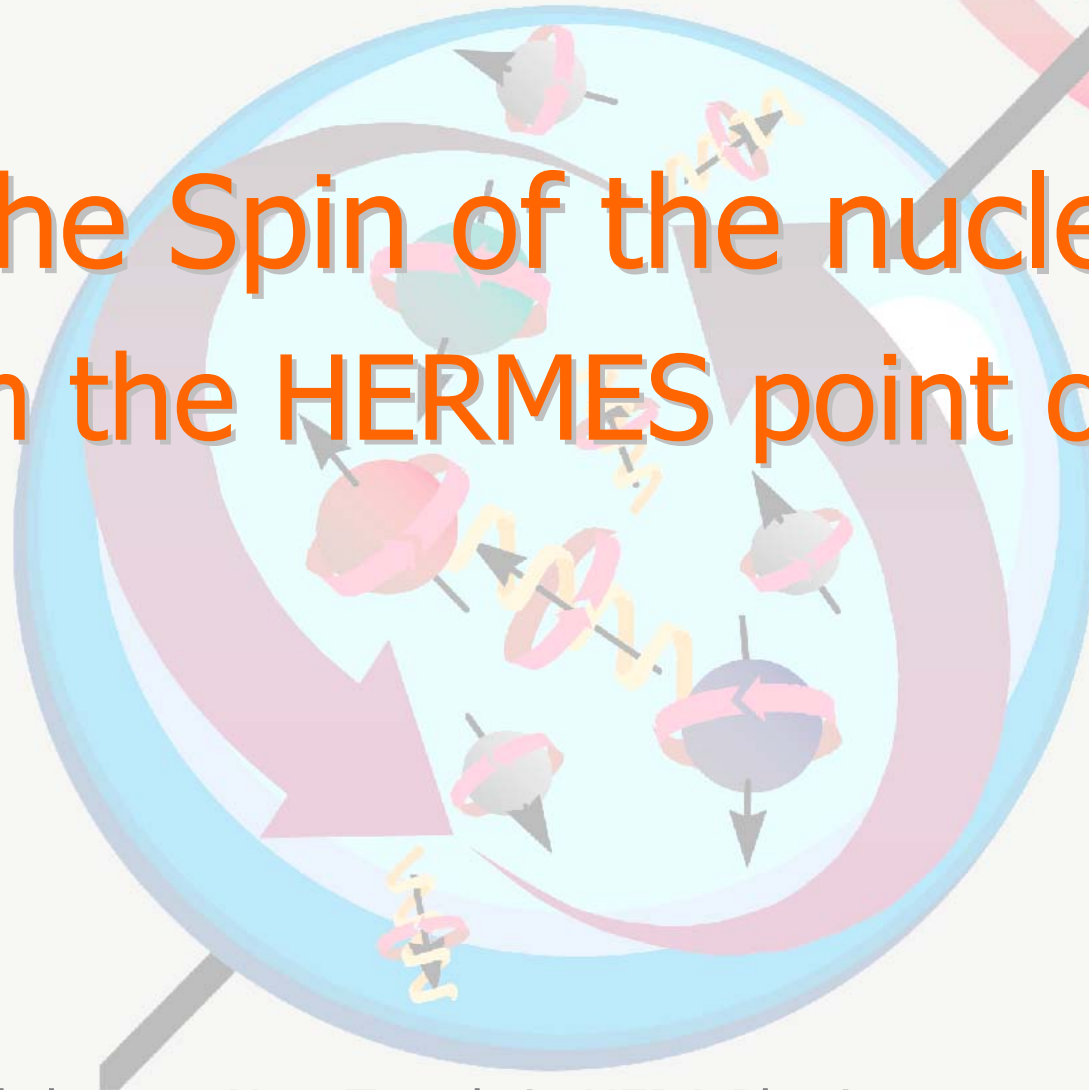


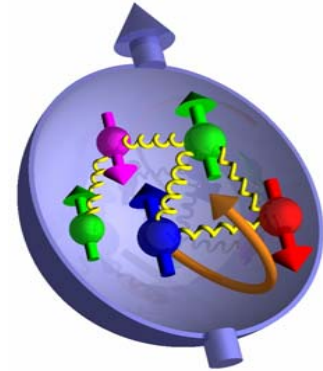
the Spin of the nucleon -from the HERMES point of view-





HERA MEasurement of Spin

$$\frac{S_z^N}{\hbar} = \frac{1}{2} = \frac{1}{2} \Delta\Sigma + L_z^q + \Delta G + L_z^g$$

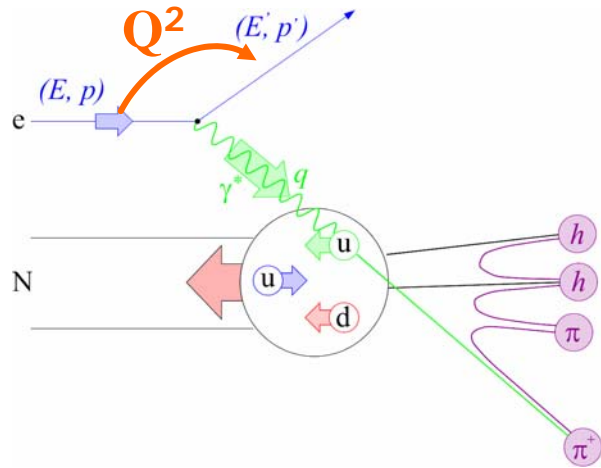


outline:

- prerequisites
- polarisation of quarks: $\Delta\Sigma = \Delta u_v + \Delta d_v + \Delta q_s$
- polarisation of gluons: ΔG
- hunting for the OAM $L_{q,g}$ → talk by M. Düren
- transverse spin phenomena → talk by U. D'Alesio

*new
developments*

polarised deep-inelastic scattering



$$Q^2 = -q^2 = 2EE'(1-\cos\theta)$$

$$x = \frac{Q^2}{2Mv}, \quad x \in [0,1] \quad v = E - E'$$

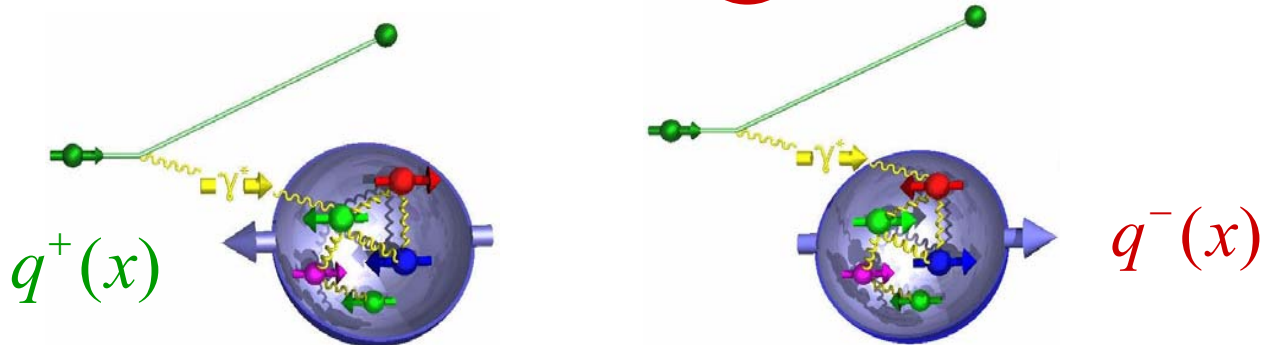
$$z = \frac{E_h}{v}$$

factorisation:

$$\sigma_{DIS}^h \propto \sum_f \hat{\sigma}_{part} \otimes pdf(x) \otimes frag^{q,g \rightarrow h}(z)$$



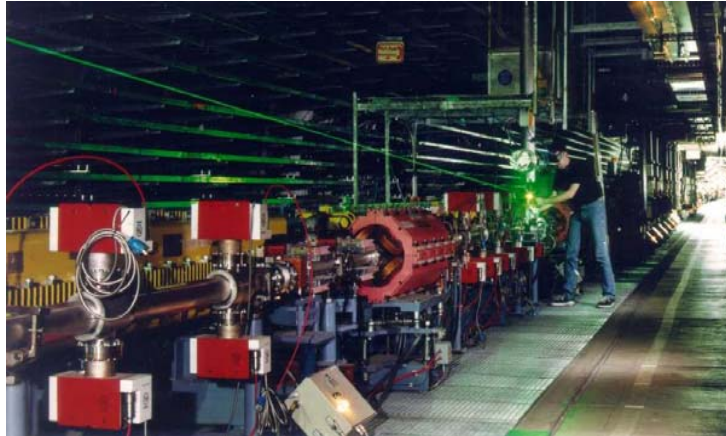
$$\Delta q(x) = q^+(x) - q^-(x)$$



experimental prerequisites

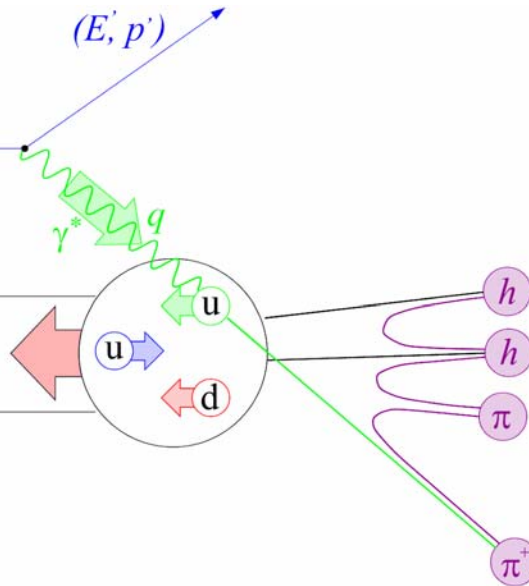
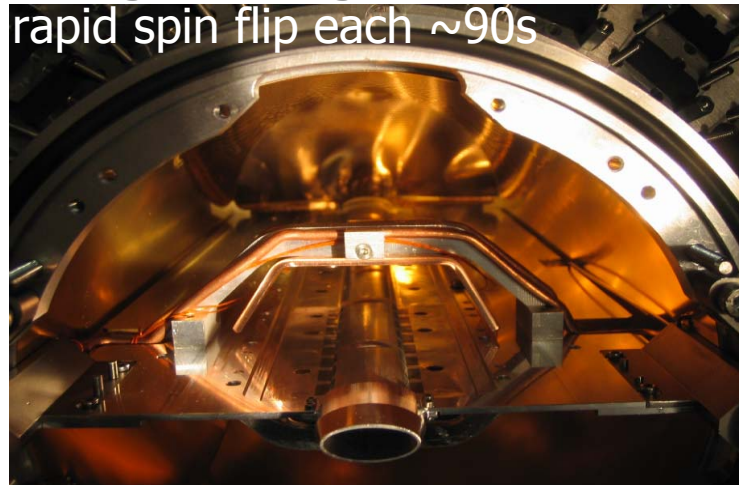


-the 2nd generation-



HERA 27.5 GeV (e⁺/e⁻) →
 $\langle P_b \rangle \sim 53 \pm 2.5 \%$

storage cell target: no dilution
 rapid spin flip each ~90s



- $^1\text{H} \rightarrow \langle |P_t| \rangle \sim 85\%$
- $^2\text{H} \rightarrow \langle |P_t| \rangle \sim 84\%$
- $^1\text{H} \uparrow \langle |P_t| \rangle \sim 74\%$

$$\delta\sigma \propto \frac{1}{P_b P_t f} \cdot \frac{1}{\sqrt{N}}$$

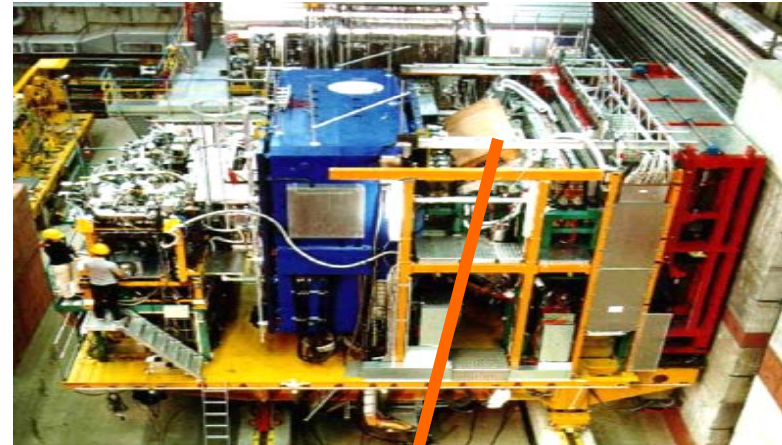
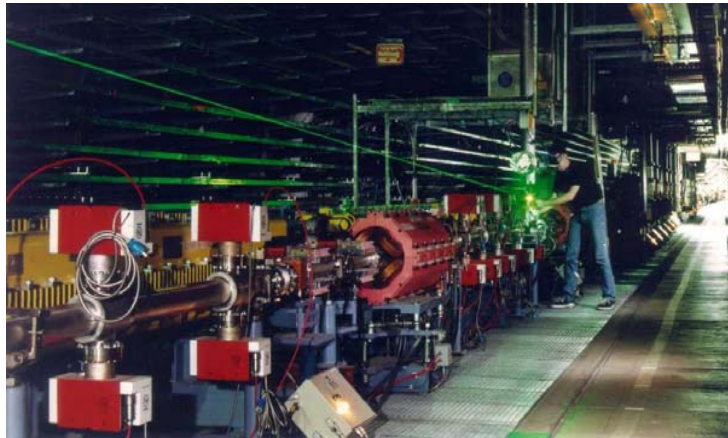
f: target dilution factor

f=1 gas targets, f~0.02 solid targets

experimental prerequisites

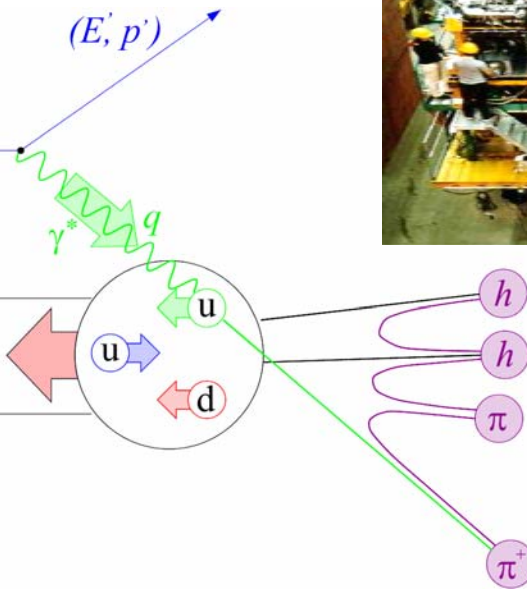
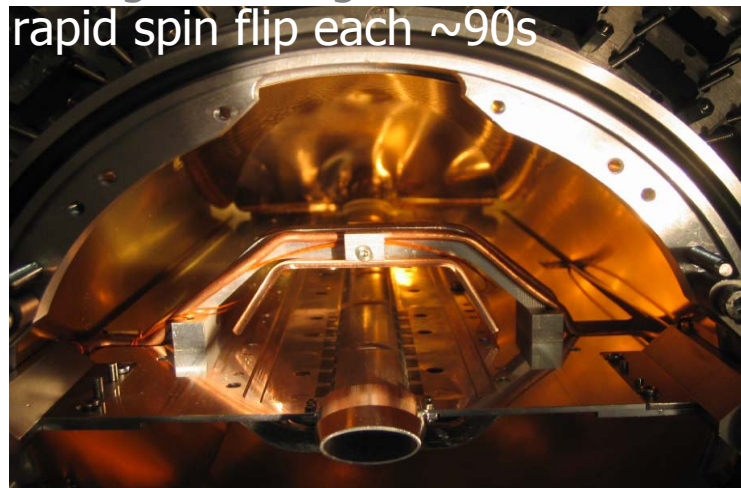


