentation functions



only distributions that survive integration over transverse momentum

# Transverse momentum dependent distributions (TMDs)

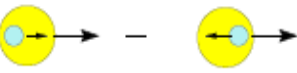
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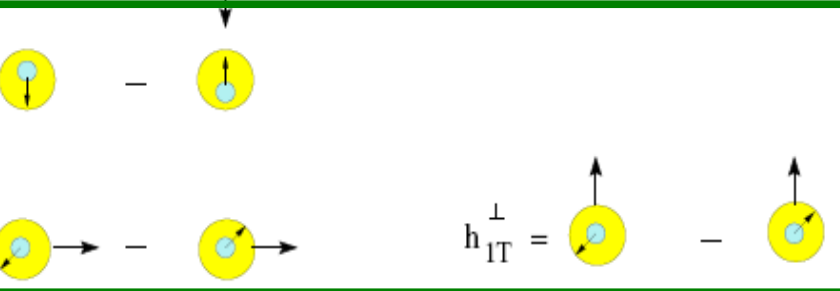
Fragmentation functions


$f_1 =$  


$g_{1L} =$  


$h_{1T} =$  


$f_{1T}^\perp =$  

$h_1^\perp =$  


$h_{1L}^\perp =$  


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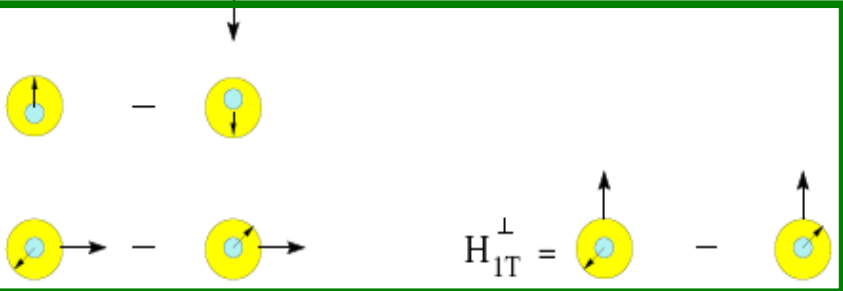
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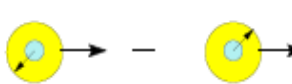
$D_1 =$  


$G_{1L} =$  


$H_{1T} =$  

$D_{1T}^\perp =$  

$H_1^\perp =$  

$H_{1L}^\perp =$  

$G_{1T} =$  

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Chiral odd: involve helicity flip of quark  
appear in pairs in cross section

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Distribution functions

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Chiral odd: involve helicity flip of transversally polarized quark  
appear in pairs in cross section

T-odd: appear in pairs in spin-independent x-section & double-spin asymmetries  
single in single-spin asymmetries

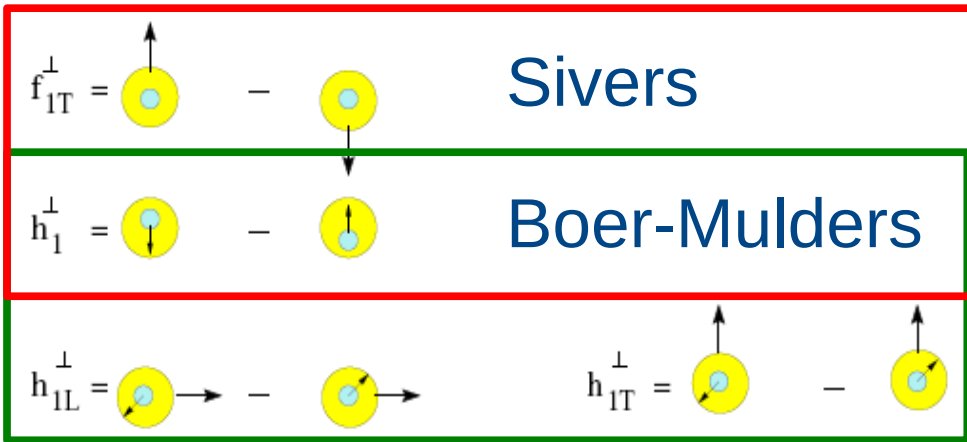
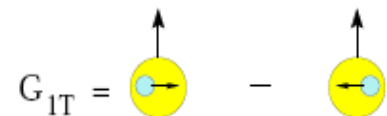
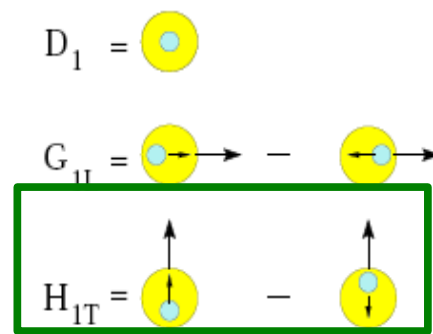
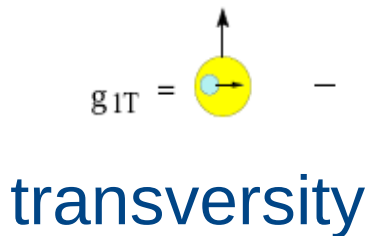
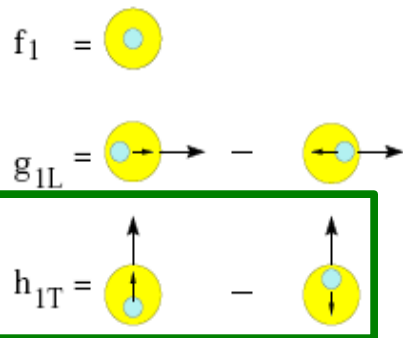
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Distribution functions

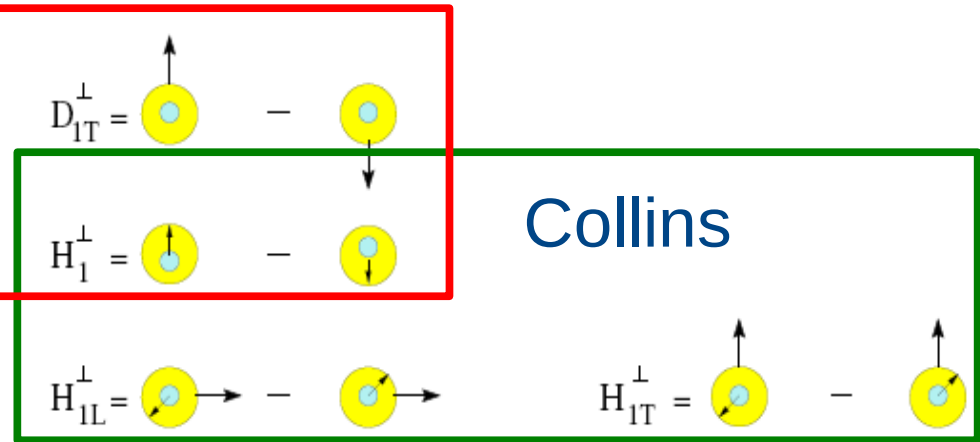
$q$   
leading twist

Fragmentation functions



Sivers

Boer-Mulders

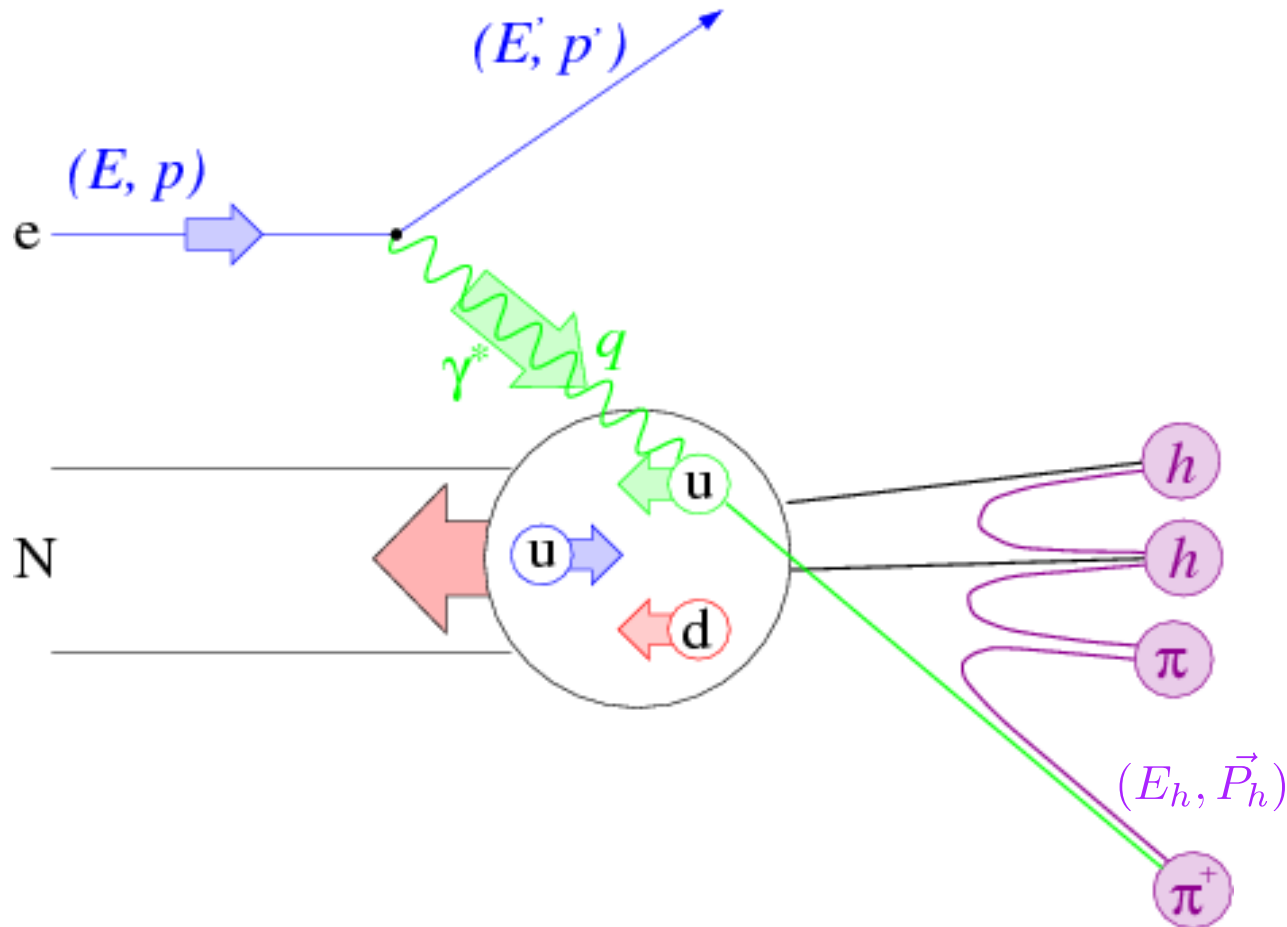


Collins

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appear in pairs in cross section

T-odd: appear in pairs in spin-independent x-section & double-spin asymmetries  
single in single-spin asymmetries

