

# Polarized Parton Distributions

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Nucleons and Nuclei"  
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$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + L_z$$

- Some Phenomenological Models
- Quark and Gluon Polarization
- Studies with Polarized  $\Lambda$  Production
- New Structures: Transversity and Friends

# Some Phenomenological Models

## Non-relativistic Quark Model

Pure valence description of constituent quarks:

$$\Delta u = +4/3, \quad \Delta d = -1/3 \quad \rightarrow \quad \Delta\Sigma = 1$$

## Relativistic Quark Model

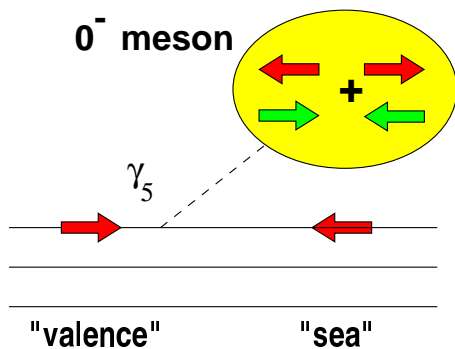
*Jaffe, Manohar, NP B337 (1990) 509*

Relativistic current quarks with light masses: orbital angular momentum is important, and accounts for the deficit of  $\Delta\Sigma$ .

$$\Delta\Sigma \simeq 0.60 - 0.75, \quad L_q = \frac{1}{2}(1 - \Delta\Sigma)$$

## Meson Cloud Models

*Li, Cheng, hep-ph/9709293*



Quark sea generated by cloud of pseudoscalar mesons.

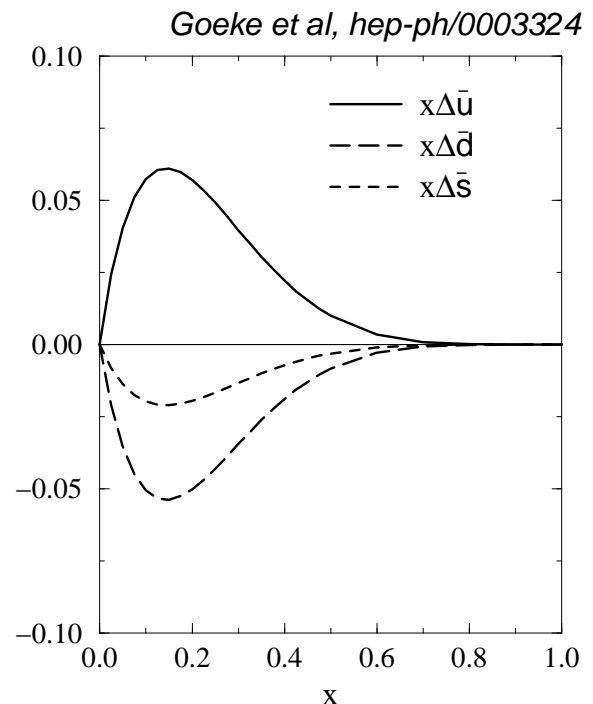
- $\Delta q_{valence} > 0$
- $\Delta q_{sea} < 0$ , but ...
- $\Delta\bar{q} = 0$

## Large $N_c$ Limit and the Chiral-Quark Soliton Model

Nucleon = chiral soliton in pion field.

$$\begin{aligned} \Delta\bar{u} - \Delta\bar{d} &\sim N_c^2 \\ \Delta\bar{u} + \Delta\bar{d} &\sim N_c \end{aligned}$$

⇒ Light sea quarks have significant polarization, but with  $\Delta\bar{u} \simeq -\Delta\bar{d}$ .

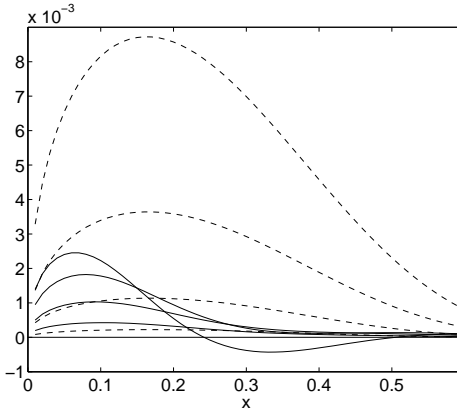


# Rho Meson Cloud

## Rho: lightest polarizable meson

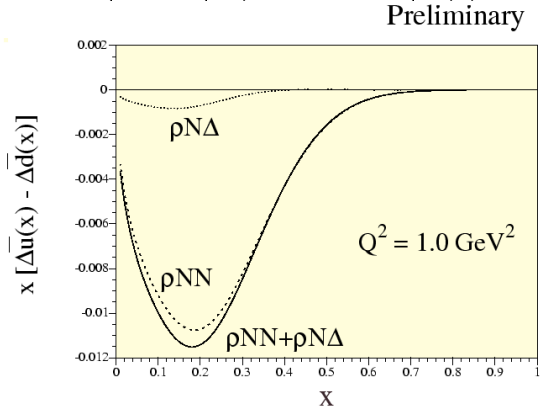
Fries, Scäfer, PLB 443 (1998) 40

$$x (\Delta \bar{d}(x) - \Delta \bar{u}(x))$$



Miyama, DIS 2001

$$x (\Delta \bar{u}(x) - \Delta \bar{d}(x))$$

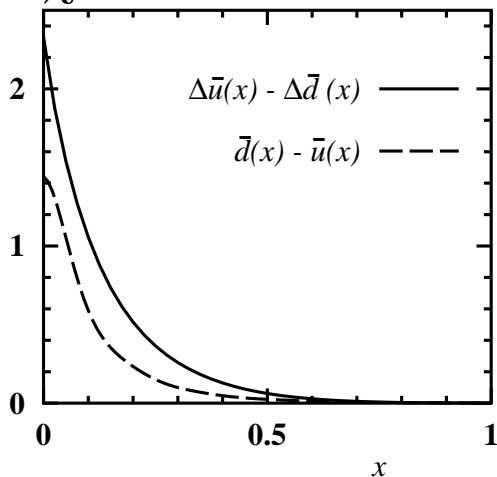


$$\rightarrow \Delta \bar{u} - \Delta \bar{d} < 0 !$$

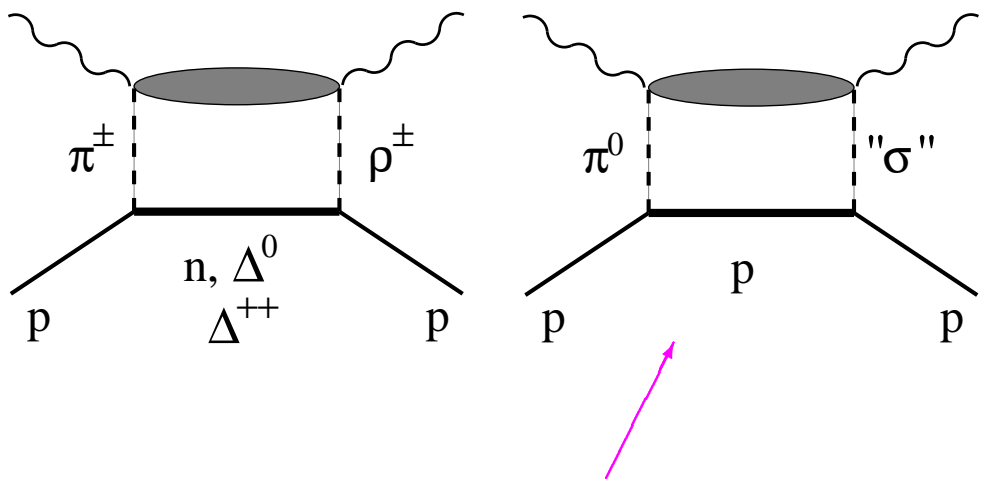
## Interference Terms

Apparent discrepancy with  $\chi$ QSM might be resolved by interference terms ...

### $\chi$ QSM Prediction



Boreskov, Kaidalov EPJC 10 (1999) 143



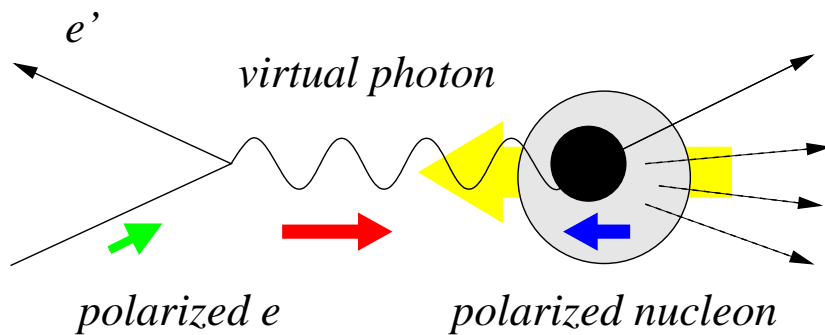
Calculation in progress: R. Fries, Ch. Weiss

Large contributions indicated ...

N.C.R. Makins, Santorini 2001

# Spin-dependent Deep Inelastic Scattering

In polarized DIS, using polarized lepton beams and polarized nuclear targets, one probes the polarization of the partons in the nucleon.



$$F_1 = \frac{1}{2} \sum_i e_i^2 q_i$$

$$g_1 = \frac{1}{2} \sum_i e_i^2 \Delta q_i$$

$$\Delta q_i = q_i^\uparrow - q_i^\downarrow$$

## QCD Fits to $g_1(x, Q^2)$ at NLO

$$g_1^{p(n)} = \frac{1}{9} \left( C_{NS} \otimes \left[ \pm \frac{3}{4} \Delta q_3 + \frac{1}{4} \Delta q_8 \right] + C_S \otimes \Delta \Sigma + 2N_f C_g \otimes \Delta g \right)$$

