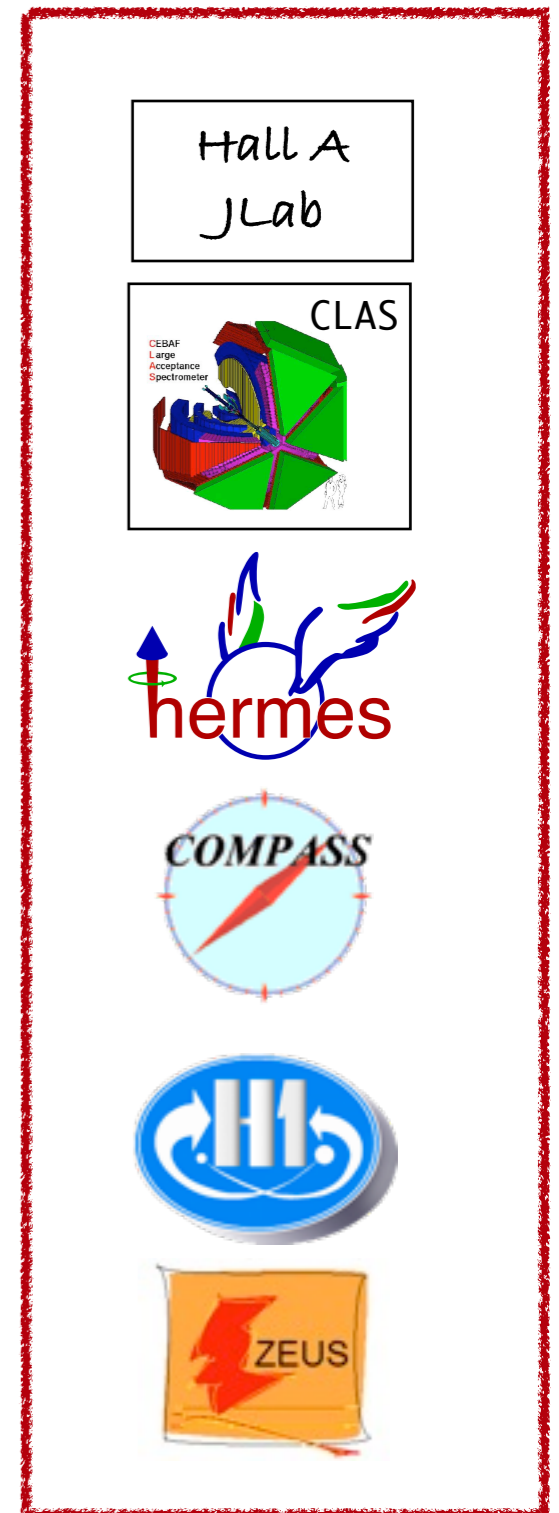
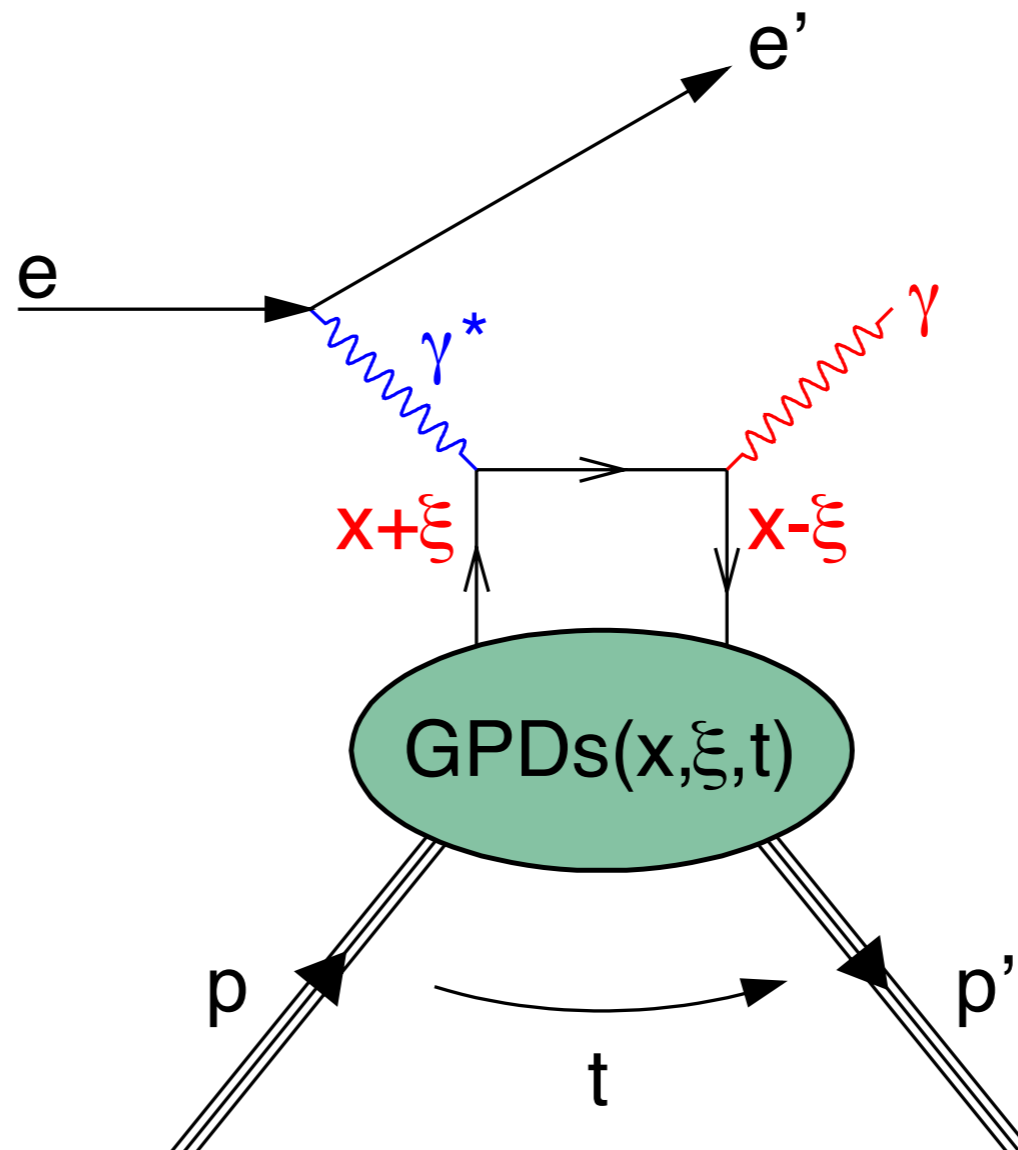


# DVCS Measurements - Past and Future

- Setting the scene
- The past and the present
- Global analysis
- The future



Caroline K. Riedl



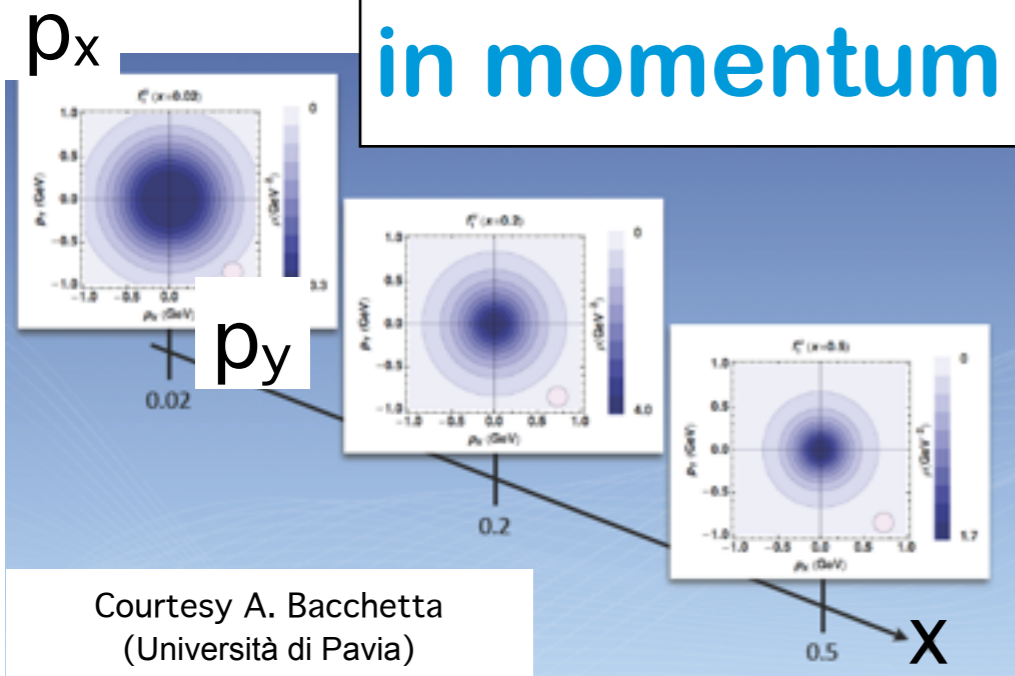
ILLINOIS  
UNIVERSITY OF ILLINOIS AT URBANA-CHAMPAIGN

5th Workshop of the APS Topical  
Group on Hadronic Physics (GHP 2013)  
Denver, April 11, 2013

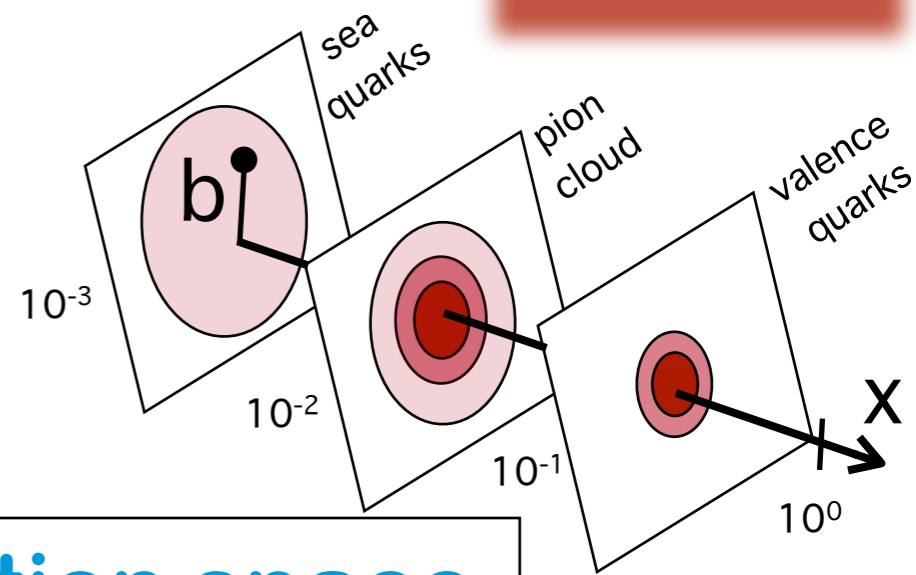
# Nucleon Tomography



in momentum space



in position space



Correlation between **spin** and **transverse momentum** ?

Correlation between **longitudinal momentum** and **transverse position** ?

Transverse Momentum dependent PDFs

**TMDs**  
 $f(x, k_{\perp})$

**GPDs**  
 $H(x, b_{\perp})$   
 $\leftrightarrow$  FT  $\leftrightarrow$   $H(x, \xi, t)$

Generalized Parton Distributions

$k_{\perp}$ -integration

PDFs  $q(x)$ , 1D:  
Parton Distribution Functions

$\xi=0, t=0$

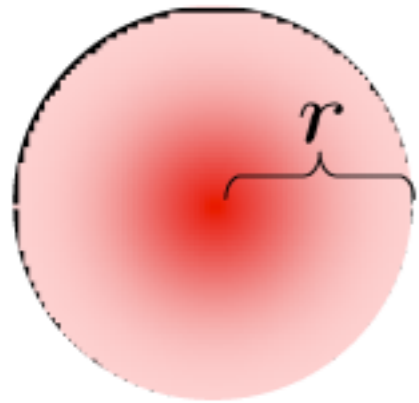
semi-inclusive measurements

inclusive measurements

exclusive measurements

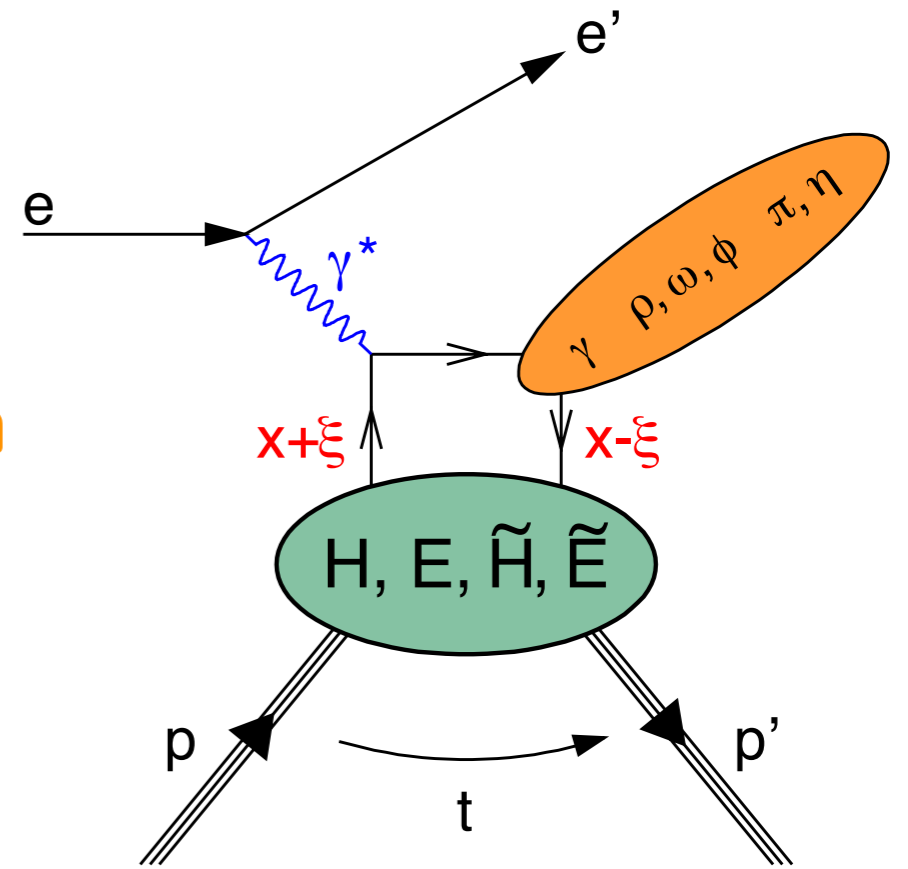
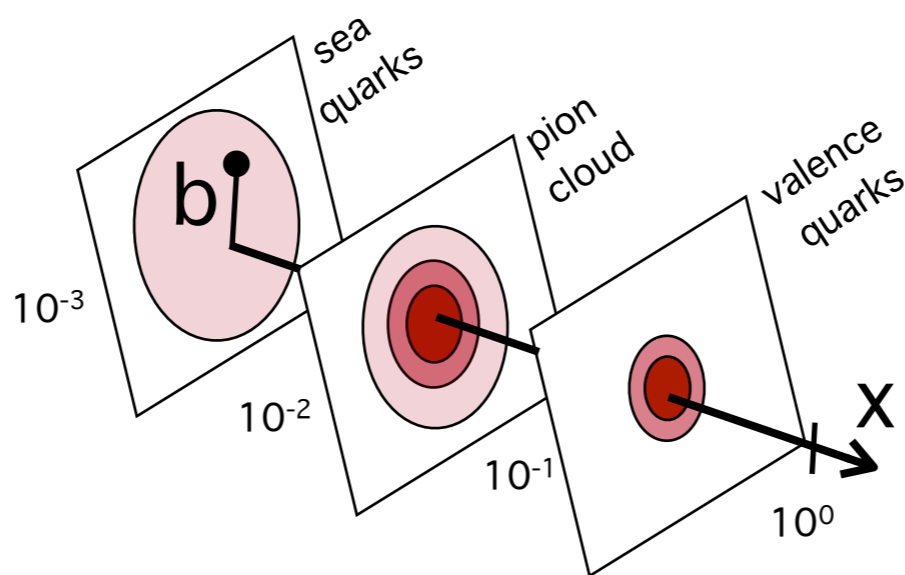
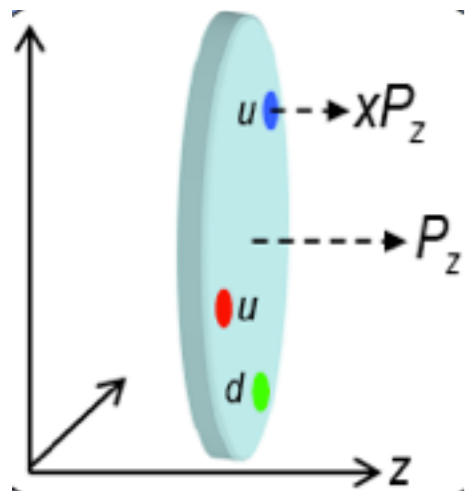
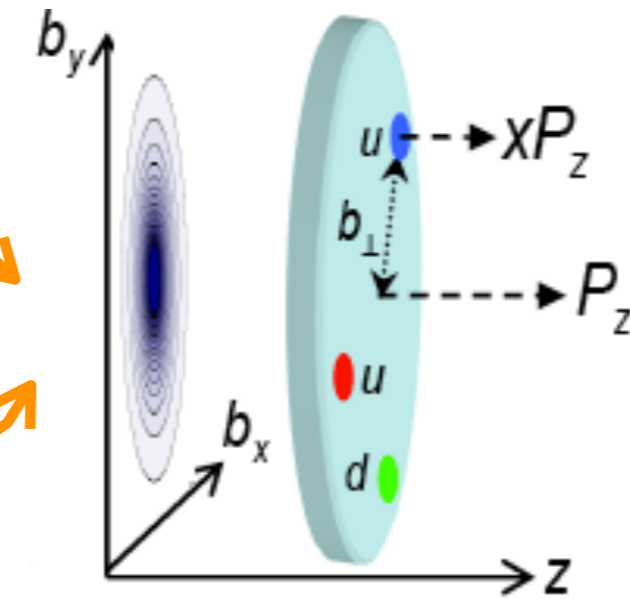
# Nucleon tomography with GPDs

## Generalized Parton Distributions



**Form Factors:**  
transverse parton positions

**Parton Distribution Functions:**  
longitudinal momentum



- $x, \xi$  : longitudinal momentum fractions of probed quark
- $t$  : 4-momentum<sup>2</sup> transfer to target
- **DVCS: Deeply Virtual Compton Scattering** = electroproduction of a real photon

4 chiral-even quark GPDs at leading twist:

Spin-1/2	flips nucleon helicity	conserves nucleon helicity
does not depend on quark helicity	<b>E</b>	<b>H</b> → $q^+ + q^-$
depends on quark helicity	$\tilde{E}$	$\tilde{H}$ → $q^+ - q^-$

forward limit  $\xi \rightarrow 0, t \rightarrow 0$

Illustrations: Ph. Högler (TUM)

# DVCS as laboratory for probing hadrons

## Access to Generalized Parton Distributions

“Nucleon Tomography”

Global analysis requires measurements

of cross-sections and

of azimuthal asymmetries related to beam charge, beam helicity, target polarization

preferably covering wide kinematic range

1.

## Access to total

angular momentum of

quarks through Ji

sum rule

$$J_q = \frac{1}{2} \lim_{t \rightarrow 0} \int_{-1}^1 dx x [H^q(x, \xi, t) + E^q(x, \xi, t)]$$

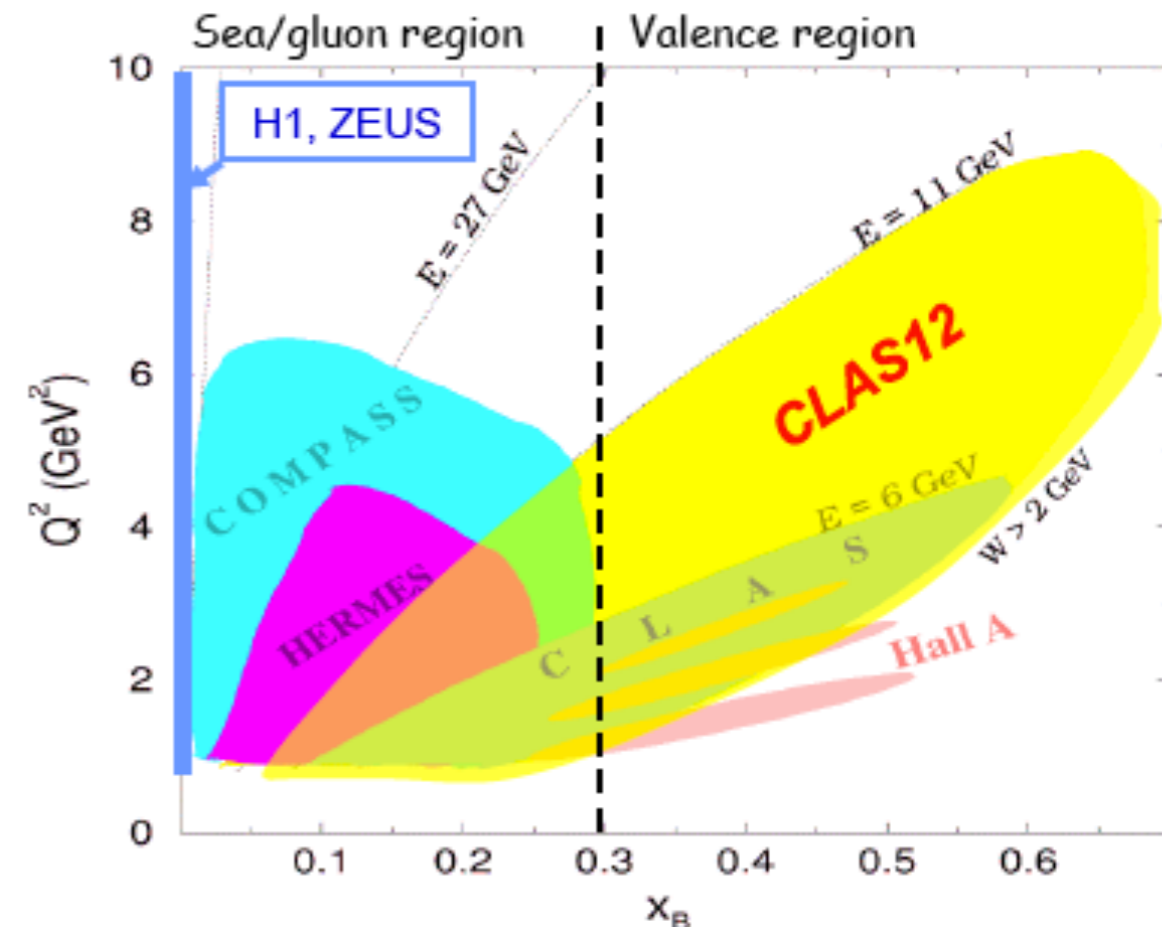
-Ji, PRL 78 (1997) 610-

3.

DVCS on hadrons other than the nucleon

Spin-1: tensor and coherent signatures?