# Semi-inclusive deep-inelastic scattering



$$Q^2 = -q^2$$

$$y \stackrel{lab}{=} \frac{\nu}{E}$$

$$x \stackrel{lab}{=} \frac{Q^2}{2M\nu}$$

$$z \stackrel{lab}{=} \frac{E_h}{\nu}$$



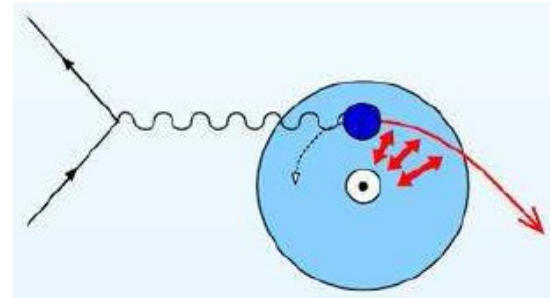
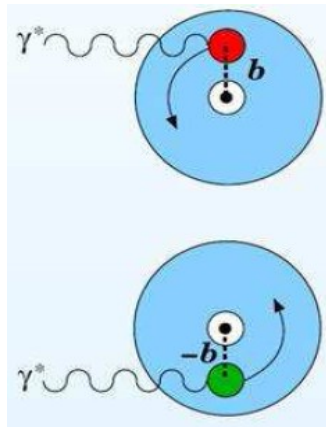
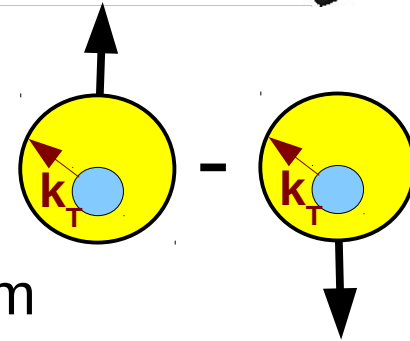
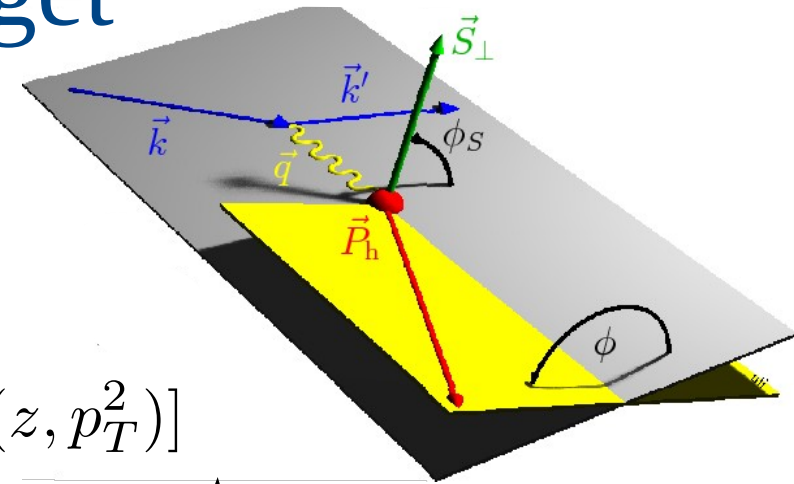
# Single-spin asymmetry on transversely polarized target

$$A_{UT} = \frac{1}{\langle |S_T| \rangle} \frac{N^\uparrow(\phi, \phi_S) - N^\downarrow(\phi, \phi_S)}{N^\uparrow(\phi, \phi_S) + N^\downarrow(\phi, \phi_S)}$$

$$\sim \sin(\phi - \phi_S) \sum_q e_q \mathcal{I} \left[ \frac{\vec{k}_T \cdot \hat{P}_{h\perp}}{M_h} f_{1T}^{\perp,q}(x, k_T^2) D_1^q(z, p_T^2) \right]$$

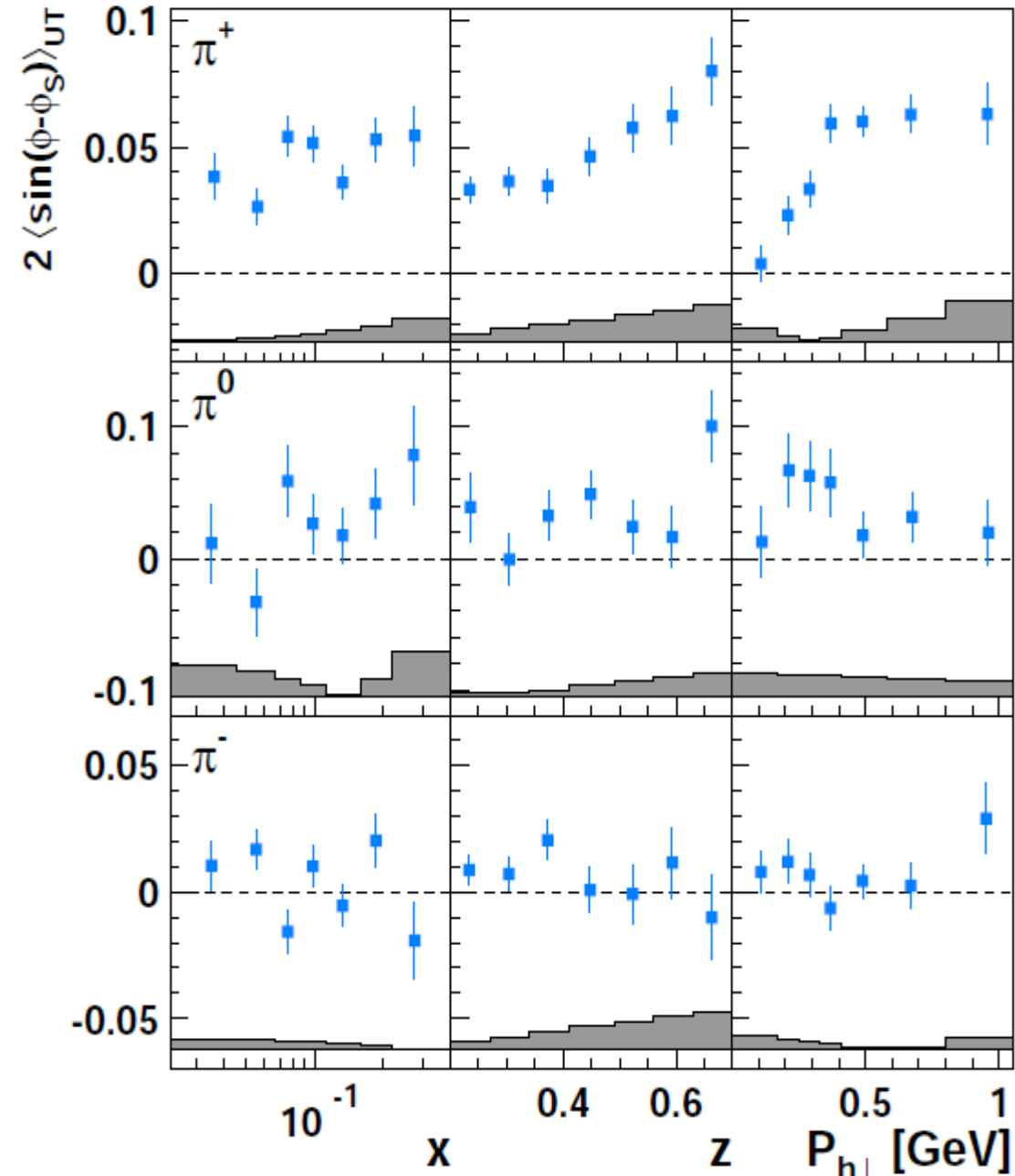
$f_{1T}^{\perp,q}(x, k_T^2)$  : **Sivers distribution function**

- requires non-zero quark orbital angular momentum
- naïve-T-odd
- FSI  $\longrightarrow$  left-right (azimuthal) asymmetry in direction of outgoing hadron



# Sivers amplitudes for pions

A. Airapetian et al., Phys. Rev. Lett. **103** (2009) 152002



- $\pi^+$ 
  - significantly positive
    - non-zero orbital angular momentum!
  - clear rise with  $z$
  - rise at low  $P_{h\perp}$ , plateau at high  $P_{h\perp}$
  - amplitude dominated by u-quark scattering:

$$\approx \frac{\mathcal{I}[f_{1T}^{\perp,u}(x, k_T^2) D_1^{u \rightarrow \pi^+}(z, p_T^2)]}{\mathcal{I}[f_1^u(x, k_T^2) D_1^{u \rightarrow \pi^+}(z, p_T^2)]}$$

→  $f_{1T}^{\perp,u}(x, k_T^2) < 0$

- $\pi^-$ 
  - consistent with zero
  - u- and d- quark cancellation
  - $f_{1T}^{\perp,d}(x, k_T^2) > 0$
- $\pi^0$ 
  - slightly positive
  - isospin symmetry fulfilled

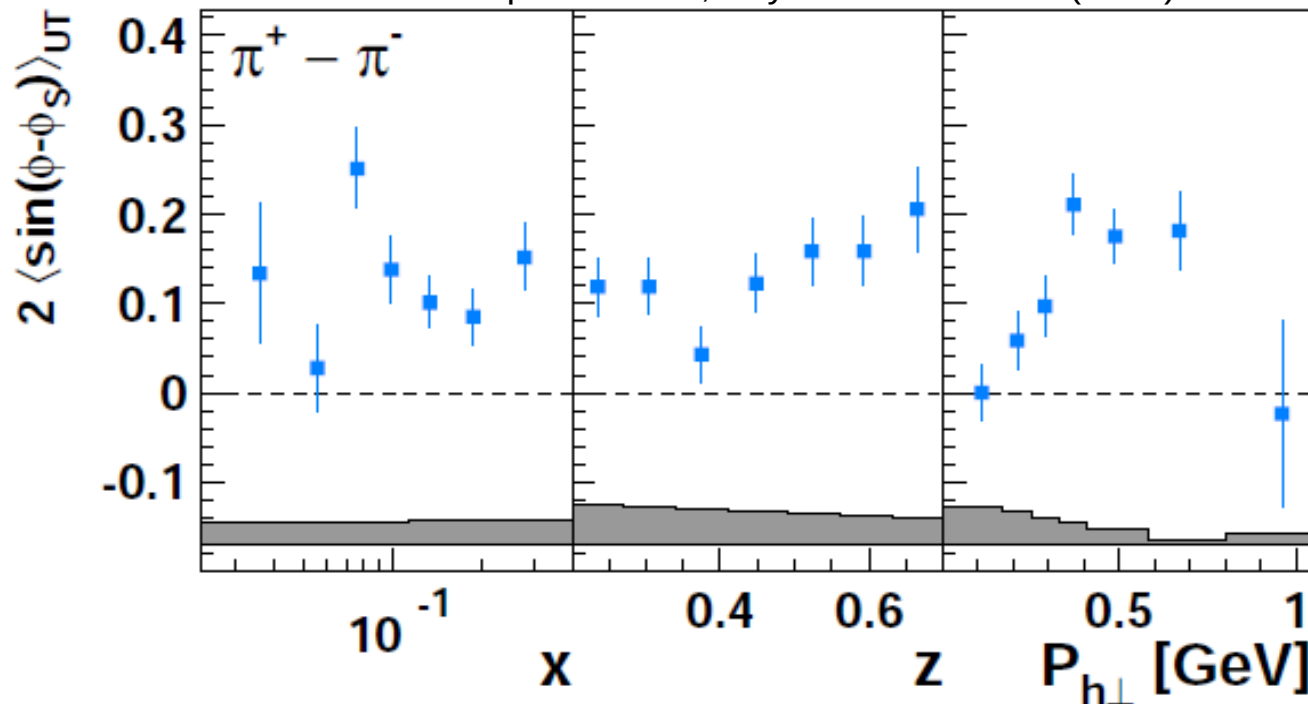
# Sivers distribution for valence quarks

$$A_{UT}^{\pi^+ - \pi^-} = \frac{1}{\langle |S_T| \rangle} \frac{(\sigma_{U\uparrow}^{\pi^+} - \sigma_{U\uparrow}^{\pi^-}) - (\sigma_{U\downarrow}^{\pi^+} - \sigma_{U\downarrow}^{\pi^-})}{(\sigma_{U\uparrow}^{\pi^+} - \sigma_{U\uparrow}^{\pi^-}) + (\sigma_{U\downarrow}^{\pi^+} - \sigma_{U\downarrow}^{\pi^-})}$$

→ suppressed exclusive VM ( $\rho^0$ ) contribution

$$\langle \sin(\phi - \phi_S) \rangle_{UT}^{\pi^+ - \pi^-} \approx - \frac{4f_{1T}^{\perp, u_v} - f_{1T}^{\perp, d_v}}{4f_1^{u_v} - f_1^{d_v}}$$

