



highlights from HERMES

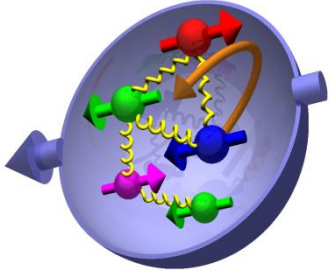
-- the nucleon structure: spin & 3D imaging --

- polarised deep-inelastic lepton-nucleon scattering
- where is the spin of the nucleon ?
- towards a 3D imaging



the mission

HERA MEAsurement of Spin



$$\frac{1}{2} = J_q + J_g$$

$$= \frac{1}{2} \Delta\Sigma + L_q + \Delta g + L_g$$

$$\Delta\Sigma = \Delta u_v + \Delta d_v + \Delta q_s$$

first

measurements:

$$\Delta\Sigma \approx 0.05$$

spin puzzle

EMC @CERN [1988]

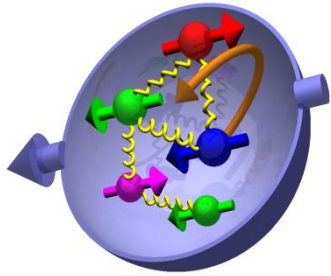
QPM: $\Delta\Sigma = 1$

relativistic
QPM: $\Delta\Sigma \approx 0.7$



the mission

HERA MEAsurement of Spin



$$\frac{1}{2} = J_q + J_g = \frac{1}{2} \Delta\Sigma + L_q + \Delta g + L_g$$

spin puzzle

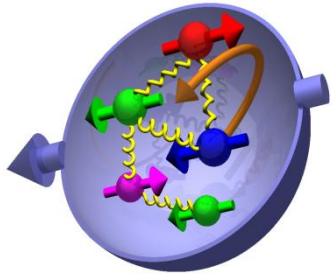
□ hunting the orbital angular momentum

→ *towards a complete 3D description of the nucleon:
beyond collinear approximation*



the mission

HERA MEAsurement of Spin

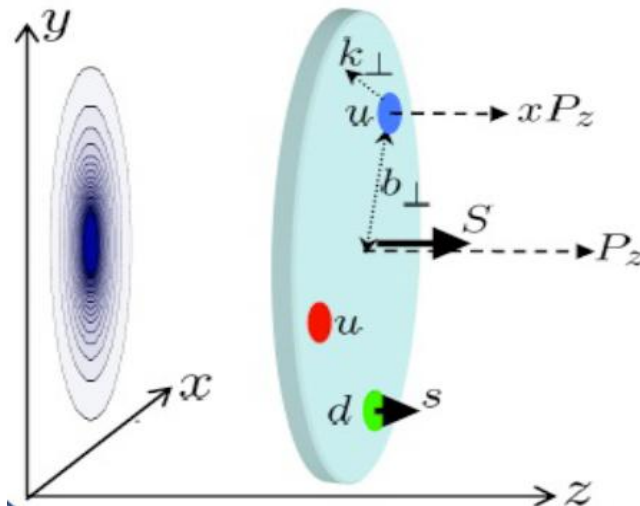


$$\frac{1}{2} = J_q + J_g = \frac{1}{2} \Delta\Sigma + L_q + \Delta g + L_g$$

spin puzzle

□ hunting the orbital angular momentum

→ towards a complete 3D description of the nucleon:
beyond collinear approximation



Wigner 'mother' distribution

$$W^{\vec{s}}(x, k_{\perp}, b_{\perp}, \vec{S})$$

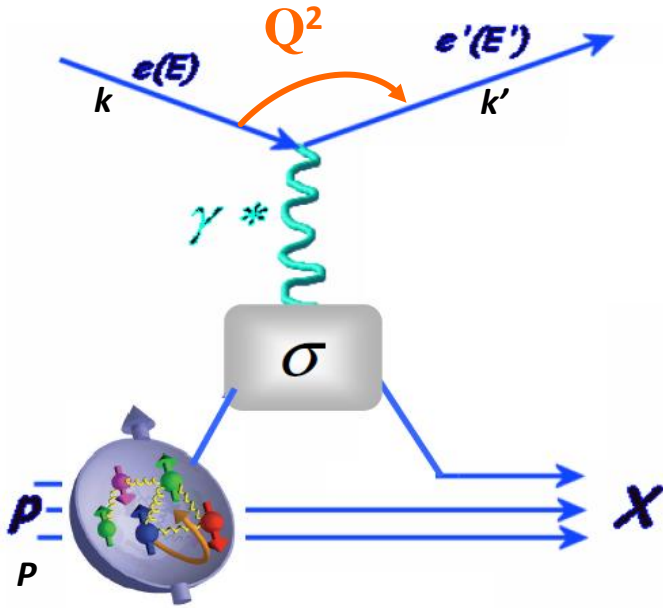
probability of finding a quark
with certain spin projection,
position and momentum

[plot: courtesy P. Haegler]

[X. Ji, PRL 2003; A. Belitsky, X. Ji, F. Yuan, PRD 2004]

[Meissner, Metz, Schlegel, JHEP 0908:056, 2009]

the tool: deep inelastic scattering



$$Q^2 = -q^2 = (k - k')^2 \quad \text{(4-momentum)}^2 \text{ of virtual photon}$$

$$\lambda \sim 1/Q^2$$

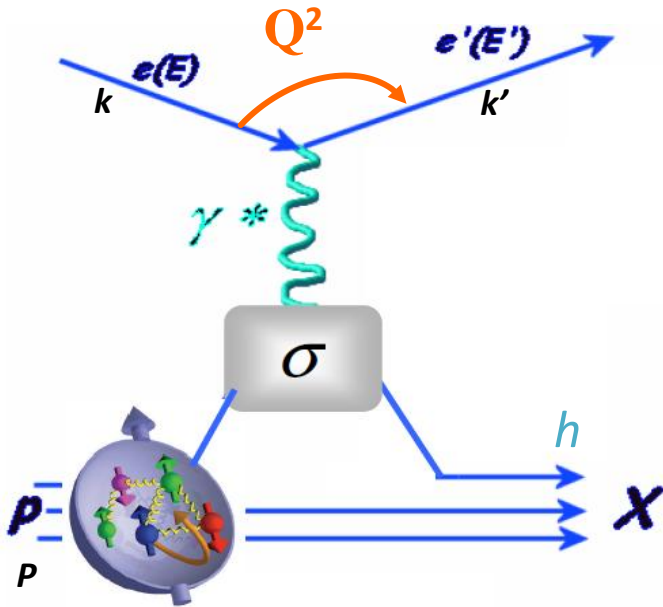
$$x = \frac{Q^2}{2P \cdot q}, \quad x \in [0,1] \quad \text{fraction of proton momentum carried by the struck parton}$$

pQCD factorisation:

$$\sigma_{DIS} \propto \sum_f \hat{\sigma}_{part} \otimes pdf(x)$$

parametrise the structure of nucleon

the tool: deep inelastic scattering



$$Q^2 = -q^2 = (k - k')^2 \quad \text{(4-momentum)}^2 \text{ of virtual photon}$$

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$$x = \frac{Q^2}{2P \cdot q}, \quad x \in [0, 1] \quad \text{fraction of proton momentum carried by the struck parton}$$

$$z = \frac{P \cdot P_h}{P \cdot q}, \quad z \in [0, 1] \quad \text{energy fraction carried by produced hadron}$$

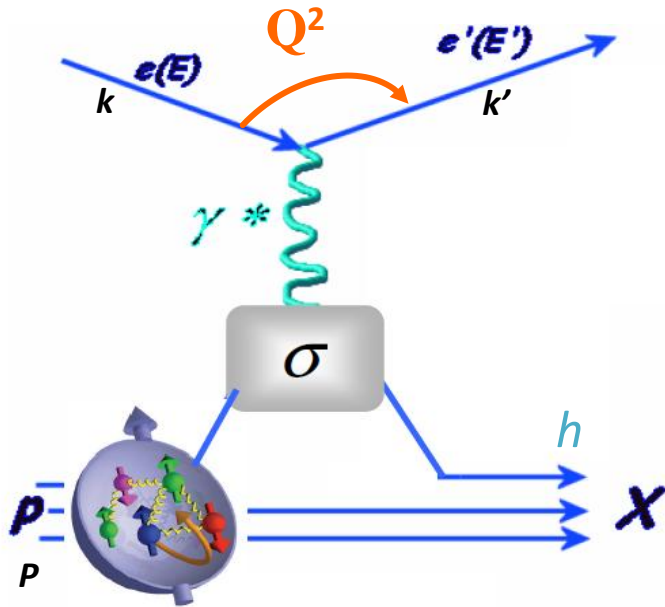
pQCD factorisation:

$$\sigma_{DIS} \propto \sum_f \hat{\sigma}_{part} \otimes \boxed{pdf(x)} \otimes \boxed{frag^{q,g \rightarrow h}(z)}$$

parametrise the
structure of nucleon

parametrise fragmentation of
parton in a hadron of type h

the tool: deep inelastic scattering



$$Q^2 = -q^2 = (k - k')^2 \quad \text{(4-momentum)}^2 \text{ of virtual photon}$$

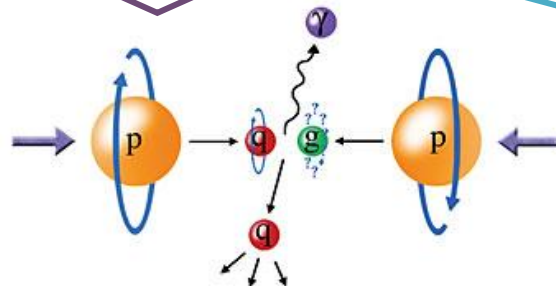
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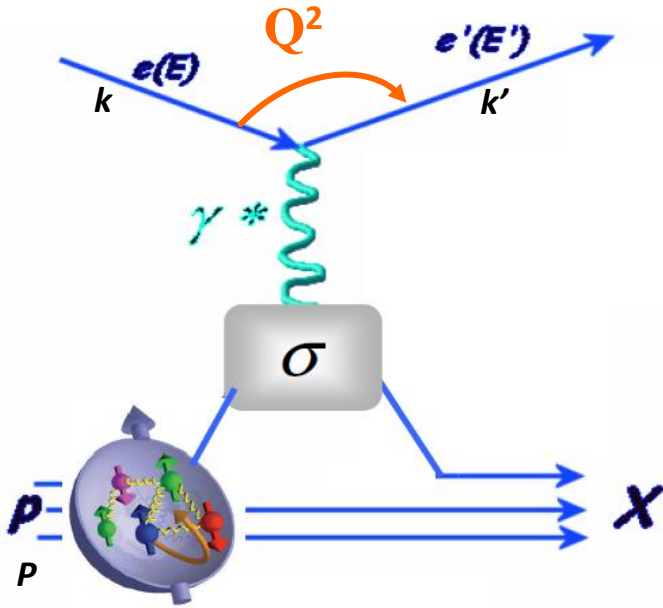
pQCD factorisation:

$$\sigma_{DIS} \propto \sum_f \hat{\sigma}_{part} \otimes pdf(x) \otimes frag^{q,g \rightarrow h}(z)$$



universal, same functions in, e.g., hadron reactions, DY, e+e-, ...

the tool: deep inelastic scattering



$$Q^2 = -q^2 = (k - k')^2 \quad \text{(4-momentum)^2 of virtual photon}$$

$$\lambda \sim 1/Q^2$$

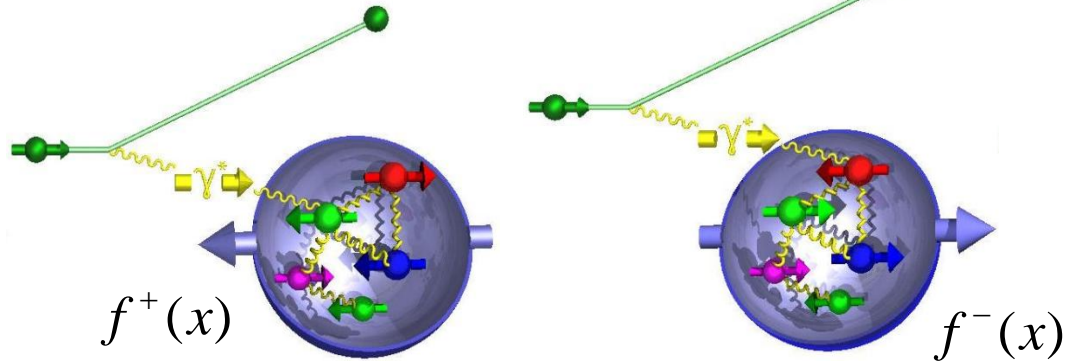
$$x = \frac{Q^2}{2P \cdot q}, \quad x \in [0, 1] \quad \text{fraction of proton momentum carried by the struck parton}$$



$$\sigma_{DIS} \propto \sum_f \hat{\sigma}_{part} \otimes pdf(x) \Rightarrow \Delta f(x) = f^+(x) - f^-(x)$$

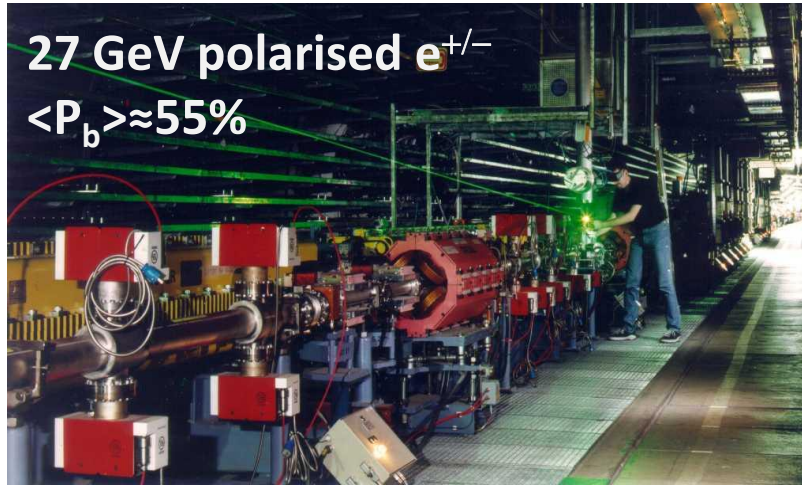
→ helicity distribution

... probability to find a quark or gluon with momentum x and spin parallel to the proton spin