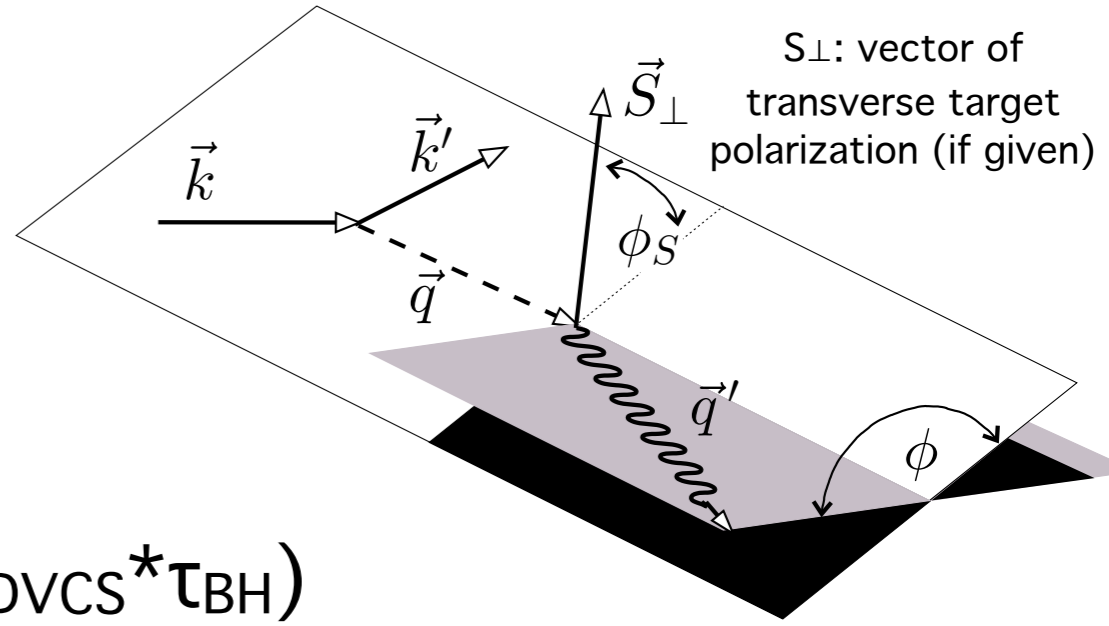
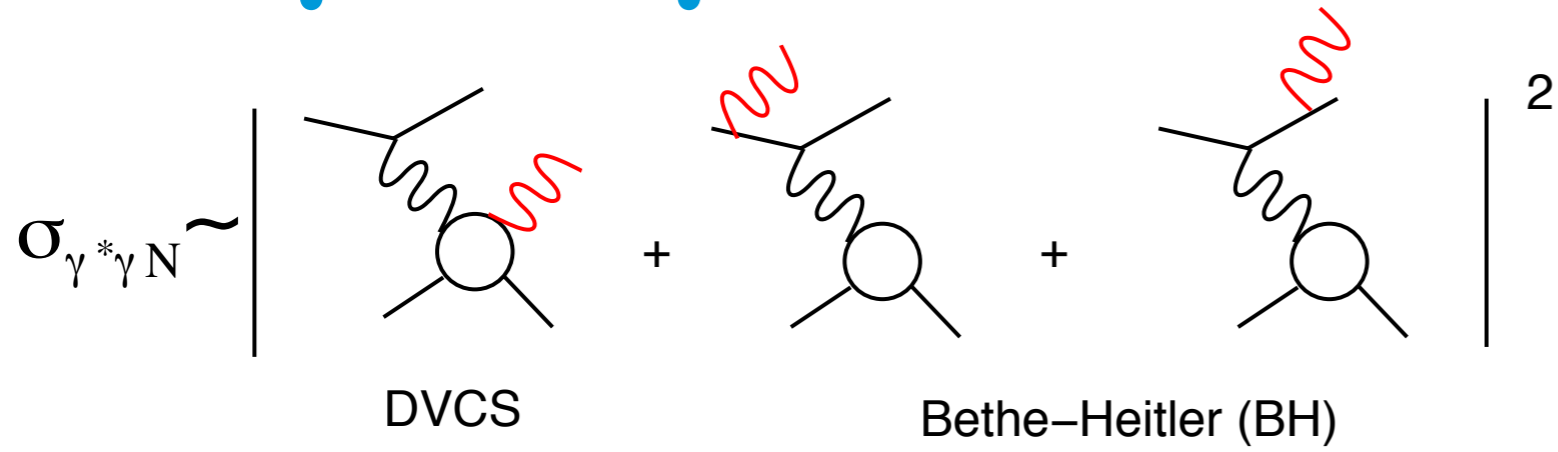
How does the nuclear environment modify the DVCS amplitude?



See also talk by Lekha Adhikari Wednesday afternoon, “Distribution of Angular Momentum in the Transverse Plane”

# The $\gamma^*N \rightarrow \gamma N$ cross section

lepton beam  $k$  with charge  $C_B$  and helicity  $P_B$



$$= |\tau_{\text{DVCS}}|^2 + |\tau_{\text{BH}}|^2 + (\tau_{\text{DVCS}}\tau_{\text{BH}}^* + \tau_{\text{DVCS}}^*\tau_{\text{BH}})$$

**DVCS-BH interference term**

high energy:  
 $|\tau_{\text{DVCS}}|^2 \approx |\tau_{\text{BH}}|^2$   
 low energy:  
 $|\tau_{\text{DVCS}}|^2 \ll |\tau_{\text{BH}}|^2$

exactly calculable in QED given nucleon elastic form factors

**Amplifies contribution of  $\tau_{\text{DVCS}}$**

All 3 contributions can be written as harmonic series wrt  $\phi$  (and  $\phi_S$ )

Measure azimuthal asymmetries....:

$$\sigma(\phi; P_B, C_B) = \sigma_{\text{UU}}(\phi) \cdot [1 + P_B A_{\text{LU}}^{\text{DVCS}}(\phi) + C_B P_B A_{\text{LU}}^{\text{I}}(\phi) + C_B A_{\text{C}}(\phi)]$$

... or measure **helicity-dependent** cross section,  
 $\Delta\sigma = \sigma(\rightarrow) - \sigma(\leftarrow)$   
 and **helicity-independent** cross section,  
 $\Sigma\sigma = \sigma(\rightarrow) + \sigma(\leftarrow)$

**Holographic principle** Belitsky, Müller, hep-ph/0206306

- BH reference amplitude magnifies DVCS
- Measure magnitude  $A$  (**real part**) and phase  $\varphi$  (**imaginary part**) of DVCS amplitude  $\tau_{\text{DVCS}} = Ae^{i\varphi}$

# Parameterization of observables in terms of GPDs / CFFs

**Harmonic analysis**  
of DVCS data with respect to beam helicity, beam charge, and/or target polarization

**Compton Form Factors:** **twist-2 GPD**

$$\mathcal{F}(\xi, t) = \sum_q \int_{-1}^1 dx C_q^\mp(\xi, x) F^q(x, \xi, t)$$

**Cross-section measurement**  
(collider example): integration over  $\Phi$

Best access

unpolarized target:

$$F_1 \mathcal{H} + \frac{x_B}{2 - x_B} (F_1 + F_2) \tilde{\mathcal{H}} - \frac{t}{4M^2} F_2 \mathcal{E}$$

dominant for the proton

dominant for the neutron

longitudinally polarized target:

$$\frac{x_B}{2 - x_B} (F_1 + F_2) \left( \mathcal{H} + \frac{x_B}{2} \mathcal{E} \right) + F_1 \tilde{\mathcal{H}} - \frac{x_B}{2 - x_B} \left( \frac{x_B}{2} F_1 + \frac{t}{4M^2} F_2 \right) \tilde{\mathcal{E}}$$

transversely polarized target:

$$\frac{t}{4M^2} \left[ (2 - x_B) F_1 \mathcal{E} - 4 \frac{1 - x_B}{2 - x_B} F_2 \mathcal{H} \right]$$

$$\frac{d\sigma}{dt}(W, t, Q^2) \approx \frac{4\pi\alpha^2}{Q^4} \frac{W^2 \xi^2}{W^2 + Q^2} \left[ |\mathcal{H}|^2 - \frac{t}{4M^2} |\mathcal{E}|^2 \right] (\xi, t, Q^2) \Big|_{\xi = \frac{Q^2}{2W^2 + Q^2}}$$

# Facilities with results available

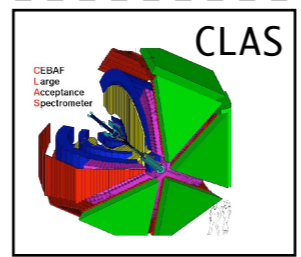
Jefferson Laboratory  
HERA  
energy

polarized  $e^-$  beam

electrons: 6 GeV

e-beam on fixed target

Hall A  
JLab



Targets:

- unpolarized p [E00-110]
- unpolarized d ( $\rightarrow$  n) [E03-106]

detected particles:  
 $e\gamma$

Targets:

- unpolarized p
- longitudinally polarized p
- $^4\text{He}$

detected particles:  
no Inner Calo:  $ep$  or  $ep\gamma$   
with Inner Calo:  $ep\gamma$

self-polarized electron beam

2 lepton beam charges: electrons and positrons

electrons: 30 GeV  
protons: 920 GeV



e-beam on fixed pure gas target

- unpolarized p, d; He, N, Ne, Kr, Xe
- longitudinally polarized p, d
- transversely polarized p

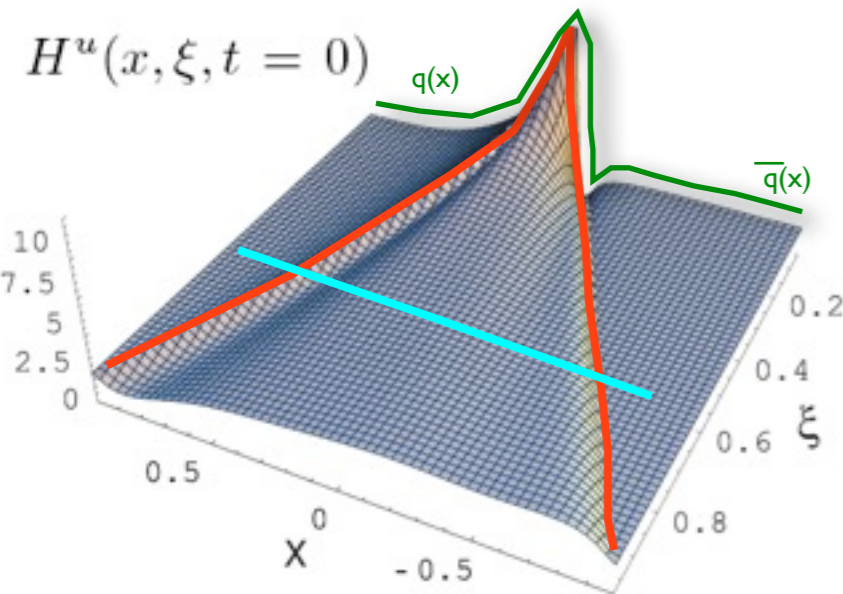
detected particles:  
no Recoil:  $e\gamma$   
with Recoil:  $ep\gamma$



ep-collider  
(unpolarized protons)

detected particles:  
 $e\gamma$  + forward veto  
ZEUS subsample:  $ep\gamma$

# Hall A (E00-110): cross section in the valence quark region

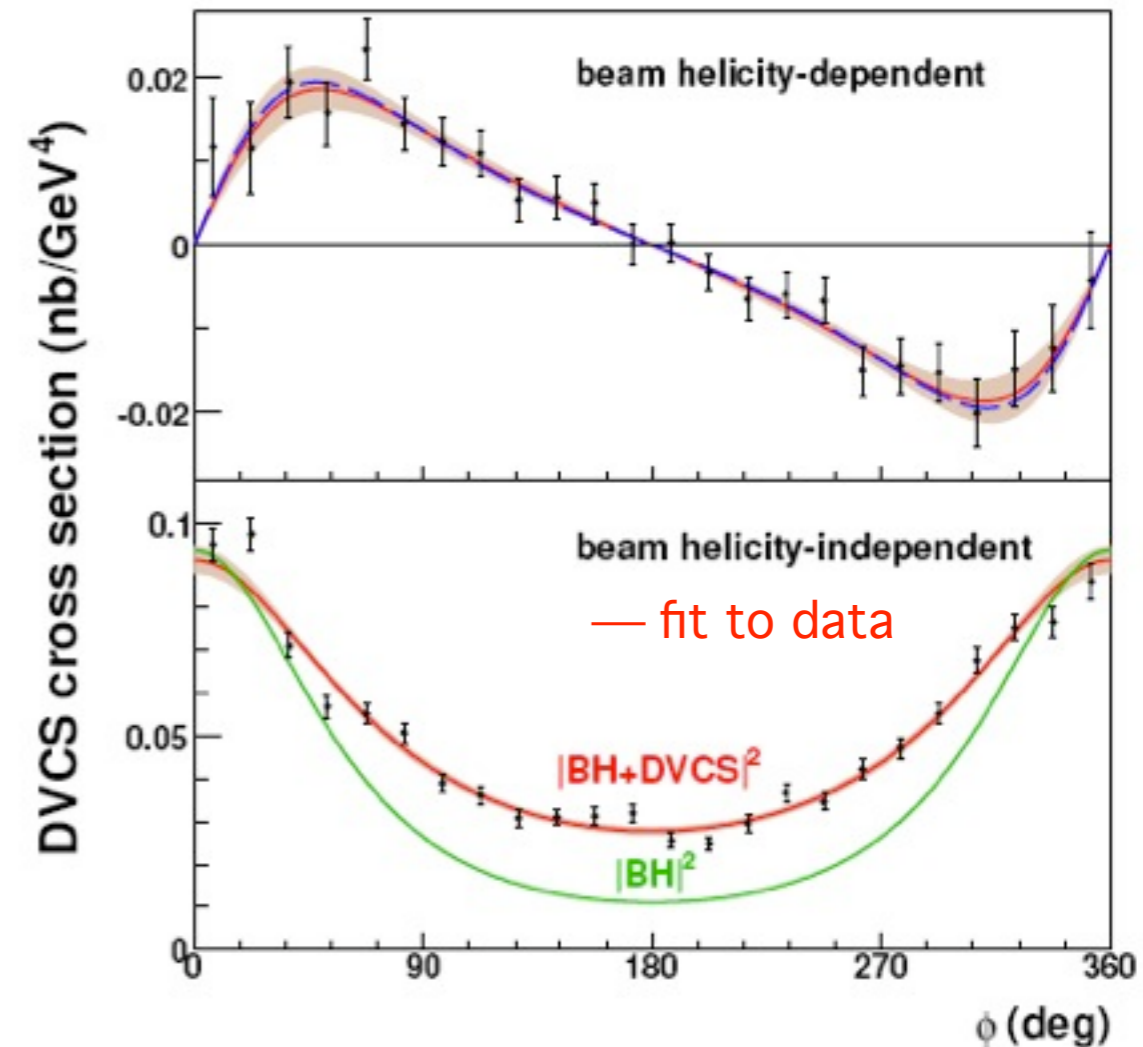


Goeke, Polyakov, Vanderhaeghen,  
hep-ph/0106012

$\Delta\sigma$   
helicity-dependent  
→  $\text{Im}(\tau_{\text{DVCS}})$   
GPDs @  $x=\xi$

$\Sigma\sigma$   
helicity-independent  
→  $\text{Re}(\tau_{\text{DVCS}})$   
integral of GPDs over  $x$

Differential cross section vs. azimuthal angle  
Bin:  $\langle x_B \rangle = 0.36$ ,  $\langle Q^2 \rangle = 2.3 \text{ GeV}^2$ ,  $\langle t \rangle = -0.28 \text{ GeV}^2$



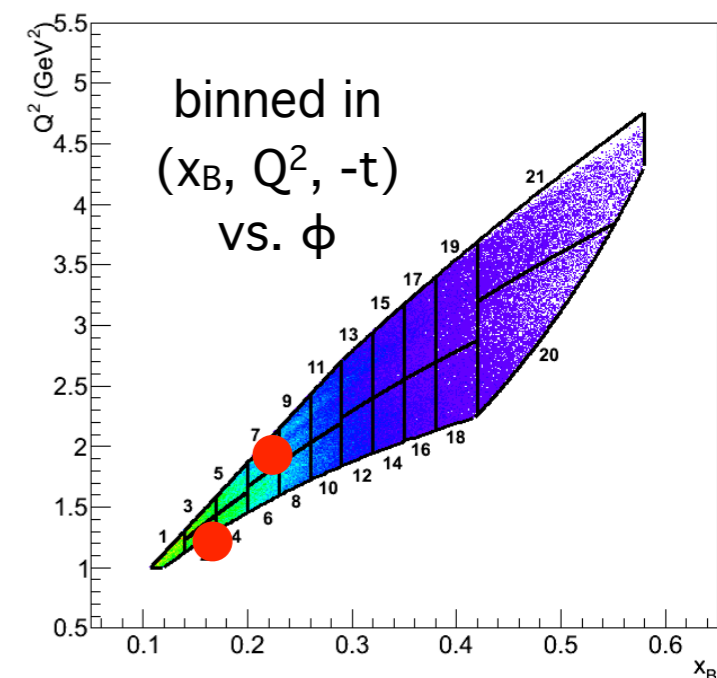
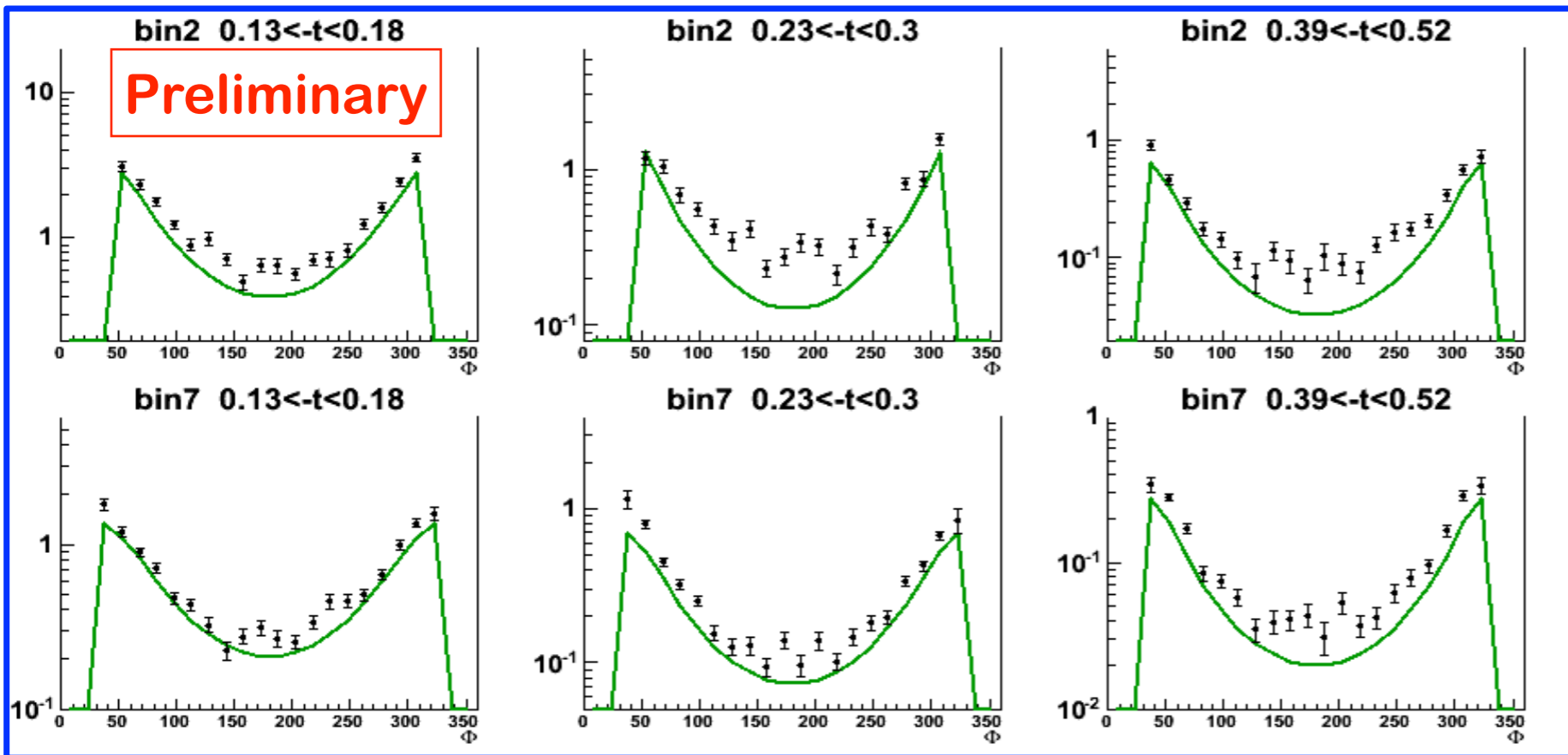
- Twist-2 (“handbag”) dominance  
→ GPDs accessible at moderate  $Q^2$ .
- No  $Q^2$  dependence of  $\text{Im}(I)$  over 1.5, 1.9 and 2.3  $\text{GeV}^2$   
→ Indication of perturbative QCD scaling behavior.