-the 2nd generation-

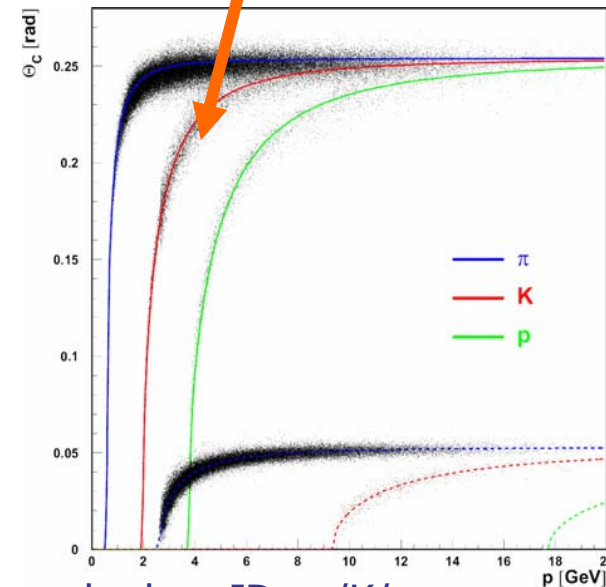


HERA 27.5 GeV (e+/e-) →
 $\langle P_b \rangle \sim 53 \pm 2.5 \%$

storage cell target: no dilution
 rapid spin flip each ~ 90 s



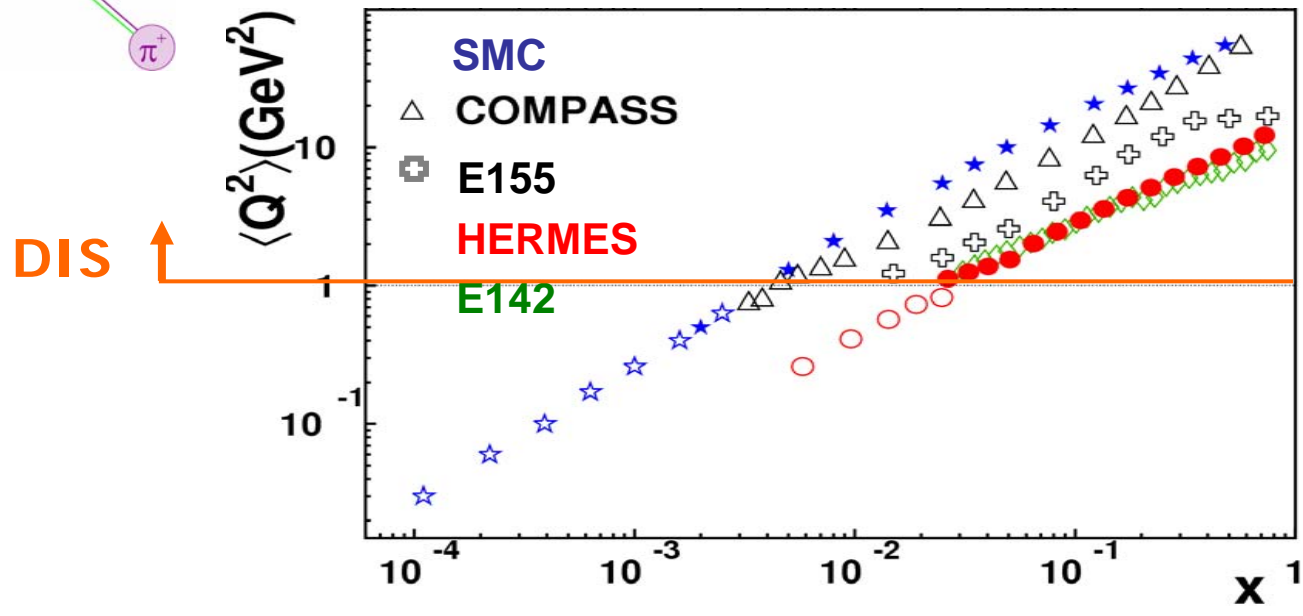
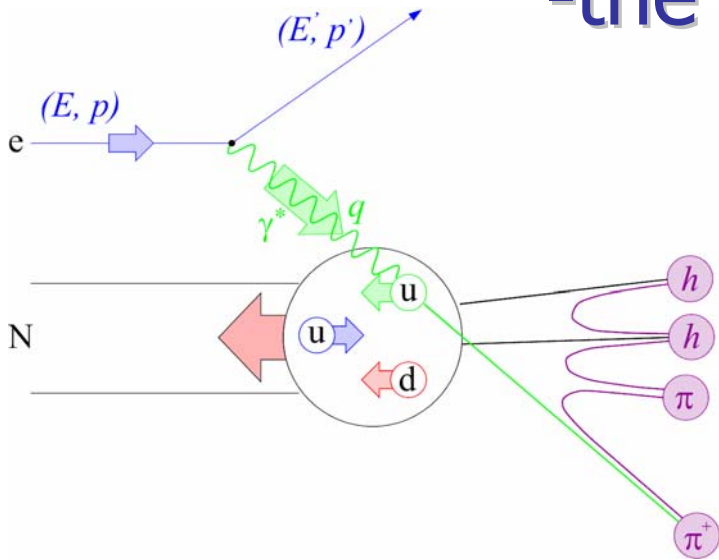
$^1H \rightarrow \langle |P_t| \rangle \sim 85\%$
 $^2H \rightarrow \langle |P_t| \rangle \sim 84\%$
 $^1H \uparrow \langle |P_t| \rangle \sim 74\%$



hadron ID: $\pi/K/p$
 $2 < E_h < 15$ GeV

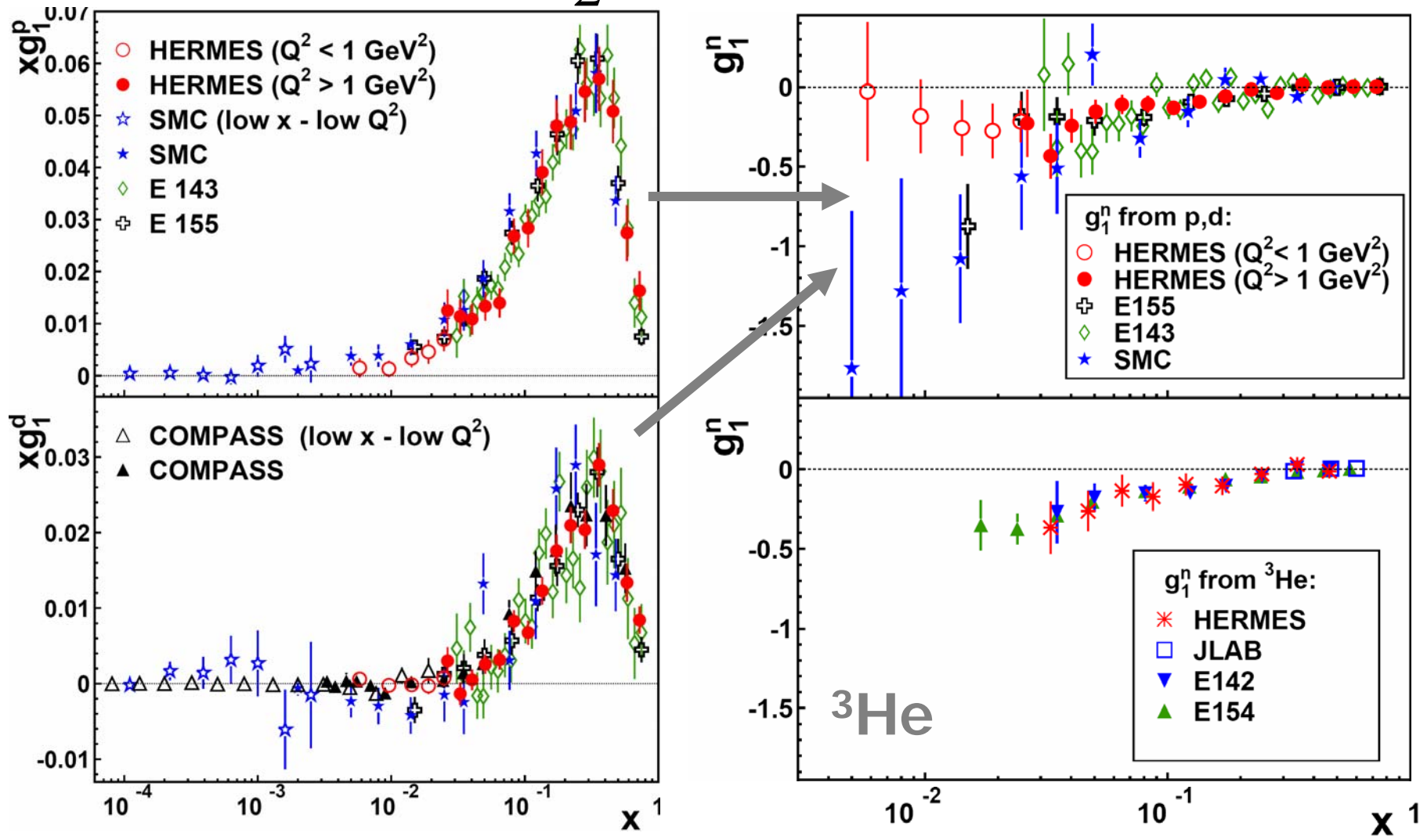
experimental prerequisites

-the 2nd generation-

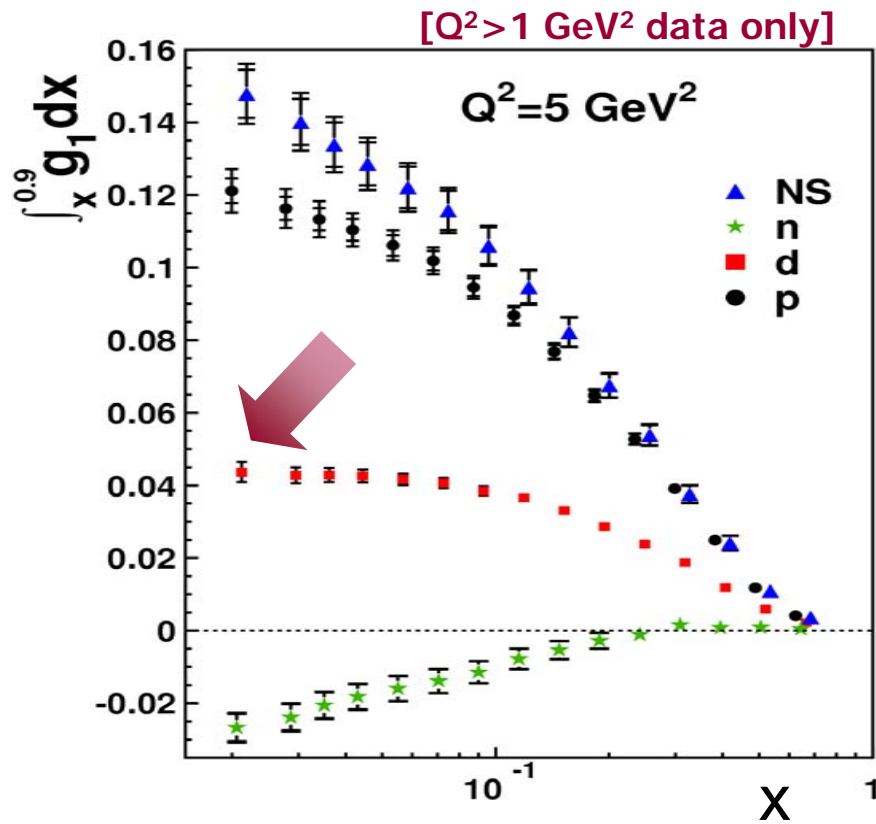


polarised structure function g_1

$$g_1(x) = \frac{1}{2} \sum_q e_q^2 (\Delta q + \Delta \bar{q})$$



first moment Γ_1^d and $\Delta\Sigma$



→ assume *saturation* of Γ_1^d : 

$$\overline{a_0}^{\text{MS}} = \Delta\Sigma \propto \frac{1}{\Delta C_s} \left[9 \Gamma_1^d - \frac{1}{4} a_8 \Delta C_{NS} \right]$$

from theory

from hyperon beta decay

$$\overline{a_0}^{\text{MS}} = \Delta\Sigma \quad \begin{array}{ccc} \text{(exp)} & \text{(theory)} & \text{(evol)} \\ = 0.330 \pm 0.025 \pm 0.011 \pm 0.028 \end{array}$$

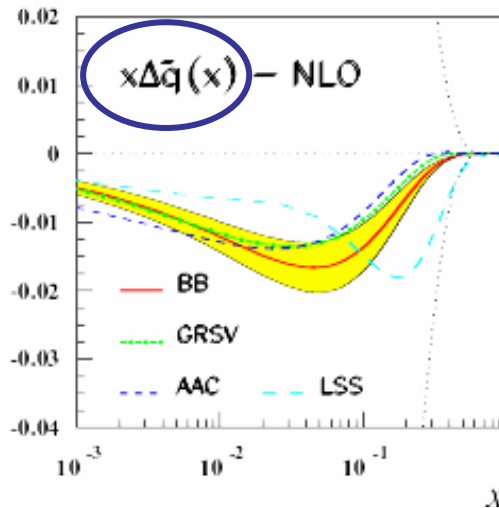
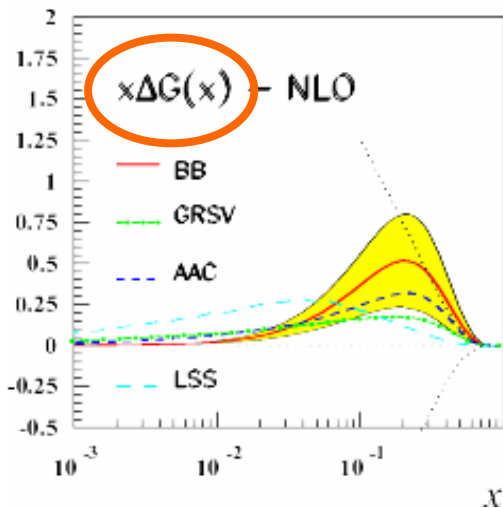
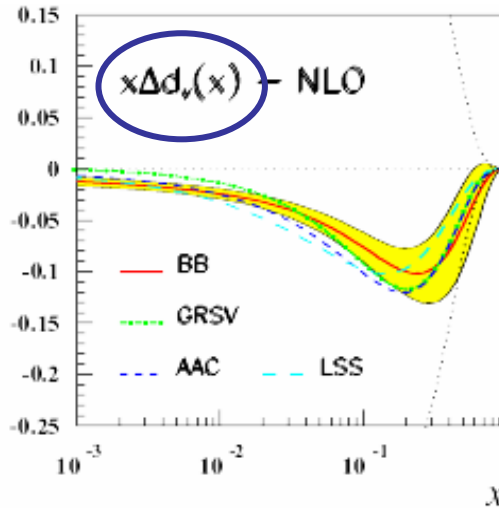
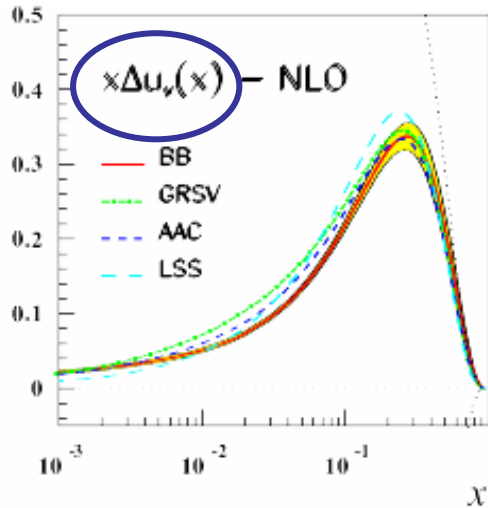


QCD-fit:

$$\overline{a_0}^{\text{MS}} = \Delta\Sigma = 0.35 \pm 0.03^{\text{(stat)}} \pm 0.05^{\text{(sys+evol)}}$$

Δq and ΔG from inclusive data

$$g_1^{\text{NLO}}(x, Q^2) = g_1^{\text{LO}} + \frac{1}{2} \langle e^2 \rangle \sum_q e_q^2 [\Delta q(x, Q^2) \otimes C_q + \Delta g(x, Q^2) \otimes C_g]$$



- valence quarks are well determined:

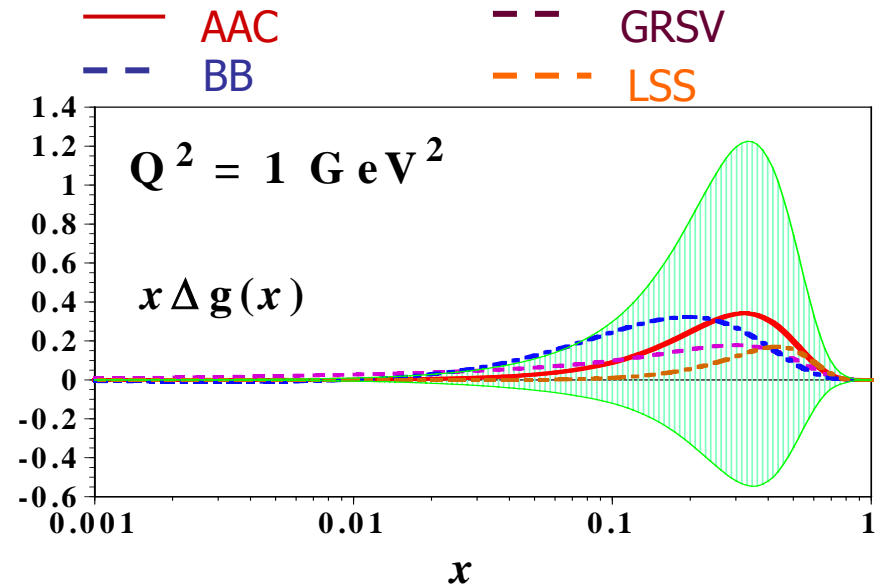
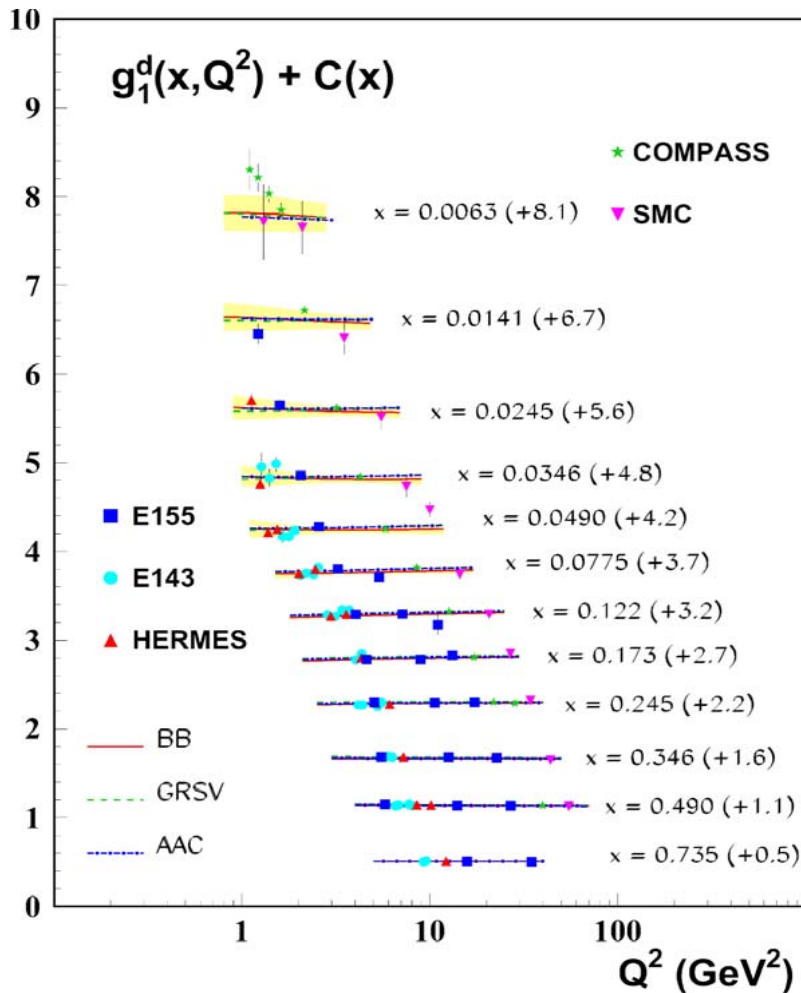
$$\Delta u_v > 0, \quad \Delta d_v < 0$$

- gluons and sea quarks are poorly constrained by data

$SU(3)_f$ symmetry implicitly assumed

call for more direct probes...

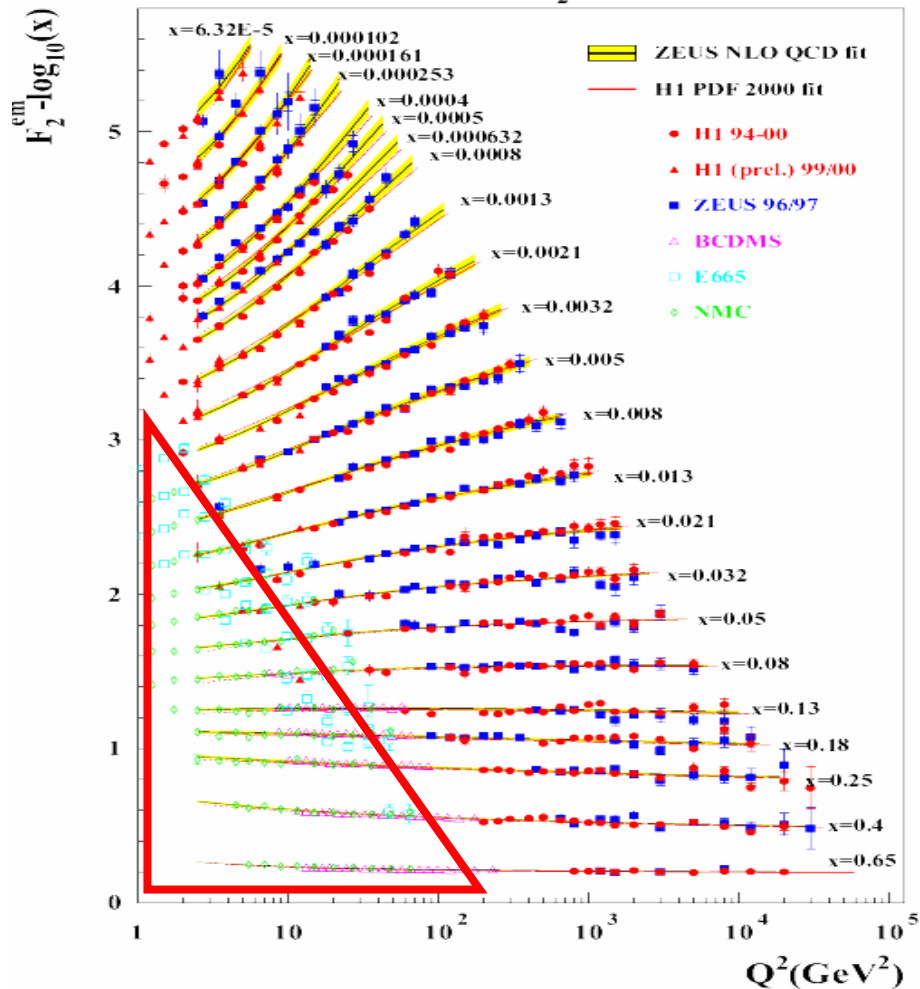
kinematic range of polarised DIS exp:



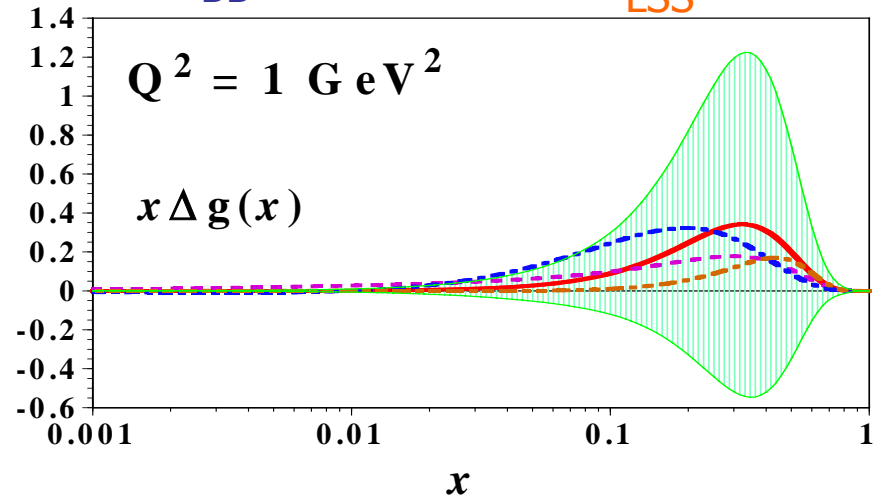
call for more direct probes...

kinematic range of polarised DIS exp:

HERA F_2 **unpolarised DIS**



— AAC
 - - GRSV
 - - BB
 - - LSS



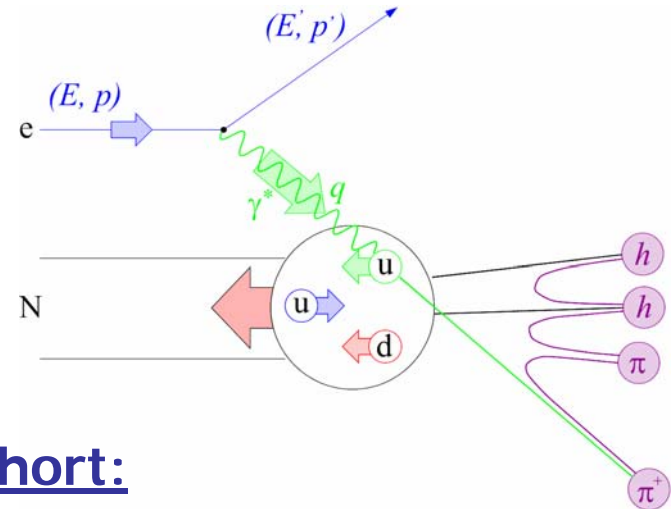
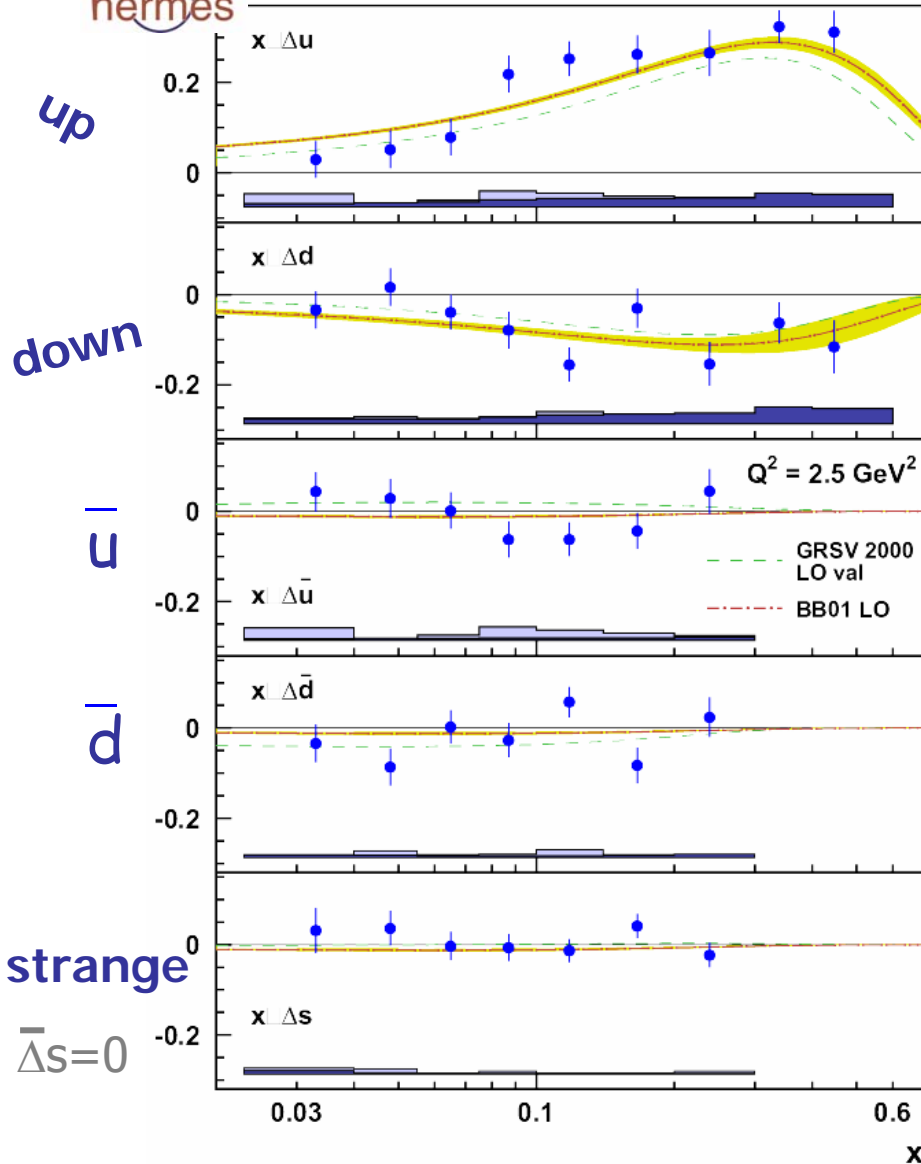
need *polarised collider* to extend kinematic coverage

→ need *more direct probes*

flavour tagging: *semi-inclusive* DIS



[PRL92(2004), PRD71(2005)]



in short:

$\Delta u(x) > 0$ and large

$\Delta d(x) < 0$ and smaller

$\Delta s(x) \approx 0$

HERMES: only direct 5-flavour separation of polarised pdfs

more about *strange* quarks

- strange quarks carry no isospin, thus the same in proton and neutron
- → use isoscalar probe and target to extract *strange-quark* distributions

more about *strange* quarks

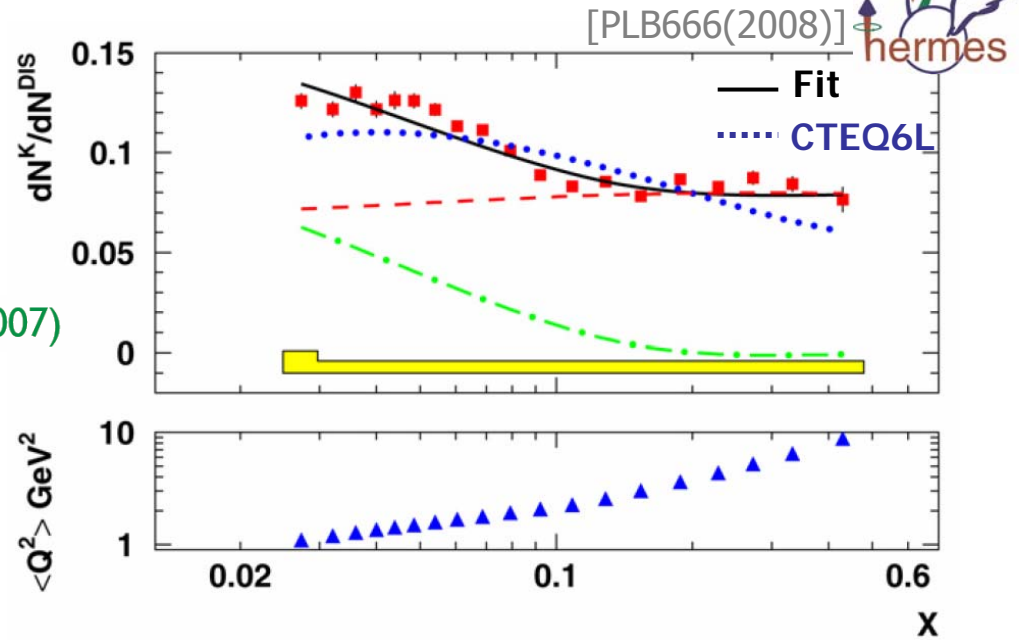
- strange quarks carry no isospin, thus the same in proton and neutron
 - → use isoscalar probe and target to extract *strange-quark* distributions
 - needed ingredients: $A_{1,d}(x, Q^2)$, $A_{1,d}^{K^+ + K^-}(x, z, Q^2)$ and $K^+ + K^-$ multiplicities
 - *strange-quark* fragmentation function either directly from data or from parametrisations
- only assumptions:
- isospin symmetry between proton and neutron
 - charge conjugation invariance in fragmentation

unpolarised *strange* quarks

$K^+ + K^-$ multiplicities:

$$\int_{0.2}^{0.8} D_S^K(z) dz = 1.27 \pm 0.13$$

de Florian et al., PRD75 (2007)