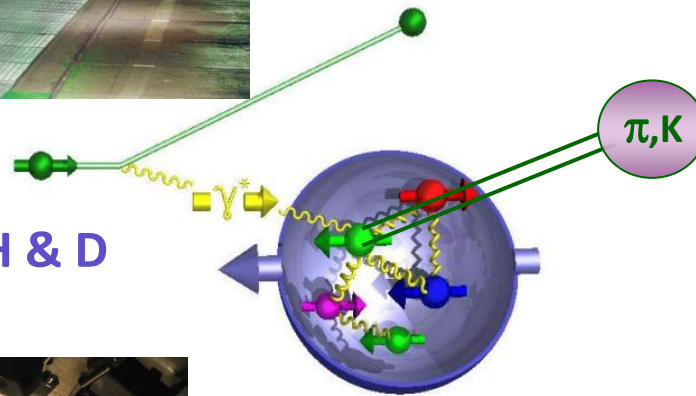
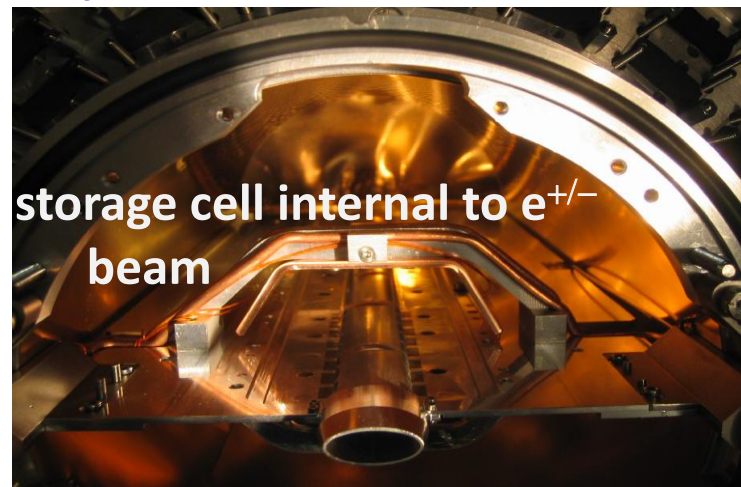


prerequisites

@HERA: 1995-2007



pure nuclear-polarised H & D
 $\langle P_t \rangle \approx 80\%$

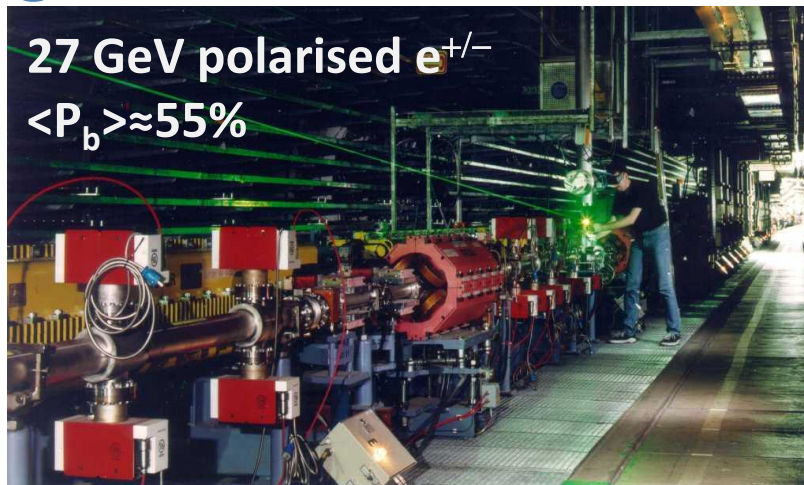




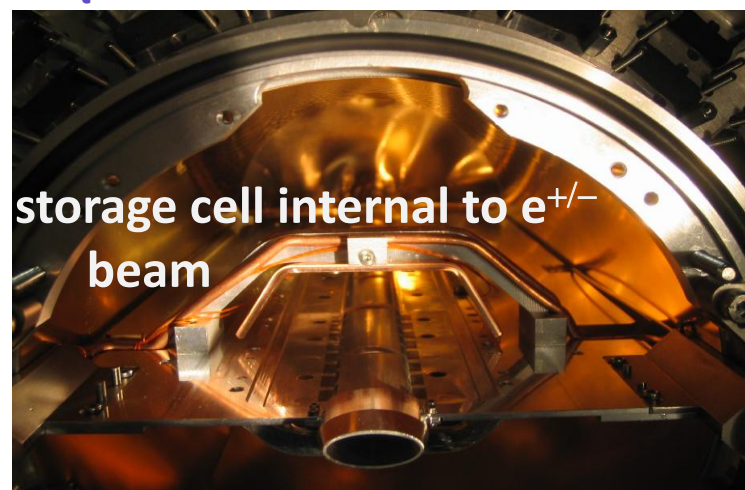
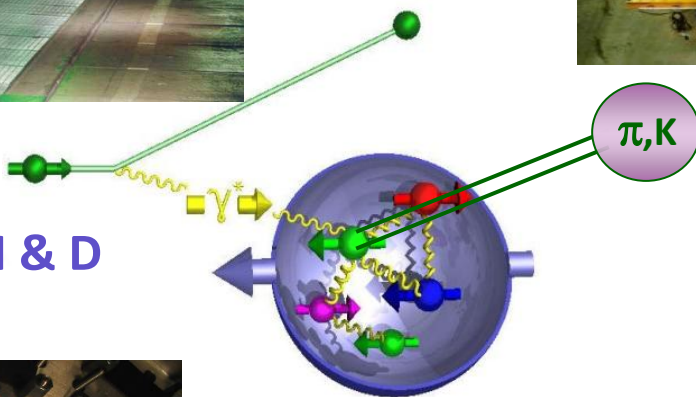
prerequisites

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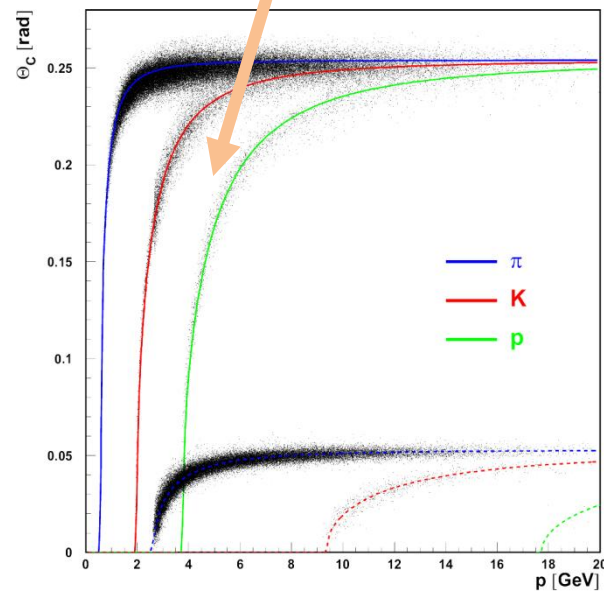
27 GeV polarised $e^{+/-}$
 $\langle P_b \rangle \approx 55\%$



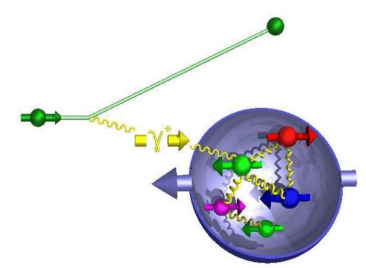
pure nuclear-polarised H & D
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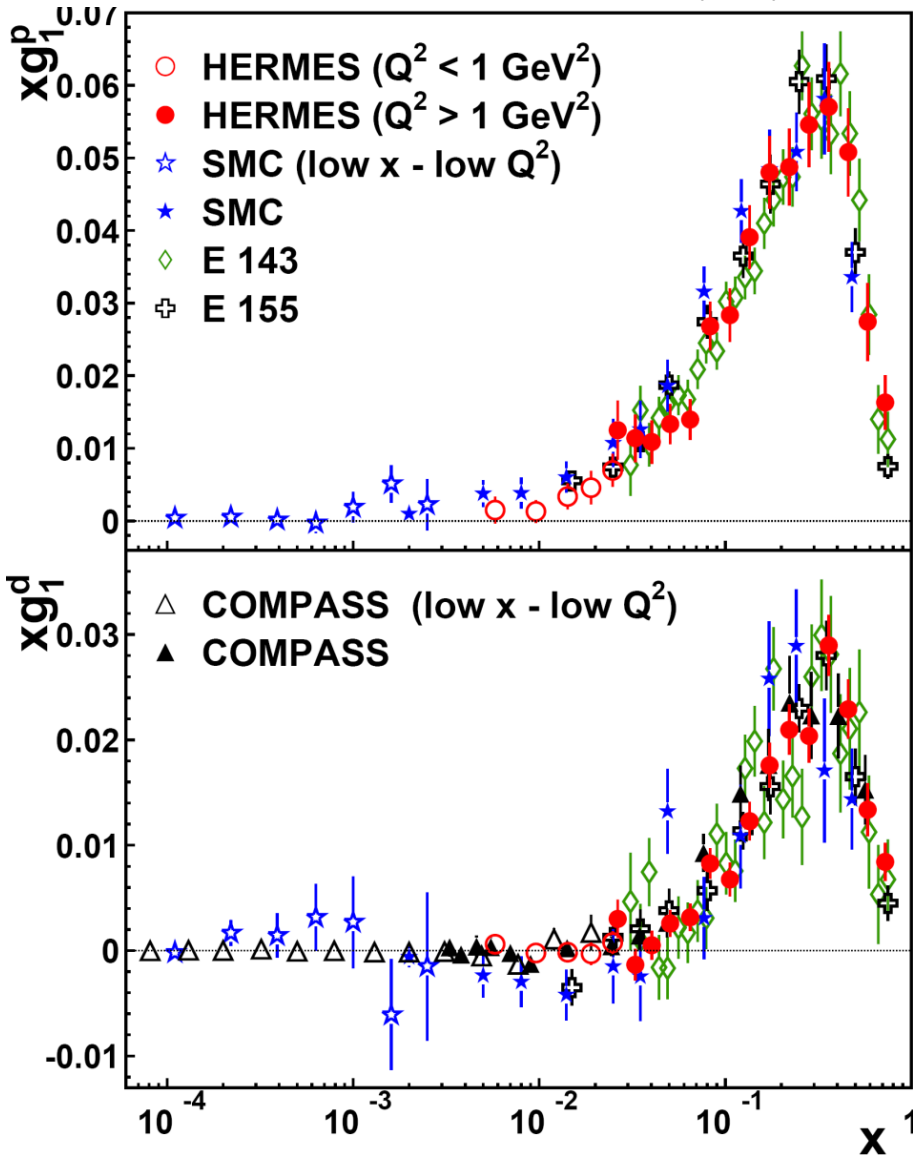
storage cell internal to $e^{+/-}$
beam



dual RICH: $p / K / p$ separation over
whole momentum range



[PRD75(2007), 012007]

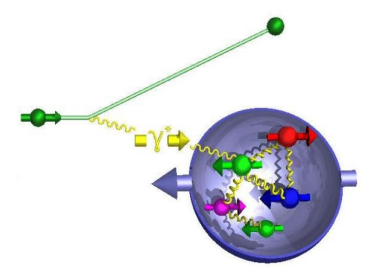


polarised structure function:

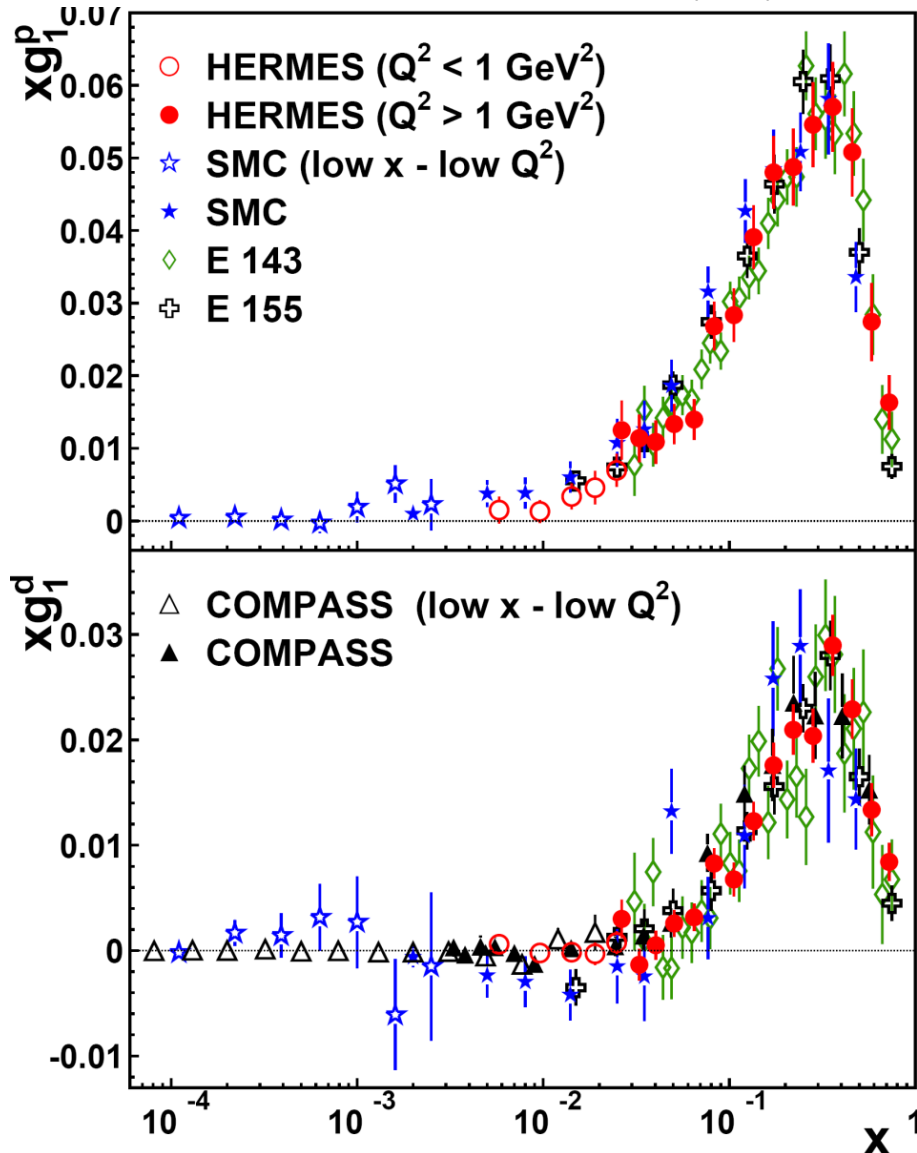
$$\sigma^{\Rightarrow} - \sigma^{\Leftarrow} \propto g_1(x)$$

$$g_1(x) \propto \frac{1}{2} \sum_q e_q^2 (\Delta q(x) + \Delta \bar{q}(x))$$

... flavour summed contribution of quarks to nucleon spin
 (...once integrated over all x ...)