Hall A: Phys. Rev. Lett. 97, 262002 (2006)



# CLAS (e1-dvcs): cross section

GPD H  
x-section

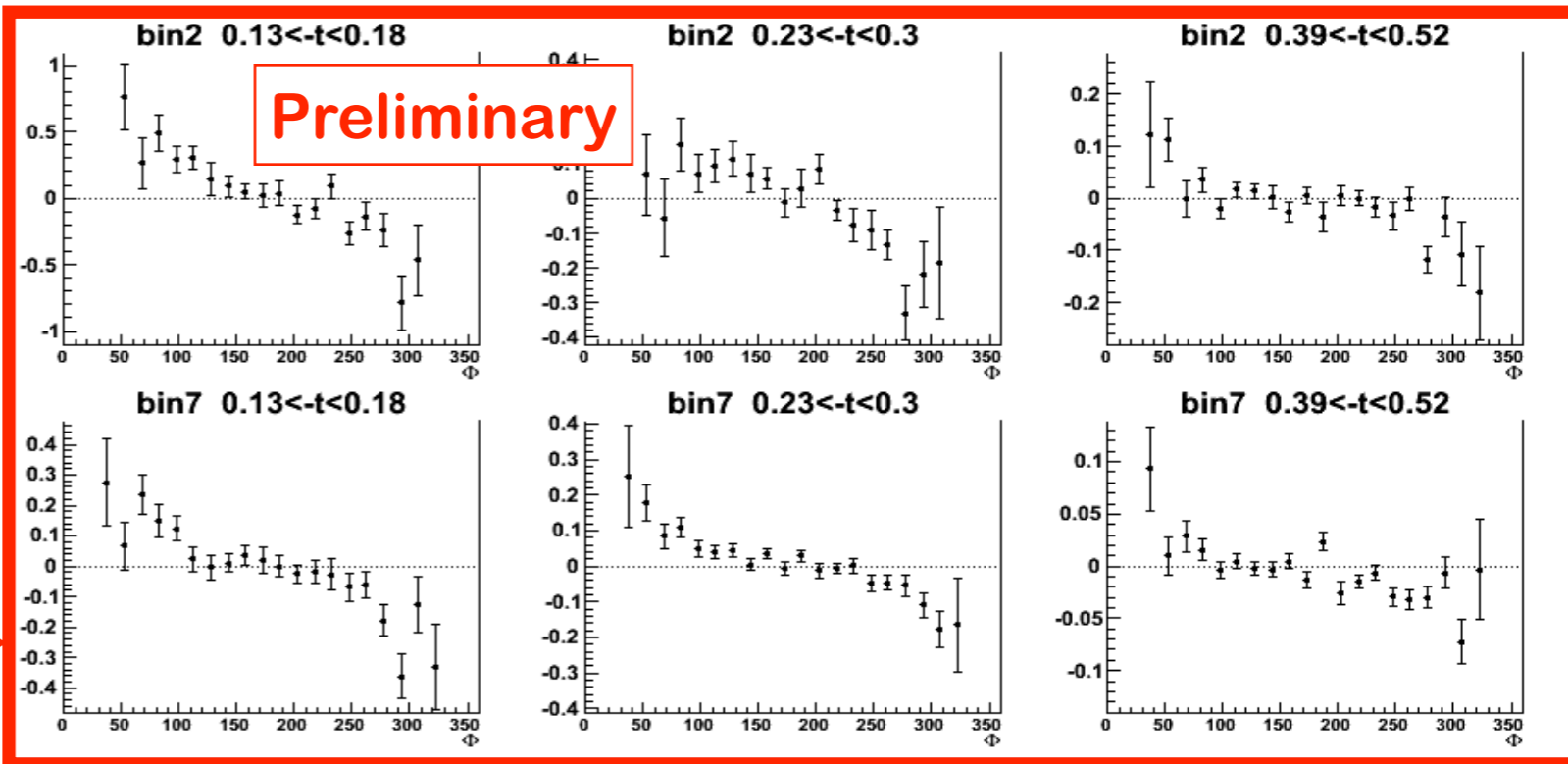


$\Sigma\sigma$   
↪  $\text{Re}(\tau_{\text{DVCS}})$

— Bethe-Heitler

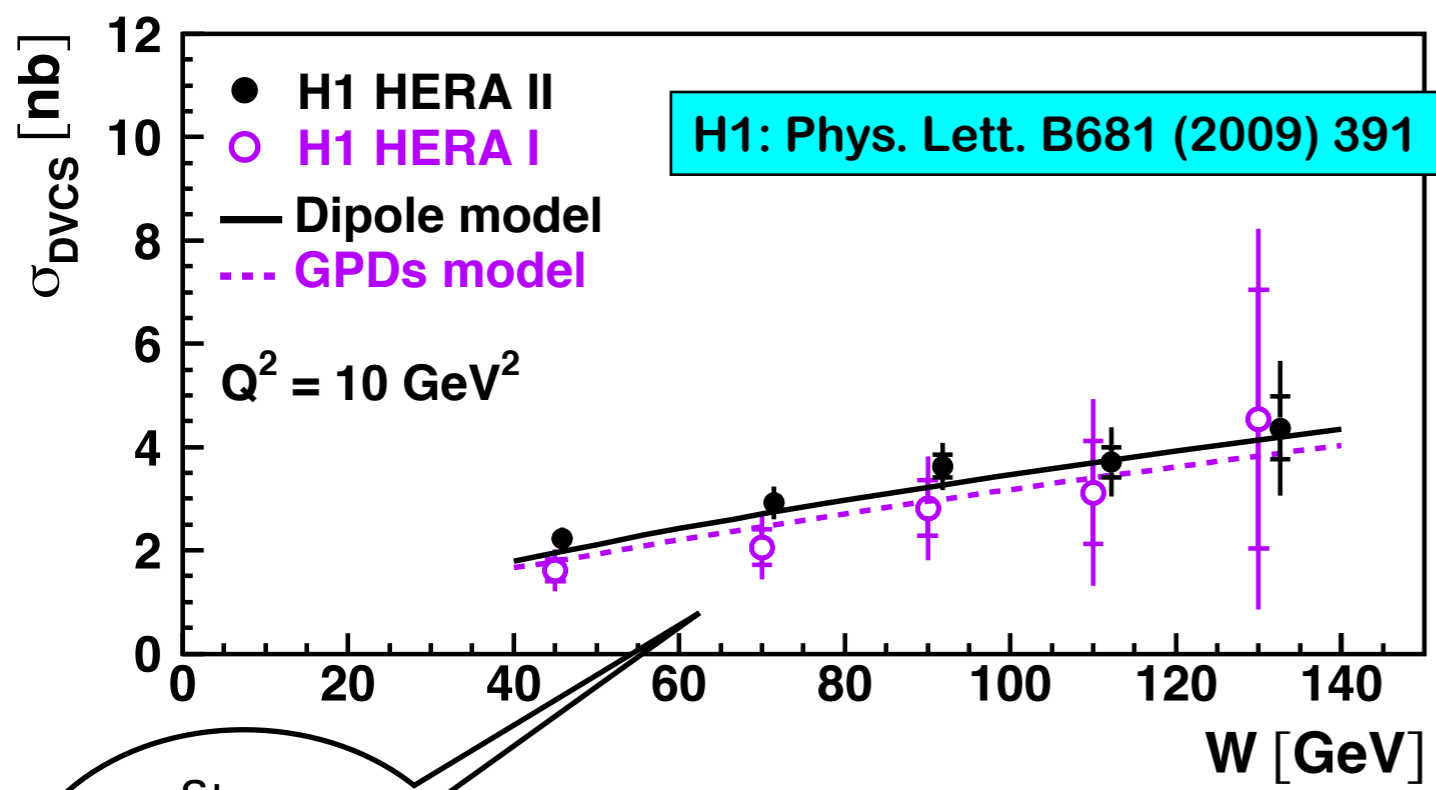
CLAS:  
preliminary  
analysis

$\Delta\sigma$   
↪  $\text{Im}(\tau_{\text{DVCS}})$



# HERA (H1 and ZEUS): cross section in the sea/glue region

Ansatz:  $d\sigma/dt \propto \exp(-b|t|)$   
t-slope:  
average impact parameter



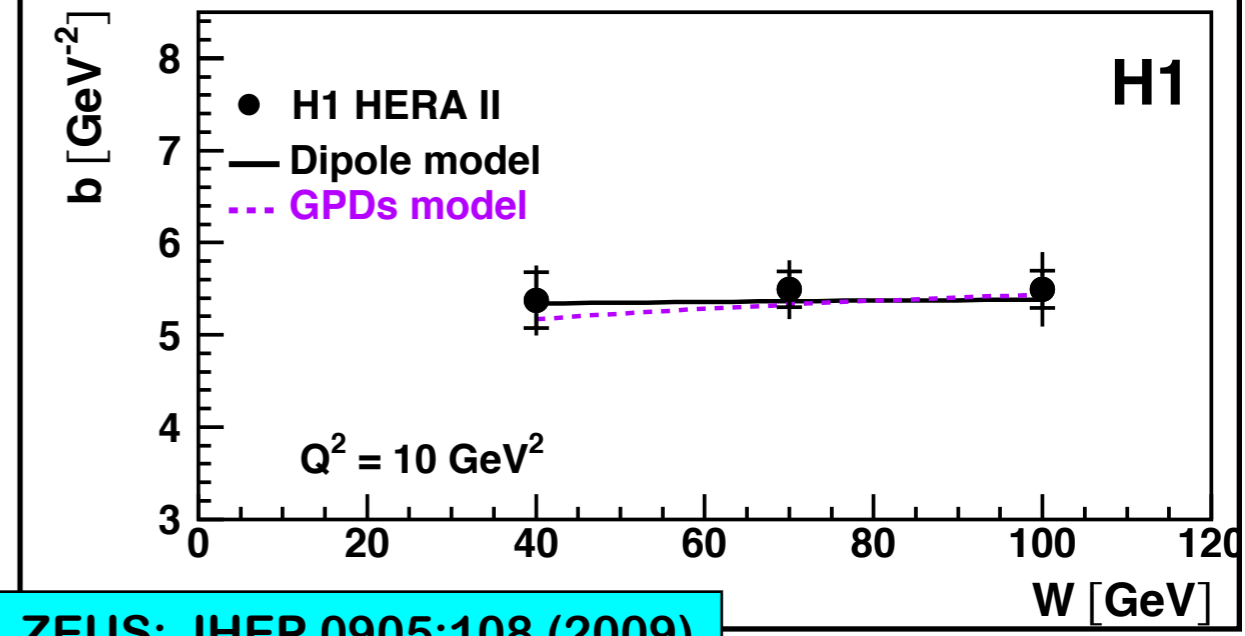
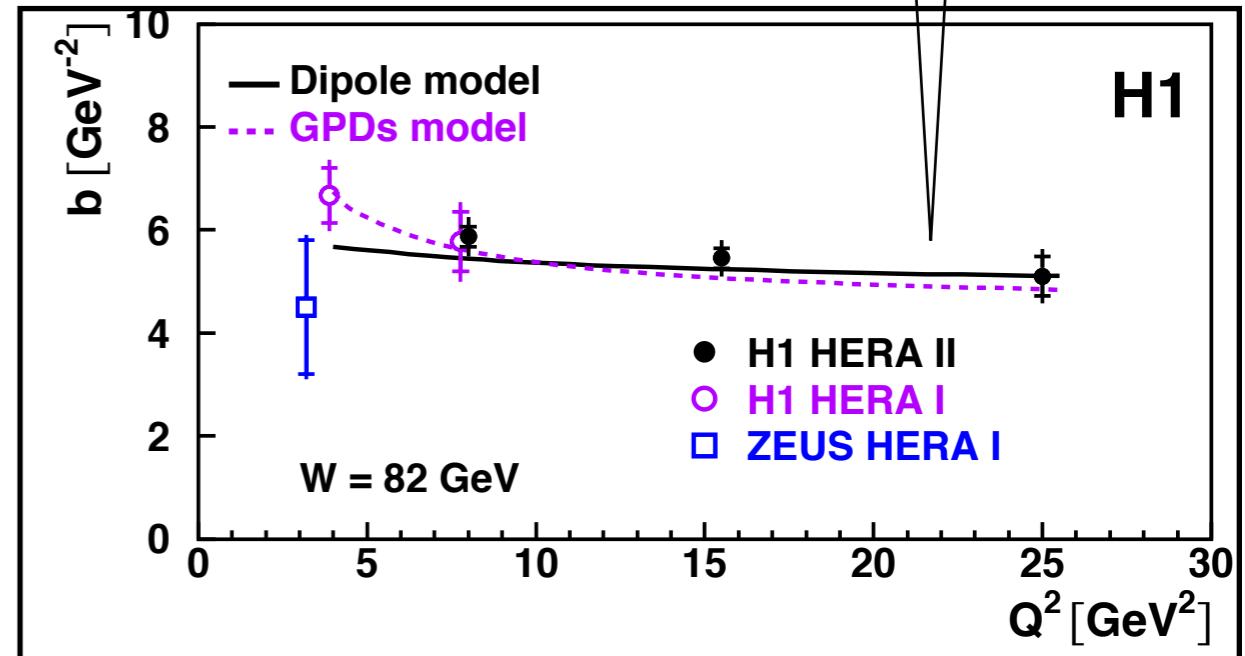
Steep  
W-dependence:  
 $\sigma(W) \propto W^\delta$   
with  $\delta \approx 0.7$

GPD model: K. Kumericki, D. Müller,  
fit to previous HERA measurement

Dipole model: C. Marquet, R. Peschanski,  
G. Soyez, hep-ph/0702171

DVCS is hard  
process, gluons  
resolved!

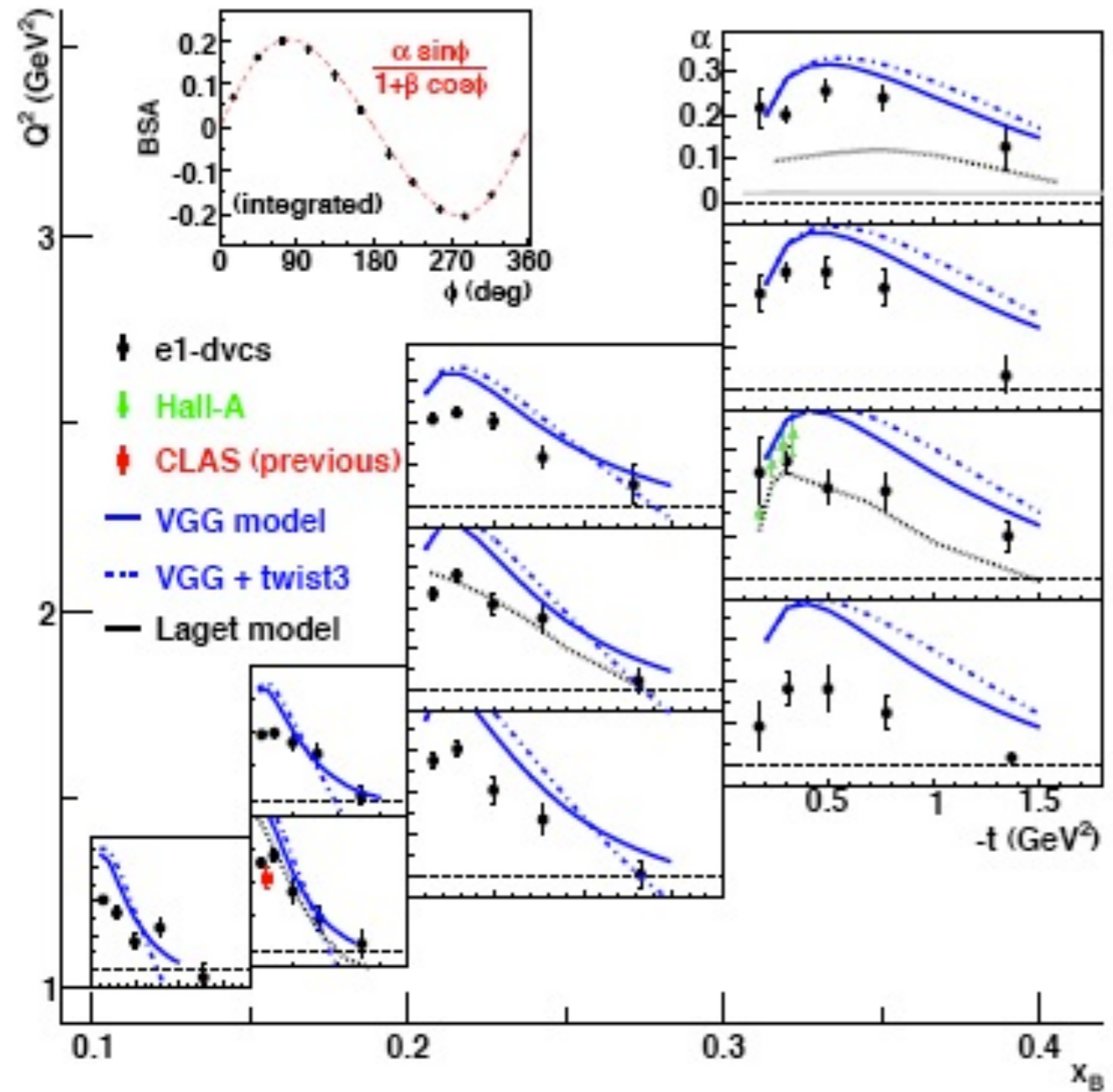
Description of transverse  
extension of partons in the proton!  
 $\sqrt{\langle r_T^2 \rangle} = (0.65 \pm 0.02) \text{ fm} @ x_B = 10^{-3}$



ZEUS: JHEP 0905:108 (2009)

# CLAS (e1-dvcs): beam-helicity asymmetry

CLAS:  $\langle Q^2 \rangle = 1.82 \text{ GeV}^2$ ,  $\langle x_B \rangle = 0.28$ ,  $\langle -t \rangle = 0.31 \text{ GeV}^2$



- Data taken with inner electromagnetic calorimeter for the detection of the BH/DVCS photon
- VGG Model overshoots data.

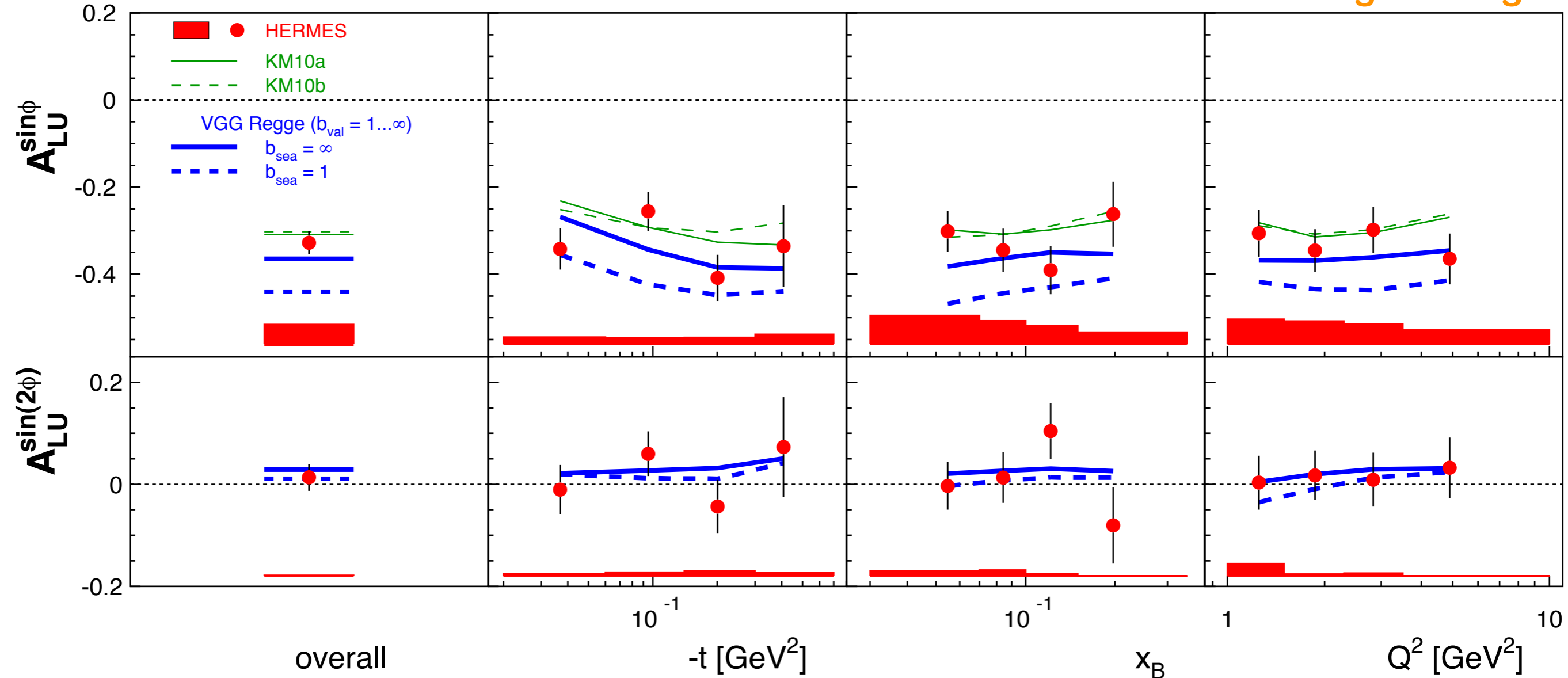
GPD model calculation  
 “VGG” (Vanderhaeghen, Guidal, Guichon):  
 Phys. Rev. D60 (1999) 094017 and  
 Prog. Nucl. Phys. 47 (2001) 401

CLAS: PRL 100 (2008) 162002

# HERMES (with recoil proton): beam-helicity asymmetry

GPD H  
Im( $\tau_{DVCS}$ )  
BSA

single-charge



Global fit of world data

JLab, HERMES and HERA,

dashed excludes JLab Hall A cross section

K. Kumericki and D. Müller, Nucl. Phys. B 841 (2010) 1

GPD model calculation "VGG Regge"

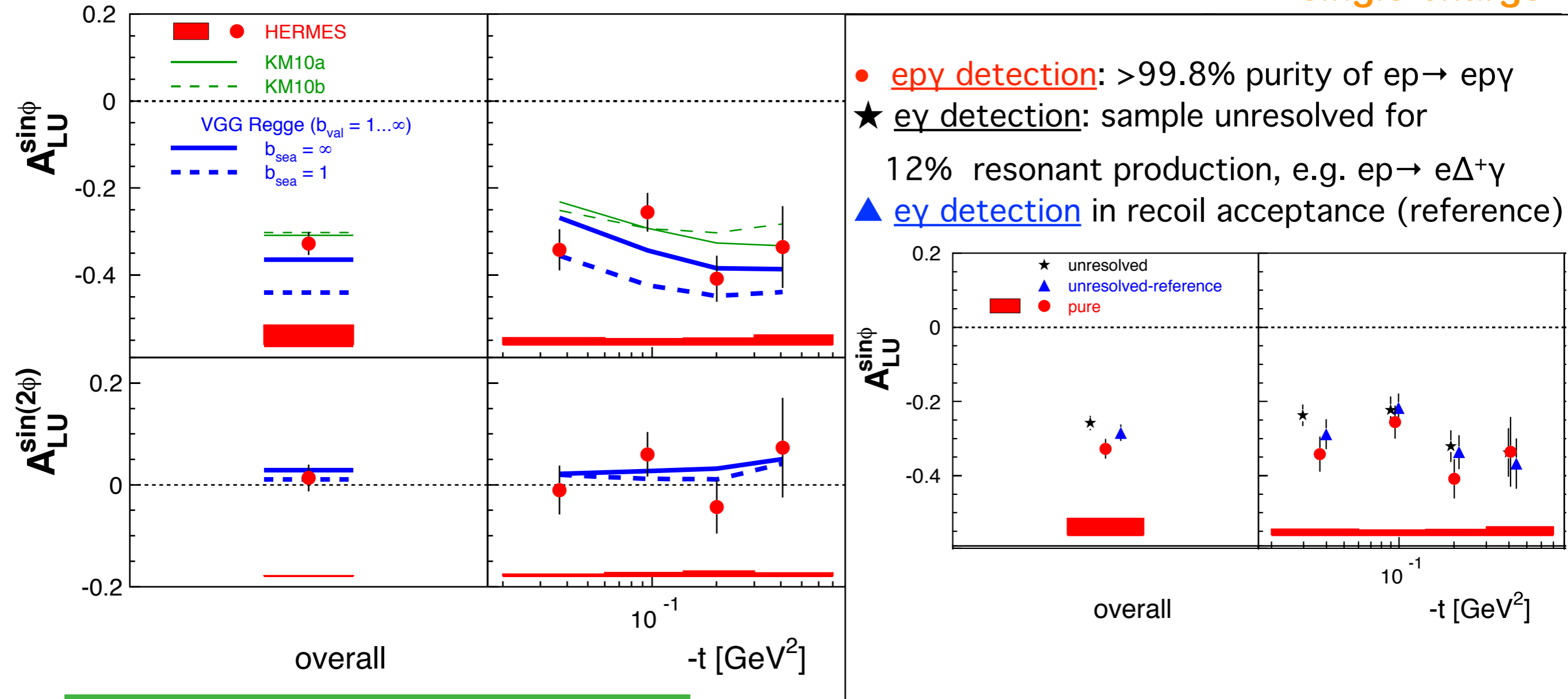
Phys.Rev. D60 (1999) 094017 and Prog.Nucl.Phys. 47 (2001) 401

