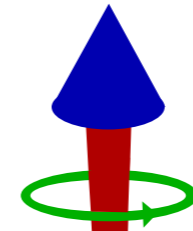


# Recent highlights

from



# hermes

## Outline:

Exploring the nucleon structure  
via

- ★ inclusive
- ★ semi-inclusive
- ★ exclusive

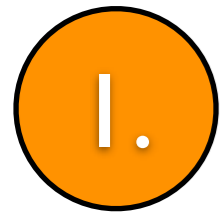
measurements in polarized  
electron-proton scattering

Caroline Riedl



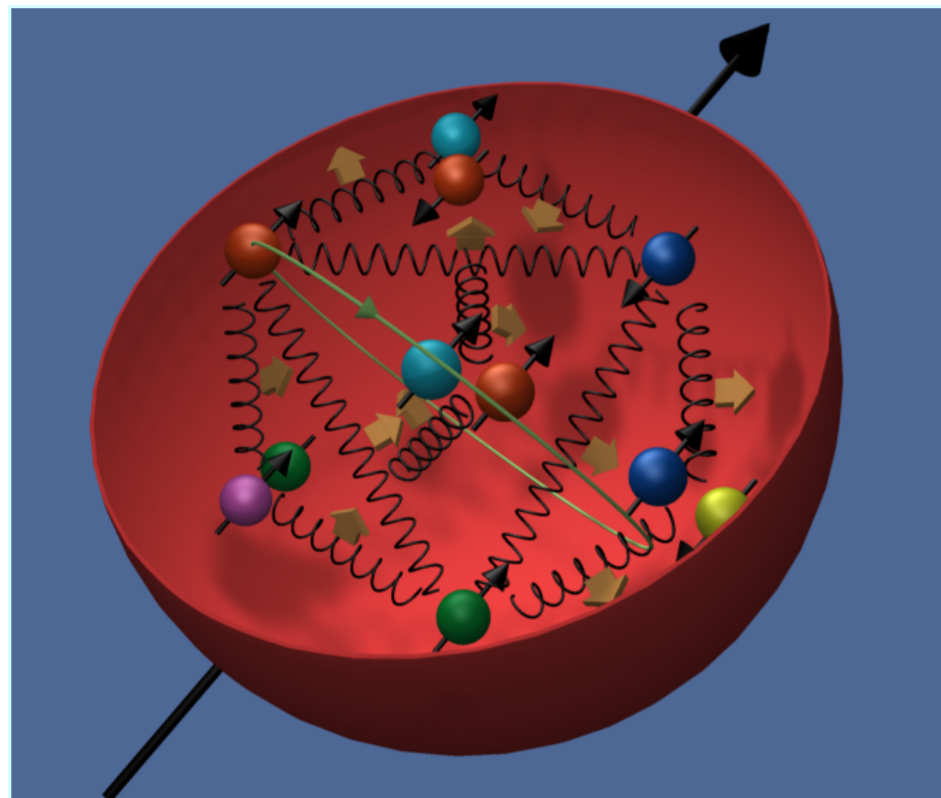
Moriond QCD and High-Energy Interactions  
La Thuile (Italy), March 16, 2012

# HERMES mission: Nucleon Structure



“Spin Puzzle”

$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + L_q + J_g$$



quark spin

quark orbital angular momentum

gluon spin and OAM

longitudinal momentum  
transverse momentum  
transverse position

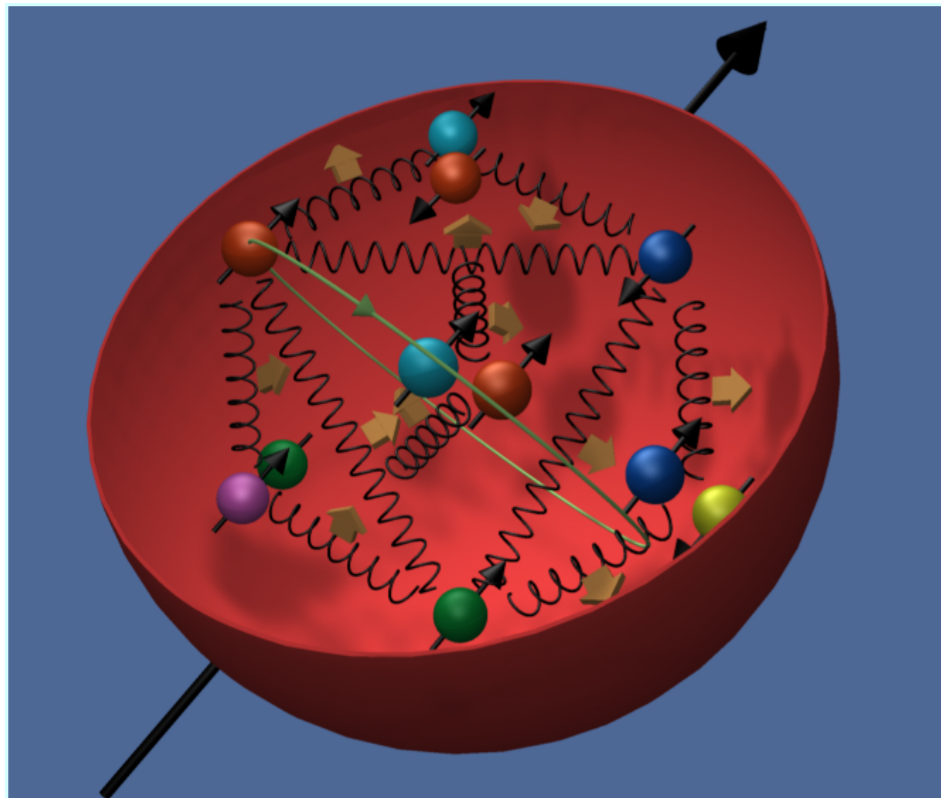
# HERMES mission: Nucleon Structure

1.

“Spin Puzzle”

$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + L_q + J_g$$

quark spin  
 quark orbital angular momentum  
 gluon spin and OAM



longitudinal momentum  
 transverse momentum  
 transverse position

Wigner phase-space distributions  
 [X. Ji, PRL 2003; A. Belitsky, X. Ji, F. Yuan, PRD 2004]

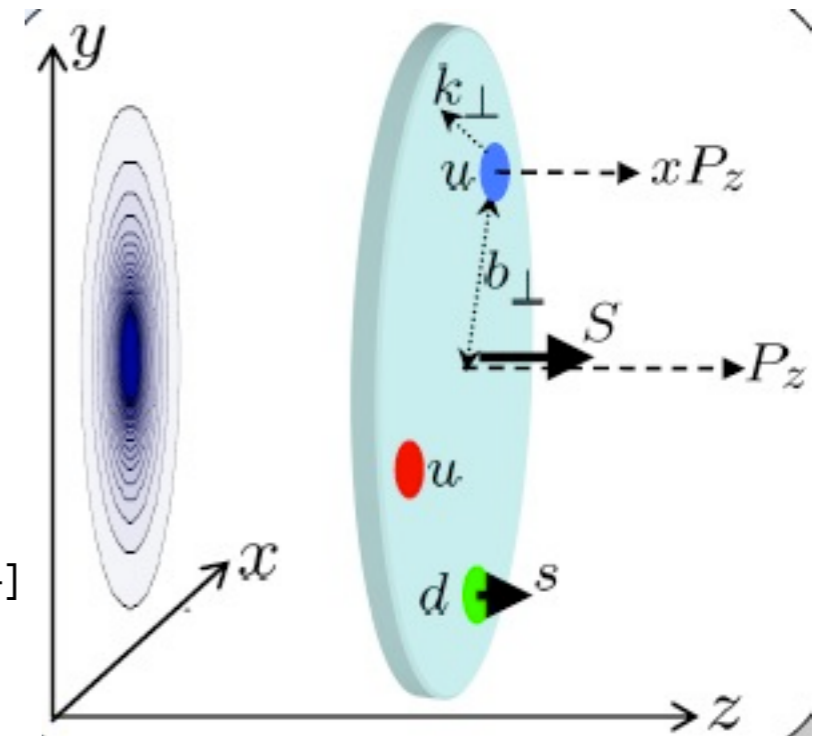
“mother distributions”  
 [Meissner, Metz, Schlegel, JHEP 0908:056, 2009]

“Dynamic Hologram”

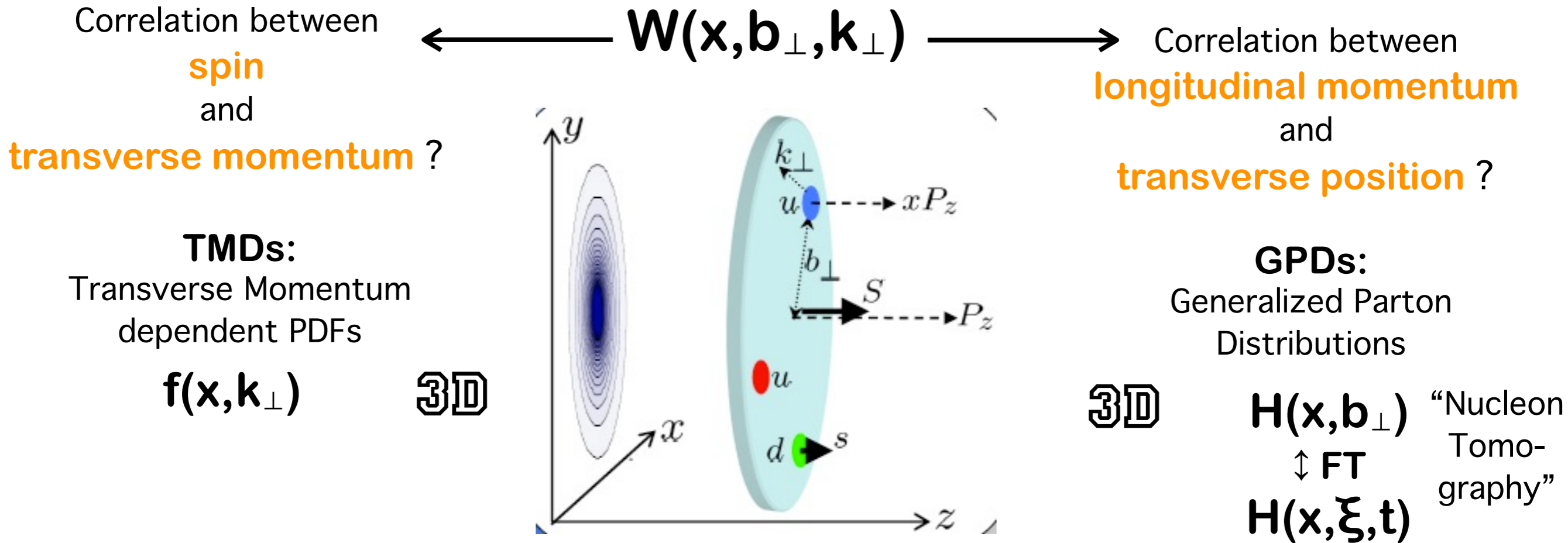
2.

$$W(x, b_{\perp}, k_{\perp})$$

probability of finding a quark with certain polarization, position and momentum



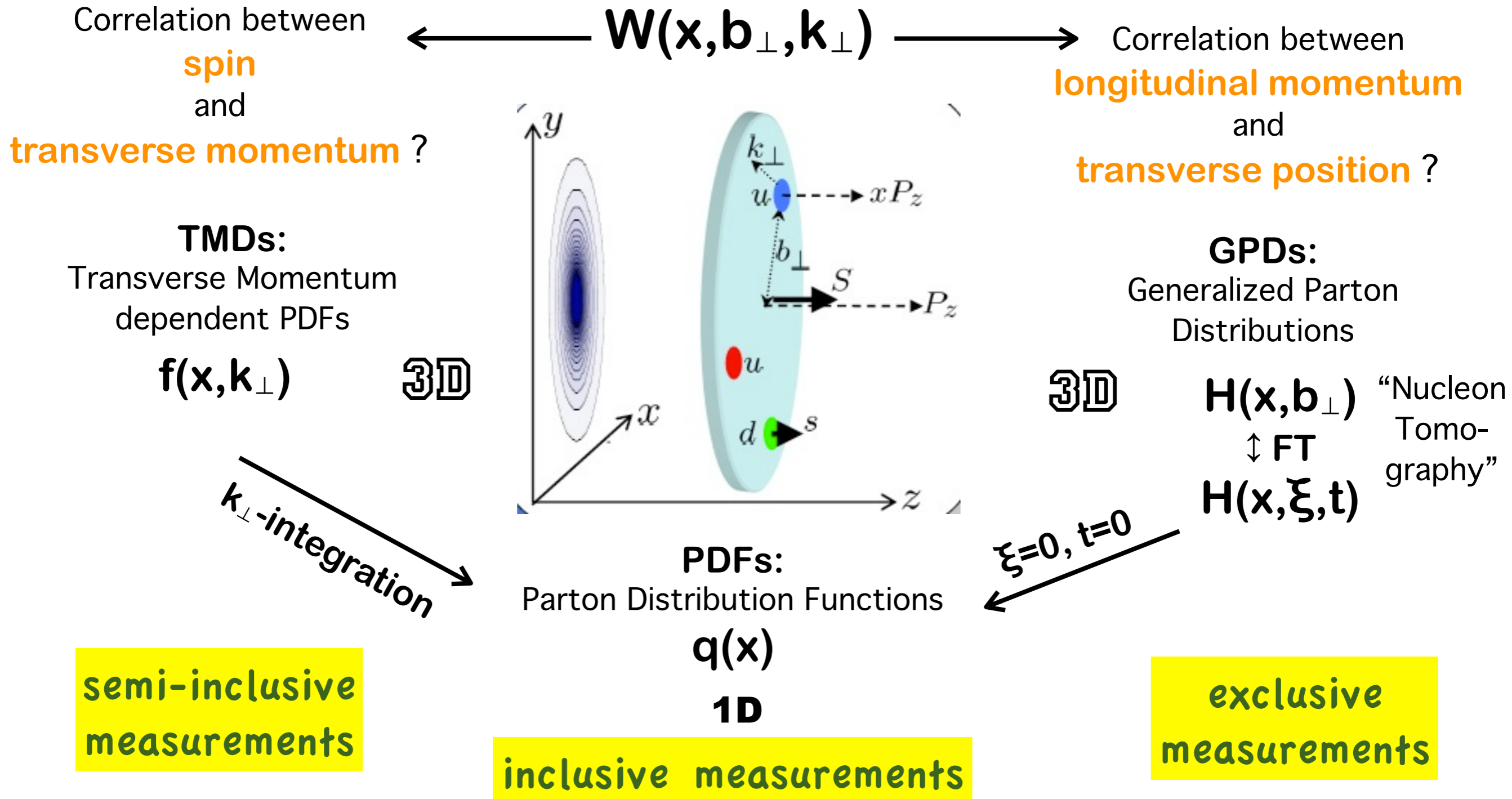
# TMDs and GPDs



**semi-inclusive measurements**

**exclusive measurements**

# TMDs and GPDs



# TMDs and GPDs

Orbital angular momentum

$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + L_q + J_g$$

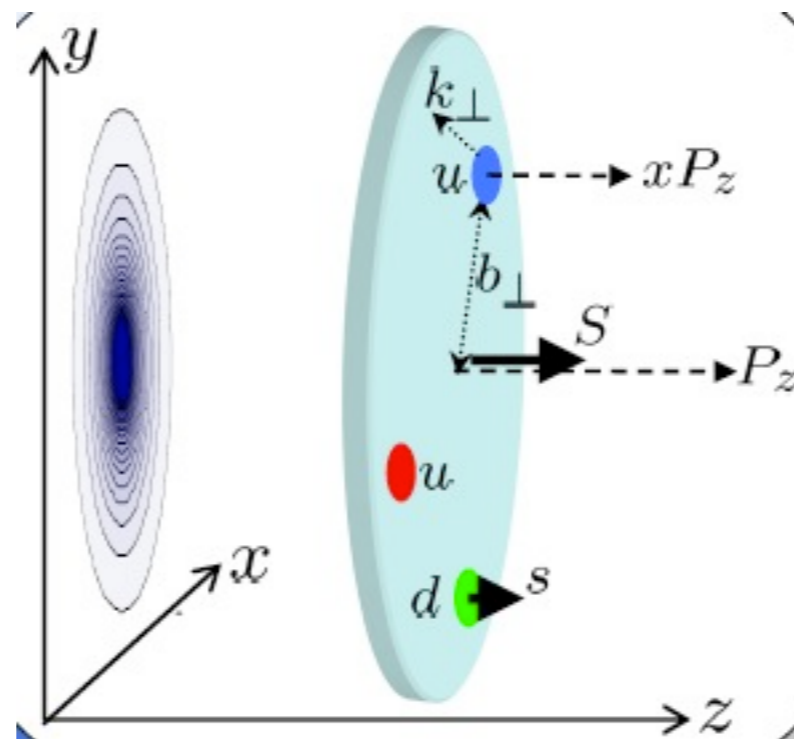
Correlation between **spin** and **transverse momentum** ?  $\leftarrow$   $W(x, b_{\perp}, k_{\perp})$   $\rightarrow$  Correlation between **longitudinal momentum** and **transverse position** ?