Using  $g_1$  measurements on both proton and neutron (deuterium) targets, one can *in principle* separate these polarized PDF's:

$$\Delta q_3(x, Q^2) = \Delta u - \Delta d,$$

$$\Delta q_8(x, Q^2) = \Delta u + \Delta d - 2\Delta s,$$

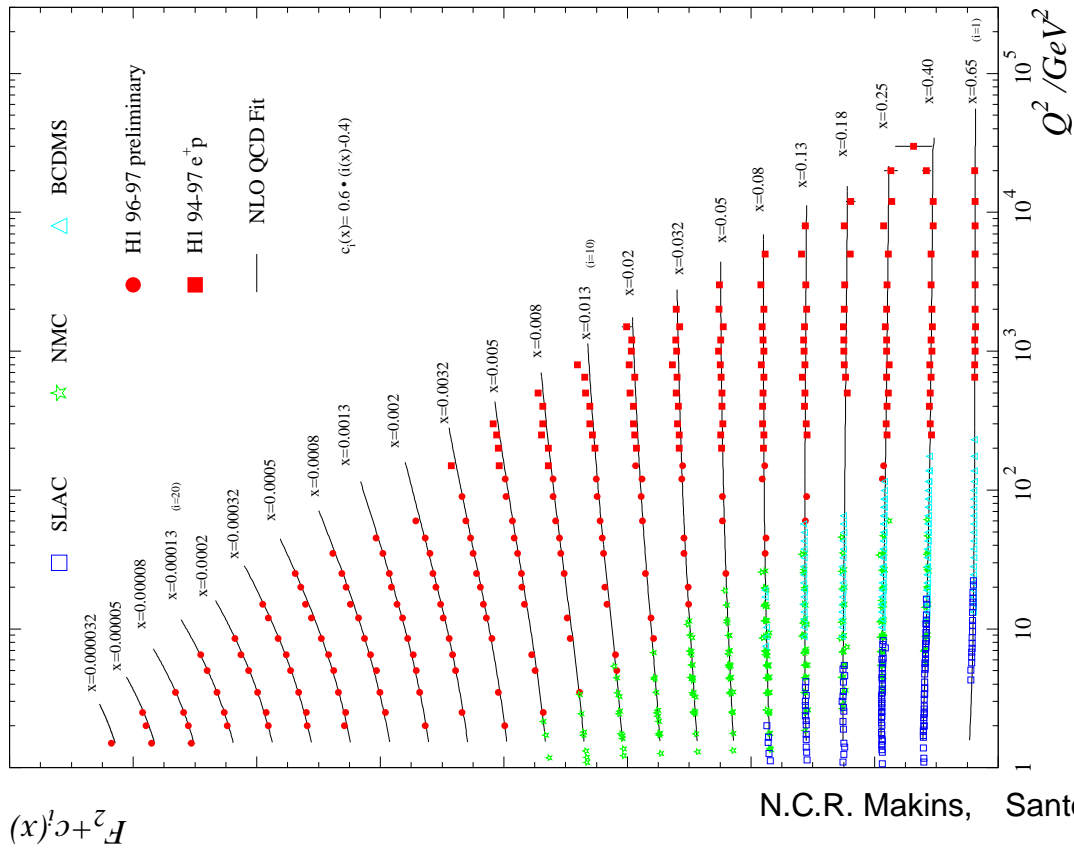
$$\Delta \Sigma(x, Q^2) = \Delta u + \Delta d + \Delta s,$$

$$\Delta g(x, Q^2)$$

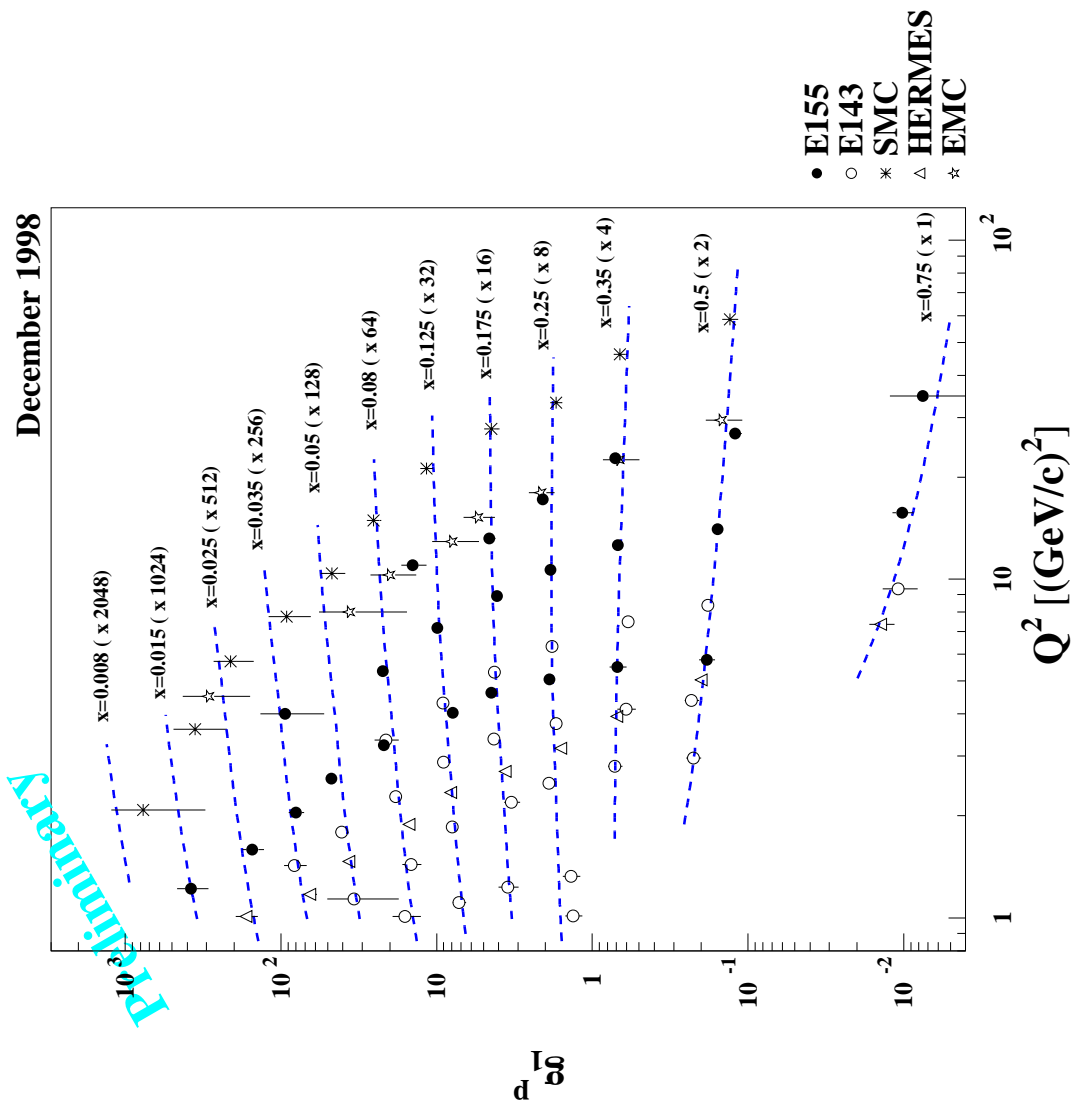
by exploiting the different  $Q^2$ -dependent behaviour of each term.

However ...

# World data on $F_1^p$



# World data on $g_1^p$



## QCD Fits to $g_1(x, Q^2)$ : Challenges

- Precision and range of present polarized data is insufficient to perform a complete separation. Present analyses also use information from **hyperon  $\beta$ -decay** to constrain non-singlet matrix elements:

$$a_3 = \Delta q_3 = F + D = 1.2601 \pm 0.0025 \text{ (Bj. sum rule)}$$

$$a_8 = \Delta q_8 = 3F - D = 0.579 \pm 0.032$$

However, expression for  $a_8$  depends on assumption of **SU(3)-symmetry** among hyperons, which is known to be inexact ...

- **Momentum sum rule** not available. In unpolarized case:

$$\int dx x [u(x) + d(x) + s(x) + g(x)] = 1$$

In polarized case, the unknown angular momentum appears:

$$\int dx \left[ \frac{1}{2} \Delta \Sigma(x) + \Delta g(x) \right] = \frac{1}{2} - L$$

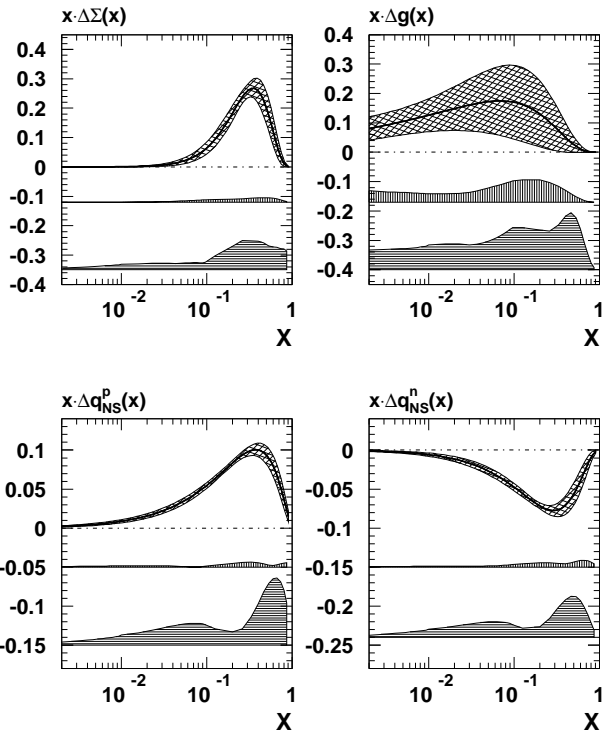
- The net quark polarization  $\Delta \Sigma(Q^2)$  is maximally **scheme dependent** ... connection between measured  $\Gamma_1^p = \int dx g_1$  and  $\Delta \Sigma$  may involve the gluon polarization.

⇒ In the  $\overline{\text{MS}}$  scheme,  $\Delta \Sigma$  is not conserved.