HERMES: JHEP 10 (2012) 042

# HERMES (with recoil proton): beam-helicity asymmetry

GPD H  
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single-charge



Global fit of world data

JLab, HERMES and HERA,

dashed excludes JLab Hall A cross section

K. Kumericki and D. Müller, Nucl. Phys. B 841 (2010) 1

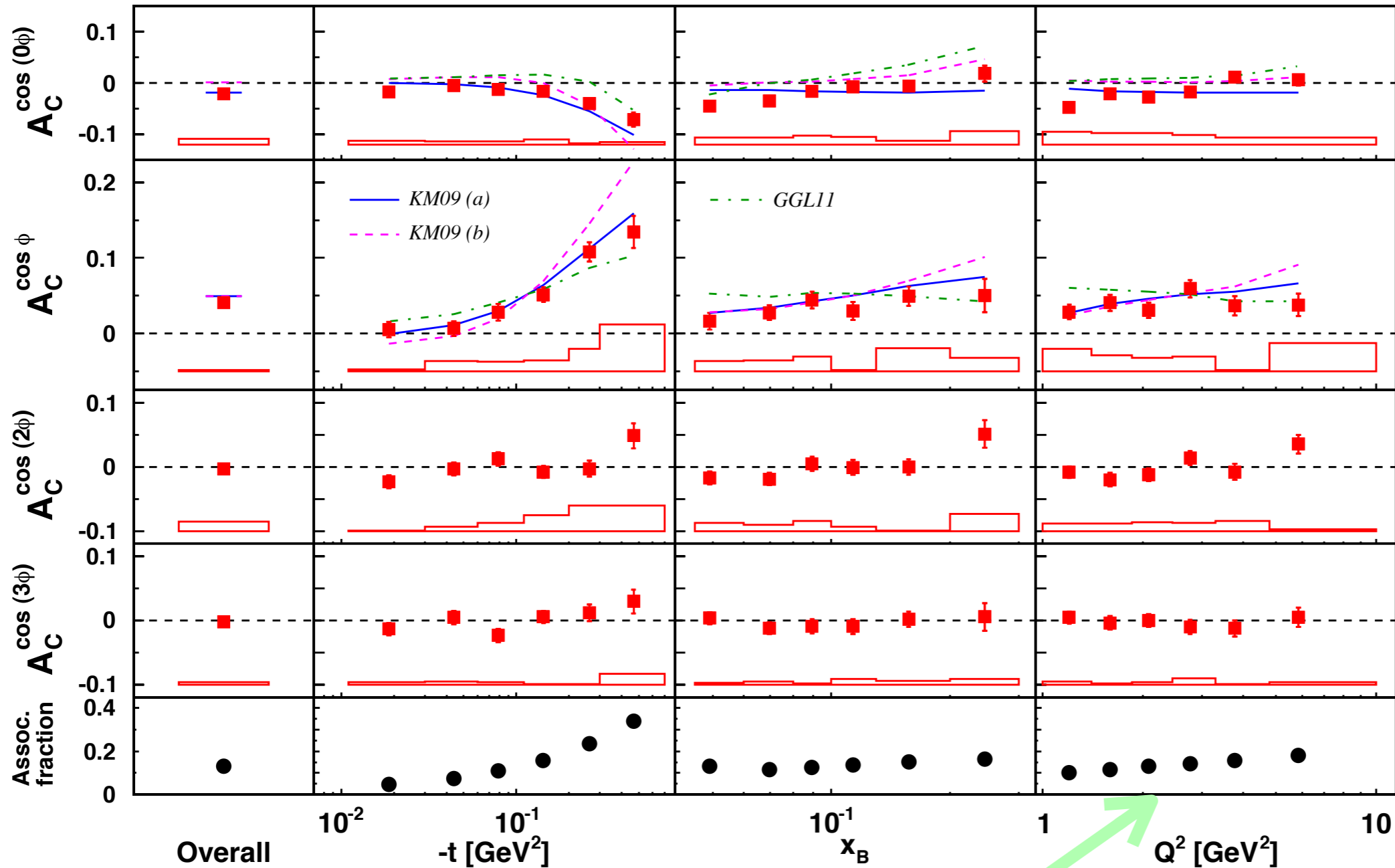
GPD model calculation “VGG Regge”

Phys.Rev. D60 (1999) 094017 and Prog.Nucl.Phys. 47 (2001) 401

HERMES: JHEP 10 (2012) 042

# HERMES: beam-charge asymmetry

**GPD H**  
 $\text{Re}(\tau_{\text{DVCS}})$   
**BCA**



★ KM10  
**Global fit**  
 including data  
 from JLab,  
 HERMES and HERA  
 colliders

(dashed excludes JLab  
 Hall A cross section)  
 K. Kumericki and D.  
 Müller, Nucl. Phys. B 841  
 (2010) 1

★ GGL11  
**Model calculation**  
 G. Goldstein, J.  
 Hernandez and S. Liuti,  
 Phys. Rev. D 84 034007  
 (2011)

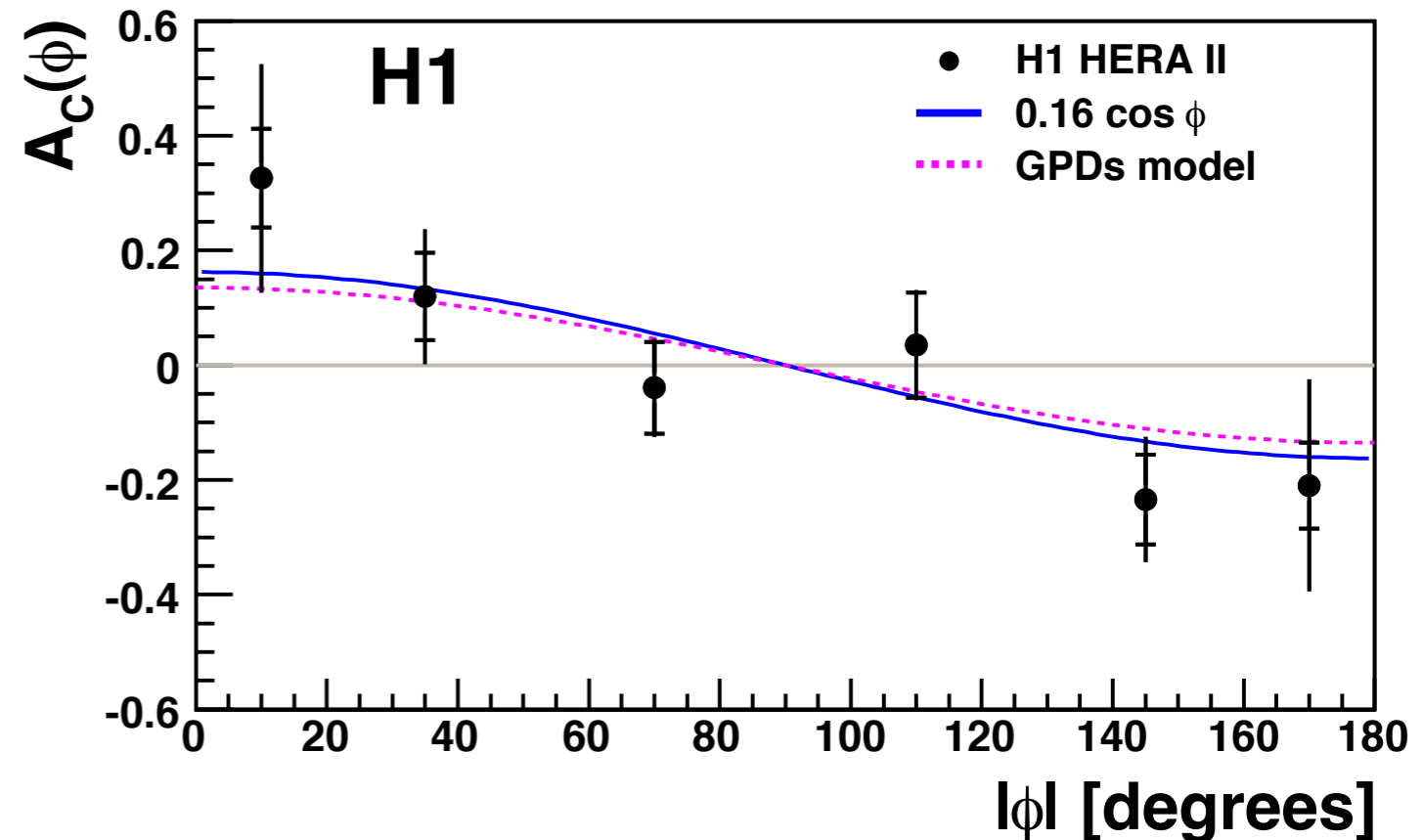
All 1996–2007 proton data.  
 No recoil-proton detection

Associated fraction  $ep \rightarrow e\Delta^+\gamma$   
 (from MC simulation)

**HERMES: JHEP 07 (2012) 032**

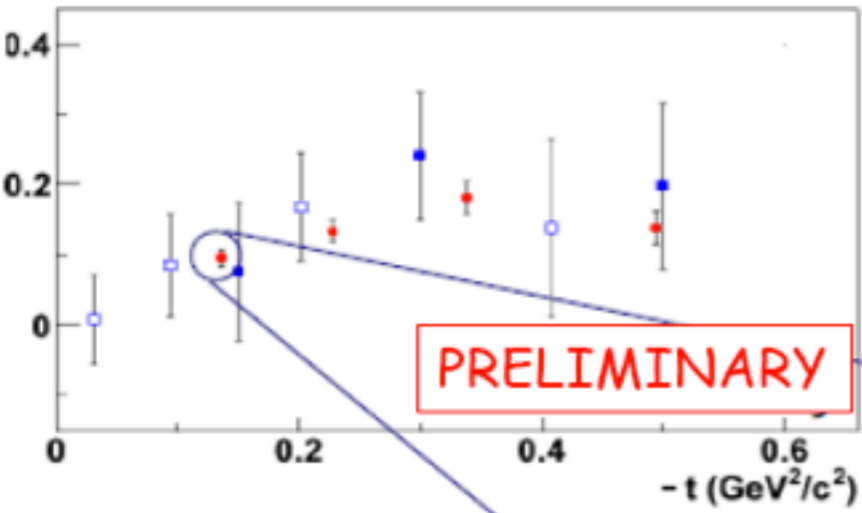
# H1: beam-charge asymmetry

- First and only measurement at collider
  - low  $x_B = 10^{-4} \dots 10^{-2}$
  - $6.5 < Q^2 < 80 \text{ GeV}^2$
  - $30 < W < 140 \text{ GeV}$
  - $|t| < 1 \text{ GeV}^2$
- Observation
  - $\text{Re}(\tau_{\text{DVCS}}) > 0$  for HERA (small  $x$ )
  - $\text{Re}(\tau_{\text{DVCS}}) < 0$  for HERMES (larger  $x$ )  
 (if same  $\phi$ -convention is used as for H1, i.e. non-Trento)
- $\rho = \text{Re}(\tau_{\text{DVCS}}) / \text{Im}(\tau_{\text{DVCS}})$ 
  - $\rho = 0.20 \pm 0.05(\text{stat}) \pm 0.08(\text{sys})$
  - In good agreement with theoretical calculation (dispersion relation)

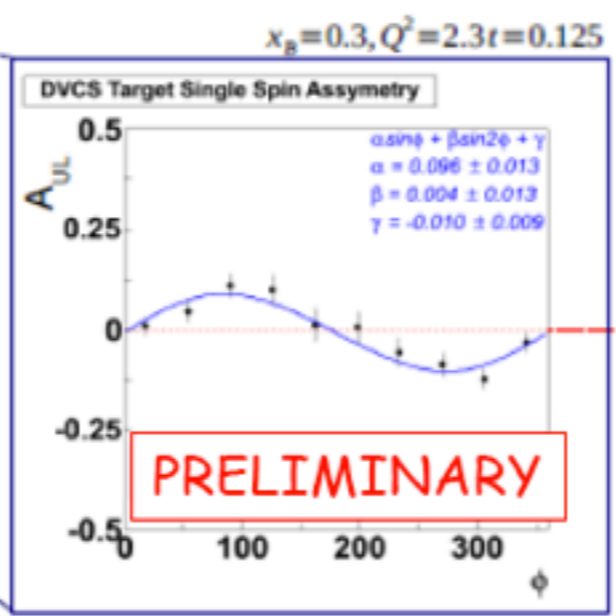


# CLAS (eg1-dvcs) and HERMES: longitudinal target-spin asymmetry

- CLAS eg1-dvcs
- measurements from CLAS-eg1b
- results from HERMES



CLAS [prelim.] target-spin UL asymmetry (no  $\pi^0$  correction yet)



eg1 b-dvcs publication:

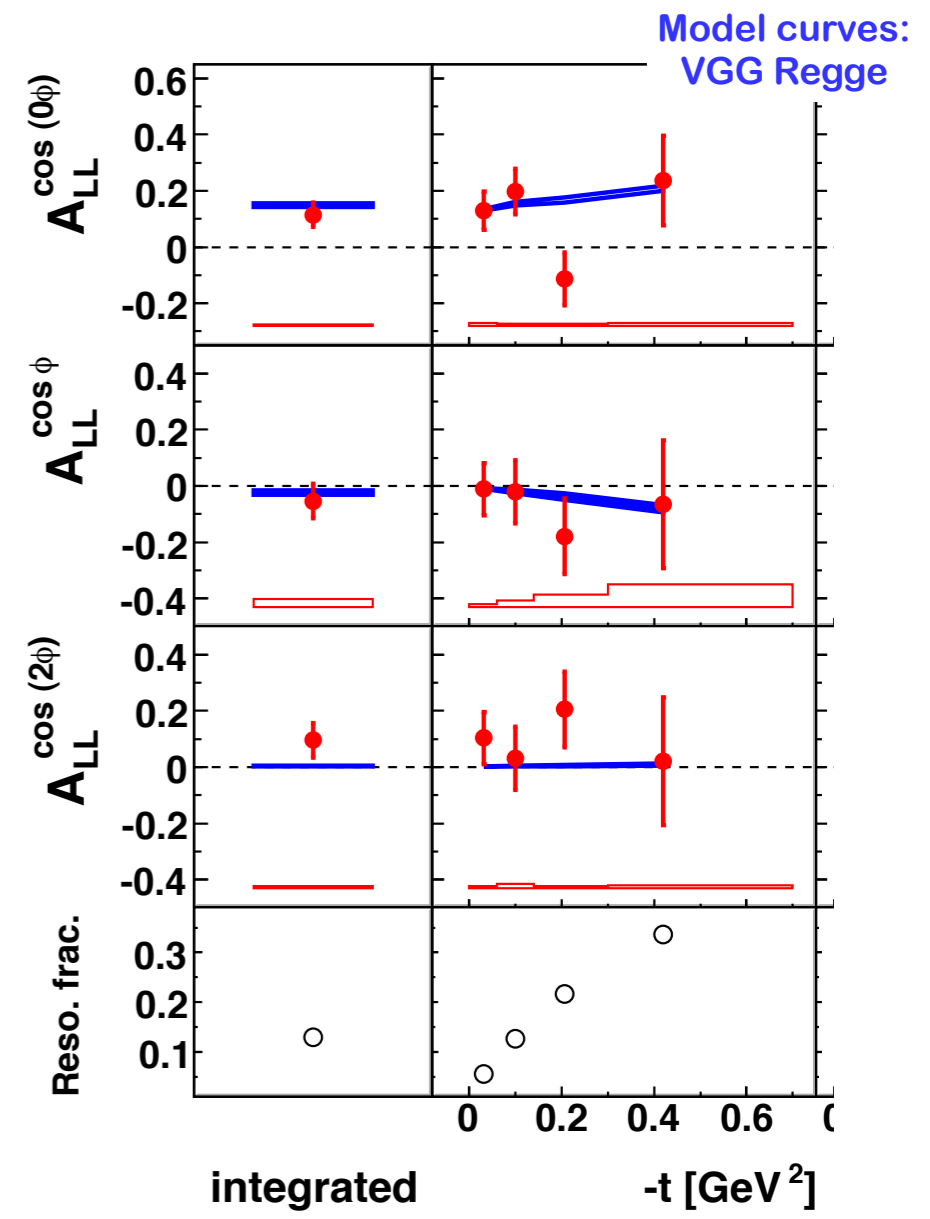
**CLAS PRL 97, 072002 (2006)**

eg1-dvcs: dedicated run 2009 with inner calo

**CLAS preliminary analysis**

More details: see talk by Andrey Kim on Wednesday afternoon: "Deeply Virtual Exclusive Production on a Longitudinally Polarized Proton with CLAS"

## HERMES double-spin LL asymmetry

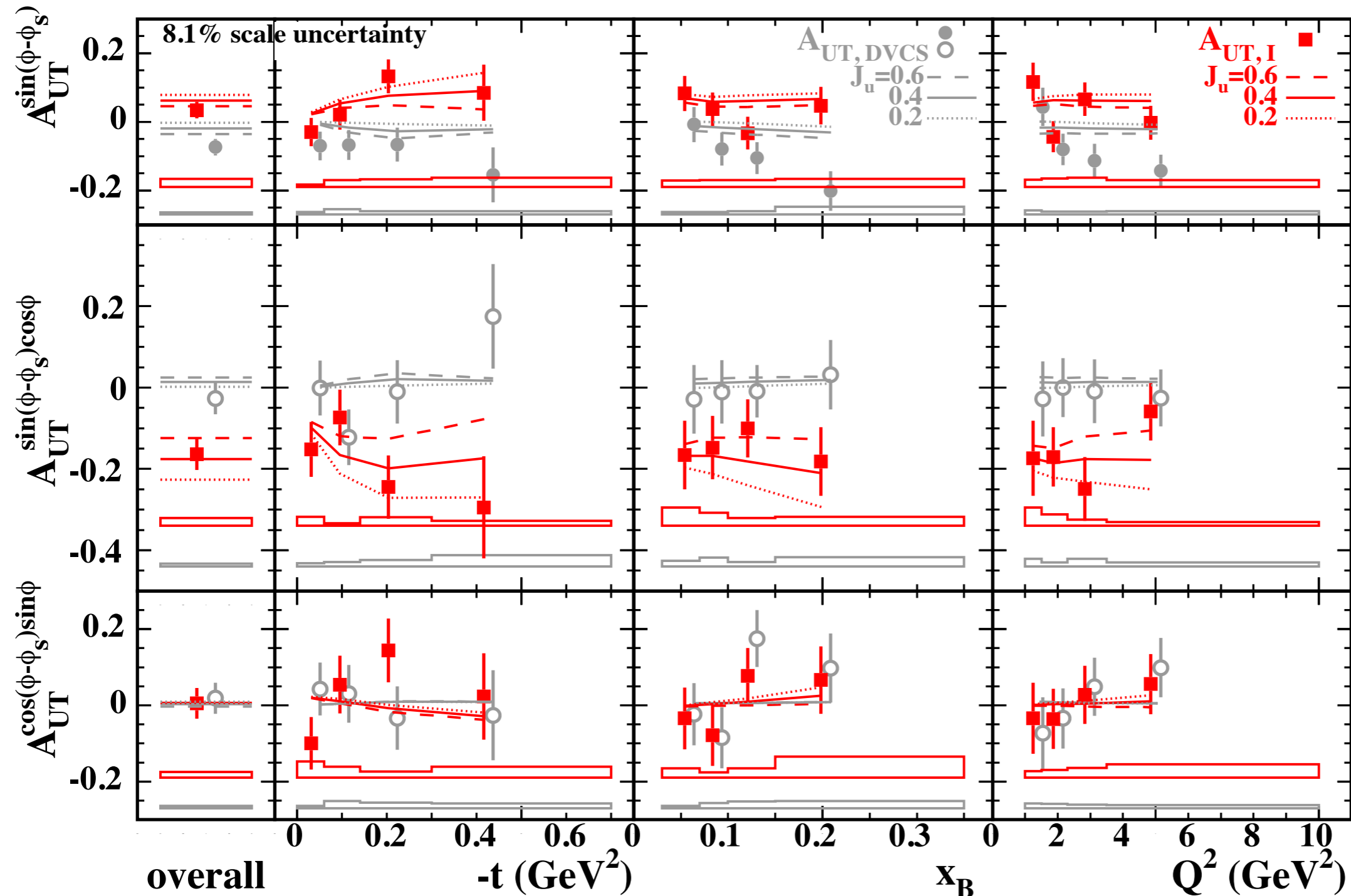


**HERMES: JHEP 06 (2010) 019**



# HERMES: transverse target-spin asymmetry

GPD E

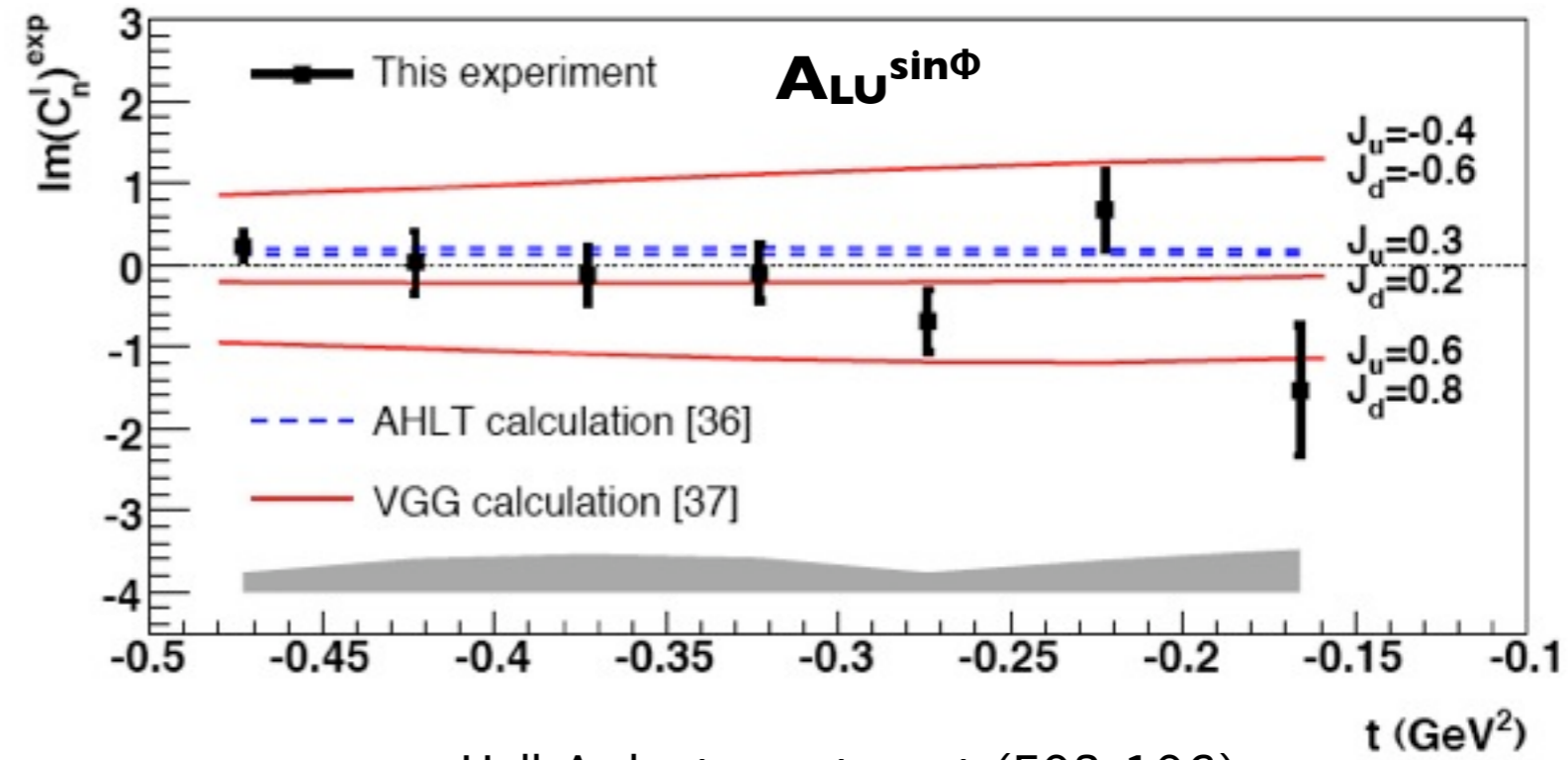


HERMES: JHEP 06 (2008) 066

# Hall A (E03-106): beam-helicity asymmetry on the neutron

## Sensitivity to GPD E

- (A) HERMES:  $ep^\uparrow \rightarrow ep\gamma$  :  
 $\mathcal{H}\text{-}\mathcal{E}$  (transversely polarized target)
- (B) Hall A:  $\vec{e}^- n \rightarrow e^- n \gamma$  :  
 $\mathcal{F}$  dominant for the neutron  
 (unpolarized target)



Hall-A deuteron target (E03-106)

**Nucleon spin**  $\frac{1}{2} = \frac{1}{2}\Delta\Sigma + L_q + J_g$

Hall A: Phys. Rev. Lett. 99, 242501 (2007)

**Ji sum rule for the nucleon**

-Ji, PRL 78 (1997) 610-

$$J_q = \frac{1}{2} \lim_{t \rightarrow 0} \int_{-1}^1 dx x [H^q(x, \xi, t) + E^q(x, \xi, t)]$$

Through these measurements, we can in principle learn something about the total angular momentum of quarks in the nucleon.