**TMDs:**  
Transverse Momentum dependent PDFs

$f(x, k_{\perp})$  **3D**

$k_{\perp}$ -integration  $\searrow$

semi-inclusive measurements



**PDFs:**  
Parton Distribution Functions

$q(x)$  **1D**

inclusive measurements

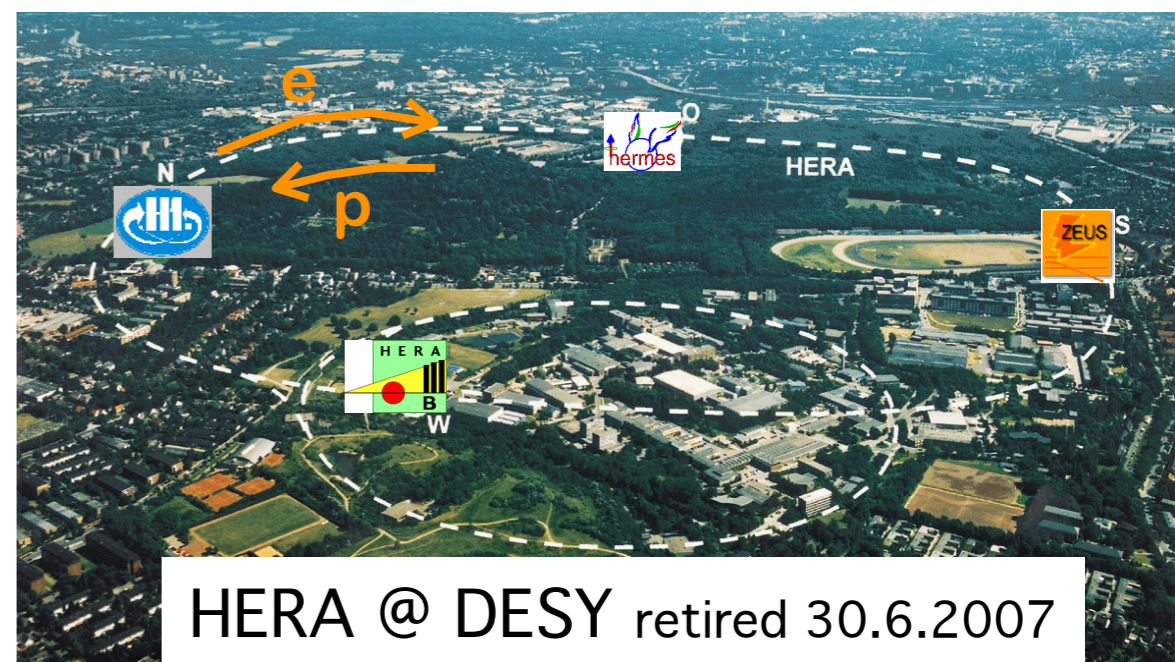
**GPDs:**  
Generalized Parton Distributions

$H(x, b_{\perp})$  "Nucleon Tomography"  
 $\updownarrow$  FT  
 $H(x, \xi, t)$

$\xi=0, t=0$   $\swarrow$

exclusive measurements

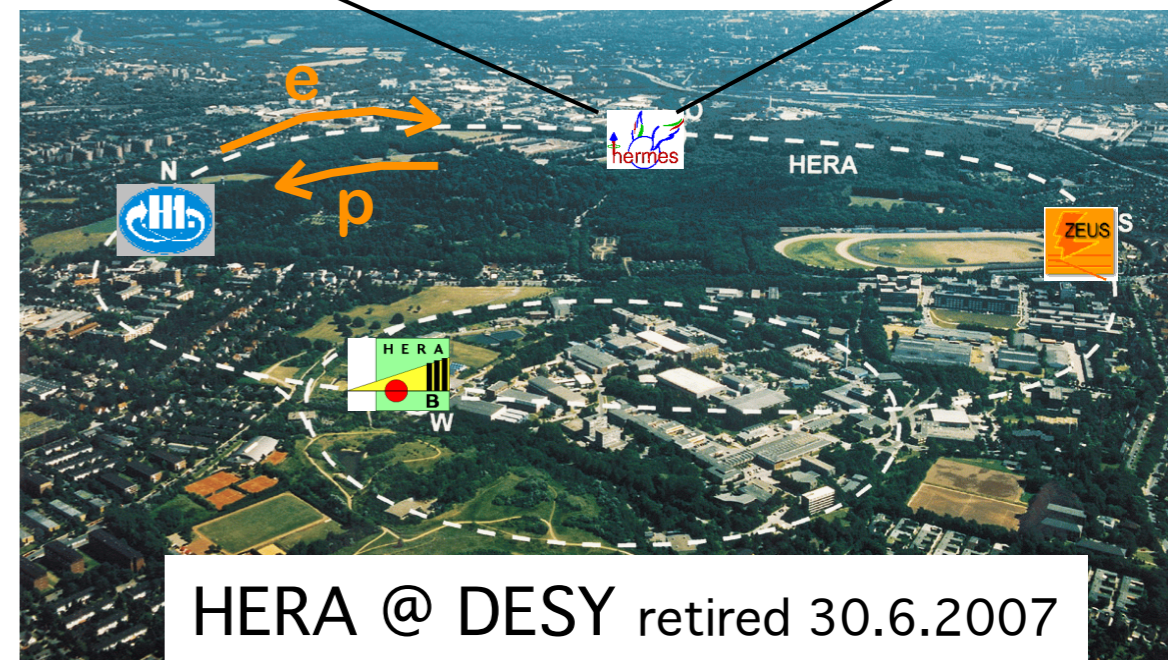
# HERMES @ DESY



# HERMES @ DESY

Hadron-type separation (pions, kaons, protons) with RICH detector

1995-2007

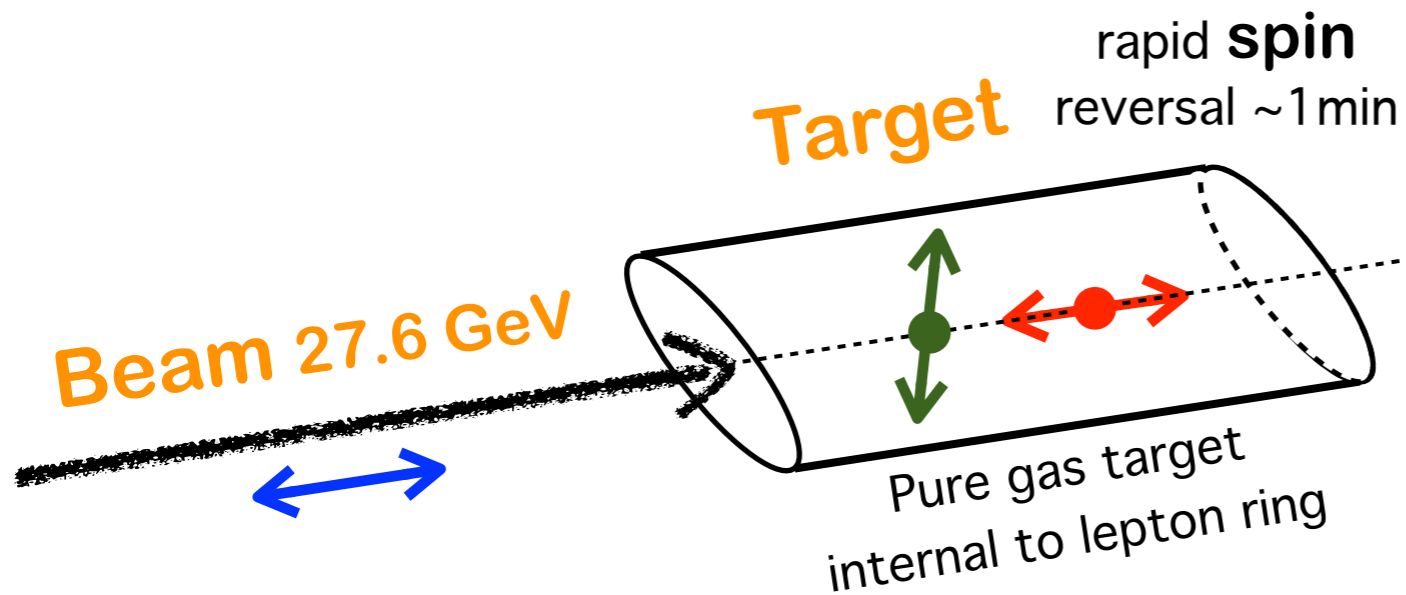




# HERMES @ DESY

Hadron-type separation (pions, kaons, protons) with **RICH detector**

1995-2007



➤ Longitudinally polarized leptons

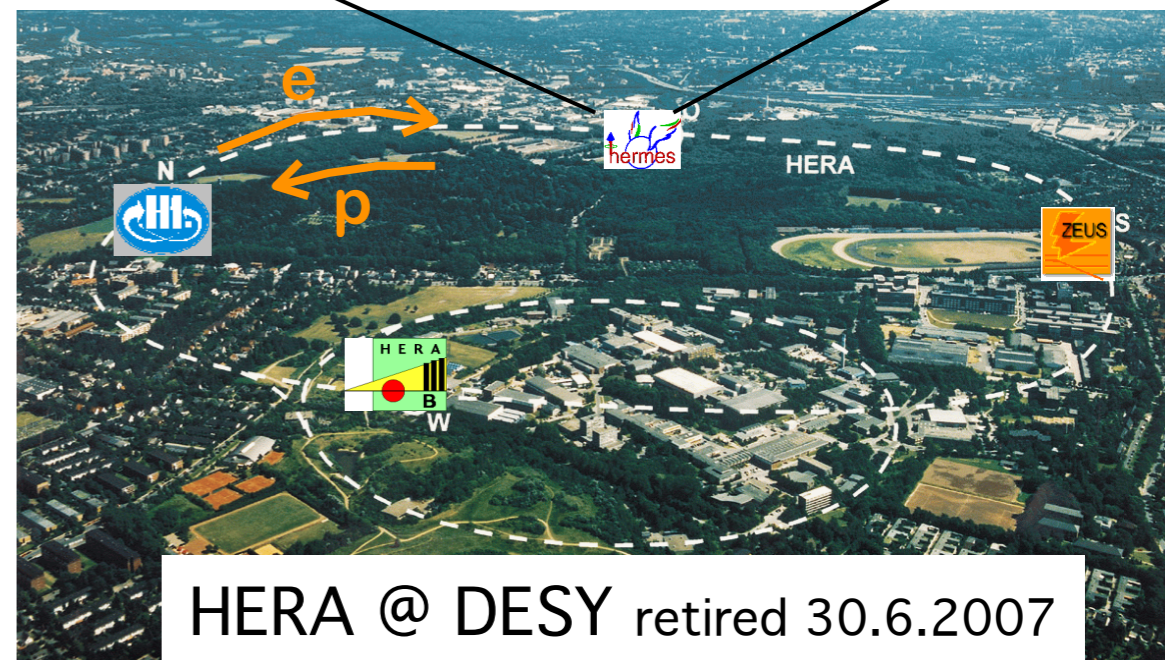
➤  $^1\text{H}$  with longitudinal (50 /pb) & transverse polarization (150 /pb)

➤ Regular helicity switch (few months)

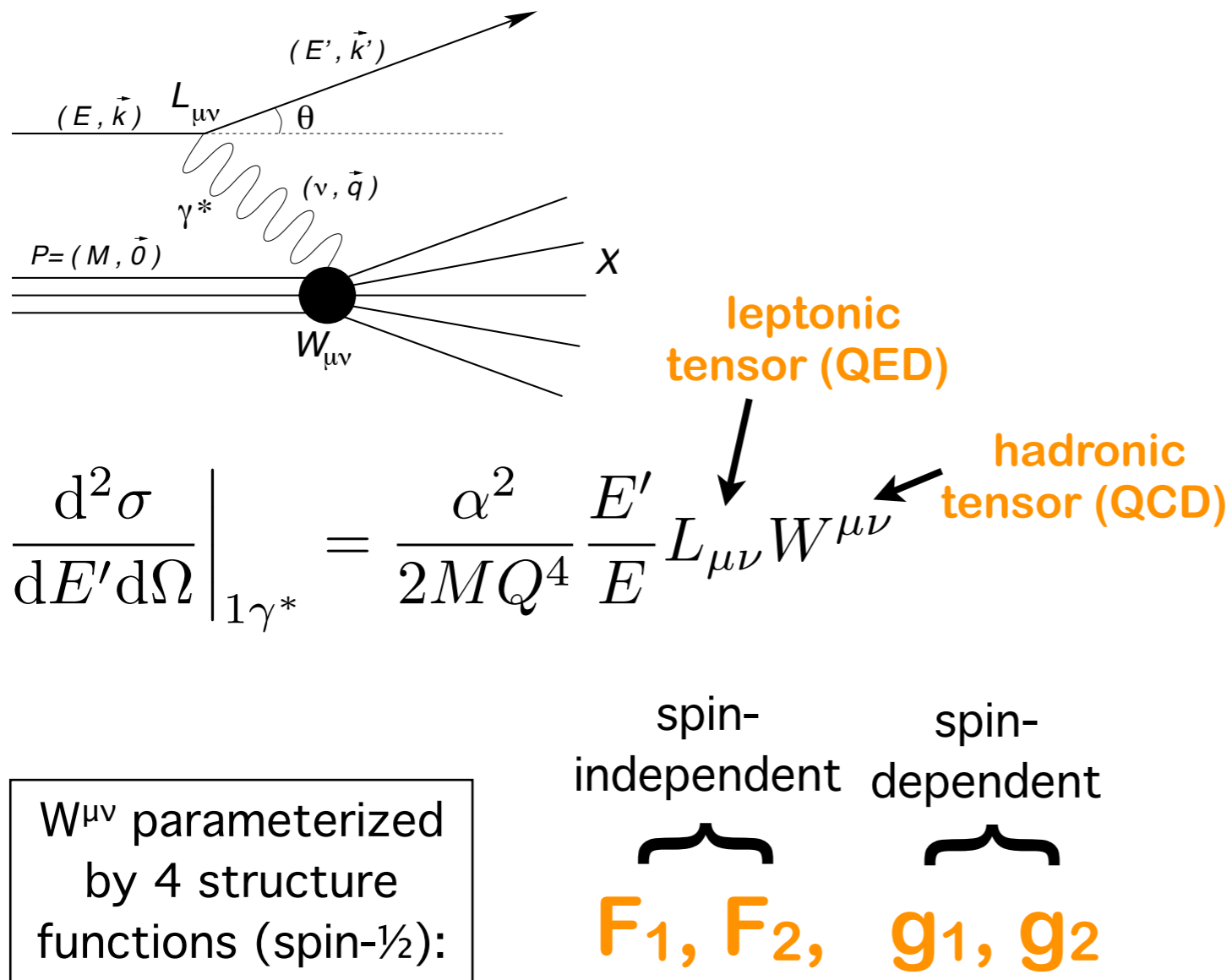
➤  $^2\text{H}$  with longitudinal polarization (200 /pb)

➤ Positrons and electrons

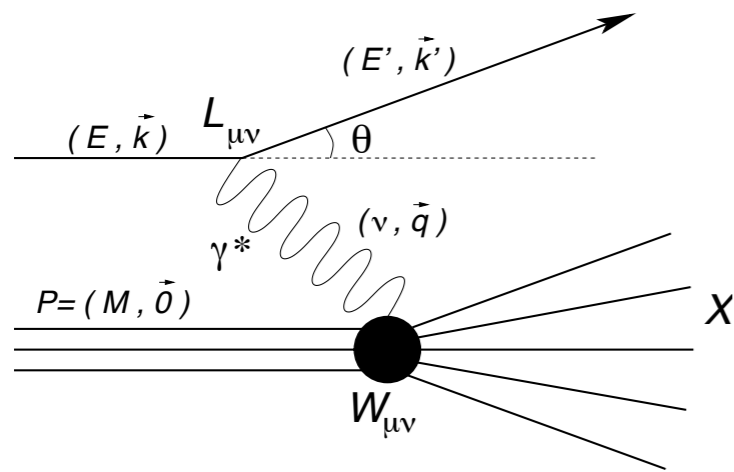
➤ Unpolarized  $^1\text{H}$  (1200 /pb),  $^2\text{H}$  (800 /pb)  
He, N, Ne, Kr, Xe (300 /pb)



# Inclusive measurements



# Inclusive measurements



$$\left. \frac{d^2\sigma}{dE' d\Omega} \right|_{1\gamma^*} = \frac{\alpha^2}{2MQ^4} \frac{E'}{E} L_{\mu\nu} W^{\mu\nu}$$

leptonic tensor (QED)

hadronic tensor (QCD)

$W^{\mu\nu}$  parameterized by 4 structure functions (spin-1/2):

spin-independent  $F_1, F_2$       spin-dependent  $g_1, g_2$

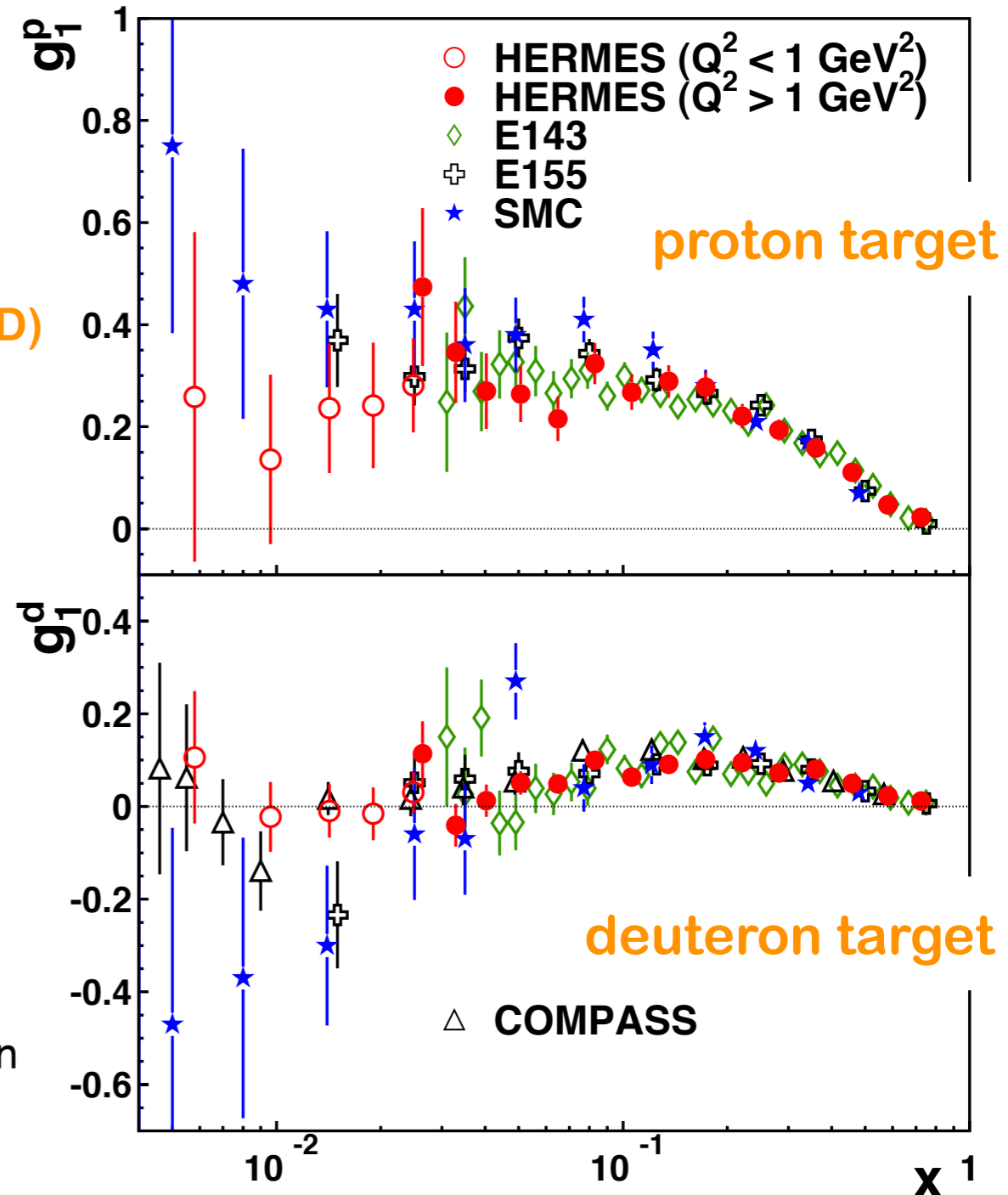
$$g_1 = \frac{1}{2} \sum_q e_q^2 (q^+ - q^-)$$

