

# Determination of the Structure Function $F_2$ at



Dominik D. Gabbert  
DESY-Zeuthen / Universität Hamburg

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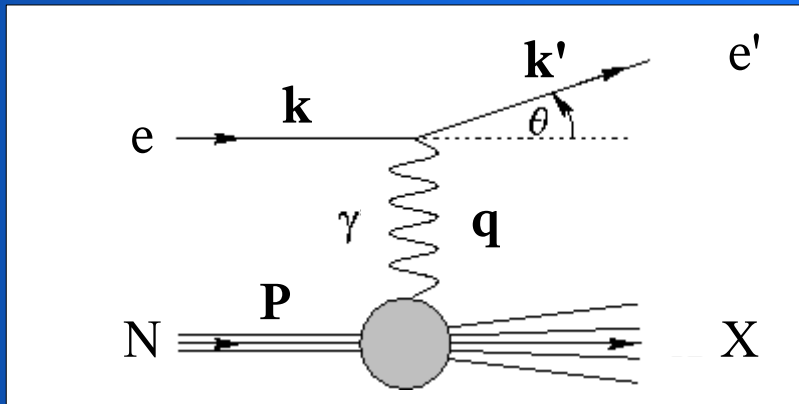


Universität Hamburg



# Probing the Structure of Nucleons

- **Deep-inelastic scattering** (DIS) plays major role in understanding of nucleon structure
- Lepton-nucleon scattering **cleanest way** to probe substructure of nucleon
- Exchange of virtual boson, **breakup** and hadronization in DIS regime



center-of-mass energy (e N)

$$s = (P + k)^2 = M^2 + 2ME$$

For given  $s$ , two kinematic variables completely describe the scattering process in the inclusive analysis, e.g.:

$$Q^2 = -q^2 = (k - k')^2 = 4EE' \sin^2 \frac{\theta}{2} \quad \text{photon virtuality}$$

$$\nu = \frac{P \cdot q}{M} = E - E' \quad \text{photon energy (lab)}$$

or

$$x = \frac{Q^2}{2 P \cdot q} = \frac{Q^2}{2 M \nu} \quad \text{Bjorken scaling variable}$$

$$y = \frac{P \cdot q}{P \cdot k} = \frac{\nu}{E} \quad \text{inelasticity}$$

Invariant mass of hadronic final state:

$$W^2 = (P + q)^2 = M^2 + 2M\nu - Q^2$$

Resolution of deep-inelastic scattering:

$$\lambda = \frac{1}{|\mathbf{q}|} = \frac{1}{\sqrt{\nu^2 + Q^2}} \approx \frac{2Mx}{Q^2}$$

# Structure Functions of the Nucleon

Deep-inelastic scattering in the *one-photon* exchange approximation can be written as:

$$\frac{d^2\sigma}{d\Omega dE'} = \frac{\alpha_{em}^2}{2MQ^2} \frac{E'}{E} L_{\mu\nu} W^{\mu\nu}$$

Leptonic and hadronic tensors have symmetric (S) and anti-symmetric (A) contributions:

$$\frac{d^2\sigma}{d\Omega dE'} = \frac{\alpha_{em}^2}{2MQ^2} \frac{E'}{E} [L_{\mu\nu}^{(S)} W^{\mu\nu(S)} + L_{\mu\nu}'^{(S)} W^{\mu\nu(S)} + L_{\mu\nu}^{(A)} W^{\mu\nu(A)} + L_{\mu\nu}'^{(A)} W^{\mu\nu(A)}]$$

Leptonic tensor known from QED.

Hadronic tensor describes a-priori unknown hadronic structure, parameterized by:

$W_{\mu\nu}^{(A)}$	Observable in polarized scattering	$G_1, G_2$ (or $g_1, g_2$ )
$W_{\mu\nu}^{(S)}$	Observable in unpolarized scattering	$W_1, W_2$ (or $F_1, F_2$ )

# Structure Functions of the Nucleon

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Consider unpolarized scattering in the following.

Parameterize hadronic structure using  $F_1$  and  $F_2$  for which Björken predicted scaling:

$$F_1(x, Q^2) = MW_1(\nu, Q^2) \rightarrow F_1(x) \quad F_2(x, Q^2) = \nu W_2(\nu, Q^2) \rightarrow F_2(x)$$

$$\frac{d^2 \sigma}{dx dQ^2} = \frac{4\pi\alpha_{em}^2}{Q^4} [y^2 F_1(x, Q^2) + (1-y - \frac{My}{2E}) \cdot F_2(x, Q^2)]$$

# Structure Functions $F_1, F_2$

In naïve Quark-Parton-Model:

$$F_1 = \frac{1}{2} \sum_f e_f^2 [q(x) + \bar{q}(x)] \quad \text{Callan-Gross relation}$$

$$F_2 = x \sum_f e_f^2 [q(x) + \bar{q}(x)] \quad F_2 = 2x F_1$$

Longitudinal ( $\sigma_L$ ) and transverse ( $\sigma_T$ ) virtual-photon contributions:

$$F_1 = \frac{MK}{4\pi\alpha_{em}} \sigma_T \quad F_2 = \frac{\nu K(\sigma_L + \sigma_T)}{4\pi\alpha_{em}(1 + Q^2/4M^2 x^2)}$$

Virtual-photon flux

$$\Gamma = \frac{\alpha_{em} K}{2\pi^2 Q^2} \frac{E'}{E} \frac{1}{1-\epsilon}$$

Hand convention:

$$K = \nu - \frac{Q^2}{2M}$$

$$\frac{d^2\sigma}{d\Omega dE'} = \Gamma [\sigma_T(x, Q^2) + \epsilon \sigma_L(x, Q^2)]$$

Virtual-photon polarization parameter

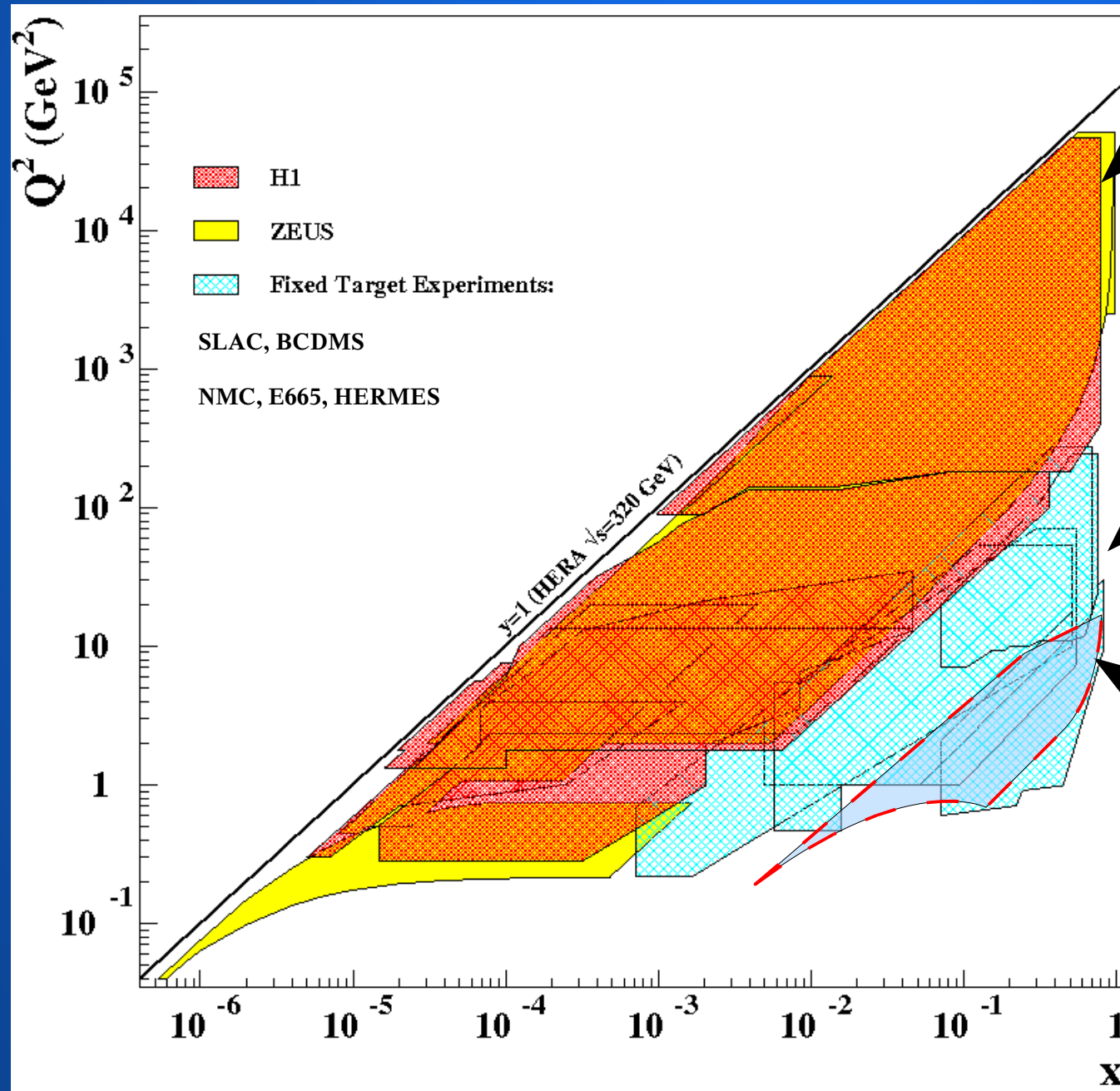
$$\epsilon = \frac{4(1-y) - Q^2/E^2}{4(1-y) + 2y^2 + Q^2/E^2}$$

Define ratio  $R$  and re-parameterize cross section

$$R = \frac{\sigma_L}{\sigma_T}$$

$$\frac{d^2\sigma}{dx dQ^2} = \frac{4\pi\alpha_{em}^2}{Q^4} \frac{F_2}{x} \times \left[ 1 - y - \frac{Q^2}{4E^2} + \frac{y^2 + Q^2/E^2}{2(1 + R(x, Q^2))} \right]$$

# Kinematic Plane in $x$ - $Q^2$



Collider experiments

Fixed target experiments

Hermes

# Why measuring *inclusive DIS cross sections* at Hermes?

World largest data set on deuteron

Hermes (1996-2005)