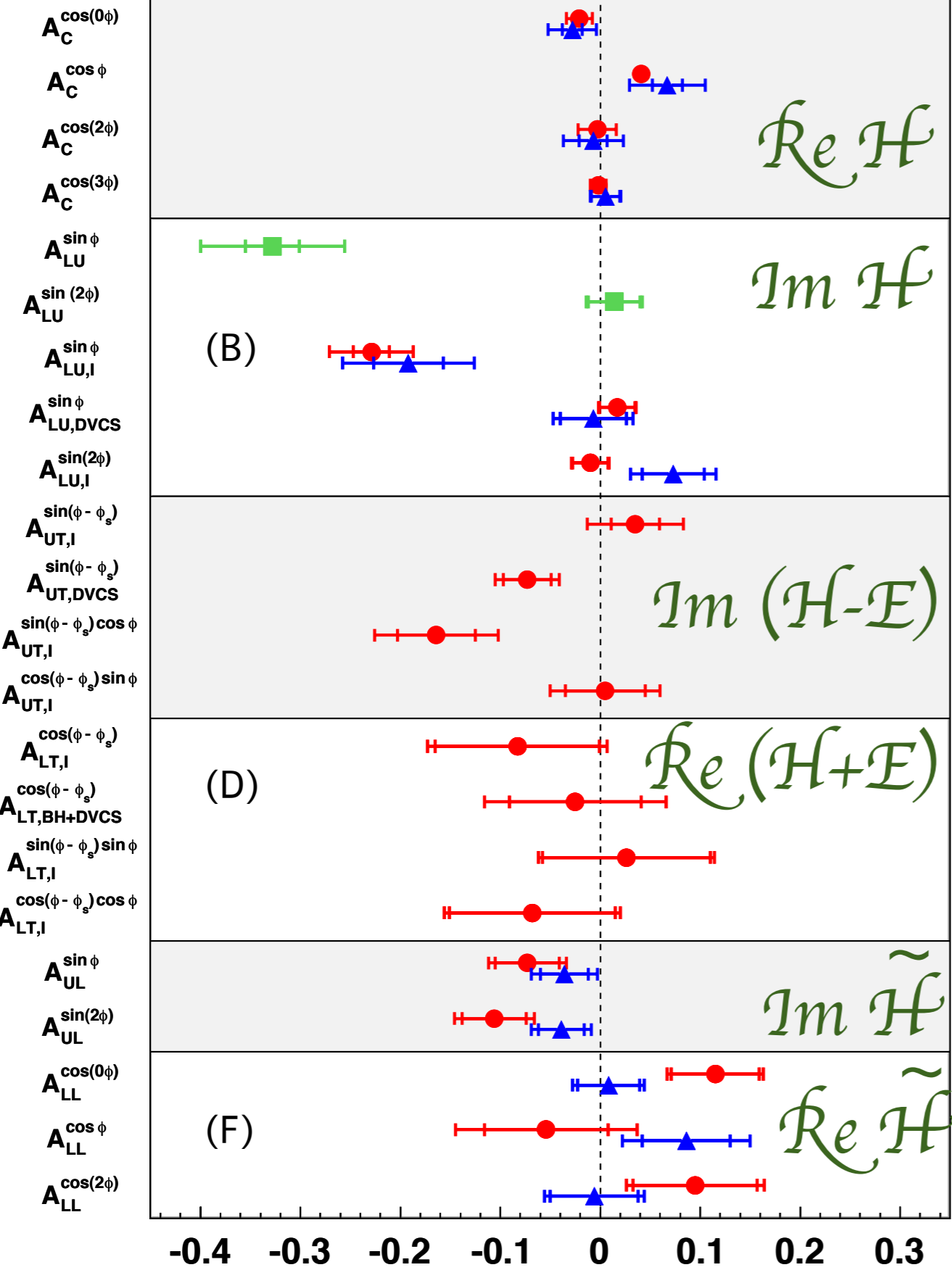
# HERMES DVCS

● Hydrogen  
▲ Deuterium  
■ Hydrogen Pure

# HERMES amplitudes

Unique & complete set

Variety highly welcome by global fitters



(A) Beam-charge asymmetry:

GPD H

[JHEP 07 (2012) 032 - Nucl. Phys. B 829 (2010) 1-27]

(B) Beam-helicity asymmetry:

GPD H

[JHEP 07 (2012) 032 - Nucl. Phys. B 829 (2010) 1-27 - JHEP10 (2012) 042]

(C) Transverse target-spin asymmetry:

GPD E

[JHEP 06 (2008) 066]

(D) Double-Spin (LT) asymmetry: GPD E

[Phys. Lett. B 704 (2011) 15-23]

(E) Longitudinal target-spin asymmetry:

GPD H~

[JHEP 06 (2010) 019 - Nucl. Phys. B 842 (2011) 265-298]

(F) Double-spin (LL) asymmetry:

GPD H~

[JHEP 06 (2010) 019 - Nucl. Phys. B 842 (2011) 265-298]

$\langle Q^2 \rangle = 2.46 \text{ GeV}^2$ ,  $\langle x_B \rangle = 0.10$ ,  $\langle -t \rangle = 0.12 \text{ GeV}^2$

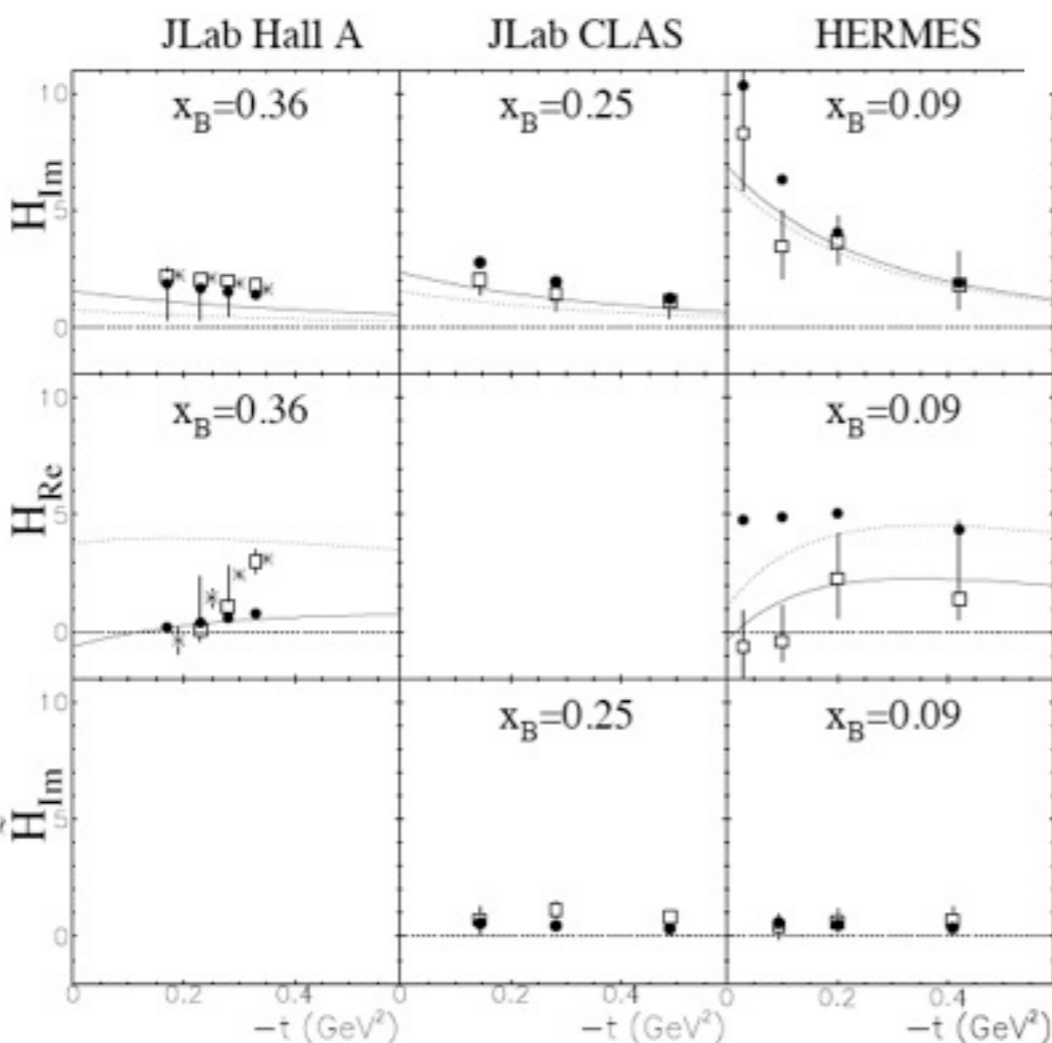
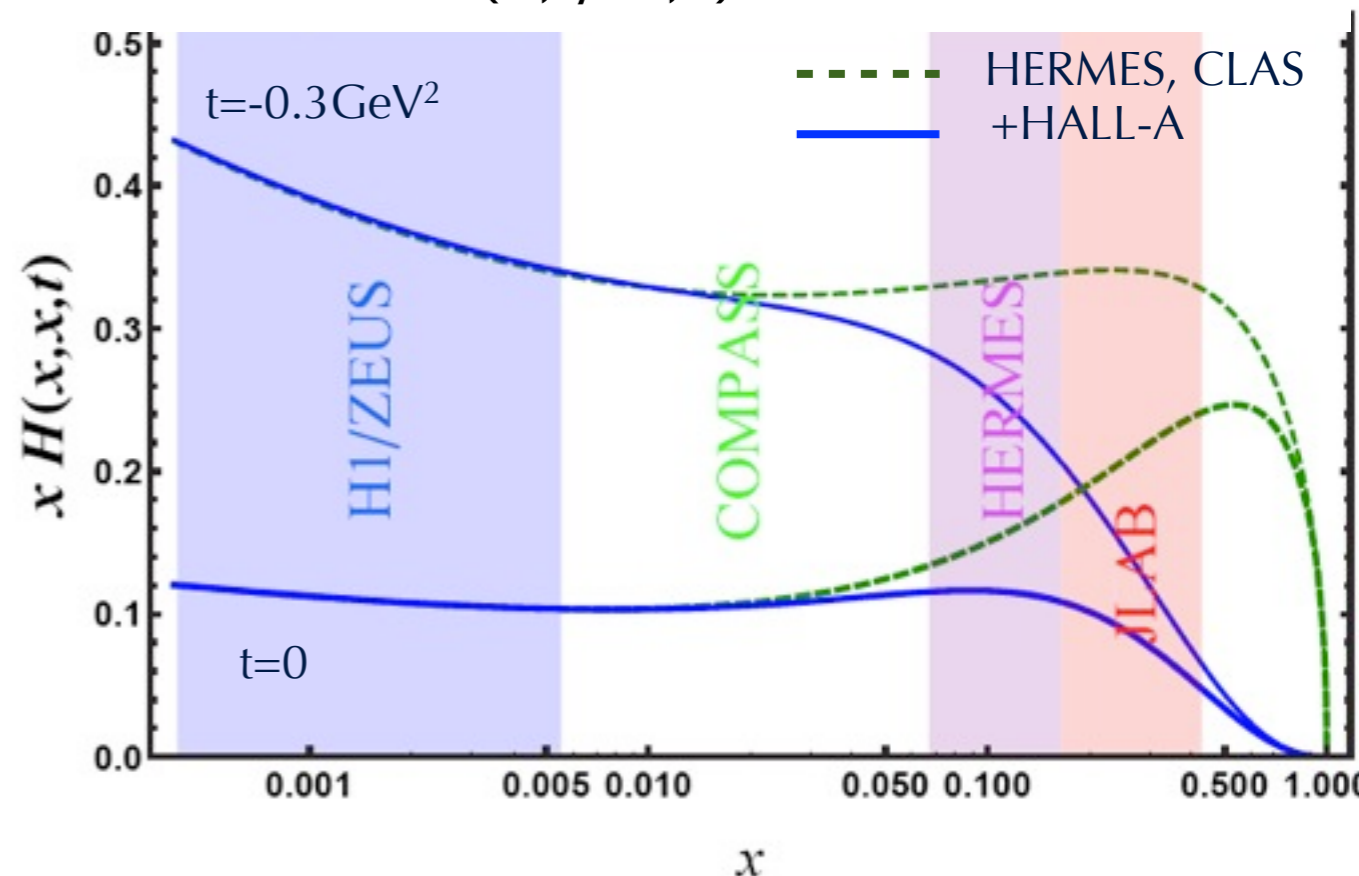
# Global analysis of DVCS data (a selection)

**K. Kumericki and D. Müller (KM)** **GPD H**

Nucl. Phys. B841 (2010) 1-58

- Global fit to extract GPD H at  $\xi=x$ . NNLO
- HERMES  $A_C$ , CLAS  $A_{LU}$  and Hall A x-section.
- Small-x behavior from HERA collider data.

Global fit to  $H(x, \xi=x, t)$  from DVCS data



Desirable:  
As many observables as possible sensitive to different CFFs

- Guidal
- \* Moutarde
- Müller/Kumericki
- VGG

**H. Moutarde** PRD 79, 094021 (2009)

- Global fit to extract  $\text{Re}(H)$  &  $\text{Im}(H)$
- Hall A x-section & CLAS  $A_{LU}$

**M. Guidal** arXiv:1011.4195

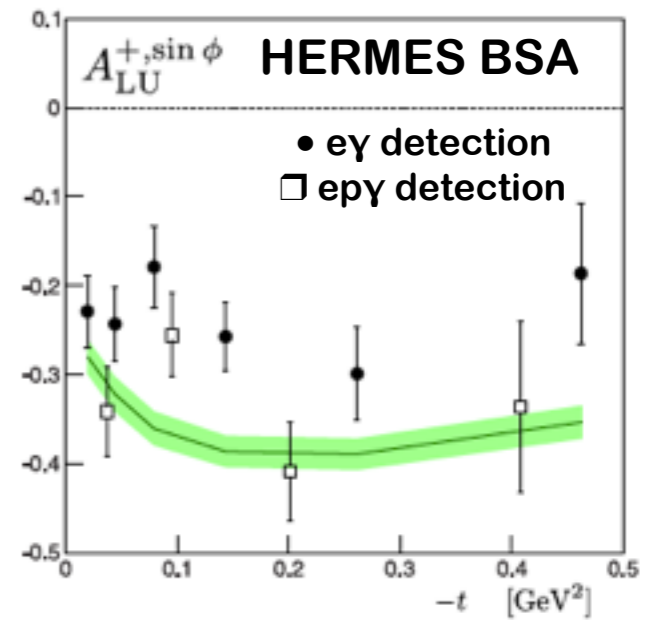
- Model-independent fit of  $\text{Re}(\text{CFF})$  &  $\text{Im}(\text{CFF})$
- HERMES  $A_C, A_{LU}, A_{UT}, A_{UL}, A_{LL}$ ; CLAS  $A_{LU}, A_{UL}$ ; Hall A x-section

**Compton Form Factors**

**K. Kumericki, D. Müller, A. Schäfer**  
arXiv:1106.2808

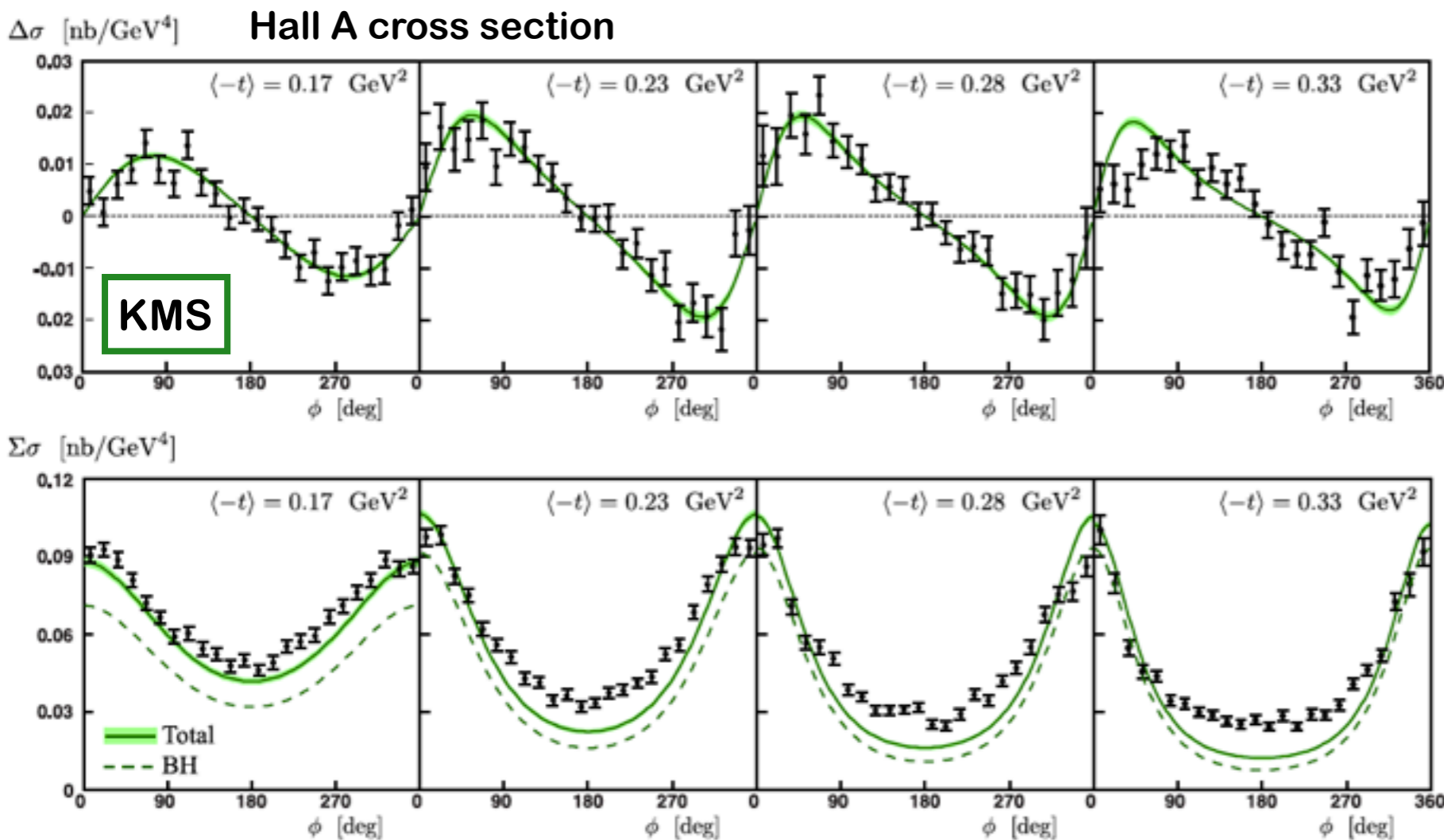
- Neural-network generated, model-independent parameterizations of CFFs
- Facilitates error propagation from data

# Check of GPD universality



P. Kroll, H. Moutarde and F. Sabatié (KMS) arXiv:1210.6975

- Use hard-exclusive meson (DVMP) data, FF and PDFs to constrain GPD parameters (LO, LT): GK model
- Compare to DVCS observables - good for HERA and HERMES, fair for JLab



Unpolarized x-section  $\Sigma\sigma =$  important normalization factor for asymmetries. Also:

- ☹ VGG model
- ☹ GK (Goloskokov-Kroll) model
- ☹ Minimal (i.e. forward) dual model ( $\rightarrow$  Polyakov and Vanderhaeghen)
- ☺ KM model, though needs large  $H\sim$ .