⇒ In the AB or JET schemes,  $\Delta \Sigma$  is conserved:

$$\Delta \Sigma(Q^2)_{\overline{\text{MS}}} = \Delta \Sigma_{\text{AB(JET)}} - 3 \frac{\alpha_s(Q^2)}{2\pi} \Delta g(Q^2)_{\text{AB(JET)}}$$

# SMC: NLO QCD Fit



**First moments at  $Q_0^2 = 1 \text{ GeV}^2$ :**

*SMC, PRD 58 (1998) 112002*

$$\Delta\Sigma_{(\overline{MS})} = 0.19 \pm 0.05 \pm 0.04$$

$$\Delta\Sigma_{(AB)} = 0.38 \begin{matrix} +0.03 & +0.03 & +0.03 \\ -0.03 & -0.02 & -0.05 \end{matrix}$$

$$\Delta g_{(AB)} = 0.99 \begin{matrix} +1.17 & +0.42 & +1.43 \\ -0.31 & -0.22 & -0.45 \end{matrix}$$

## Sensitivity to SU(3) symmetry breaking

Consider variation of  $a_8$  matrix element from hyperon  $\beta$ -decay, around SU(3)-symmetric value of  $3F - D = 0.58$ . In JET scheme:

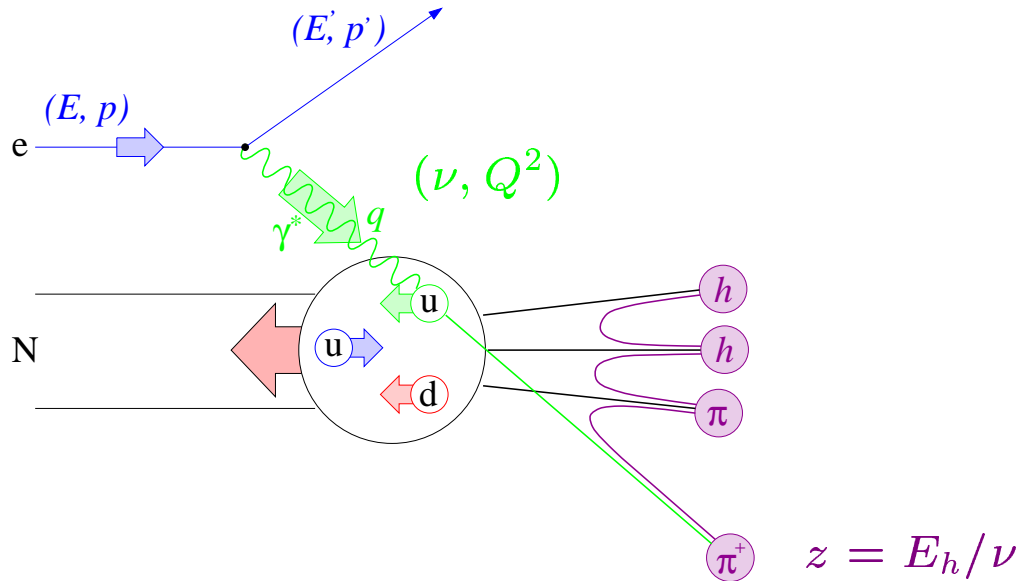
*E.Leader, A.Sidorov, D.Stamenov, hep-ph/0004106*

$a_8$	$\chi^2/\text{DOF}$	$\Delta\Sigma$	$\Delta g$	$\Delta s$
0.40	0.82	$0.34 \pm 0.05$	$0.13 \pm 0.14$	$-0.02 \pm 0.01$
0.58	0.83	$0.40 \pm 0.04$	$0.57 \pm 0.14$	$-0.06 \pm 0.01$
0.86	0.82	$0.40 \pm 0.06$	$0.84 \pm 0.30$	$-0.15 \pm 0.02$

$\Rightarrow$  Gluon and strange quark polarizations are strongly dependent on the SU(3)-symmetry assumption.

# Quark Polarization from Semi-Inclusive DIS

In semi-inclusive DIS a hadron  $h$  is detected in coincidence with the scattered lepton



## Flavour Tagging

The flavour content of the final state hadrons is related to the flavour of the struck quark through the agency of the **fragmentation functions**  $D_q^h(z, Q^2)$ . In LO QCD:

$$A_1^h(x, Q^2) = \frac{\int_{z_{\min}}^1 dz \sum_q e_q^2 \Delta q(x, Q^2) \cdot D_q^h(z, Q^2)}{\int_{z_{\min}}^1 dz \sum_q e_q^2 q(x, Q^2) \cdot D_q^h(z, Q^2)}$$

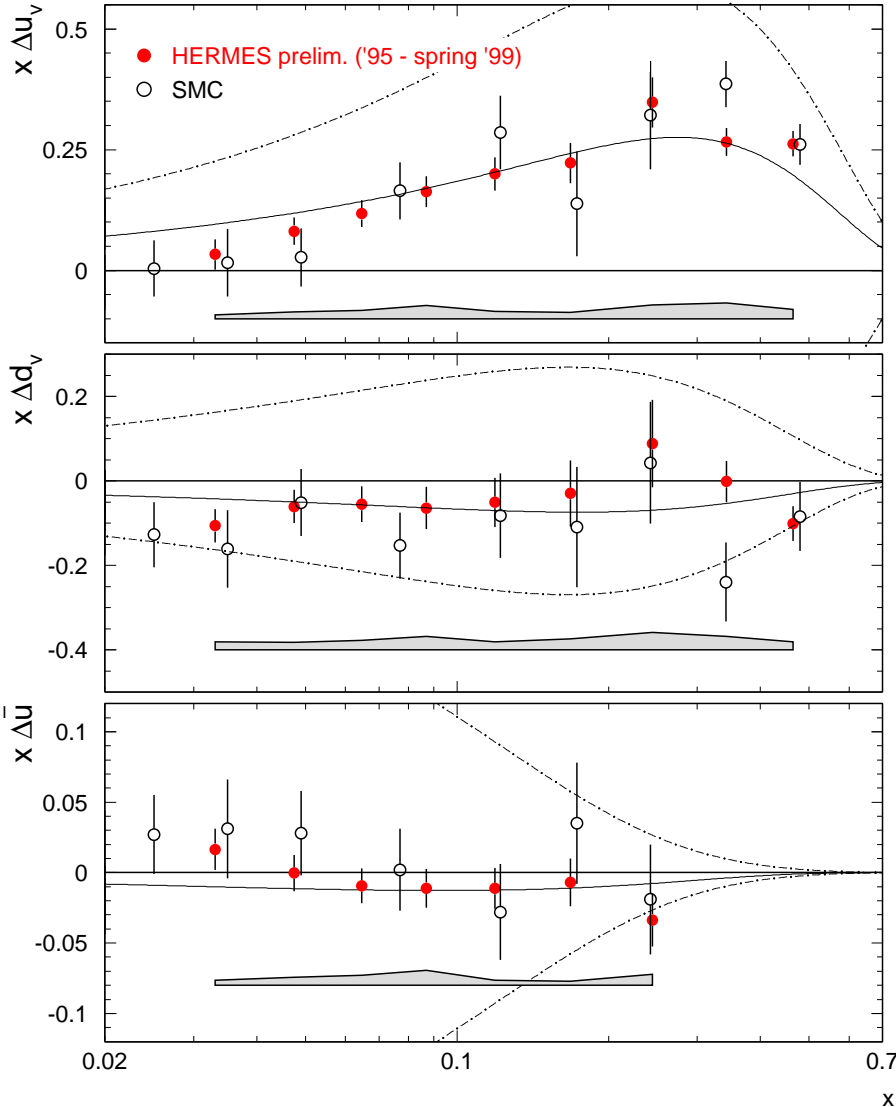
Can rewrite in terms of a **purity matrix** :

$$A_1^h(x, z) = \sum_q P_q^h(x, z) \frac{\Delta q(x)}{q(x)}$$

Purities are *spin-independent*, and may be computed via Monte Carlo.



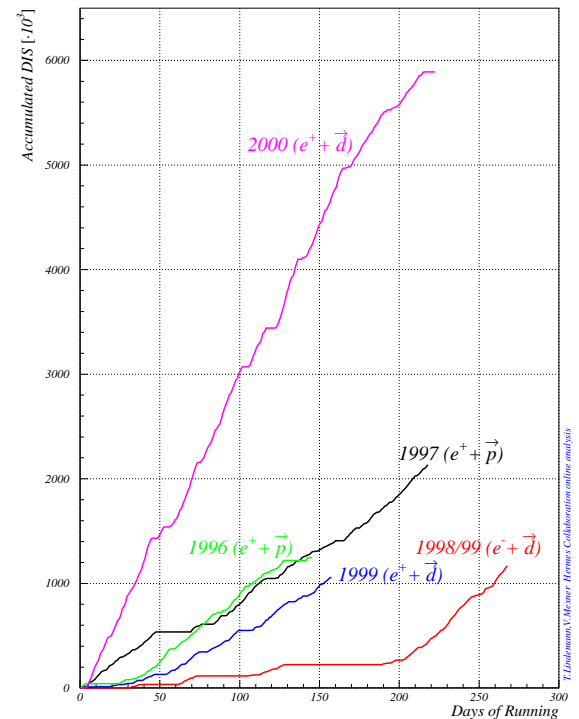
# Quark Polarizations at LO



Not yet included ...

- large 2000 data set on Deuterium
- Kaon asymmetries from RICH detector → access to  $\Delta s$

Hermes Running 1996-2000



- So far: agreement with Gehrman, Stirling fit to **inclusive data** (Gluon A, LO)
- Result insensitive to choice of SU(3)-symmetric **sea assumption** :

$$\frac{\Delta q_s}{q_s} \equiv \frac{\Delta u_s}{u_s} = \frac{\Delta d_s}{d_s} = \frac{\Delta s}{s} = \frac{\Delta \bar{u}}{\bar{u}} = \frac{\Delta \bar{d}}{\bar{d}} = \frac{\Delta \bar{s}}{\bar{s}}$$

$$\Delta q_s \equiv \Delta u_s = \Delta d_s = \Delta s = \Delta \bar{u} = \Delta \bar{d} = \Delta \bar{s}$$

There are other possibilities ... 2000 data will permit 4- and 5-parameter fits

# Global Fit with Semi-Inclusive Data

## deFlorian & Sassot 2000

de Florian, Sassot, PRD 62 (2000) 094025

- Assume isospin / charge conjugation sym betw fragmentation functions:

$$\begin{array}{ll}
 \text{FAVOURED} & D_1^\pi \equiv D_u^{\pi^+} = D_{\bar{u}}^{\pi^-} = D_d^{\pi^-} = D_{\bar{d}}^{\pi^+} \\
 \text{DISFAVOURED} & D_2^\pi \equiv D_u^{\pi^-} = D_{\bar{u}}^{\pi^+} = D_d^{\pi^+} = D_{\bar{d}}^{\pi^-} \\
 \text{STRANGE} & D_s^\pi \equiv D_s^{\pi^+} = D_{\bar{s}}^{\pi^+} = D_s^{\pi^-} = D_{\bar{s}}^{\pi^-}
 \end{array}$$

- Relax  $F$ ,  $D$  constraints:

$$\Delta q_3 = (F + D)(1 + \epsilon_{Bj}) \quad \Delta q_8 = (3F - D)(1 + \epsilon_{SU(3)})$$

- Try 3 choices for  $\int \Delta g @ \mu_0$ :
  - ①  $\Delta G|_{\mu_0} < 0.4$
  - ②  $0.4 < \Delta G|_{\mu_0} < 0.7$
  - ③  $\Delta G|_{\mu_0} > 0.7$  ...  $\chi^2$  same for all 3