PRD75(2007), 012007]



polarised structure function:

$$\sigma^{\Rightarrow} - \sigma^{\Leftarrow} \propto g_1(x)$$

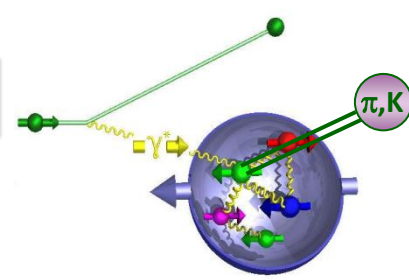
$$g_1(x) \propto \frac{1}{2} \sum_q e_q^2 (\Delta q(x) + \Delta \bar{q}(x))$$

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values from recent *NLO* analyses of world data:

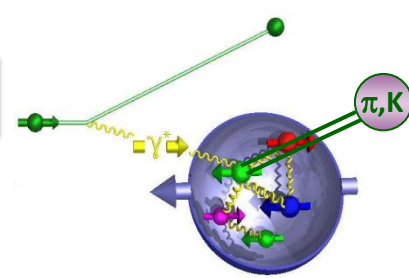
$$\int dx g_1(x) \rightarrow \Delta\Sigma = 0.2 \div 0.35$$

inclusive DIS & beyond

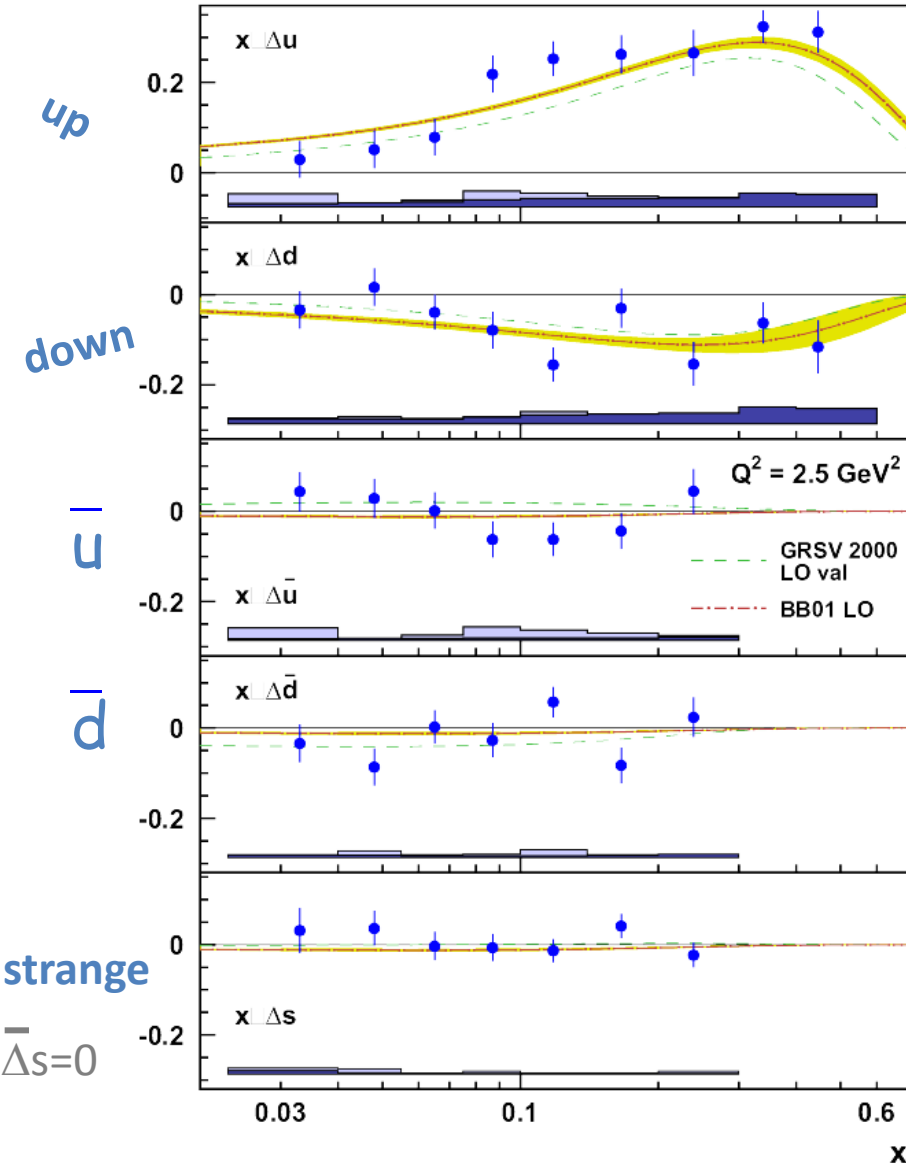


*what about the individual quark contributions
&
gluons ?*

inclusive DIS & beyond



[PRL92(2004),012004;PRD(2005)012003]



quark polarisations from
flavour tagging

in short:

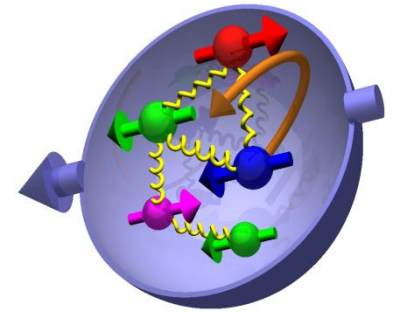
$$\Delta u(x) > 0 \quad \text{and large}$$

$$\Delta d(x) < 0 \quad \text{and smaller}$$

$$\Delta s(x) \approx 0$$

→ first *direct* 5-flavour separation
of polarised pdfs

the spin budget



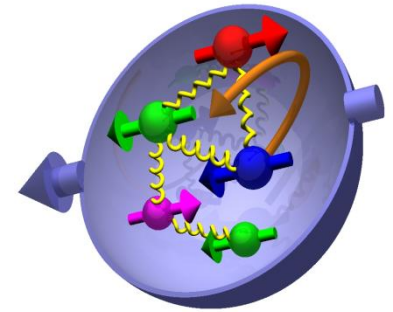
- contribution of quarks 25-35% :

$$\frac{1}{2} \hbar \uparrow + \frac{1}{2} \Delta \Sigma_d \uparrow \downarrow + \frac{1}{2} \Delta \Sigma_s \uparrow$$

The diagram illustrates the spin budget for quarks. It features three main components: 1) A large orange arrow pointing upwards, labeled with the fraction $\frac{1}{2}$ and the symbol \hbar . 2) A smaller blue arrow pointing upwards, labeled with the fraction $\frac{1}{2}$ and the symbol $\Delta \Sigma_d$. 3) A green arrow pointing downwards, which is part of the $\frac{1}{2} \Delta \Sigma_d$ term. To the right of these arrows is a small icon of a graduation cap, followed by the fraction $\frac{1}{2}$ and the symbol $\Delta \Sigma_s$.

- *gluon polarisation* surprisingly *small* in measured range ($0.05 < x_g < 0.2$)
significant contributions of gluons and/or sea quarks @low x ?

the spin budget



- contribution of quarks 25-35% :

$$\frac{1}{2} \hbar \uparrow \quad \frac{1}{2} \Delta \Sigma_d \uparrow \downarrow \quad \frac{1}{2} \Delta \Sigma_s$$

The diagram illustrates the spin budget for quarks. It features three main components: 1) A large orange arrow pointing upwards, labeled with $\frac{1}{2} \hbar$, representing the total spin of the quarks. 2) A smaller blue arrow pointing upwards and a green arrow pointing downwards, both labeled with $\frac{1}{2} \Delta \Sigma_d$, representing the difference in spin contributions from different quark flavors. 3) A small grey arrow pointing upwards, labeled with $\frac{1}{2} \Delta \Sigma_s$, representing the spin contribution from sea quarks.

- *gluon polarisation* surprisingly *small* in measured range ($0.05 < x_g < 0.2$)
significant contributions of gluons and/or sea quarks @low x ?
- *what about the orbital angular momentum ?*

→ **new concepts: GPDs & TMDs**

Generalised Parton Distributions

Transverse Momentum Dependent functions



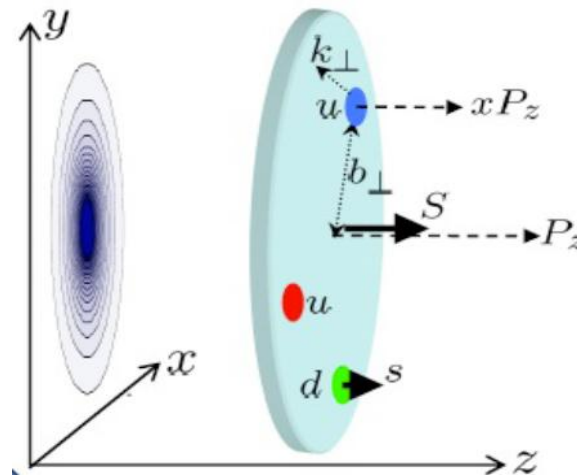
towards nucleon
tomography

nucleon tomography



Wigner 'mother' distribution

$$W^{\vec{s}}(x, k_{\perp}, b_{\perp}, \vec{S})$$



cannot be measured... but its *projections*
in coordinate or momentum space

nucleon tomography



$$W^{\vec{s}}(x, k_{\perp}, b_{\perp}, \vec{S})$$

cannot be measured... but its *projections* in coordinate or momentum space

transverse
coordinate space

GPDs

[*generalised parton distributions*]

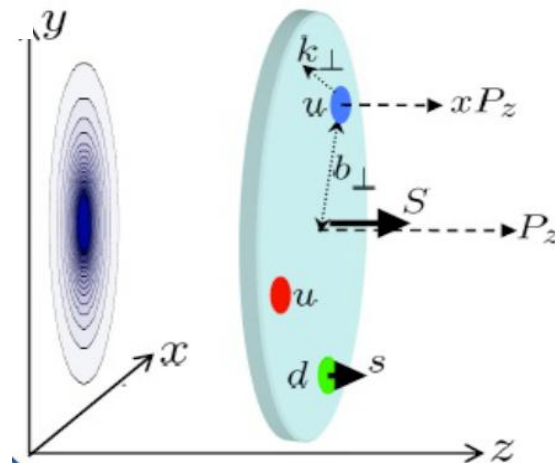
transverse
momentum space

TMDs

[*transverse momentum dependent PDFs/FFs*]

correlation between
longitudinal momentum
&
transverse position

correlation between
spin
&
transverse momentum



nucleon tomography



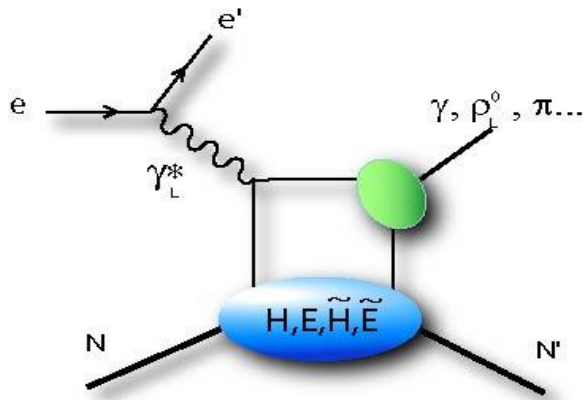
$$W^{\vec{s}}(x, k_{\perp}, b_{\perp}, \vec{S})$$

cannot be measured... but its *projections* in coordinate or momentum space

transverse
coordinate space

GPDs

[generalised parton distributions]

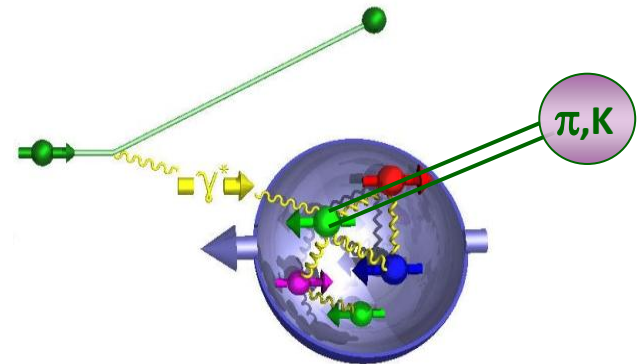


exclusive reactions

transverse
momentum space

TMDs

[transverse momentum dependent PDFs/FFs]



fully differential semi-inclusive DIS

[... preferably with polarised beam and/or target ...]

nucleon tomography



$$W^{\vec{s}}(x, k_{\perp}, b_{\perp}, \vec{S})$$

cannot be measured... but its *projections* in coordinate or momentum space

transverse
coordinate space

GPDs

[generalised parton distributions]

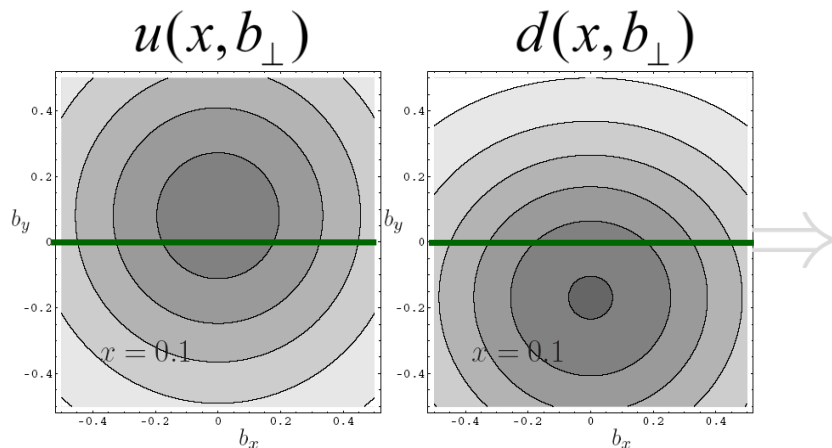
transverse
momentum space

TMDs

[transverse momentum dependent PDFs/FFs]

model calculations for a *transversely* polarised nucleon

GPD E



[model calculation by M. Burkardt]

nucleon tomography



$$W^{\vec{s}}(x, k_{\perp}, b_{\perp}, \vec{S})$$

cannot be measured... but its *projections* in coordinate or momentum space

transverse
coordinate space

GPDs

[generalised parton distributions]

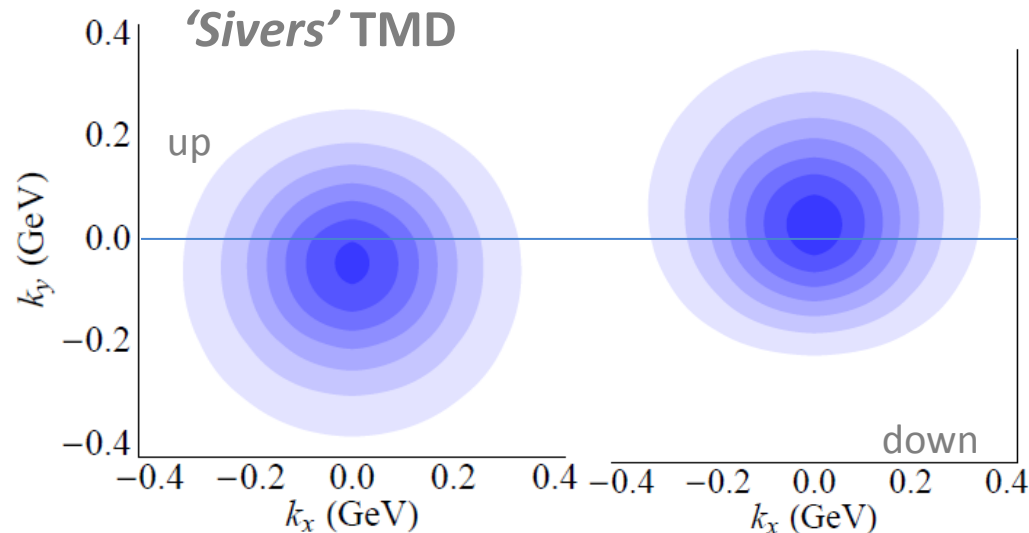
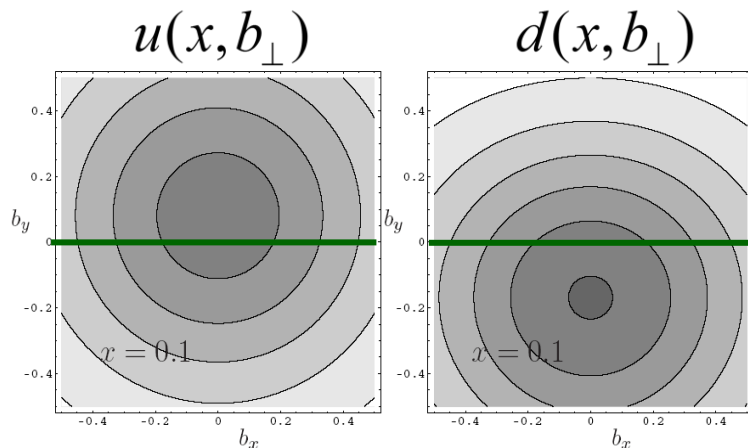
transverse
momentum space