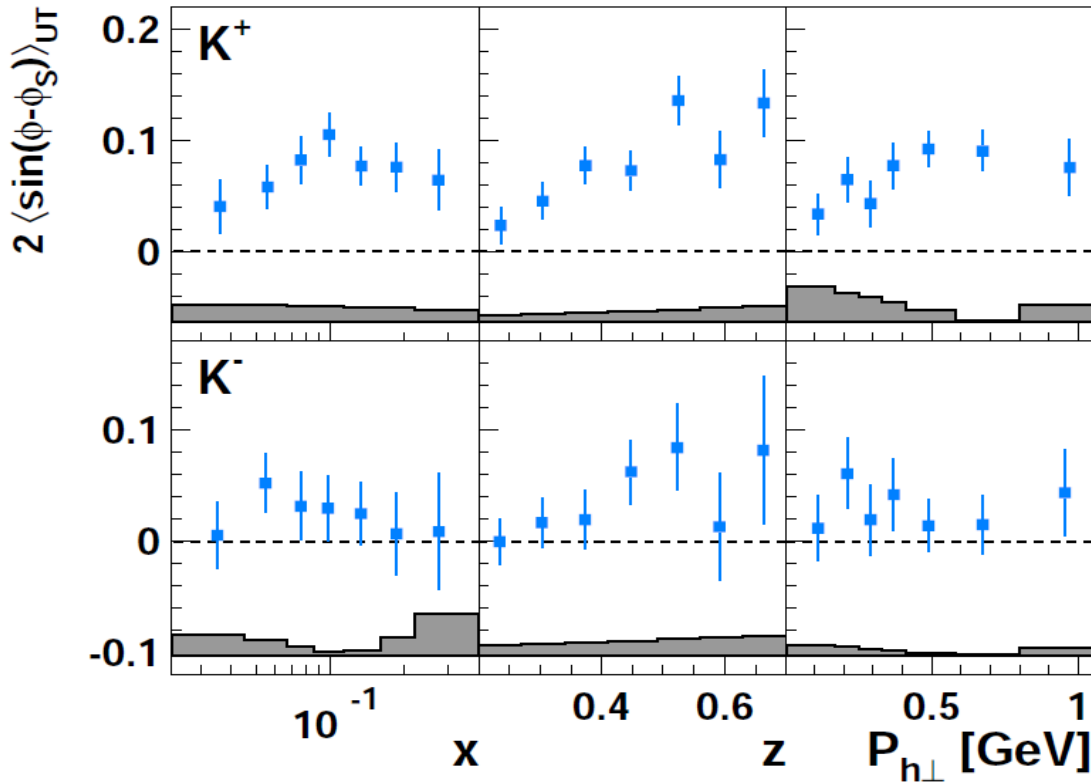
A. Airapetian et al., Phys. Rev. Lett. **103** (2009) 152002



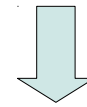
- Sivers distribution for d-valence  $\gg$  u-valence or
- Sivers distribution for u-valence is large &  $< 0$  (more likely)

# Sivers amplitudes for kaons

A. Airapetian et al., Phys. Rev. Lett. **103** (2009) 152002



- $K^+$ 
  - significantly positive
  - clear rise with  $z$
  - rise at low  $P_{h\perp}$ , plateau at high  $P_{h\perp}$
  - larger than  $\pi^+$

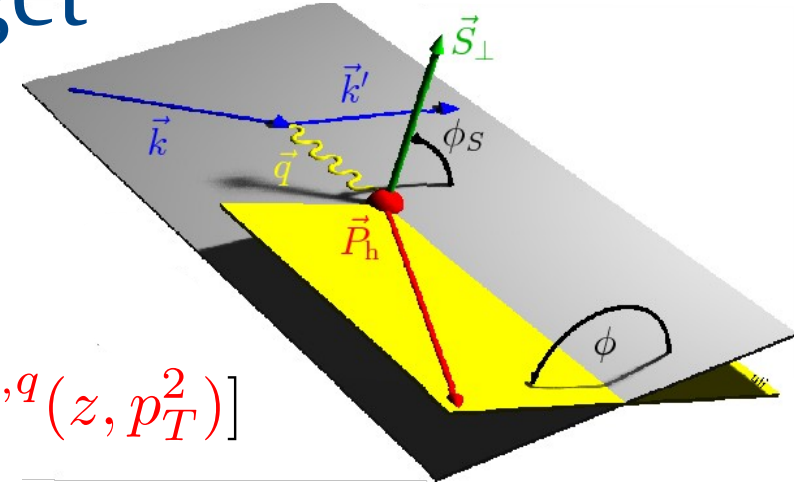


non-trivial role of sea quarks?

- $K^-$ 
  - slightly positive

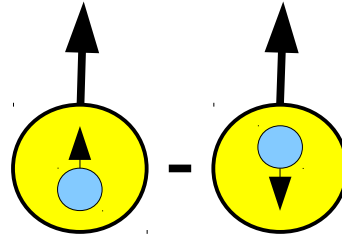
# Single-spin asymmetry on transversely polarize target

$$A_{UT} = \frac{1}{\langle |S_T| \rangle} \frac{N^\uparrow(\phi, \phi_S) - N^\downarrow(\phi, \phi_S)}{N^\uparrow(\phi, \phi_S) + N^\downarrow(\phi, \phi_S)}$$



$$\sim \sin(\phi + \phi_S) \sum_q e_q^2 \mathcal{I} \left[ \frac{\vec{p}_T \cdot \hat{P}_{h\perp}}{M_h} h_{1T}^q(x, k_T^2) H_1^{\perp,q}(z, p_T^2) \right]$$

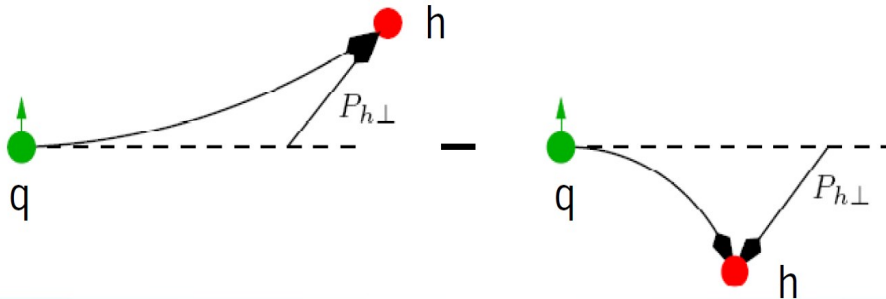
$h_{1T}^q(x, k_T^2)$ : transversity



- chiral odd

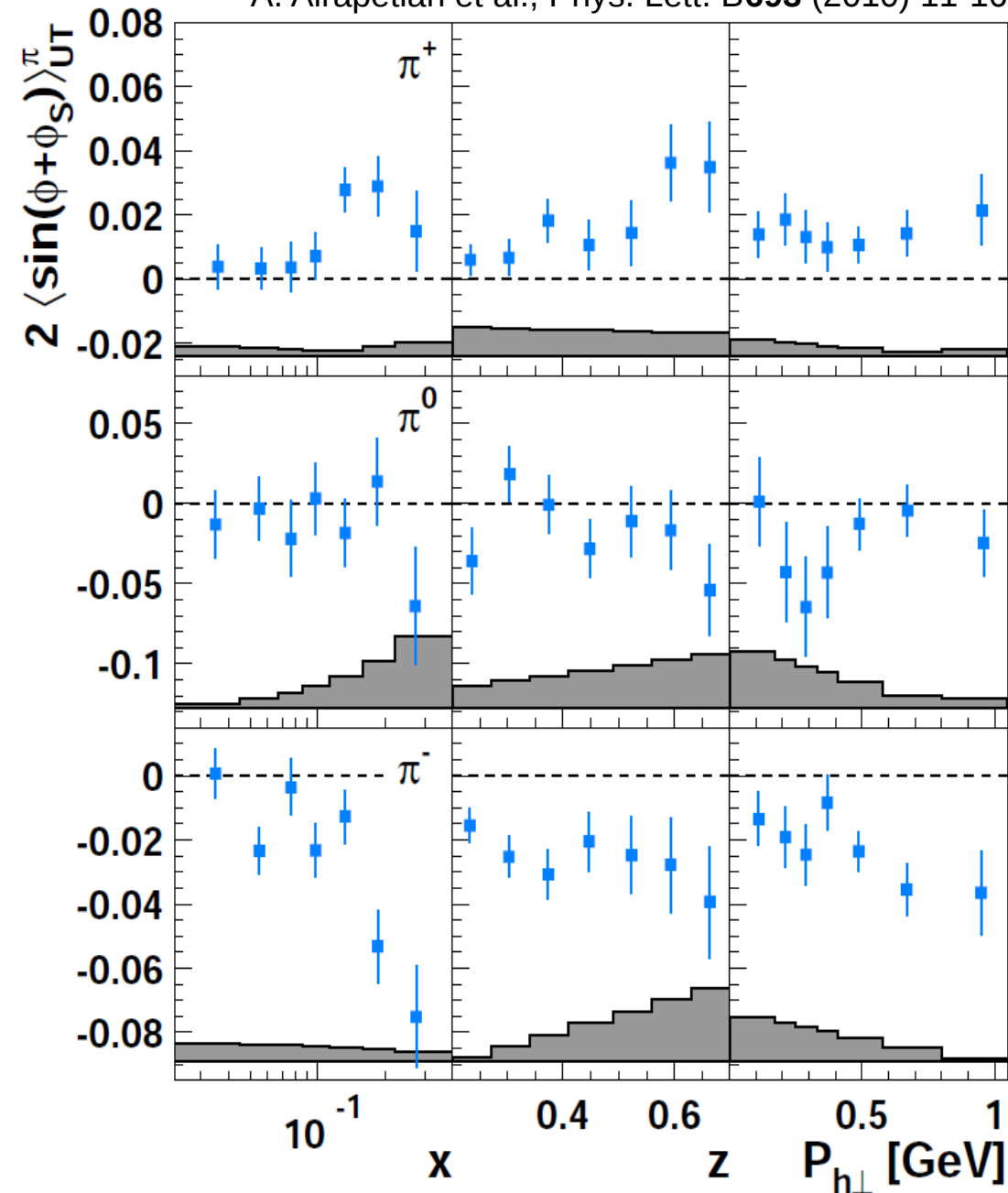
$H_1^{\perp,q}(z, p_T^2)$ : Collins fragmentation function

- chiral odd
- naïve-T-odd



# Collins amplitudes for pions

A. Airapetian et al., Phys. Lett. B**693** (2010) 11-16

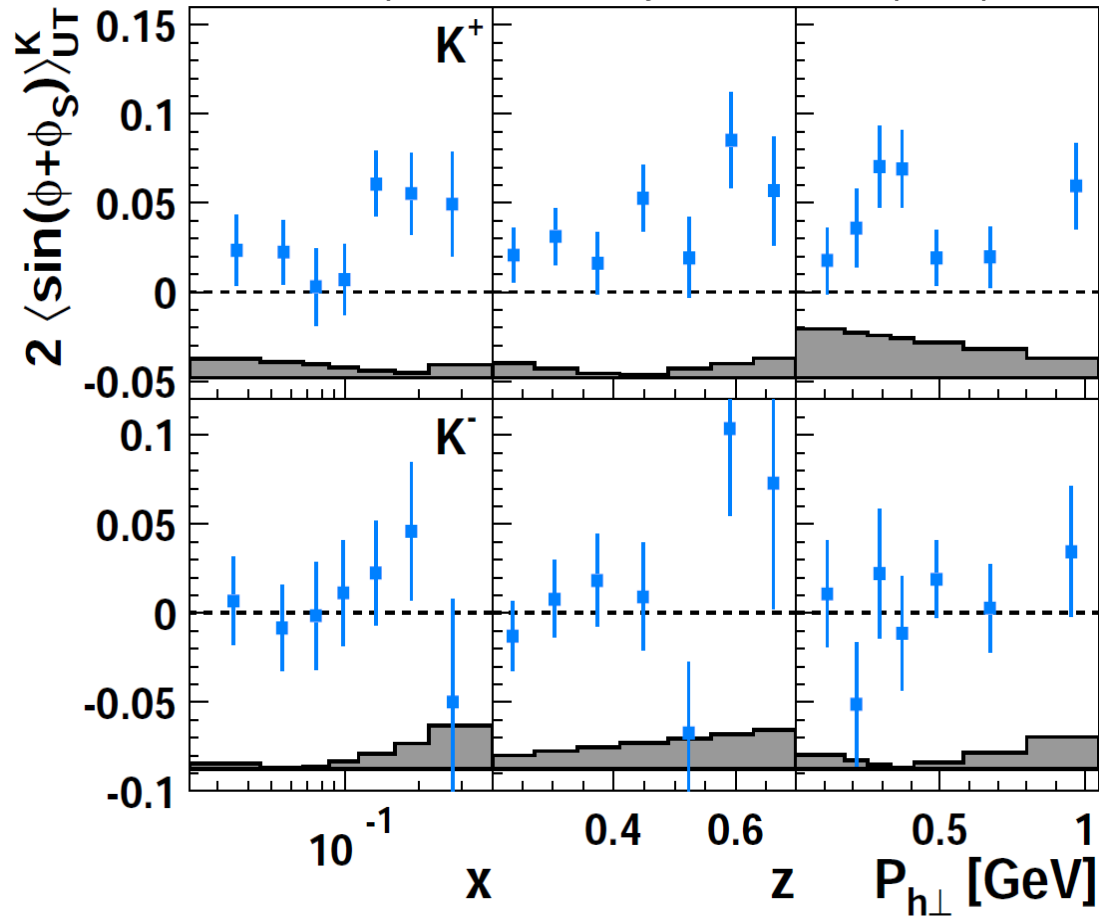


- $\pi^\pm$  increasing with  $z$  and  $x_B$
- positive for  $\pi^+$
- large & negative for  $\pi^-$ 