- 2 scenarios for light quark sea:
  - “+” scenario:  $\delta \bar{u} = \delta \bar{d}$
  - “-” scenario:  $\delta \bar{u} = -\delta \bar{d}$

@  $\mu_0$

MOMENTS:	$\Delta \Sigma$	$\Delta G$	$\Delta q_{\text{sea}}$
@ $Q^2 = 10$	0.15 – 0.19	0.8 – 1.8	$\Delta s = -0.06 - -0.07$ + scen: $\Delta \bar{u} = 0.06$ $\Delta \bar{d} = 0.06$ – scen: $\Delta \bar{u} = 0.04$ $\Delta \bar{d} = -0.05$

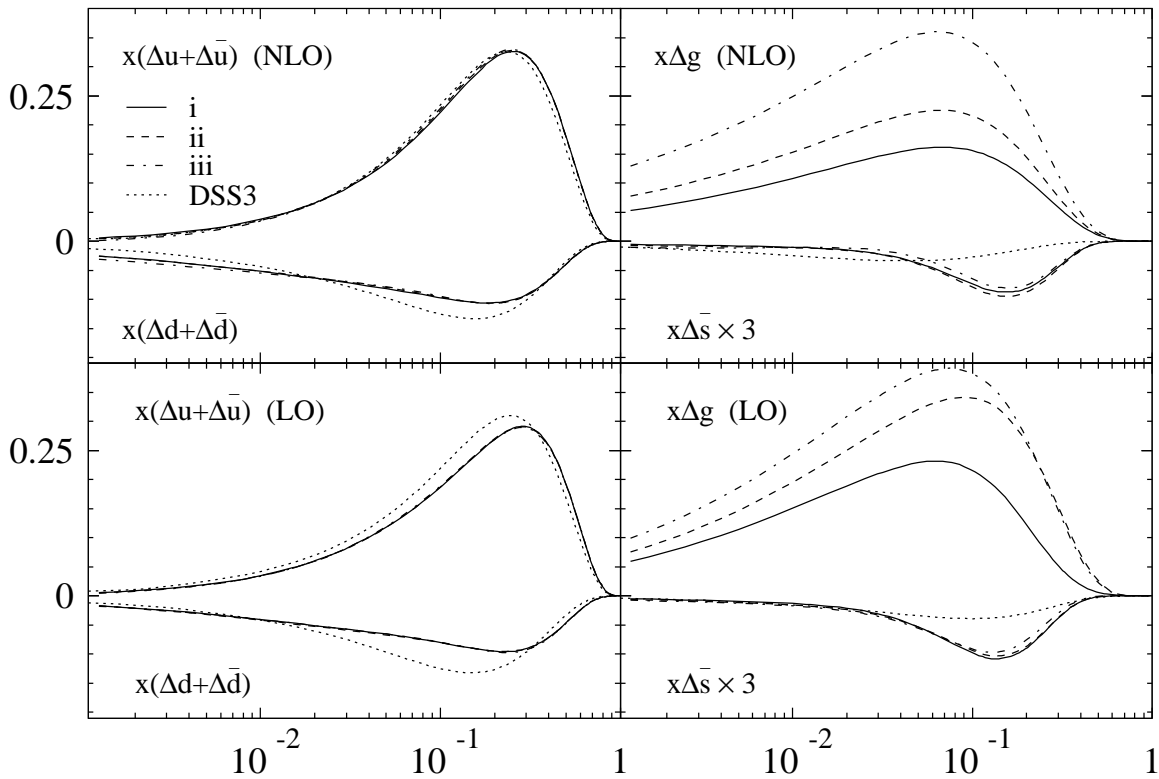
## Conclusions:

- SIDIS data  $\Rightarrow$   $\delta \bar{u} > 0$  but  $\delta \bar{d}$  unconstrained  
 $\rightarrow$  no  $\chi^2$  change between + and – scenarios
- $\Delta s < 0$  indicated, with  $\epsilon_{Bj} \approx -2\%$  and  $\epsilon_{SU(3)} \approx -6\% - 7\%$

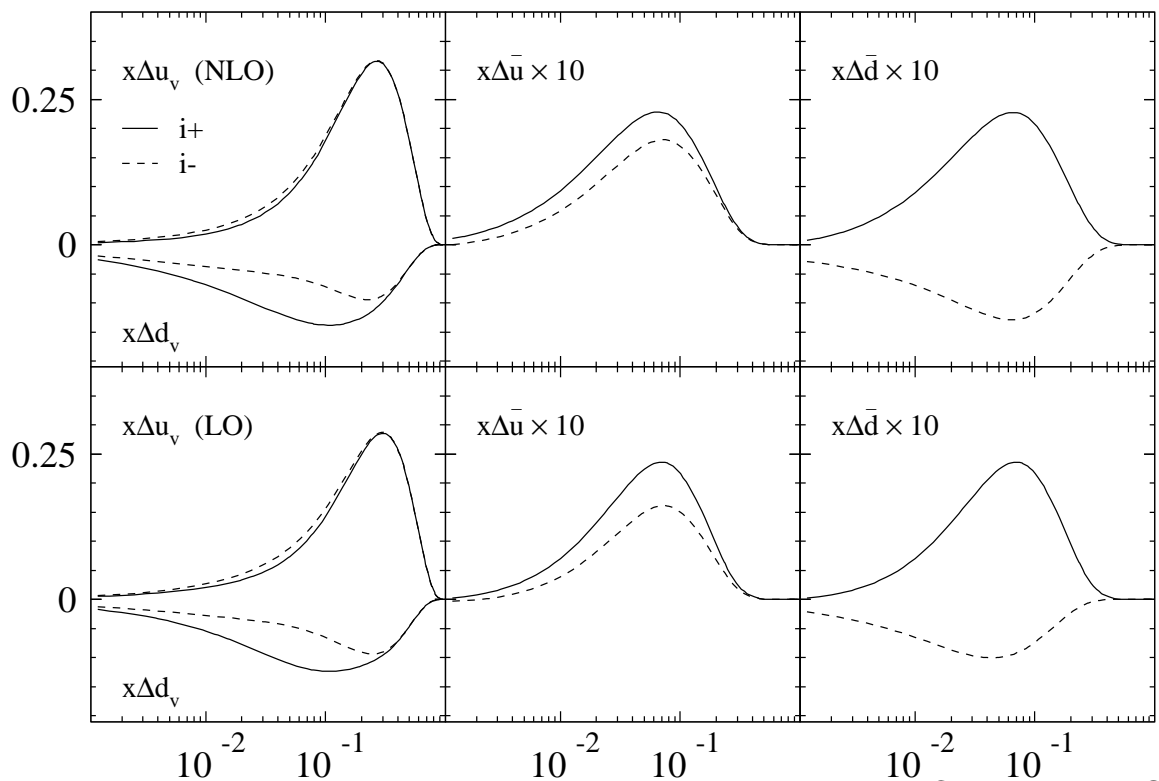
# Global Fit with Semi-Inclusive Data

Using inclusive data only ...

de Florian, Sassot, PRD 62 (2000) 094025

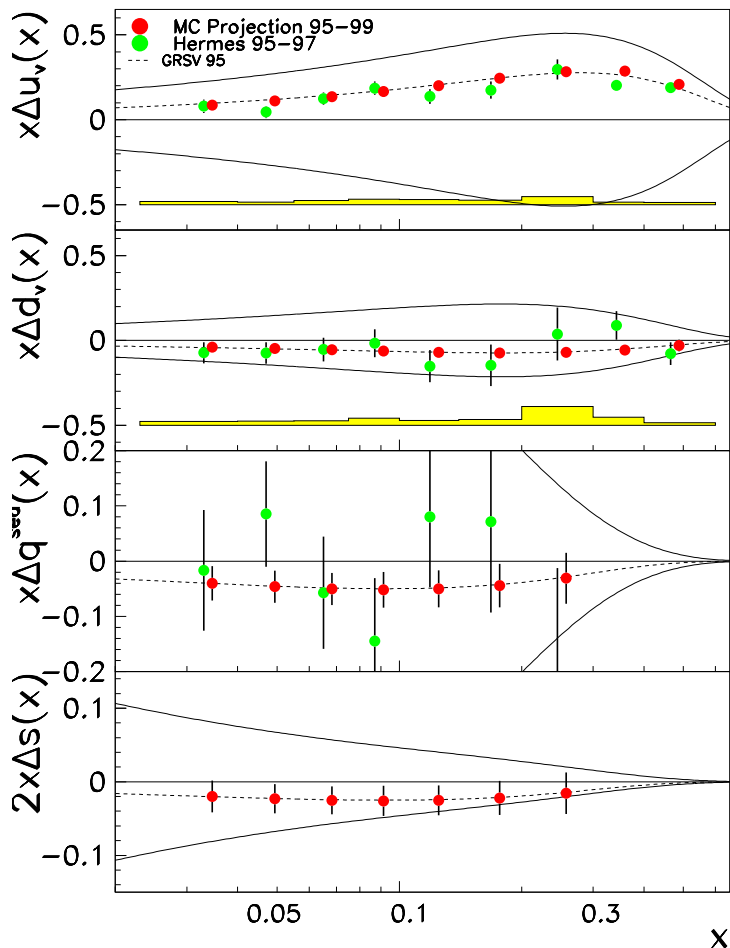


Adding semi-inclusive data ...