TMDs

[transverse momentum dependent PDFs/FFs]

model calculations for a *transversely* polarised nucleon

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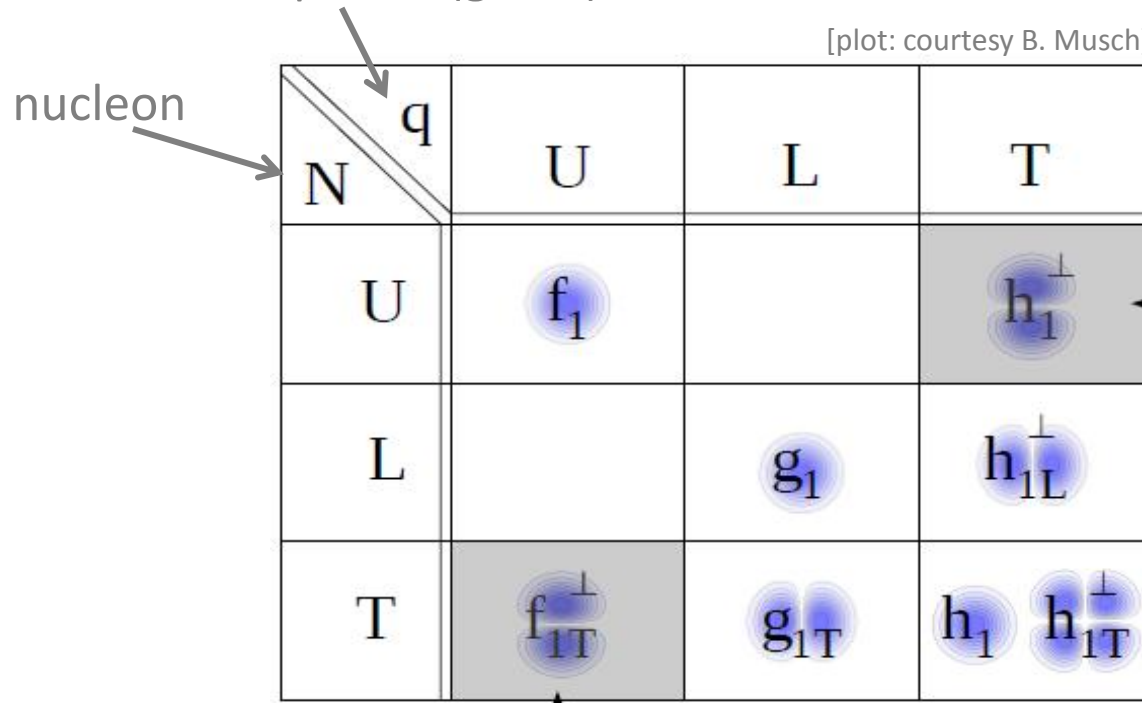
[model calculation by B. Pasquini, F. Yuan]

nucleon tomography

classification of TMDs



polarization of quark / (gluon)

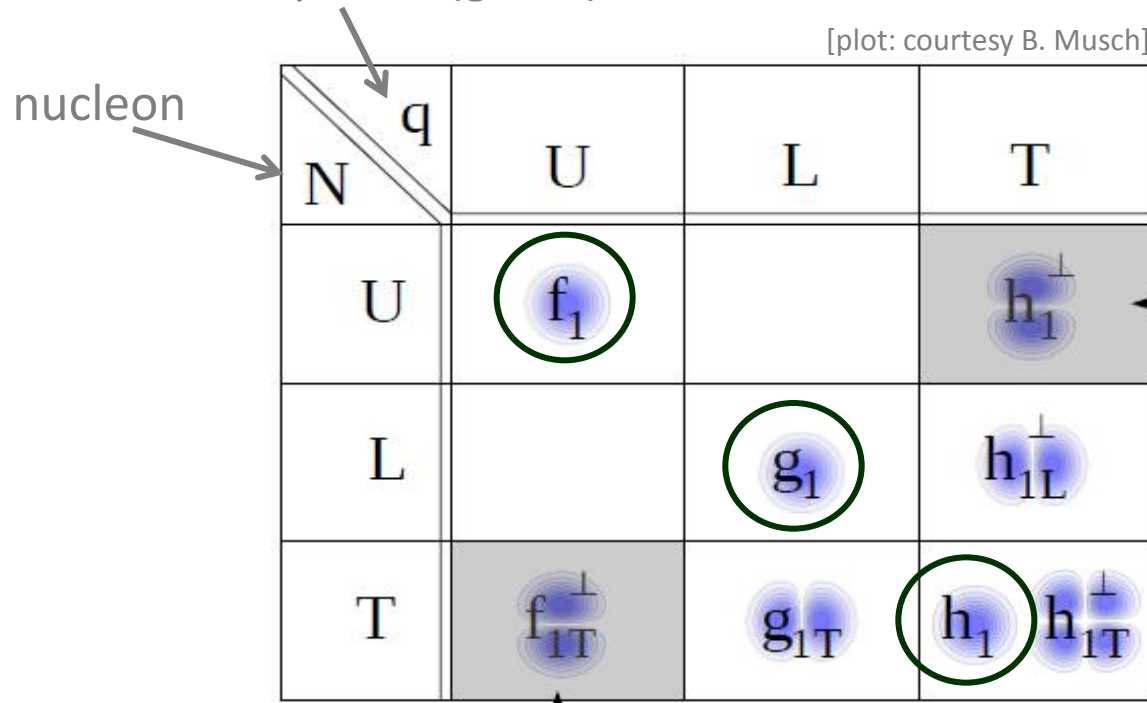


nucleon tomography

classification of TMDs



polarization of quark / (gluon)



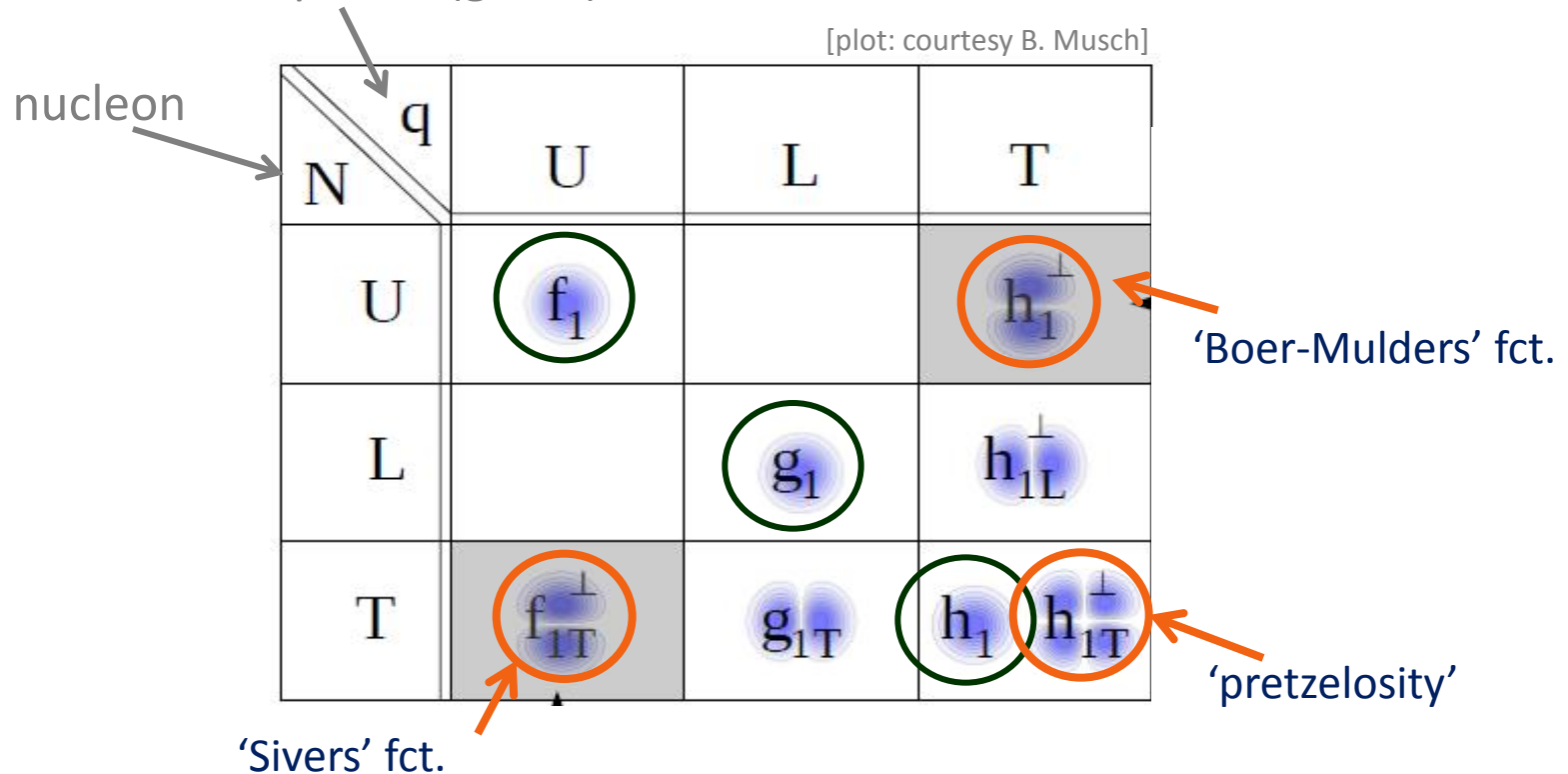
survive integration over intrinsic transverse momenta: *collinear approximation*

nucleon tomography



classification of TMDs

polarization of quark / (gluon)



require interference of nucleon wave fct.s with
different units **OAM** \rightarrow spin-orbit correlations

nucleon tomography

classification of TMDs



polarization of quark / (gluon)

[plot: courtesy B. Musch]

nucleon



	q	U	L	T
N				
U		f_1		h_1^\perp
L			g_1	h_{1L}^\perp
T		f_{1T}^\perp	g_{1T}	h_1 h_{1T}^\perp

all functions or related observables measured: select two TMDs

'Boer-Mulders' fct.

'Sivers' fct.

'pretzelosity'

require interference of nucleon wave fct.s with different units **OAM** → spin-orbit correlations

nucleon tomography

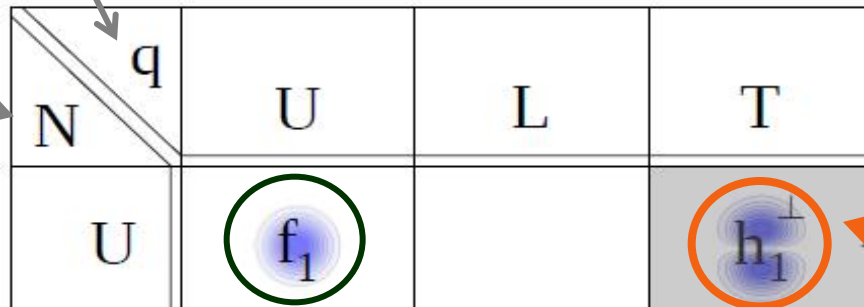


classification of TMDs

polarization of quark / (gluon)

[plot: courtesy B. Musch]

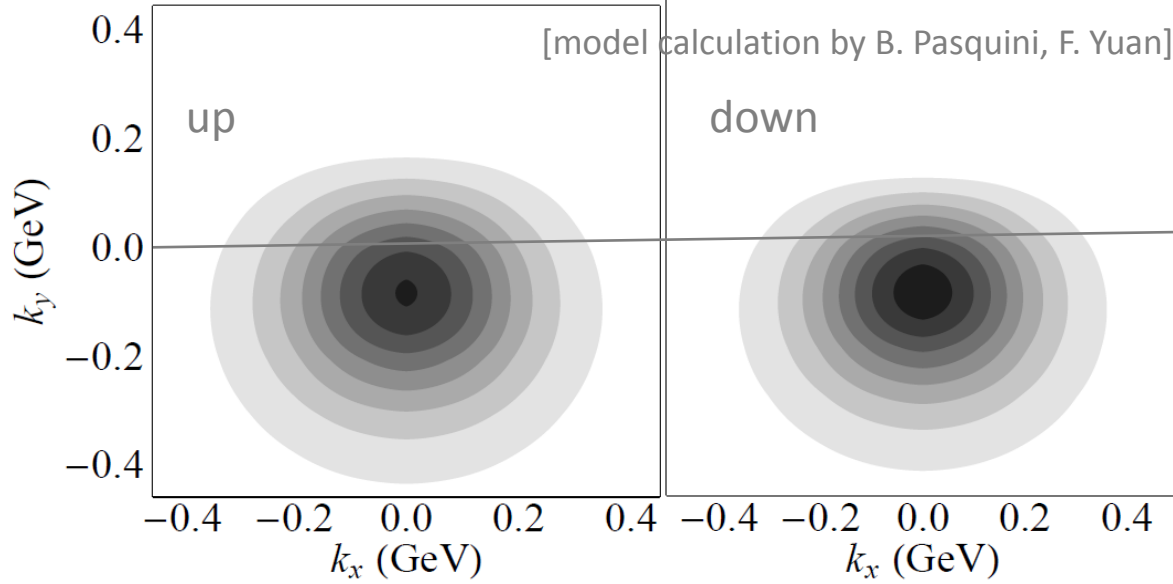
nucleon



'Boer-Mulders' fct.

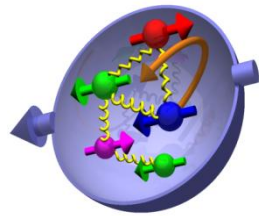
*distortion of distribution even for unpol protons !
→ interpretation of HIC*

'pretzelosity'



nucleon wave fct.s with n-orbit correlation

relation to OAM



GPDs

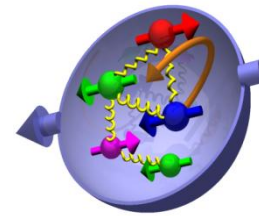
TMDs

N \ q	U	L	T
U	f_1		h_1^\perp ← $\Delta L=1$ 'Boer-Mulders' fct.
L		g_1	h_{1L}^\perp
T	f_{1T}^\perp ↗ $\Delta L=1$ 'Sivers' fct.	g_{1T}	h_1 h_{1T}^\perp ↘ $\Delta L=2$ 'pretzelosity'

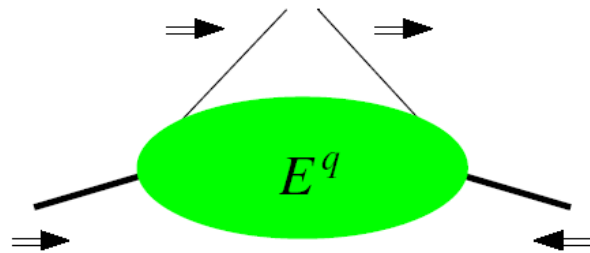
require interference of nucleon wave fct.s with different units OAM

→ spin-orbit correlation

relation to OAM



GPDS



proton helicity flipped but
quark helicity conserved

$E^q \neq 0$ requires OAM

$$J^q = \Delta\Sigma + L^q = \frac{1}{2} \int x dx H^q + E^q$$

[X. Ji, PRL(1997)]

TMDs

N \ q	U	L	T
U	f_1		h_1^\perp
L		g_1	h_{1L}^\perp
T	f_{1T}^\perp	g_{1T}	h_1 h_{1T}^\perp

$\Delta L=1$

'Boer-Mulders' fct.