30 M proton + 28 M deuteron  
~450 pb<sup>-1</sup>      ~460 pb<sup>-1</sup>

e.g.: compared to NMC

3 M proton + 6 M deuteron

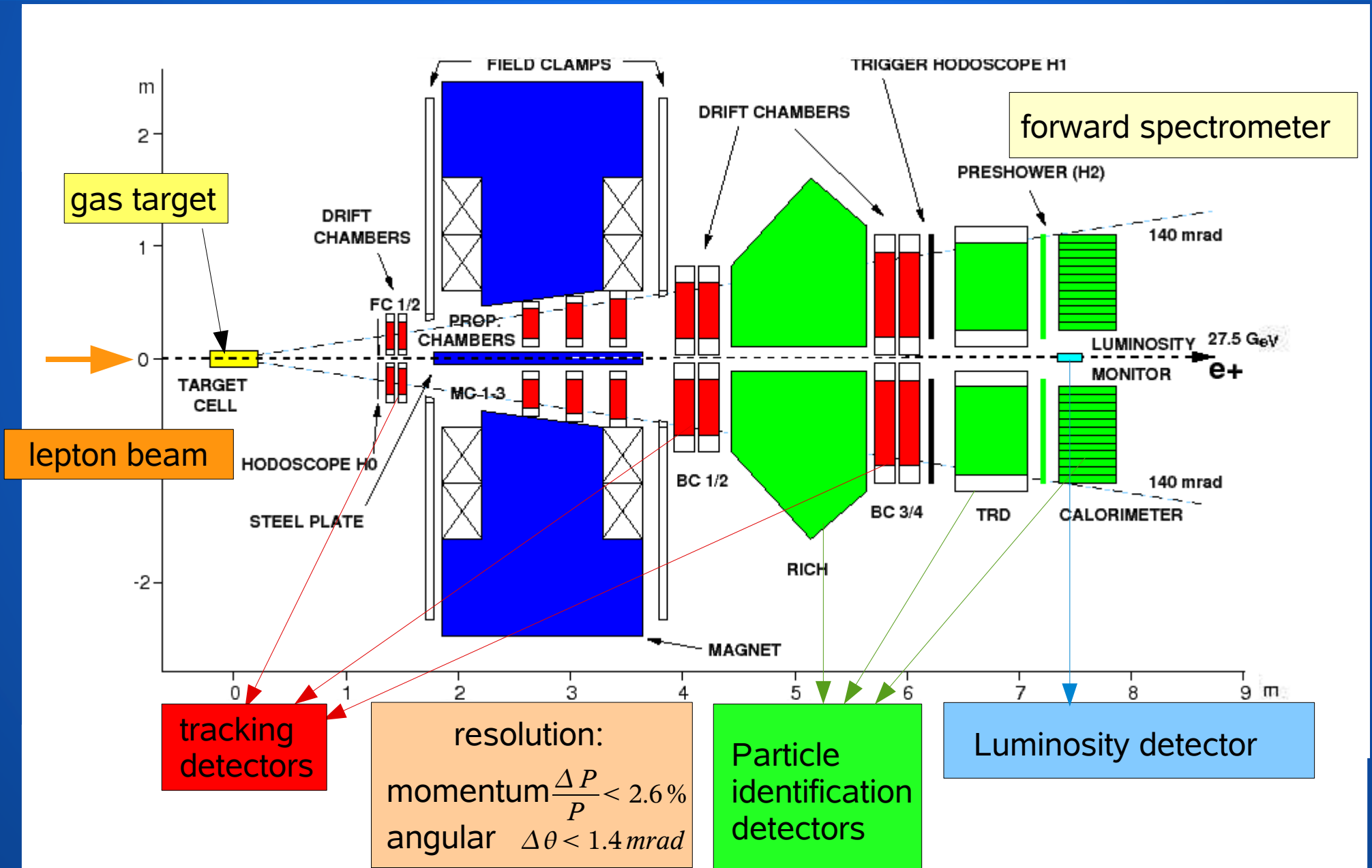
$$F_2^p, F_2^d$$

World data fits  
 $\sigma^{p,d}, \sigma^d/\sigma^p$

Gottfried Sum  
 $\int \frac{dx}{x} (F_2^p - F_2^n)$

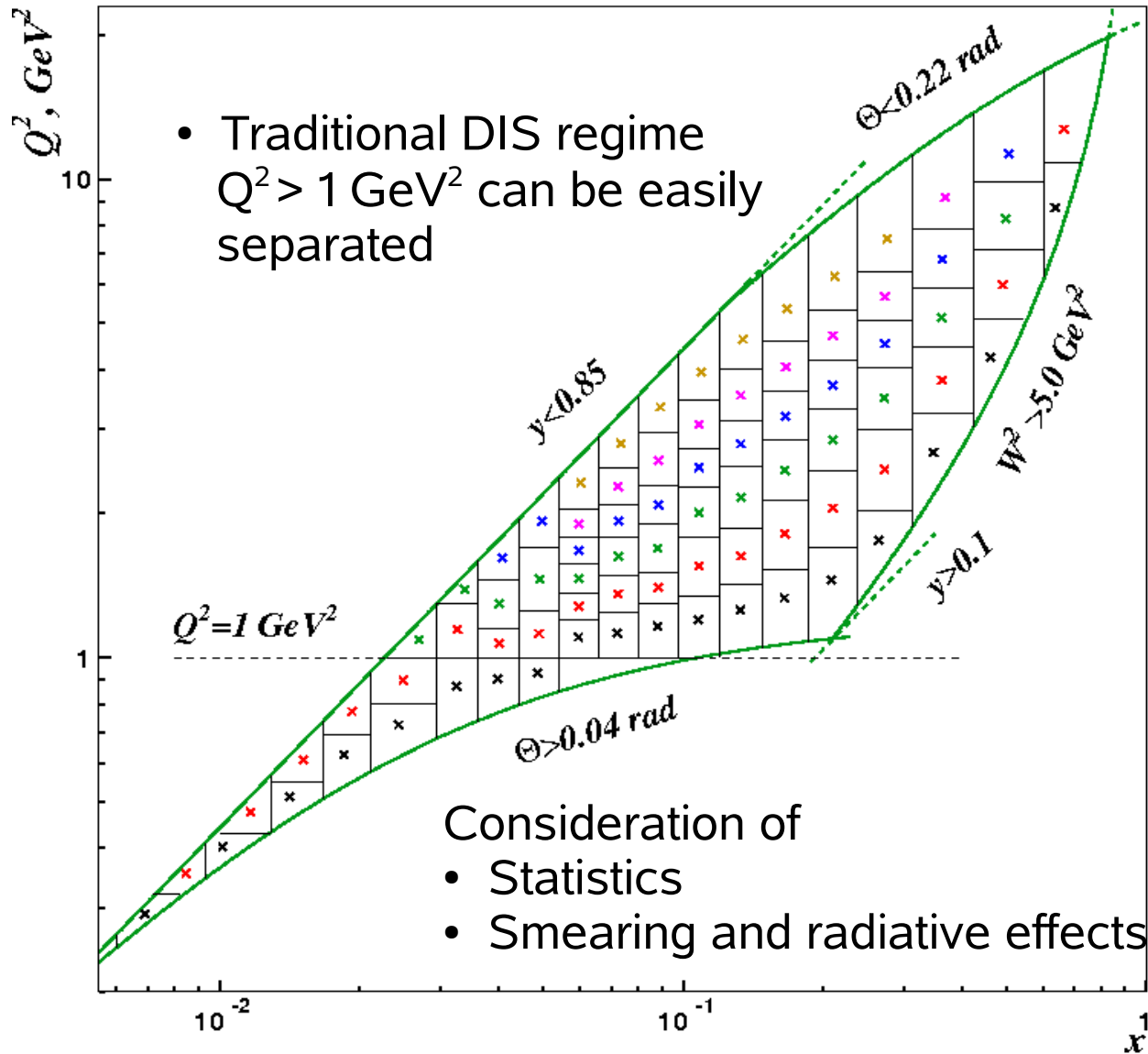
$$d_v / u_v$$

# The HERMES Spectrometer





# Binning in $x$ and $Q^2$



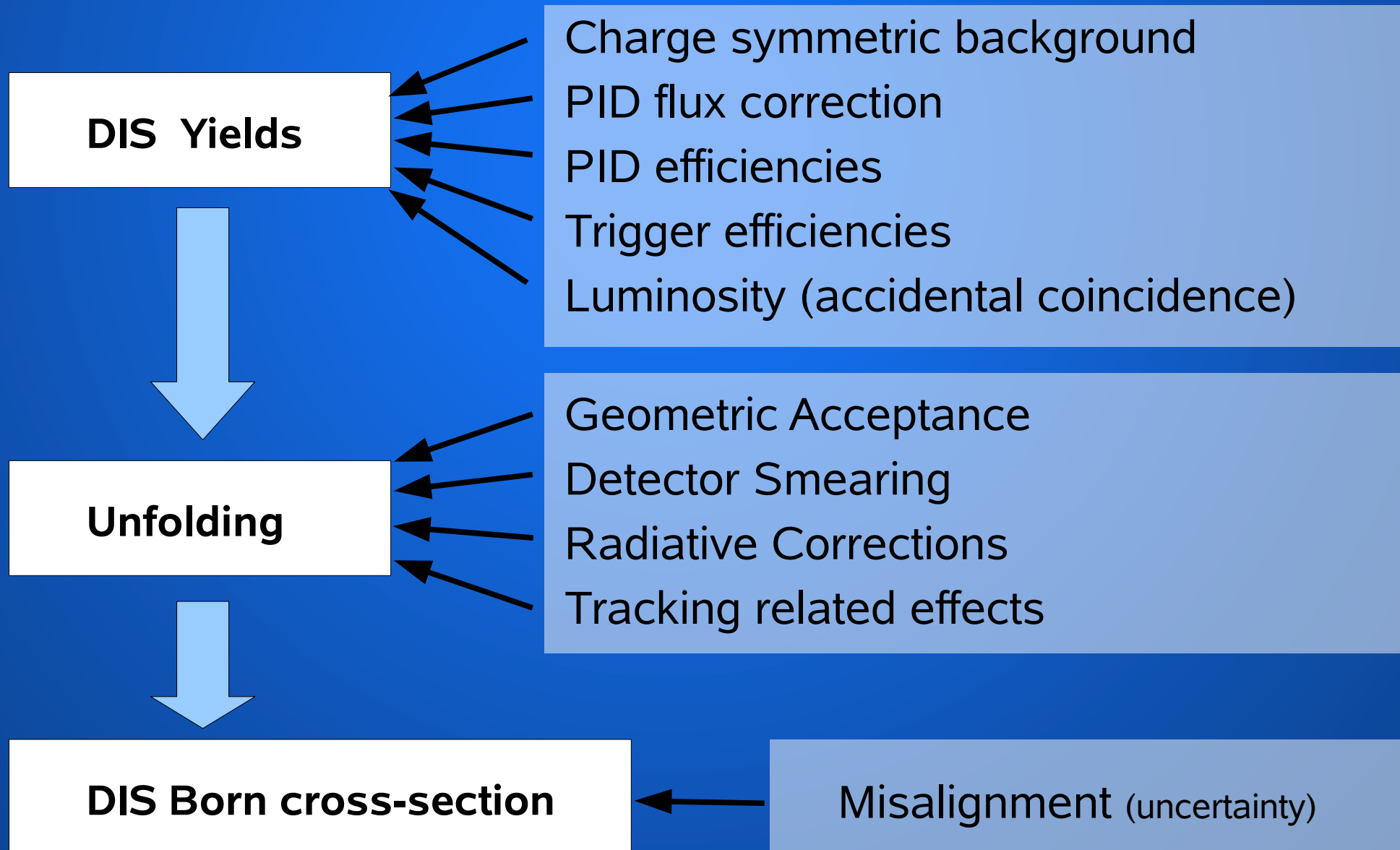
## kinematic region

- $0.006 < x < 0.9$
- $0.1 < y < 0.85$
- $0.2 \text{ GeV}^2 < Q^2 < 20 \text{ GeV}^2$
- $W^2 > 5 \text{ GeV}^2$
- $0.04 \text{ rad} < \Theta < 0.22 \text{ rad}$

## binning

- 19  $x$  bins
- up to 6  $Q^2$  bins
- Total: 81 bins

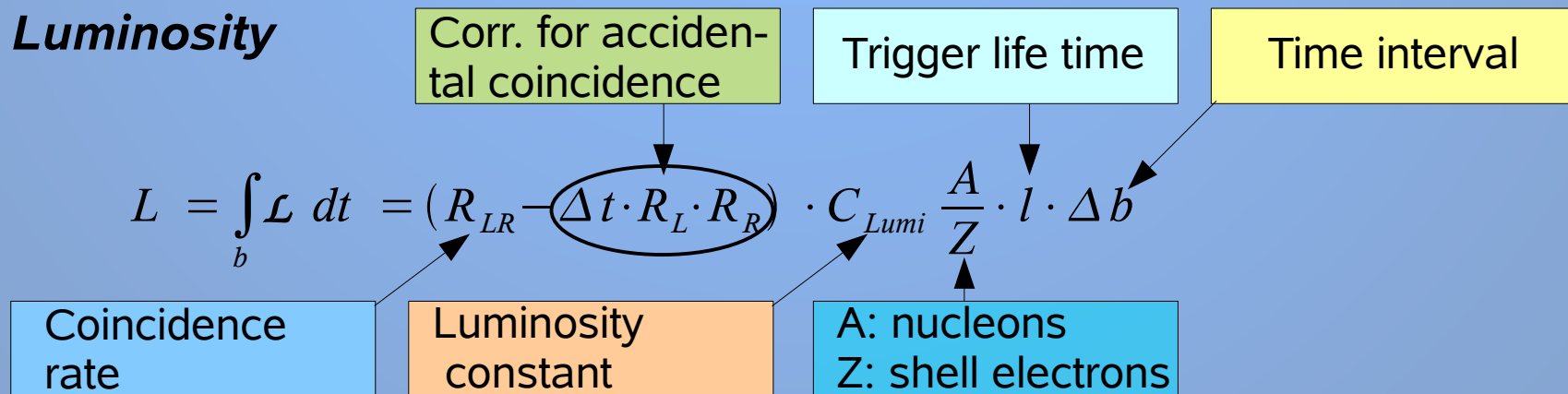
# Extraction of cross sections



# Luminosity

- Elastic reference process
- Interaction of beam with shell electrons
  - Electron Beam: Møller scattering  $e^- e^- \rightarrow e^- e^-$
  - Positron Beam: Bhabha scattering  $e^+ e^- \rightarrow e^+ e^-$ , annihilation  $e^+ e^- \rightarrow \gamma\gamma$
- Coincidence rate  $R_{RL}$  in  $\Delta t = 80\text{ns}$  time resolution window
- Luminosity “constants”  $C_{Lumi}$  convert coincidence rate into luminosity ( $\text{pb}^{-1}$ )
- Uncertainties of  $\sim 3\% - 8\%$ . Acceptance of L. detector depends on e.g.
  - beam conditions
  - magnetic fields