Probabilistic interpretation in Quark Parton Model (QPM)

$$\Delta\Sigma \approx 1/3$$

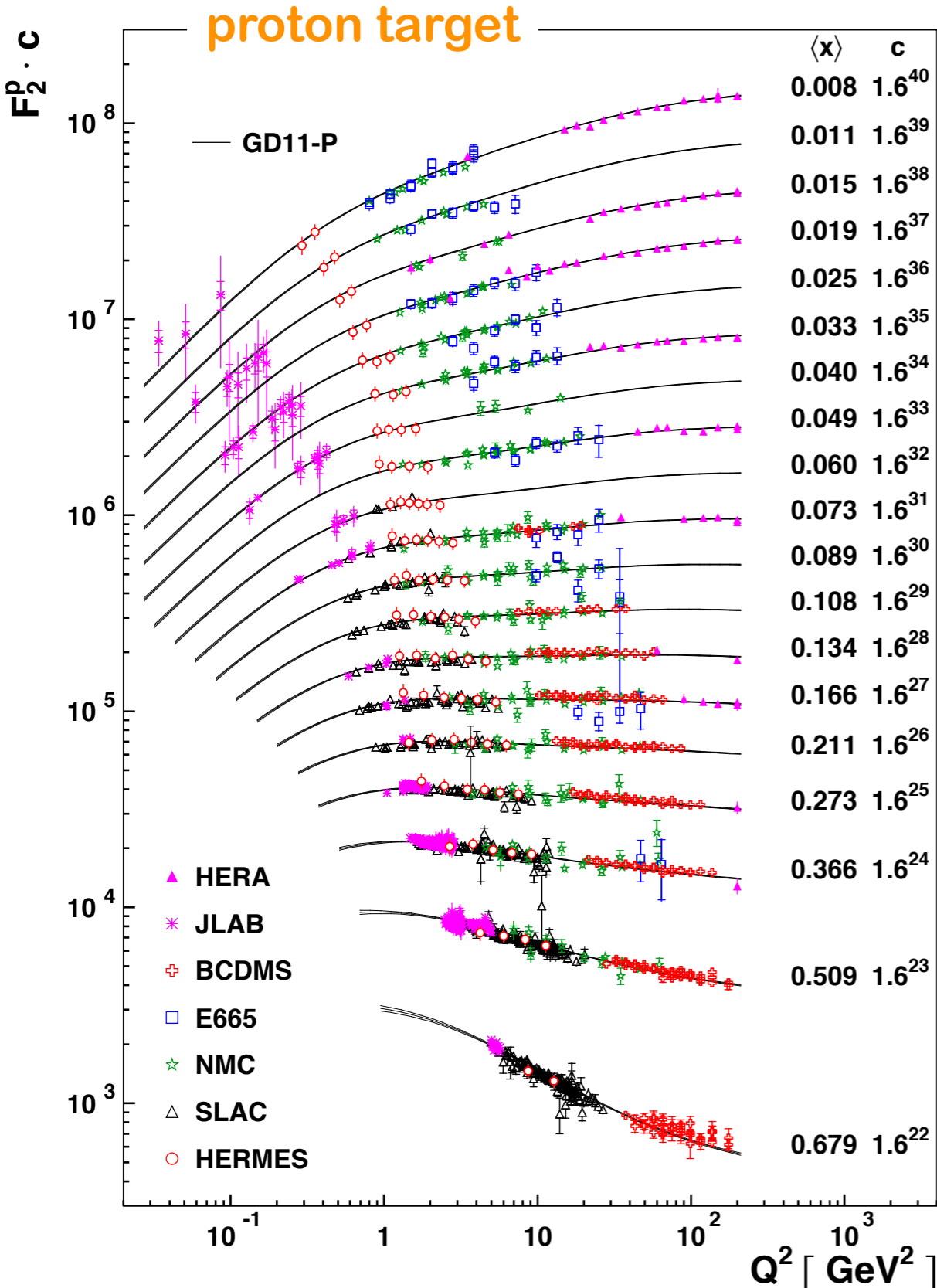
## Spin structure function $g_1$ (HERMES final result 2007)

A. Airapetian et al. [HERMES], Phys. Rev. D 75 (2007) 012007

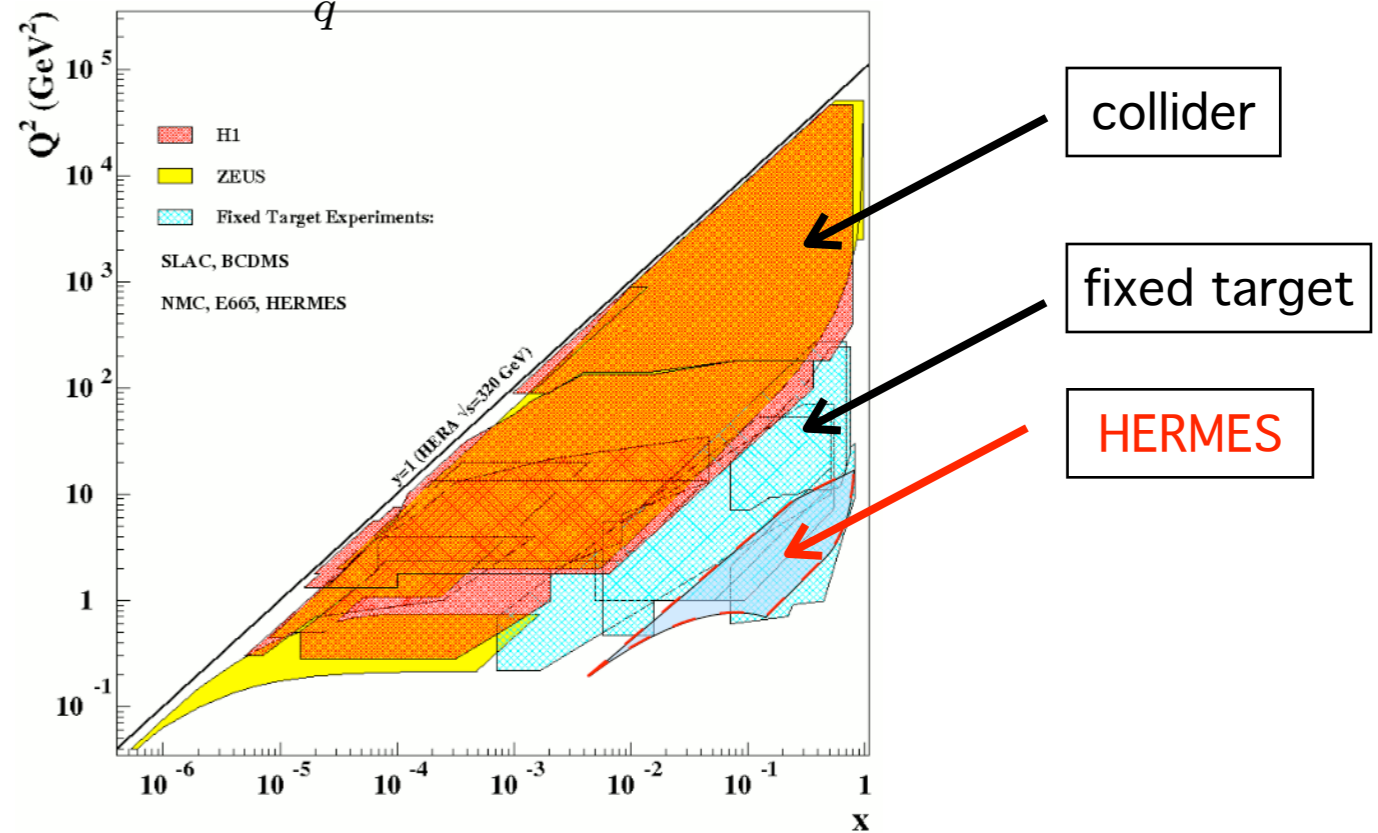


# Structure function $F_2$

A. Airapetian et al. [HERMES], JHEP 05 (2011)



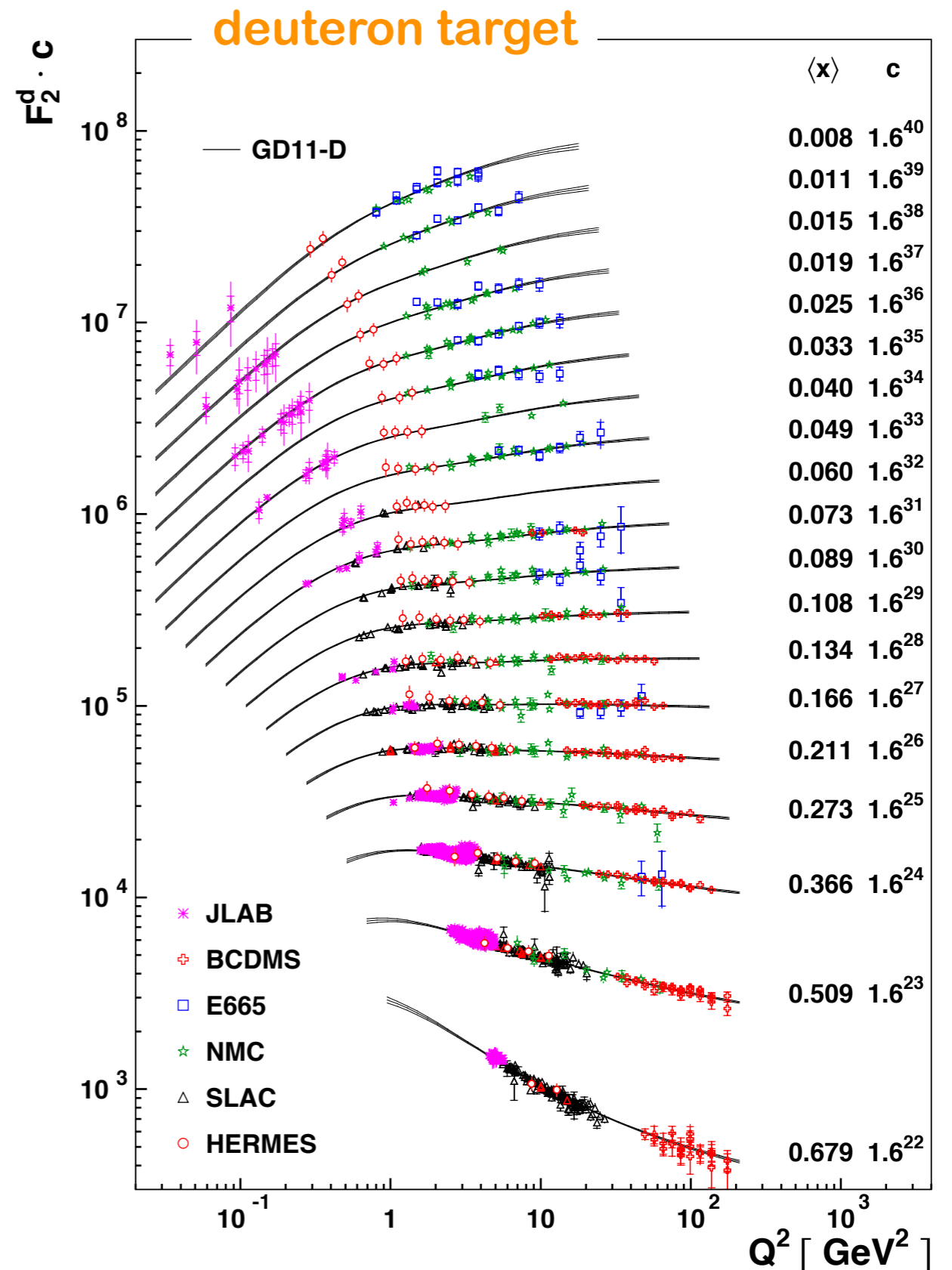
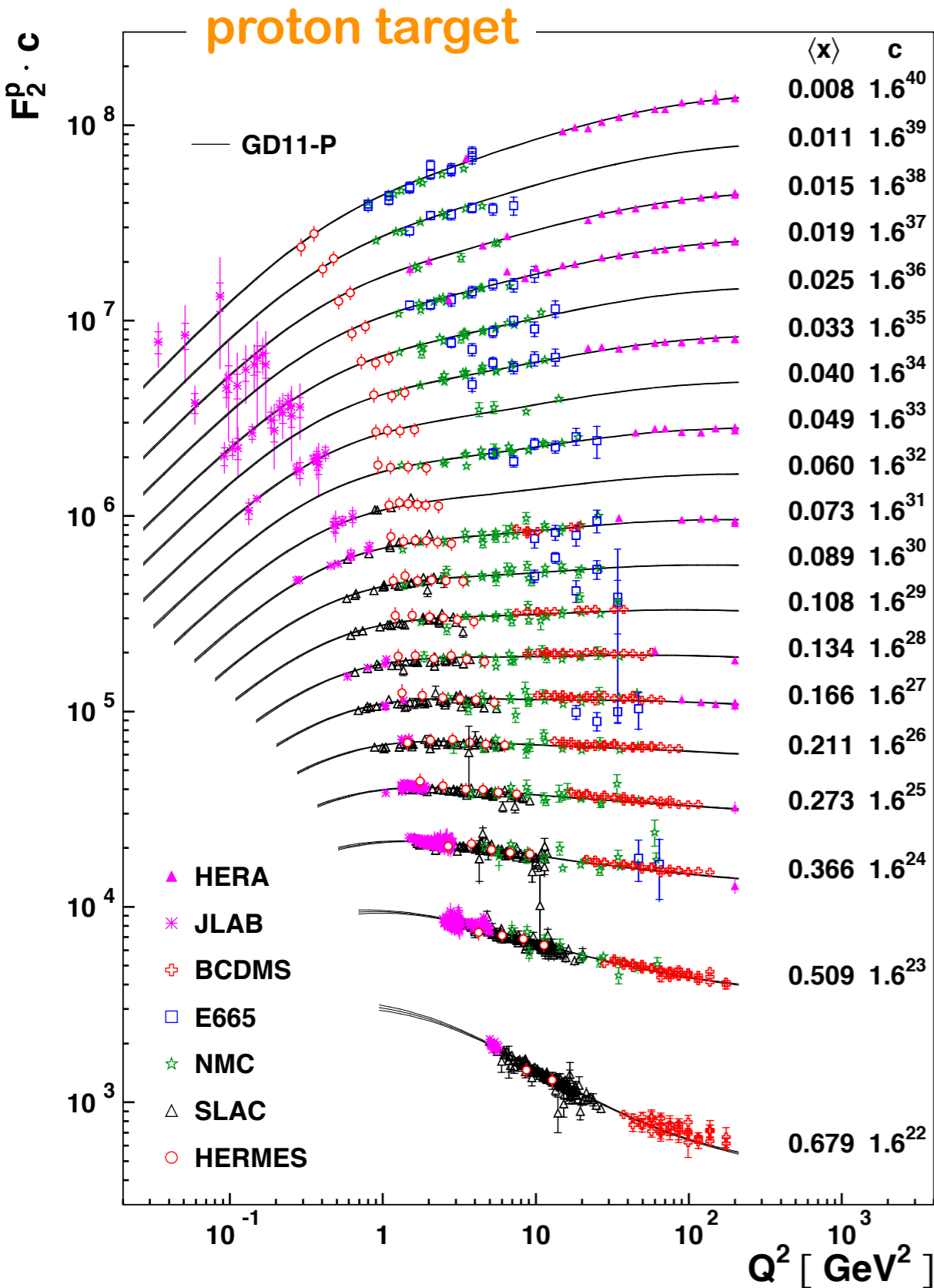
$$F_1 = \frac{1}{2} \sum_q e_q^2 (q^+ + q^-) \quad F_2 = f(F_1, R)$$



- HERMES data complementary to collider data, cover transition region between perturbative and non-perturbative regimes of QCD
- Agreement with world data in overlap region
- New region covered by HERMES
- GD11 global fit  
HERMES rel. normalization  $\sim 2\%$ ,  $0.5\%$  for p/d.

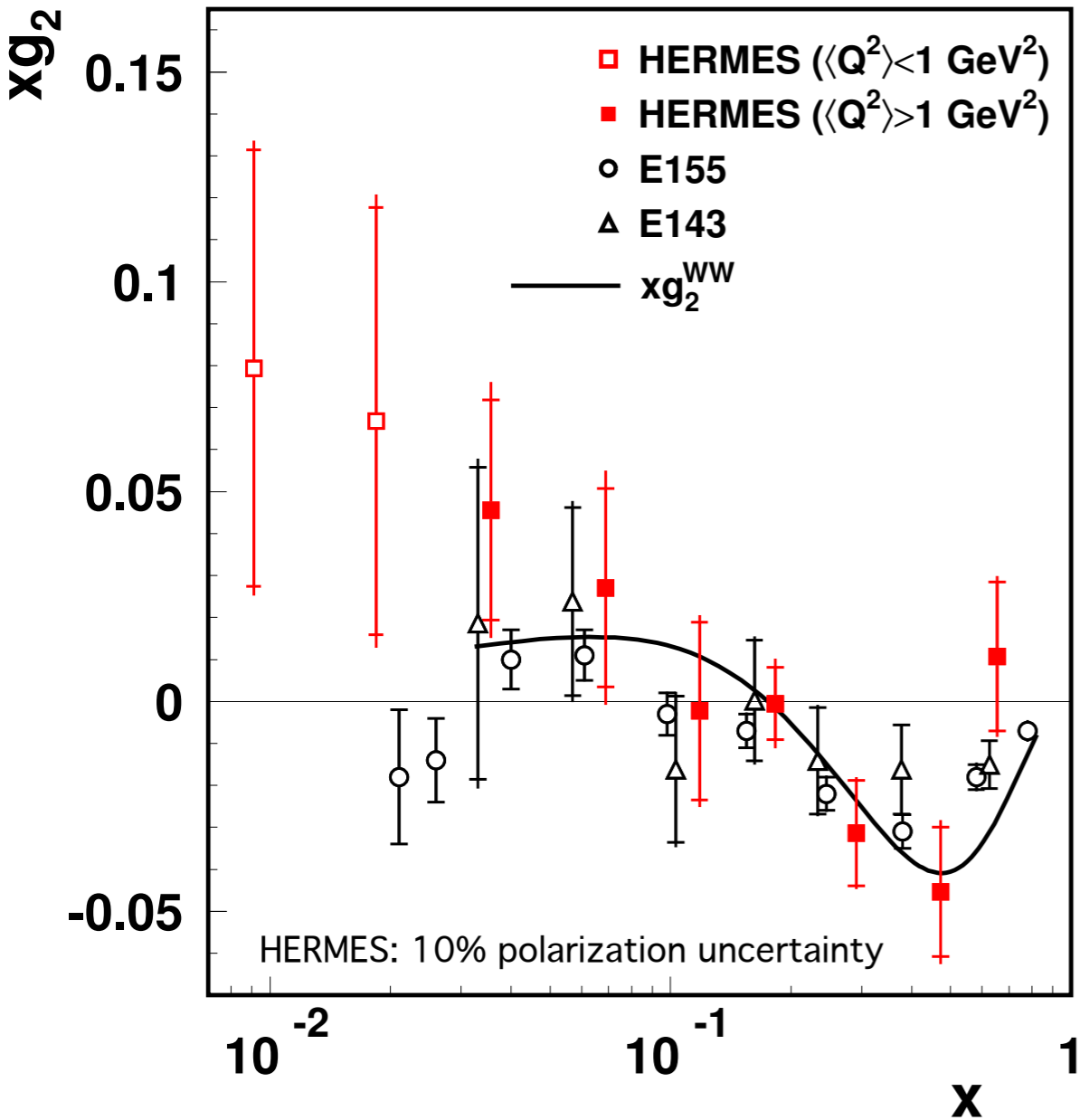
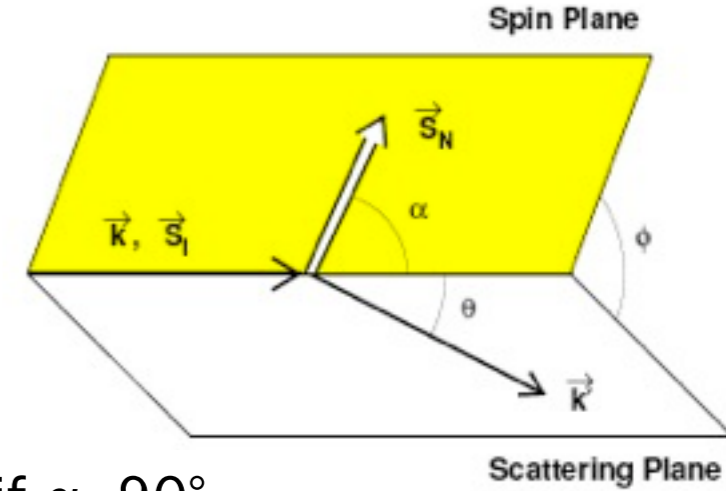
# Structure function $F_2$