$\Delta L=2$

'pretzelosity'

$\Delta L=1$

'Sivers' fct.

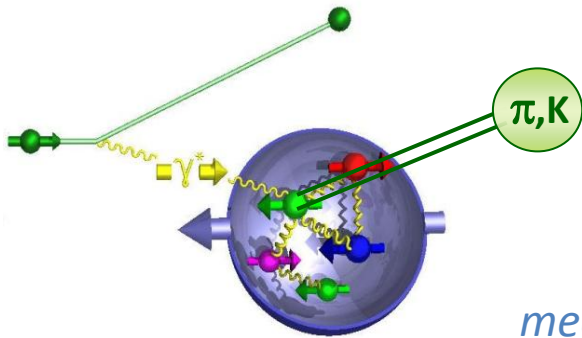
require interference of nucleon wave
fct.s with different units OAM

→ spin-orbit correlation

observables of TMD

N \ q	U	L	T
U	f_1		h_{1T}^\perp
L		g_1	h_{1L}^\perp
T	\tilde{h}_{1T}^\perp	g_{1T}	h_1, h_{1T}

most successfully probed in semi-inclusive DIS:



factorization for kinematic regime:

$$P_{hT} \cong k_\perp \cong \Lambda_{QCD} \ll Q^2$$

measure fully differential cross section:

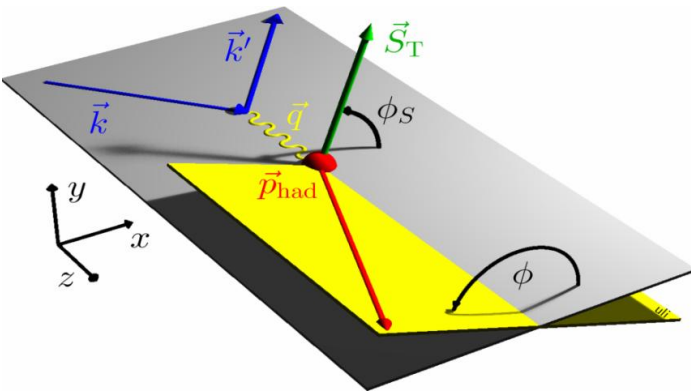
$$\frac{d\sigma}{dx_B dy d\phi_S dz_h d\phi_h dP_{hT}^2} \propto \left\{ F_{UU,T} + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} \right.$$

$$+ S_{\parallel} \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} + S_{\parallel} \lambda_\ell \sqrt{1 - \varepsilon^2} F_{LL}$$

$$+ |S_{\perp}| \left[\sin(\phi_h - \phi_S) F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} \right.$$

$$\left. + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} \right]$$

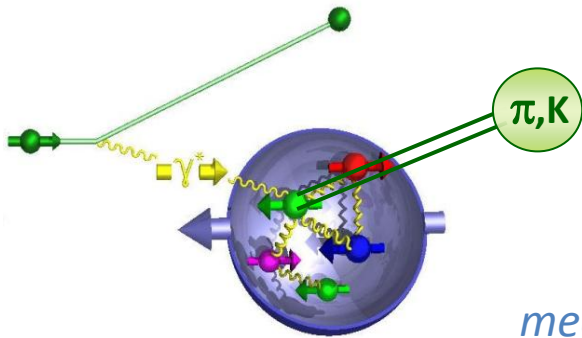
$$+ |S_{\perp}| \lambda_e \sqrt{1 - \varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \dots \left. \right\}.$$



observables of TMD

N \ q	U	L	T
U	f_1		h_{1T}^\perp
L		g_1	h_{1L}^\perp
T	h_{1T}^\perp	g_{1T}	h_1, h_{1T}^\perp

most successfully probed in semi-inclusive DIS:



factorization for kinematic regime:

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measure fully differential cross section:

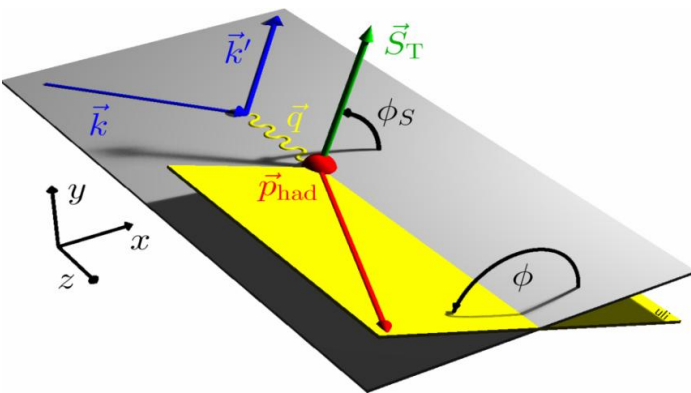
$$\frac{d\sigma}{dx_B dy d\phi_S dz_h d\phi_h dP_{hT}^2} \propto \left\{ F_{UU,T} + \varepsilon \cos(2\phi_h) F_{UU}^{\cos 2\phi_h} \right.$$

$$+ S_{\parallel} \varepsilon \sin(2\phi_h) F_{UL}^{\sin 2\phi_h} + S_{\parallel} \lambda_\ell \sqrt{1 - \varepsilon^2} F_{LL}$$

$$+ |S_{\perp}| \left[\sin(\phi_h - \phi_S) F_{UT,T}^{\sin(\phi_h - \phi_S)} + \varepsilon \sin(\phi_h + \phi_S) F_{UT}^{\sin(\phi_h + \phi_S)} \right.$$

$$\left. + \varepsilon \sin(3\phi_h - \phi_S) F_{UT}^{\sin(3\phi_h - \phi_S)} \right]$$

$$+ |S_{\perp}| \lambda_e \sqrt{1 - \varepsilon^2} \cos(\phi_h - \phi_S) F_{LT}^{\cos(\phi_h - \phi_S)} + \dots \left. \right\}.$$



$$F_{UT}^{\sin(\phi - \phi_S)} \prec \sum_q e_q^2 f_{1T}^{\perp q}(x, k_\perp) \otimes D_1^q(z, P_\perp)$$

↑ beam
 ↑ target
 polarisation

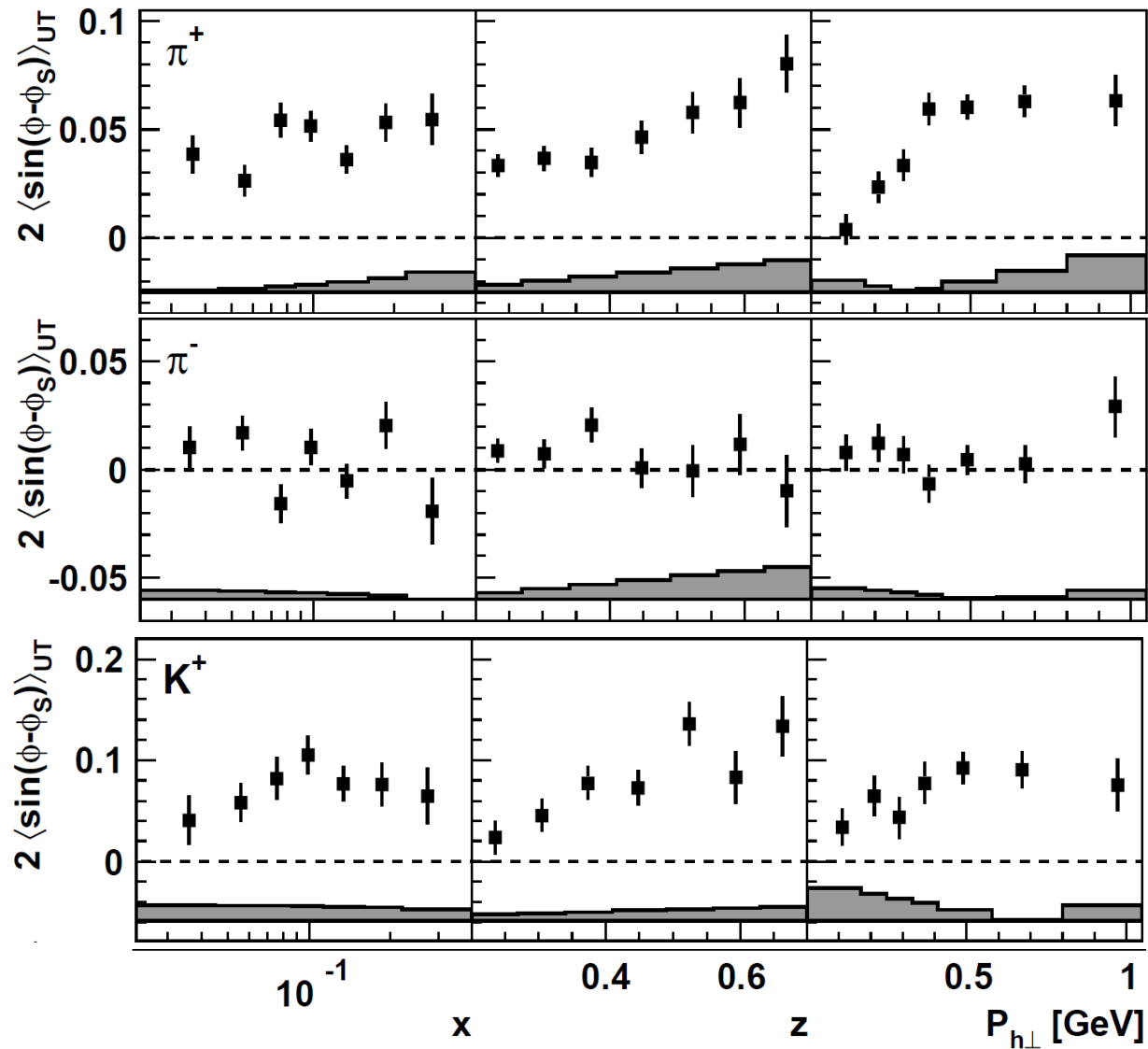


Sivers TMD

-- spin-orbit correlations & role of OAM --

N \ q	U	L	T
U	f_1		h_{1T}^+
L		g_1	h_{1T}^-
T	h_{1T}^+	g_{1T}	h_1, h_{1T}^+

[PRL103(2009)152002]



➤ first clear evidence for significant role of OAM and effects of spin-orbit correlations

➤ cancellation of u and d quark contributions

➤ surprisingly large signal for K^+ role of sea quarks ?

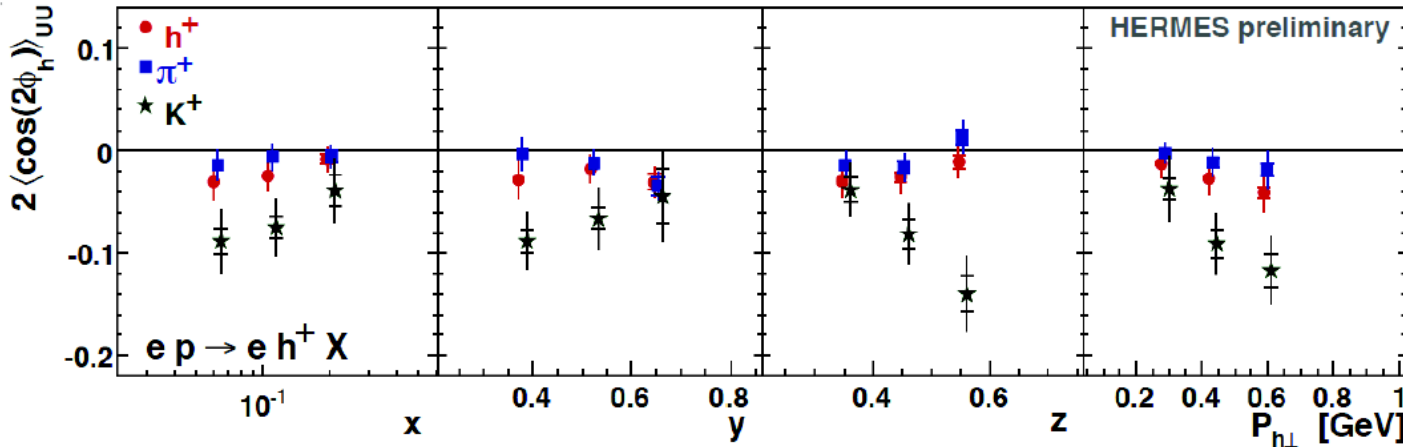


Boer-Mulders TMD

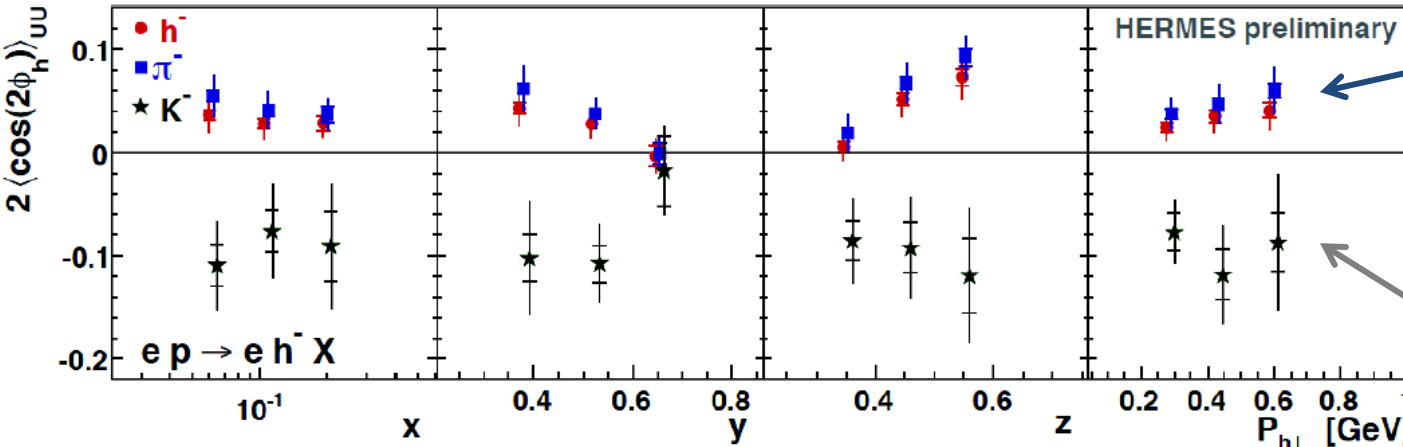
-- spin effects & spin-orbit correlations even in the unpolarised proton --