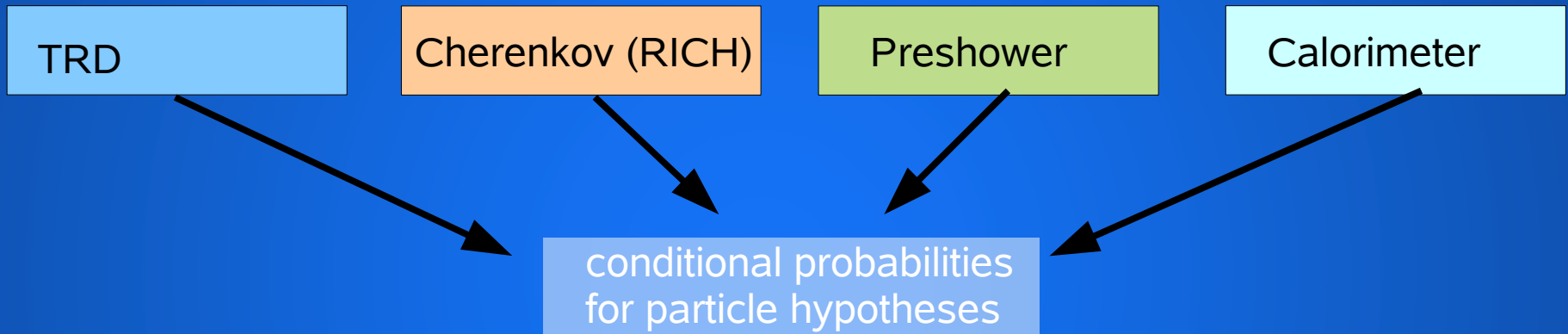
## Luminosity



$$\sigma_{DIS} = \frac{N_{DIS}}{\int \mathcal{L} dt}$$

**DIS yield**

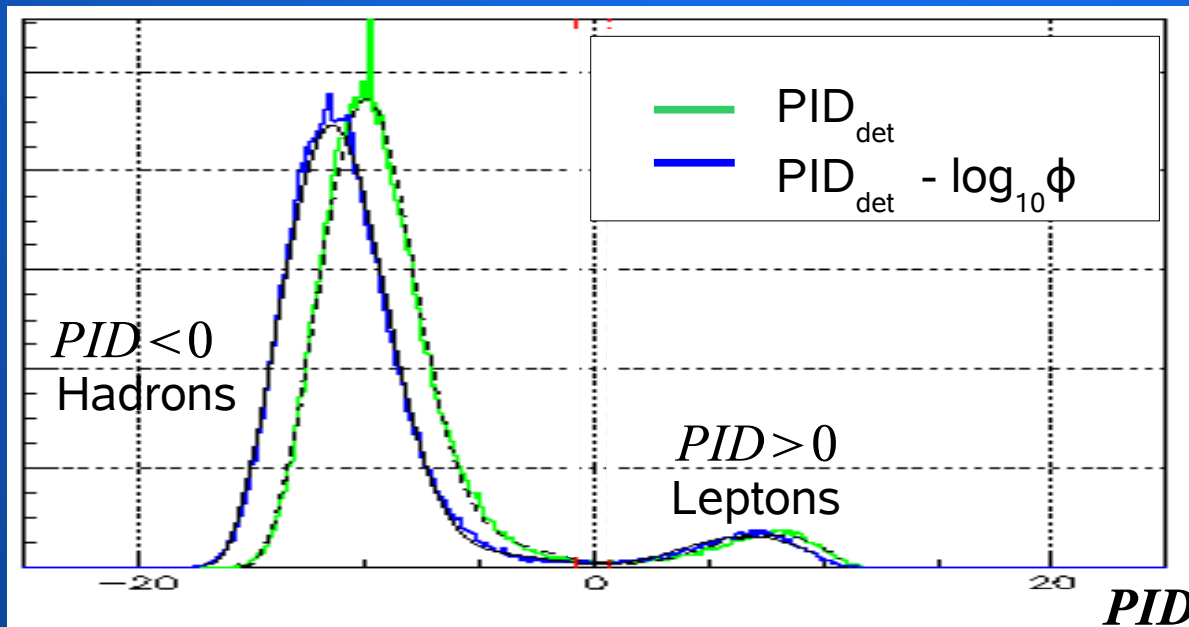
# Particle identification



$$PID = PID_{det} - \log_{10} \Phi$$

$$\Phi = \frac{\phi_h}{\phi_l} = \frac{P(H_h|p, \theta)}{P(H_l|p, \theta)}$$

relative contributions  
hadrons and leptons



# PID efficiency and contamination

**Lepton sample** identified by:  $PID > PID_l$  with  $PID_l = 0$

- high efficiencies and small contaminations at same time

**Contamination of lepton sample**

$C$  = Fractional contribution of hadrons in the lepton sample

$$\frac{\int_{PID_l} dPID N_h}{\int_{PID_l} dPID (N_l + N_h)}$$

**Efficiency lepton identification**

$\epsilon$  = Fraction of leptons selected with  $PID > 0$

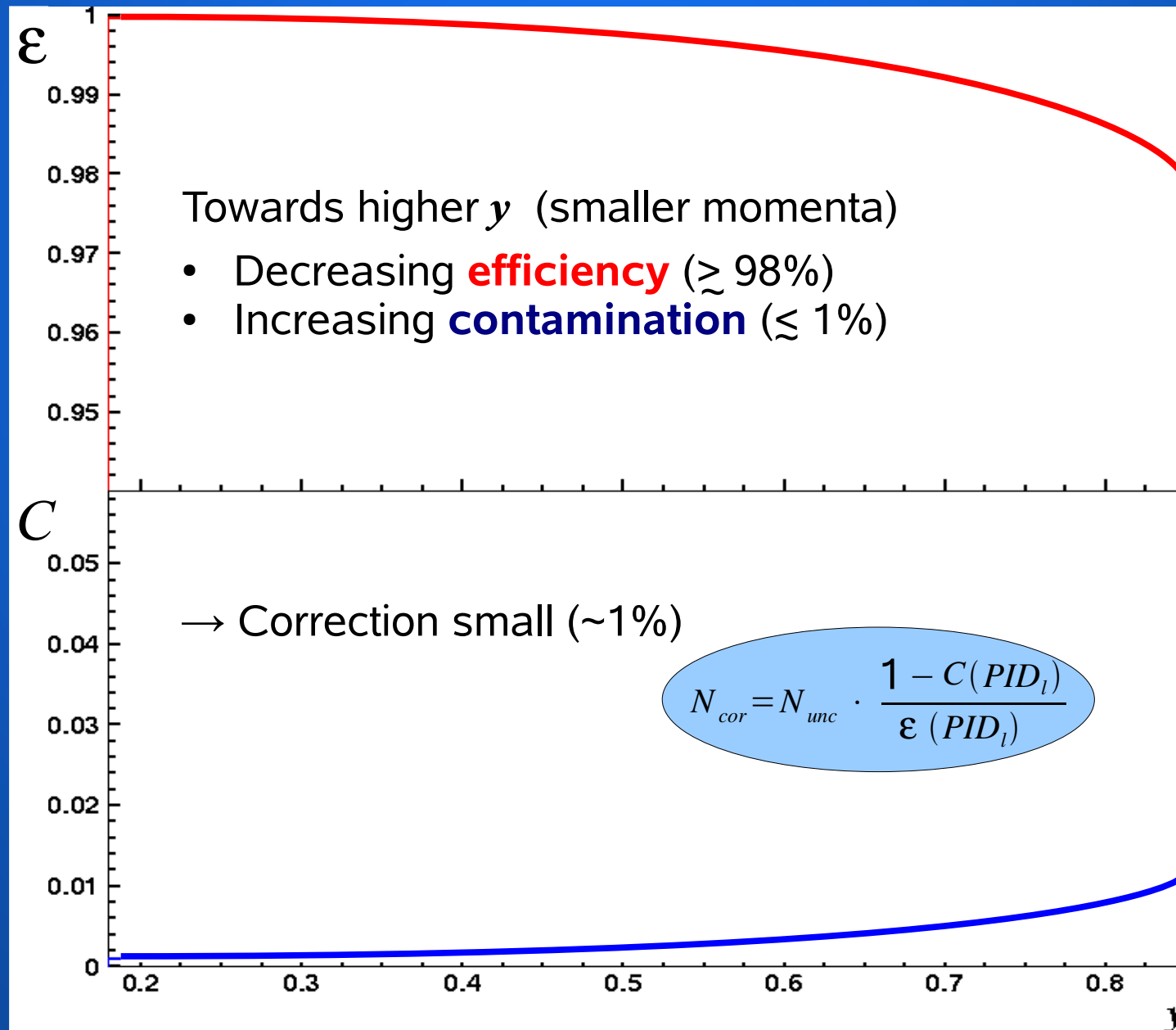
$$\frac{\int_{PID_l} dPID N_l}{\int dPID N_l}$$

**Correction:**

$$N_{cor} = N_{unc} \cdot \frac{1 - C(PID_l)}{\epsilon(PID_l)}$$

Due to correlations between PID detectors, assign uncertainty of full size of correction

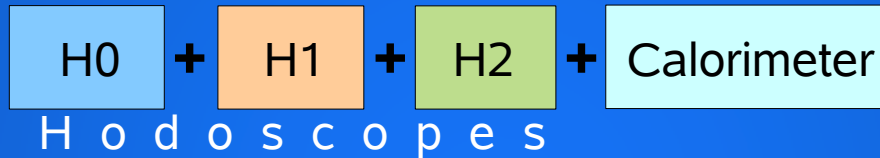
# PID efficiency and contamination



# Trigger efficiencies

- Trigger = combination of fast signals
- Select events of specific interest

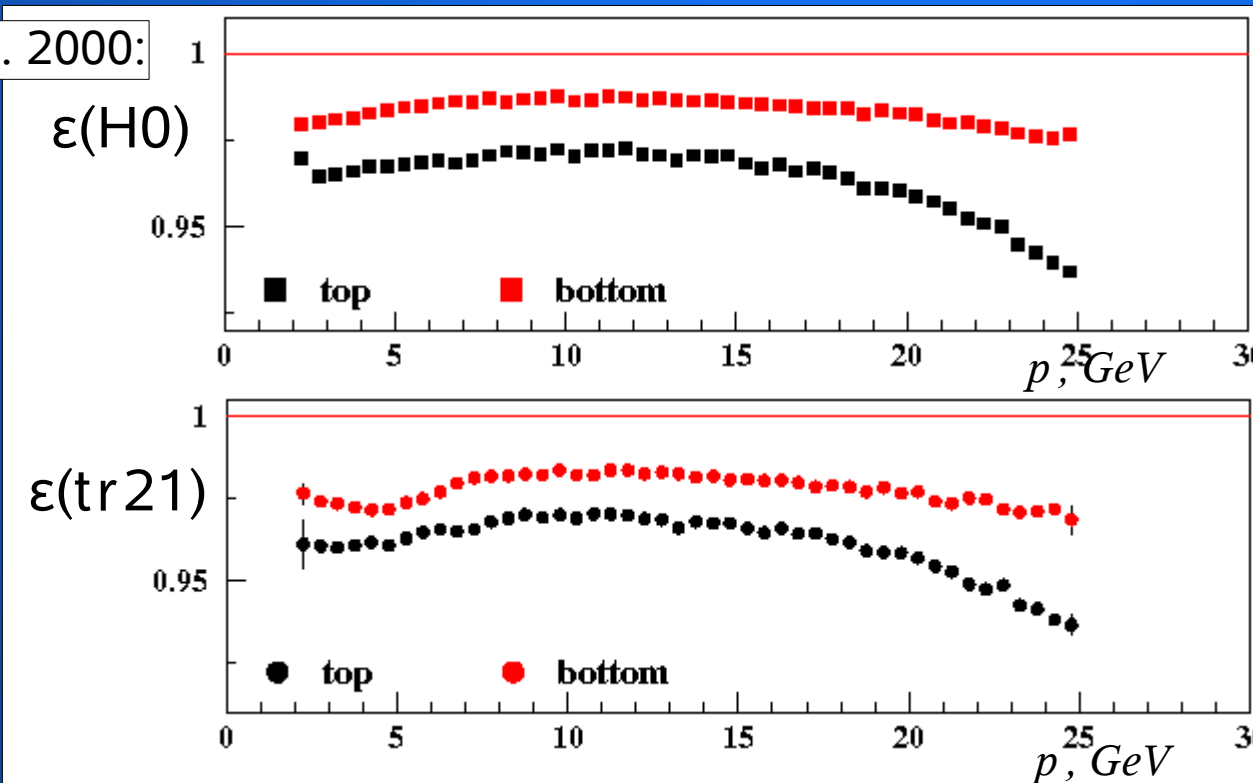
**DIS trigger  
(tr21)**



$$\epsilon(\text{tr21}) = \epsilon(\text{H0}) \cdot \epsilon(\text{H1}) \cdot \epsilon(\text{H2}) \cdot \epsilon(\text{CA})$$

- Trigger efficiencies for each year. Depend on time, momentum, angle.

E.g. 2000:



- $\epsilon(\text{H1}), \epsilon(\text{H2}), \epsilon(\text{CA}) > 99\%$
- $\epsilon(\text{H0}) \sim 97\%$  low!
- Different in top, bot.

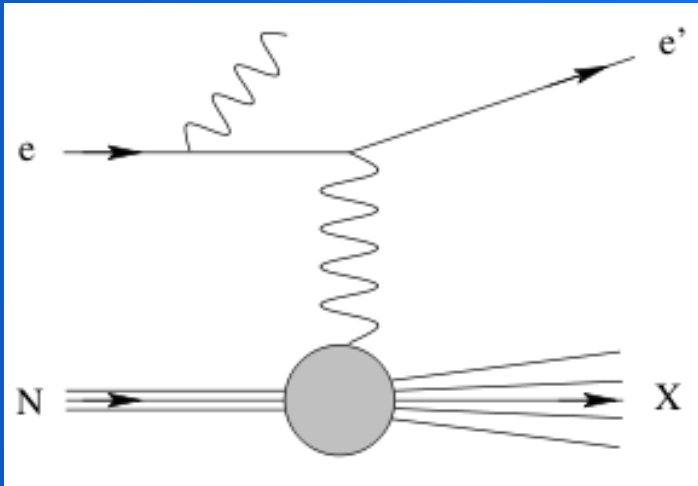
- H0 inefficiencies dominate trigger 21 inefficiency  
→ contrib. to top-bot-asym.

$$w = \frac{1}{\epsilon}$$

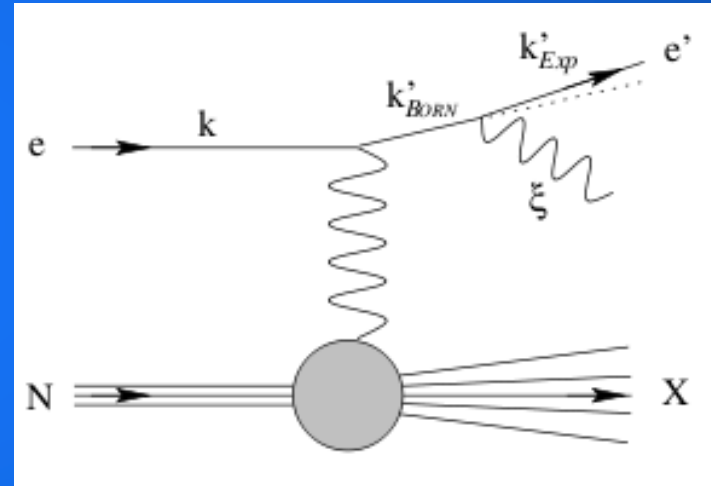
- Correction by counting each event with inverse of efficiencies

# QED radiative effects

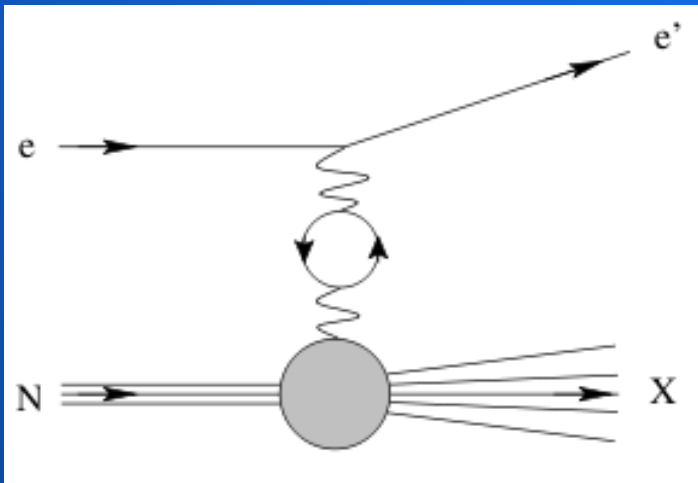
Feynman diagrams of processes contributing to radiative corrections:



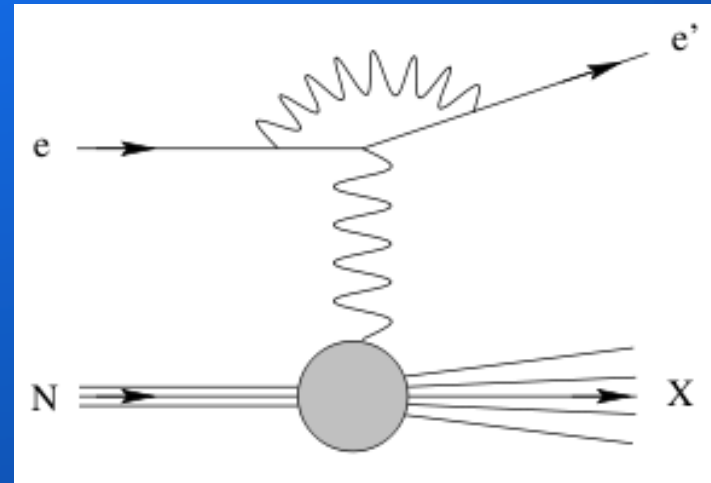
initial state radiation



final state radiation



vacuum polarization



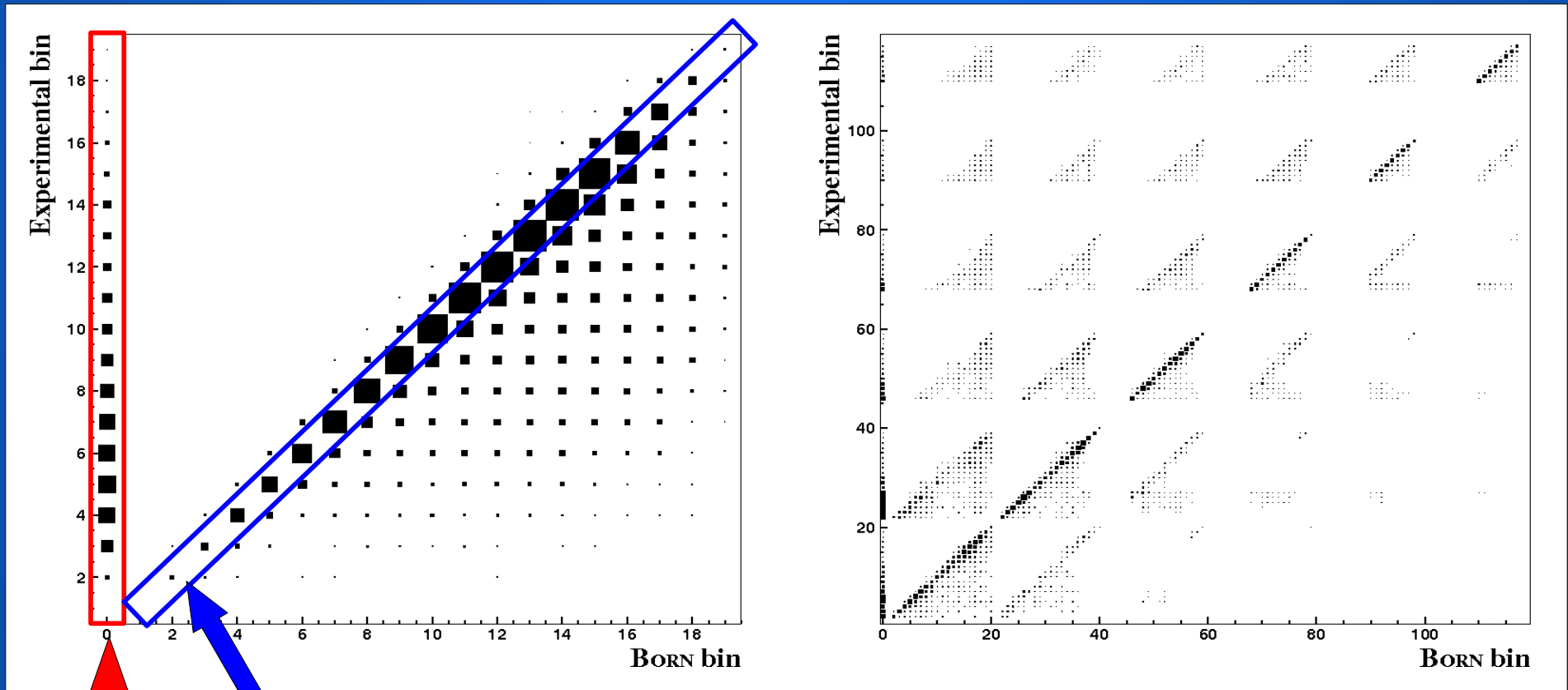
vertex correction



# Migration matrix

Binning in  $x$

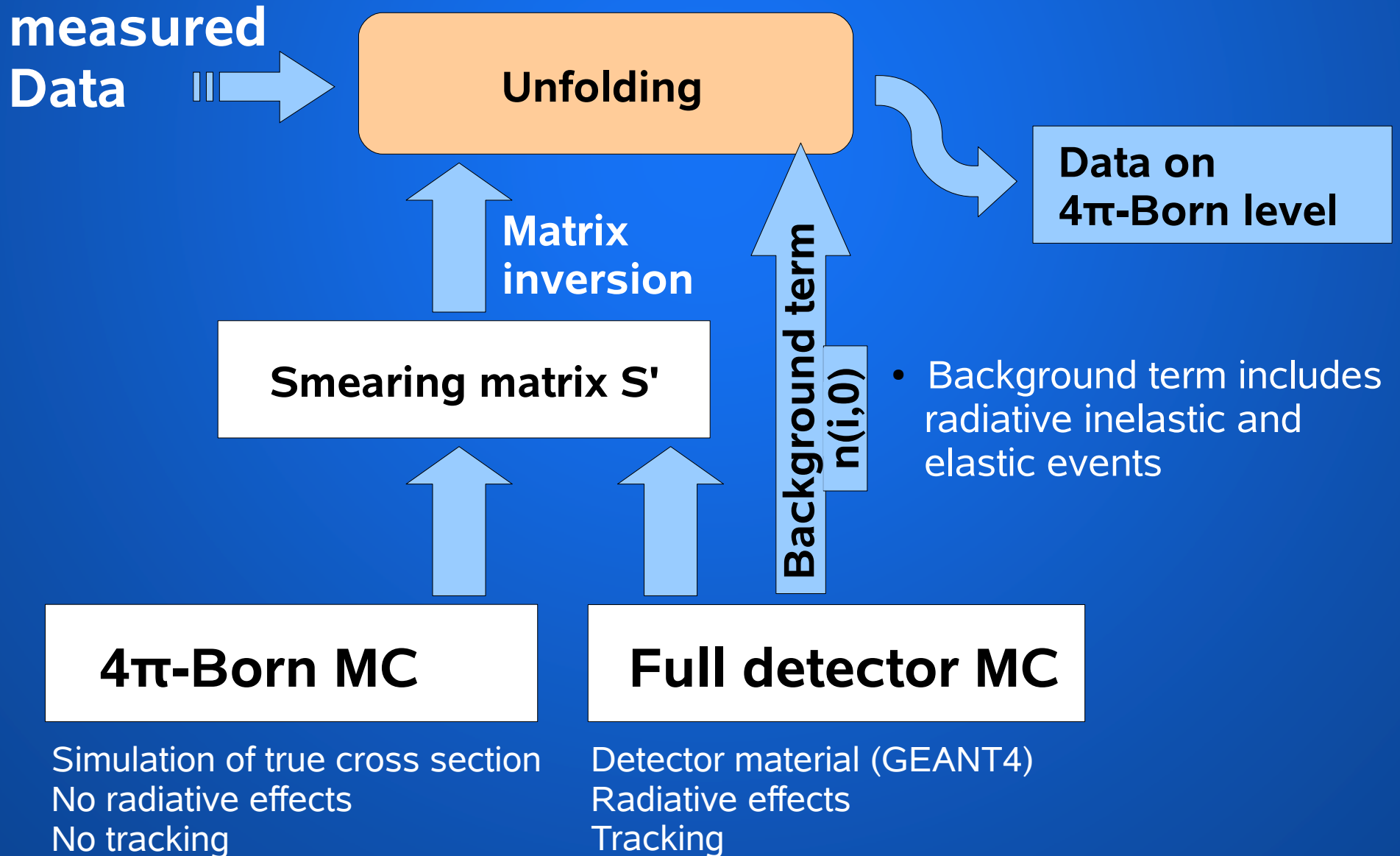
Binning in  $x-Q^2$



Diagonal elements on migration matrix, measured bin = Born level bin

Migration into acceptance from outside  $n(i,0)$ ,  $i>0$

# Unfolding of kinematic bin migration

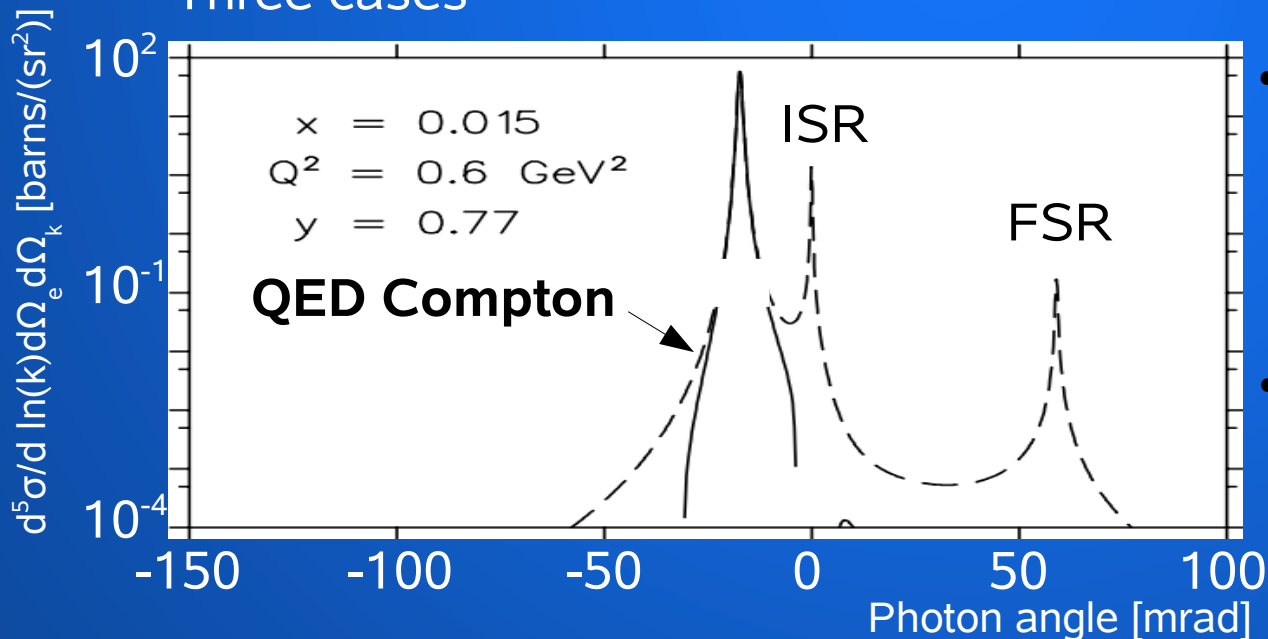


# Bethe-Heitler Cross section

**Bethe-Heitler:** Radiation of real photons associated with elastic interaction of charged particle with the electromagnetic nuclear field

Due to photon radiation, the apparent kinematic variables of Bethe-Heitler events can be indistinguishable from DIS events. → Background to DIS.

Three cases



- Initial state radiation (ISR) photon radiation along incoming lepton (lost in the beam pipe)
- Final state radiation (FSR) photon radiation along outgoing lepton

- **QED Compton** photon radiation at finite angles

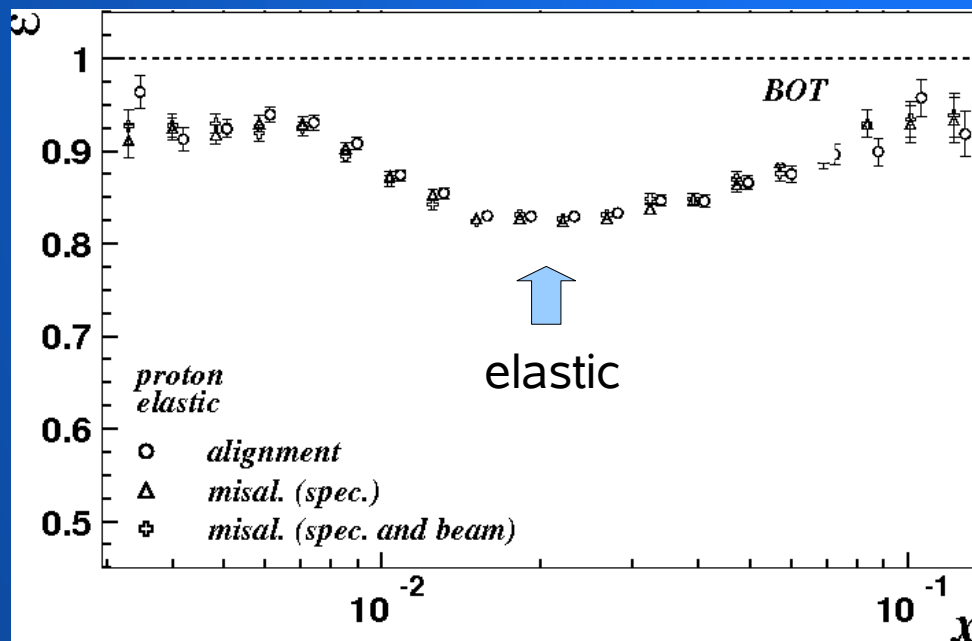
$$(1 - y) \sin \theta_{e'} = y \sin \theta_{\gamma}$$

→ high probability to **hit detector frames**

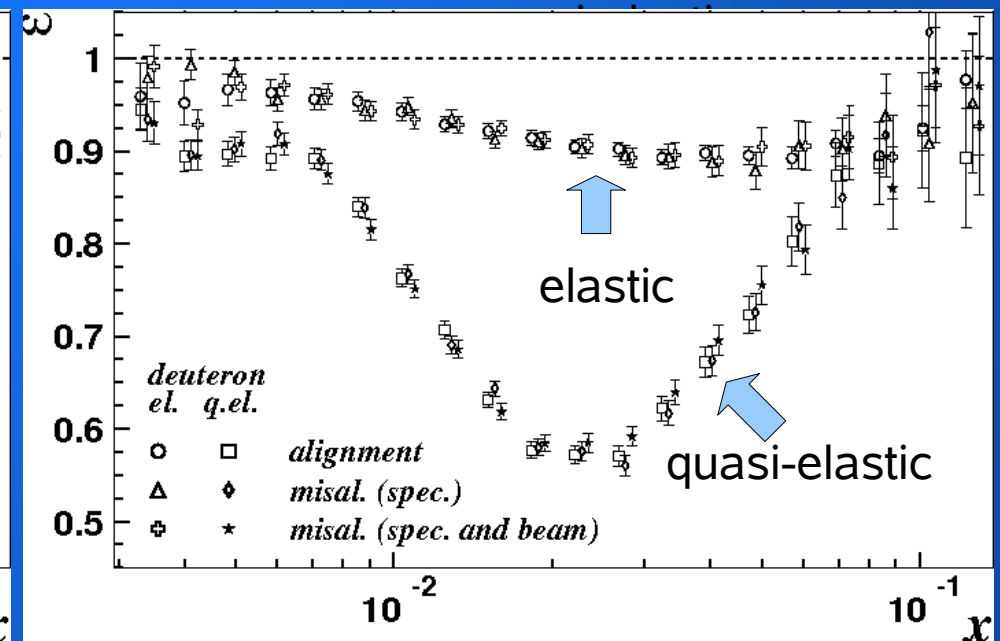
# Bethe-Heitler efficiencies

- Bethe-Heitler efficiencies **extracted from MC** for proton and deuteron

## Proton

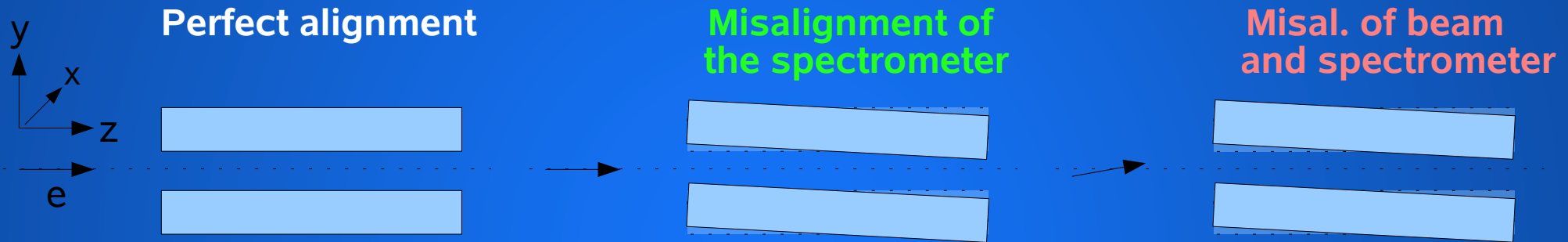


## Deuteron



- Bethe-Heitler efficiencies are relevant for unfolding

# Misalignment



- **Ideal situation:** Perfect alignment of beam and spectrometer
- In practice:
  - Top and bottom parts of **spectrometer** displaced
  - **Beam position** differs from nominal position
- Beam misalignment measured by beam monitors
- Analysis of tracks in the top and bottom halves provides information about misalignment of spectrometer

Misalignment of  
**Beam** (1998, 2000)                      **Spectrometer**

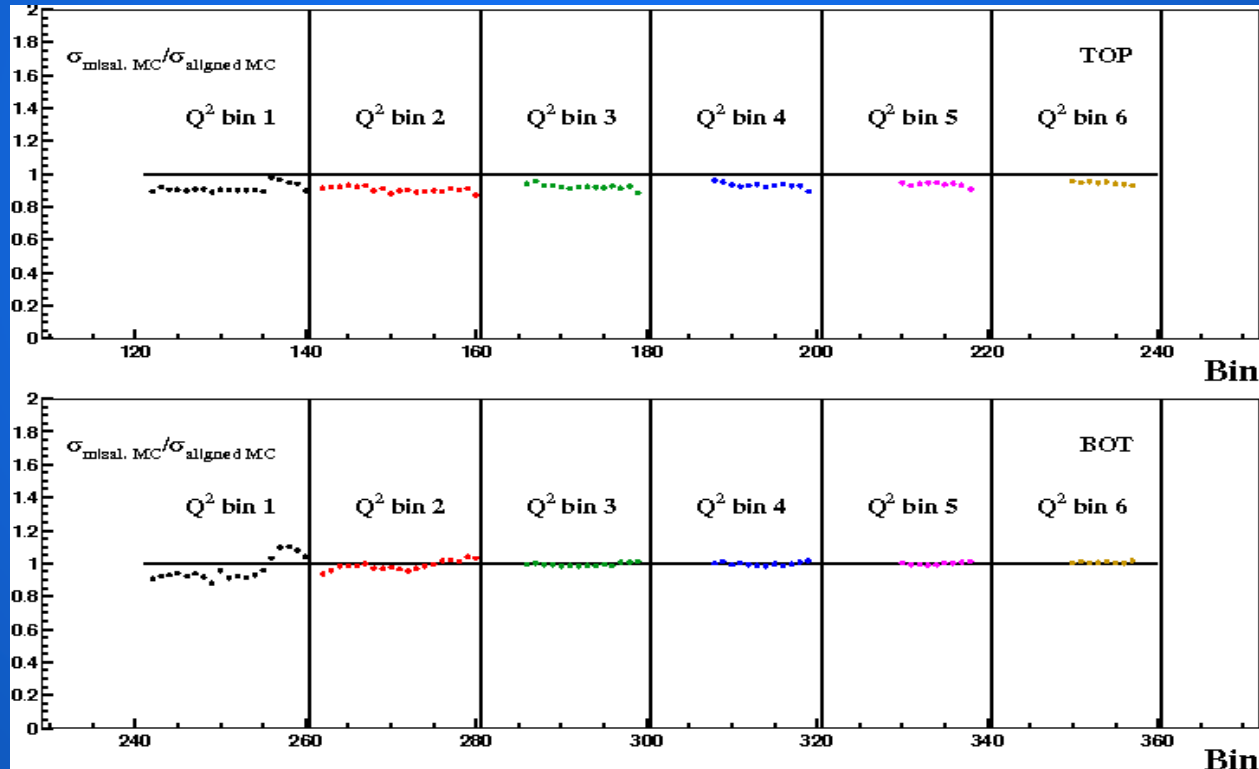
	e <sup>-</sup>	e <sup>+</sup>
X-slope (mrad)	-0.014	-0.035
Y-slope (mrad)	-1.200	-0.420
X-offset (cm)	0.015	0.017
Y-offset (cm)	0.090	0.160

	top	bot
X-slope (mrad)	0.44	0.24
Y-slope (mrad)	-1.2	0.02
X-offset (cm)	-0.09	-0.11
Y-offset (cm)	-0.01	0.11