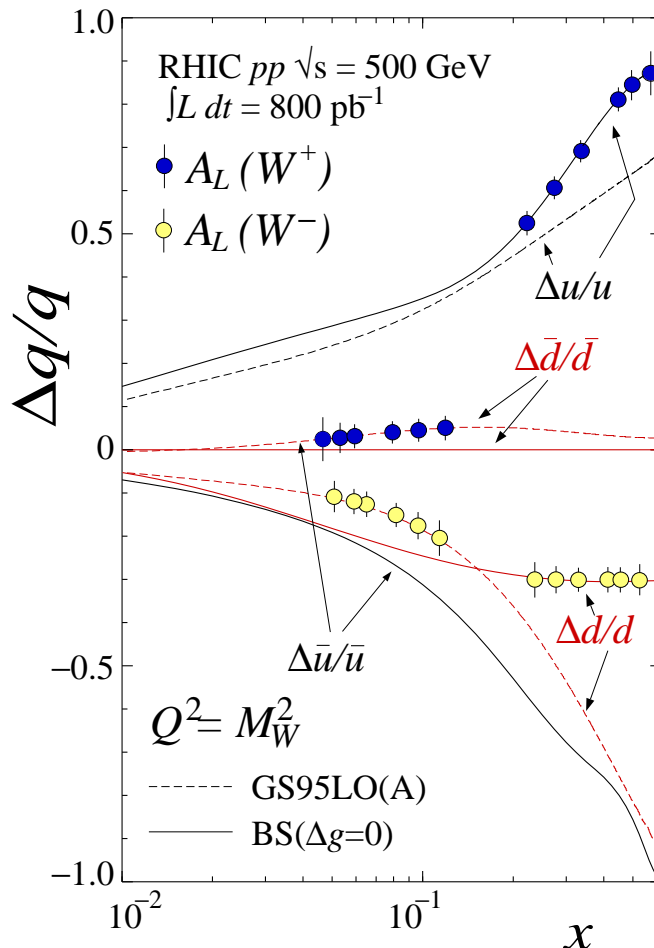


# Quark Polarization: Future

**HERMES** : data up to 2000

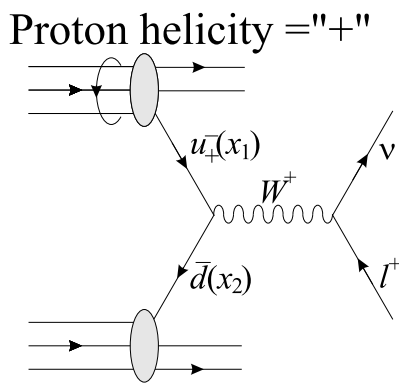


**RHIC-spin** : 2002 - ...



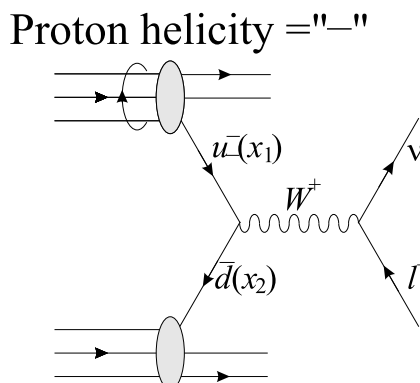
- Pion & Kaon asymmetries

→  $\Delta s$ ,  $\Delta \bar{s}$  sensitivity



- Polarized  $W$  production

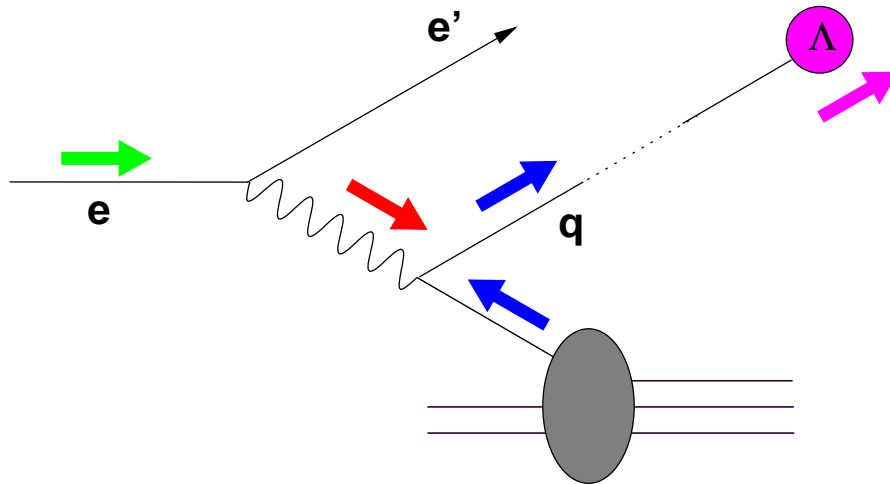
→  $\Delta \bar{u}$  vs  $\Delta \bar{d}$  sensitivity



And further DIS data expected from COMPASS and HERMES Run II

# Longitudinal $\Lambda$ Polarization

$\Lambda$  polarization accessible via angular distribution of decay  $p, \pi$



Using **polarized beam** and unpolarized target, measure **longitudinal spin transfer** in fragment<sup>n</sup> (from struck  $q$  to  $\Lambda$ )

$$P_{\Lambda} = P_{\text{beam}} \cdot D(y) D_{LL'}$$

$\nearrow$  final state  $\Lambda$  polarization  
 $\uparrow$  struck quark polarization  
 $\nwarrow$  spin transfer

$$D_{LL'} = \frac{\sum e_q^2 q(x) \Delta D_q^{\Lambda}(z)}{\sum e_q^2 q(x) D_q^{\Lambda}(z)} = \sum \frac{\Delta D_q^{\Lambda}(z)}{D_q^{\Lambda}(z)} \cdot \omega_q^{\Lambda}(x)$$

$\nwarrow$  "purity"

Note: In Mulders notation,  $\Delta D(z) = G_1(z)$

$\rightarrow$  fragmentation analogue of  $g_1(x)$

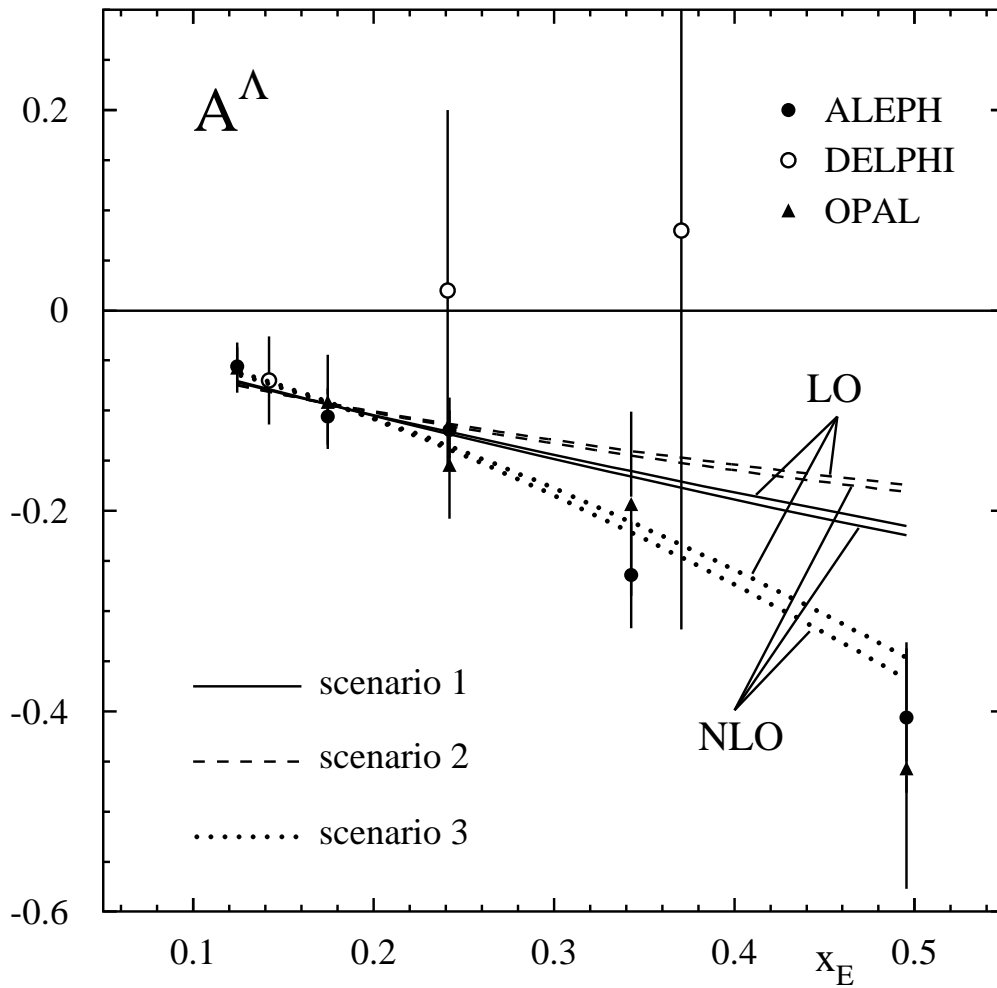
# SPIN TRANSFER $\vec{q} \rightarrow \vec{\Lambda}$

$$D_{LL'} = \sum \omega_q^\Lambda(x) \frac{G_{1,q}^\Lambda(z)}{D_{1,q}^\Lambda(z)}$$

... **IF**  $q$  helicity conserved in fragmentation ...

$$\Rightarrow \frac{G_{1,q}^\Lambda}{D_{1,q}^\Lambda} \sim \frac{\Delta q^\Lambda}{q^\Lambda}$$

*i.e. directly related to quark polarization in  $\Lambda$*



*deFlorian, Stratmann, Vogelsang, PRD 57 (1988) 5811*

SCENARIO ① **NRQM** :  $\Delta u^\Lambda = \Delta d^\Lambda = 0, \quad \Delta s^\Lambda = 1$

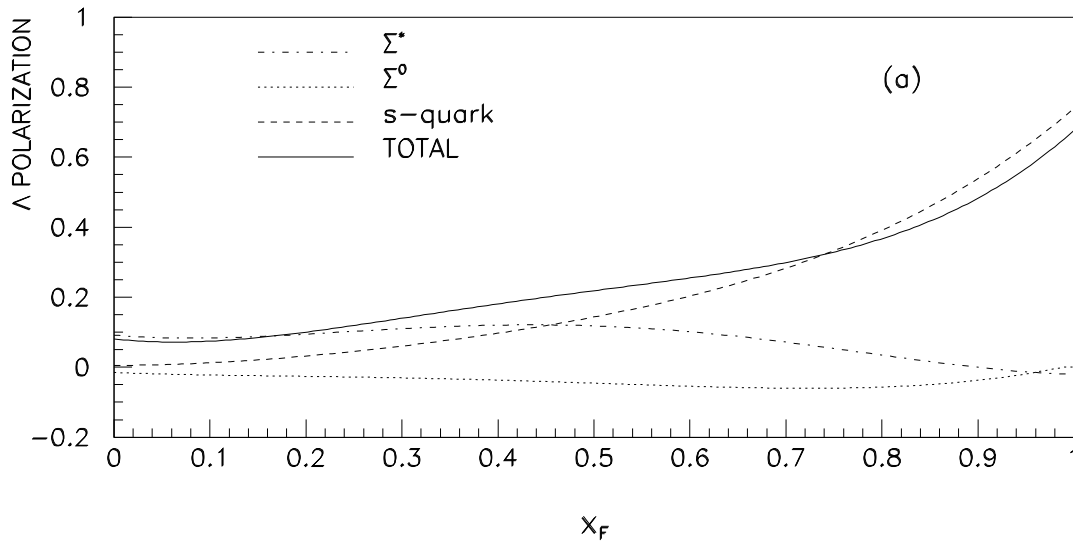
SCENARIO ② **Burkardt & Jaffe** :  $\Delta u^\Lambda = \Delta d^\Lambda \approx -0.2$