$$H_1^{\perp, fav} \approx -H_1^{\perp, unfav}$$
- isospin symmetry fulfilled

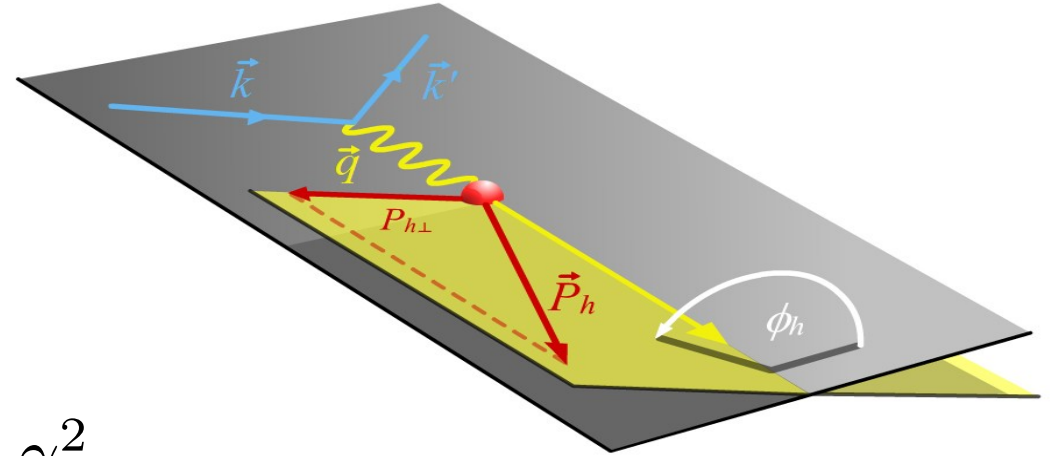
# Collins amplitudes for kaons

A. Airapetian et al., Phys. Lett. B**693** (2010) 11-16



- $K^+$ : increasing with  $z$  and  $x_B$
- positive for  $K^+$  & larger than for  $\pi^+$ 
  - role of s-quark
  - u-dominance  $\xrightarrow{?}$
$$H_1^{\perp, u \rightarrow K^+} > H_1^{\perp, u \rightarrow \pi^+}$$
- $K^- \approx 0$ ,  $\neq$  from  $\pi^-$   
 $K^-$  is pure sea object:  
 sea-quark transversity expected to be small

# Spin-independent semi-inclusive DIS cross section



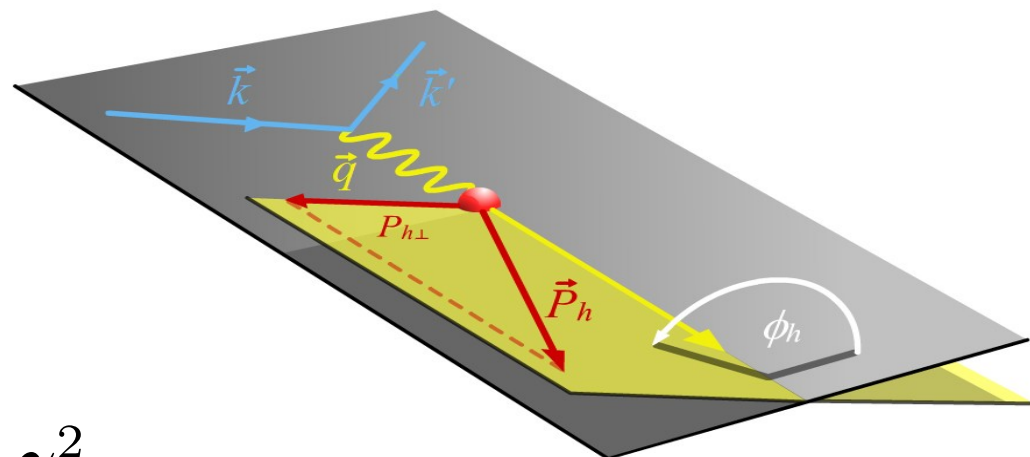
non-collinear cross section

$$\frac{d\sigma}{dx dy dz dP_{h\perp}^2 d\phi_h} = \frac{\alpha^2}{xyQ^2} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ A(y) F_{UU,T} + B(y) F_{UU,L} \right. \\ \left. + C(y) \cos \phi_h F_{UU}^{\cos \phi_h} + B(y) \cos 2\phi_h F_{UU}^{\cos 2\phi_h} \right\}$$

$$\gamma = \frac{2Mx}{Q}, \quad F = F(x, Q, z, \vec{P}_{h\perp})$$



# Spin-independent semi-inclusive DIS cross section



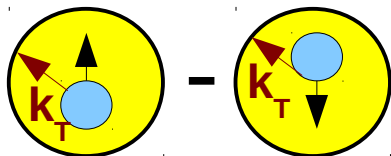
non-collinear cross section

$$\frac{d\sigma}{dx dy dz dP_{h\perp}^2 d\phi_h} = \frac{\alpha^2}{xyQ^2} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ A(y) F_{UU,T} + B(y) F_{UU,L} \right. \\ \left. + C(y) \cos \phi_h F_{UU}^{\cos \phi_h} + B(y) \cos 2\phi_h F_{UU}^{\cos 2\phi_h} \right\}$$

$$\gamma = \frac{2Mx}{Q}, \quad F = F(x, Q, z, \vec{P}_{h\perp})$$

leading twist

$$F_{UU}^{\cos 2\phi_h} = \mathcal{I} \left[ - \frac{2(\hat{P}_{h\perp} \cdot \vec{k}_T)(\hat{P}_{h\perp} \cdot \vec{p}_T) - \vec{k}_T \cdot \vec{p}_T}{M_h M} h_1^\perp H_1^\perp \right]$$



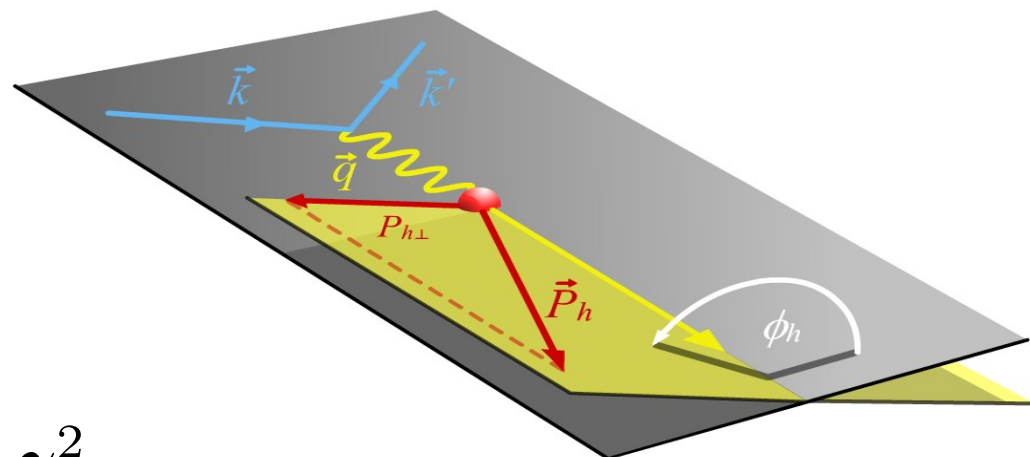
**Boer-Mulders DF**

- chiral odd
- naïve-T-odd

**Collins FF**

- chiral odd
- naïve-T-odd

# Spin-independent semi-inclusive DIS cross section



non-collinear cross section

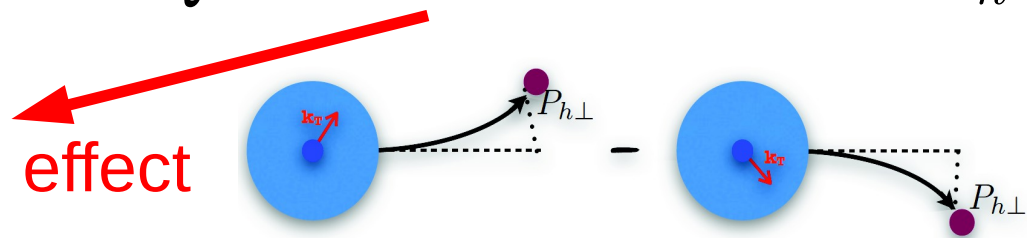
$$\frac{d\sigma}{dx dy dz dP_{h\perp}^2 d\phi_h} = \frac{\alpha^2}{xyQ^2} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ A(y) F_{UU,T} + B(y) F_{UU,L} \right. \\ \left. + C(y) \cos \phi_h F_{UU}^{\cos \phi_h} + B(y) \cos 2\phi_h F_{UU}^{\cos 2\phi_h} \right\}$$

$$\gamma = \frac{2Mx}{Q}, \quad F = F(x, Q, z, \vec{P}_{h\perp})$$

sub-leading twist

$$F_{UU}^{\cos \phi_h} = \frac{2M}{Q} \mathcal{I} \left[ -\frac{\hat{P}_{h\perp} \cdot \vec{k}_T}{M} f_1 D_1 - \frac{\hat{P}_{h\perp} \cdot \vec{p}_T}{M_h} \frac{k_T^2}{M^2} h_1^\perp H_1^\perp + \dots \right]$$

**Cahn effect**



quark-gluon-quark correlations

# Extraction of the cosine moments

$$\langle \cos(n\phi_h) \rangle \stackrel{th.}{=} \frac{\int d\phi_h \cos(n\phi_h) \sigma_{UU}(\omega, \phi_h)}{\int d\phi_h \sigma_{UU}(\omega, \phi_h)} \quad \omega = (x, y, z, P_{h\perp}^2)$$

$$\langle \cos(n\phi_h) \rangle \stackrel{exp.}{=} \frac{\int d\phi_h \cos(n\phi_h) \epsilon_{acc}(\omega, \phi_h) \epsilon_{rad}(\omega, \phi_h) \sigma_{UU}(\omega, \phi_h)}{\int d\phi_h \epsilon_{acc}(\omega, \phi_h) \epsilon_{rad}(\omega, \phi_h) \sigma_{UU}(\omega, \phi_h)}$$