$N \backslash q$	U	L	T
U	f_1		h_1^\perp
L		g_1	h_{1L}
T	g_{1T}	g_{1T}	h_1 h_{1T}

fully differential 5D information available, here only projections shown



➤ intriguing pattern for different hadron types

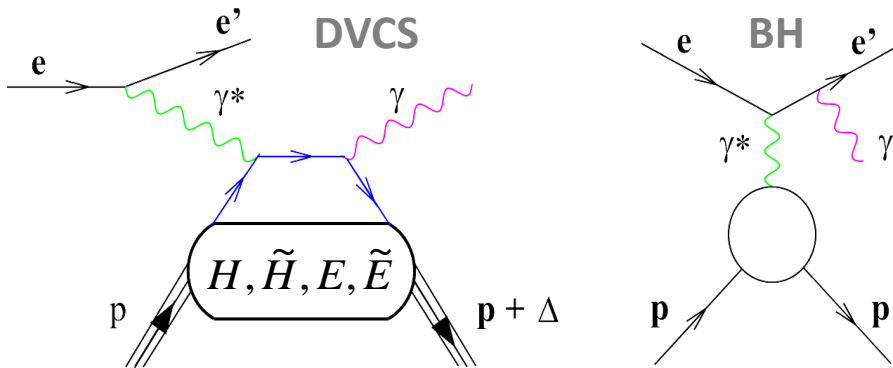


← pions

← kaons

observables of GPDs

golden channel : deeply virtual Compton scattering (DVCS)



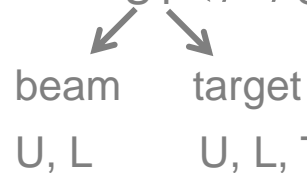
$$d\sigma \propto |\tau_{BH}|^2 + |\tau_{DVCS}|^2 + (\tau_{BH}^* \tau_{DVCS} + \tau_{DVCS}^* \tau_{BH})$$

→ linear in GPDs

isolate interference term:

- different beam charges: e^+e^- only @HERA

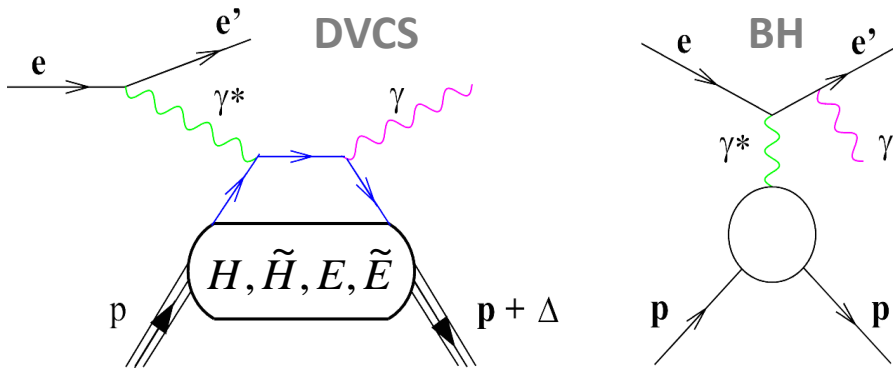
- polarisation observables: $\Delta\sigma_{UT}(\phi, \phi_S, \dots)$



Unpolarised, Longitudinally, Transversely polarised

observables of GPDs

golden channel : deeply virtual Compton scattering (DVCS)



$$d\sigma \propto |\tau_{BH}|^2 + |\tau_{DVCS}|^2 + (\tau_{BH}^* \tau_{DVCS} + \tau_{DVCS}^* \tau_{BH})$$

→ linear in GPDs

isolate interference term:

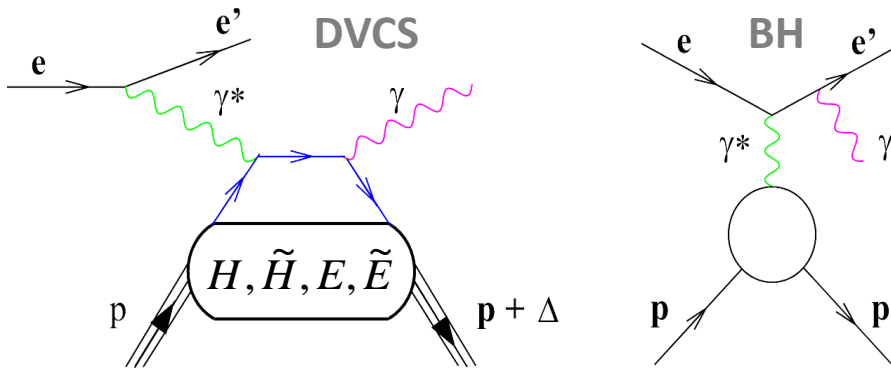
- different beam charges: e^+e^- only @HERA
- polarisation observables: $\Delta\sigma_{UT}(\phi, \phi_S, \dots)$
 - beam: U, L
 - target: U, L, T

$\Delta\sigma_C, \Delta\sigma_{LU}$	→ H_p, E_n
$\Delta\sigma_{UL}$	→ H, \tilde{H}
$\Delta\sigma_{UT}$	→ H, E

@kinematics of current fixed target exp.

observables of GPDs

golden channel : deeply virtual Compton scattering (DVCS)



$$d\sigma \propto |\tau_{\text{BH}}|^2 + |\tau_{\text{DVCS}}|^2 + (\tau_{\text{BH}}^* \tau_{\text{DVCS}} + \tau_{\text{DVCS}}^* \tau_{\text{BH}})$$

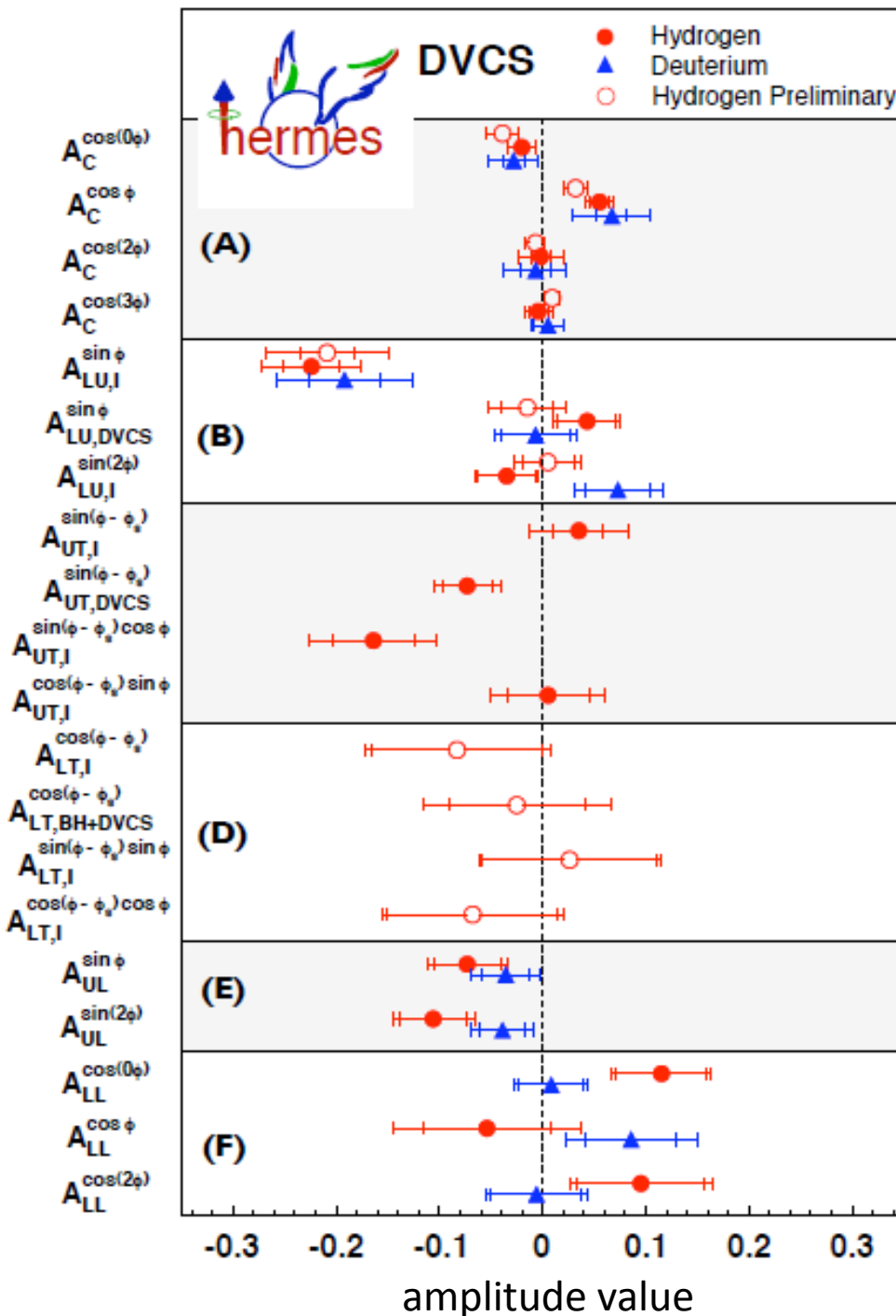
→ linear in GPDs

isolate interference term:

→ explore azimuthal dependence of cross section, e.g.:

$$\Delta\sigma_{\text{XY}} \propto \sum_{n=1}^3 c_{\text{unp},n}^{\text{I}} \cos(n\phi) + \lambda \sum_{n=1}^2 s_{\text{unp},n}^{\text{I}} \sin(n\phi)$$

... coefficients related to GPDs



unique data set

→ charge asymmetry

$$Re(H)$$

→ beam-spin asymmetry

$$Im(H)$$

→ transverse target spin asymmetry

$$Im(H-E)$$

→ transverse-target double-spin

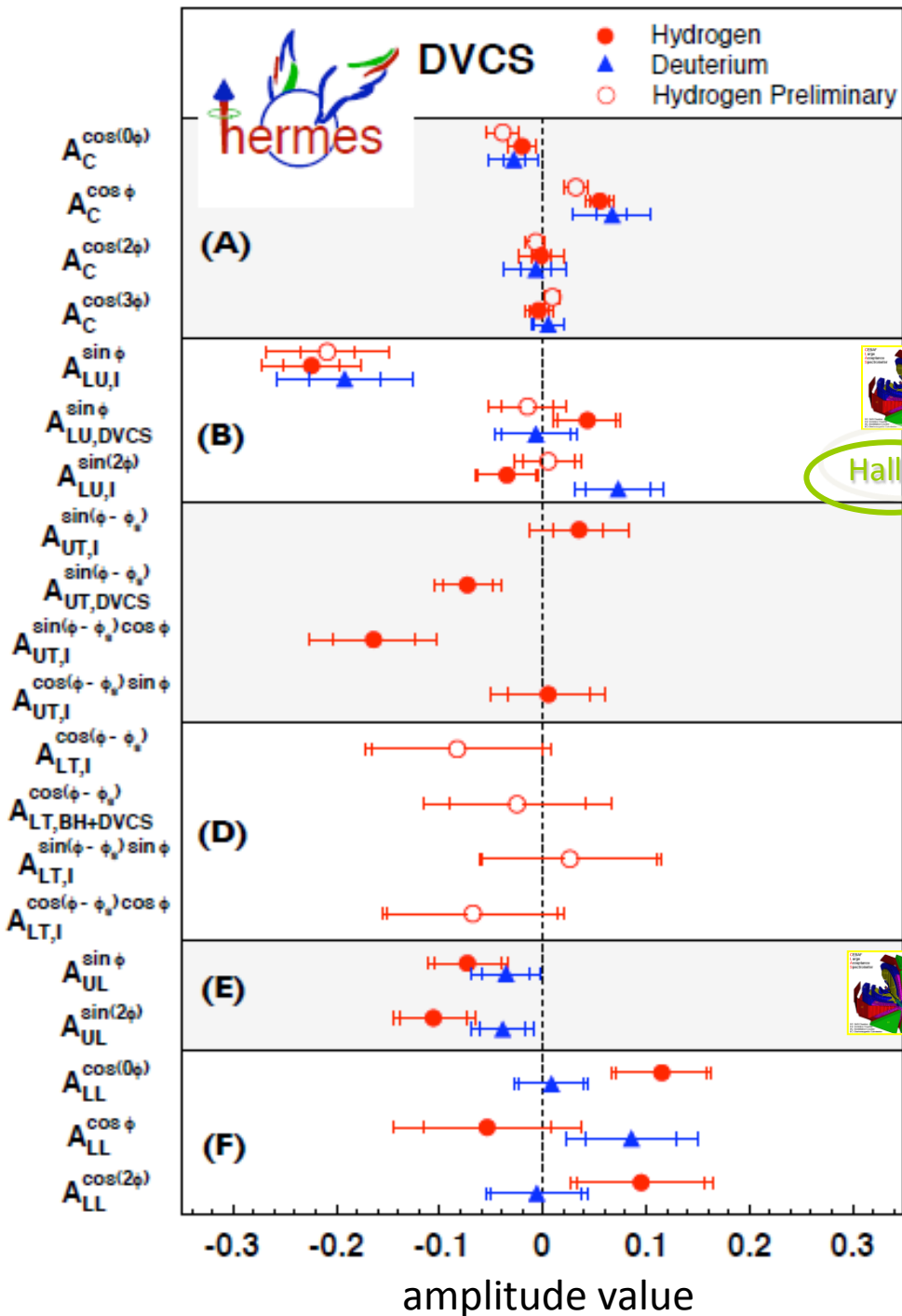
$$Re(H-E)$$

→ longitudinal target spin asymm.

$$Im(\tilde{H})$$

→ longitudinal-target double-spin

$$Re(\tilde{H})$$



unique data set

→ charge asymmetry

$$Re(H)$$

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→ transverse target spin asymmetry

$$Im(H-E)$$

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$$Re(H-E)$$

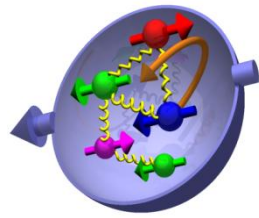
→ longitudinal target spin asymm.