unpolarised *strange* quarks

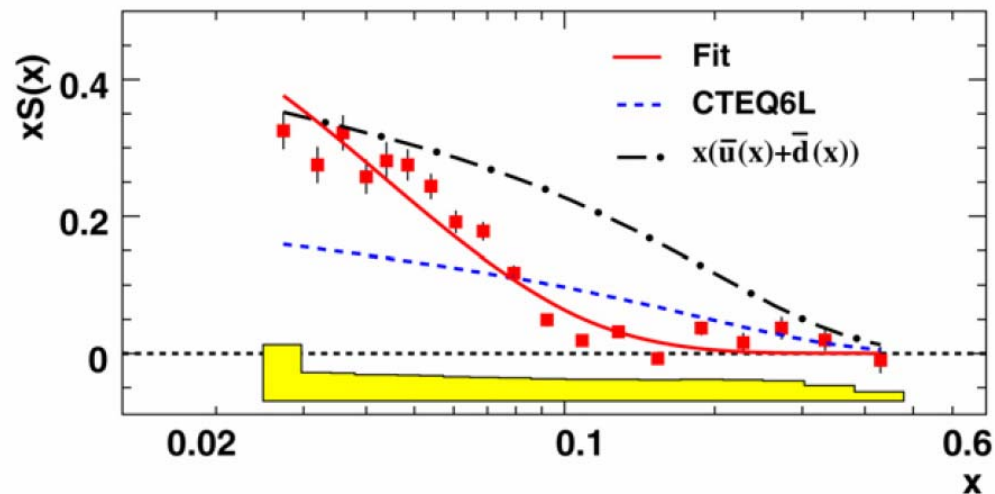
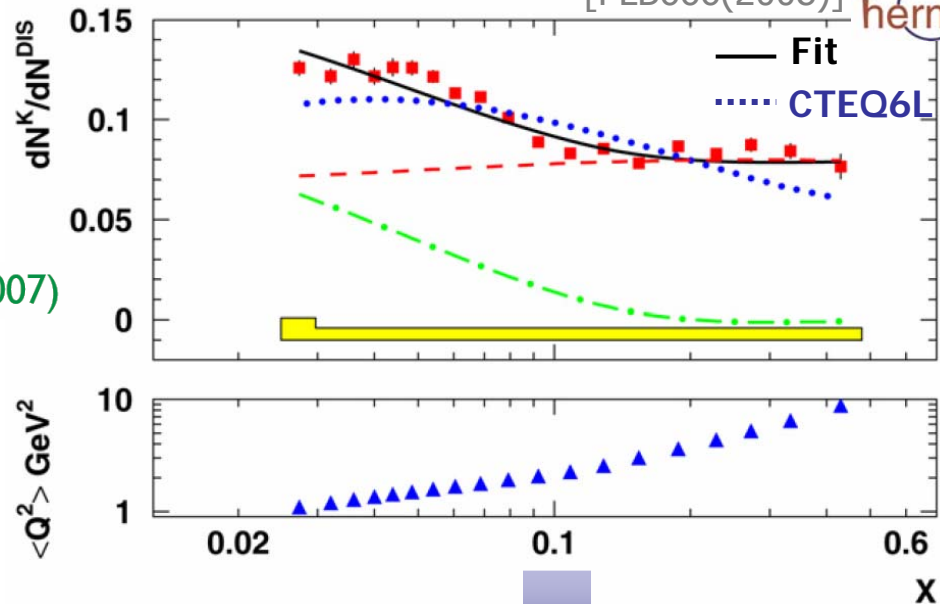
$K^+ + K^-$ multiplicities:

$$\int_{0.2}^{0.8} D_S^K(z) dz = 1.27 \pm 0.13$$

de Florian et al., PRD75 (2007)

- $S(x)$ non-zero for $x < 0.1$
vanishes for $x > 0.1$
- apparent discrepancy with
CTEQ6L
- $S(x)$ NOT an average of an
isoscalar non-strange sea

[PLB666(2008)]



polarised *strange* quarks

results consistent with previous
flavour decomposition

no sizeable negatively polarised
strange sea as expected from
inclusive DIS results

sign of violation of $SU(3)_f$
symmetry or of substantial
contribution from low-x region

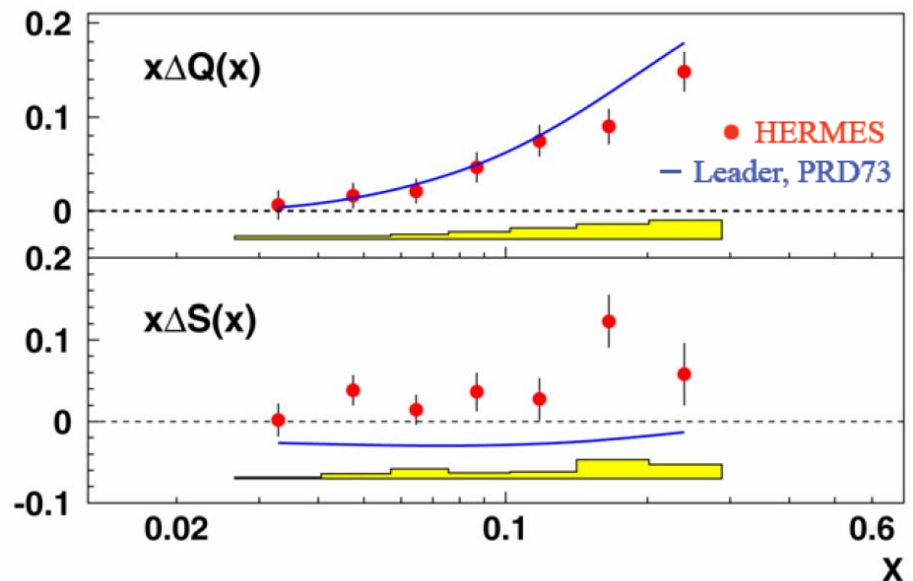
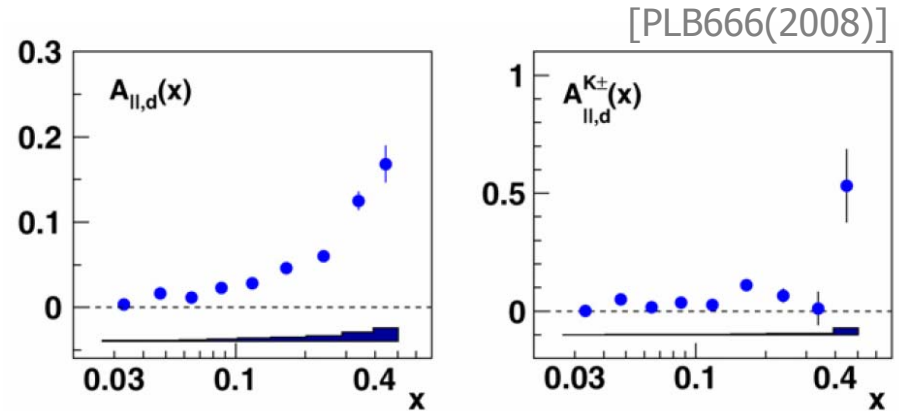
axial charge: $a_8 = \Delta q_8 = \Delta Q - 2\Delta S$

→ HERMES: $(0.02 < x < 0.6)$

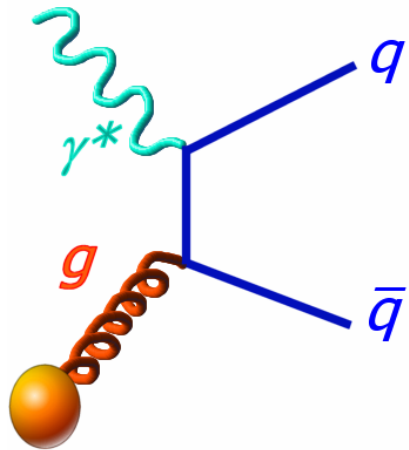
$$\Delta q_8 = 0.285 \pm 0.073$$

→ hyperon decay constants ($SU(3)$ symm)

$$\Delta q_8 = 0.586 \pm 0.031$$



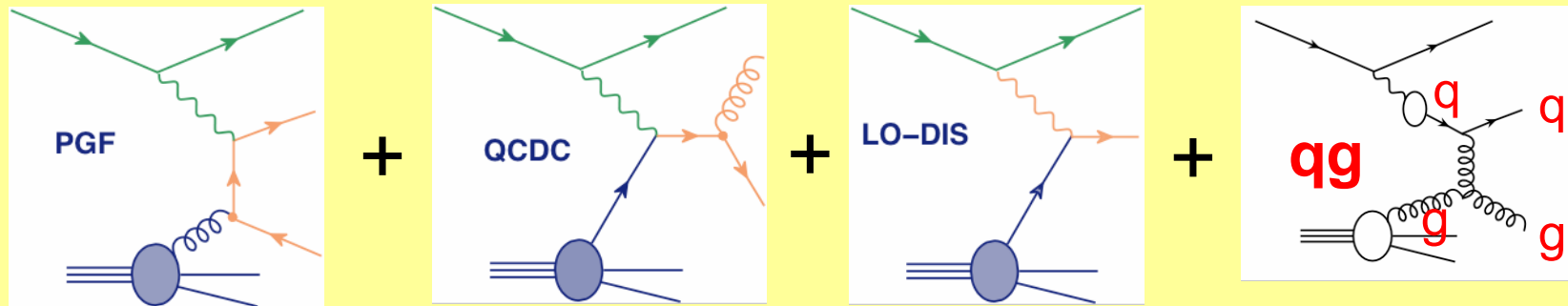
'direct' measurement of ΔG



Photon-Gluon Fusion (PGF)

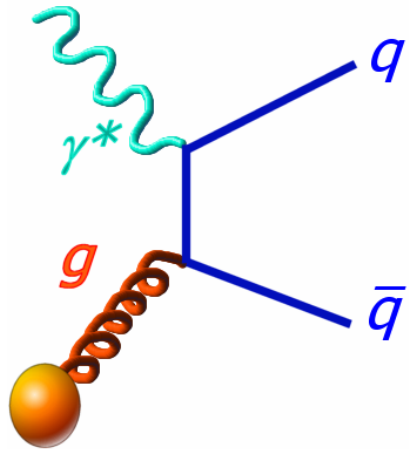
- golden channel: charm production
 - theoretically very clean
 - experimentally very challenging
- @HERMES ($\sqrt{s}=7$ GeV):
 - hadron production at high P_T
 - experimentally very clean
 - highly model dependent due to variety of background processes

other sub-processes make life hard:



extraction relies on Monte Carlo description of subprocesses (pythia)

direct measurement of ΔG



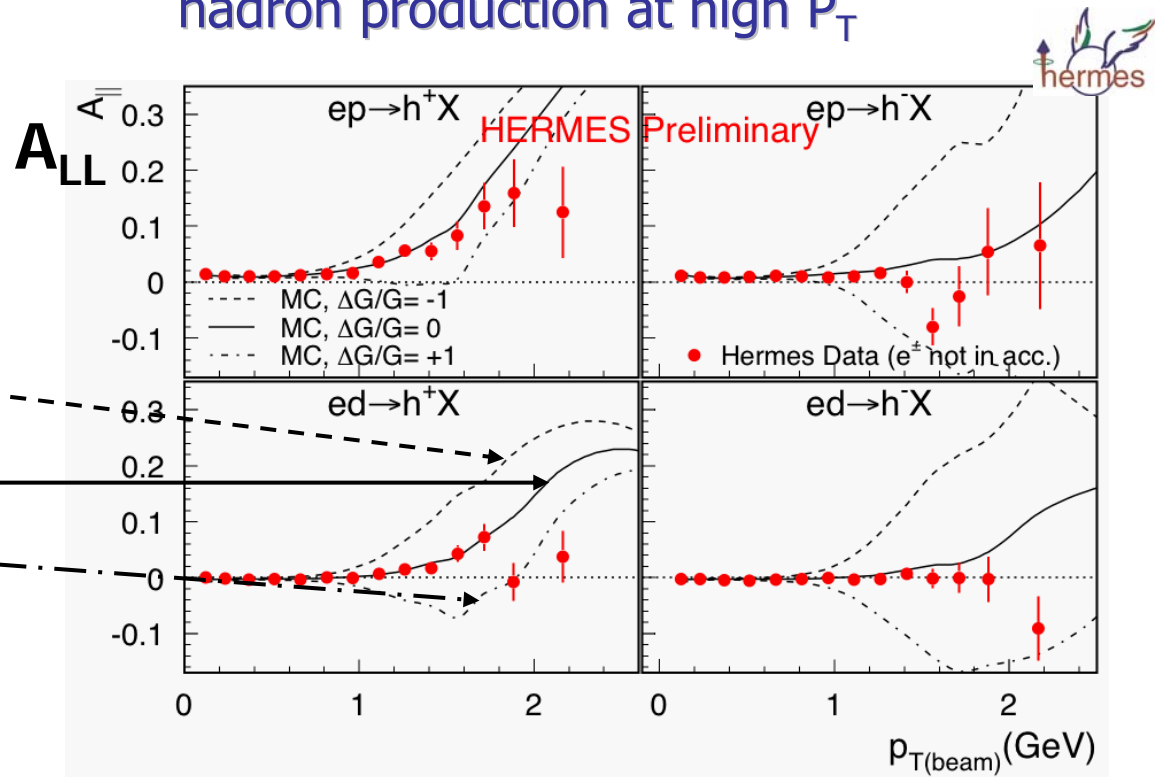
- golden channel: charm production
 - theoretically very clean
 - experimentally very challenging
- @HERMES ($\sqrt{s}=7$ GeV):
 - hadron production at high P_T

PythiaMC:

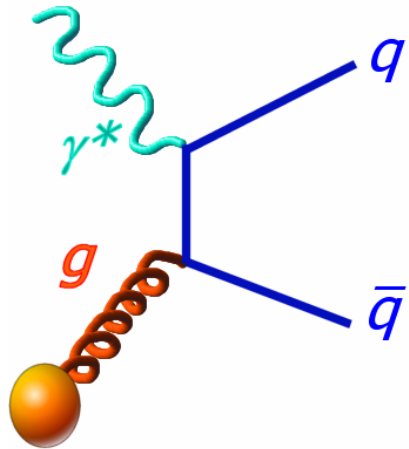
$$\Delta g/g = -1$$

$$\Delta g/g = 0$$

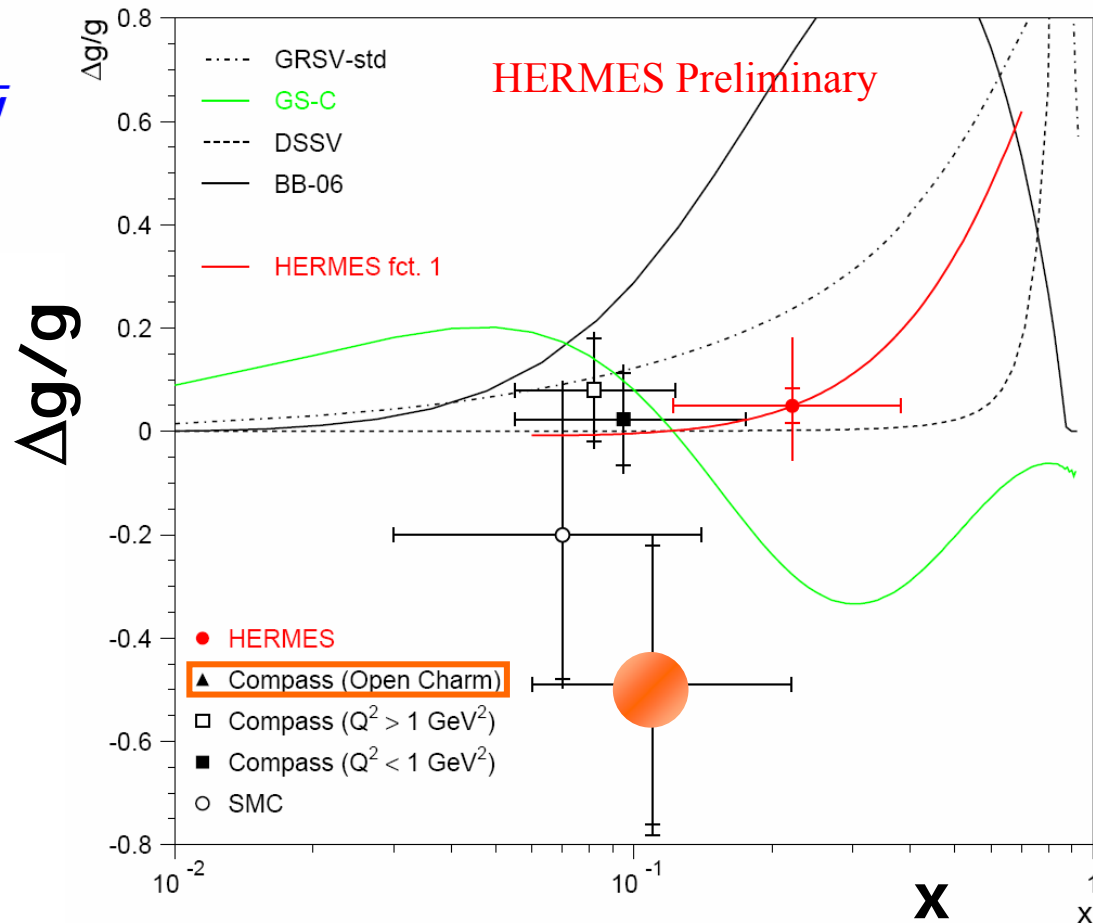
$$\Delta g/g = +1$$



direct measurement of ΔG



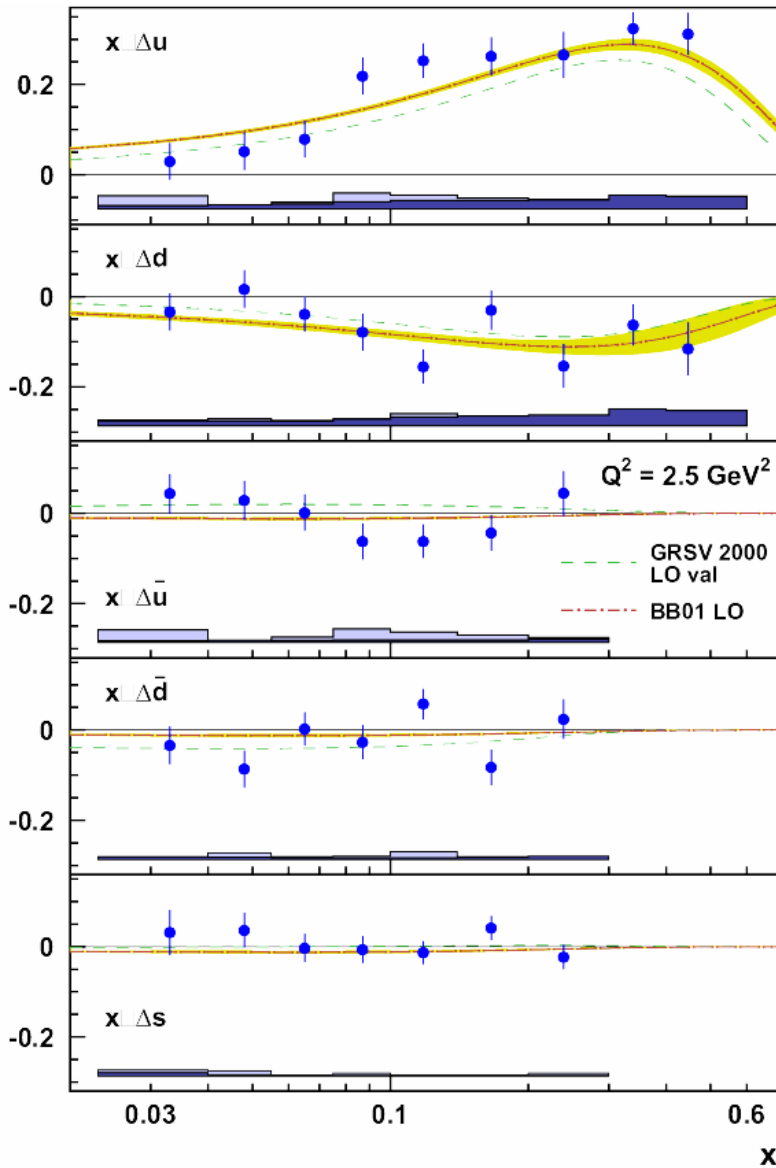
- golden channel: charm production
- hadron production at high P_T



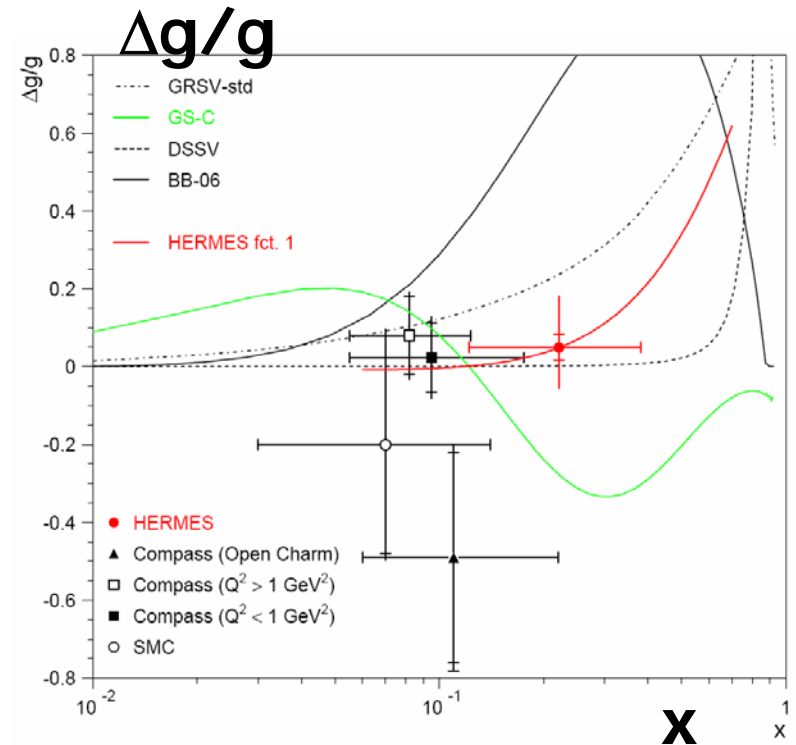
@ $x[0.06,0.3]$

$\Delta g/g \sim \text{zero!}$

quark and gluon polarisations



$\Delta \Sigma \sim 0.3$
 $\Delta G \sim 0$
 → orbital angular momentum → next talk



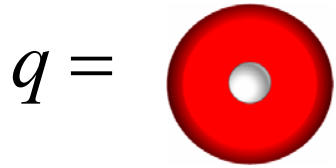
transverse spin phenomena



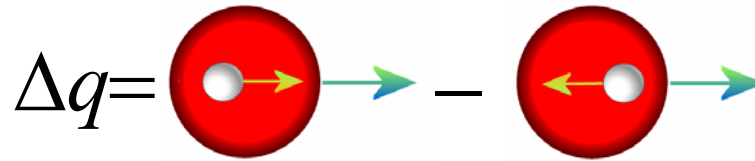
beyond collinear approximation

quark structure of the nucleon

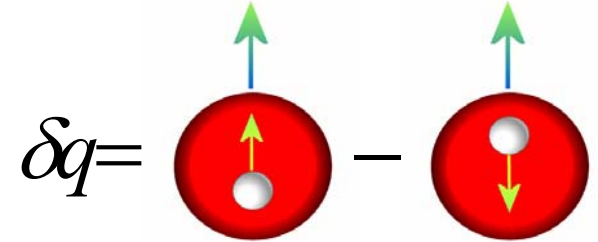
$$\Phi_{\text{Corr}}^{\text{Tw2}}(x) = \frac{1}{2} \left\{ q(x) + S_L \Delta q(x) \gamma_5 + \delta q(x) \gamma_5 \gamma^1 S_T \right\} n^+$$



unpolarised quarks
and nucleons



longitudinally polarised
quarks and nucleons



**transversely polarised
quarks and nucleons**

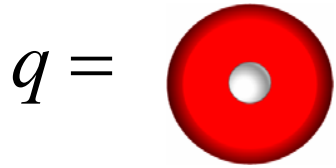
[also: $h_1^q, \Delta_T q$]

Peculiarities of δq

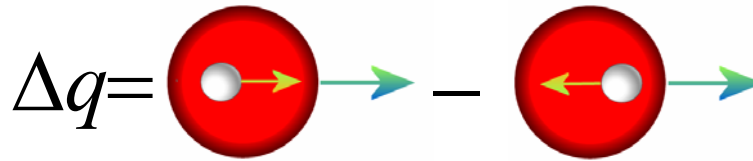
- probes relativistic nature of quarks
→ otherwise $\delta q = \Delta q$
- no gluon analog for spin-1/2 nucleon
→ different Q^2 evolution than Δq
- sensitive to *valence* quark polarisation
- only known way to obtain tensor charge

quark structure of the nucleon

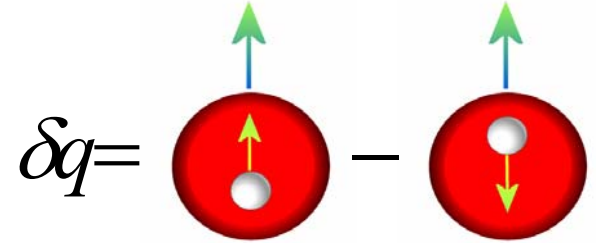
$$\Phi_{\text{Corr}}^{\text{Tw2}}(x) = \frac{1}{2} \left\{ q(x) + S_L \Delta q(x) \gamma_5 + \delta q(x) \gamma_5 \gamma^1 S_T \right\} n^+$$



$q =$
unpolarised quarks
and nucleons



$\Delta q =$
longitudinally polarised
quarks and nucleons



$\delta q =$
transversely polarised
quarks and nucleons

[also: $h_1^q, \Delta_T q$]

δq : helicity-flip of both nucleon and quark

δq is chiral-odd \rightarrow needs a chiral odd partner:

$$\text{SIDIS: } \sigma^{ep \rightarrow ehX} \propto \sum_q \sigma^{eq \rightarrow eq} \otimes \delta q(x) \otimes FF^{q \rightarrow h}(z)$$

chiral-odd
PDF

chiral-odd
FF

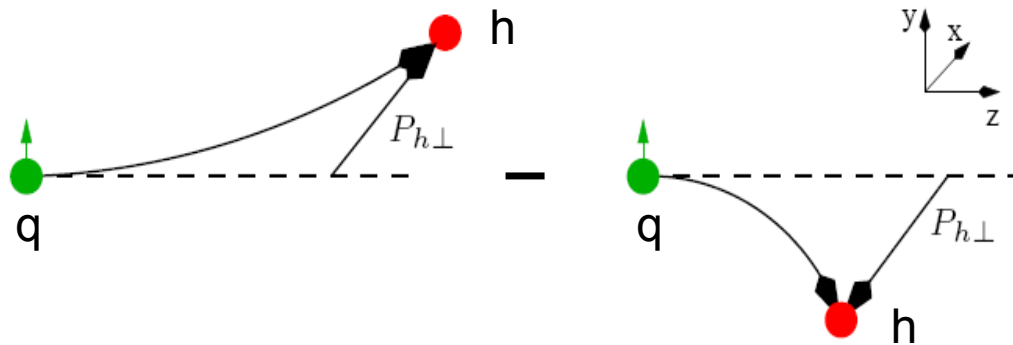
chiral-even



**chiral-odd fragmentation
function** acts as polarimeter of
transverse quark polarisation

"Collins-effect"

- **Collins FF** $H_1^\perp(z, k_T^2)$ correlates *transverse spin* of fragmenting quark and *transverse momentum* $P_{h\perp}$ of produced **hadron h**



→ left-right (azimuthal) asymmetry in the direction of the outgoing hadron

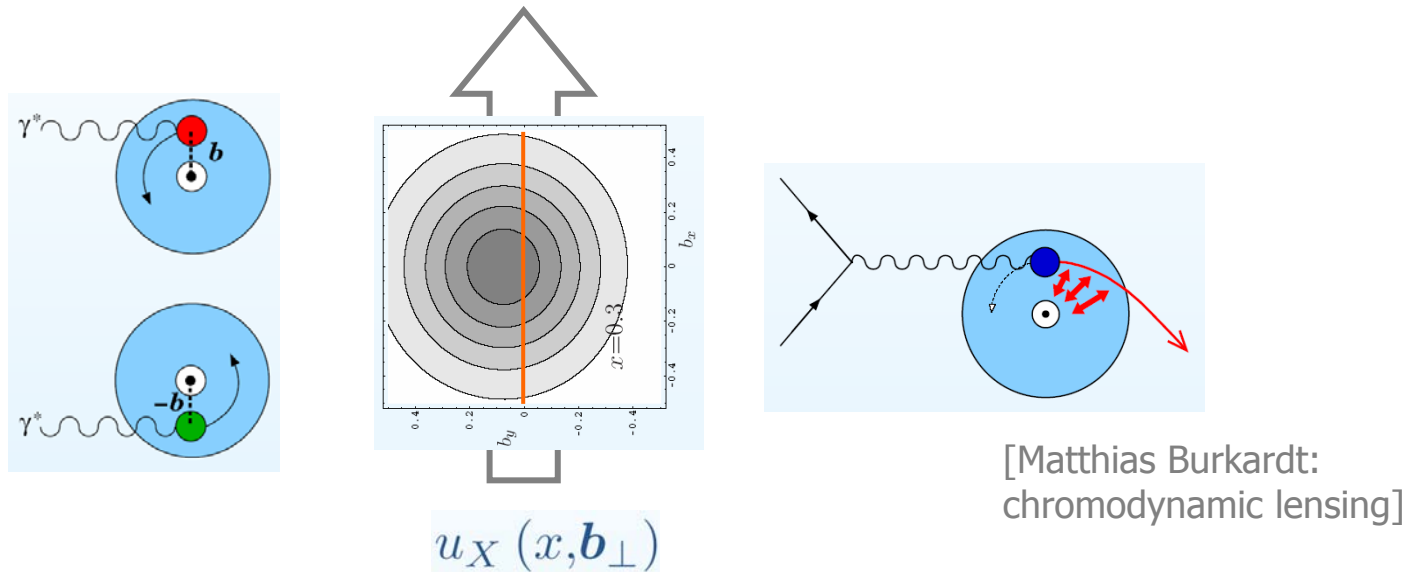
our observable: single-spin azimuthal asymmetry

is this observable unique?

"Sivers-effect"

- another mechanism that produces single-spin azimuthal asymmetries:

Sivers distribution function : distribution of unpolarised quarks in a transversely polarised nucleon → describes **spin-orbit correlations**



a non-zero Sivers fct. requires non-zero orbital angular momentum !

Sivers fct. is (naively) time-reversal *odd* !