A. Airapetian et al. [HERMES], JHEP 05 (2011)



# Spin structure function $g_2$

A. Airapetian et al. [HERMES], accepted by EPJ C (in press) [arXiv:1112.5584]

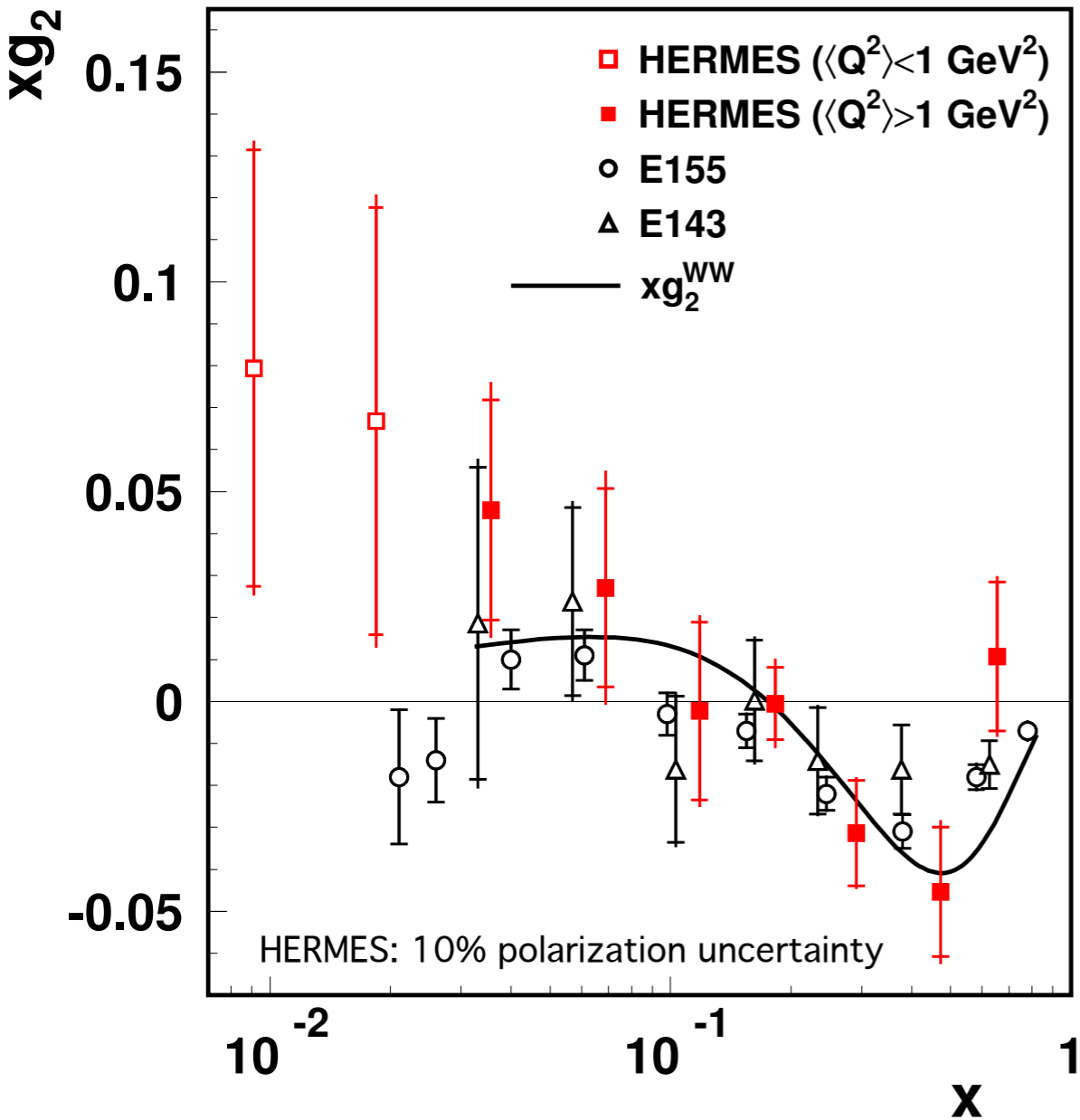
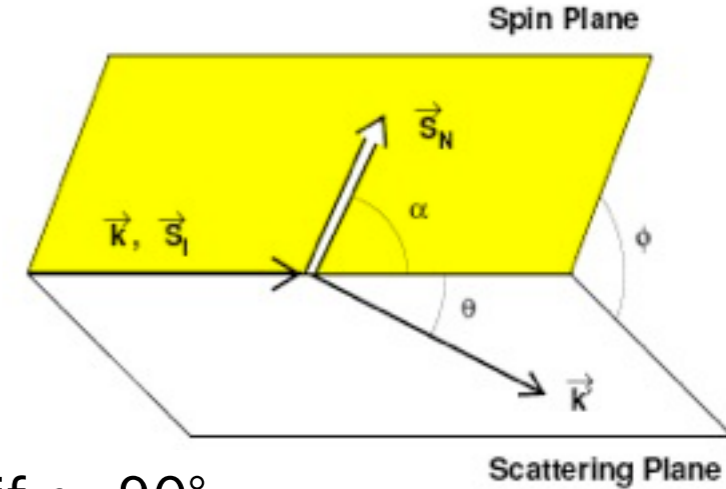


➡ Sensitivity to  $g_2$  highest if  $\alpha=90^\circ$

➡ QPM:  $g_2 \equiv 0$   
(no transverse degrees of freedom)

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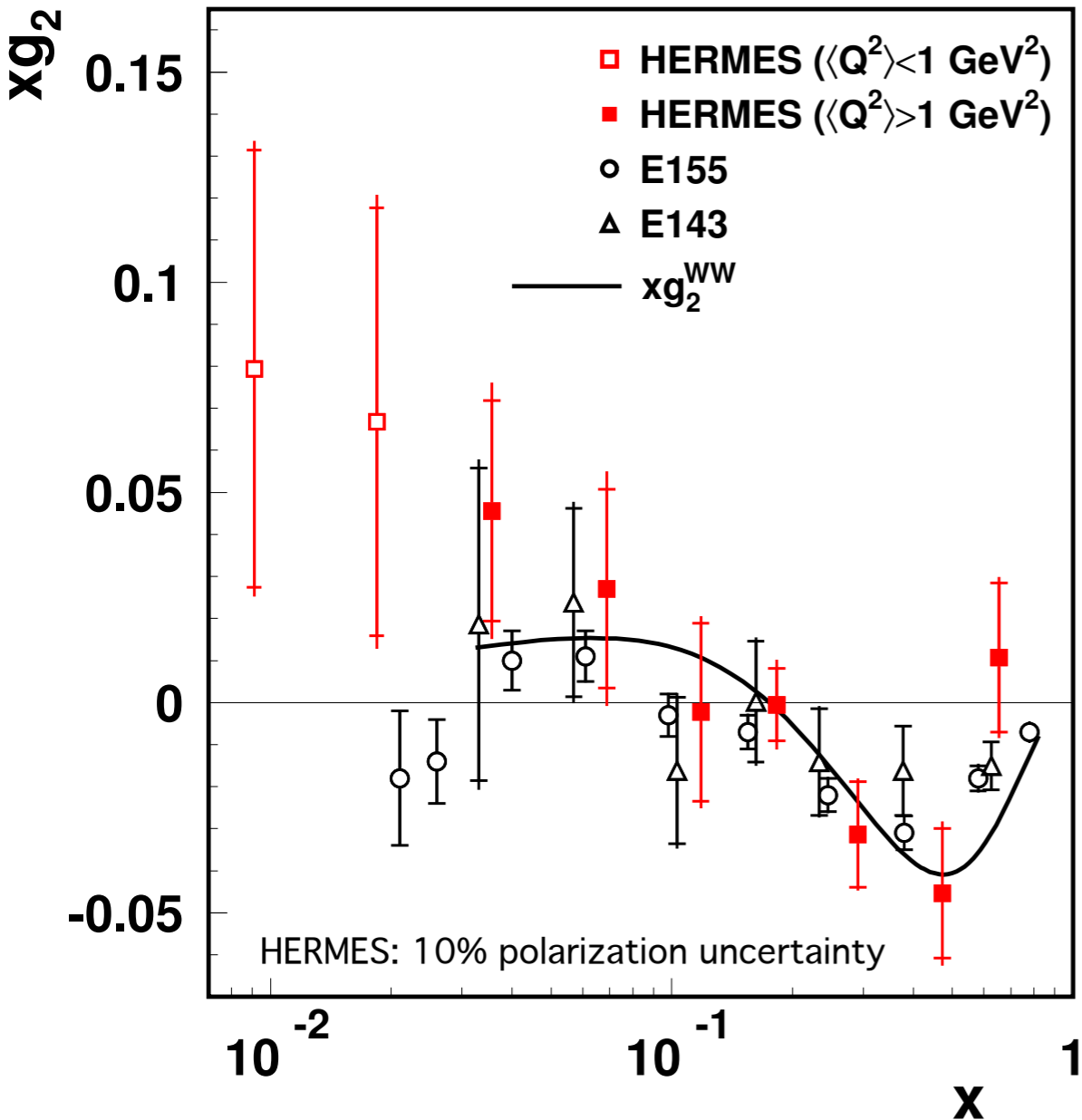
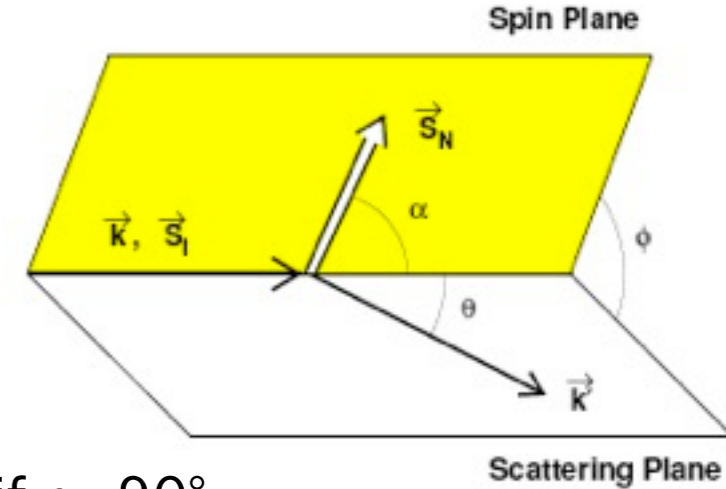
➡ OPE: **twist-2** **twist-3**

$$g_2(x, Q^2) = g_2^{\text{WW}}(x, Q^2) + \bar{g}_2(x, Q^2)$$

$$g_2^{\text{WW}}(x, Q^2) = -g_1(x, Q^2) + \int_x^1 g_1(y, Q^2) \frac{dy}{y} \quad \text{Wandzura-Wilczek relation}$$

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➤ Test of deviation from WW part:

$$d_2(Q^2) = 3 \int_0^1 x^2 \bar{g}_2(x, Q^2) dx$$

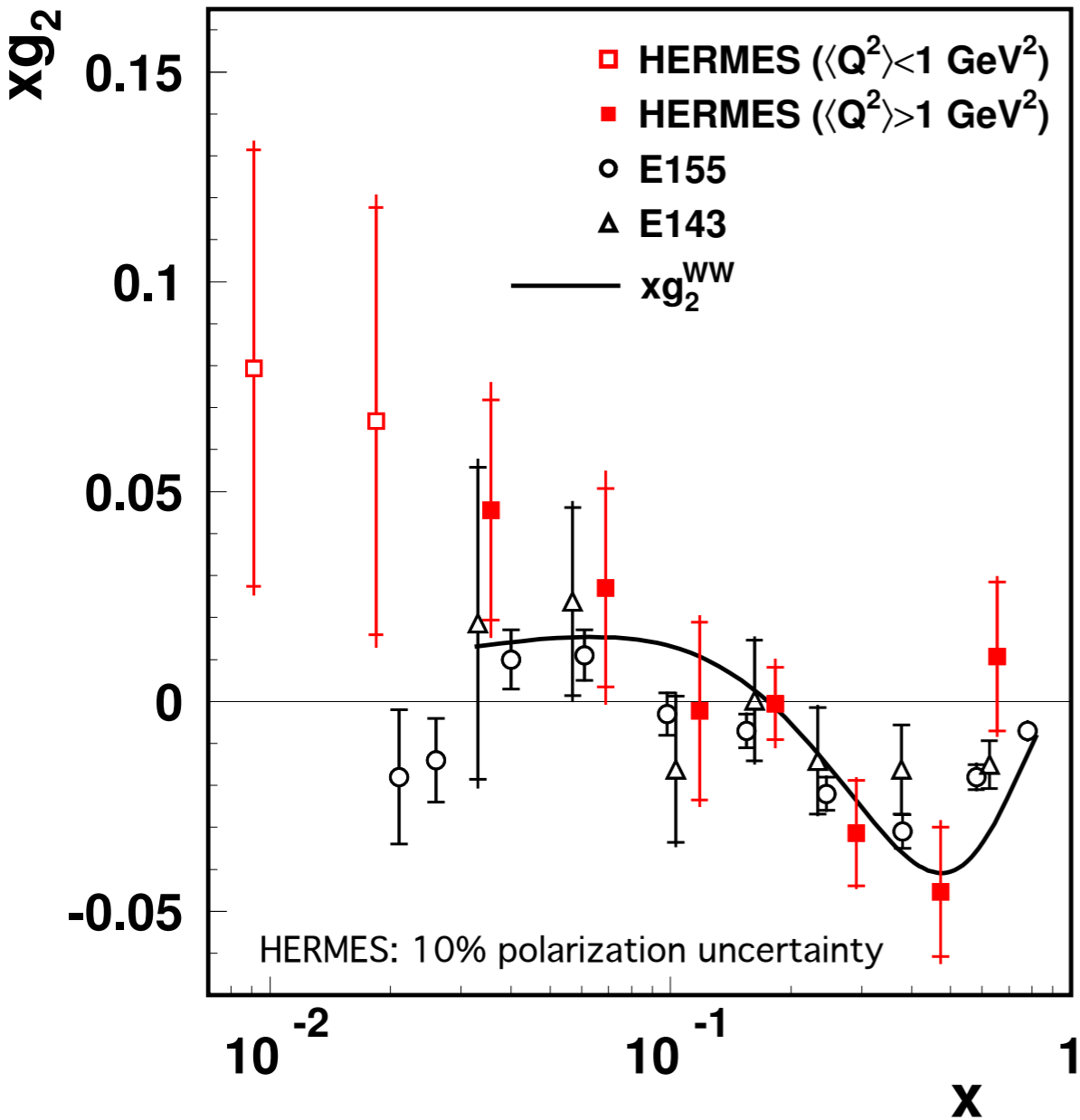
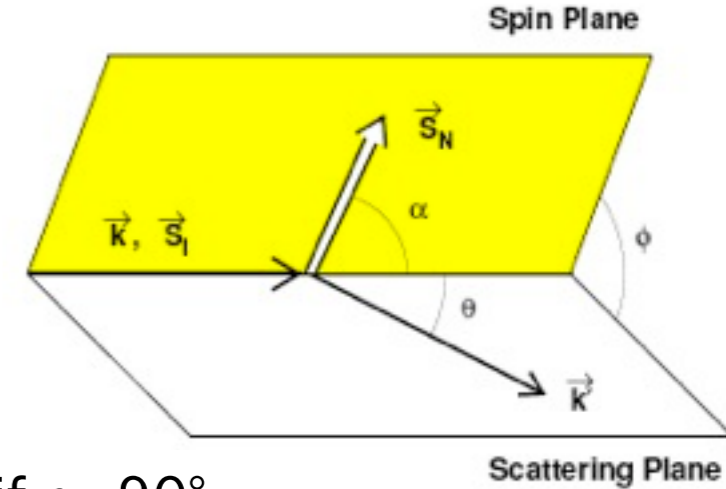
**HERMES:**

$$d_2 = 0.0148 \pm 0.0096(\text{stat}) \pm 0.0048(\text{sys})$$



# Spin structure function $g_2$

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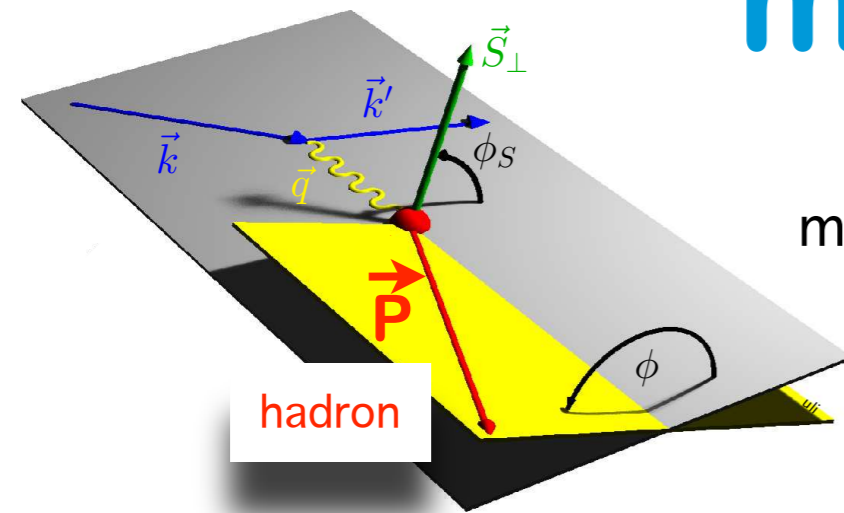
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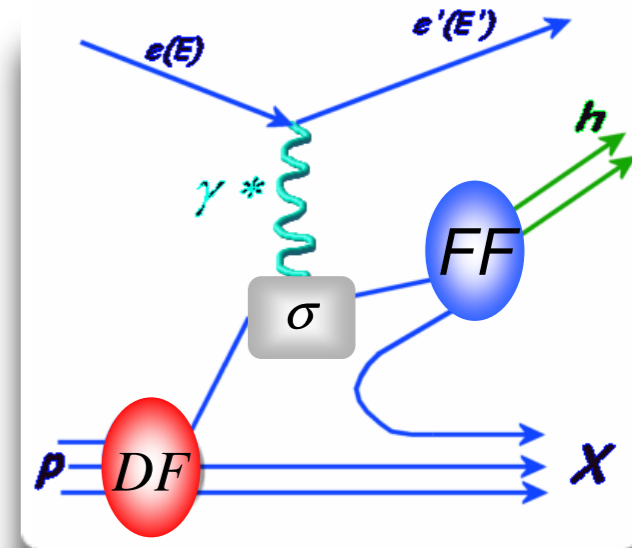
➡ Burkhardt-Cottingham sum rule:  $\int_0^1 g_2(x, Q^2) dx = 0$   $\equiv 0$  in absence of higher-twist effects

$$0.006 \pm 0.024(\text{stat}) \pm 0.017(\text{sys}) \quad [0.023 < x < 0.9 @ Q^2 = 5 \text{ GeV}^2]$$

# Semi-inclusive measurements



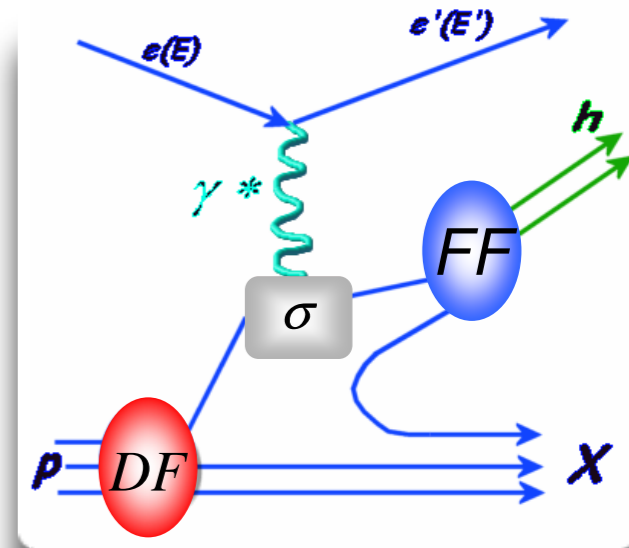
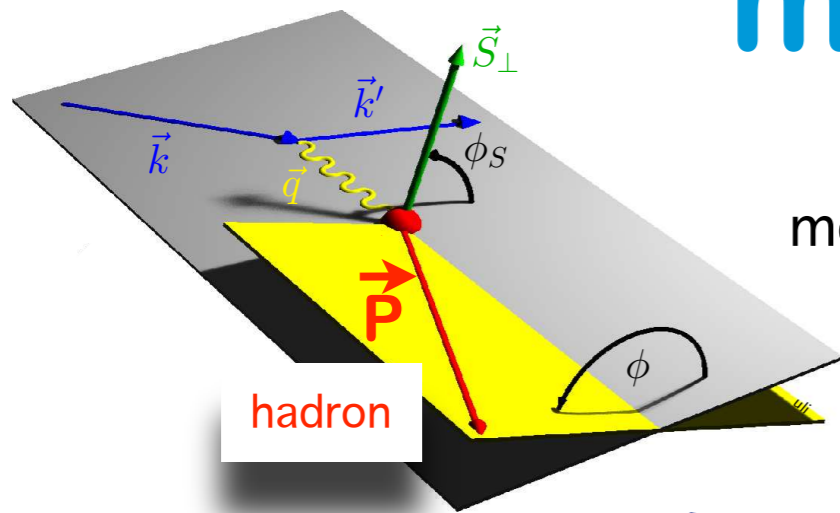
Analysis of harmonic azimuthal modulations ( $\Phi$ ,  $\Phi_S$ ) in the cross section.