$$Im(\tilde{H})$$

→ longitudinal-target double-spin

$$Re(\tilde{H})$$

GPD E & OAM



$$J^q = \Delta\Sigma + L^q = \frac{1}{2} \int x dx H^q - E^q$$

$\Delta\sigma_C, \Delta\sigma_{LU}$

$\rightarrow H_p, E_n$

Hall-A

$\Delta\sigma_{UL}$

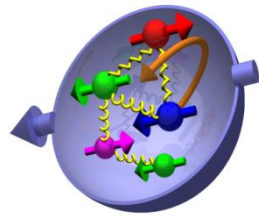
$\rightarrow H, \tilde{H}$

$\Delta\sigma_{UT}$

$\rightarrow H, E$



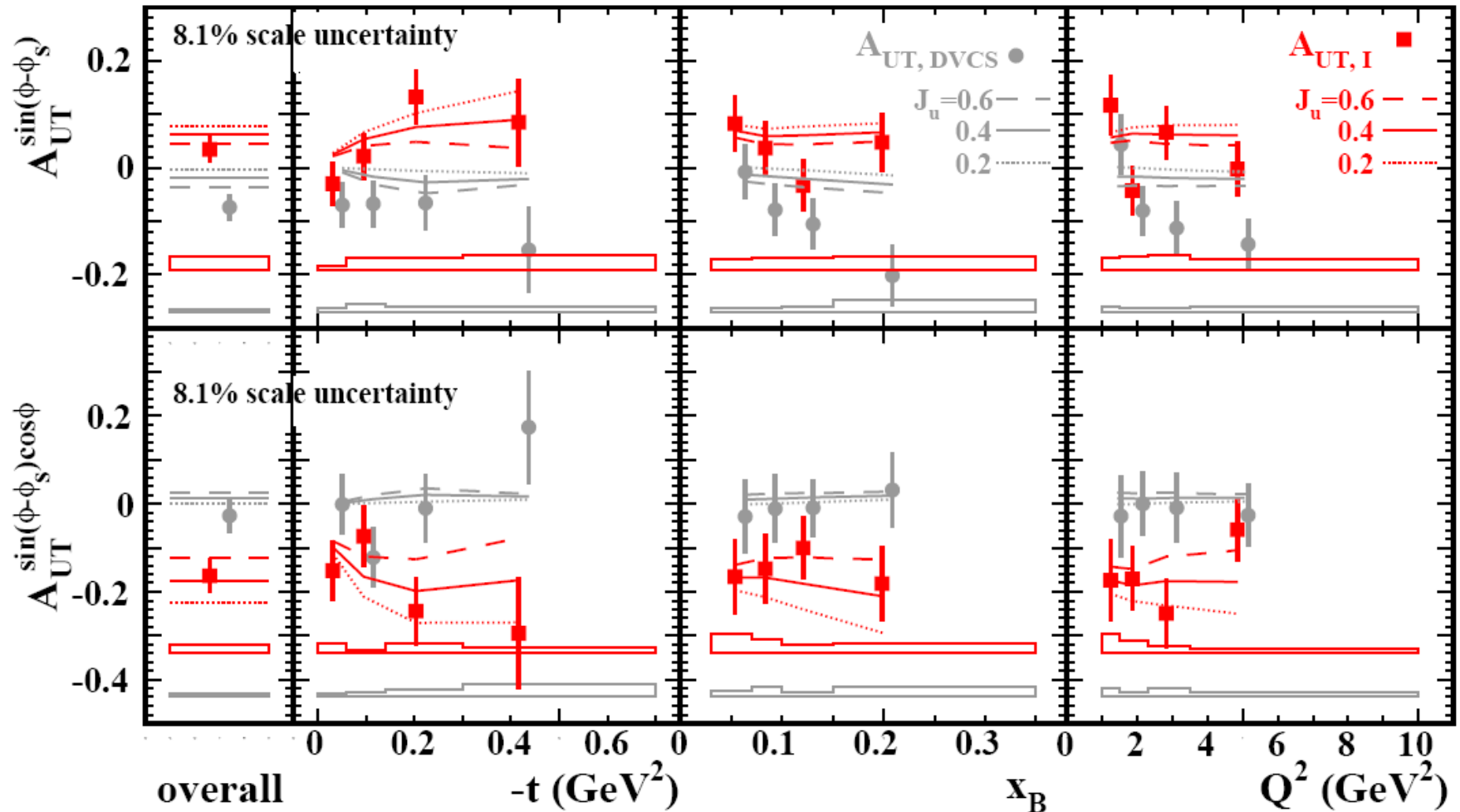
@kinematics of current fixed target exp.



$$J^q = \Delta\Sigma + L^q = \frac{1}{2} \int x dx H^q - E^q$$

→ GPD models: J^q free parameter in ansatz for E

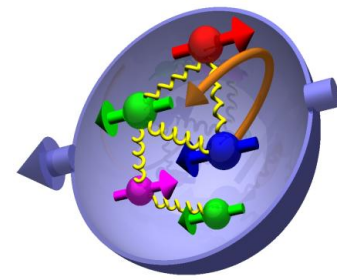
[JHEP06(2008)]





HERA MEasurment of Spin

summary

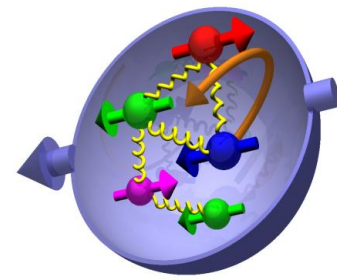


- ❑ 2nd generation *polarised* DIS experiment @HERA: polarised $e^{+/-}$ beam & novel target technology of storage cell with pure nuclear-polarised H or D
- ❑ *mission*: exploring the nucleon structure *beyond* fully inclusive DIS

many *pioneering* measurements:

- first direct 5-flavour extraction of helicity distributions
- quest for the orbital angular momentum:

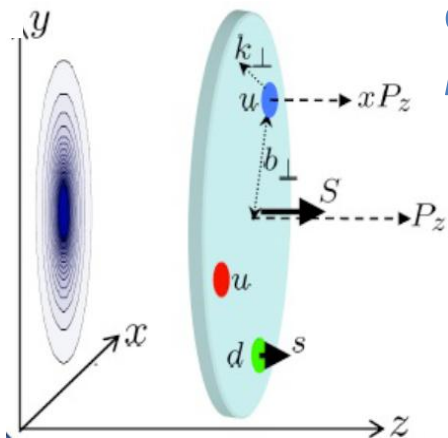
summary



- 2nd generation *polarised* DIS experiment @HERA: polarised $e^{+/-}$ beam & novel target technology of storage cell with pure nuclear-polarised H or D
- *mission*: exploring the nucleon structure *beyond* fully inclusive DIS

many *pioneering* measurements:

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exploring novel distributions: **GPDs & TMDs**, which go *beyond the collinear approximation* → nucleon tomography

from first signals of GPDs & TMDs
to the
most complete data set measured so far

**for additional information, please have a look
at the following pages...**

Δq and ΔG from NLO QCD fits

@Next-to-Leading Order in α_s :

$$g_1^{\text{NLO}}(x, Q^2) = g_1^{\text{LO}} + \frac{1}{2} \langle e^2 \rangle \sum_q e_q^2 [\underline{\Delta q(x, Q^2)} \otimes C_q + \underline{\Delta g(x, Q^2)} \otimes C_g]$$

$\Delta f(x)$... to be measured (parametrised) !

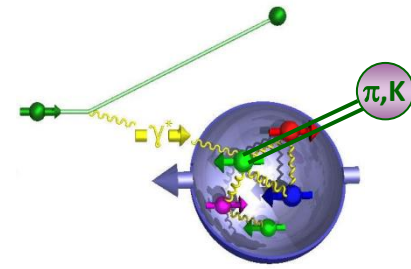
$\Delta f(x, Q^2)$... fully calculable in QCD !
(splitting functions)

*→ different Q^2 evolution for
different quark flavour and for gluons*

$$\chi^2 = \sum_{\text{data}} \frac{(g_1^{\text{meas}} - g_1^{\text{calc}})^2}{\sigma_{\text{stat}}^2}$$

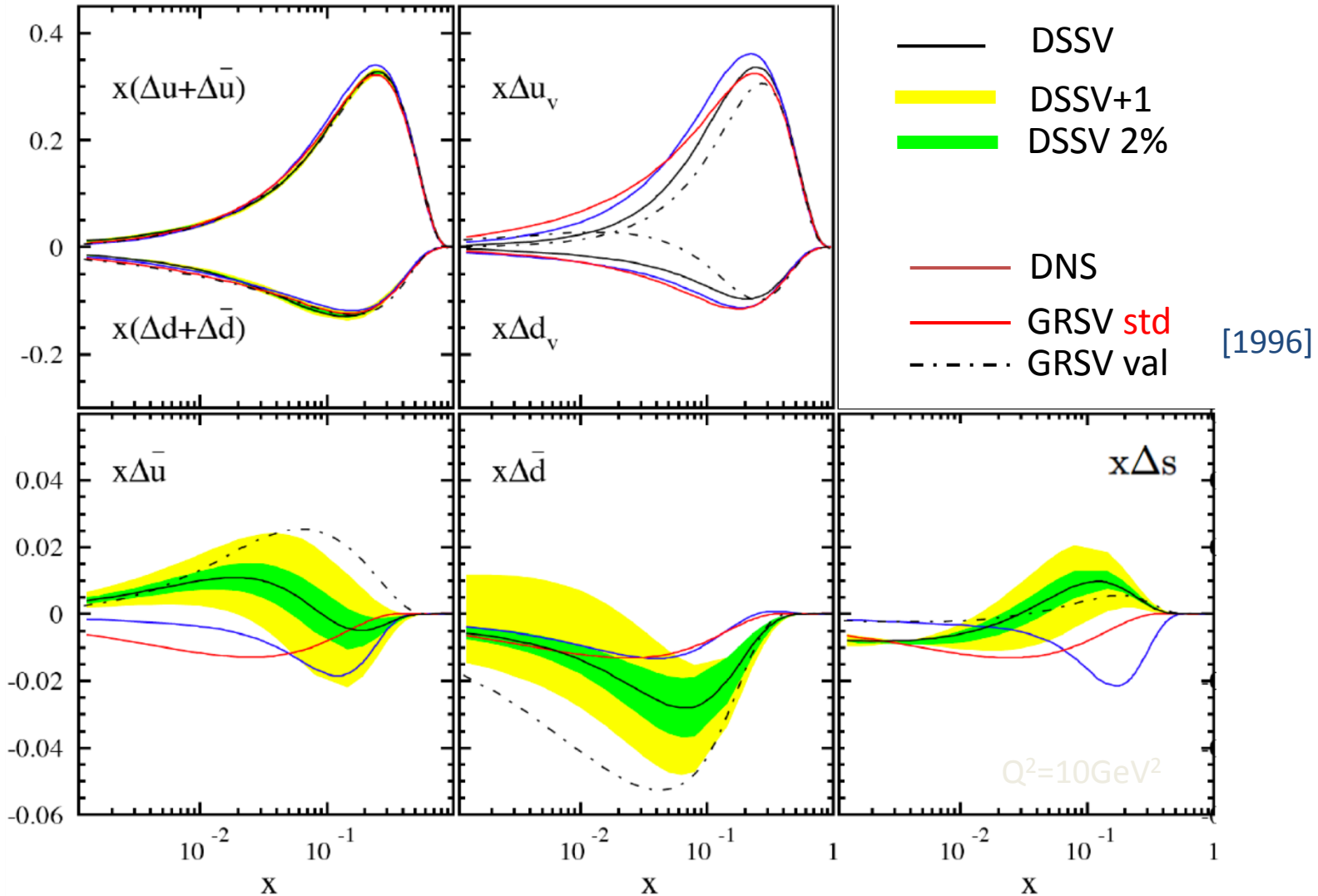
→ requires g_1 data in wide kinematic range in x and Q^2

polarised pdfs: Δq

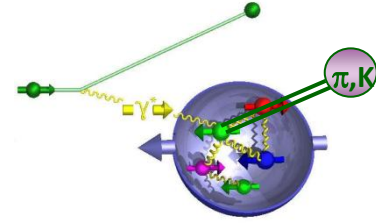


results driven by inclusive and *semi*-inclusive DIS

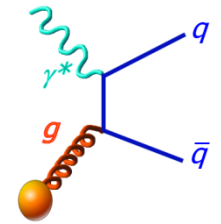
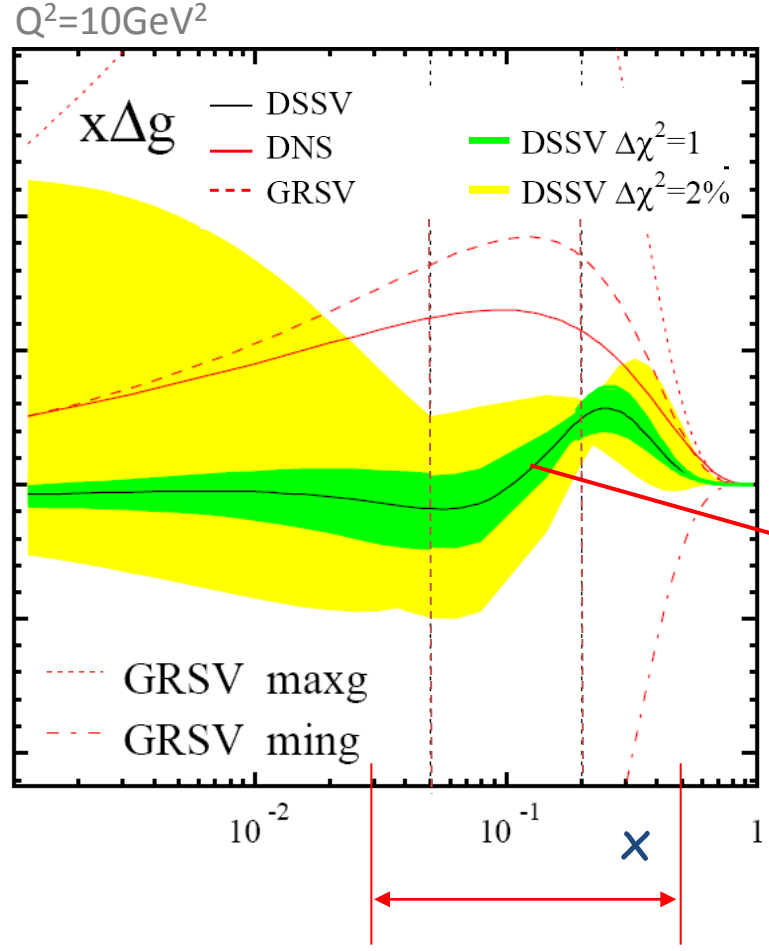
[DSSV, PRL101(2008), PRD(2009)]