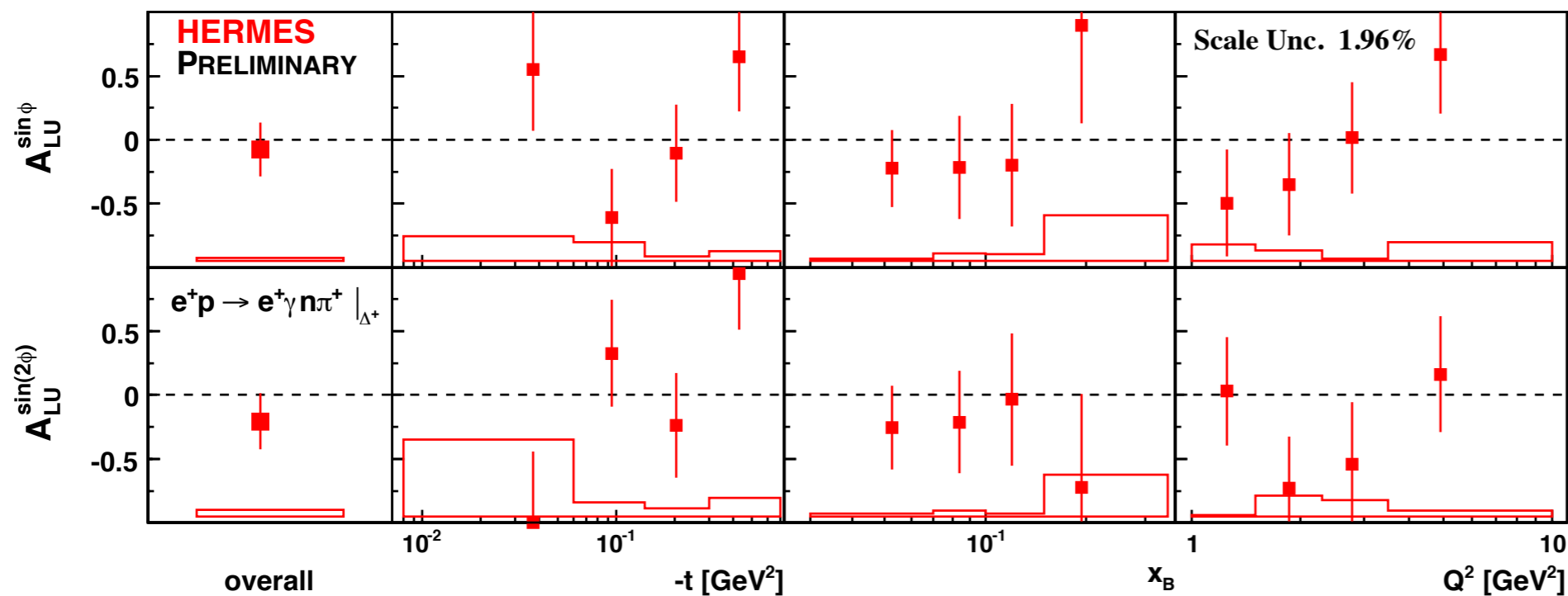
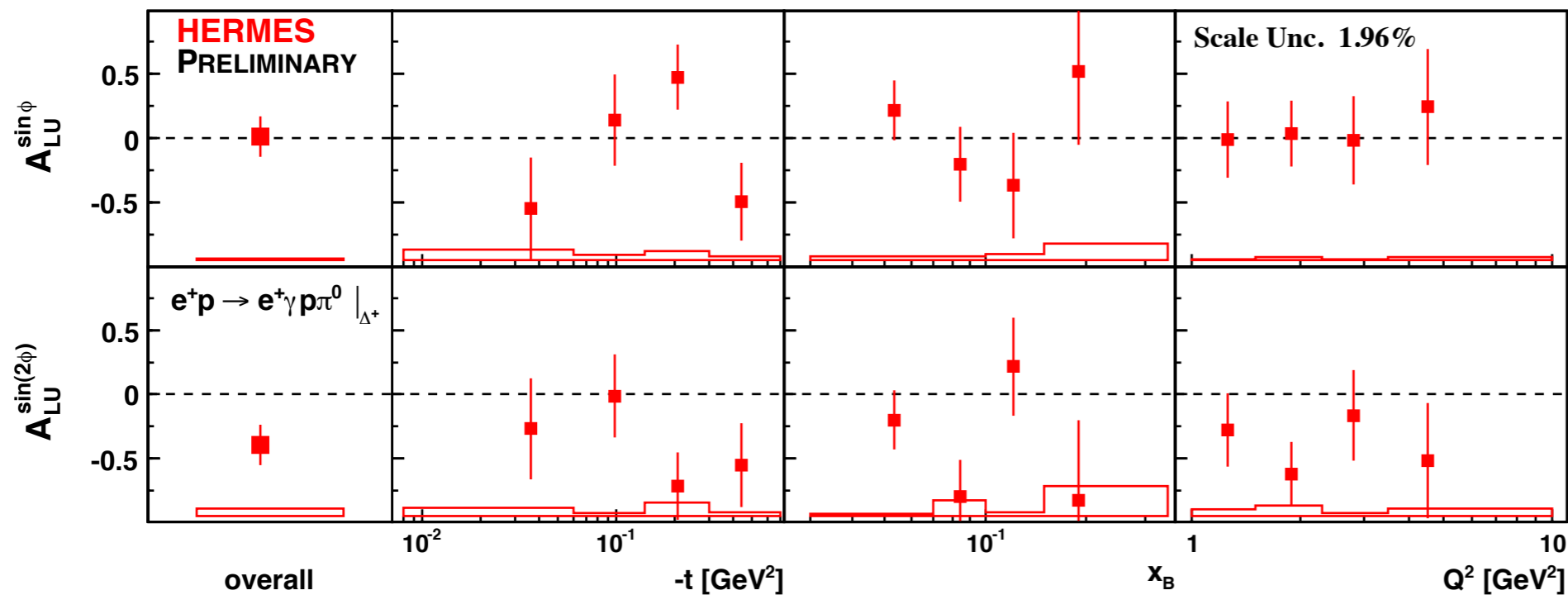
**Recent review article:**

M. Guidal, H. Moutarde, M. Vanderhaeghen: Generalized Parton Distributions in the valence region from Deeply Virtual Compton Scattering, arxiv.org:1303.6600

**Polarized x-section**, and in general imaginary part of  $\tau(\text{DVCS})$  known better.

# HERMES: beam-helicity asymmetry

## in $ep \rightarrow e\gamma(\pi N)$ in the $\Delta$ -resonance region



➡ The **charged particle** of ( $\pi N$ ) reconstructed by the recoil detector.

➡ This result is consistent with the slight increase of the beam-helicity asymmetry amplitude with recoil proton.

➡ Associated process acts as small dilution in the asymmetries for the unresolved sample.

➡ Only existing model prediction for  $\sin\phi$  amplitude:

$\pi^0 p$ : -0.15,  $\pi^+ n$ : -0.10

P.A.M. Guichon, L. Mossé, M. Vanderhaeghen: Pion production in deeply virtual Compton scattering, Phys. Rev. D68, 034018 (2003).

**HERMES: preliminary analysis**

# HERMES: DVCS on hadrons other than the proton

Coherent and  
tensor signatures;  
nuclear medium

GPD  $H_{1\sim}$

GPD  $H_{5\sim}$

GPD  $H_A$

HERMES: Nucl. Phys. B  
842 (2011) 265-298

longitudinally polarized deuterium

HERMES:  
Search for  
**coherent signature**  
on polarized d, spin 1

HERMES:  
Search for  
**tensor signature** on  
tensor-polarized d, spin 1

CLAS [eg6]:  
**coherent DVCS**  
on  $^4\text{He}$ , spin 0

# HERMES: DVCS on hadrons other than the proton

Coherent and tensor signatures; nuclear medium

GPD  $H_1 \sim$

GPD  $H_5 \sim$

GPD  $H_A$

HERMES: Nucl. Phys. B 842 (2011) 265-298

longitudinally polarized deuterium

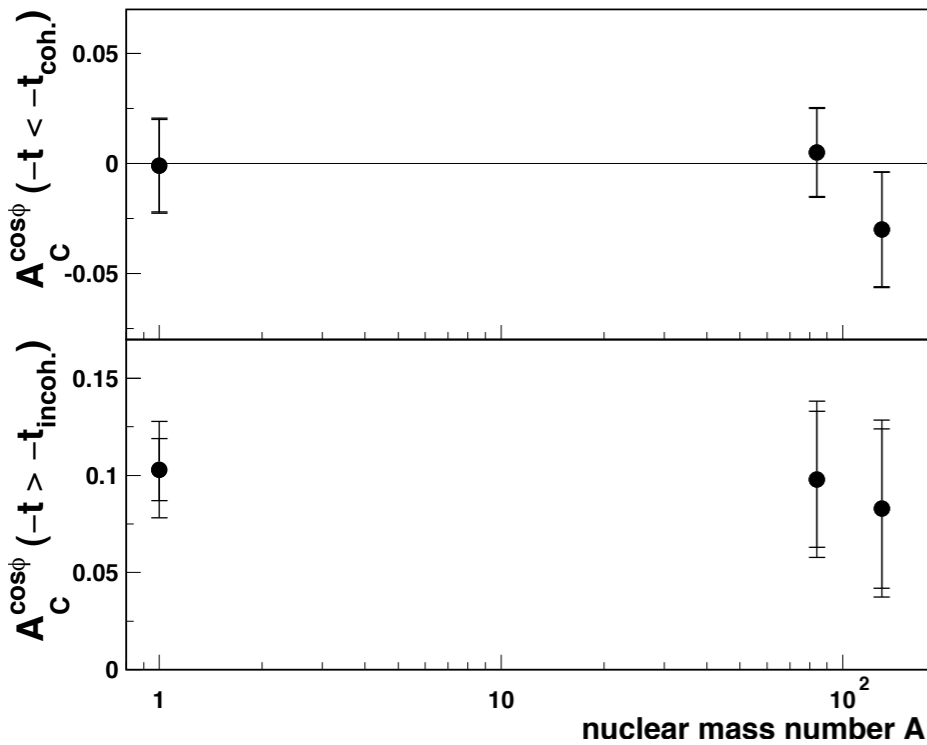
HERMES: Search for coherent signature on polarized d, spin 1

HERMES: Search for tensor signature on tensor-polarized d, spin 1

CLAS [eg6]: coherent DVCS on  $^4\text{He}$ , spin 0

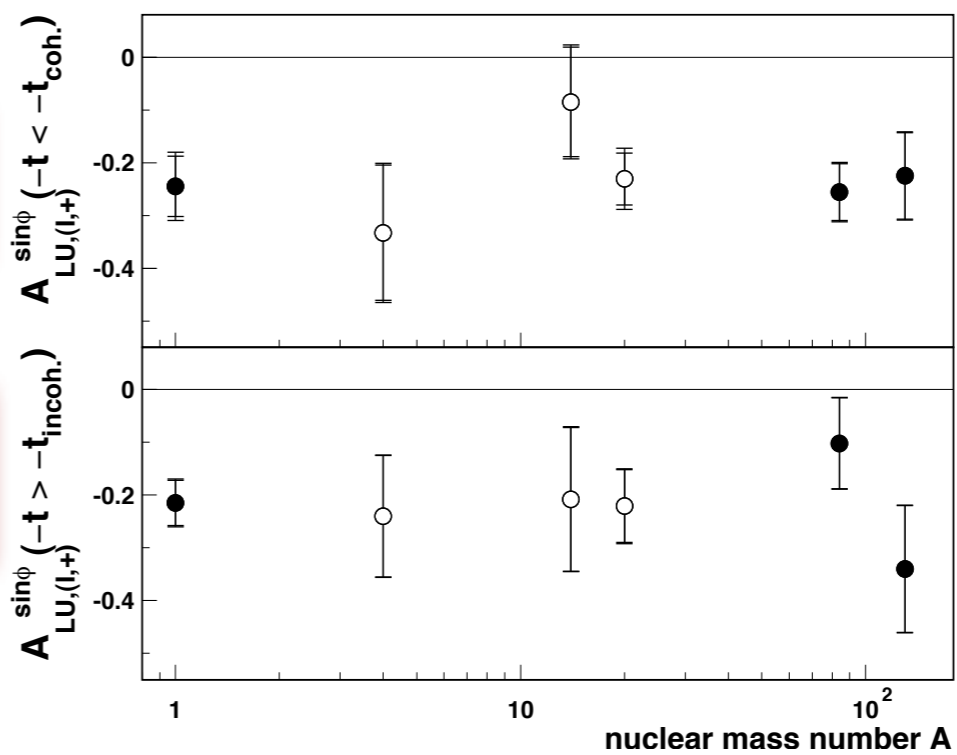
$A_C^{\cos\phi}$  vs. A

$A_{LU}^{\sin\phi}$  vs. A



coherent enriched

incoherent enriched



Average  $A_{LU}^A / A_{LU}^H$ :

$0.91 \pm 0.19$

$0.93 \pm 0.23$

Normalization to hydrogen  $^1\text{H}$

Beam-charge asymmetry

Beam-helicity asymmetry

HERMES: Phys. Rev. C 81 (2010) 035202



➡ Hall A: DVCS on the proton (E12-06-114).

Scaling tests of x-section; separation of Re and Im parts of  $\tau$  DVCS; E=6.6, 8.8, 11 GeV.

E07-007 for p, E08-025 for n ran successfully in 2010 with 12GeV-equipment. Rosenbluth analysis ongoing.

➡ CLAS12:  $A_{LU}$ ,  $A_{UL}$ ,  $A_{UT}$  and  $A_{LT}$  on the proton and  $A_{LU}$  on the neutron.

Transversely polarized HD-Ice target. Timelike Compton Scattering; DDVCS?

More details: see talk by Stepan Stepanyan on Wednesday afternoon: "The CLAS12 Physics Program"

## COMPASS

➡ Phase 1: 2015/16: GPD H, large recoil detector: separation of Re and Im parts of  $\tau$ (DVCS) by using two different combinations of beam charge and helicity; t-slope.

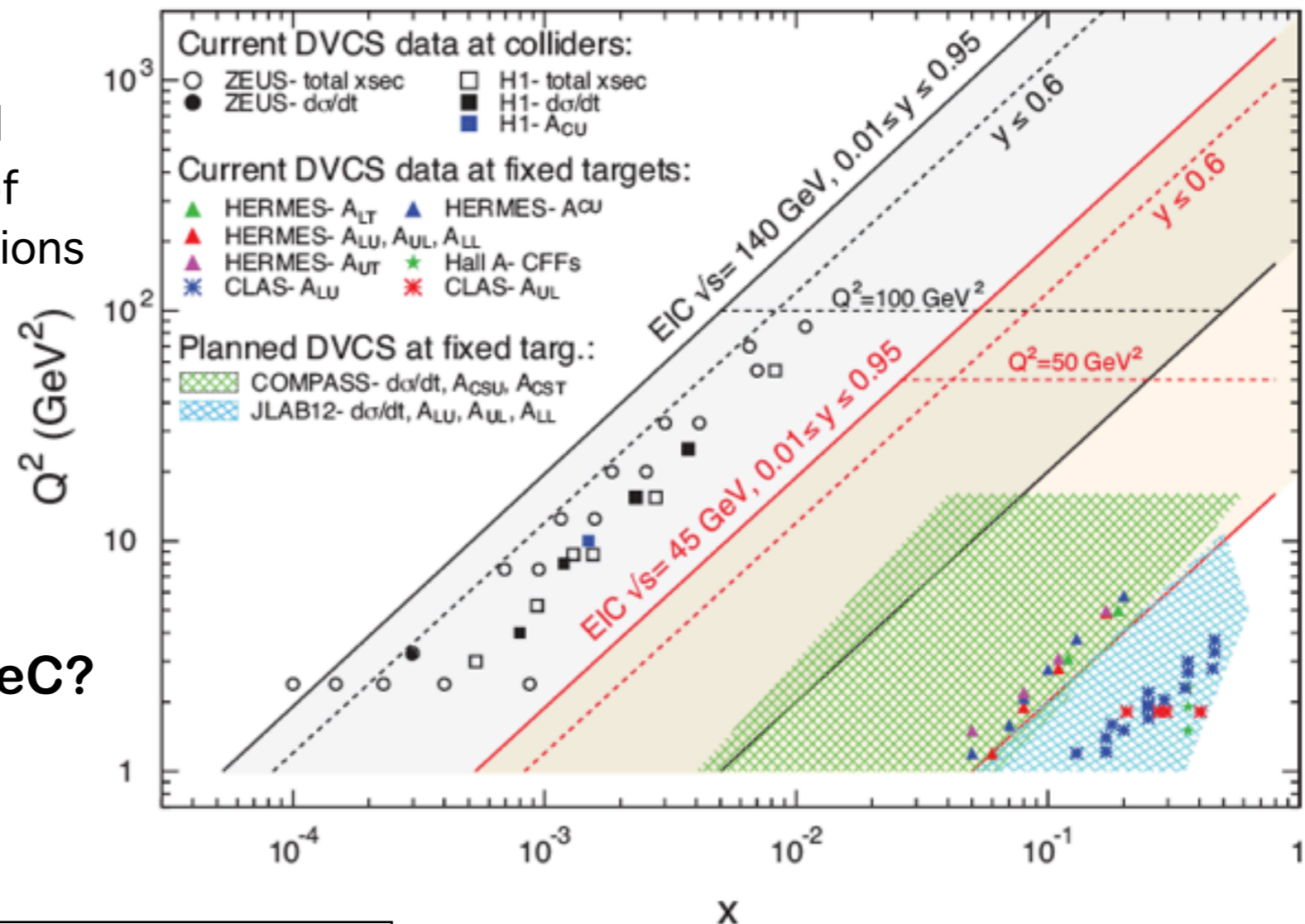
➡ Phase 2: 2018 (?): GPD E: transversely polarized target.

## Future Electron-Ion Collider (2025+)

➡ ELIC @ JLab or eRHIC @ BNL:  
 $\sqrt{s} = 20-70$  GeV

➡ ENC @ GSI:  $\sqrt{s} = 40$  GeV, ...

LHeC?



"Deeply Virtual Compton Scattering at a Proposed High-Luminosity Electron-Ion Collider", E.-C. Aschenauer, S. Fazio, K. Kumericki and D. Mueller, [arXiv:1304.0077](https://arxiv.org/abs/1304.0077)

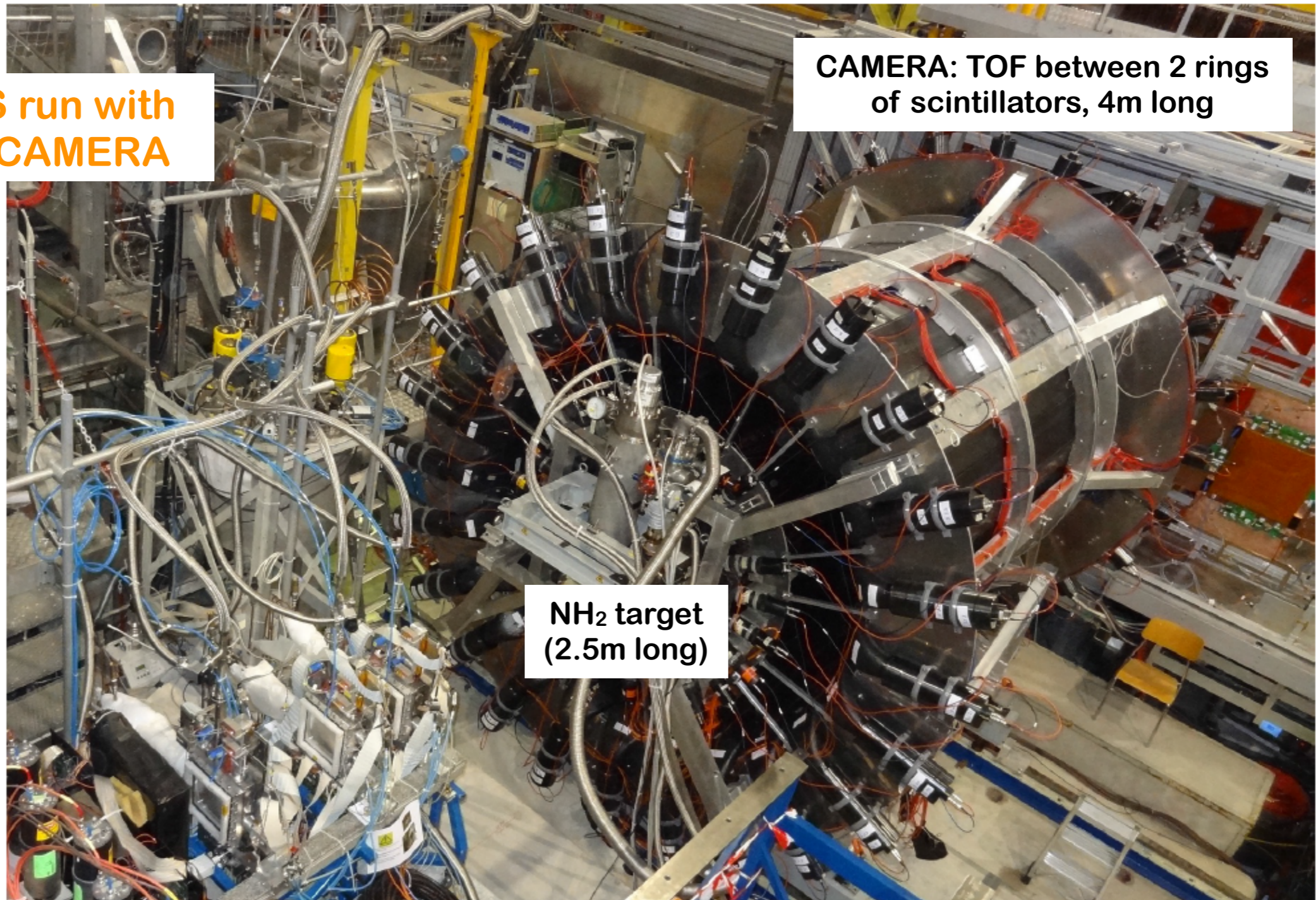
See also talk by Oleg Eyser Wednesday afternoon: "Future Opportunities at an Electron-Ion Collider"

# COMPASS CAMERA

2008/09: DVCS test runs with small recoil detector (not shown)

2012: first DVCS run with recoil detector CAMERA

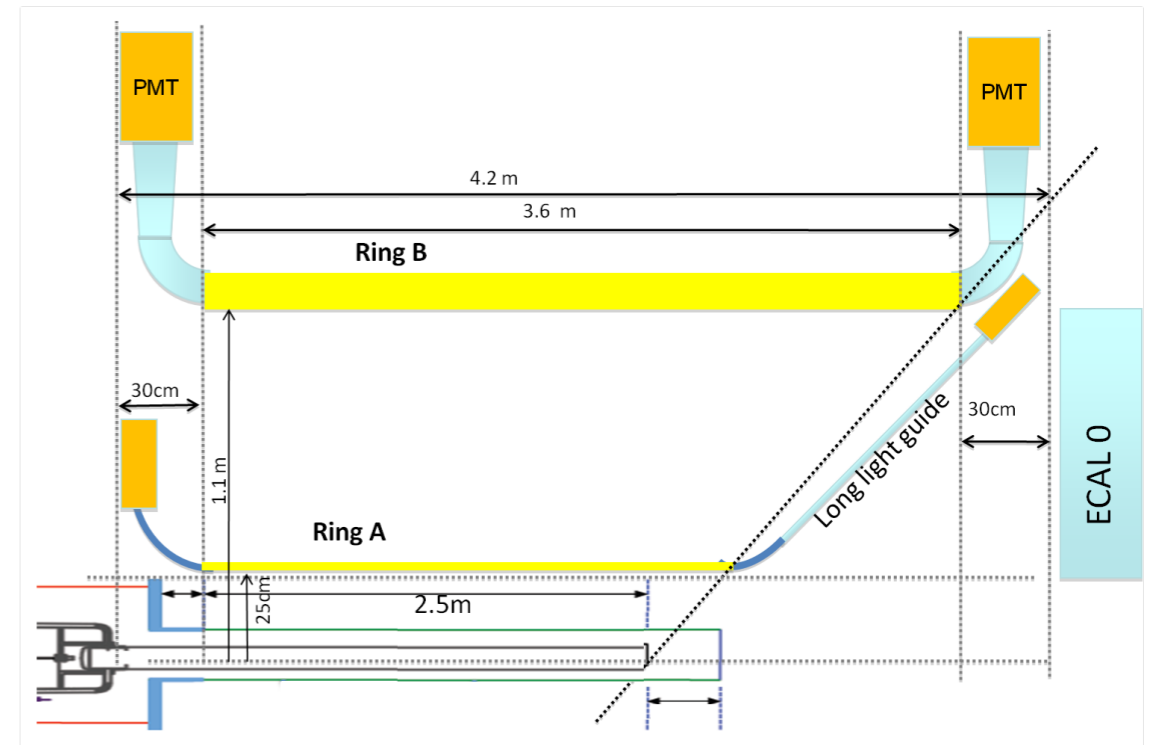
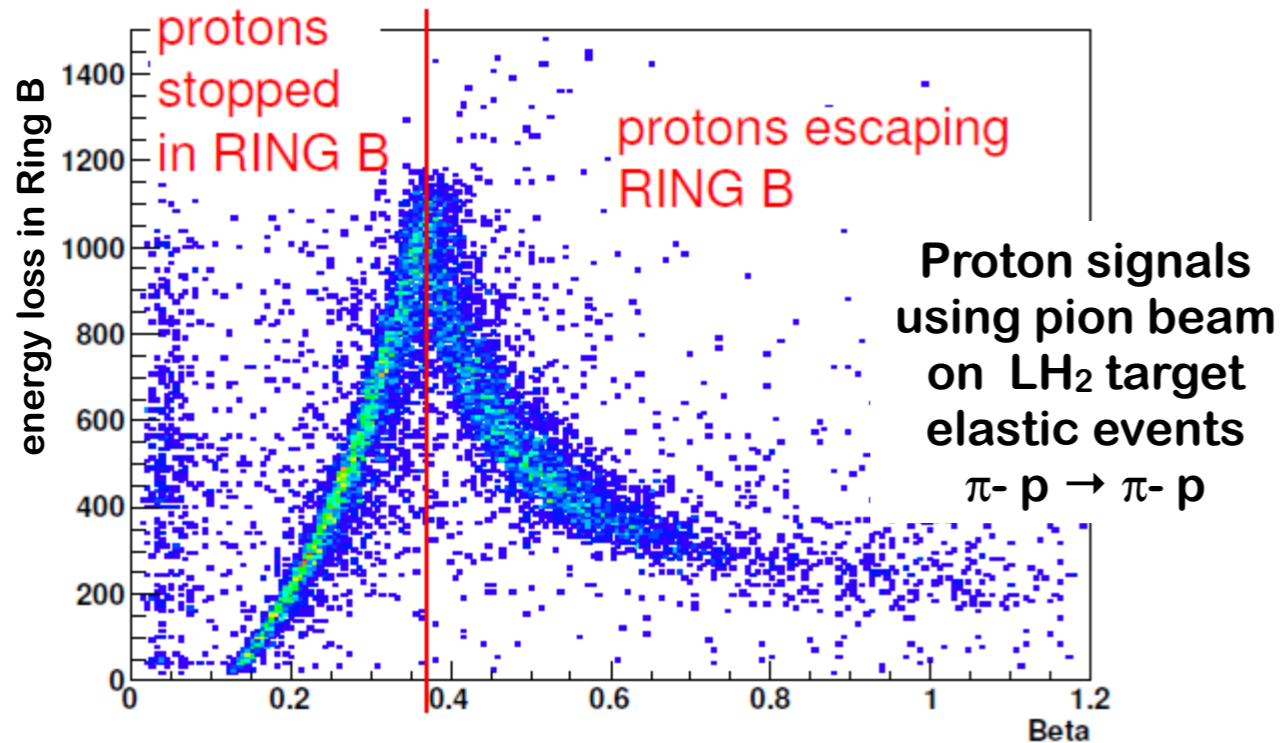
- Detection of recoil proton
- First DVCS run Sept 26 until Dec. 2012