$$\sigma^{ep \rightarrow ehX} = \sum_q (DF \otimes \sigma^{eq \rightarrow eq} \otimes FF)$$

# Semi-inclusive measurements

Analysis of harmonic azimuthal modulations ( $\Phi$ ,  $\Phi_S$ ) in the cross section.



$$\sigma^{ep \rightarrow ehX} = \sum_q (DF \otimes \sigma^{eq \rightarrow eq} \otimes FF)$$

## Leading-twist TMDs

(transverse-momentum dependent PDFs)

### Nucleon polarization

	U	L	T
U	$f_1$ Number Density 		$h_1^\perp$ Boer Mulders 
L		$g_1$ Helicity 	$h_{1L}^\perp$ Worm-gear 
T	$f_{1T}^\perp$ Sivers 	$g_{1T}^\perp$ Worm-gear 	$h_1$ Transversity  $h_{1T}^\perp$ Pretzelosity 

Indication to be not-zero!  
Preliminary result

Consistent with zero  
PLB 562 (2003) 182  
PRL 84 (2000) 4047

Different from zero!  
PRL 94 (2005) 012002  
PLB 693 (2010) 11

Consistent with zero  
Preliminary result

Different from zero!  
PRL 94 (2005) 012002  
PRL 103 (2009) 152002

Indication to be non-zero!  
Preliminary result



**Diagonal elements**  
'Survive' integration over transverse momentum  $k_T$ .  
"Collinear analysis"

Courtesy M. Contalbrigo (Ferrara)

# Sivers amplitudes

DF  $\otimes$  FF

$$2\langle \sin(\phi - \phi_S) \rangle_{UT} = - \frac{\sum_q e_q^2 f_{1T}^{\perp,q}(x, p_T^2) \otimes_{\mathcal{W}} D_1^q(z, K_T^2)}{\sum_q e_q^2 f_1^q(x, p_T^2) \otimes D_1^q(z, K_T^2)}$$

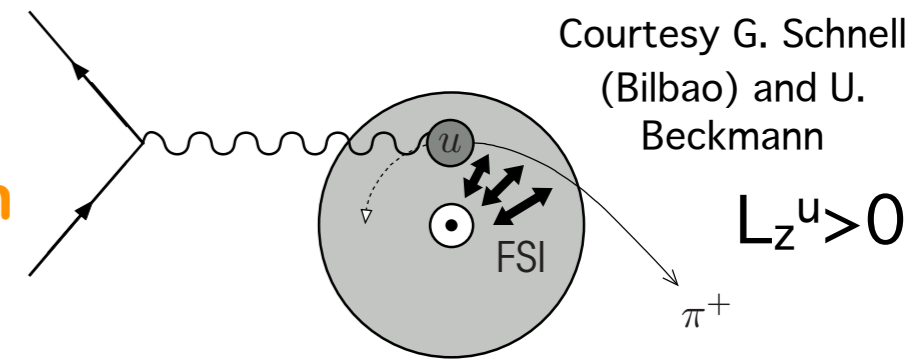
➡  $\pi^+$  dominated by u-quark scattering:

$$\simeq - f_{1T}^{\perp}(x, p_T^2) \otimes D_1^{u \rightarrow \pi^+}(z, k_T^2)$$

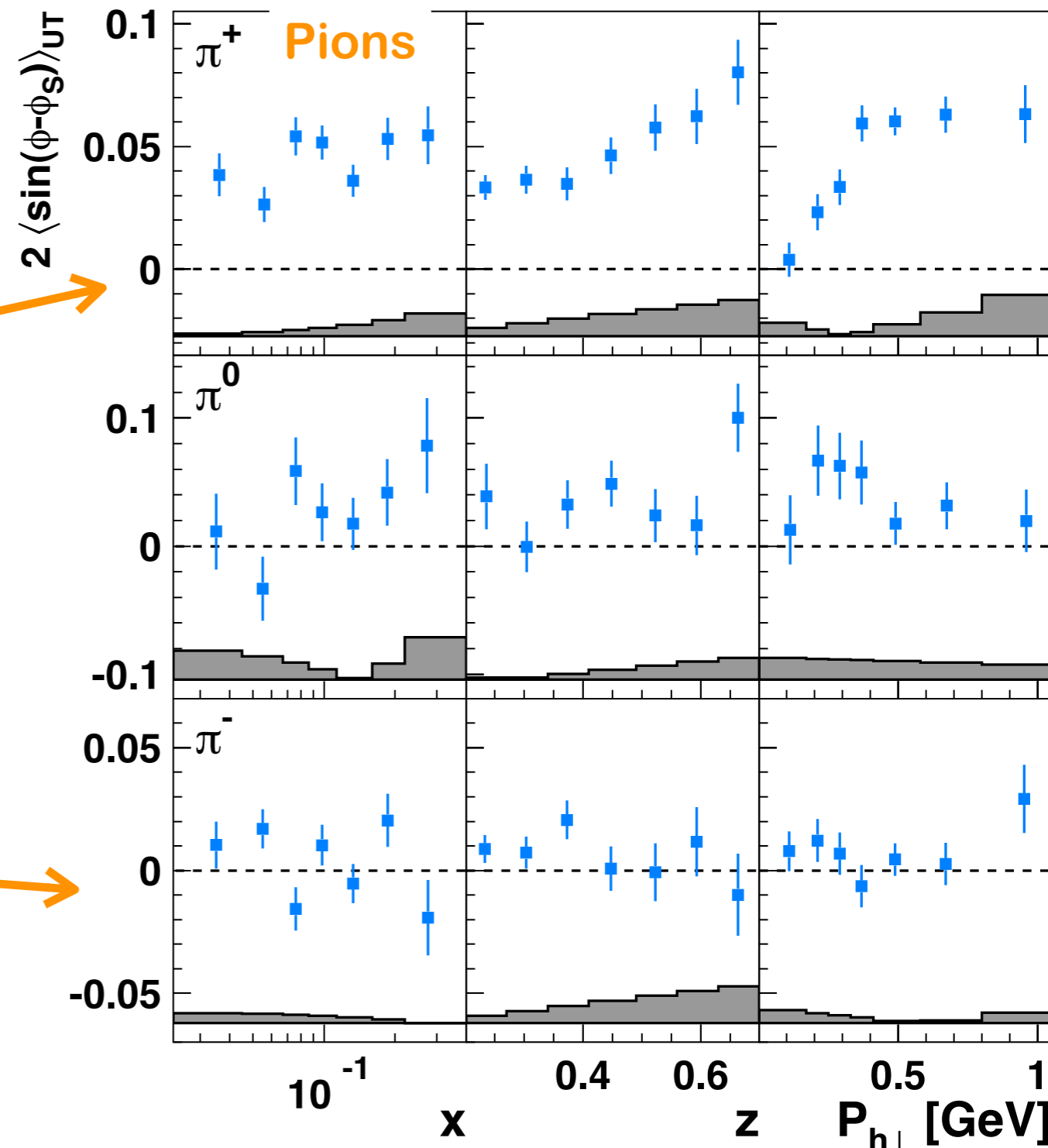
➡ u-quark Sivers function  $< 0$

➡ d-quark Sivers function  $> 0$   
(cancellation for  $\pi^-$ )

Indication of orbital motion

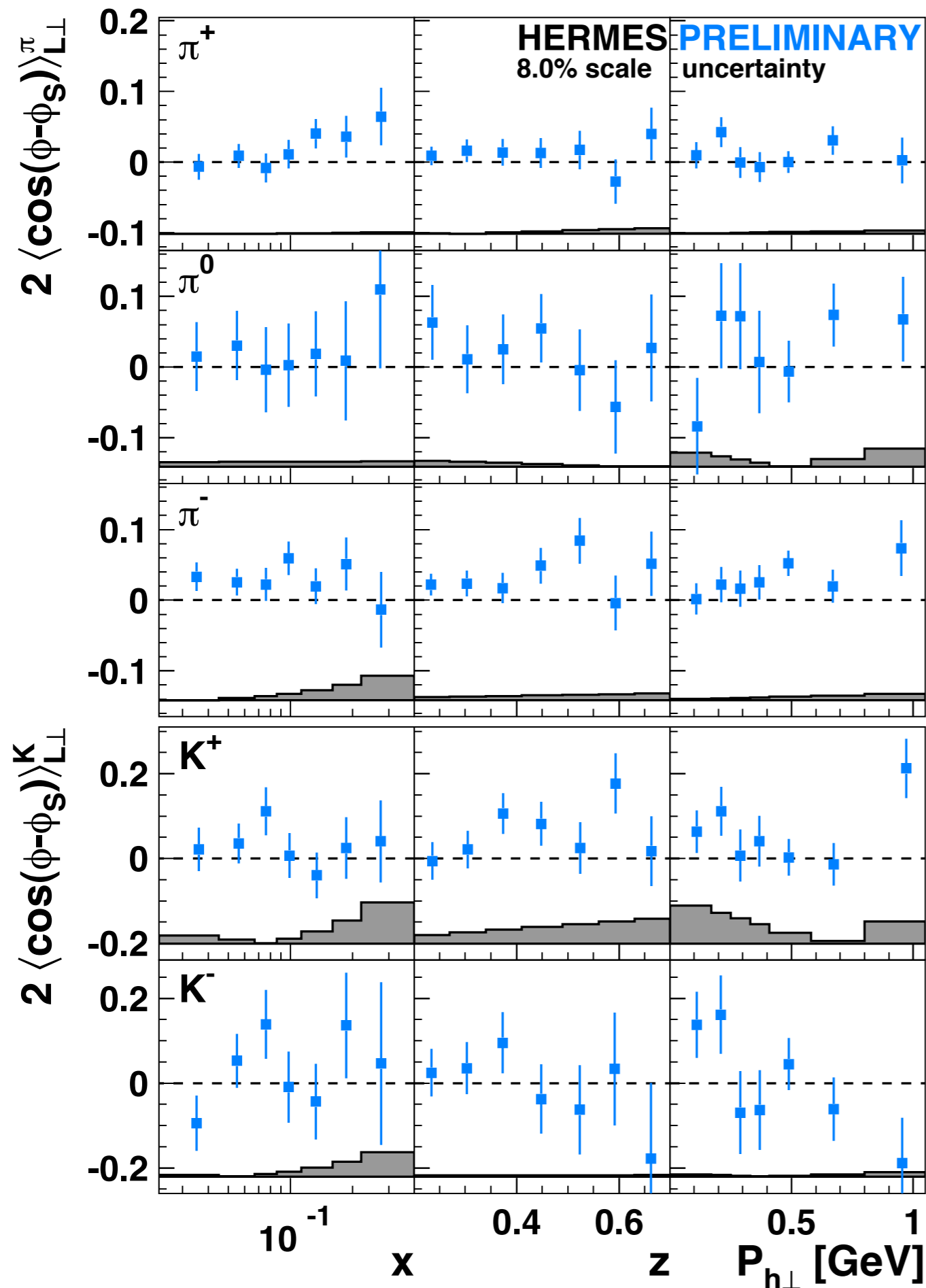


[M. Burkardt, Phys. Rev. D66 (2002) 114005]



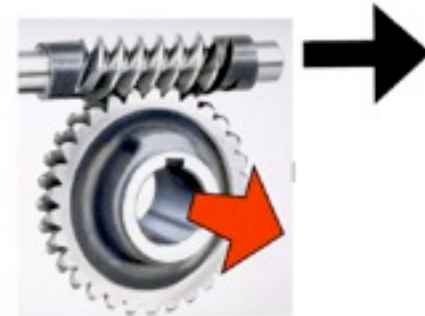
A. Airapetian et al. [HERMES], Phys. Rev. Lett. 103 (2009) 152002

# Worm-gear TMD



$$\sigma_{LT}^{\cos(\phi - \phi_s)} \propto g_{1T}^{\perp} \otimes D_1$$

DF  $\otimes$  FF

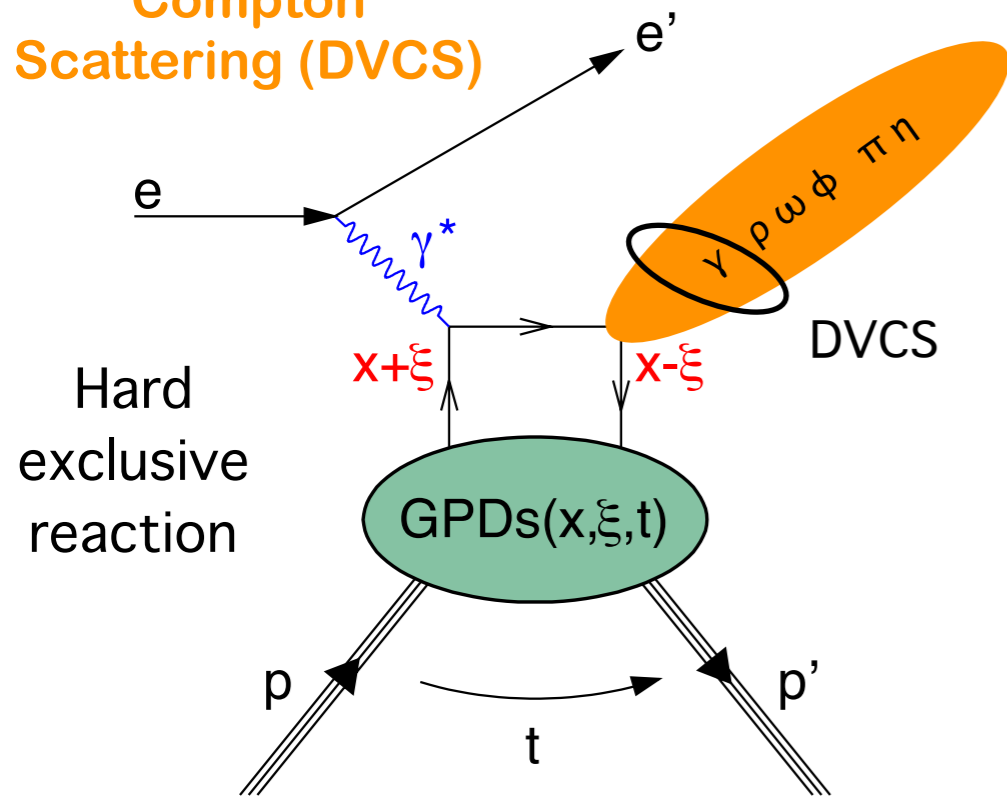


- Longitudinally polarized quarks in transversely polarized nucleon
- Related to parton orbital motion – requires interference between wave functions with OAM difference by 1 unit
- Wandzura-Wilczek type approximation:

$$g_{1T}^{\perp}(x) \approx x \int_0^1 \frac{dy}{y} g_1(y)$$

# Exclusive measurements

Deeply Virtual  
Compton  
Scattering (DVCS)



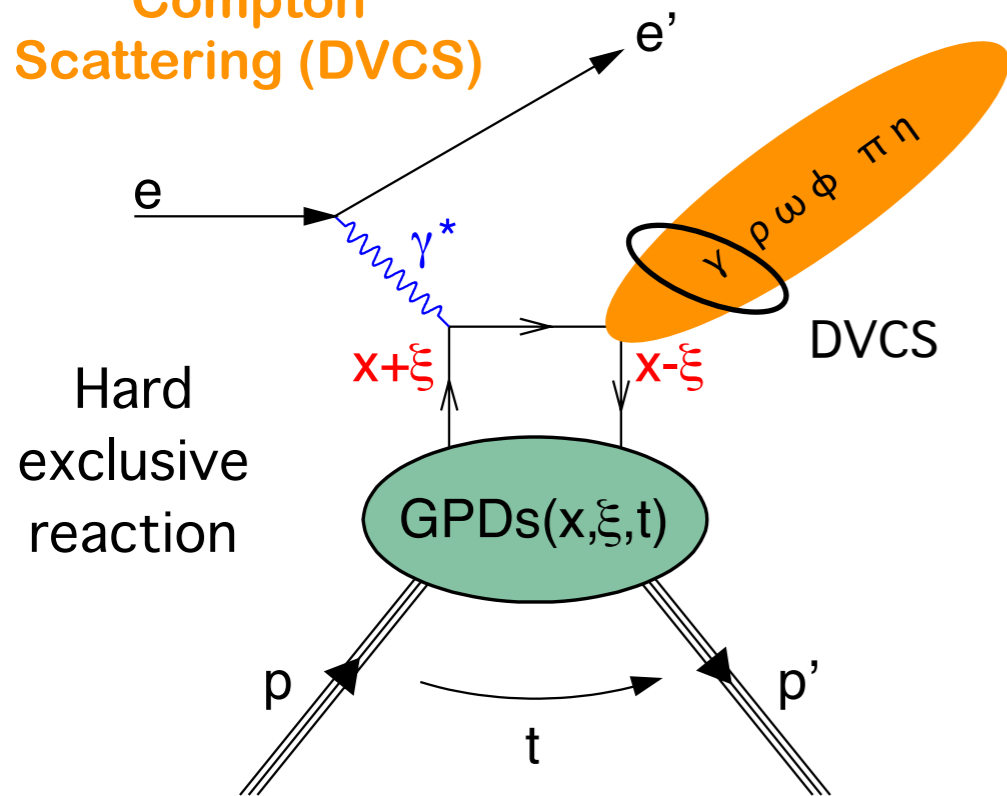
Cross section of  $ep \rightarrow ep\gamma$  :

$$\sigma_{\gamma^* \gamma N} \sim \left| \begin{array}{c} \text{DVCS} \\ \text{Bethe-Heitler (BH)} \end{array} \right|^2 + (\tau_{\text{DVCS}} \tau_{\text{BH}}^* + \tau_{\text{DVCS}}^* \tau_{\text{BH}})$$

Small at HERMES
Exactly calculable in QED
**DVCS-BH interference term**

# Exclusive measurements

## Deeply Virtual Compton Scattering (DVCS)



## Cross section of $ep \rightarrow ep\gamma$ :

$$\sigma_{\gamma^* \gamma N} \sim \left| \text{DVCS} + \text{Bethe-Heitler (BH)} \right|^2$$

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**DVCS-BH interference term**