SCENARIO ③ **“extreme”** : equal polariz<sup>n</sup> of flavours  $\Delta u^\Lambda \approx \Delta d^\Lambda \approx \Delta s^\Lambda$   
(e.g. if  $\exists$  sizable contrib<sup>s</sup> from decays of heavier hyperons)

# Influence of Heavy Hyperon Decays

## Heavier Hyperons at E665

Ashery, Lipkin, PLB 469 (1999) 263

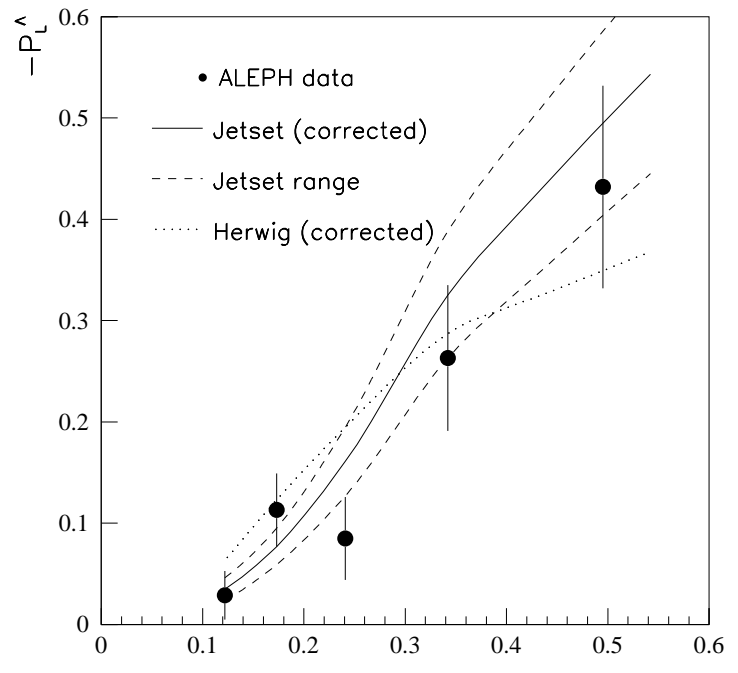
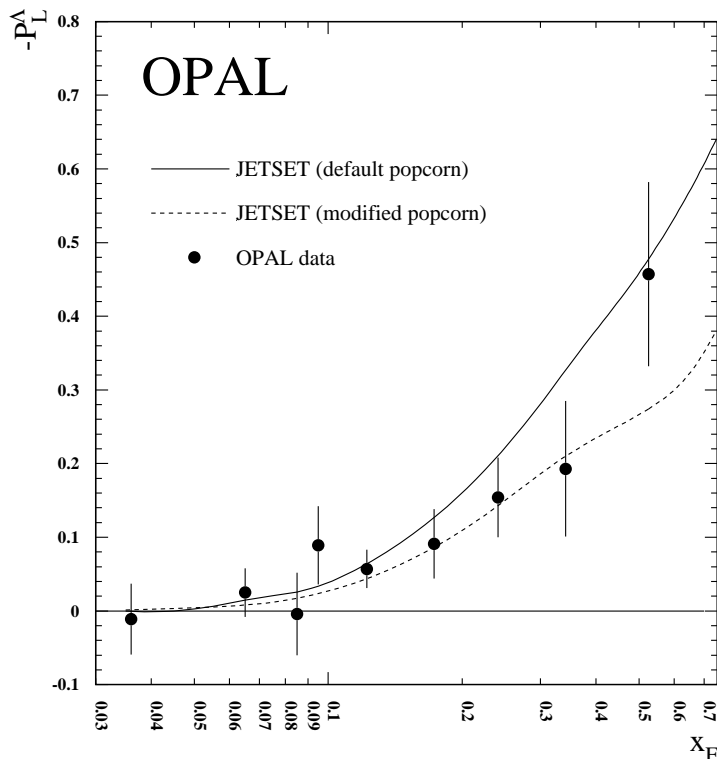


## LEP Analyses

OPAL, EPJ C2 (1998) 49; ALEPH, PLB 374 (1996) 319

OPAL and ALEPH data on  $P_\Lambda$  confronted with Monte Carlo models:

- simple SU(3)-symmetric hyperon spin structure
- hyperons **not** containing primary  $q$  unpolarized
- perfect helicity conservation of primary  $q$



N.C.R. Mäkins, Santorini 2001

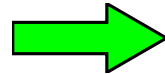
# Λ Spin Structure as $x \rightarrow 1$

## • Gribov-Lipatov relation

$$q_h(x) \propto D_q^h(z)$$

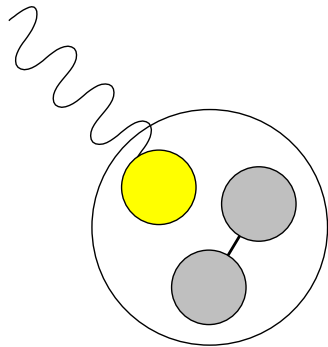
endpoint  
easy to see:

$z_\Lambda \rightarrow 1$   
Λ carries all energy  
ν of struck quark



$x_\Lambda \rightarrow 1$   
struck q carries all  
energy of Λ

## ① Quark-Diquark Model



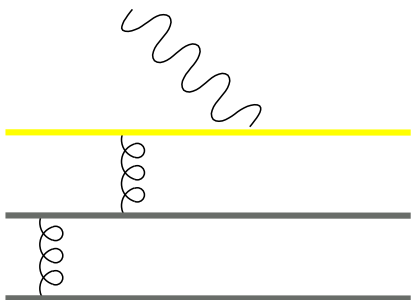
spectator diquark D in scalar or vector state

$$\psi_D(x, k_\perp) \sim \exp - \left[ \frac{1}{8\beta_D^2} \left( \frac{m_q^2 + k_\perp^2}{x} + \frac{m_D^2 + k_\perp^2}{1-x} \right) \right]$$

... as  $x \rightarrow 1$ , VECTOR diq config<sup>n</sup> suppressed

	$\frac{d}{u} \rightarrow 0$	$\rightarrow$	$\frac{F_2^n}{F_2^p} \rightarrow \frac{1}{4}$
	$\frac{\Delta u}{u} \rightarrow 1$		$\frac{\Delta d}{d} \rightarrow -\frac{1}{3}$

## ② pQCD Model



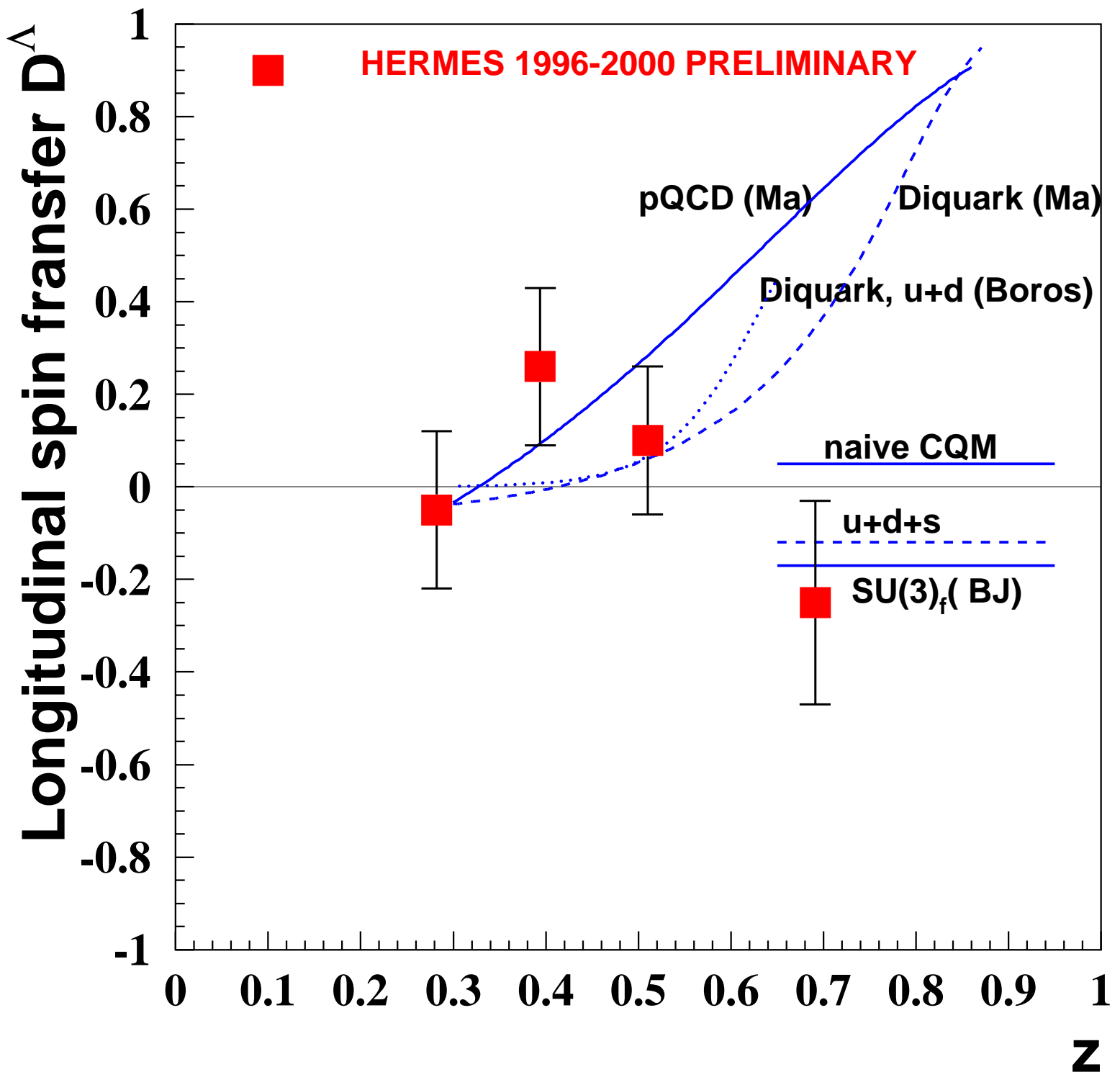
$x \rightarrow 1$  wavefn obtained from “normal” wavefn by exchange of large invariant mass gluons from spectator q’s ... propagators  $\sim \frac{1}{p^2}$  small  
→ small couplings, perturbative methods possible

	$\frac{d}{u} \rightarrow \frac{1}{5}$	thus	$\frac{F_2^n}{F_2^p} \rightarrow \frac{3}{7}$ ,	$\frac{\Delta q}{q} \rightarrow 1$ for $u$ and $d$
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For Λ: Both models predict  $\frac{\Delta q^\Lambda}{q^\Lambda} \rightarrow 1$  for all flavours!