CAMERA: TOF between 2 rings of scintillators, 4m long

NH<sub>2</sub> target (2.5m long)

# COMPASS: DVCS “Phase 1”



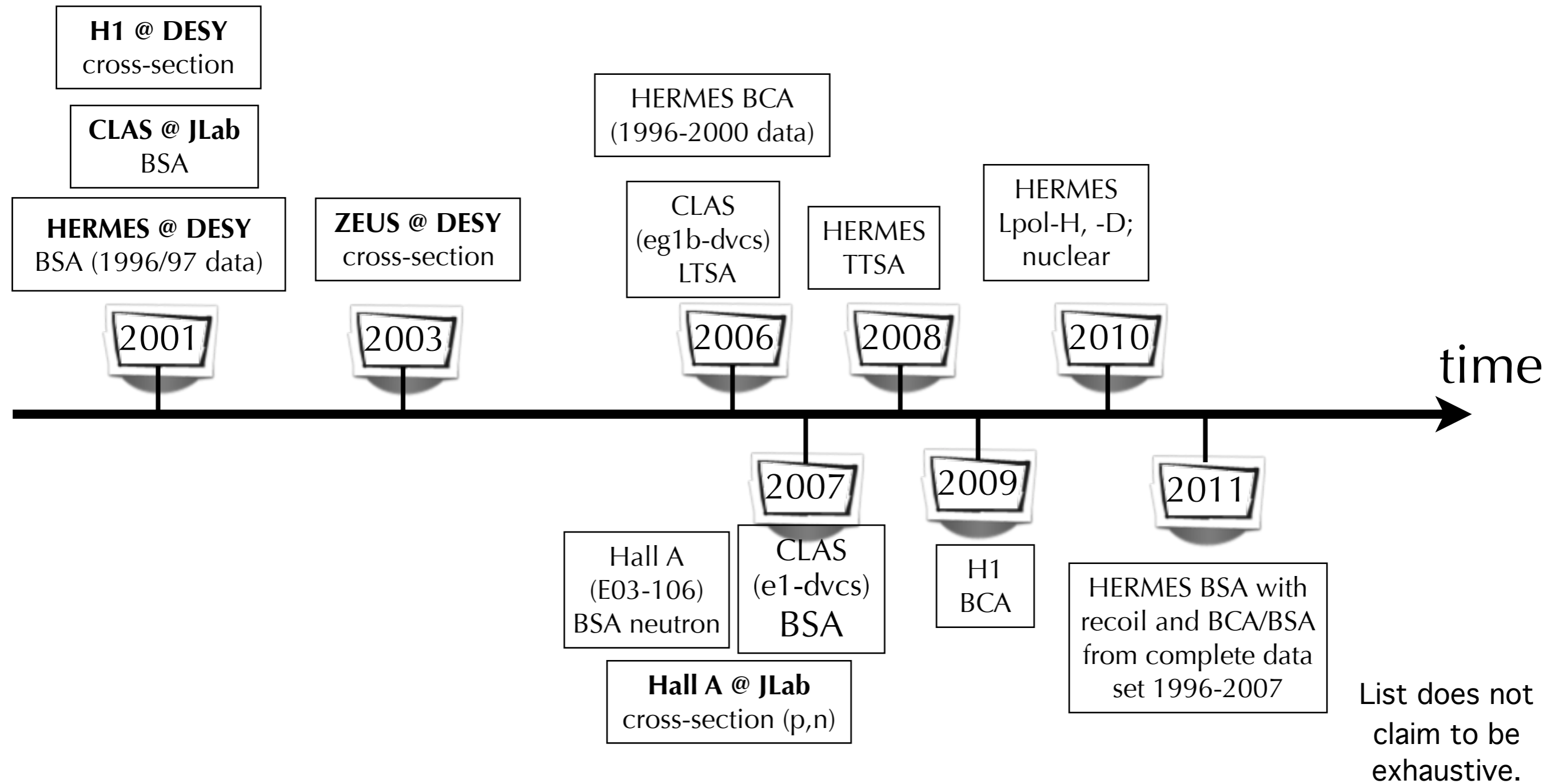
- First test run with large recoil detector end of 2012.
- Dedicated 2 years of data taking 2015/2016 with 160 GeV longitudinally polarized muon beam ( $\mu^+\leftarrow$  and  $\mu^-\rightarrow$ ).
- t-slope on  $\phi$ -integrated helicity-independent cross section. Transverse imaging
- Helicity-independent x-section:  $\sigma(\mu^+\leftarrow) + \sigma(\mu^-\rightarrow)$ ,  $\text{Re}(\text{CFF-H})$ . GPD H
- Helicity-dependent x-section:  $\sigma(\mu^+\leftarrow) - \sigma(\mu^-\rightarrow)$ ,  $\text{Im}(\text{CFF-H})$ .

# DVCS evolution over the years

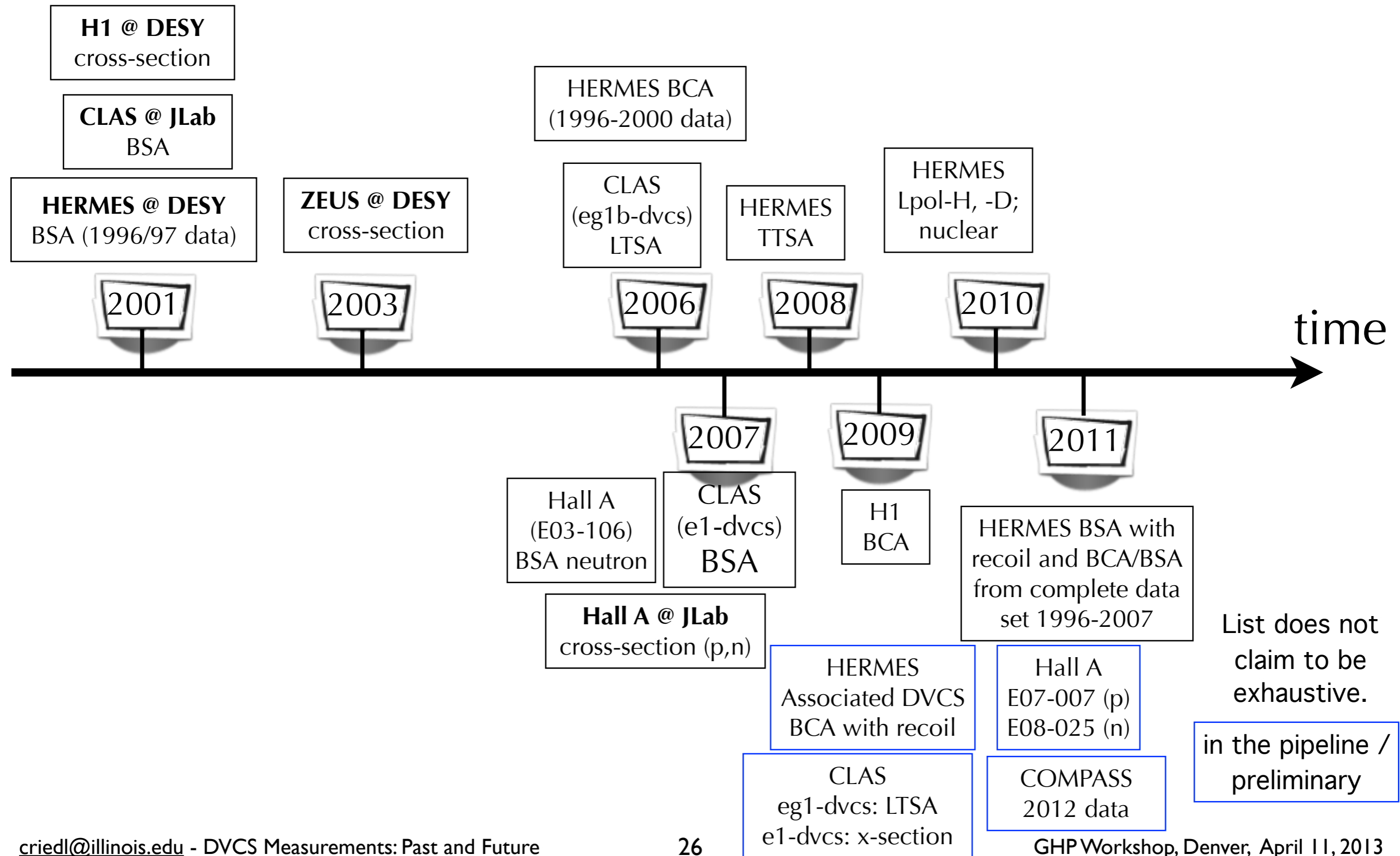


List does not claim to be exhaustive.

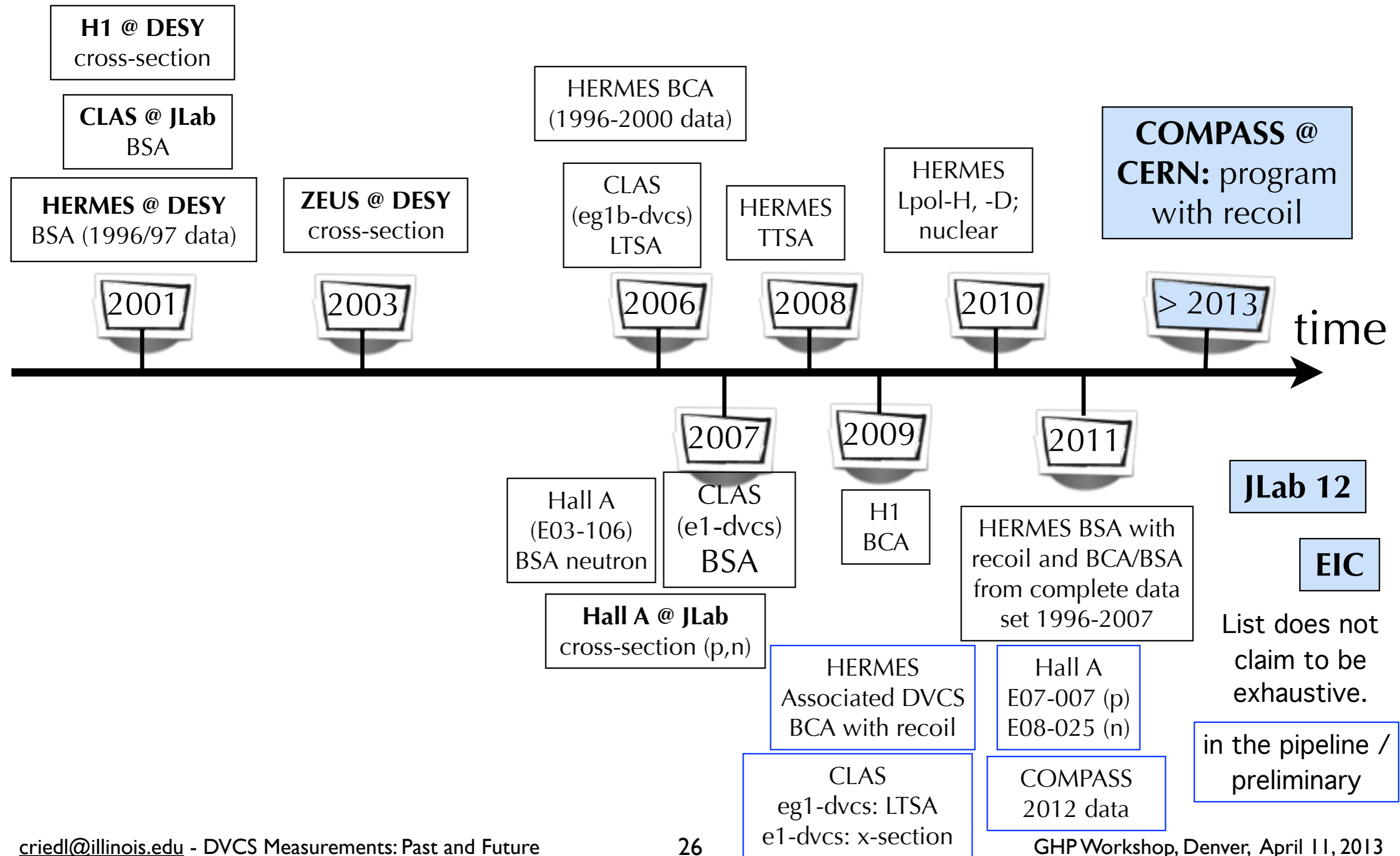
# DVCS evolution over the years



# DVCS evolution over the years

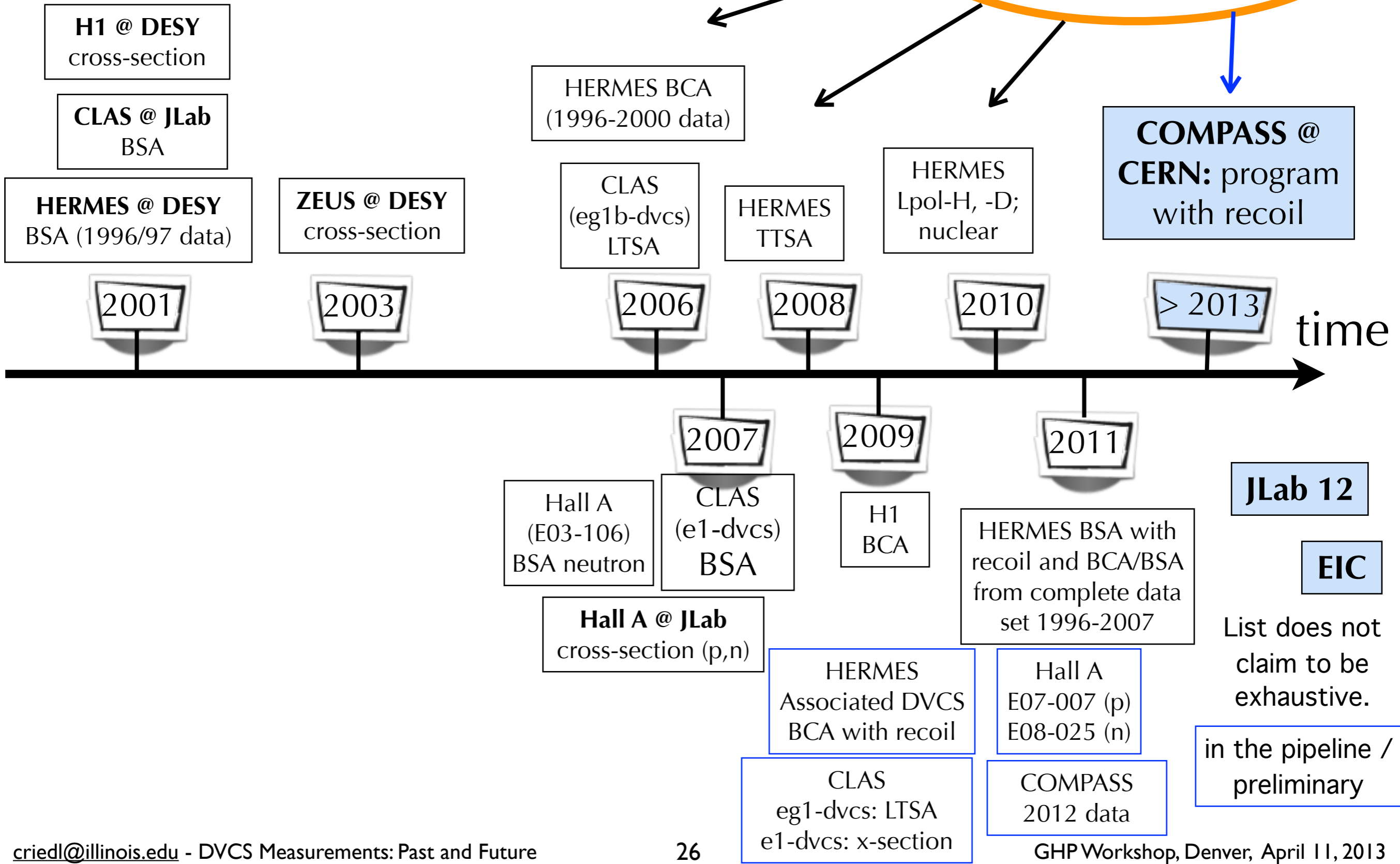
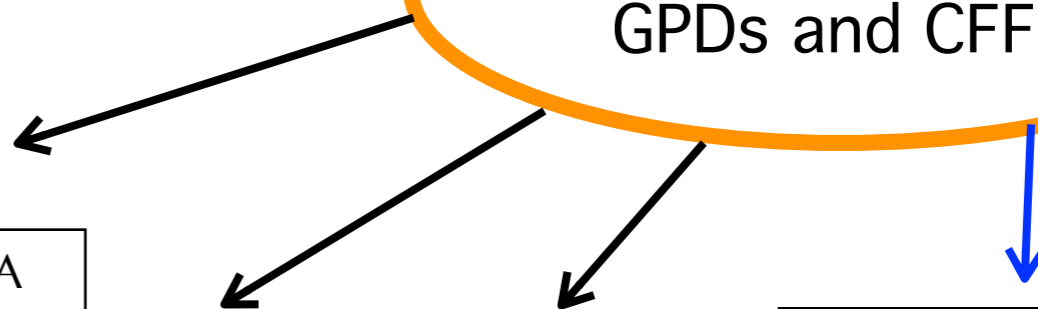


# DVCS evolution over the years



# DVCS evolution over the years

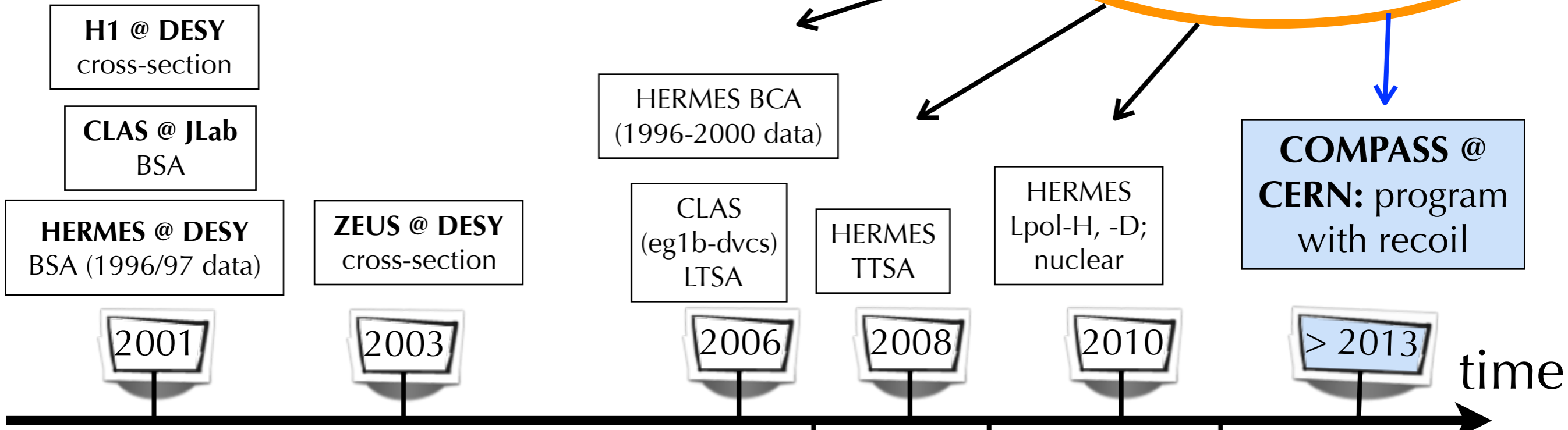
Global analysis of GPDs and CFFs





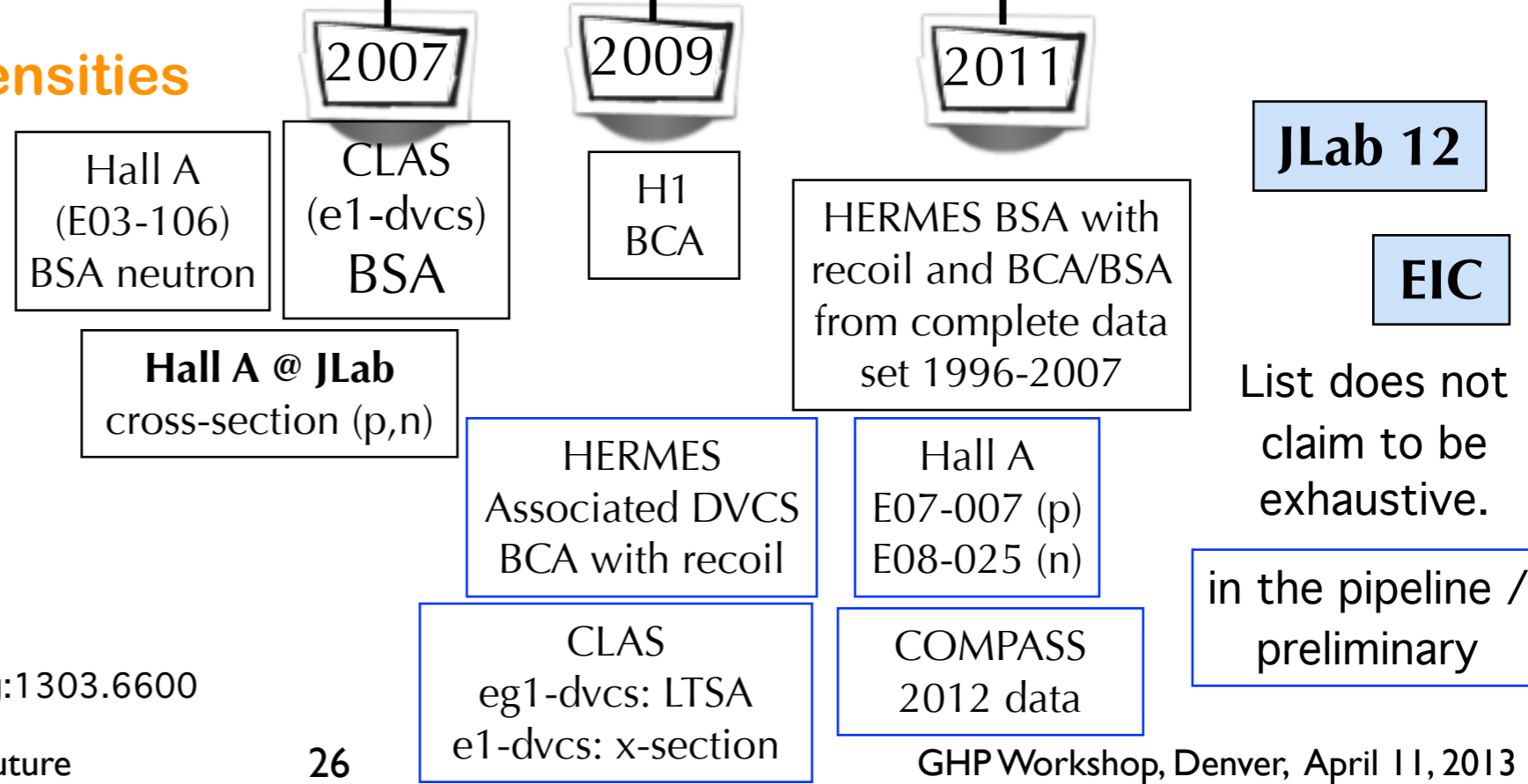
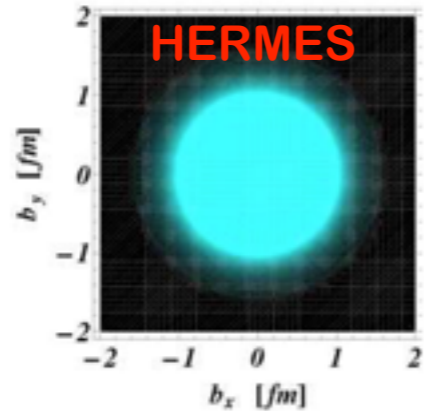
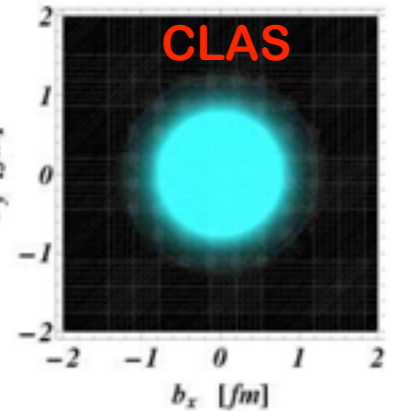
# DVCS evolution over the years