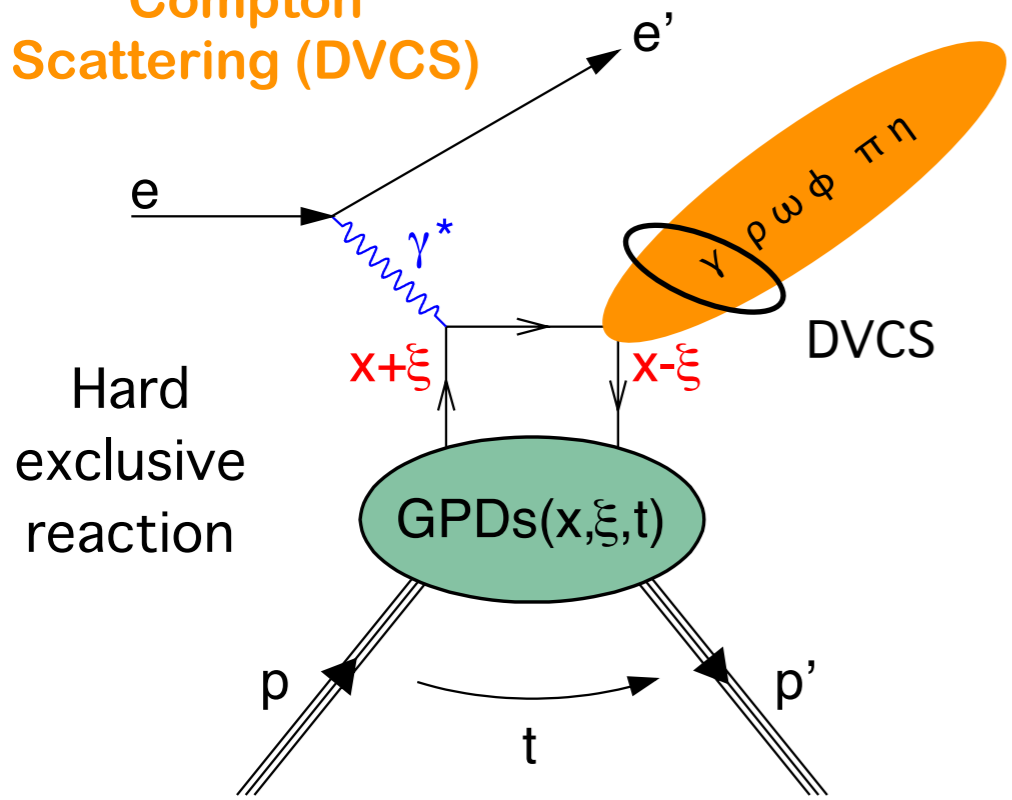
4 chiral-even quark GPDs at leading twist

Spin-1/2	flips nucleon helicity	conserves nucleon helicity
does not depend on quark helicity	$E$	$H \rightarrow q(x)$
depends on quark helicity	$\tilde{E}$	$\tilde{H} \rightarrow \Delta q(x)$

forward limit  $\xi \rightarrow 0, t \rightarrow 0$

# Exclusive measurements

## Deeply Virtual Compton Scattering (DVCS)



## Cross section of $ep \rightarrow ep\gamma$ :

$$\sigma_{\gamma^* \gamma N} \sim \left| \text{DVCS} + \text{Bethe-Heitler (BH)} \right|^2$$

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**DVCS-BH interference term**

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depends on quark helicity	$\tilde{E}$	$\tilde{H}$	$\rightarrow \Delta q(x)$

forward limit  $\xi \rightarrow 0, t \rightarrow 0$

## Ji sum rule for the nucleon

-Ji, PRL 78 (1997) 610-

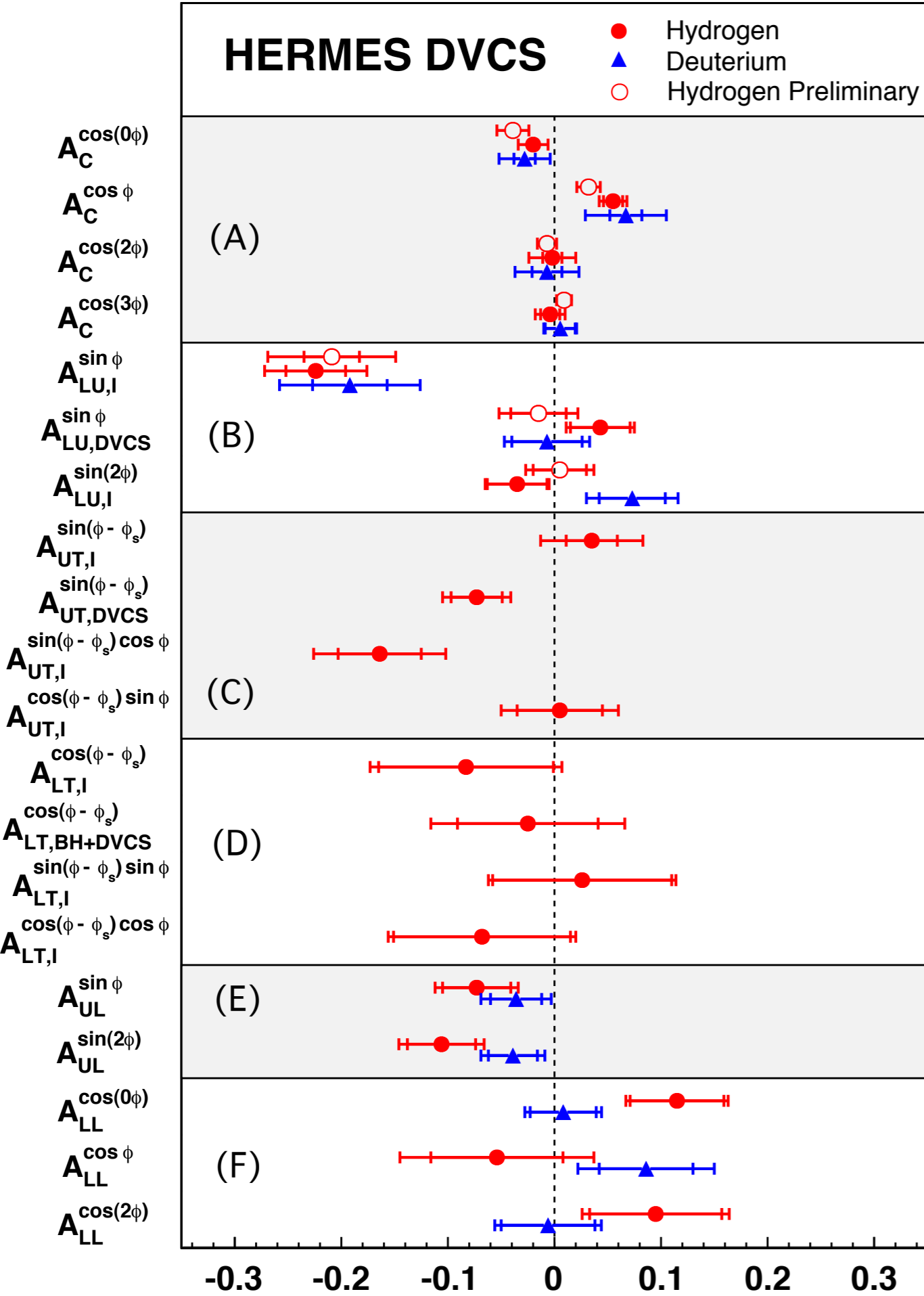
$$J_q = \frac{1}{2} \lim_{t \rightarrow 0} \int_{-1}^1 dx x [H^q(x, \xi, t) + E^q(x, \xi, t)]$$

$$\frac{1}{2} = \frac{1}{2} \Delta \Sigma + L_q + J_g$$

**Orbital angular momentum**



# DVCS Amplitudes



(A) Beam-charge asymmetry: **Unique & complete set**  
GPD H

[JHEP 11 (2009) 083 – Nucl. Phys. B 829 (2010) 1–27]

(B) Beam-helicity asymmetry: GPD H

[JHEP 11 (2009) 083 – Nucl. Phys. B 829 (2010) 1–27]

(C) Transverse target-spin asymmetry: GPD E

[JHEP 06 (2008) 066]

**Variety highly welcome by global fitters**

(D) Double-Spin (LT) asymmetry: GPD E

[Phys. Lett. B 704 (2011) 15–23]

(E) Longitudinal target-spin asymmetry: GPD  $H_{\sim}$

[JHEP 06 (2010) 019 – Nucl. Phys. B 842 (2011) 265–298]

(F) Double-spin (LL) asymmetry: GPD  $H_{\sim}$

[JHEP 06 (2010) 019 – Nucl. Phys. B 842 (2011) 265–298]

# Beam-charge asymmetry amplitudes in DVCS

☆ All 1996–2007 HERMES proton data

☆ Detection of e and  $\gamma$

arXiv:1103.xxxx

to be submitted to JHEP

☆ KM10

## Global fit

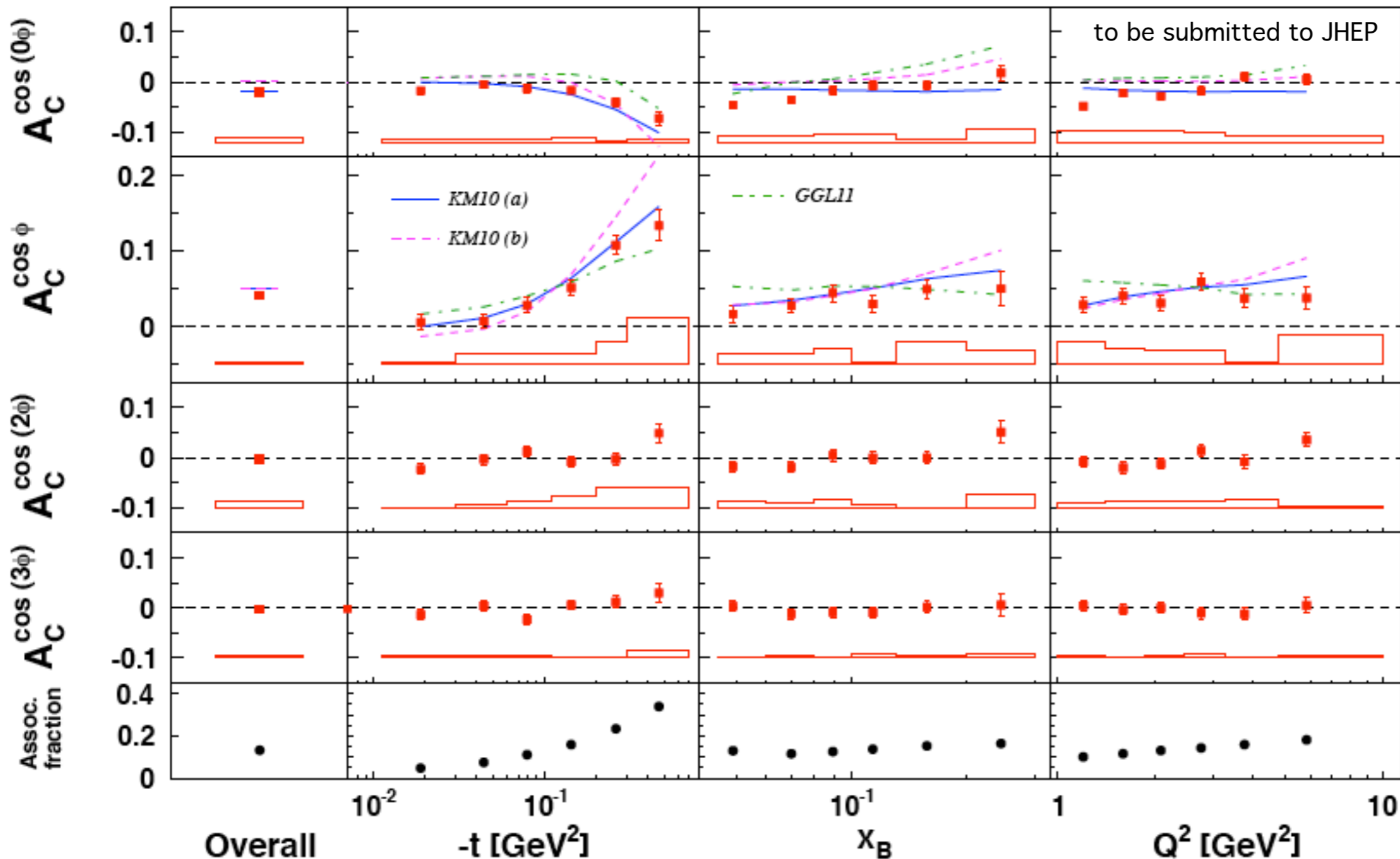
including data from JLab, HERMES and HERA colliders

(dashed excludes JLab Hall A cross section)  
K. Kumericki and D. Müller, Nucl. Phys. B 841 (2010) 1  
[arXiv:0904.0458]

☆ GGL11

## Model calculation

G. Goldstein, J. Hernandez and S. Liuti, Phys. Rev. D 84 034007 (2011)  
[arxiv:1012.3776]



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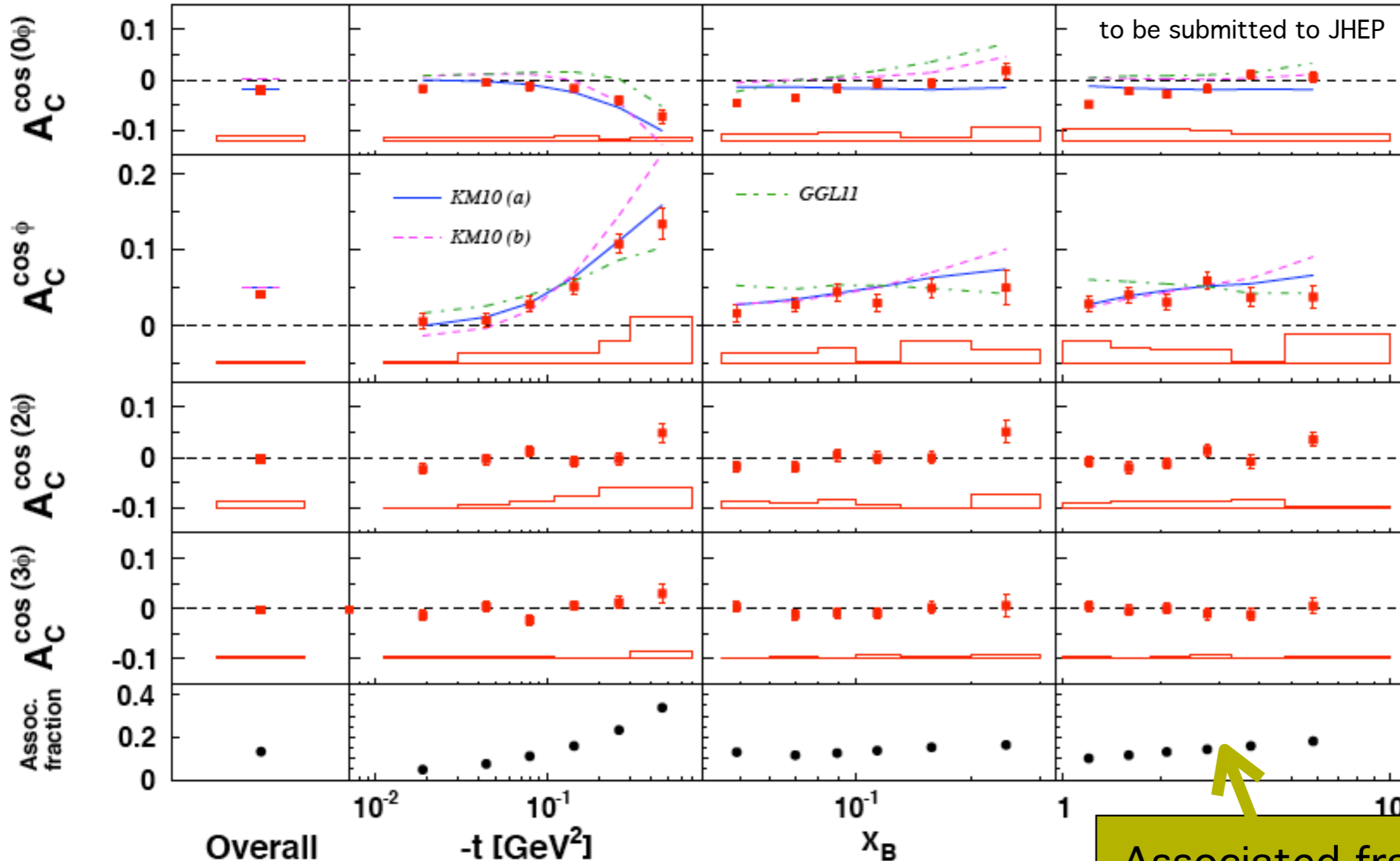
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☆ GGL11

## Model calculation

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[arxiv:1012.3776]



Associated fraction  $ep \rightarrow e\Delta^+\gamma$   
(from MC simulation)

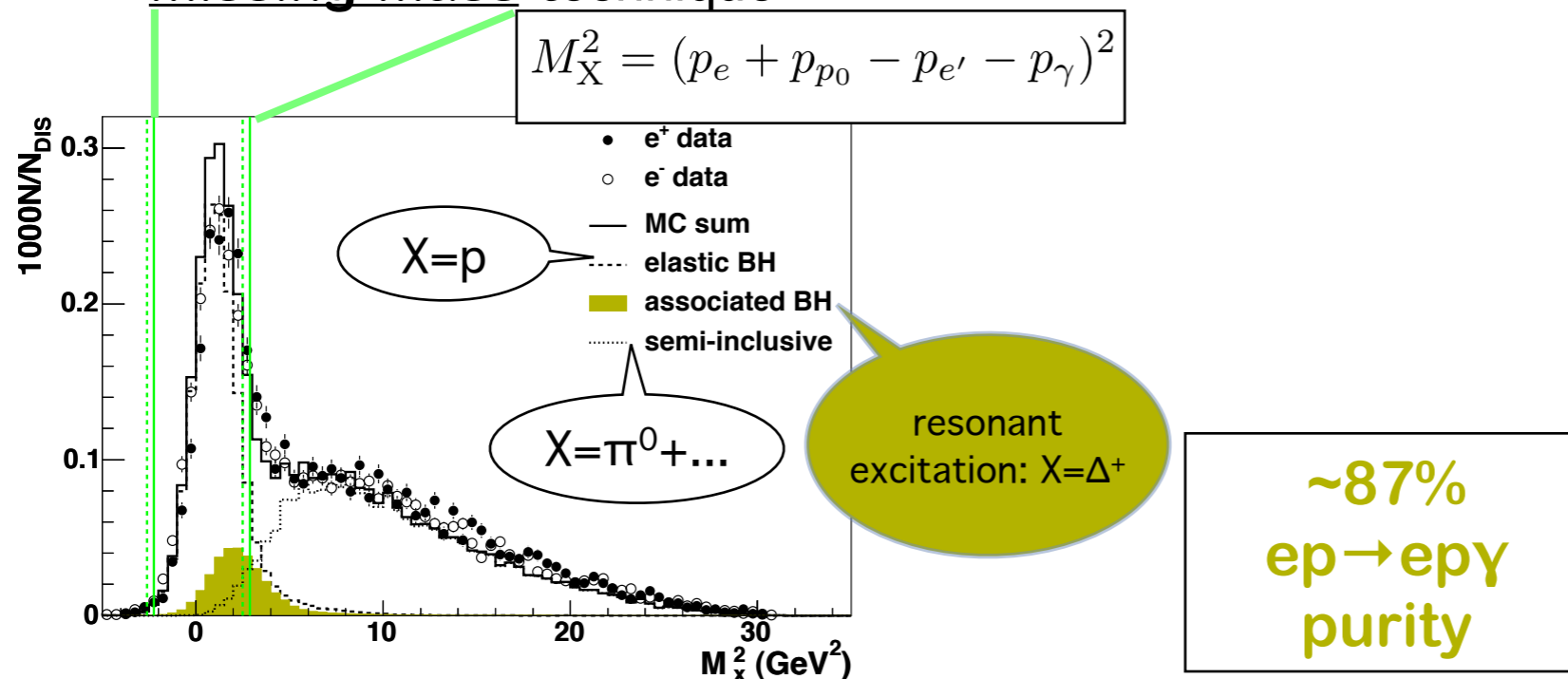
# DVCS event samples

## Only $e\gamma$ detection

“Unresolved” for associated production.