# Misalignment

## Simulation of misalignment in MC:

$$\frac{\sigma_{\text{misaligned}}}{\sigma_{\text{aligned}}}(\text{top})$$



$$\frac{\sigma_{\text{misaligned}}}{\sigma_{\text{aligned}}}(\text{bot})$$

- “Misalignment ratio”: Effect of misalignment is in the order of 7%.
- No correction for misalignment but assignment of uncertainty:
- Unfolding of the misalignment ratio to Born level

$$\left| \frac{\sigma_{\text{misaligned}}}{\sigma_{\text{aligned}}} - 1 \right|$$

# Systematic uncertainties on $\sigma^p, \sigma^d$

- Which systematic uncertainties are assigned.

$\delta_{\text{PID}}$  : PID misidentification  
typically  $\sim 1\%$

$\delta_{\text{rad.}}$  : Unc. of BH efficiencies due to misalignment  
 $\lesssim 1\%$

$\delta_{\text{mis}}$  : Misalignment effect on DIS events  
 $\sim 7\%$

$\delta_{\text{nor}}$  : Overall normalization unc.: Luminosity  
 $\delta_{\text{nor}}^p = 6.4\%$     $\delta_{\text{nor}}^d = 6.6\%$

# Fit to world data of proton DIS cross-sections

Fit with the following features

- Based on the *ALLM functional form* for the  $\gamma p$  cross section
  - Regge-motivated, phenomenological approach
  - allows very good description of measured regions
  - constructed so that photoproduction data at  $Q^2=0$  can be included

**NEW**

- *Normalization uncertainties* are considered by an accurate method involving a penalty term in  $\chi^2$ .

**NEW**

- *Fit uncertainties* are determined.  
Covariance matrix provided for the first time.

**NEW**

- *Self-consistent* with respect to the use of  $R = \frac{\sigma_L}{\sigma_T}$

**NEW**

- This fit includes *newer data* and covers **2821 data points**. This is more than twice as much as used in ALLM97 (1356 data points).

- Fit results available in FORTRAN routine:

[http://www-hermes.desy.de/users/dgabbert/SIGMATOT\\_PARAM.tgz](http://www-hermes.desy.de/users/dgabbert/SIGMATOT_PARAM.tgz)



# Fit to world data of proton DIS cross-sections

- The DIS cross-section in the 1-photon exchange approximation:

$$\frac{d^2\sigma}{dx dQ^2} = \frac{4\pi\alpha_{em}^2}{Q^4} \frac{F_2}{x} \times \left[ 1 - y - \frac{Q^2}{4E^2} + \frac{y^2 + Q^2/E^2}{2(1+R(x, Q^2))} \right]$$

for all data sets

- $F_2$  can be related to the full cross-section  $\sigma = \sigma_L + \sigma_T$

$$\sigma_{L+T}(\gamma p) = \frac{4\pi\alpha}{Q^2(1-x)} \frac{Q^2 + 4M^2x^2}{Q^2} F_2(W^2, Q^2)$$

- Consistent treatment of  $R$

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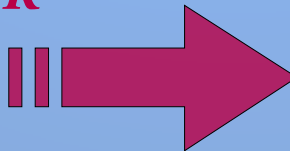
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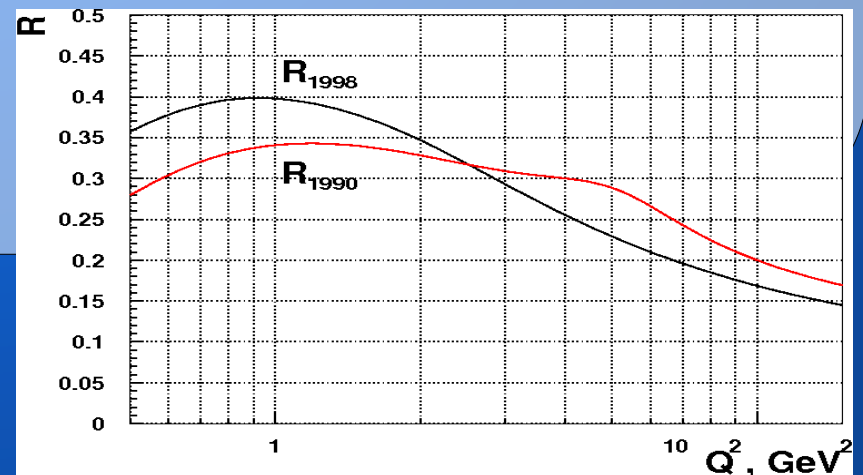
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Central values of the two common parameterizations



# $\chi^2$ - Minimization

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$$\chi^2 = \sum_i^{n_{max}} \frac{(\sigma_i^{exp} - \sigma_i^{th})^2}{\delta_{i\ sta}^2 + \delta_{i\ sys}^2}$$

General definition

# $\chi^2$ - Minimization

## $\chi^2$ - Minimization

$$\chi^2 = \underbrace{\sum_i^{n_{max}} \frac{(\sigma_i^{\text{exp}} - \sigma_i^{\text{th}} / (1 + \mathbf{v}_k \delta_{k(i)}^{\text{norm}}))^2}{\delta_{i \text{ sta}}^2 + \delta_{i \text{ sys}}^2}}_{\text{data points}} + \underbrace{\sum_k \mathbf{v}_k^2}_{\text{data sets}}$$

- Introduce normalization parameters  $\mathbf{v}_k$  considered to be normal distributed – implemented by a penalty term.
- The normalization parameters  $\mathbf{v}_k$  defined in order to perform a re-normalization according to normalization error  $\delta_{k(i)}^{\text{norm}}$ .
- The analytic solution of  $\mathbf{v}_k$  for a fixed set of model parameters can be obtained from  $d\chi^2/d\mathbf{v}_k = 0$ , since  $\mathbf{v}_k$  are independent.

# Error propagation

## Error propagation

$$V[\sigma_{L+T}(\mathbf{p}, x, Q^2)] = \sum_{i,j} cov_{i,j}^p \frac{d\sigma_{L+T}(\mathbf{p}, x, Q^2)}{dp_i} \frac{d\sigma_{L+T}(\mathbf{p}, x, Q^2)}{dp_j}$$

$V$	variance
$\mathbf{p}$	parameter vector
$cov_{i,j}^p$	covariance matrix for $\mathbf{p}$

# $F_2$ fit results (GD08)

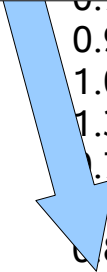
Nr.	Exp	n	$\chi^2/n$	$\delta_k^{\text{nor}}$	$v_k$
1.	SLAC-E49a	98	0.51	2.1	0.06
2.	SLAC-E49b	187	1.15	2.1	-0.28
3.	SLAC-E61	25	0.24	2.1	0.01
4.	SLAC-E87	94	0.68	2.1	0.07
5.	SLAC-E89a	72	1.06	2.1	1.31
6.	SLAC-E89b	98	1.01	2.1	0.17
7.	NMC 90 GeV	73	0.77	2.0	-0.37
8.	NMC 120 GeV	65	1.54	2.0	0.14
9.	NMC 200 GeV	75	1.13	2.0	-0.09
10.	NMC 280 GeV	79	0.94	2.0	-0.24
11.	E665	91	1.04	1.8	0.67
12.	BCDMS 100 GeV	58	1.13	3.0	-1.20
13.	BCDMS 120 GeV	62	0.73	3.0	0.03
14.	BCDMS 200 GeV	57	1.32	3.0	-1.09
15.	BCDMS 280 GeV	52	1.12	3.0	-1.03
16.	H1 94 a	37	0.35	3.9	0.05
17.	H1 94 b	156	0.63	1.5	1.13
18.	H1 SVX	44	0.49	3.0	-3.02
19.	ZEUS 94	188	1.15	2.0	1.66
20.	ZEUS BPC	34	0.40	2.4	-1.28
21.	ZEUS SVX	36	0.76	3.0	-1.00
24.	ZEUS 9697	242	0.75	2.0	0.09
25.	ZEUS 97	70	0.97	2.0	-2.23
26.	H1 99 00	147	1.01	1.5	-1.08
27.	H1 98 99	126	1.37	1.8	-1.38
28.	H1 94 97	130	0.79	1.5	-1.46
29.	H1 96 97 a	67	1.05	1.7	1.77
30.	H1 96 97 b	80	0.82	1.7	2.02
<b>31.</b>	<b>this analysis, HERMES</b>	<b>81</b>	<b>0.40</b>	<b>6.4</b>	<b>0.67</b>

Total:  $\chi/n = 0.93$

# F<sub>2</sub> fit results (GD08)

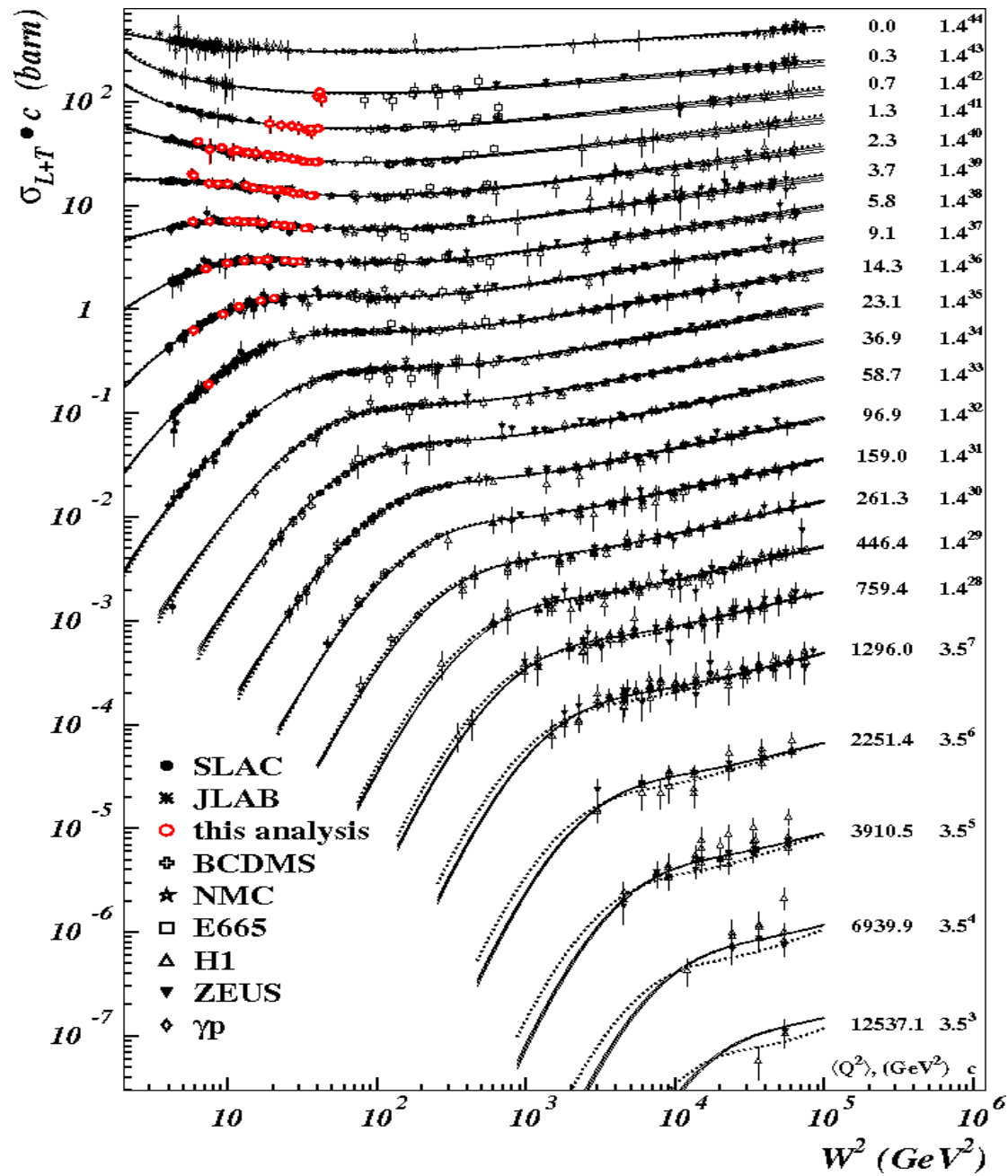
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5.	SLAC-E89a	72	1.06	2.1	1.31
6.	SLAC-E89b	98	1.01	2.1	0.17
7.	NMC 90 GeV	73	0.77	2.0	-0.37
8.	NMC 120 GeV	65	1.54	2.0	0.14
9.	NMC 200 GeV	75	1.13	2.0	-0.09
10.	NMC 280 GeV	79	0.94	2.0	-0.24
11.	E665	91	1.04	1.8	0.67
12.	BCDMS 100 GeV	58	1.13	3.0	-1.20
13.	BCDMS 120 GeV	62	0.73	3.0	0.03
14.	BCDMS 200 GeV	57	1.32	3.0	-1.09
15.	BCDMS 280 GeV	52	1.12	3.0	-1.03
16.	H1 94 a				0.05
17.	H1 94 b				1.13
18.	H1 SVX				-3.02
19.	ZEUS 94				1.66
20.	ZEUS B				-1.28
21.	ZEUS S				-1.00
24.	ZEUS 96/97	472	0.75	2.0	0.09
25.	ZEUS 97	70	0.97	2.0	-2.23
26.	H1 99 00	147	1.01	1.5	-1.08
27.	H1 98 99	126	1.37	1.8	-1.38
28.	H1 94 97	130	0.79	1.5	-1.46
29.	H1 96 97 a	67	0.05	1.7	1.77
30.	H1 96 97 b	80	0.82	1.7	2.02
<b>31.</b>	<b>this analysis, HERMES</b>	<b>81</b>	<b>0.40</b>	<b>6.4</b>	<b>0.67</b>