# $\Lambda$ Spin Structure as $x \rightarrow 1$



# Transversity

A complete description of the momentum and spin structure of the nucleon at leading twist requires the third parton distribution  $\delta q(x)$ .

$$f_1 = \text{circle with a black dot in the center}$$

$$g_{1L} = \text{circle with black dot and red arrow pointing right} - \text{circle with black dot and red arrow pointing left}$$

**transversity:**  
 $h_1(x) \sim \delta q(x)$

$$h_1 = \text{circle with black dot and red arrow pointing up} - \text{circle with black dot and red arrow pointing down}$$

## Helicity Flip Amplitudes

$$\left| \begin{array}{c} \text{wavy line } q \\ \text{line } P \end{array} \right. \rightarrow \left| \begin{array}{c} \text{wavy line } q \\ \text{line } P \end{array} \right|^2 \sim \text{Im} \left\{ \begin{array}{c} \text{wavy line } q \\ \text{line } P \end{array} \right\}$$

$$f_1 \sim \text{diagram 1} + \text{diagram 2}$$

Diagram 1: Two grey circles on a grey bar with red arrows pointing right. Green arrows point away from the circles.

Diagram 2: Two grey circles on a grey bar with red arrows pointing right. Green arrows point towards the circles.

$$g_1 \sim \text{diagram 1} - \text{diagram 2}$$

Diagram 1: Two grey circles on a grey bar with red arrows pointing right. Green arrows point away from the circles.

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$$h_1 \sim \text{diagram 1} - \text{diagram 2}$$

Diagram 1: Two grey circles on a grey bar with red arrows pointing right. Green arrows point away from the circles.

Diagram 2: Two grey circles on a grey bar with red arrows pointing right. Green arrows point towards the circles.

Target not in helicity eigenstate  
 $\Rightarrow$  **transversity basis**

$$\text{diagram 1} - \text{diagram 2}$$

Diagram 1: Two grey circles on a grey bar with red arrows pointing up. Green arrows point away from the circles.

Diagram 2: Two grey circles on a grey bar with red arrows pointing up. Green arrows point towards the circles.

## In Non-Relativistic Case ...

In the absence of **relativistic effects**, boosts and rotations commute:

$$\delta q(x) = \Delta q(x)$$

## Tensor Charge of the Nucleon

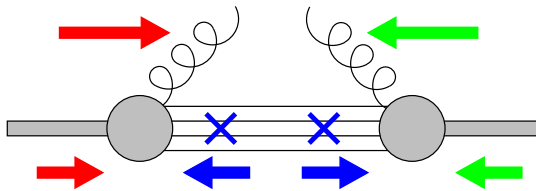
Fundamental matrix elements:

axial charge  $\Delta q(\mu) = \langle PS | \bar{\psi} \gamma^\mu \gamma_5 \psi | PS \rangle = \int_0^1 dx g_1(x) + \bar{g}_1(x)$

tensor charge  $\delta q(\mu) = \langle PS | \bar{\psi} \sigma^{\mu\nu} \psi | PS \rangle = \int_0^1 dx h_1(x) - \bar{h}_1(x)$

⇒ tensor charge is **pure valence object** ...  
promising for comparison with lattice QCD

## No Gluons



Angular momentum conservation

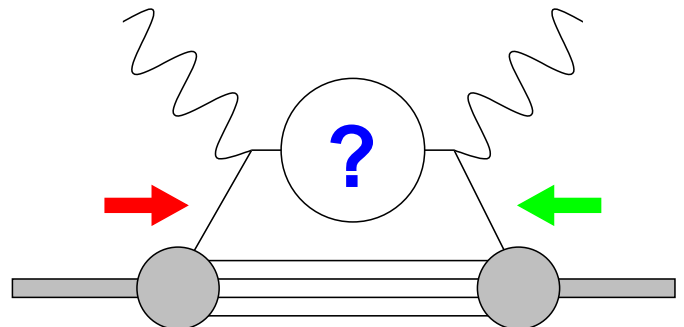
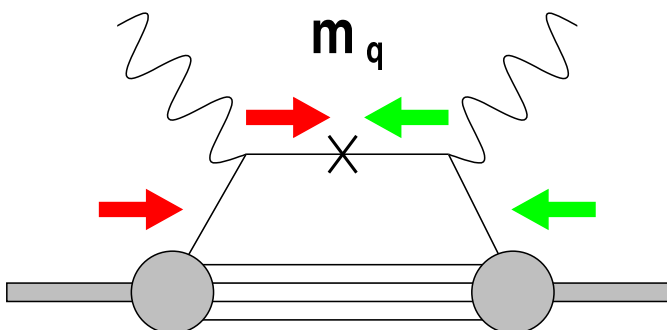
$$\Rightarrow \Lambda - \lambda = \Lambda' - \lambda'$$

Different  $Q^2$  **evolution** than  $g_1$ .

## Chiral Odd

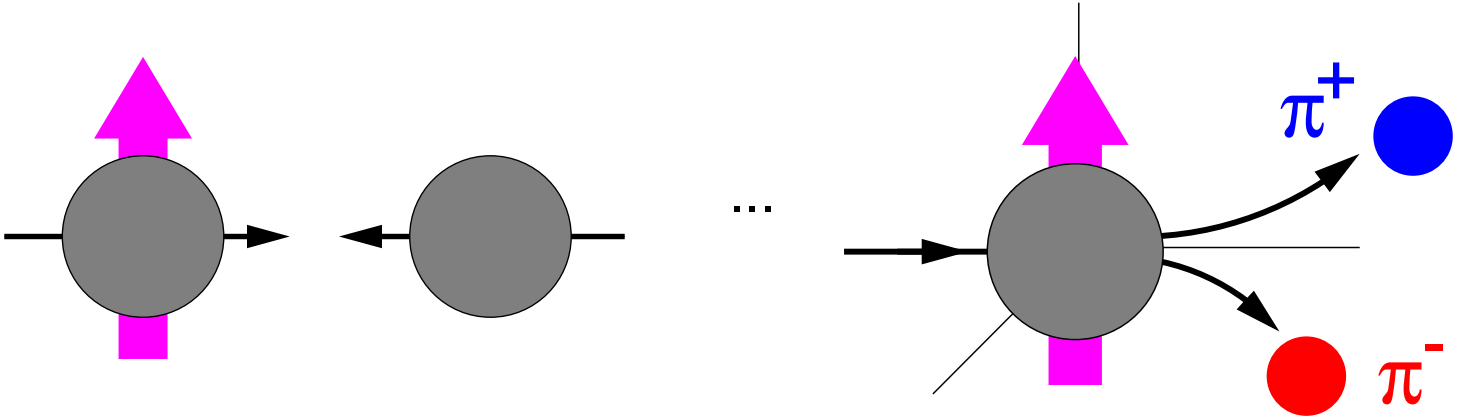
Helicity flip amplitudes occur only at  $\mathcal{O}(m_q/Q)$  in inclusive DIS ...

but they are observable in e.g. **semi-inclusive** reactions



# Single Spin Asymmetries

**E704:**  $p^\uparrow p \rightarrow \pi X$



From perturbative QCD considerations, it was expected that transverse spin effects would be **small**:  $\sim m_q/\sqrt{\hat{s}}$  ...

$$A_N(p^\uparrow p \rightarrow \pi X) \sim \int h_1(x_a) f_1(x_b) D_1^\pi(x_c) \hat{a}_{ab} \frac{d\sigma}{dt}(a^\uparrow b \rightarrow cd)$$

with helicity flip in subprocess asymmetry:

$$\hat{a}_{ab} = \frac{d\sigma(a^\uparrow b \rightarrow cd) - d\sigma(a^\downarrow b \rightarrow cd)}{d\sigma(a^\uparrow b \rightarrow cd) + d\sigma(a^\downarrow b \rightarrow cd)}$$

## No large effects possible:

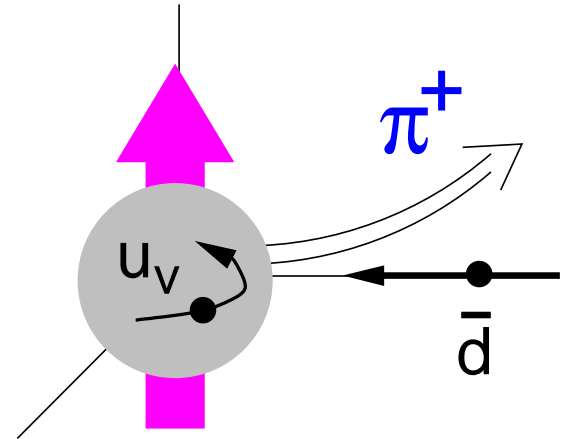
- $q$  helicity flip vanishes in the limit  $m_q = 0$
- $\hat{a}_{ab}$  arises from **interference** between a non-flip and a single-flip helicity amplitude ... and no imaginary phases possible at Born level.