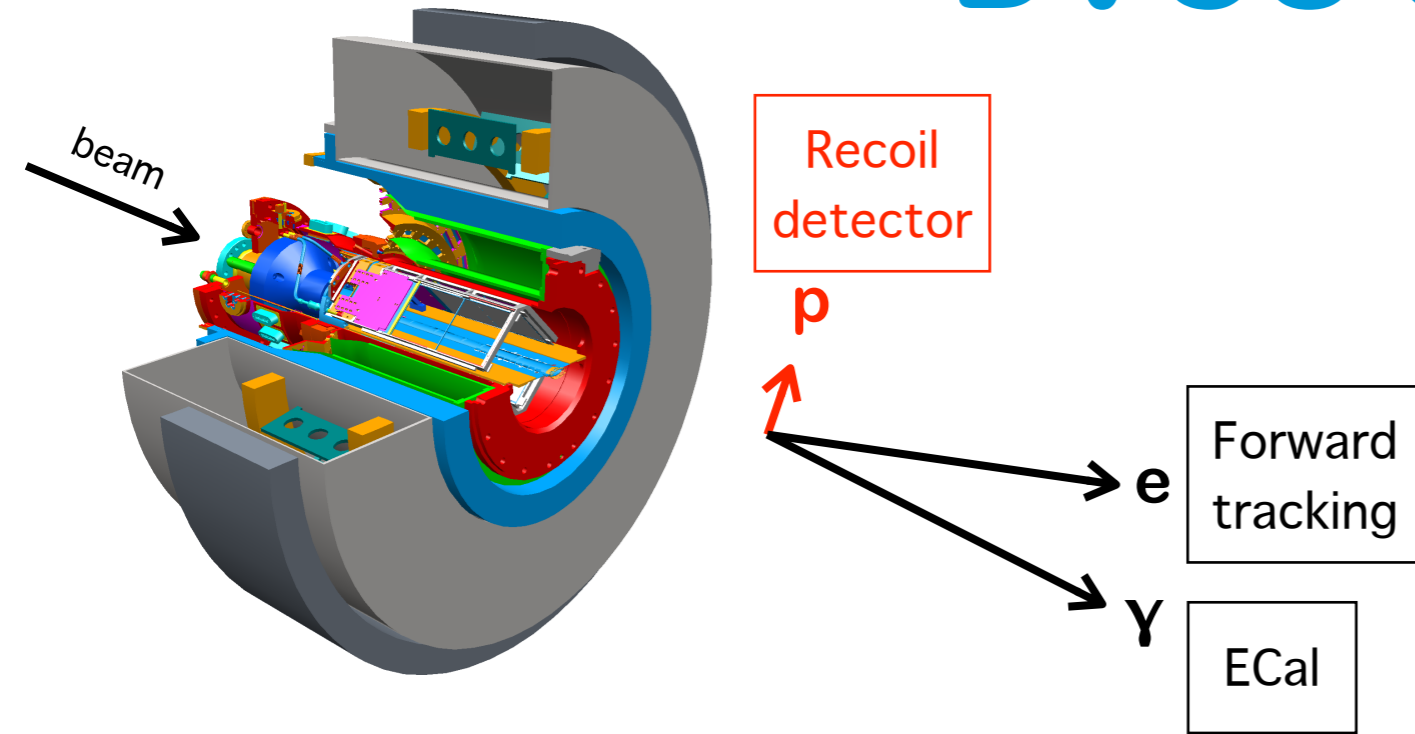
Exclusive sample selected by

**missing-mass** technique



# Improvement by Recoil detector

# DVCS event samples

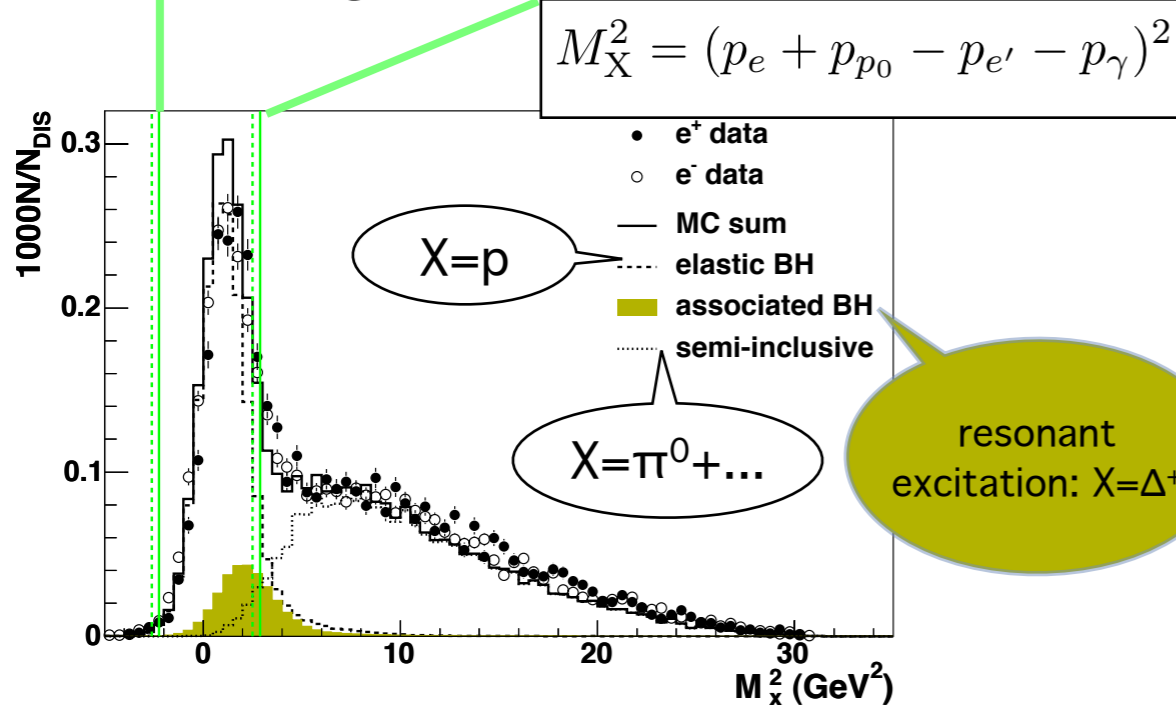


## Only eγ detection

“Unresolved” for associated production.

Exclusive sample selected by

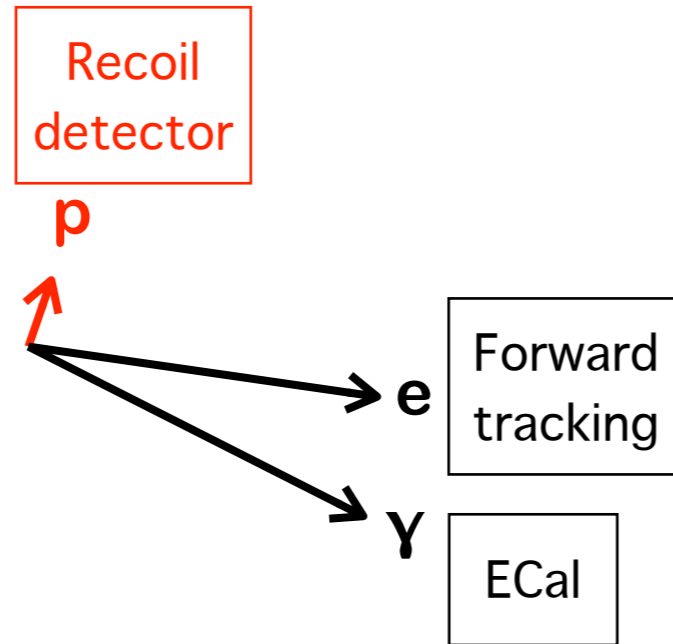
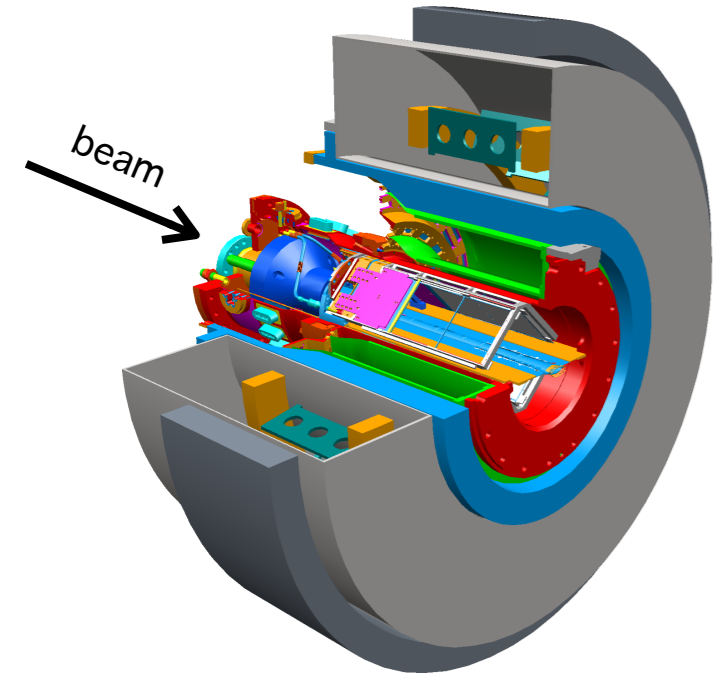
**missing-mass** technique



~87%  
ep → eγ  
purity

Improvement by  
Recoil detector

# DVCS event samples

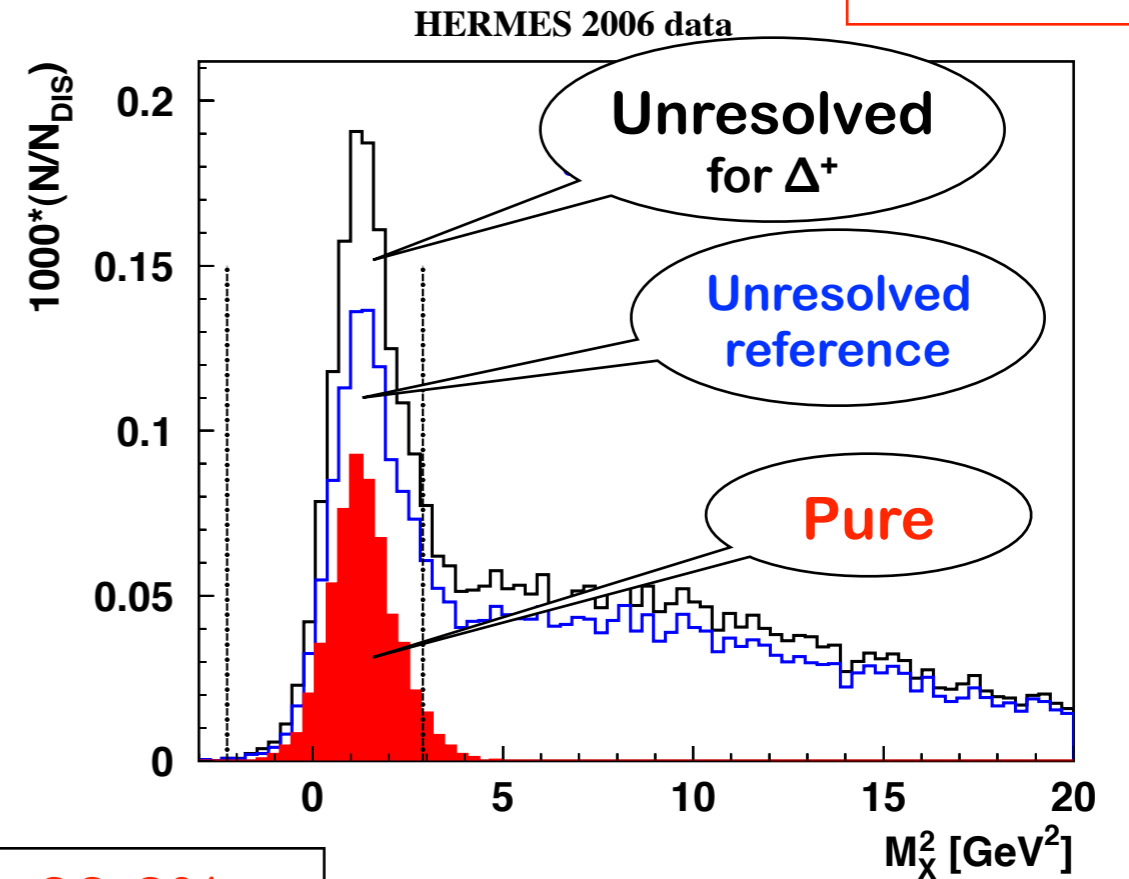
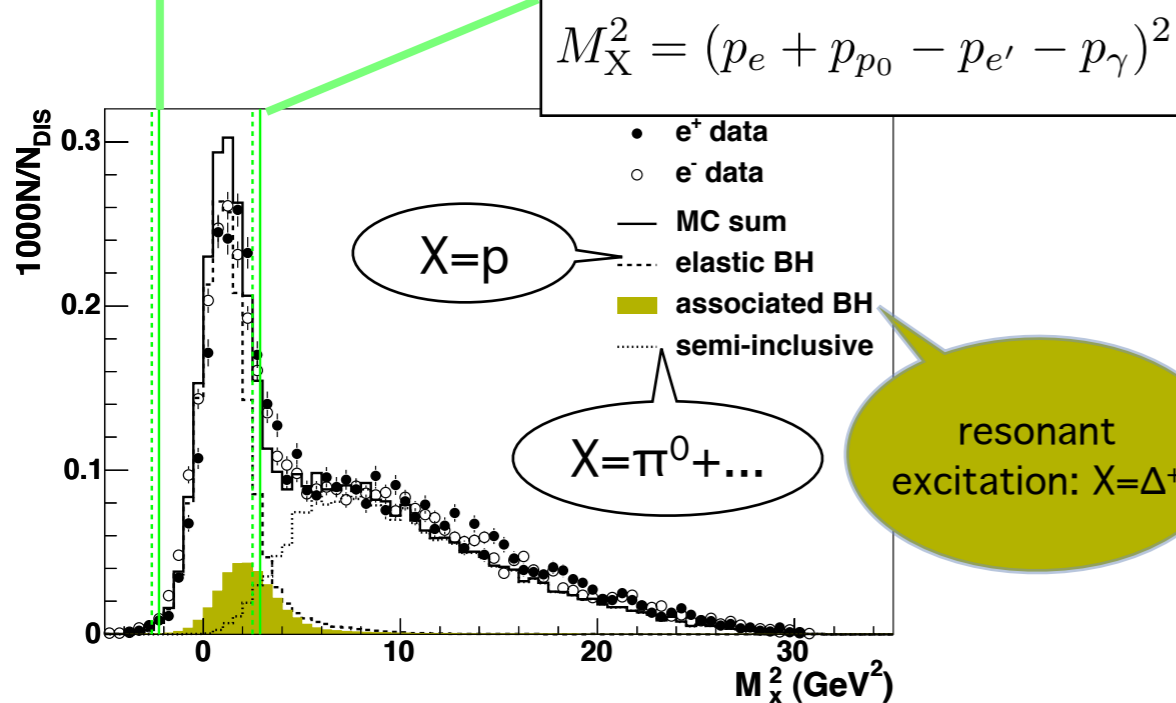


ep $\gamma$  detection

Kinematic event fit

Only ey detection

“Unresolved” for associated production.  
Exclusive sample selected by  
missing-mass technique