Low value of  $\chi^2/n$  reflects conservative assignment of uncertainties: misalignment, overall normalization



Total:  $\chi/n = 0.93$

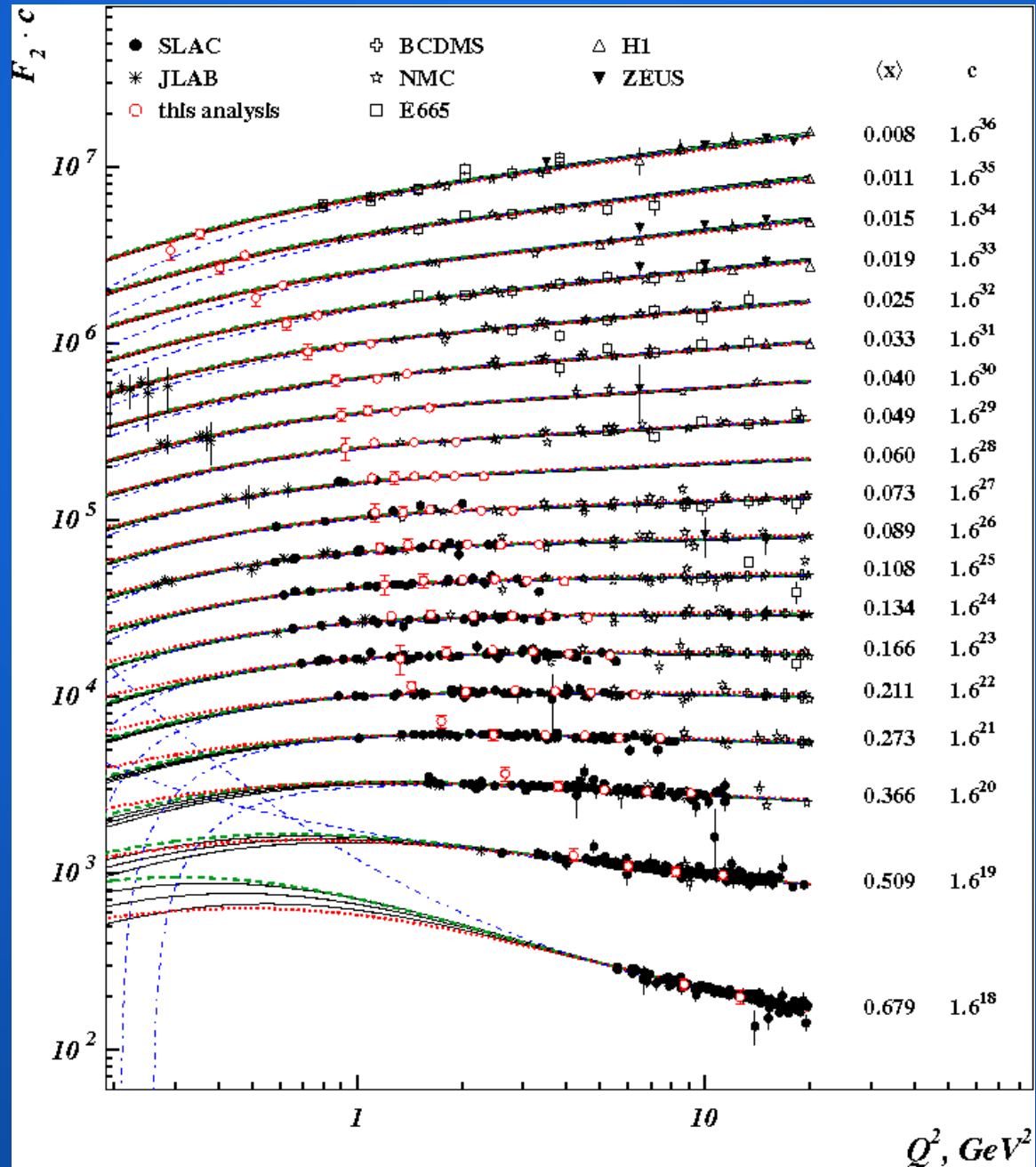
# F<sub>2</sub> fit results (GD08)





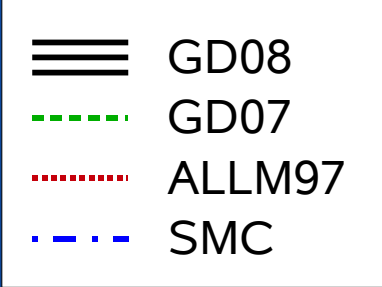
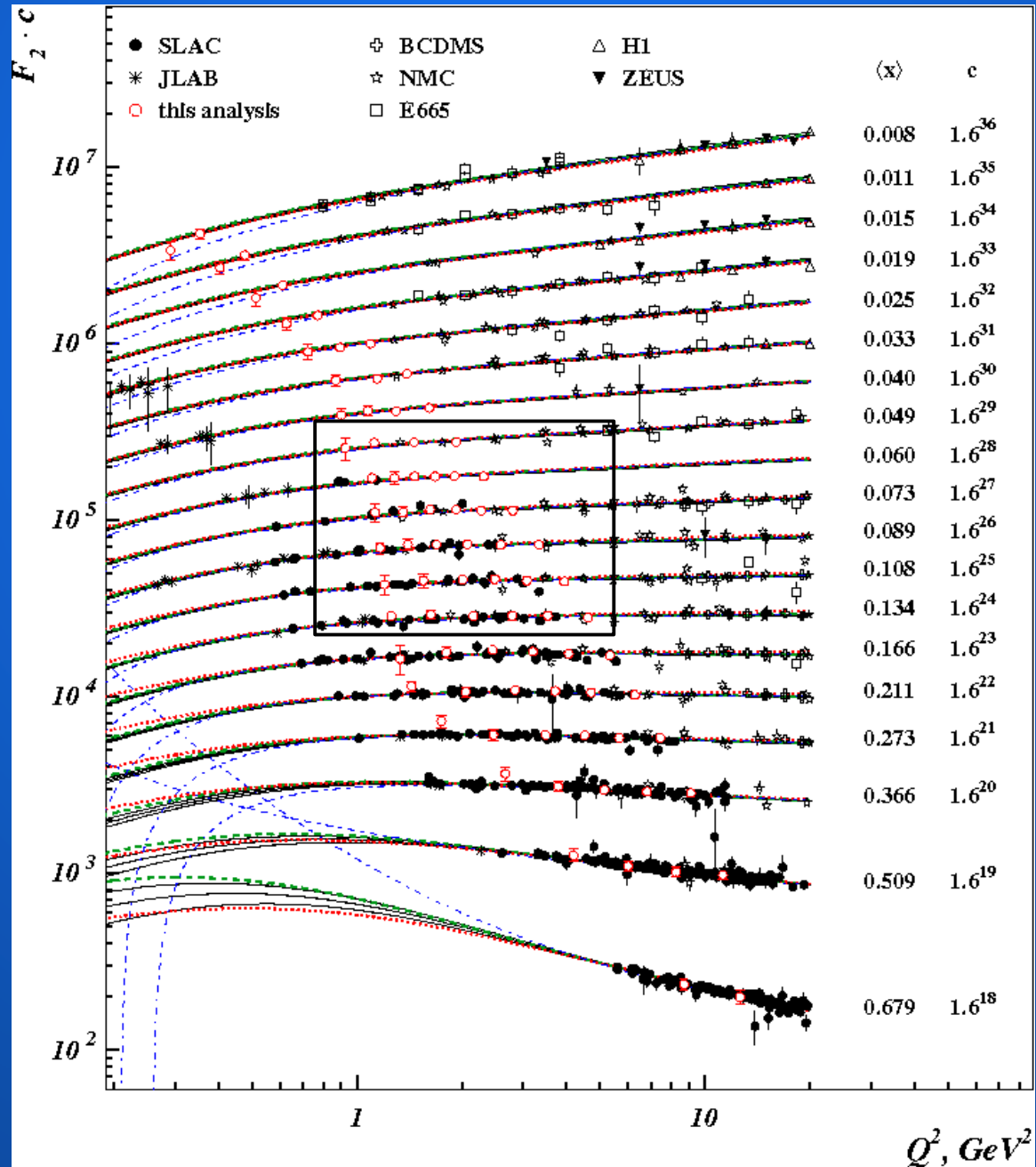
# Results on $F_2^p$