Global analysis of GPDs and CFFs



## From CFFs to spatial charge densities

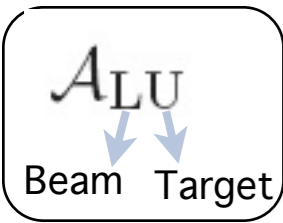
$$H(x, b_{\perp}) = \int_0^{\infty} \frac{d\Delta_{\perp}}{2\pi} \Delta_{\perp} J_0(b_{\perp} \Delta_{\perp}) H(x, 0, -\Delta_{\perp}^2)$$



M. Guidal, H. Moutarde, M. Vanderhaeghen, arxiv.org:1303.6600

# Backup

# Azimuthal asymmetries and GPDs



Single-charge beam-helicity asymmetry

$$A_{LU}(\phi) \equiv \frac{d\sigma^{\rightarrow} - d\sigma^{\leftarrow}}{d\sigma^{\rightarrow} + d\sigma^{\leftarrow}}$$

no separate access to  $s_1^l$  and  $s_1^{DVCS}$

Beam-helicity asymmetries with 2 beam charges

Charge-average  $A_{LU}$

Charge-difference  $A_{LU}$

$s_1^{DVCS}$  and  $s_1^l$  can be disentangled

Beam-charge asymmetry

$$A_C(\phi) \equiv \frac{d\sigma^+ - d\sigma^-}{d\sigma^+ + d\sigma^-}$$

## Compton Form Factors (CFFs)

$$\mathcal{F}(\xi, t) = \sum_q \int_{-1}^1 dx C_q^{\mp}(\xi, x) F^q(x, \xi, t)$$

twist-2 GPD

Measure asymmetry

Extract its azimuthal moments (extended Maximum Likelihood Fit)

Those azimuthal asymmetry amplitudes are related to certain linear or bi-linear combinations of CFFs.

Transverse target-spin asymmetry

$$A_{UT}^{DVCS}(\phi, \phi_S) \quad A_{UT}^I(\phi, \phi_S)$$

Double-spin (LT) asymmetry

$$\mathcal{A}_{LT}^I(\phi, \phi_S) \quad \mathcal{A}_{LT}^{BH+DVCS}(\phi, \phi_S)$$

$A_{UL}(\phi, e_l) \equiv$  Longitudinal target-spin asymmetry

$$\frac{[\sigma^{\leftarrow \Rightarrow}(\phi, e_l) + \sigma^{\rightarrow \Rightarrow}(\phi, e_l)] - [\sigma^{\leftarrow \leftarrow}(\phi, e_l) + \sigma^{\rightarrow \leftarrow}(\phi, e_l)]}{[\sigma^{\leftarrow \Rightarrow}(\phi, e_l) + \sigma^{\rightarrow \Rightarrow}(\phi, e_l)] + [\sigma^{\leftarrow \leftarrow}(\phi, e_l) + \sigma^{\rightarrow \leftarrow}(\phi, e_l)]}$$

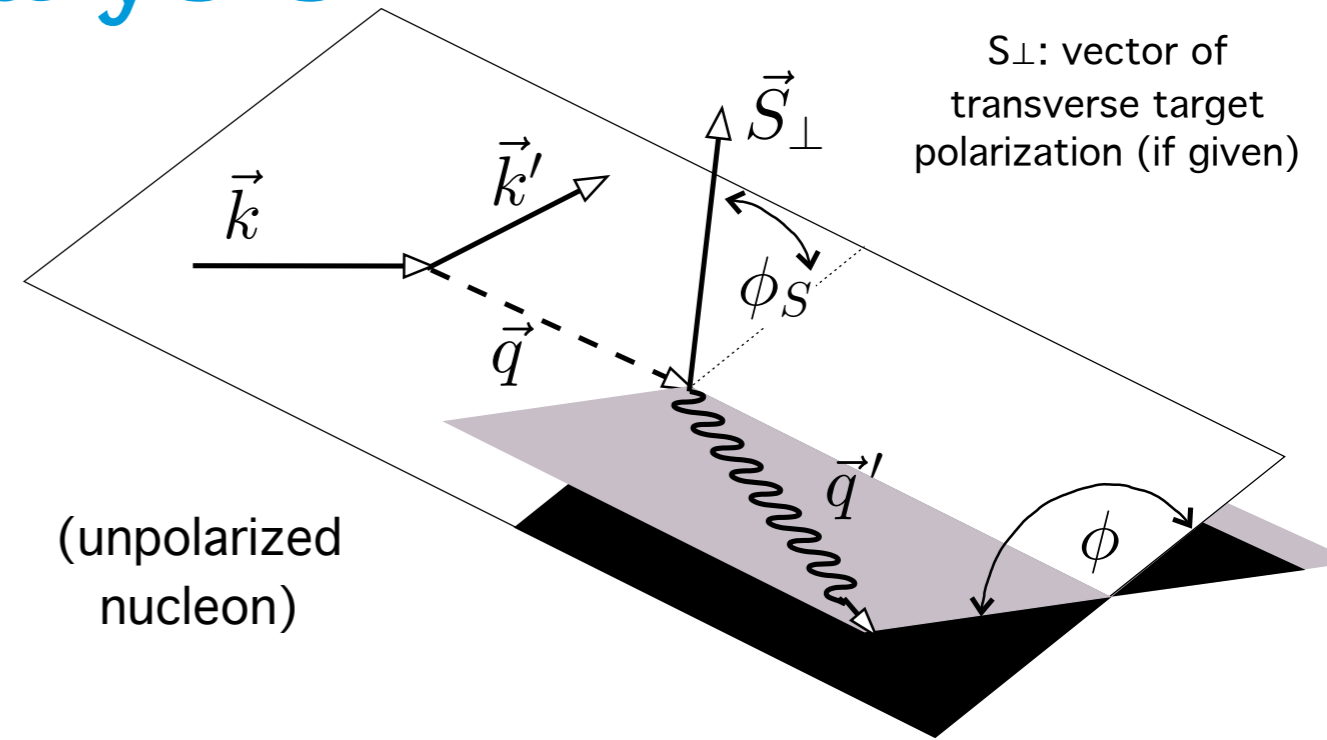
$A_{LL}(\phi, e_l) \equiv$  Double-spin (LL) asymmetry

$$\frac{[\sigma^{\rightarrow \Rightarrow}(\phi, e_l) + \sigma^{\leftarrow \leftarrow}(\phi, e_l)] - [\sigma^{\leftarrow \Rightarrow}(\phi, e_l) + \sigma^{\rightarrow \leftarrow}(\phi, e_l)]}{[\sigma^{\rightarrow \Rightarrow}(\phi, e_l) + \sigma^{\leftarrow \leftarrow}(\phi, e_l)] + [\sigma^{\leftarrow \Rightarrow}(\phi, e_l) + \sigma^{\rightarrow \leftarrow}(\phi, e_l)]}$$

# Harmonic analysis

lepton beam  $k$  with charge  $C_B$  and helicity  $P_B$

$S_{\perp}$ : vector of transverse target polarization (if given)



$$|\tau_{\text{BH}}|^2 = \frac{K_{\text{BH}}}{\mathcal{P}_1(\phi) \mathcal{P}_2(\phi)} \left\{ \sum_{n=0}^2 c_n^{\text{BH}} \cos(n\phi) \right\}$$

$$|\tau_{\text{DVCS}}|^2 = \frac{1}{Q^2} \left\{ \sum_{n=0}^2 c_n^{\text{DVCS}} \cos(n\phi) + \lambda s_1^{\text{DVCS}} \sin \phi \right\}$$

$$I = \frac{-e_{\ell} K_I}{\mathcal{P}_1(\phi) \mathcal{P}_2(\phi)} \left\{ \sum_{n=0}^3 c_n^{\text{I}} \cos(n\phi) + \sum_{n=1}^2 \lambda s_n^{\text{I}} \sin(n\phi) \right\}$$

(unpolarized nucleon)

$$\sigma(\phi; P_B, C_B) = \sigma_{\text{UU}}(\phi) \cdot [1 + P_B \mathcal{A}_{\text{LU}}^{\text{DVCS}}(\phi) + C_B P_B \mathcal{A}_{\text{LU}}^{\text{I}}(\phi) + C_B \mathcal{A}_{\text{C}}(\phi)]$$

Old approach at HERMES and CLAS: single-charge  $\mathcal{A}_{\text{LU}}$

**Beam-helicity asymmetries**

**Beam-charge asymmetry**

$$\mathcal{A}_{\text{LU}}(\phi) \equiv \frac{d\sigma^{\rightarrow} - d\sigma^{\leftarrow}}{d\sigma^{\rightarrow} + d\sigma^{\leftarrow}}$$

$$\mathcal{A}_{\text{C}}(\phi) \equiv \frac{d\sigma^{+} - d\sigma^{-}}{d\sigma^{+} + d\sigma^{-}}$$

no separate access to  $s_1^{\text{I}}$  and  $s_1^{\text{DVCS}}$

Approach at HERMES:  
 $s_1^{\text{I}}$  and  $s_1^{\text{DVCS}}$  can be disentangled  
**Need 2 beam charges!**

**Charge-average  $\mathcal{A}_{\text{LU}}$ :**

**Charge-difference  $\mathcal{A}_{\text{LU}}$ :**

$$\mathcal{A}_{\text{LU}}^{\text{DVCS}}(\phi) \equiv \frac{(d\sigma^{+\rightarrow} - d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} - d\sigma^{-\leftarrow})}{(d\sigma^{+\rightarrow} + d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} + d\sigma^{-\leftarrow})}$$

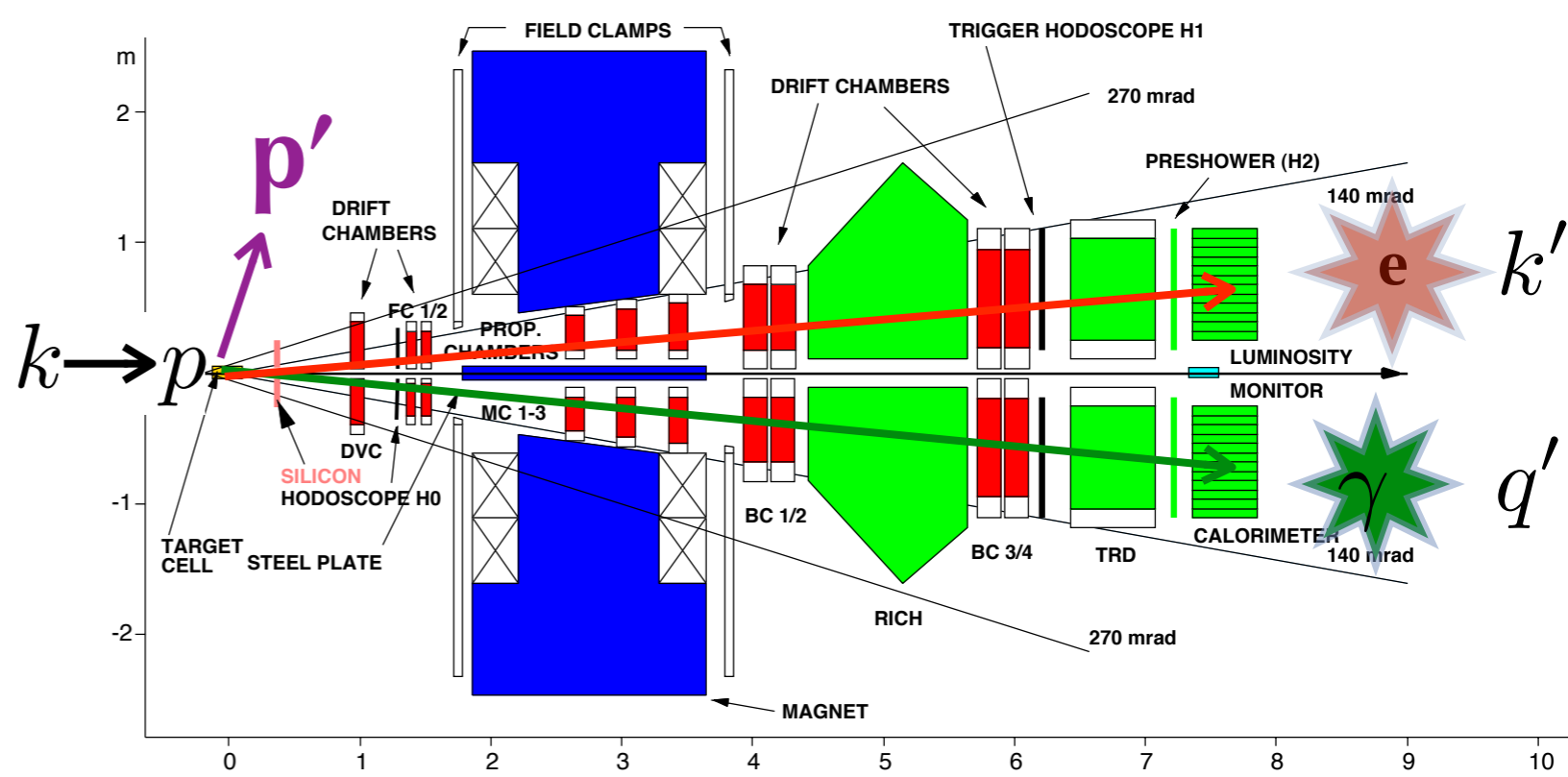
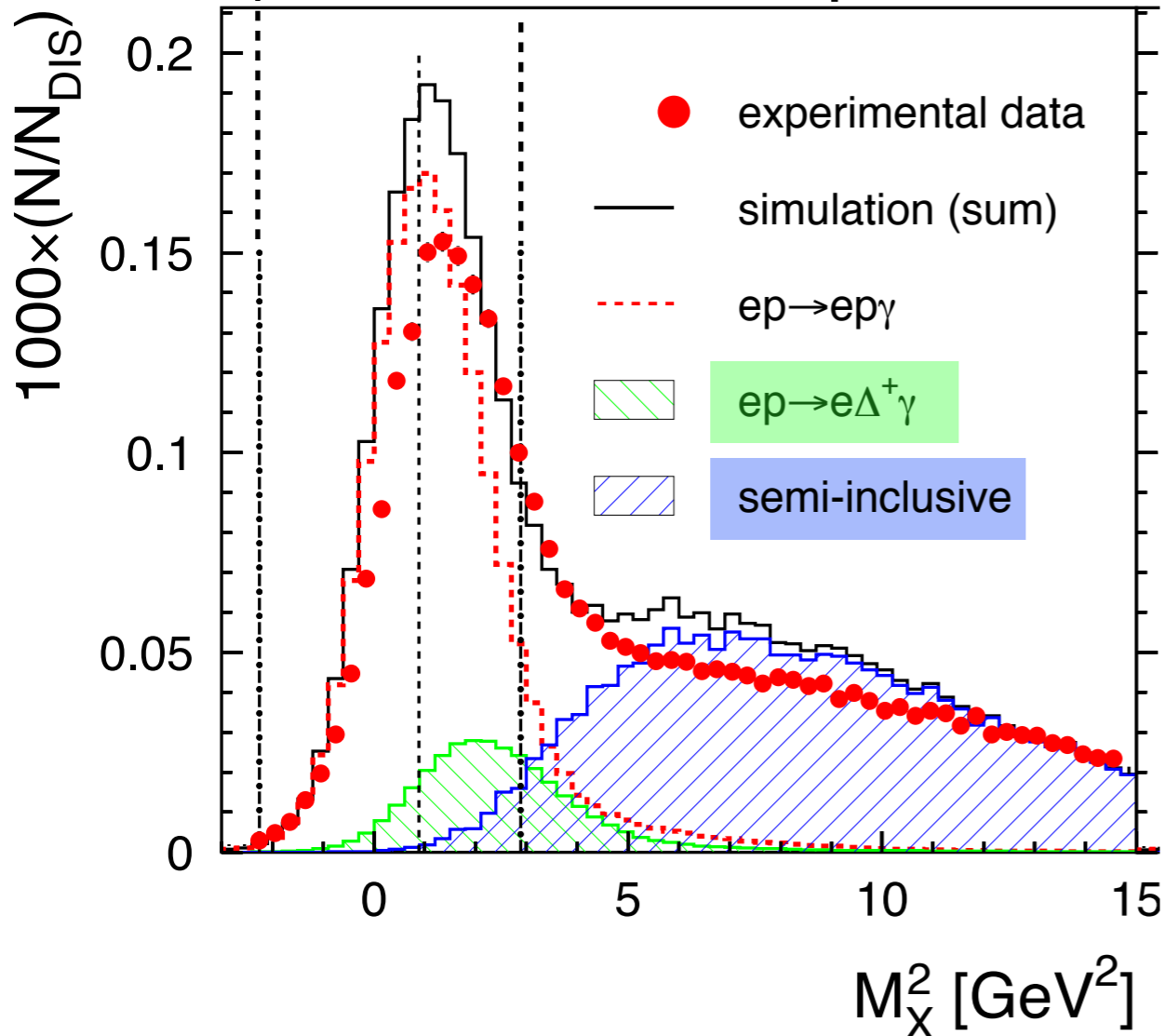
$$\mathcal{A}_{\text{LU}}^{\text{I}}(\phi) \equiv \frac{(d\sigma^{+\rightarrow} - d\sigma^{+\leftarrow}) - (d\sigma^{-\rightarrow} - d\sigma^{-\leftarrow})}{(d\sigma^{+\rightarrow} + d\sigma^{+\leftarrow}) + (d\sigma^{-\rightarrow} + d\sigma^{-\leftarrow})}$$

# “Traditional” DVCS Analysis at HERMES

“exclusive region” in  $(\text{missing mass})^2$



unresolved sample



- No other charged tracks reconstructed
- No other untracked clusters in the calorimeter

Missing-mass technique

$$M_X^2 = (k + p - k' - q')^2$$

$ep \rightarrow eX\gamma$  sample

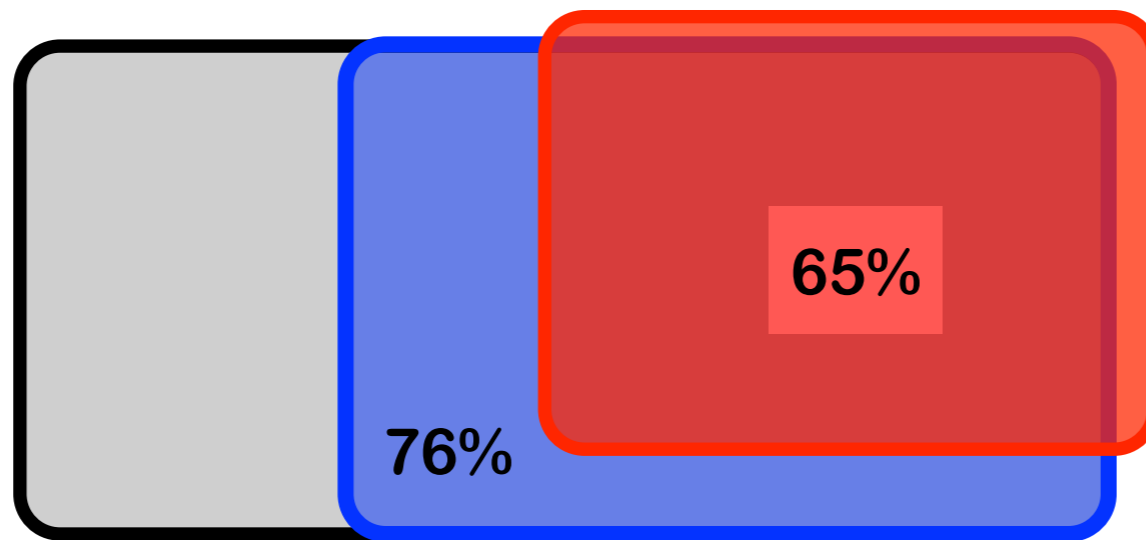
about 12%

- ✗ Unresolved for associated production
- ✓ Semi-inclusive neutral pion production corrected for

about 3%

# HERMES: unresolved reference sample

Disentangling the effects of recoil-detector acceptance and purification



Loss due to

- lower-mom. threshold
- $\Phi$ -gaps of SSD

Deficit due to

- removal of background
- inefficiencies of  $\chi^2$  cut
- recoil-det. inefficiencies