**extraction is challenging!**

azimuthal modulations also possible due to

- detector geometrical acceptance
- higher-order QED effects

# Extraction of the cosine moments

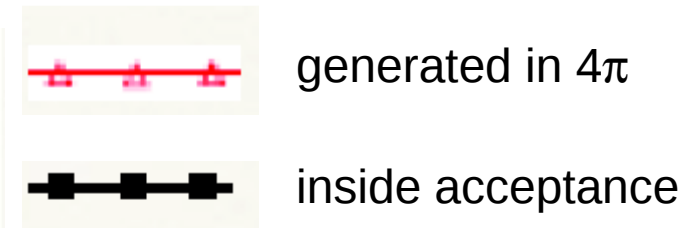
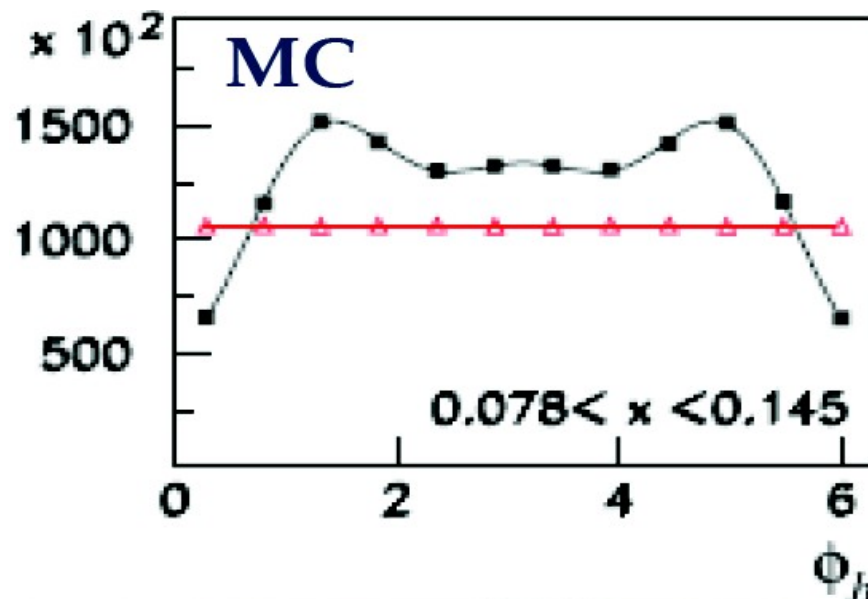
$$\langle \cos(n\phi_h) \rangle \stackrel{th.}{=} \frac{\int d\phi_h \cos(n\phi_h) \sigma_{UU}(\omega, \phi_h)}{\int d\phi_h \sigma_{UU}(\omega, \phi_h)} \quad \omega = (x, y, z, P_{h\perp}^2)$$

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**extraction is challenging!**

azimuthal modulations also possible due to

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**fully differential analysis needed**  
**unfolding procedure with 400 x 12 bins**

## BINNING

400 kinematic bins x 12  $\phi$ -bins

Variable	Bin limits						#
x	0.023	0.042	0.078	0.145	0.27	1	5
y	0.3	0.45	0.6	0.7	0.85		4
z	0.2	0.3	0.45	0.6	0.75	1	5
$P_{hT}$	0.05	0.2	0.35	0.5	0.75		4

# Extraction of the cosine moments

$$\langle \cos(n\phi_h) \rangle \stackrel{th.}{=} \frac{\int d\phi_h \cos(n\phi_h) \sigma_{UU}(\omega, \phi_h)}{\int d\phi_h \sigma_{UU}(\omega, \phi_h)} \quad \omega = (x, y, z, P_{h\perp}^2)$$

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**extraction is challenging!**

azimuthal modulations also possible due to

- detector geometrical acceptance
- higher-order QED effects

unfolding

**fully differential analysis needed  
unfolding procedure with 400 x 12 bins**

$$\langle \cos(n\phi_h) \rangle \approx \left. \frac{\int d\phi_h \cos(n\phi_h) \sigma_{UU}(\omega, \phi_h)}{\int d\phi_h \sigma_{UU}(\omega, \phi_h)} \right|_{\text{bin } i}$$

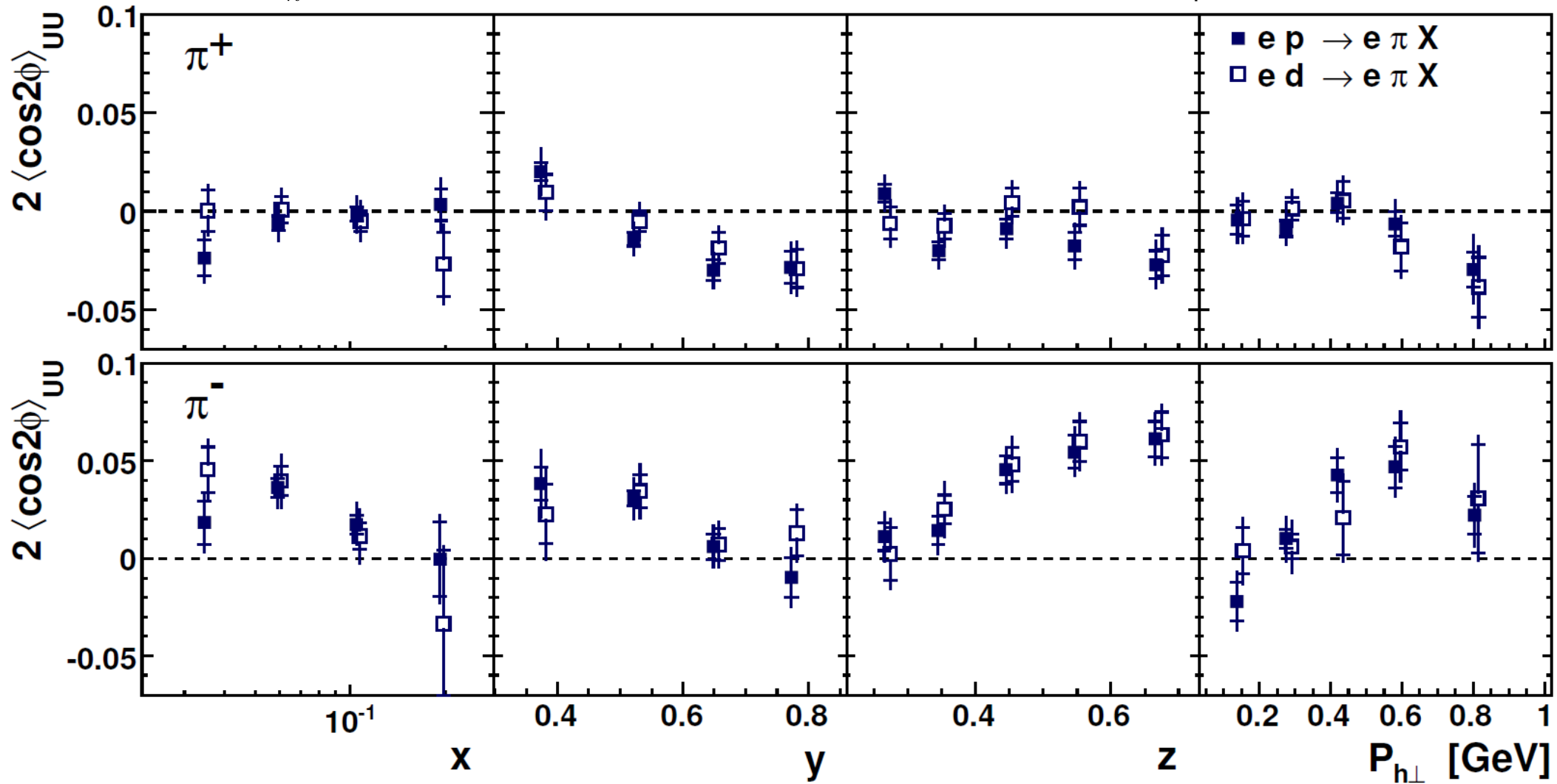
BINNING  
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# Results for $\langle \cos 2\phi_h \rangle$ : pions

$$\mathcal{I}\left[-\frac{2(\hat{P}_{h\perp}\cdot\vec{k}_T)(\hat{P}_{h\perp}\cdot\vec{p}_T) - \vec{k}_T\cdot\vec{p}_T}{M_h M} h_1^\perp H_1^\perp\right]$$

A. Airapetian et al., arXiv:1204.4161

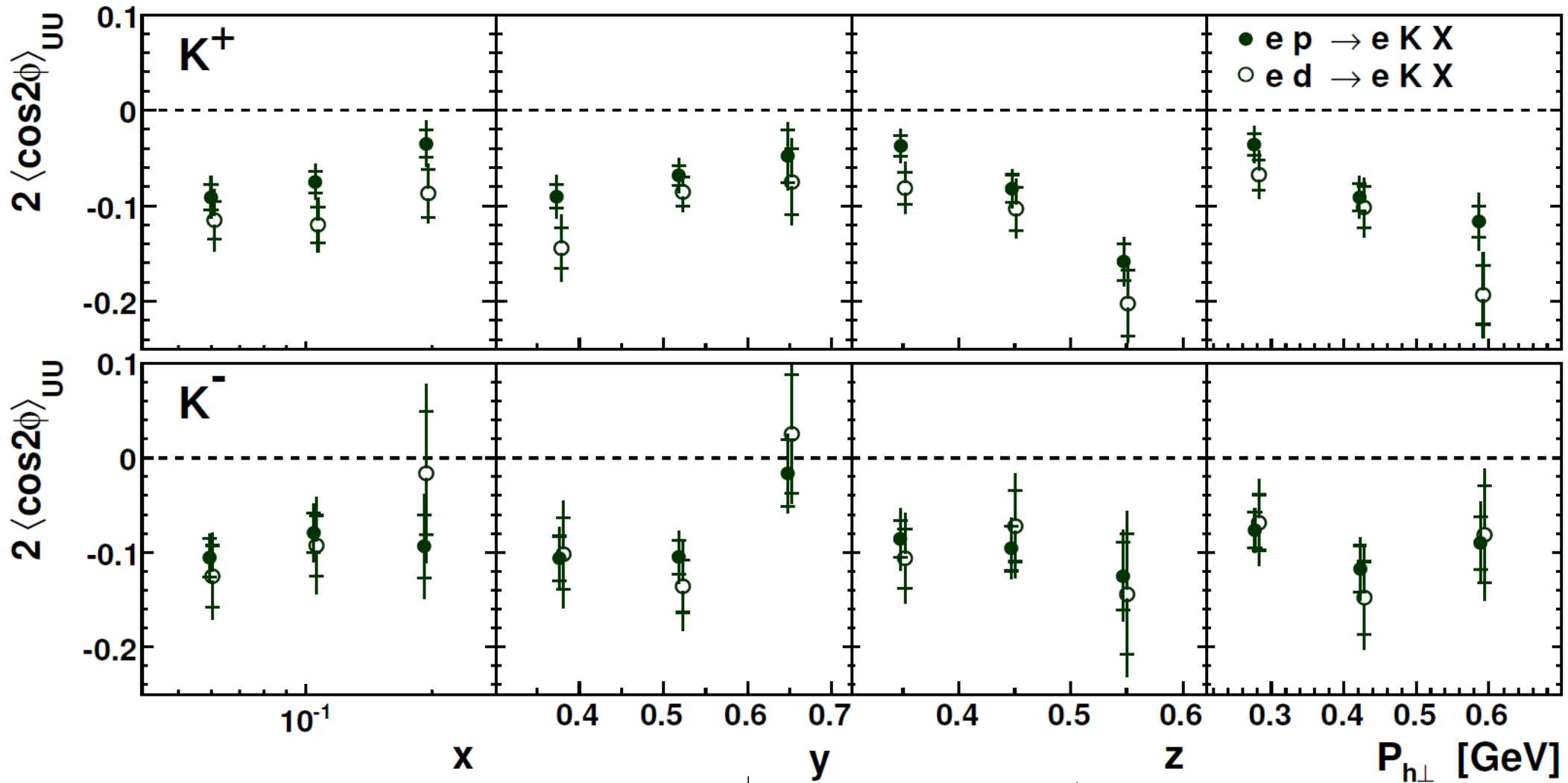


- H-D comparison:  $h_1^{\perp,u} \approx h_1^{\perp,d}$
- $\pi^- > 0 \longleftrightarrow \pi^+ \leq 0$ :  $H_1^{\perp, fav} \approx -H_1^{\perp, unfav}$