Proton



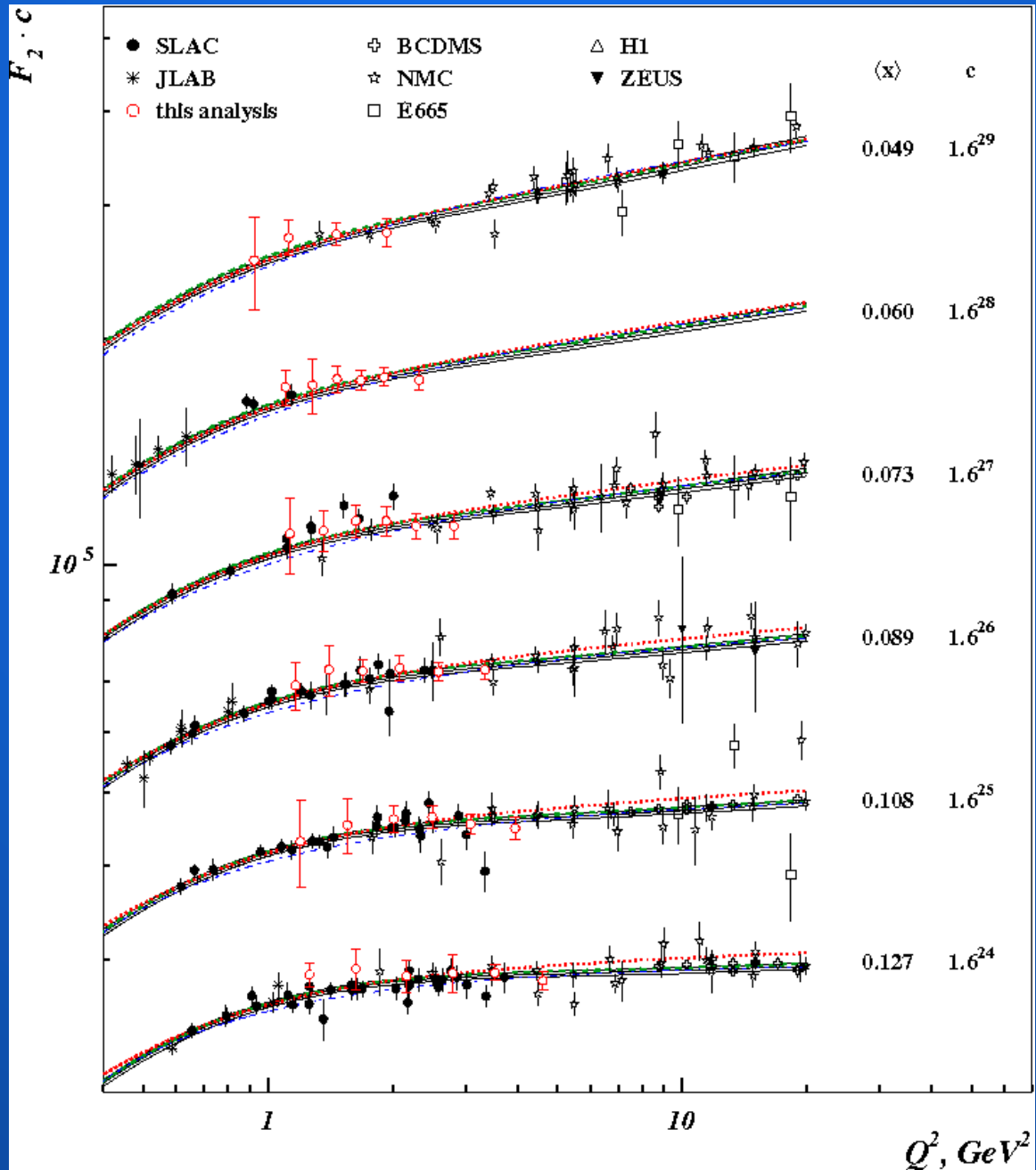
# Results on $F_2^p$

Proton



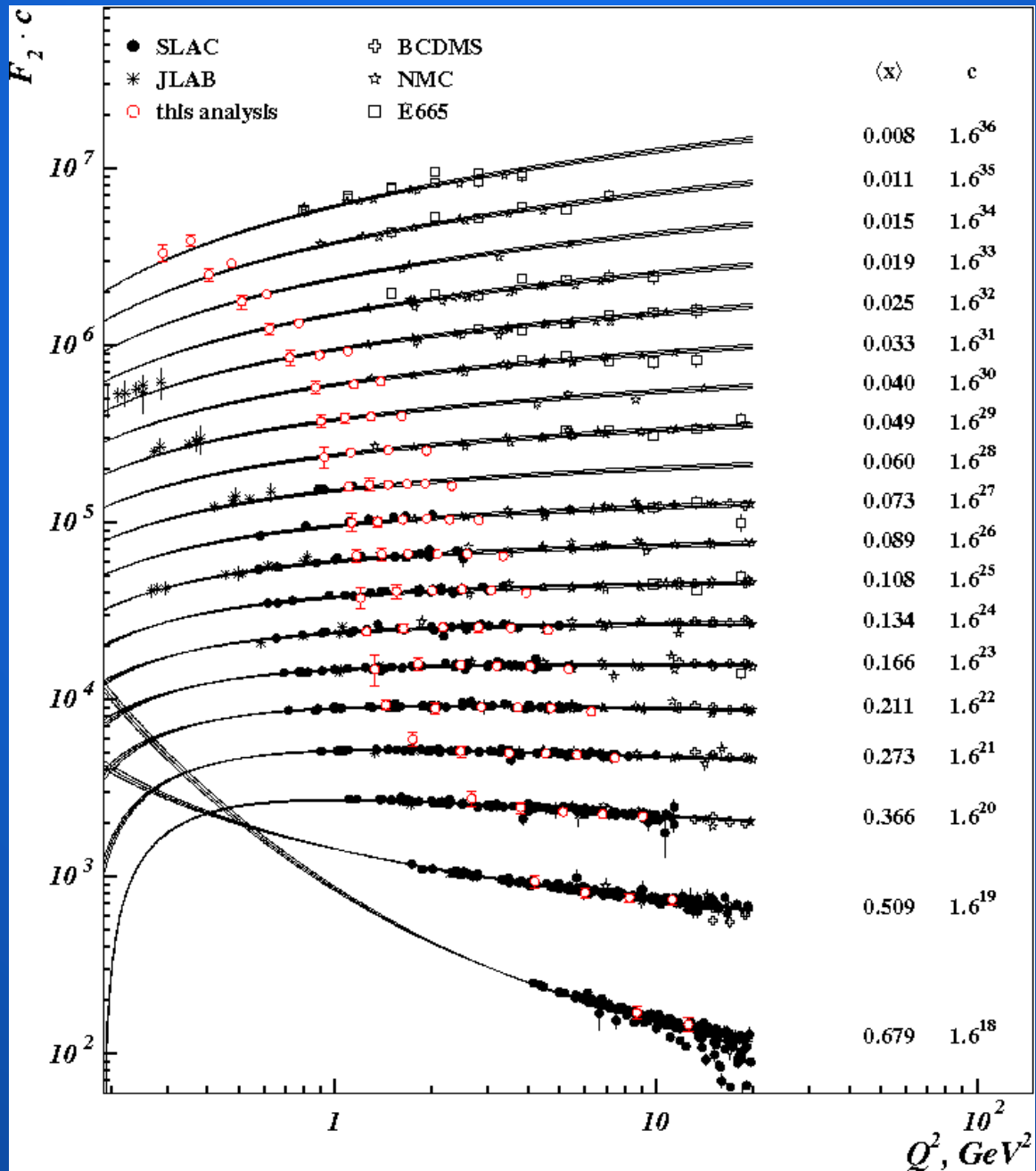
# Results on $F_2^p$

Proton



# Results on $F_2^d$

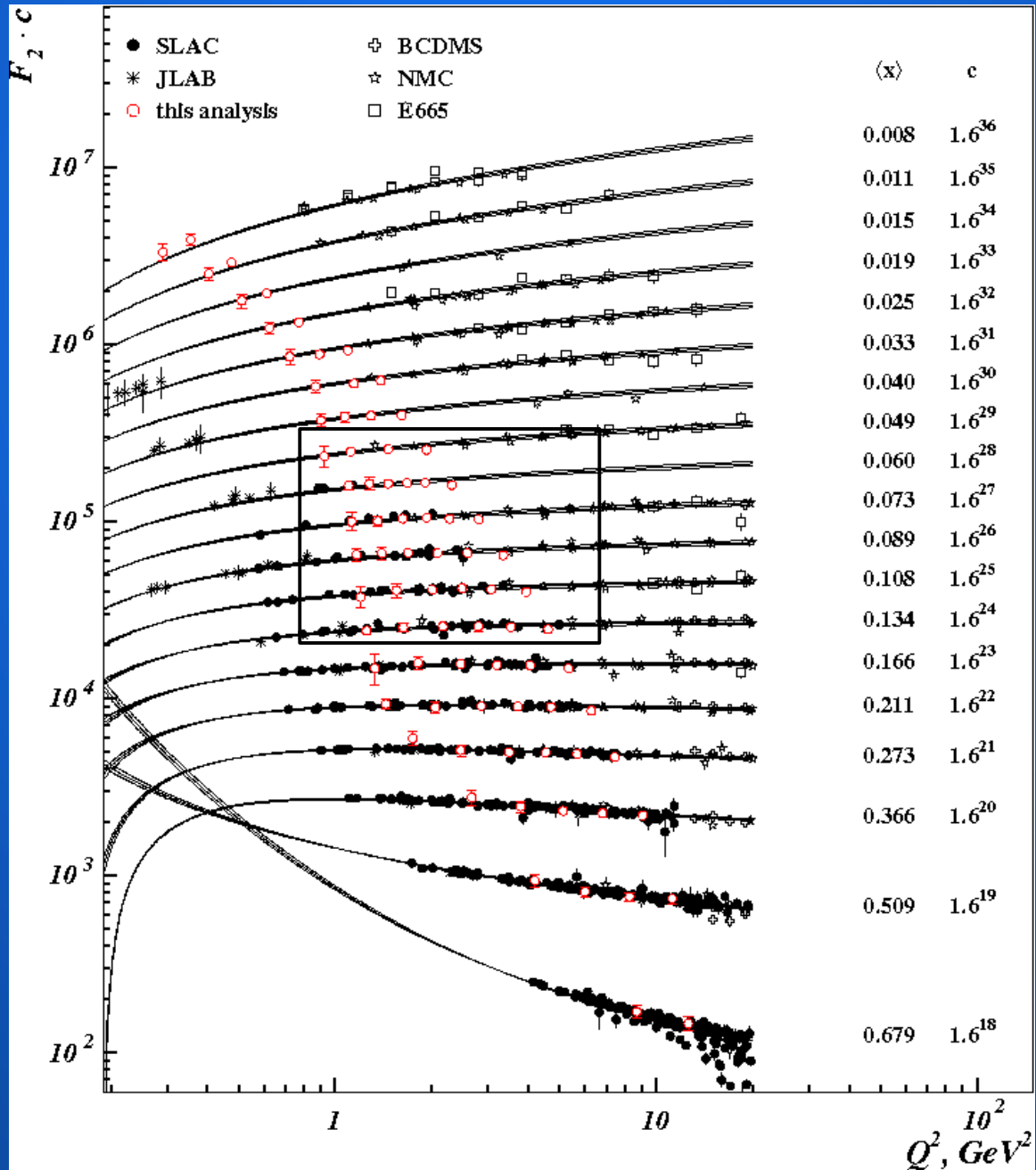
## Deuteron



≡ SMC

# Results on $F_2^d$

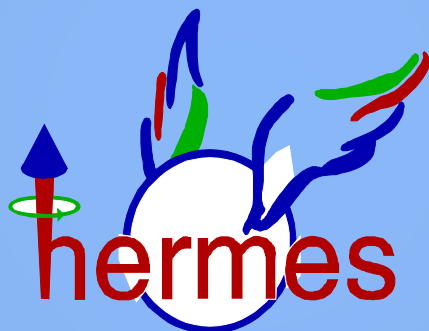
Deuteron



≡ SMC



# Why measuring *inclusive DIS cross sections* at Hermes?



$$F_2^p, F_2^d$$

World data fits

$$\sigma^{p,d} \quad \sigma^d / \sigma^p$$

Gottfried Sum

$$\int \frac{dx}{x} (F_2^p - F_2^d)$$

$$d_v / u_v$$

# Basic nucleon structure from sum rules

## Quark-Parton Model

Adler sum rule

$$\int dx/x (F_2^{\bar{v}p} - F_2^{vp}) = \int dx/x (F_2^{\bar{v}n} - F_2^{vp}) = 2 \int dx (u_v - d_v) = 2$$

← Sensitive to difference between u and d valence quarks

Gross-Llewellyn Smith sum rule

$$\int dx (F_3^{\bar{v}p} + F_3^{vp}) = \int dx (F_3^{\bar{v}n} + F_3^{vp}) = 2 \int dx (u_v + d_v) = 6$$

← Sensitive to sum of u and d valence quarks

Gottfried sum rule

••••



# Basic nucleon structure from sum rules

## Quark-Parton Model

Adler sum rule

$$\int dx/x (F_2^{\bar{\nu}p} - F_2^{\nu p}) = \int dx/x (F_2^{\bar{\nu}n} - F_2^{\nu p}) = 2 \int dx (u_v - d_v) = 2$$

← Sensitive to difference between u and d valence quarks

Gross-Llewellyn Smith sum rule

$$\int dx (F_3^{\bar{\nu}p} + F_3^{\nu p}) = \int dx (F_3^{\bar{\nu}n} + F_3^{\nu p}) = 2 \int dx (u_v + d_v) = 6$$

← Sensitive to sum of u and d valence quarks

Gottfried sum rule

$$\int dx/x (F_2^{e,\mu p} - F_2^{e,\mu n}) = \frac{1}{3} \int dx (u_v - d_v) + \frac{2}{3} \int dx (\bar{u} - \bar{d}) \stackrel{\bar{u} = \bar{d}}{\downarrow} \frac{1}{3}$$

$$\bar{u} = \bar{d}$$

- Gottfried sum rule (charged lepton scattering) → Sensitive to
  - Difference between u and d valence quarks
  - **Sea quark flavor symmetry / asymmetry?**

# Sea quark asymmetry

Measurements, e.g:

DIS data : SLAC, BCDMS, NMC, HERMES  
 Drell-Yan data: E288, (E772), NA51, E866

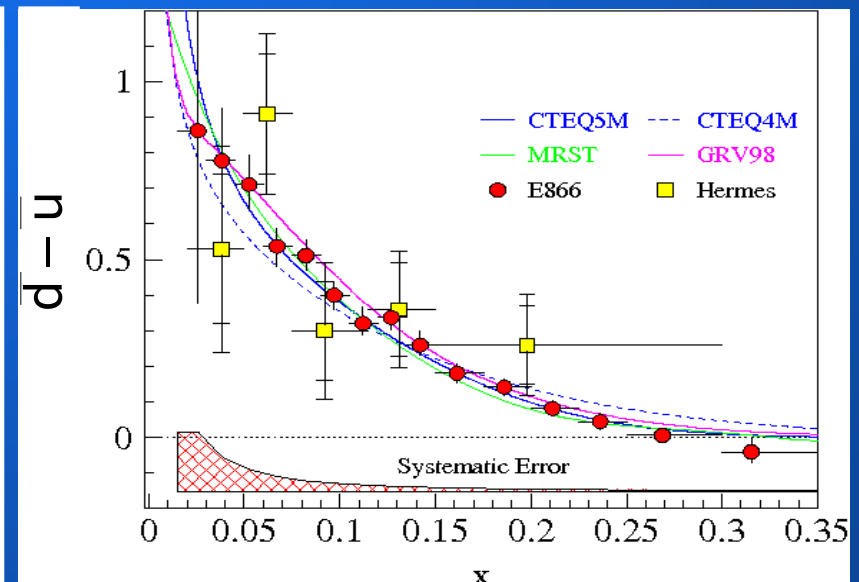
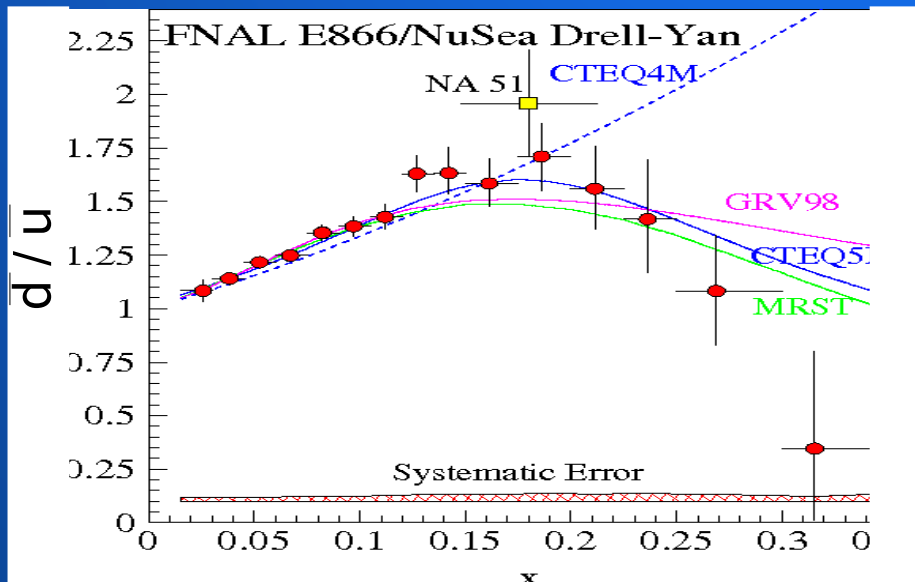
E.g.: NMC( $Q^2=4 \text{ GeV}^2$ ):  $I_G(0.004,0.8) = 0.236 \pm 0.008$

Extrapolation:  $I_G(0,1) = 0.258 \pm 0.017$

→ Significant **violation of Gottfried sum rule**

Sea flavor asymmetry  $\bar{u} \neq \bar{d}$ .  $I_G(0,1) < 1/3$ : excess of  $\bar{d}$  quarks over  $\bar{u}$  quarks.

$\bar{d}$  quark excess confirmed in Drell-Yan and semi-inclusive analysis:



# The Gottfried Integral

$$I_G(x_{min}, x_{max}) = \int_{x_{min}}^{x_{max}} (F_2^p(x) - F_2^n(x)) dx/x = \int_{x_{min}}^{x_{max}} 2(F_2^p - F_2^d) dx/x$$
$$= \int_{x_{min}}^{x_{max}} 2 F_2^p \left(1 - \frac{F_2^d}{F_2^p}\right) dx/x$$

Fit to  $F_2^p$

Fit to  $\sigma^d/\sigma^p$

Evaluation of the **measured** Gottfried Integral:

GD 08

Fit to  $\sigma^d/\sigma^p$

Evaluation of the **leading twist (LT)** Gottfried integral

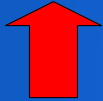
CTEQ6L

Fit to  $\sigma^d/\sigma^p$  (LT)

# Fits to $\sigma^d/\sigma^p$

$$\frac{\sigma^d}{\sigma^p} \simeq \frac{F_2^d}{F_2^p} \left( 1 - \frac{1-\epsilon}{(1+\bar{R}(x))(1+\epsilon\bar{R}(x))} \Delta R(x) \right)$$

Relation of cross-section ratio to  $F_2$ -ratio



$$\frac{F_2^d}{F_2^p} \simeq \frac{F_2^{d,LT}}{F_2^{p,LT}}(x, Q^2) \left( 1 + \frac{C^d(x) - C^p(x)}{Q^2} \right)$$