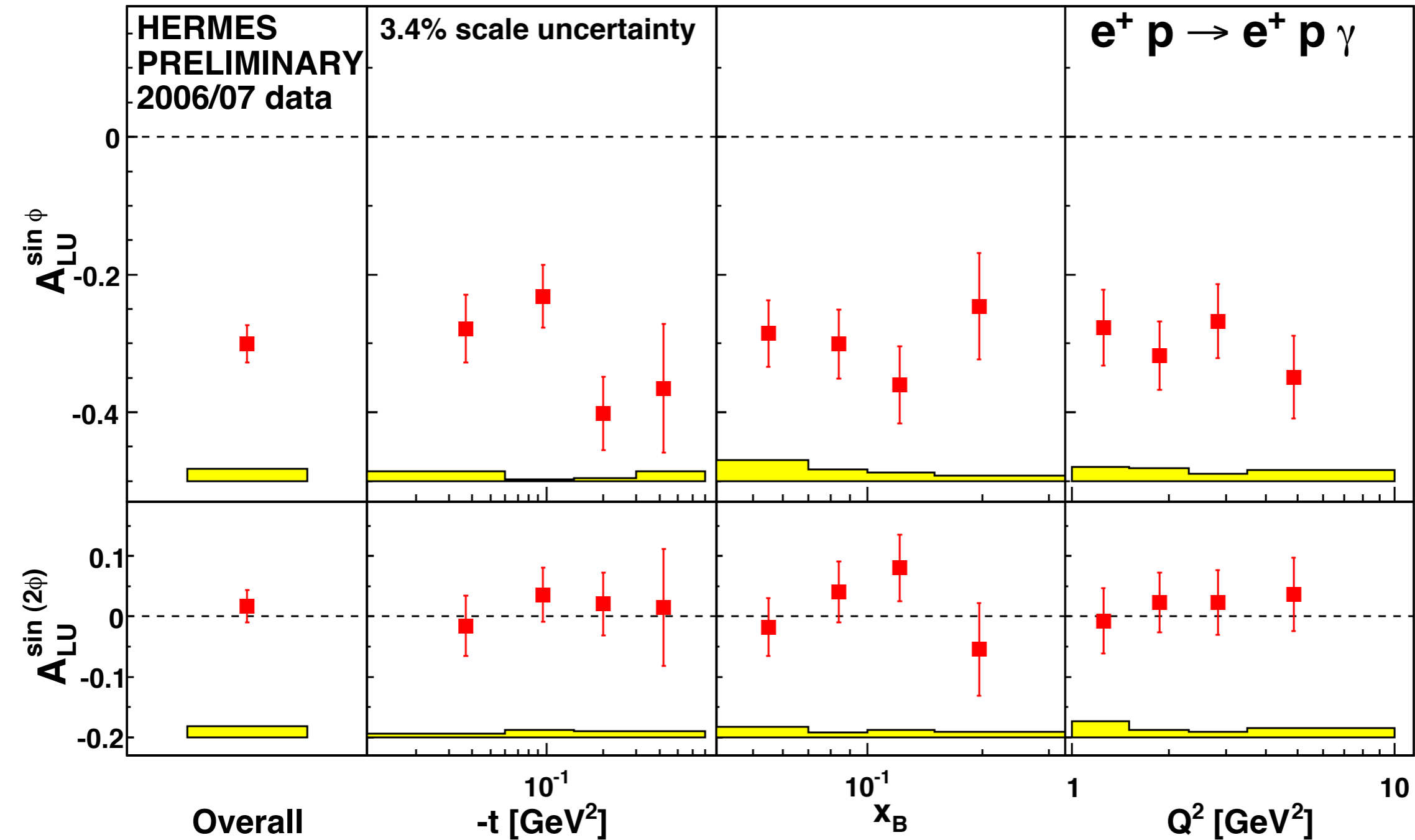
>99.9%  
ep → ep $\gamma$   
purity

~87%  
ep → ep $\gamma$   
purity

“Hypothetical” proton  
required in recoil-detector  
acceptance

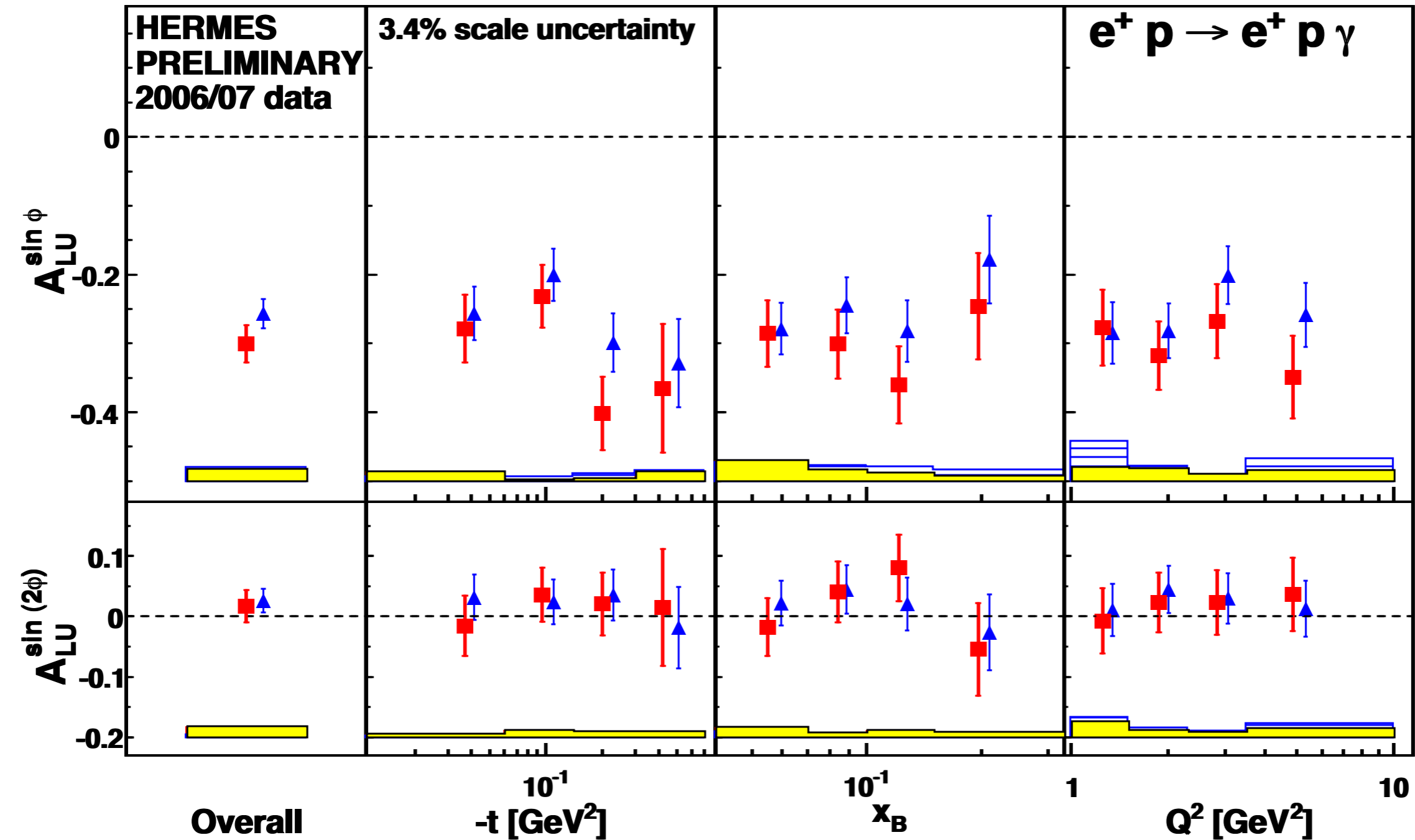
# Beam-helicity asymmetry amplitudes in DVCS

■ Pure (with recoil proton detection)



# Beam-helicity asymmetry amplitudes in DVCS

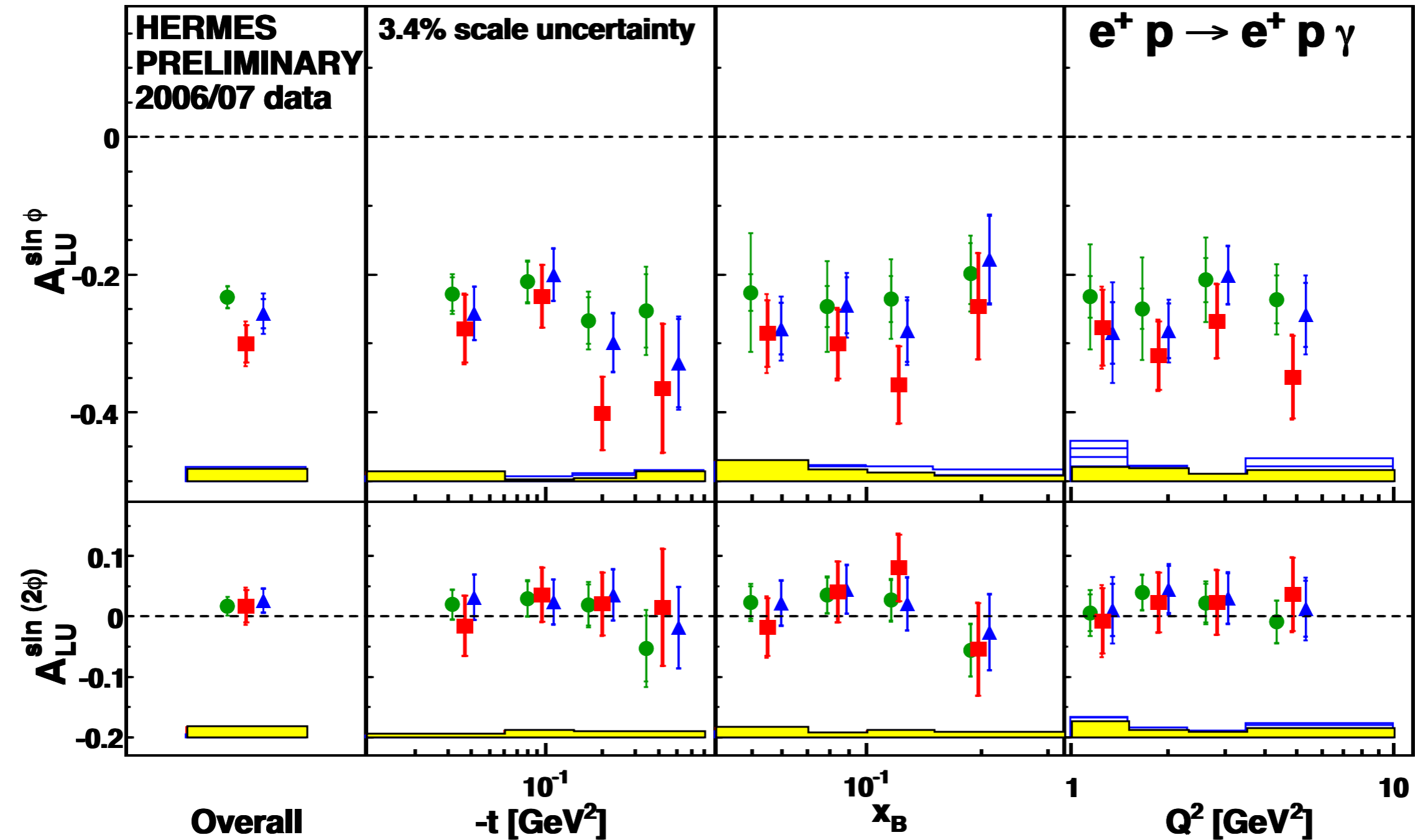
- Pure (with recoil proton detection)
- ▲ Unresolved reference (in recoil acceptance)



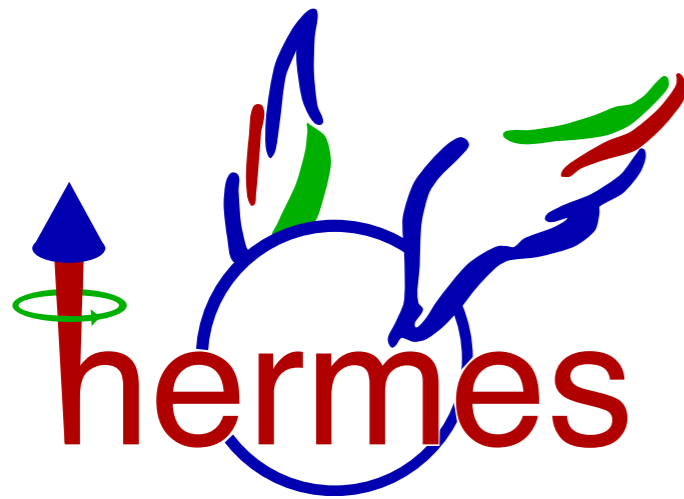


# Beam-helicity asymmetry amplitudes in DVCS

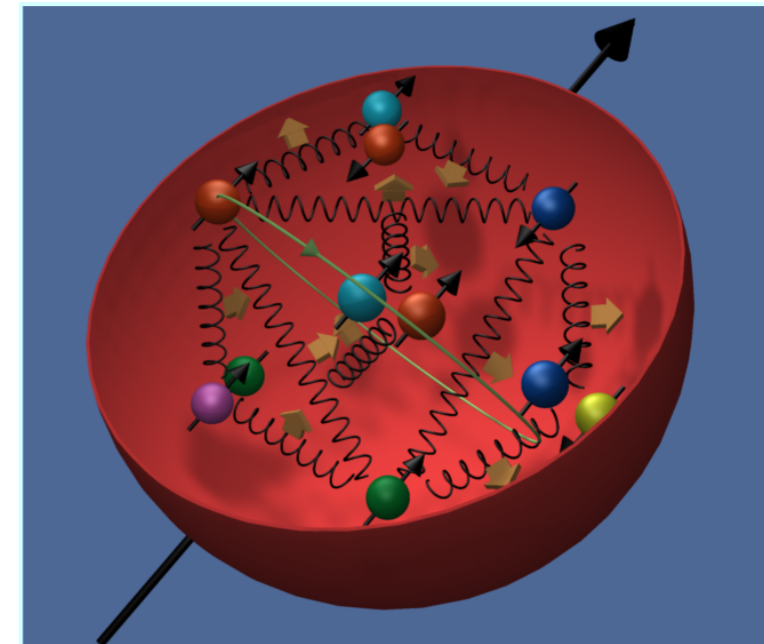
- Pure (with recoil proton detection)
- ▲ Unresolved reference (in recoil acceptance)
- Unresolved



# Summary



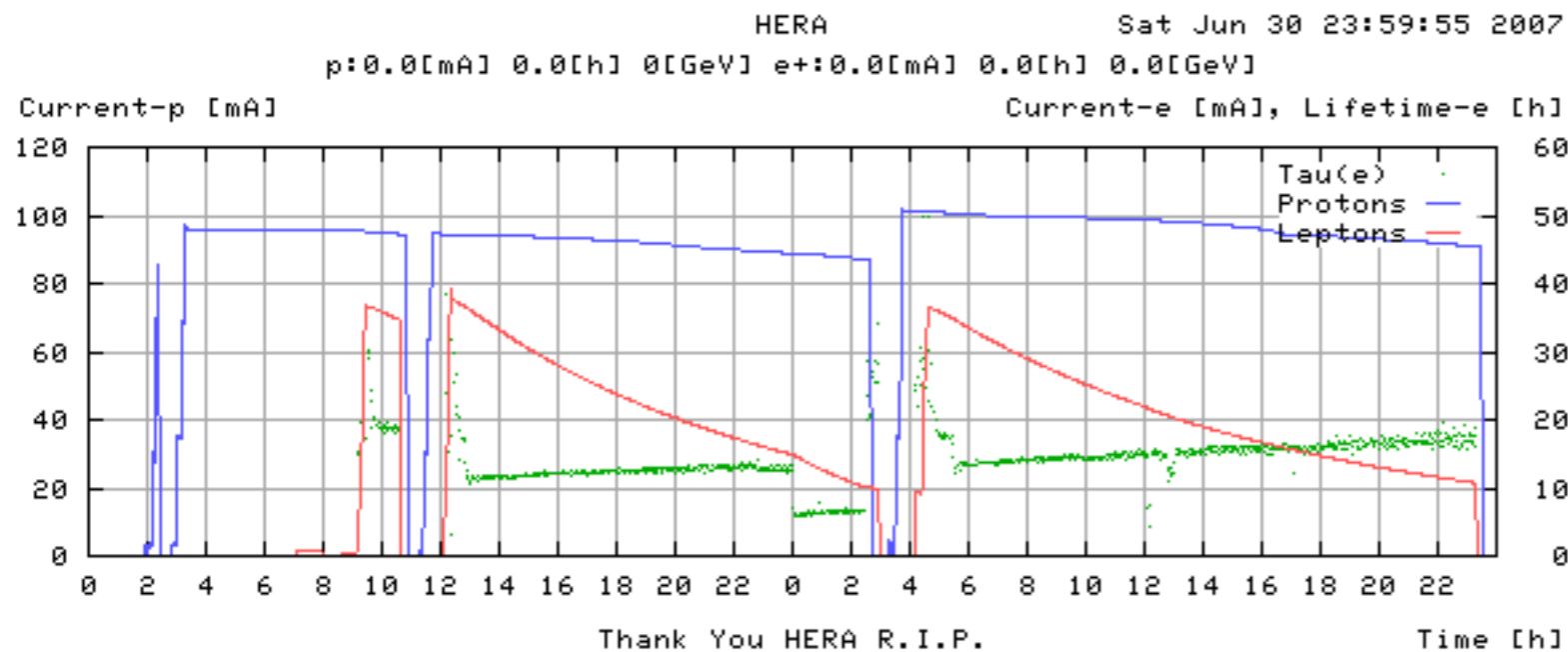
Quark Spin  
Generalized Parton Distributions



Orbital angular momentum  
Transverse-momentum dependent PDFs

Almost 5 years after the dump of the last HERA beams... (June 30, 2007)

“Dynamic nucleon hologram”



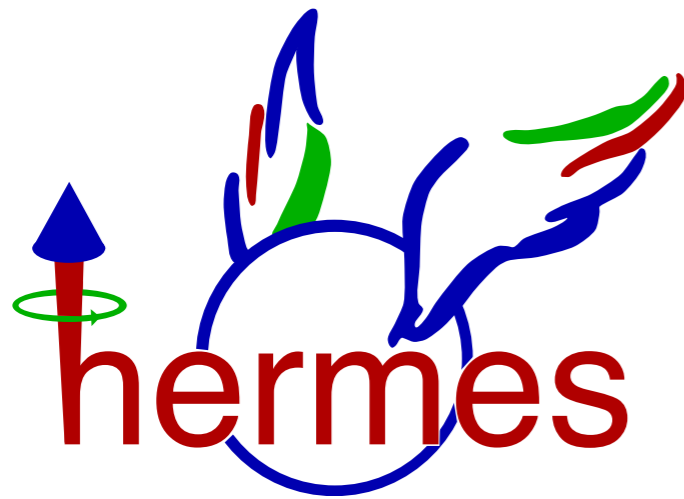
Many pioneering measurements

A lot of exciting topics could not be addressed in this talk!

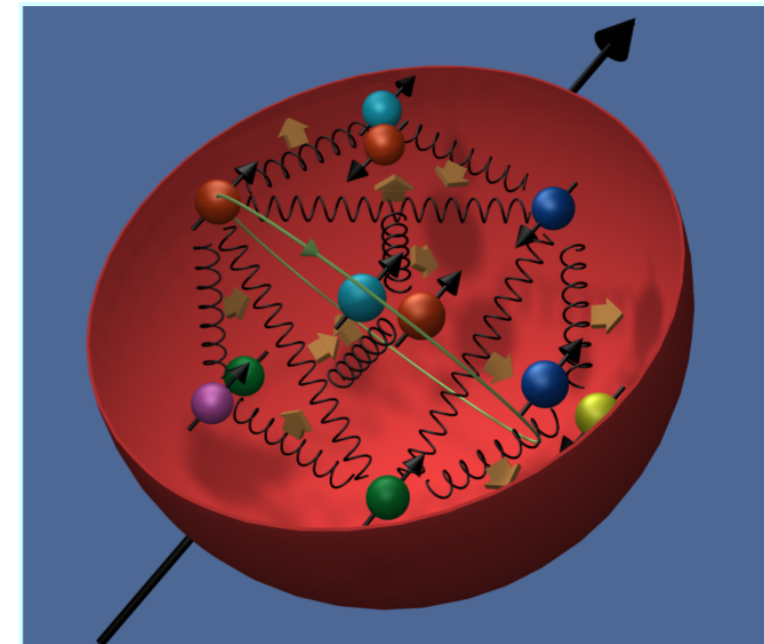
Click here for more:

<http://www-hermes.desy.de/notes/pub/publications.html>

# Summary



Quark Spin  
Generalized  
Parton  
Distributions

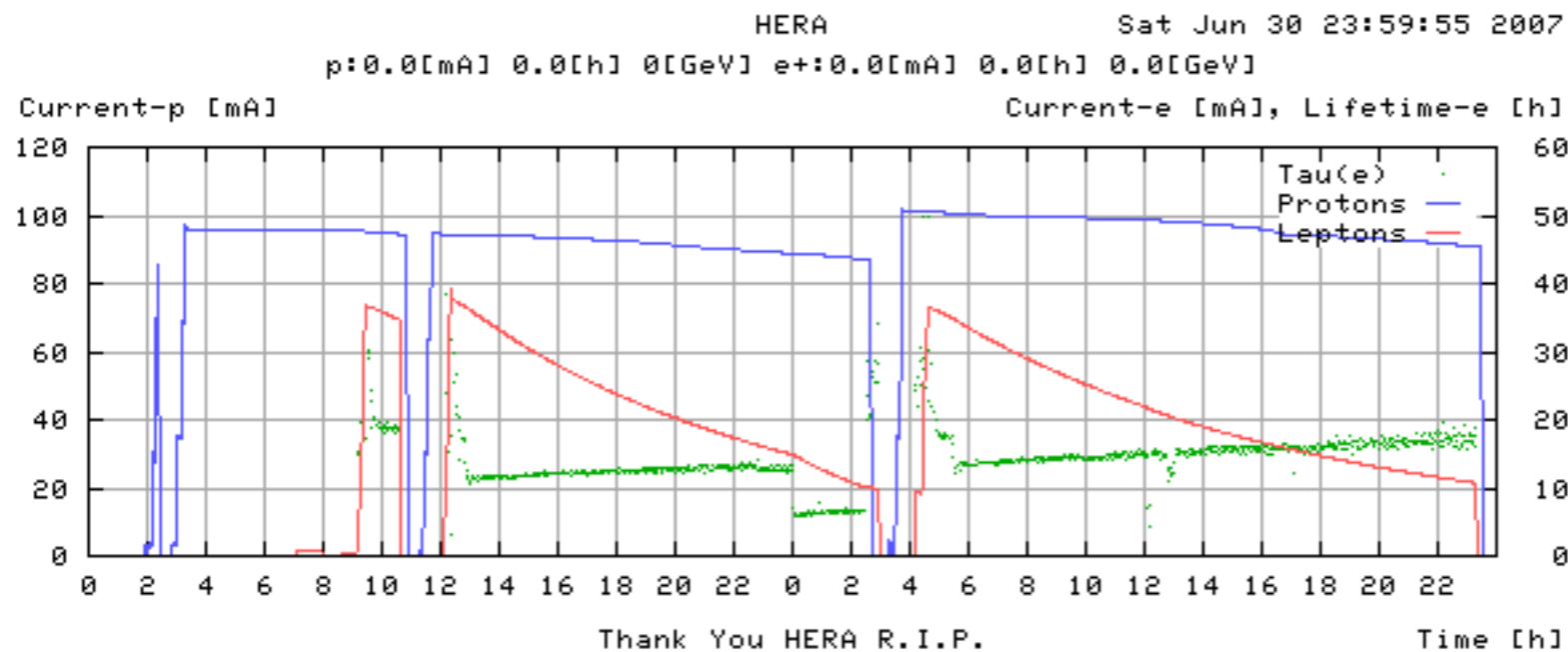


Orbital  
angular  
momentum

Transverse-  
momentum  
dependent  
PDFs

Almost 5 years after the dump of the  
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“Dynamic nucleon hologram”



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pioneering  
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