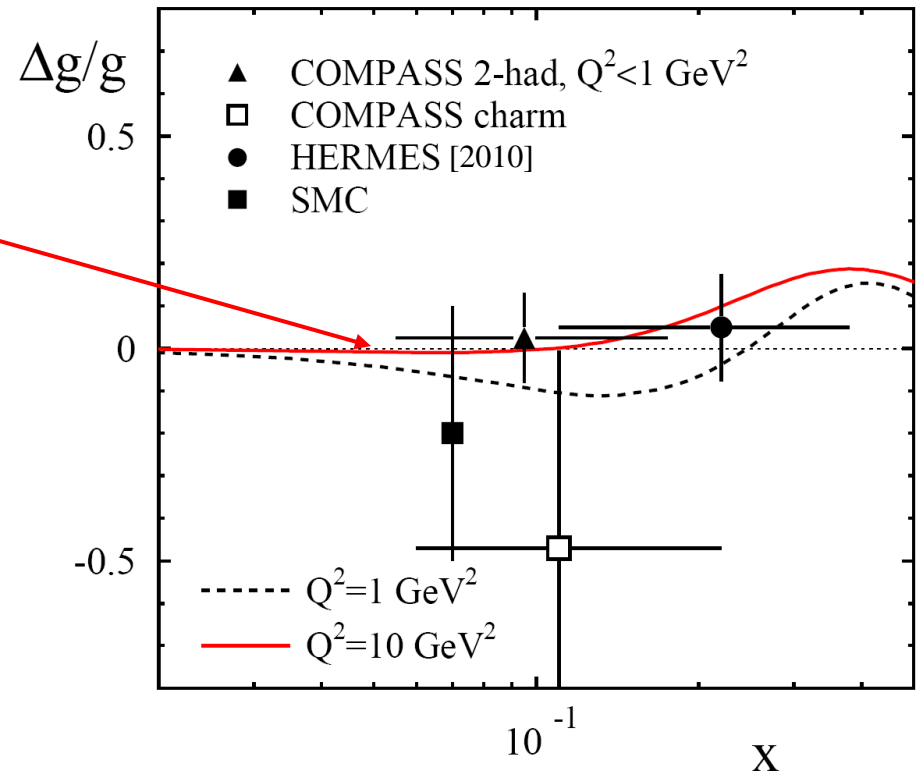
polarised pdfs: ΔG



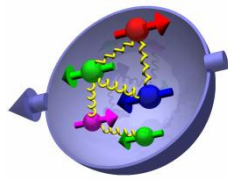
results driven by inclusive DIS & *pp*-scattering data



model dependent
LO analyses of PGF
 process in DIS:



polarised pdfs: Δq & ΔG



global analysis of polarised DIS & pp-scattering data

contributions to nucleon spin:

$$\Delta f \equiv \int_{x_{\min}}^1 dx \Delta f(x)$$

$Q^2=10\text{GeV}^2$

	$x_{\min} = 0$ best fit	$\Delta\chi^2 = 1$	$x_{\min} = 0.001$ $\Delta\chi^2/\chi^2 = 2\%$
$\Delta u + \Delta \bar{u}$	0.813	0.793 $^{+0.011}_{-0.012}$	0.793 $^{+0.028}_{-0.034}$
$\Delta d + \Delta \bar{d}$	-0.458	-0.416 $^{+0.011}_{-0.009}$	-0.416 $^{+0.035}_{-0.025}$
$\Delta \bar{u}$	0.036	0.028 $^{+0.021}_{-0.020}$	0.028 $^{+0.059}_{-0.059}$
$\Delta \bar{d}$	-0.115	-0.089 $^{+0.029}_{-0.029}$	-0.089 $^{+0.090}_{-0.080}$
$\Delta \bar{s}$	-0.057	-0.006 $^{+0.010}_{-0.012}$	-0.006 $^{+0.028}_{-0.031}$
Δg	-0.084	0.013 $^{+0.106}_{-0.120}$	0.013 $^{+0.702}_{-0.314}$
$\Delta \Sigma$	0.242	0.366 $^{+0.015}_{-0.018}$	0.366 $^{+0.042}_{-0.062}$

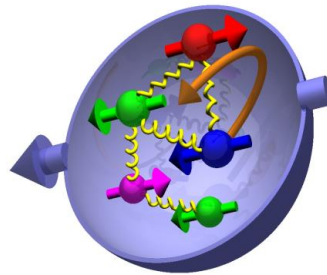
■ Δs receives large negative contribution @small x

■ Δg : huge uncert. below $x \approx 0.01$
 \rightarrow 1st moment *undetermined*

[DSSV, PRL101(2008), PRD(2009)]

call for new facilities: high energy polarised ep collider needed !

the quest for the orbital angular momentum

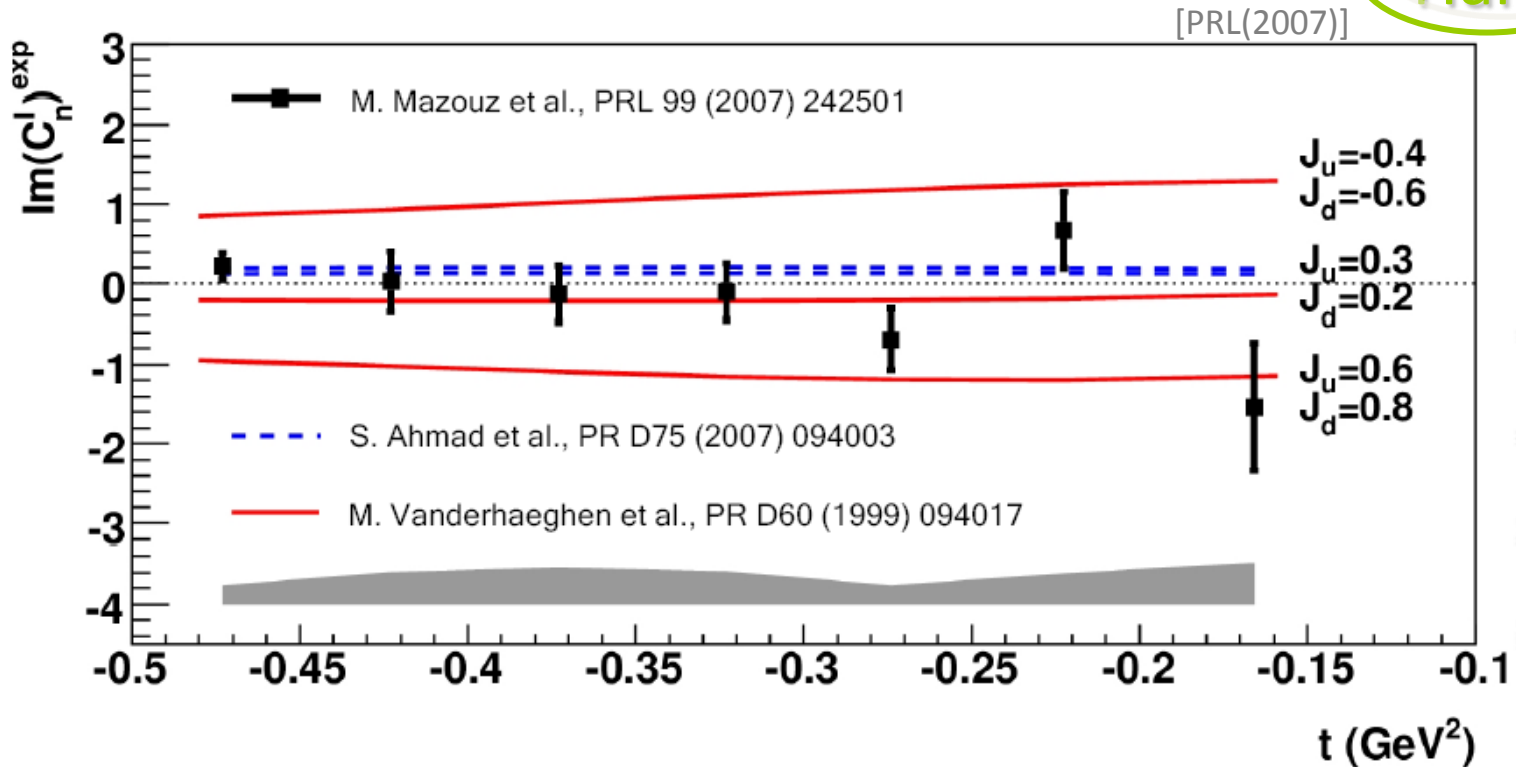


hunting the OAM

-- nDVCS : beam-spin cross section difference --

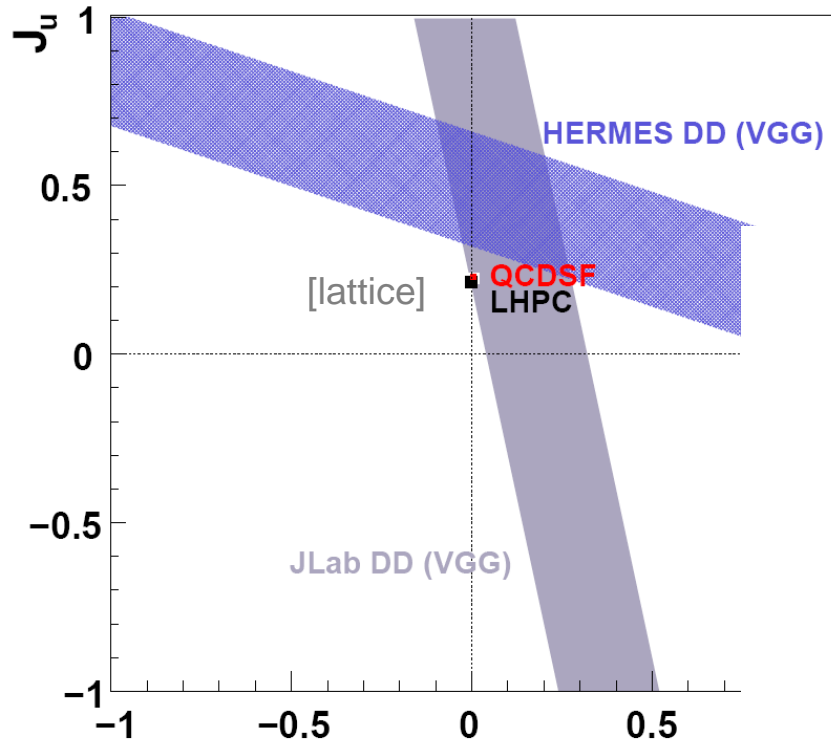
→ GPD models: J^q free parameter in ansatz for E

Hall-A

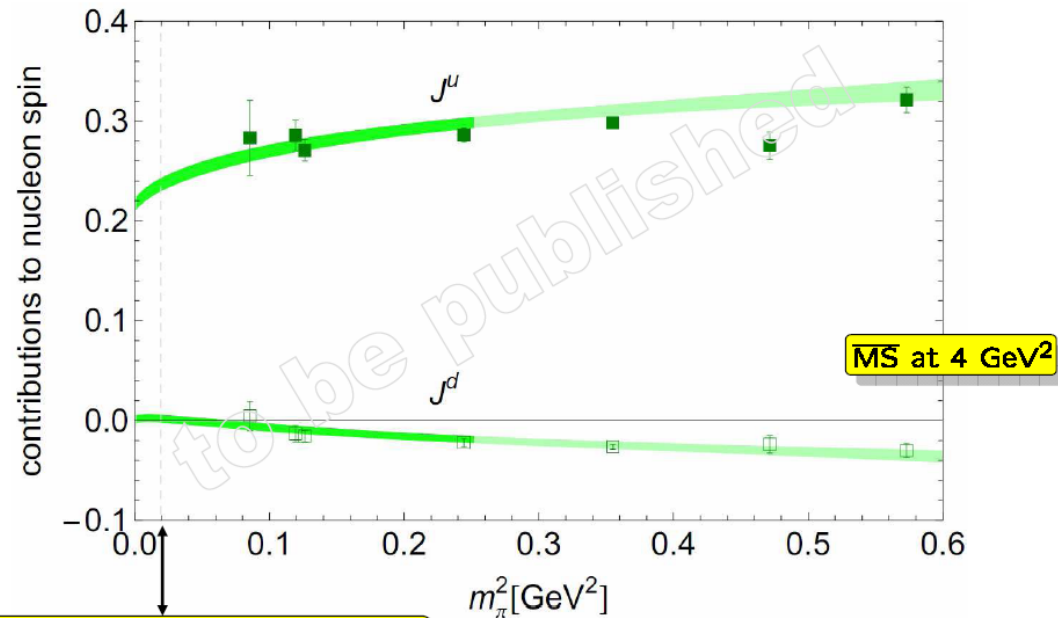


hunting the OAM

-- *model dependent* [VGG(1999)] constrain of J_u vs J_d --



lattice in more detail:

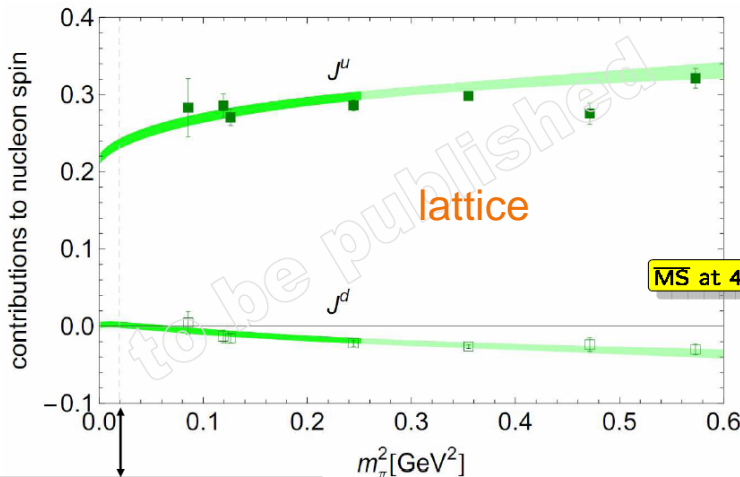
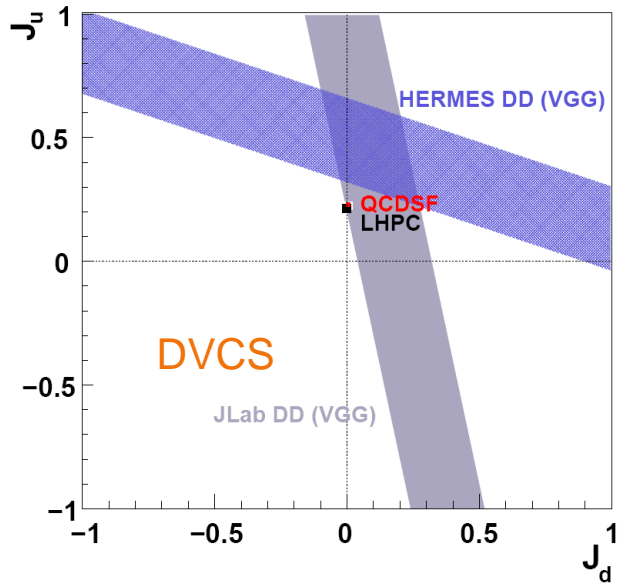


$$J^u = 0.236(6) \approx 47\% \text{ of } 1/2$$

$$J^d = 0.0018(37) \approx 1\% \text{ of } 1/2$$

$$J^{u+d} \approx 0.238 \pm 0.008 \approx 48\% \text{ of } 1/2$$

hunting the OAM



$J^u = 0.236(6) \approx 47\%$ of $1/2$
 $J^d = 0.0018(37) \approx 1\%$ of $1/2$

$J^{u+d} \approx 0.238 \pm 0.008 \approx 48\%$ of $1/2$

- *GPD* model tuned to **VM** [GK (2008)]

J^u	J^d	J^s	J^g
0.250	0.020	0.015	0.214
0.276	0.046	0.041	0.132
0.225	-0.005	-0.011	0.286
0.209	0.013	0.015	0.257
0.230	0.024	0.015	0.228
0.234	0.028	0.019	0.214

variants for
GPD E

- **TMD** models: [→ A. Bacchetta]

model dependent relation:

$$f_{1T}^{\perp(0)a}(x; Q_L^2) = -L(x) E^a(x, 0, 0; Q_L^2)$$

$$J^u = 0.266 \pm 0.002_{-0.014}^{+0.009},$$

$$J^d = -0.012 \pm 0.003_{-0.006}^{+0.024}$$