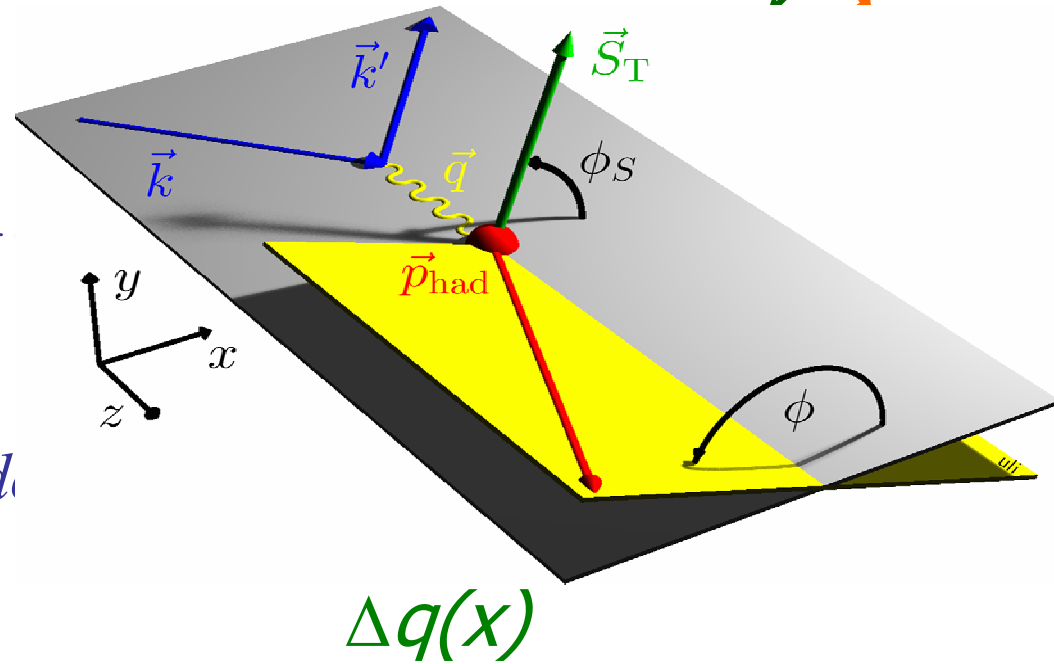
polarised DIS^h cross section

σ_{UU}

$$d\sigma^h(x, y, z, P_{h\perp}, \phi, \dots) =$$

$$d\sigma_{UU} + \cos 2\phi d\sigma_{UU} + \frac{1}{Q} q(x)$$

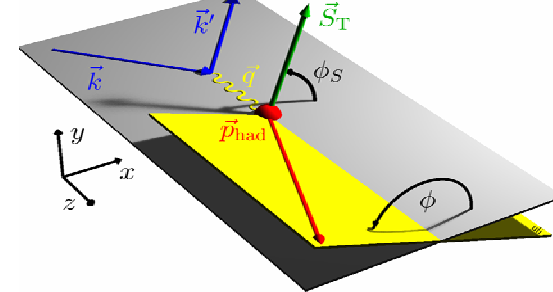
$$+ S_L \left[\sin 2\phi d\sigma_{UL} + \frac{1}{Q} \sin \phi d\sigma_{UL} \right]$$



$$+ S_T \left[\sin(\phi + \phi_S) d\sigma_{UT} + \sin(\phi - \phi_S) d\sigma_{UT} + \sin(3\phi - \phi_S) d\sigma_{UT} + \frac{1}{Q} \dots \right]$$

$$+ \lambda S_T \left[\cos(\phi - \phi_S) + \frac{1}{Q} \dots \right] + \dots$$

polarised DIS^h cross section



$$d\sigma^h(x, y, z, P_{h\perp}, \phi, \dots) =$$

$$d\sigma_{UU} + \cos 2\phi d\sigma_{UU} + \frac{1}{Q} \cos \phi d\sigma_{UU} + \lambda \frac{1}{Q} \sin \phi d\sigma_{LU}$$

$q(x)$

$$+ S_L \left[\sin 2\phi d\sigma_{UL} + \frac{1}{Q} \sin \phi d\sigma_{UL} \right] + \lambda S_L \left[d\sigma_{LL} + \frac{1}{Q} \cos \phi d\sigma_{LL} \right]$$

$$\delta q \otimes H_1^\perp + f_{1T}^\perp \otimes D_1 + h_L \dots \quad \Delta q(x)$$

$$+ S_T \left[\sin(\phi + \phi_S) d\sigma_{UT} + \sin(\phi - \phi_S) d\sigma_{UT} + \sin(3\phi - \phi_S) d\sigma_{UT} + \frac{1}{Q} \dots \right]$$

$$\delta q \otimes H_1^\perp$$

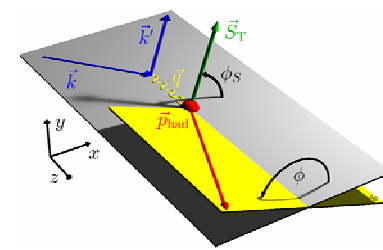
$$f_{1T}^\perp \otimes D_1$$

transversity
(Collins effect)

SIDIS with *transversely*
polarised targets but not only...

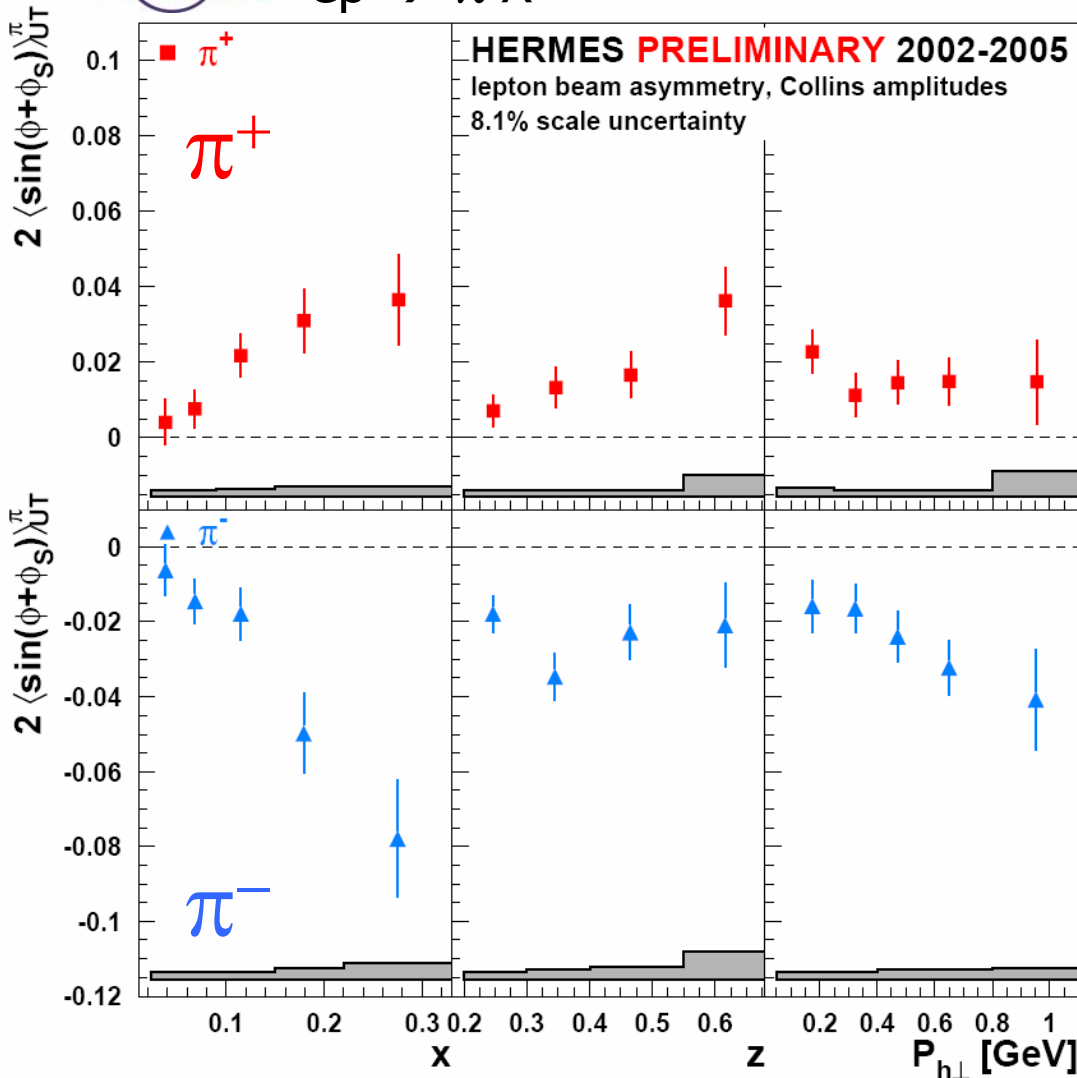
$$\dots \left[\sin(\phi - \phi_S) + \frac{1}{Q} \dots \right] + \dots$$

Collins asymmetries



$ep \rightarrow \pi X$

$$\delta q(x) \otimes H_1^{\perp q}(z)$$



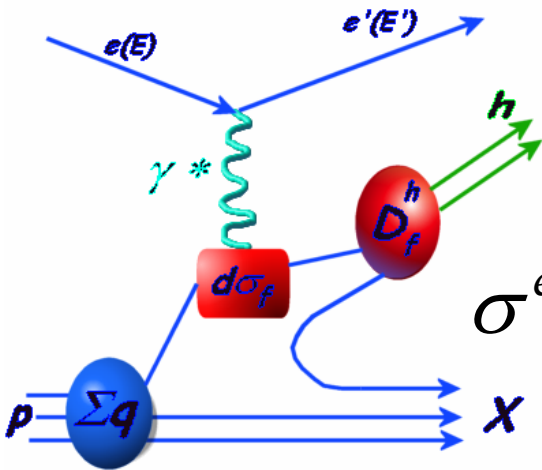
first time: *transversity* & *Collins FF* are **non-zero!**

- π^+ asymmetries positive – no surprise: u-quark dominance and expect $\delta q > 0$ since $\Delta q > 0$

- large negative π^- asymmetries – **ARE** a surprise: suggests the disfavoured Collins FF being large and with opposite sign:

$$H_1^{\perp, \text{disfav}}(z) \approx -H_1^{\perp, \text{fav}}(z)$$

extracting *transversity*



$$\sigma^{ep \rightarrow ehX}$$

$$\propto \sum_q$$

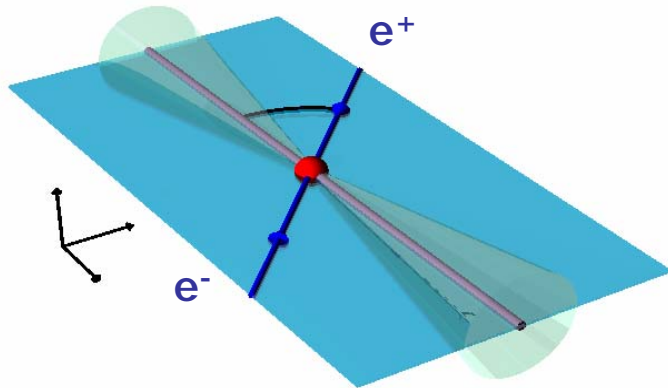
$$\sigma^{eq \rightarrow eq}$$

$$\otimes \delta q(x)$$

$\otimes FF^{q \rightarrow h}(z)$

spin-dependent
fragmentation
function

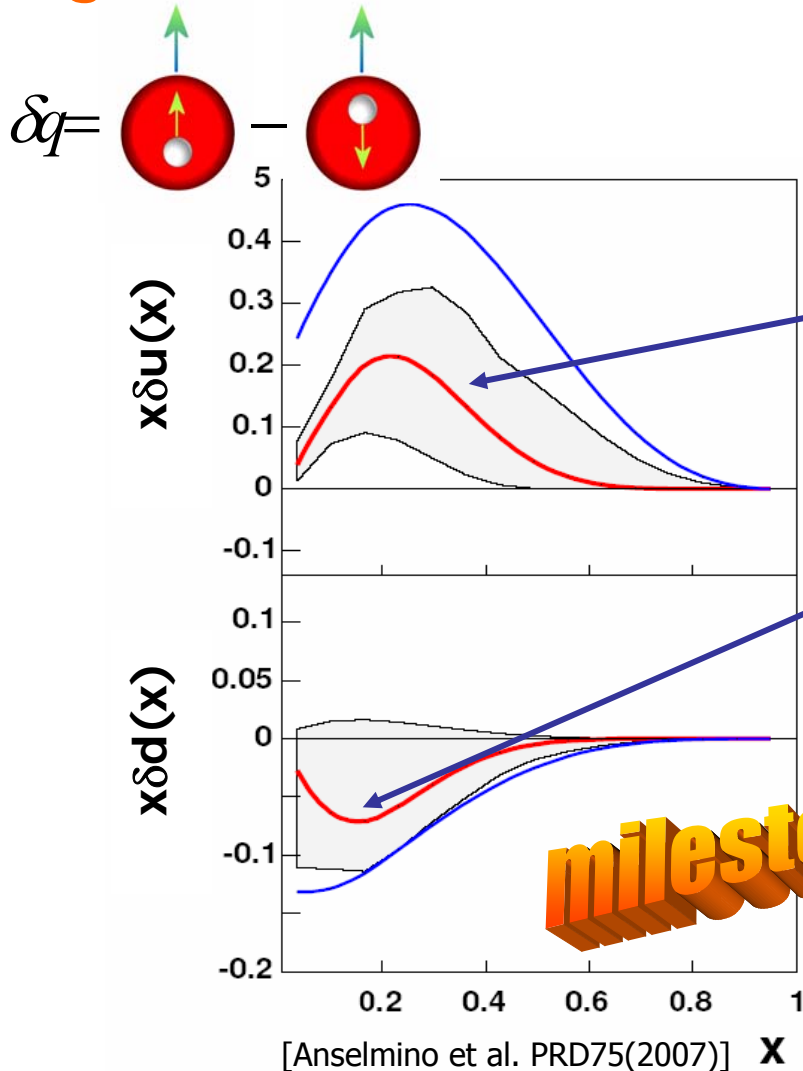
→
 e^+e^-



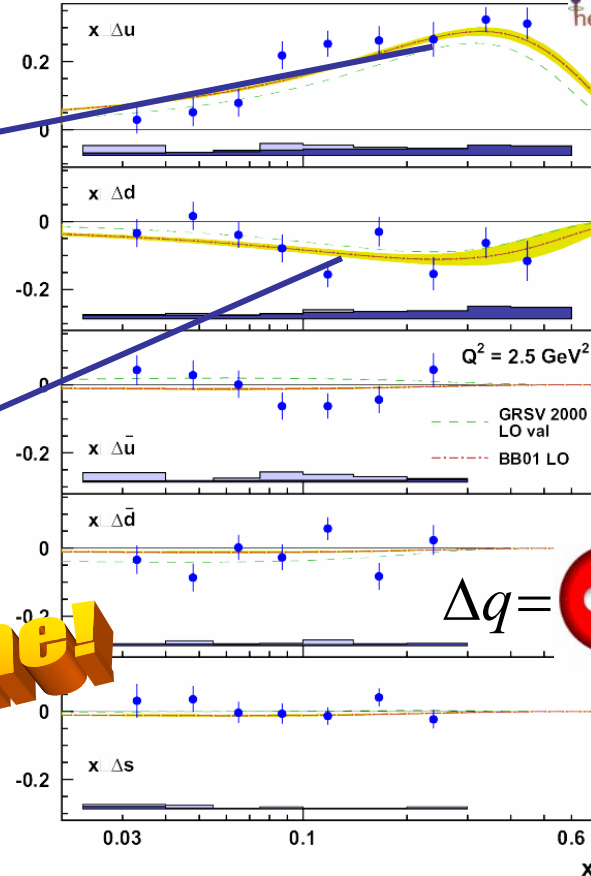
$$e^+e^- \rightarrow \pi_{\text{jet1}}^+ \pi_{\text{jet2}}^- X$$

first glimpse of transversity

global, simultaneous fit:



compare to Δq :



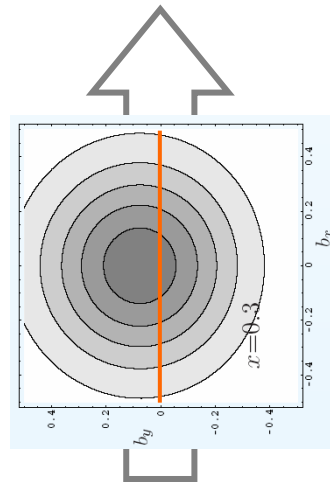
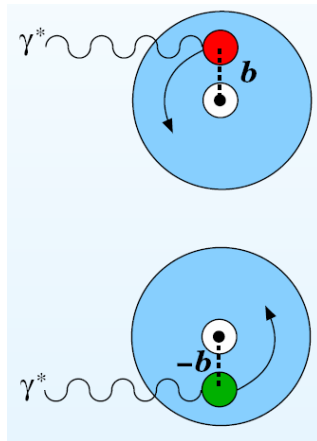
milestone!