# Results for $\langle \cos 2\phi_h \rangle$ : kaons

$$\mathcal{I}\left[-\frac{2(\hat{P}_{h\perp} \cdot \vec{k}_T)(\hat{P}_{h\perp} \cdot \vec{p}_T) - \vec{k}_T \cdot \vec{p}_T}{M_h M} h_1^\perp H_1^\perp\right]$$

A. Airapetian et al., arXiv:1204.4161



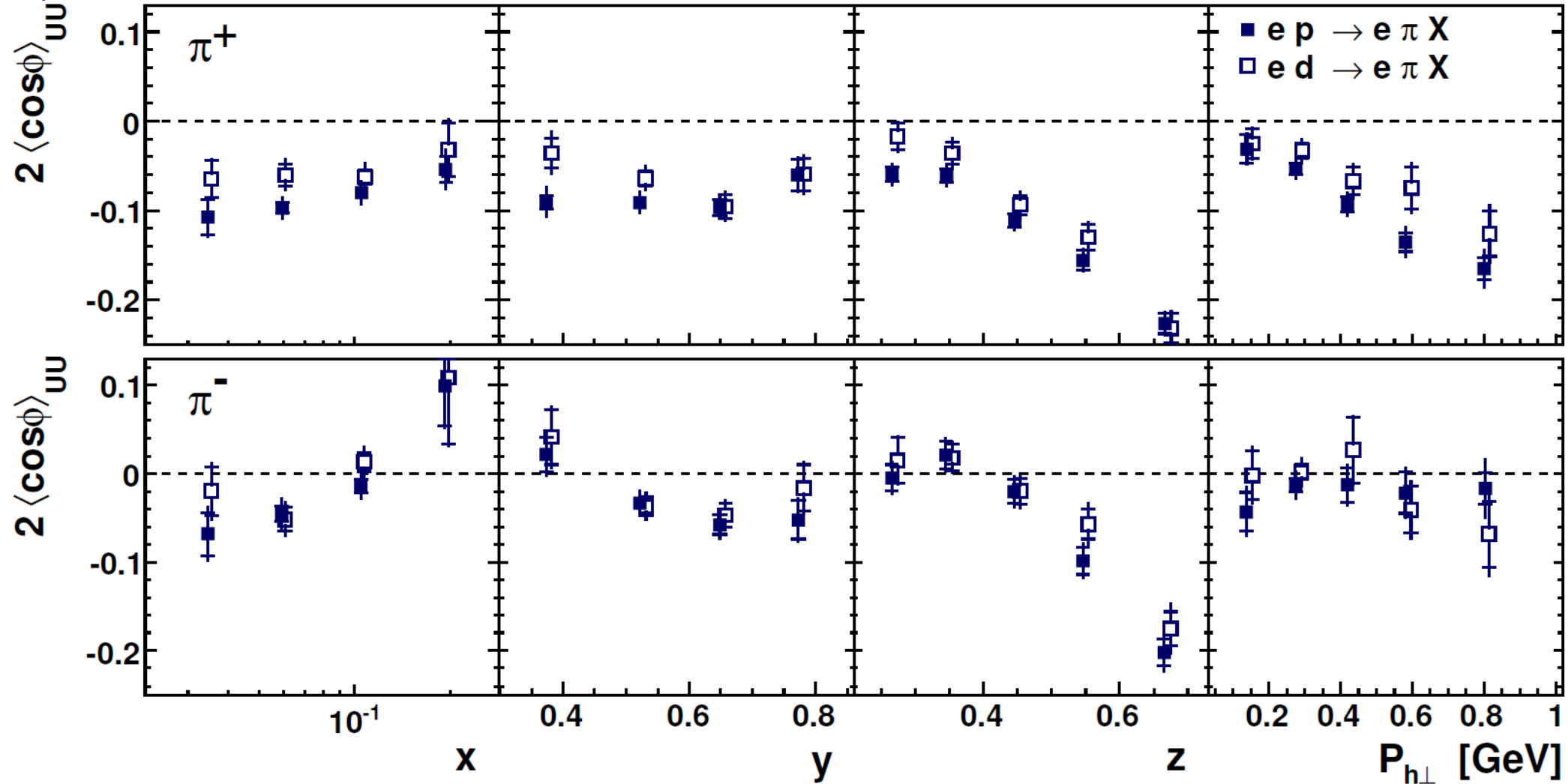
- $K^+ < 0$ : - Artru model:  $\text{sign } H_1^\perp, u \rightarrow K^+ = \text{sign } H_1^\perp, u \rightarrow \pi^+$
- $K^- \approx K^+$ : - u-dominance  $\xrightarrow{?} H_1^\perp, u \rightarrow K^+ \approx H_1^\perp, u \rightarrow K^-$   
- role of sea-quarks



# Results for $\langle \cos \phi_h \rangle$ : pions

$$\frac{2M}{\mathcal{Q}} \mathcal{I} \left[ -\frac{\hat{P}_{h\perp} \cdot \vec{k}_T}{M} f_1 D_1 - \frac{\hat{P}_{h\perp} \cdot \vec{p}_T}{M_h} \frac{k_T^2}{M^2} h_1^\perp H_1^\perp + \dots \right]$$

A. Airapetian et al., arXiv:1204.4161

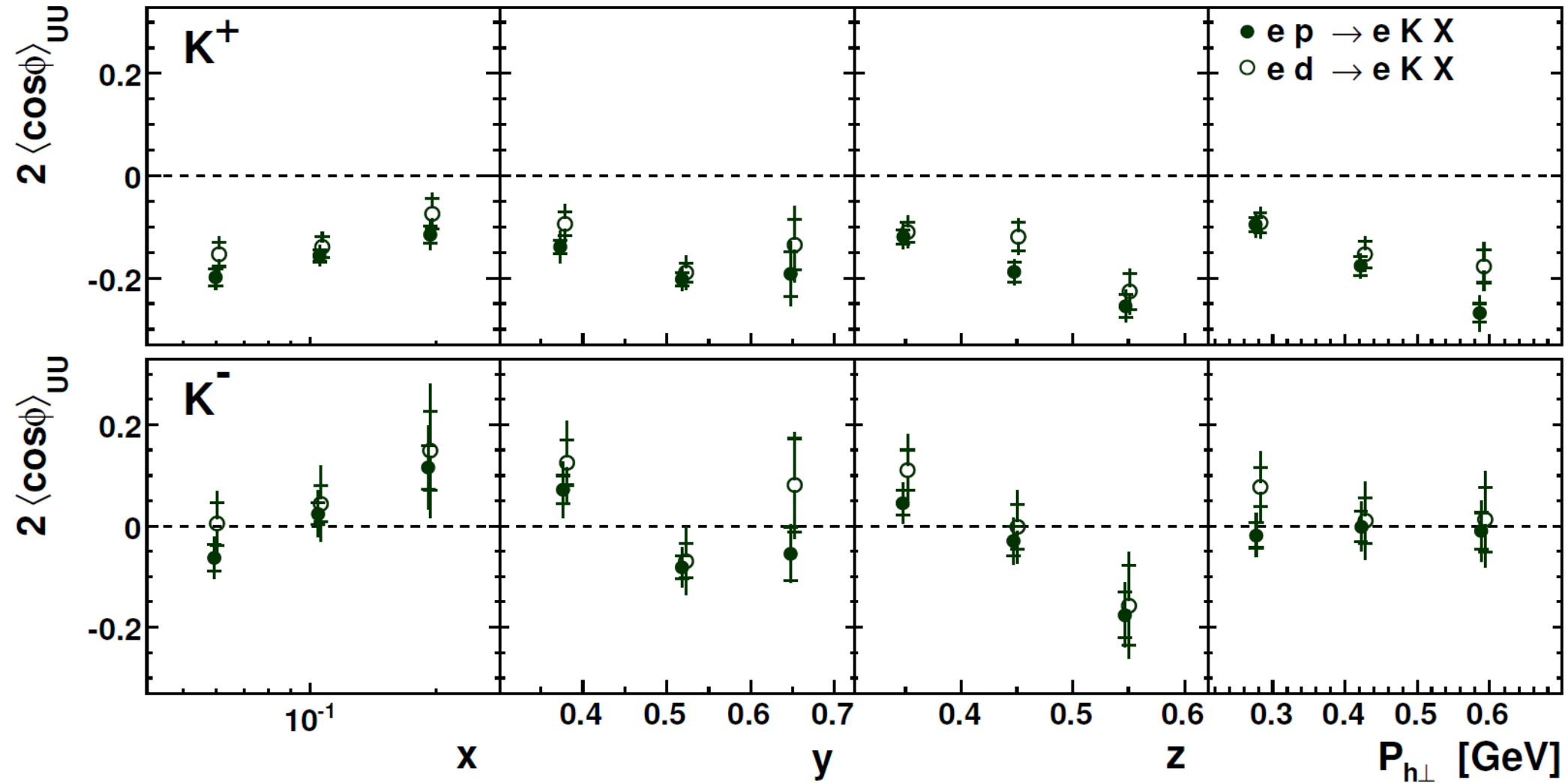


- H-D comparison: weak flavor dependence
- magnitude increases with  $z$
- $\pi^+$ : magnitude increases with  $P_{h\perp}$

# Results for $\langle \cos \phi_h \rangle$ : kaons

$$\frac{2M}{Q} \mathcal{I} \left[ -\frac{\hat{P}_{h\perp} \cdot \vec{k}_T}{M} f_1 D_1 - \frac{\hat{P}_{h\perp} \cdot \vec{p}_T}{M_h} \frac{k_T^2}{M^2} h_1^\perp H_1^\perp + \dots \right]$$

A. Airapetian et al., arXiv:1204.4161



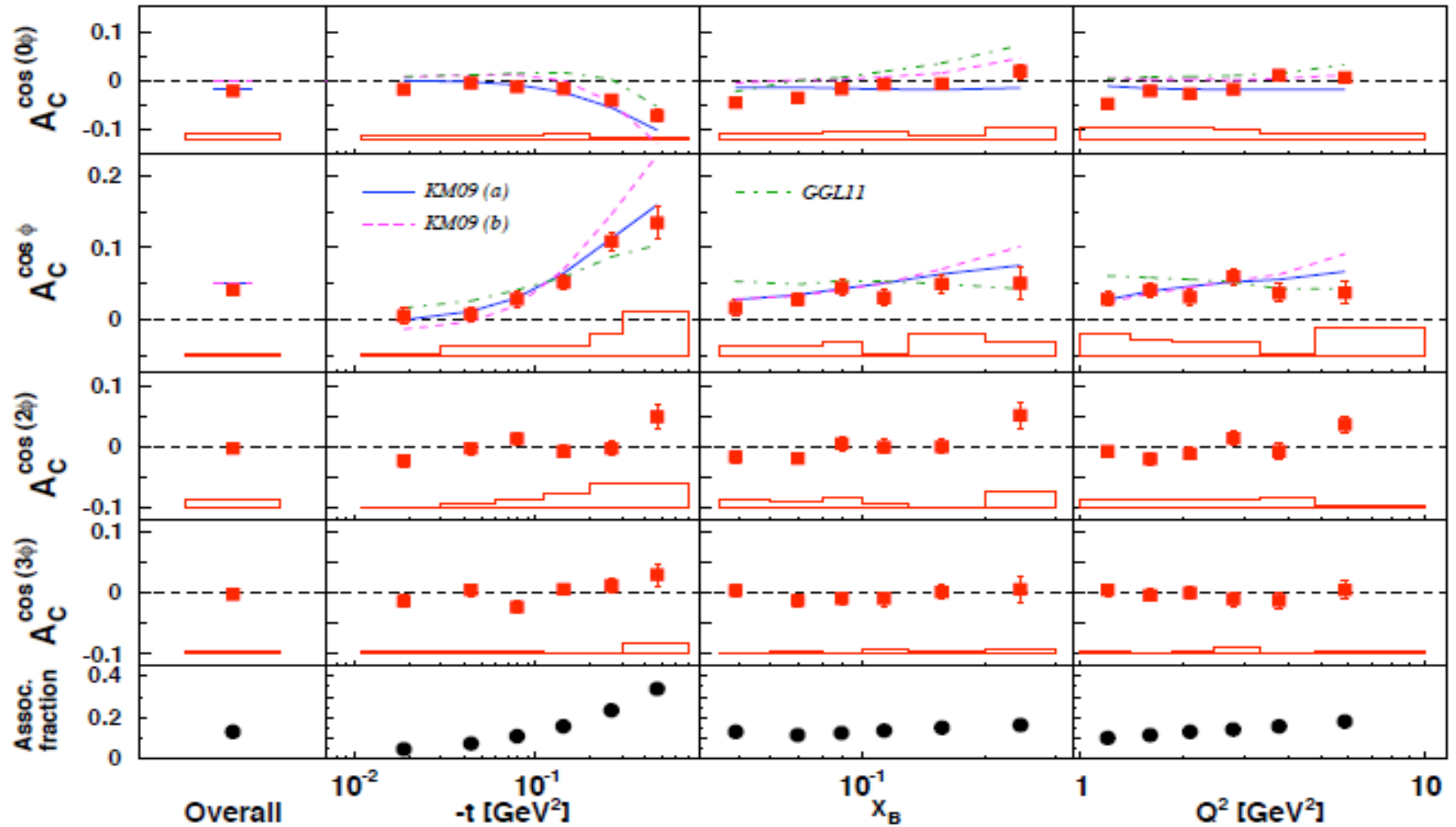
- $K^+ < 0$ , larger in magnitude than  $\pi^+$
- $K^- \approx 0$