Higher twist effects



$$\frac{F_2^{d,LT}}{F_2^{p,LT}}(x, Q^2) \simeq b_1(x) + b_2(x) \ln Q^2$$

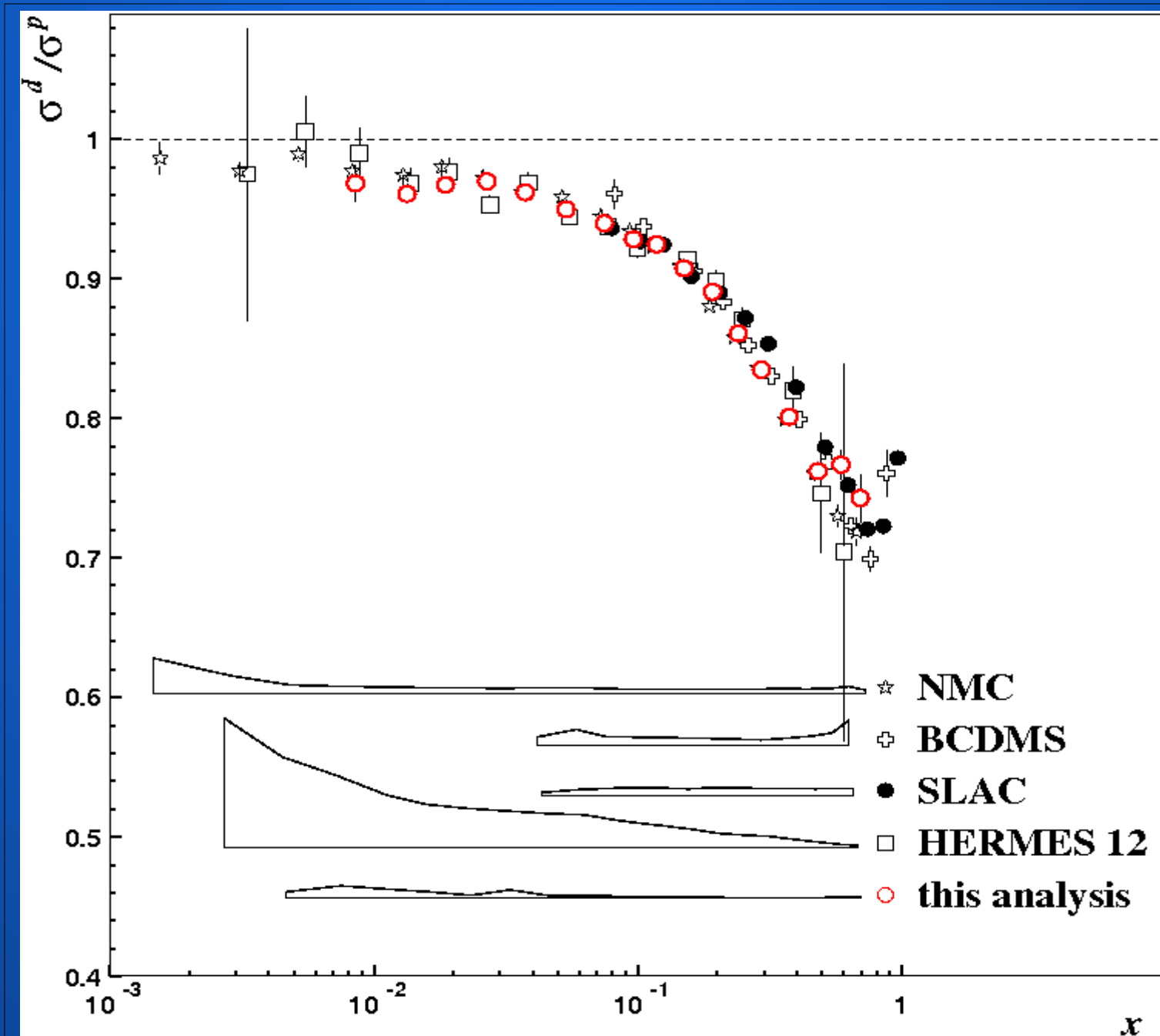
$Q^2$  evolution

## Parameterization

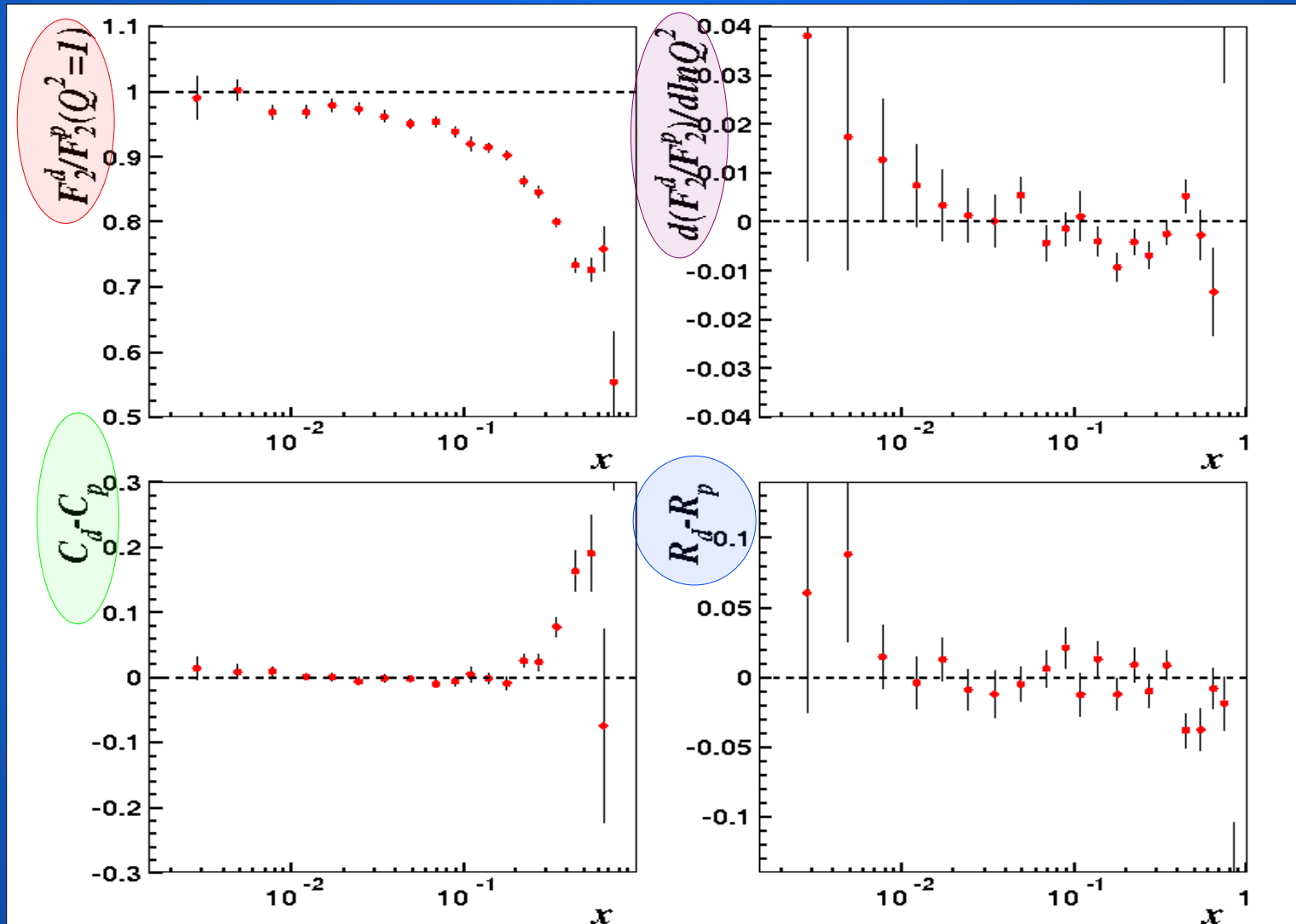
$$\frac{\sigma^d}{\sigma^p} \simeq \frac{F_2^d}{F_2^p} \left( b_1(x) + b_2(x) \ln Q^2 \right) \left( 1 + \frac{C^d(x) - C^p(x)}{Q^2} \right) \left( 1 - \frac{1-\epsilon}{(1+\bar{R}(x))(1+\epsilon\bar{R}(x))} \Delta R(x) \right)$$

- **4-parameter Fit** in each  $x$  bin  
based on world data from **NMC, SLAC, BCDMS, HERMES**

# World data on $\sigma^d/\sigma^p$

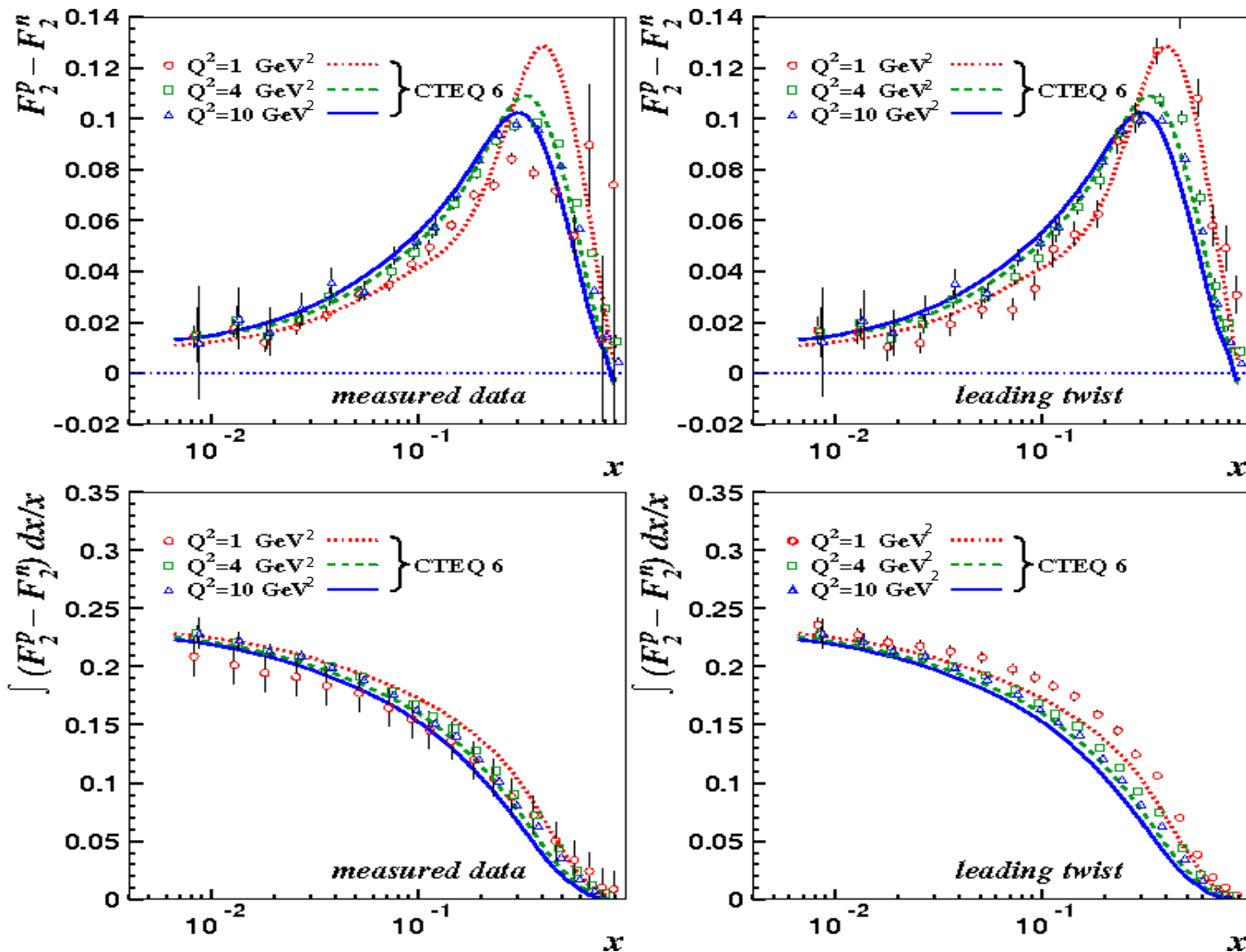


# 4 Parameters from Fit of $\sigma^d/\sigma^p$ to world data



- $F_2^d/F_2^p(Q^2=1)$  : approaching unity for small  $x$ .
- $d(F_2^d/F_2^p)/d\ln Q^2$  : tendency to negative slopes at high  $x$ .
- $C_d - C_p$  : significant only at  $x > 0.2$
- $R_d - R_p$  : Consistent with zero

# Evaluation of the Gottfried integral

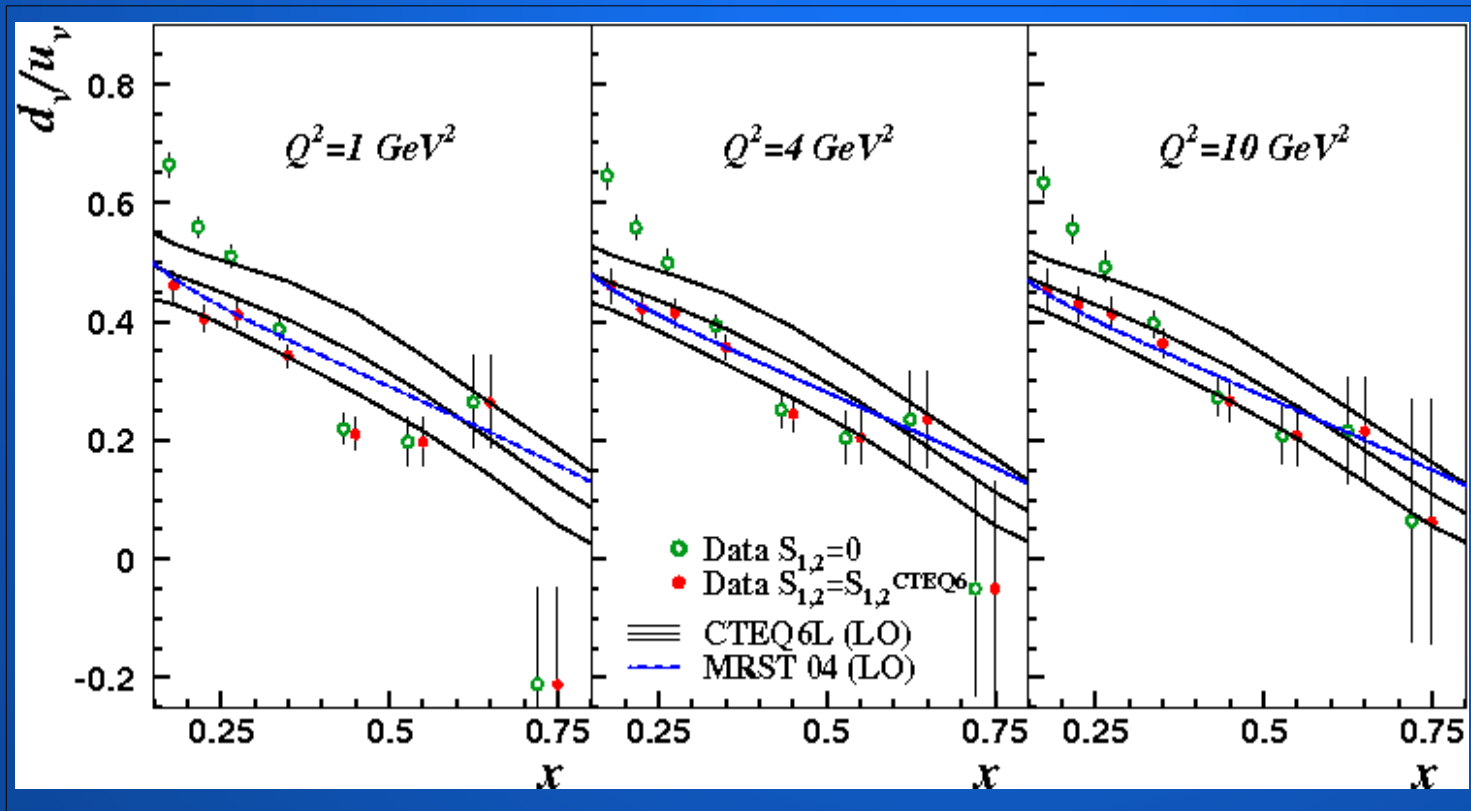


$Q^2$	$x$ - range	$I_G^{meas.}$	$I_G^{LT}$
1 $\text{GeV}^2$	0.006-0.9	$0.208 \pm 0.016$	$0.236 \pm 0.006$
4 $\text{GeV}^2$	0.006-0.9	$0.228 \pm 0.006$	$0.228 \pm 0.006$
10 $\text{GeV}^2$	0.006-0.9	$0.228 \pm 0.013$	$0.228 \pm 0.012$

# Extraction of $d_v/u_v$

Extraction of  $d_v/u_v$

$$\frac{F_2^d}{F_2^p} = \frac{1}{2} \left( 1 + \frac{F_2^n}{F_2^p} \right) \simeq \frac{1}{2} \left( 1 + \frac{4 \frac{d_v}{u_v} + 1 + S_1}{4 + \frac{d_v}{u_v} + S_2} \right) \stackrel{S_{1,2}=0}{\simeq} \frac{5}{2} \cdot \frac{1 + \frac{d_v}{u_v}}{4 + \frac{d_v}{u_v}}$$



$$S_1 = \frac{2}{u_v} (u_s + 4d_s + s_s)$$

$$S_2 = \frac{2}{u_v} (4u_s + d_s + s_s)$$

- $S_1$  and  $S_2$  taken from CTEQ6L
- Impact of  $S_1$  and  $S_2$  negligible at  $x > 0.35$

- Comparison of  $d_v/u_v$  with CTEQ6L (LO) result reveals compatibility.



# Summary

- First measurement of  $F_2^p$  and  $F_2^d$  at Hermes.
- Fit of the proton DIS cross section based on the ALLM functional form
  - Larger data set, 2821 data points, incl. Hermes
  - Self-consistent with respect to R
  - Normalization uncertainties taken into account
  - Covariance matrix provided
- Fit of the cross section ratio  $\sigma^d/\sigma^p$ 
  - Extraction of the Gottfried integral
  - Compatibility with the NMC result
  - Indicates violation of Gottfried sum rule
  - No indication for  $Q^2$  dependence found