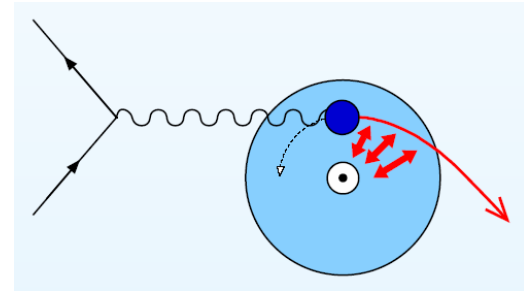
all details:
U. D'Alesio

spin-orbit structure

Sivers function:



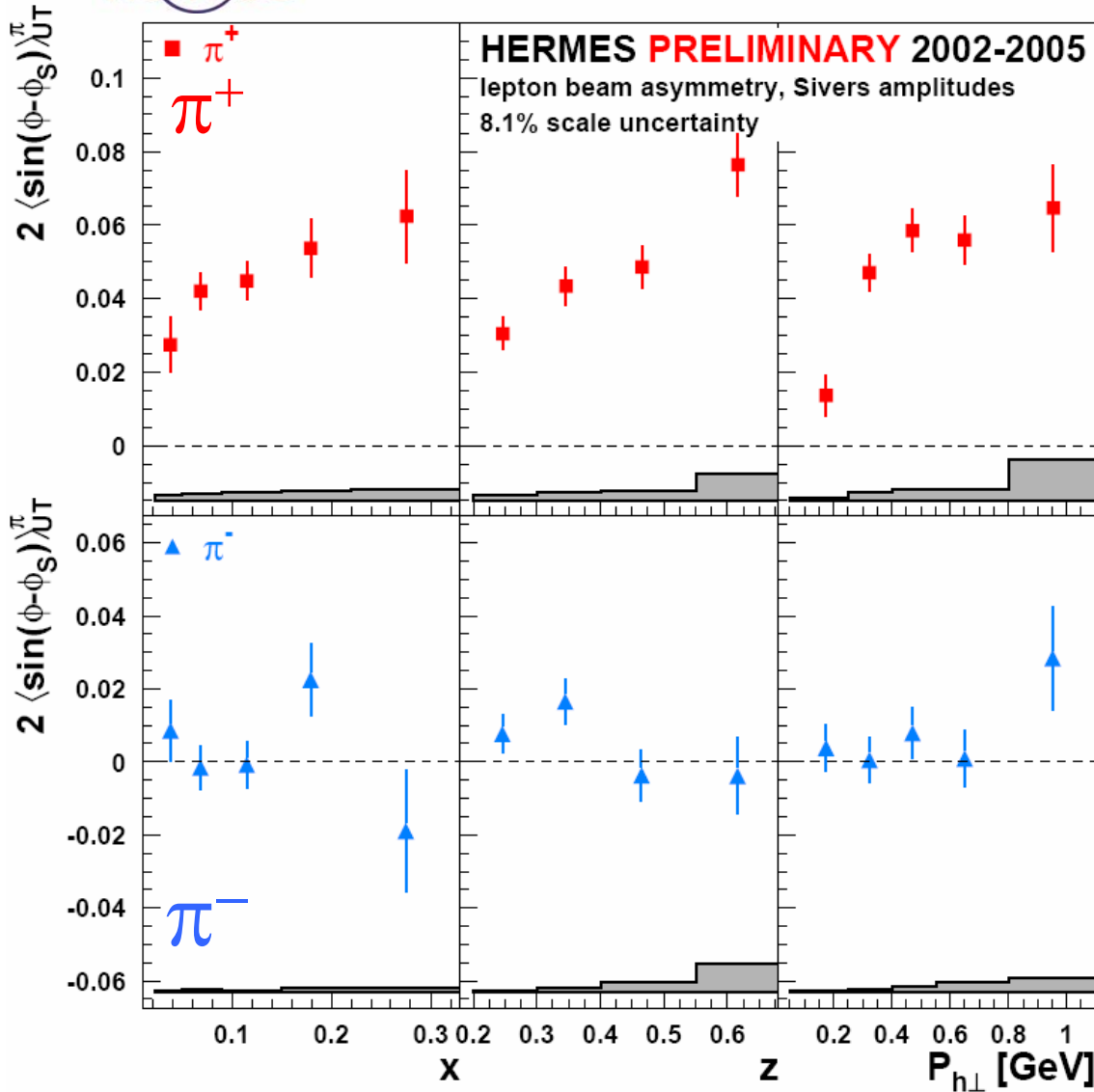
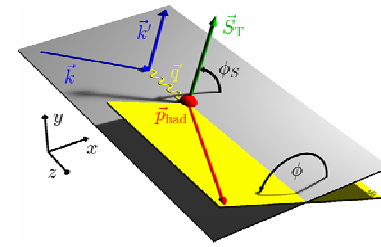
$$u_X(x, \mathbf{b}_\perp)$$



[Matthias Burkardt]

a non-zero Sivers fct. requires non-zero orbital angular momentum !

Sivers asymmetries



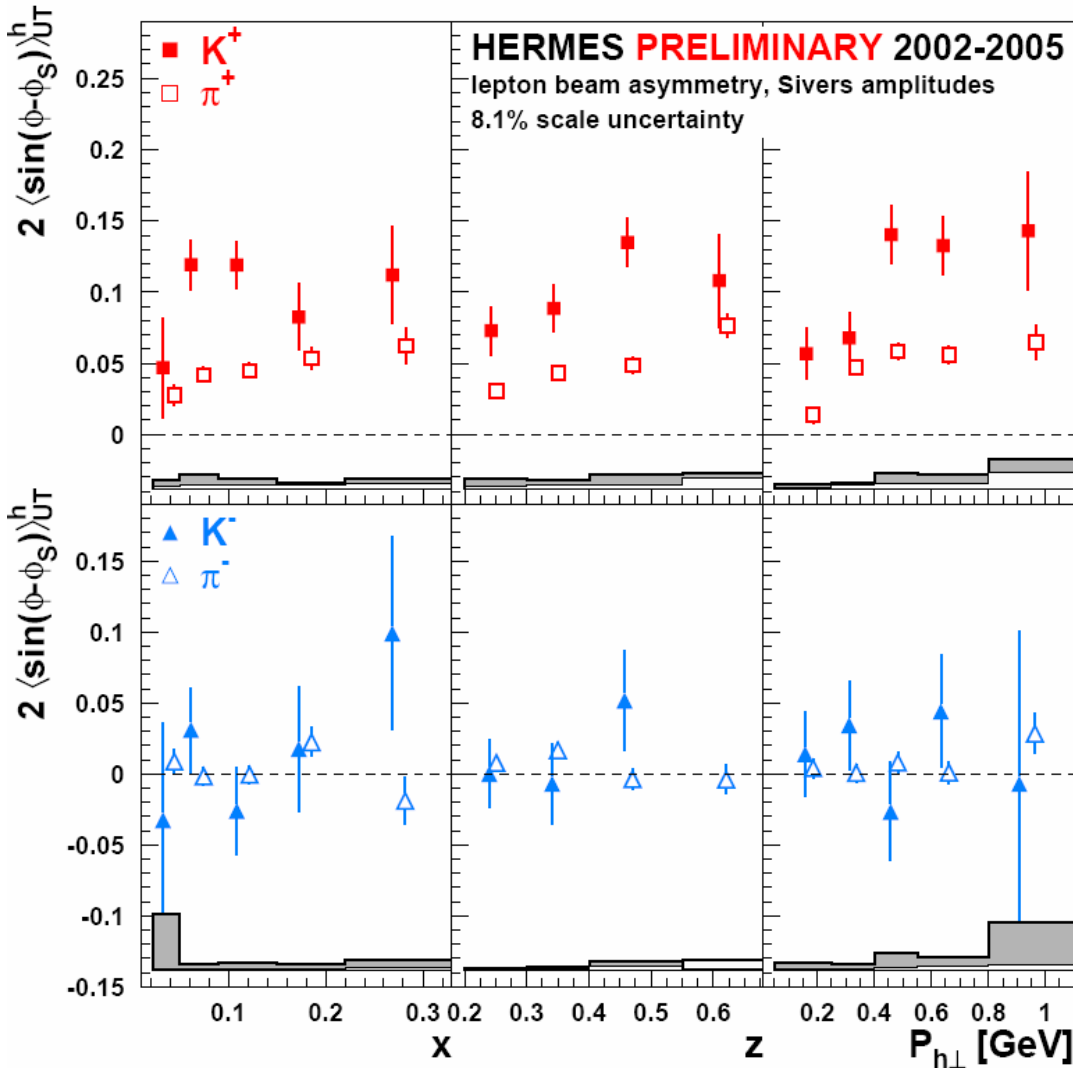
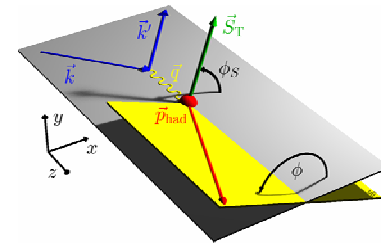
$$f_{1T}^{\perp q}(x) \otimes D_1^q(z)$$

π^+ are substantial and positive:

- first unambiguous evidence for a **non-zero T-odd** distribution function in DIS
- a signature for quark orbital angular momentum !



Sivers asymmetries



$$f_{1T}^{\perp q}(x) \otimes D_1^q(z)$$

• **SURPRISE:**

K^+ amplitude 2.3 ± 0.3 times larger than for π^+

→ conflicts with usual expectations based on u-quark dominance

→ suggests substantial magnitude of the Sivers fct. for sea quarks

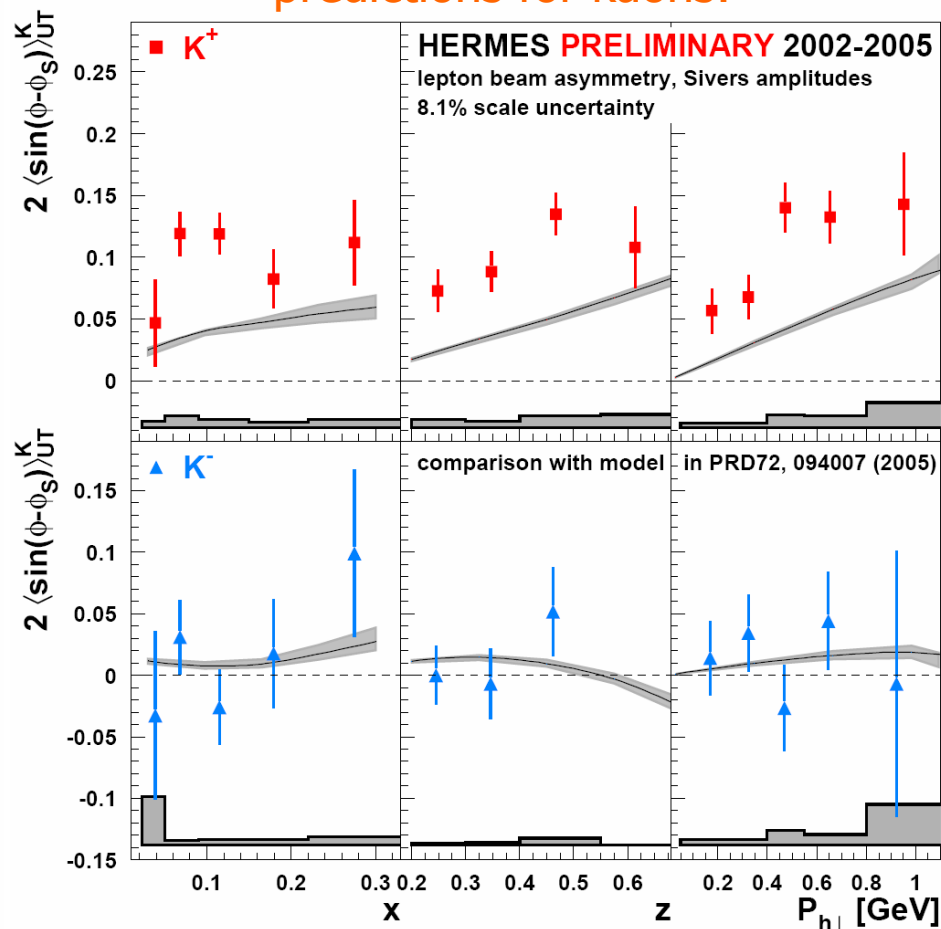
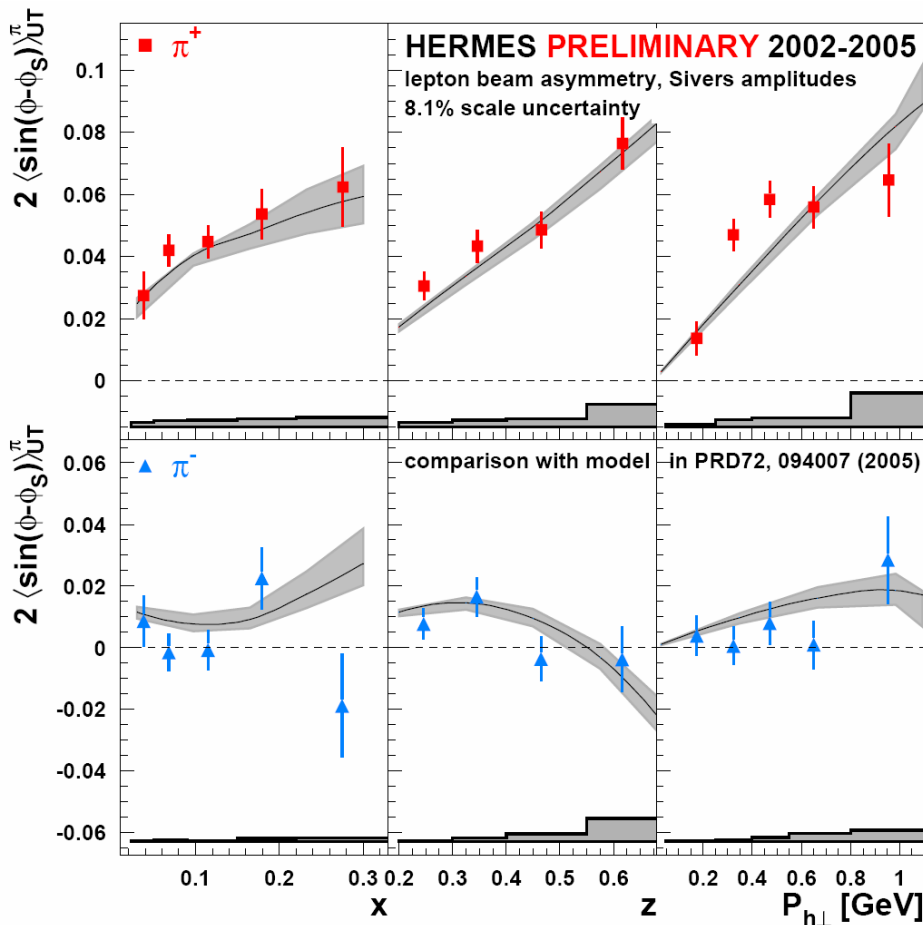
$$K^+ = |u\bar{s}\rangle \quad \pi^+ = |u\bar{d}\rangle$$

comparison to models

[Anselmino et al. PRD72(2005)]

excellent description of pion data
but: cannot constrain sea

predictions for kaons:



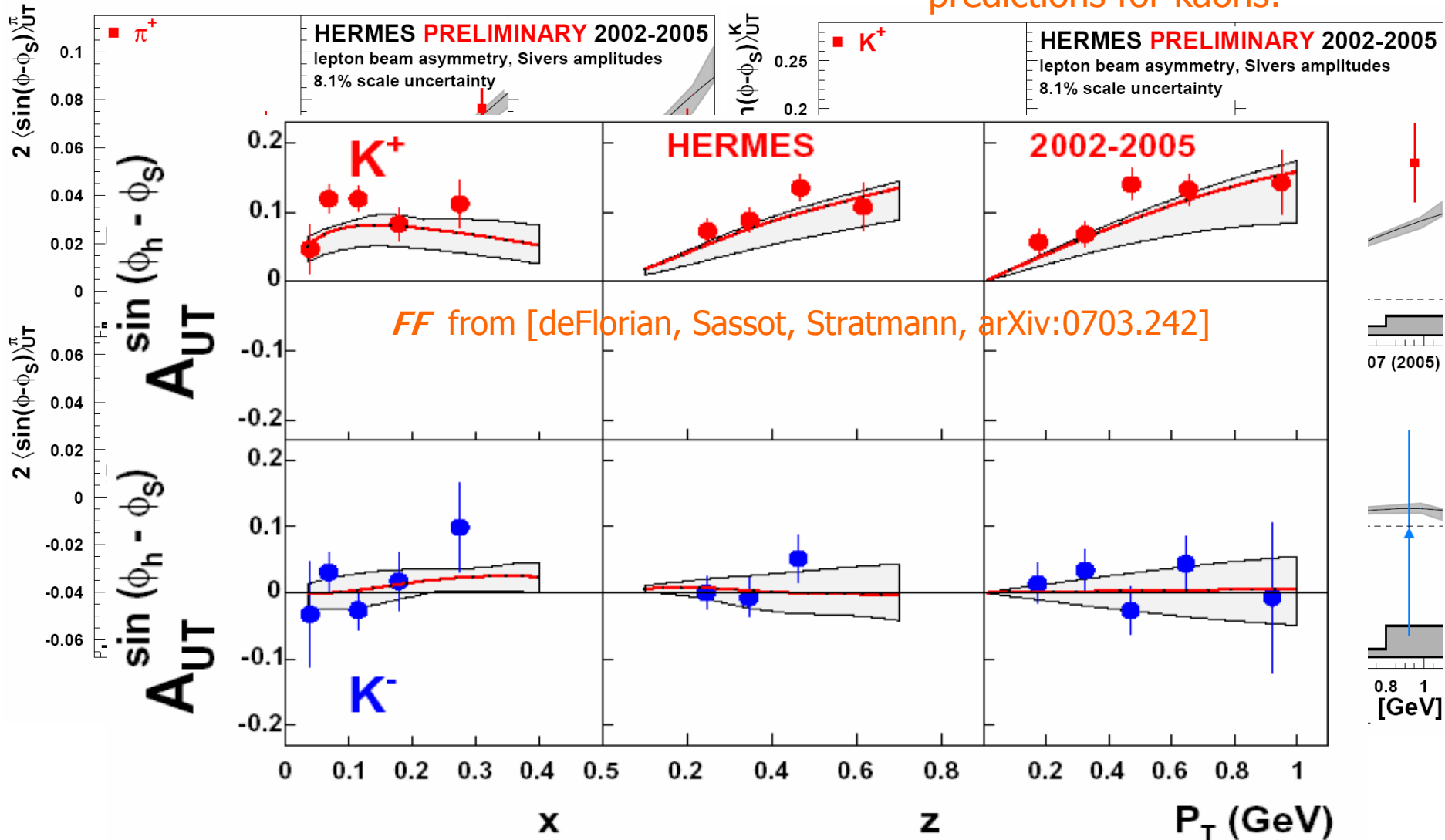
kaon data suggest that sea quark contribution may be significant

comparison to models

[Anselmino et al. PRD72(2005)]

excellent description of pion data
but: cannot constrain sea

predictions for kaons:



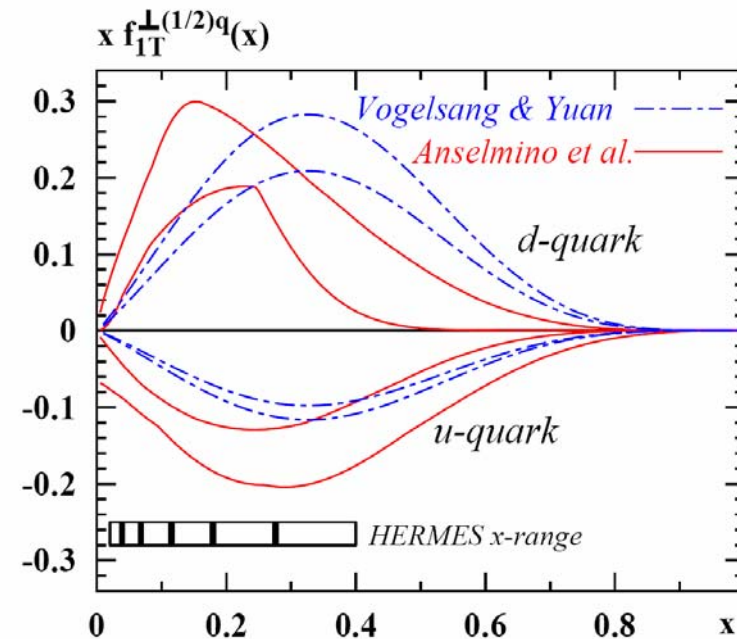
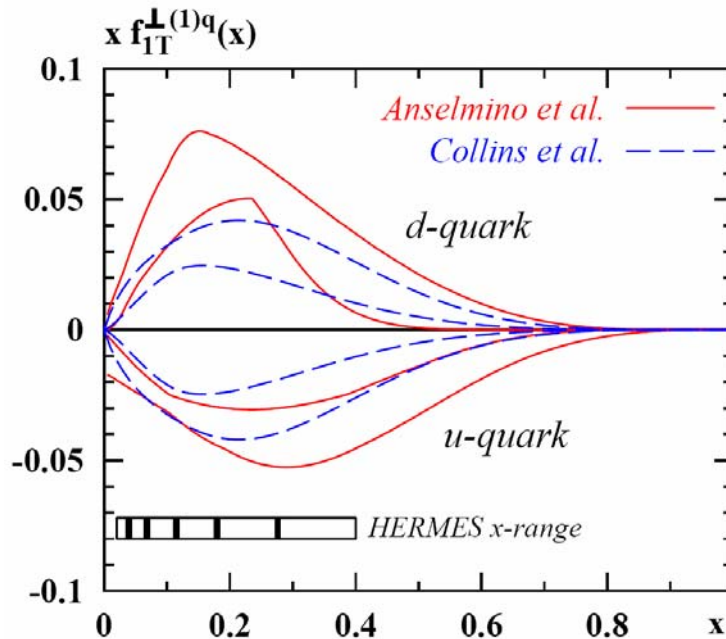
extracting the *Sivers* function



$$A_{UT}^{\sin(\phi-\phi_S)} \propto$$

$$f_{1T}^{\perp q}(x) \otimes D_1^q(z)$$

usual unpolarised
fragmentation
function



ToDo:

crucial test of pQCD:

$$(f_{1T}^{\perp q})_{DIS} \approx - (f_{1T}^{\perp q})_{DY}$$



Polarized Antiproton Experiments

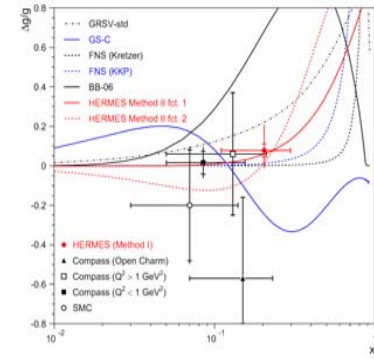
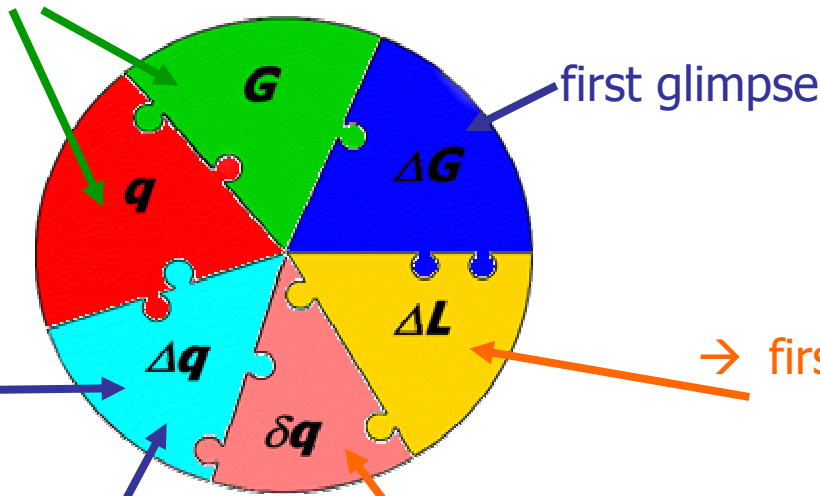
@FAIR (GSI)

structure of the nucleon

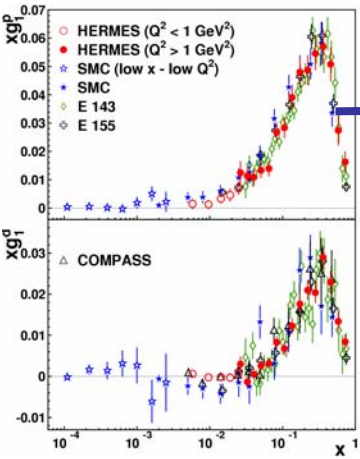
from unpolarised DIS

from polarised DIS :

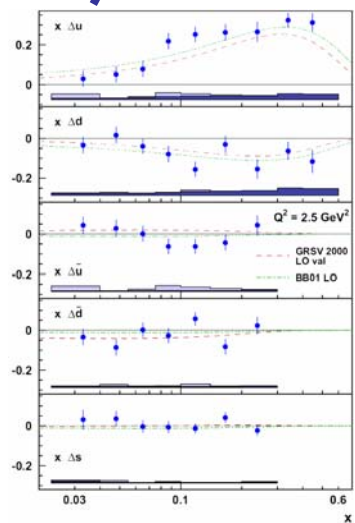
$$\rightarrow a_0 = \Delta\Sigma = 0.330 \pm 0.025^{(exp)}$$



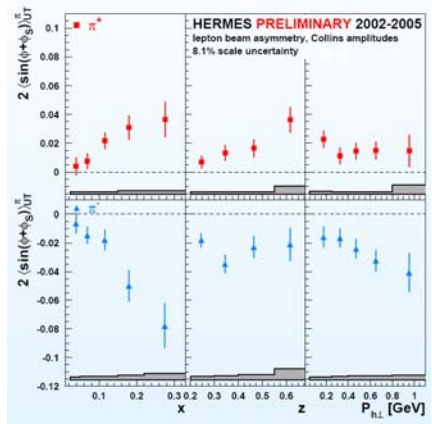
→ first signals of GPDs: $J_u + J_d$
 → see next talk !



→ direct flavour decomposition



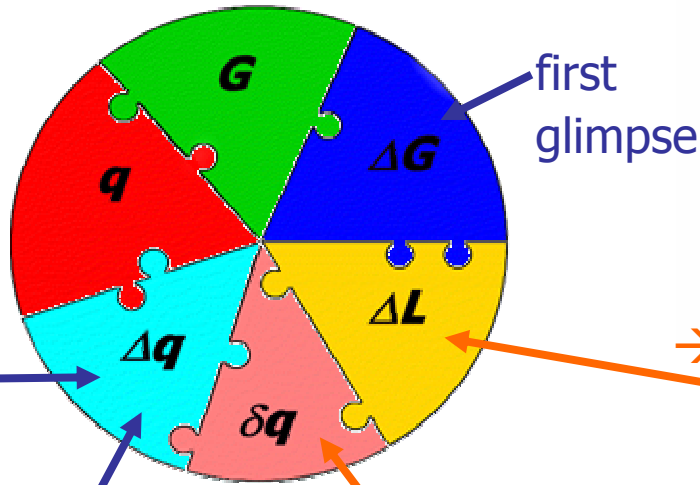
first extraction of δq , spin-orbit structures & OAM



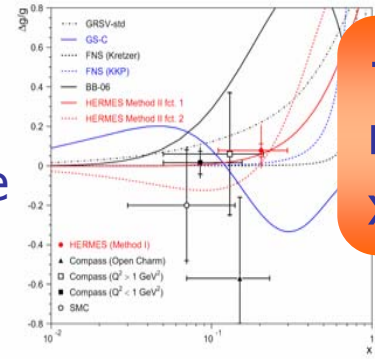
new concepts:
GPDs → 3D picture of the nucleon
TMDs → beyond collinear approximation

structure of the nucleon

-the open tasks-



first glimpse

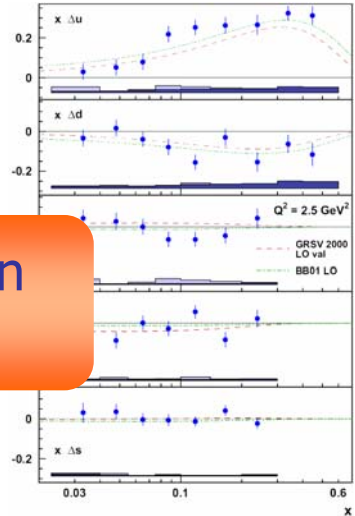
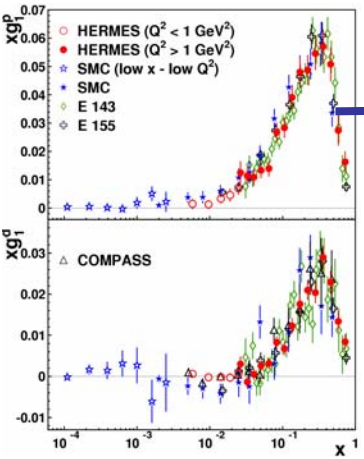


→ detailed measurement of x-dependence

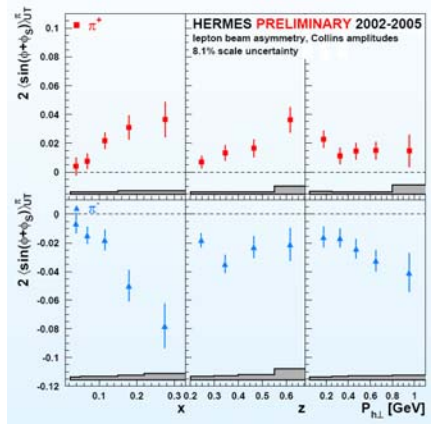
→ first signals of GPDs: $J_u + J_d$

→ see next talk !

→ detailed measurement in 3 kine variables



first extraction of δq



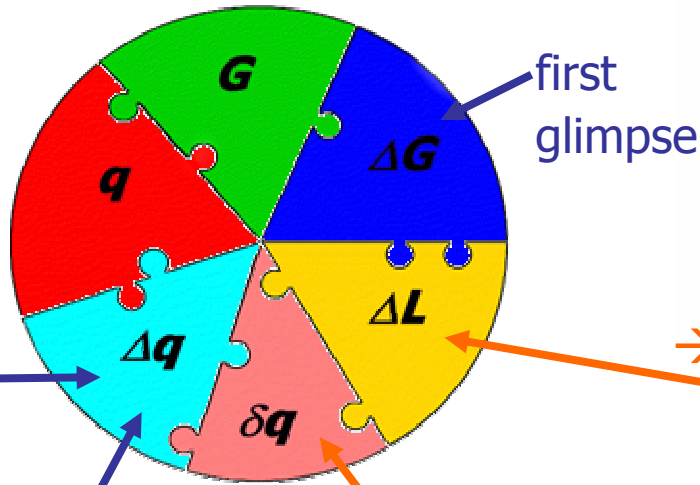
→ detailed measurement in 2 kine variables

→ extrapolation $x \rightarrow 0, x \rightarrow 1$

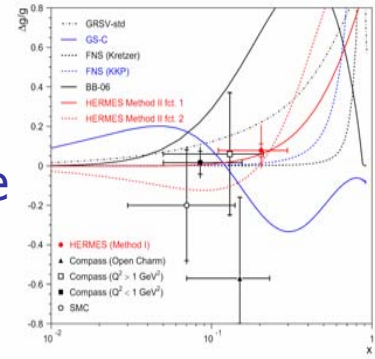
structure of the nucleon

-the future facilities-

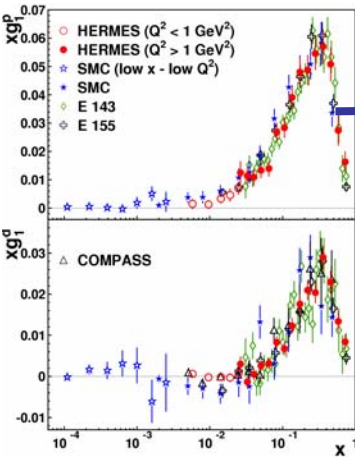
RHIC,
EIC,
(JPARC)



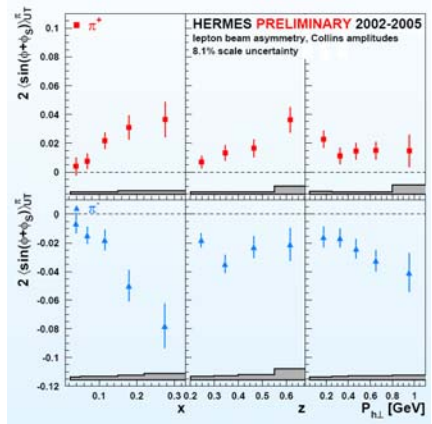
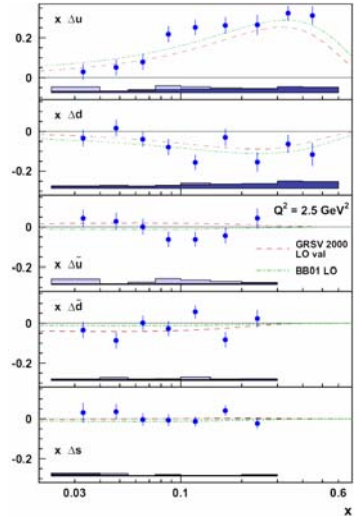
first glimpse



→ first signals of GPDs: $J_u + J_d$
→ see next talk !



first extraction of δq



JLab@12GeV
EIC

polarised
collider:
EIC

EIC,
FAIR

Backup slides



multiplicities compared to theory

new FF from combined NLO analysis of single-inclusive hadron production in e^+e^- , pp and DIS

[deFlorian,Sassot,Stratmann arXiv:0708.0769]