# Summary

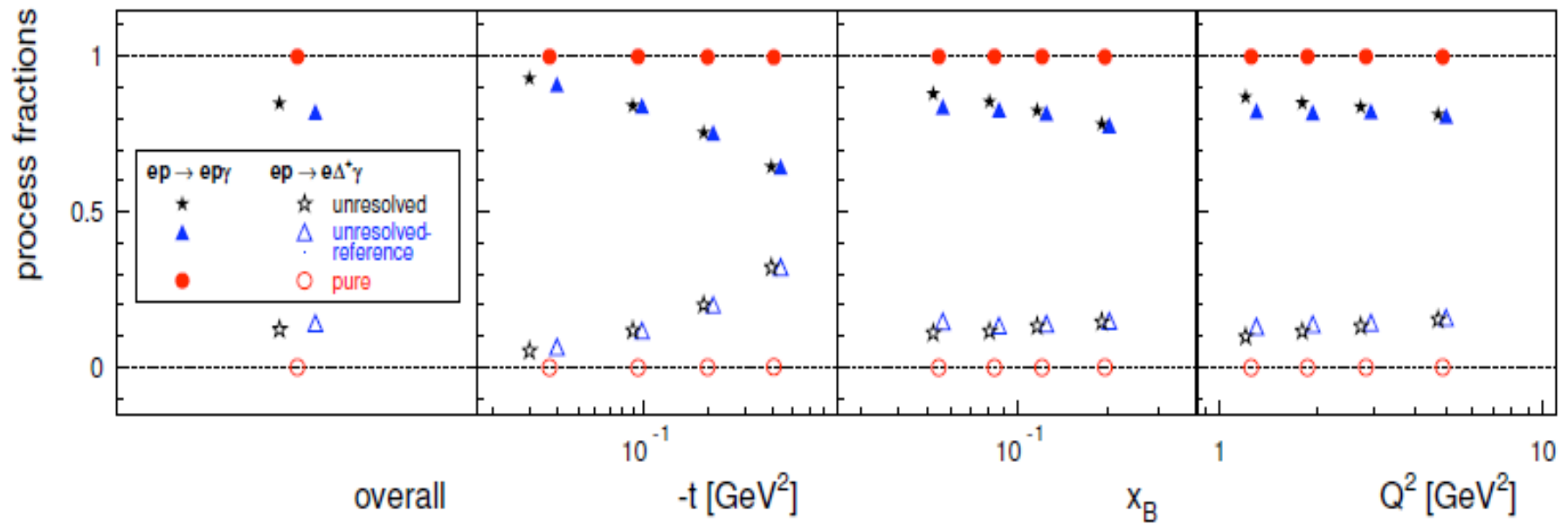
- DVCS beam-helicity asymmetries:
  - complete data set: large increase in statistics
  - complete event reconstruction: negligible background
- significant Sivers amplitudes for  $\pi^+$  and  $K^+$  (role of sea quarks)  
non-zero orbital angular momentum
- significant Collins amplitudes for  $\pi^\pm$  and  $K^+$   
access to transversity and Collins fragmentation function
- Spin-independent non-collinear cross section:
  - evidence for non-zero Boer-Mulders distribution function and Collins fragmentation function
  - through Cahn effect constraint on quark intrinsic momentum and spin-independent transverse-momentum fragmentation functions

# Backup

# Beam-charge asymmetry



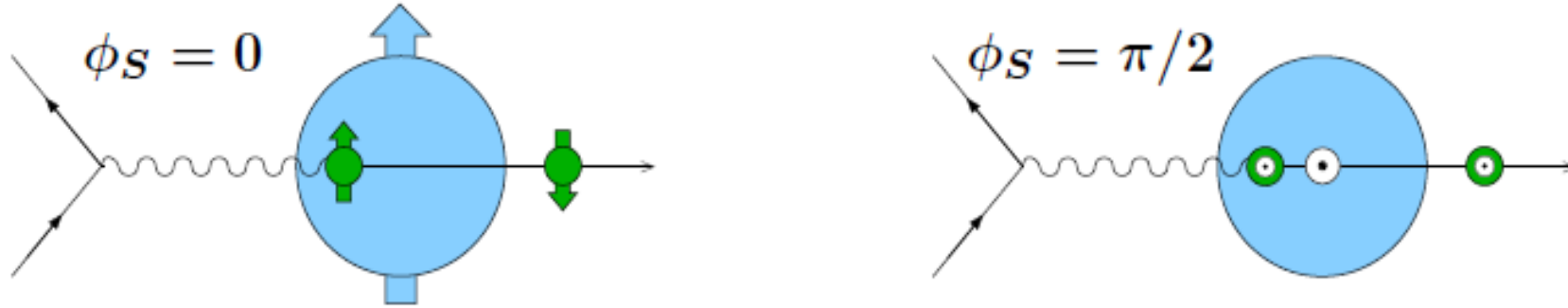
# DVCS sample purity



# Collins fragmentation function: Artru model

X. Artru et al. , Z. Phys. C73 (1997) 527

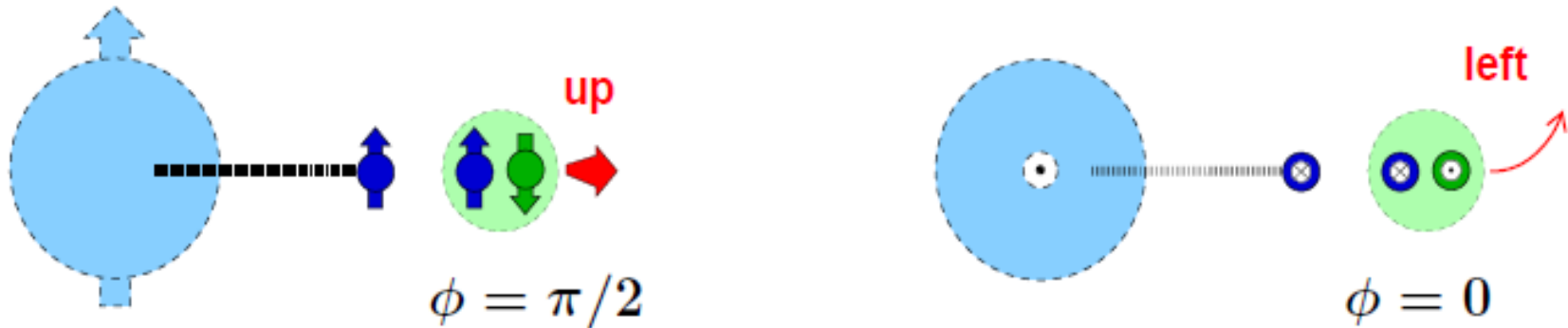
polarisation component in lepton scattering plane reversed by photoabsorption:



string break, quark-antiquark pair with vacuum numbers:

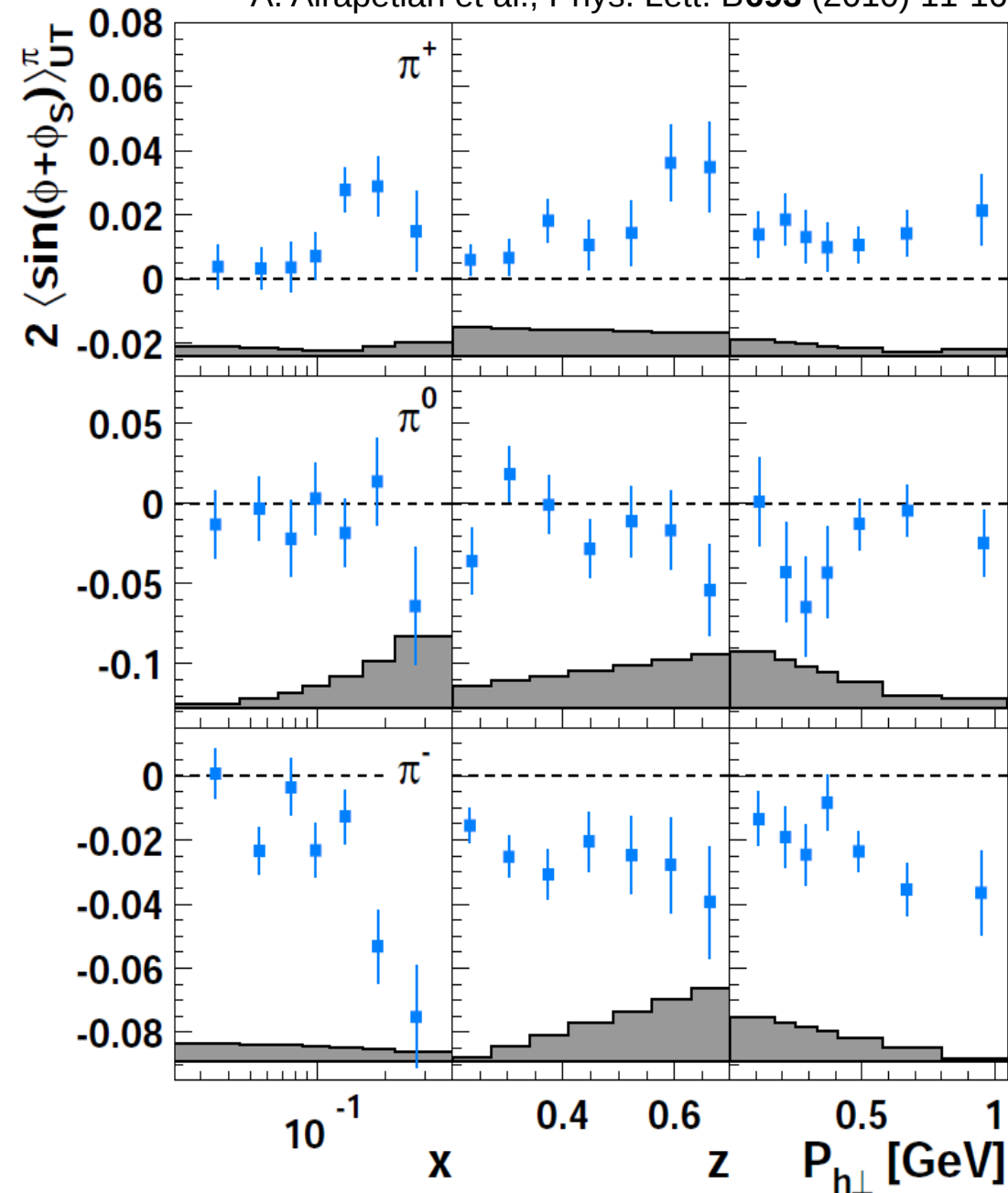


orbital angular momentum creates transverse momentum:



# Collins amplitudes for pions

A. Airapetian et al., Phys. Lett. B**693** (2010) 11-16

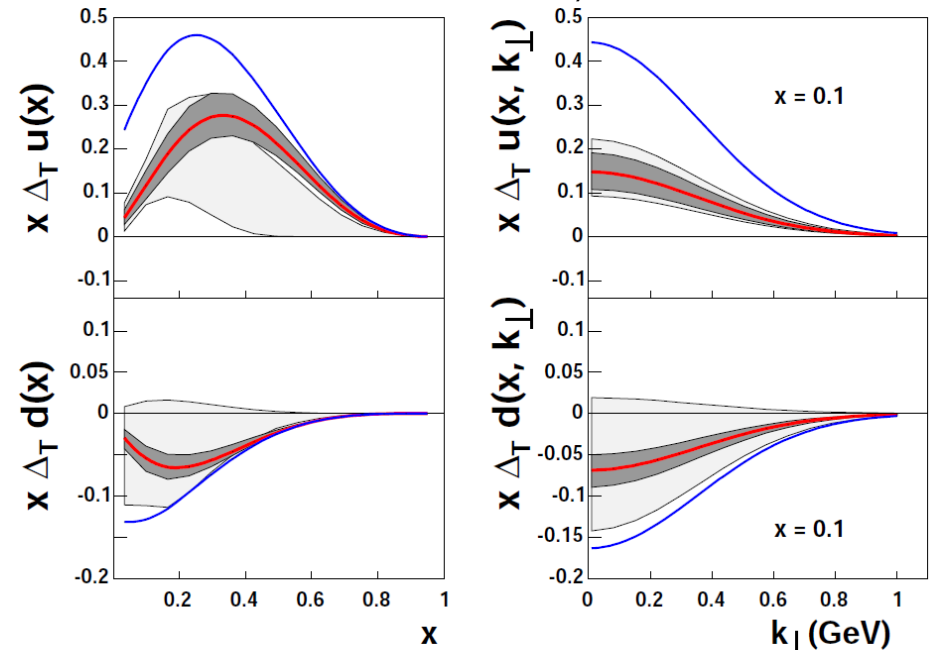


- $\pi^\pm$  increasing with  $z$
- positive for  $\pi^+$
- large & negative for  $\pi^-$

$$H_1^{\perp, fav} \approx -H_1^{\perp, unfav}$$

- isospin symmetry fulfilled
- data from BELLE, COMPASS & HERMES  $\longrightarrow$  extraction of  $h_{1T}^q$

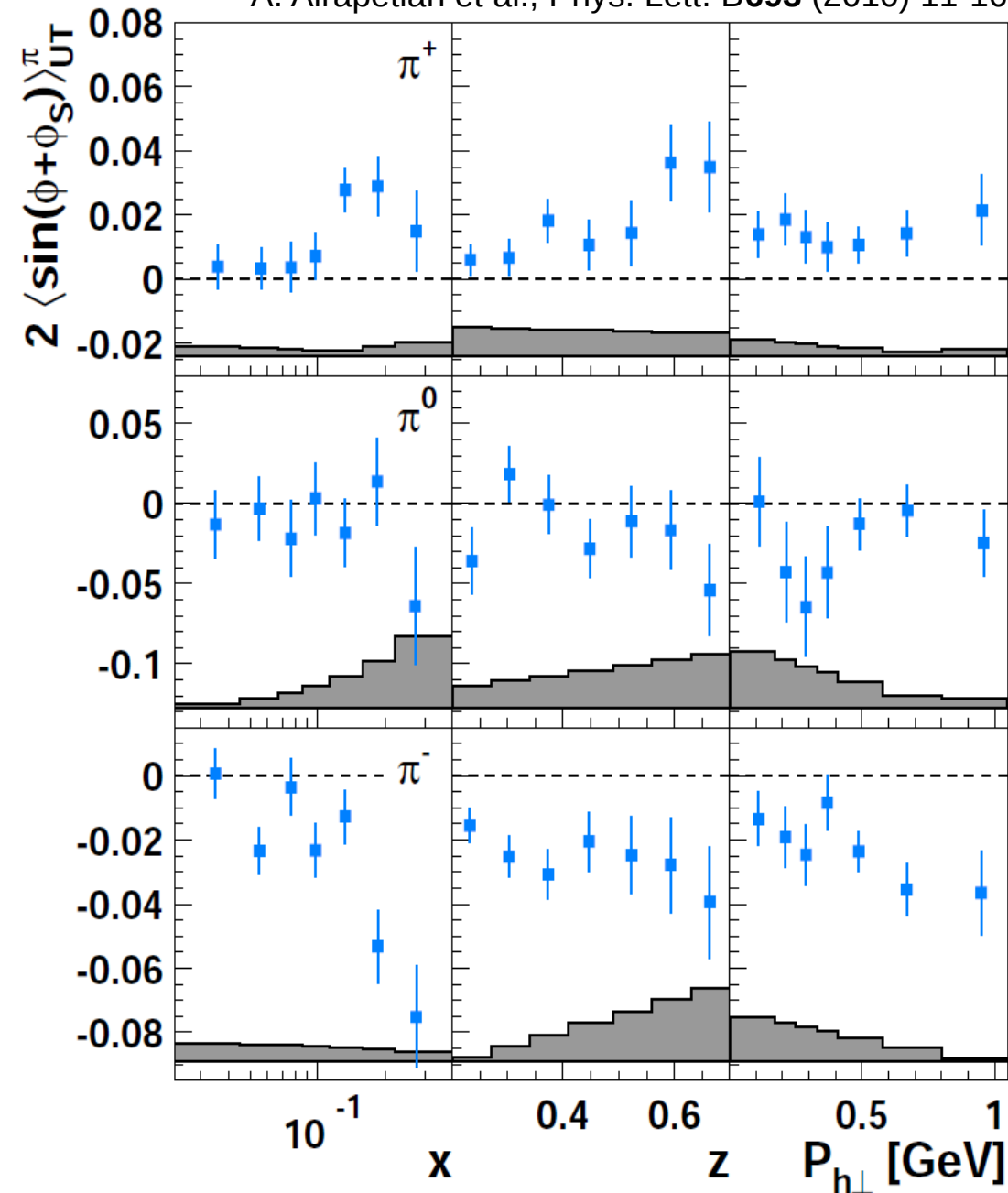
Anselmino et al., arXiv: 0807.0173





# Collins amplitudes for pions

A. Airapetian et al., Phys. Lett. B**693** (2010) 11-16

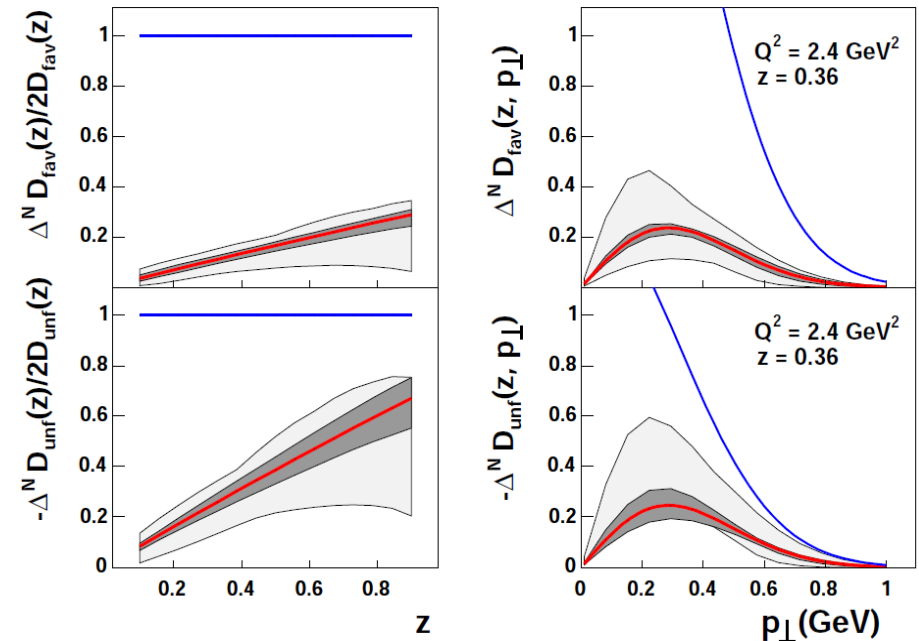


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- isospin symmetry fulfilled
- data from BELLE, COMPASS & HERMES  $\longrightarrow$  extraction of  $H_1^{\perp}$

Anselmino et al., arXiv: 0807.0173

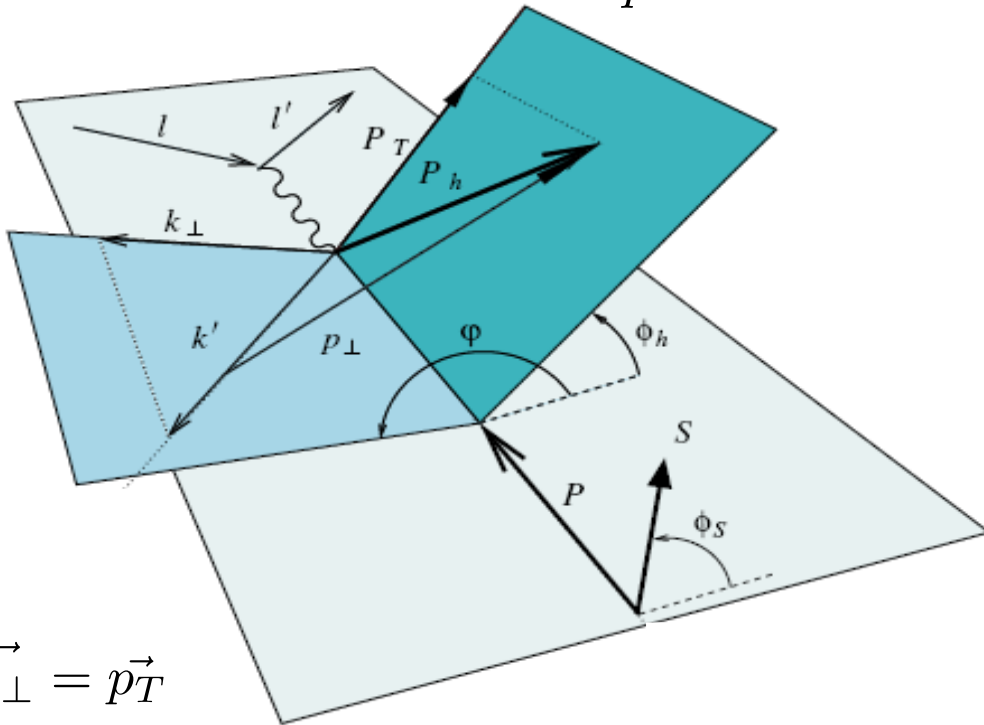


# Cahn effect

R. N. Cahn, Phys. Lett. B78:269, 1978  
 Phys. Rev. D40: 3107, 1989

M. Anselmino et al., Phys. Rev. D71:074006, 2005

$$\frac{d\sigma}{dx dQ^2 dz dP_{h\perp}^2} \sim \sum_q \int d^2 p_T f_1^q(x, p_T) \frac{d\hat{\sigma}^{lq \rightarrow lq}}{dQ^2} D_1^q(z, p_\perp) \dots$$



$$\frac{2\pi\alpha^2}{x^2 s^2} \frac{\hat{s}^2 + \hat{u}^2}{Q^4} \sim \vec{l} \cdot \vec{p}_T \sim \cos \varphi$$

and

$$\vec{P}_{h\perp} \simeq z\vec{p}_T + \vec{k}_T$$

after integration over  $p_T$  azimuthal dependence remains, reflected in  $\cos \phi_h$