# Sivers Effect

## Chou-Yang Model

Valence quarks = relativistic Dirac particles in central potential

- relativistic quarks in eigenstates of  $J$ , which is shared between  $L$  and  $S$
- symmetrized wavefunction  
 $\rightarrow \Delta u = +4/3, \Delta d = -1/3$
- forward  $\pi^+$  produced directly from orbiting  $u_v$  quark at front surface of beam proton



## Sivers Idea

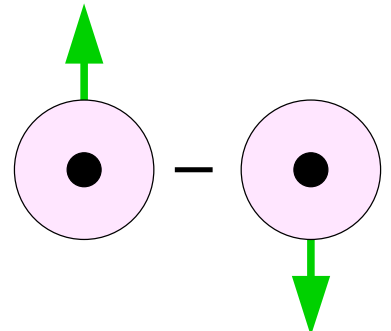
Consider dependence of parton densities on **intrinsic**  $k_T$  :

$$A_N \sim \int f_{1T}^\perp(x_a, \mathbf{k}_{Ta}) f_1(x_b, k_{Tb}) D_1^\pi(x_c, k_{Tc}) \frac{d\sigma}{dt}(ab \rightarrow cd)$$

- Unknown **soft dynamics** absorbed into  $f_{1T}^\perp$  ... hard subprocess merely transmits the asymmetry to large transverse momentum by kinematics.
- Intrinsic  $k_T$  introduces **hadronic scale**  $M$  into the problem: transverse effects of order  $p_T/M$  (not just  $p_T/s$ )

## New structure function: $f_{1T}^\perp(x, \mathbf{k}_T)$

- disappears on integration over  $\mathbf{k}_T$
- odd under time reversal ... requires initial state interactions between colliding hadrons



# Collins Effect and Transversity

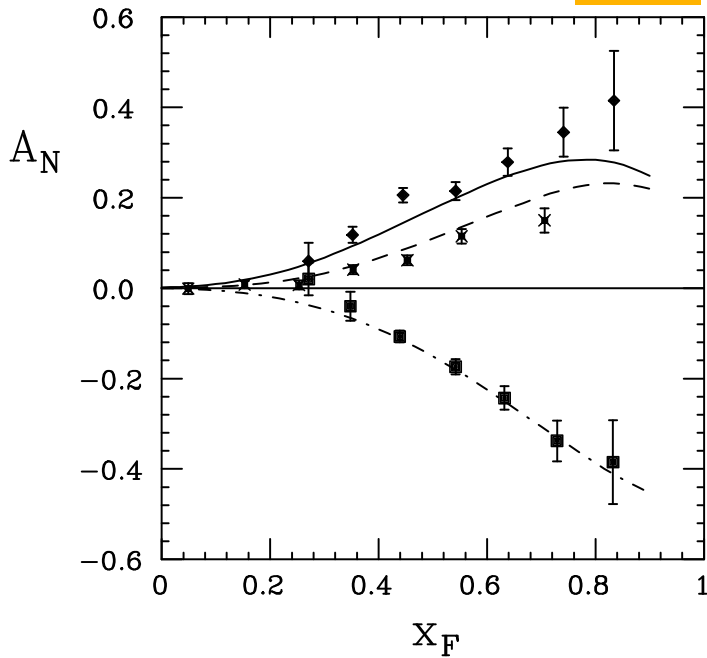
There is another possible explanation ...

the E704 single-spin asymmetry could be due to:

## Sivers Effect:

T-odd **distribut<sup>n</sup> function**

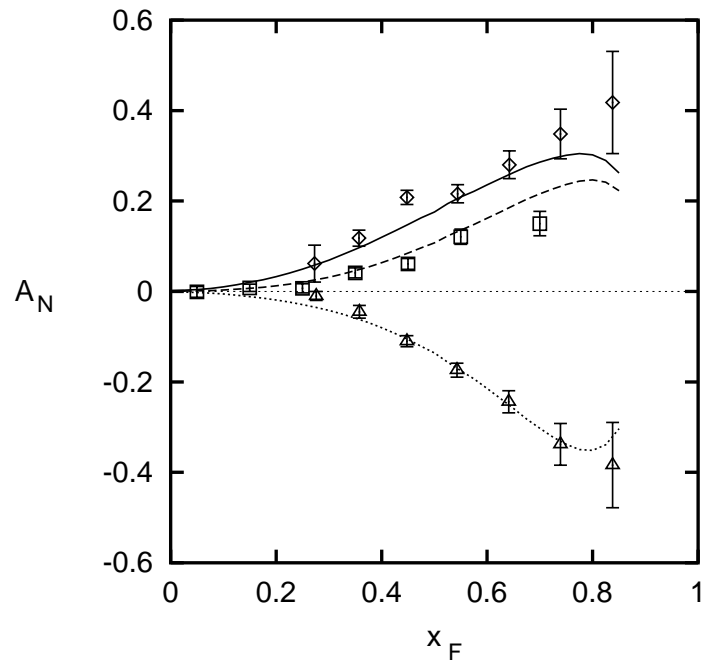
$$f_{1T}^\perp$$



## Collins Effect:

T-odd **fragmentat<sup>n</sup> function**

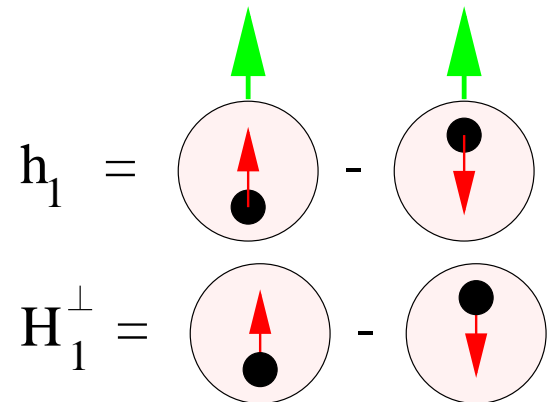
$$H_1^\perp$$



## Collins Effect

In this case,  $A_N \sim h_1(x) H_1^\perp(z)$

$\Rightarrow$  access to **transversity!**



**How to separate?**

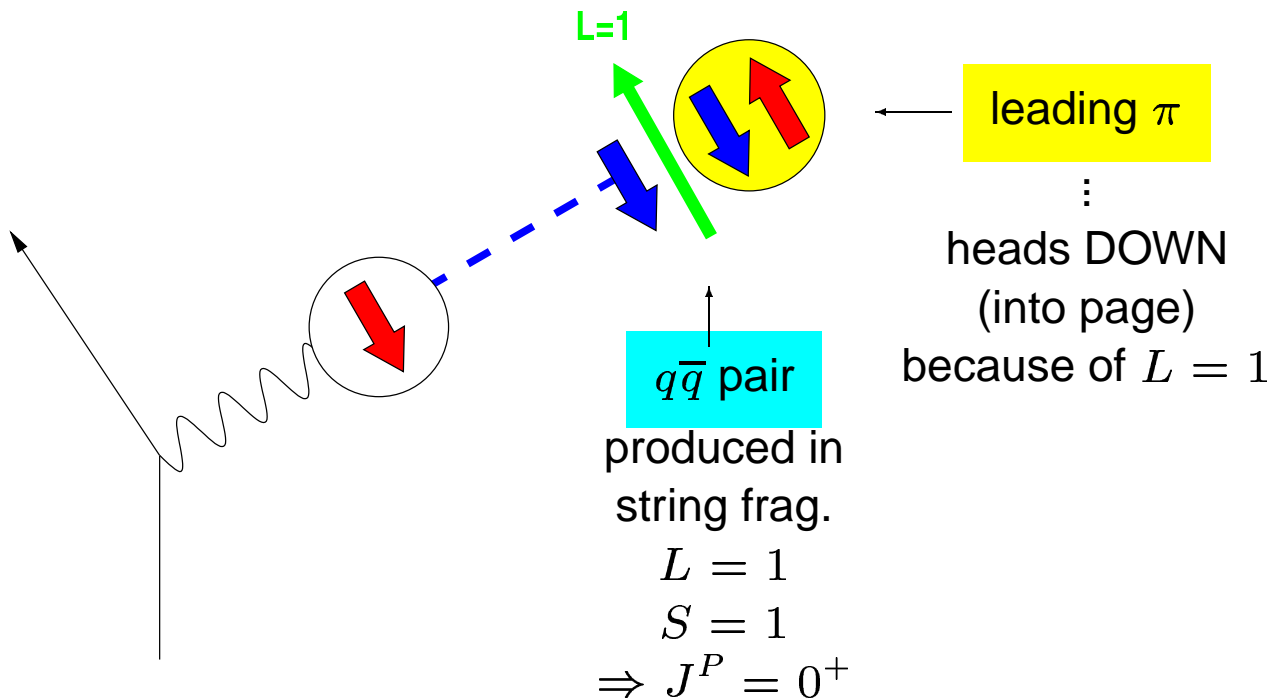
**Single Spin Asymmetries in DIS**

# The Collins Effect in the String Fragmentation Model

## Collins Fragmentation Function

$$H_1^\perp(z)$$

- **chiral-odd** like  $h_1(x)$  ... chiral-odd distribution and fragmentation functions appear in pairs in DIS cross-section
- **T-odd** ... one T-odd function required to produce single-spin asymmetry in semi-inclusive DIS

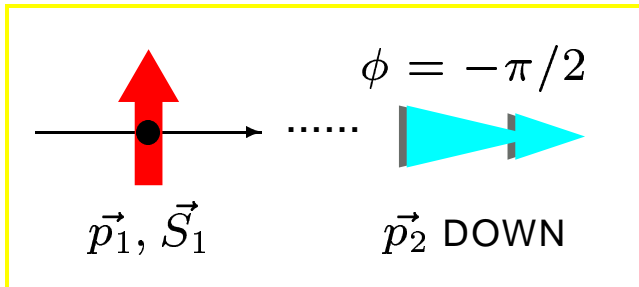


The Collins function is indicative of **phase coherence** in fragmentation  
 $\Rightarrow$  generate interference between non-flip and single-flip amplitudes

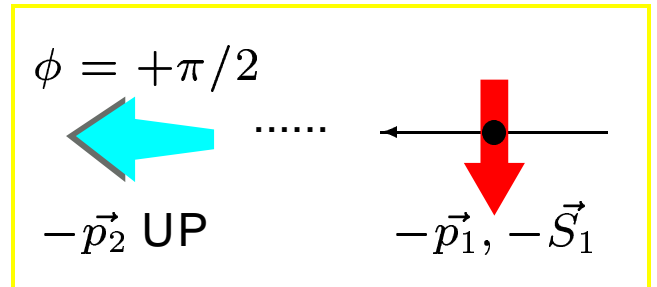
# T-Odd Functions

Spin Spin Azimuthal Asymmetry:  $\sigma \sim \vec{S}_1 \cdot (\vec{p}_1 \times \vec{p}_2) \sim \sin \phi$

⇒ ODD under time reversal



APPLY  
 $\hat{T}$



⇒  $\hat{T}$  transforms  $\phi$  to  $-\phi$

But elementary QCD processes are  $\hat{T}$ -invariant ...

can build  $\hat{T}$ -odd term in xsec ( $\sim \sin \phi$ ) from **interference**

## TOY EXAMPLE

Any amplitude  $A = \langle f | \hat{\mathcal{H}} | i \rangle$  for  $\hat{T}$ -invariant  $\hat{\mathcal{H}}$  satisfies  
 $A^*(-\phi) = A(\phi)$

① No spin flip  $A_1 = \langle S_1 = \uparrow | \hat{\mathcal{H}} | \phi, S_2 = \uparrow \rangle \sim e^{i\phi}$

② Spin flip  $A_2 = \langle S_1 = \uparrow | \hat{\mathcal{H}} | \phi, S_2 = \downarrow \rangle \sim 1$

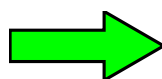
... suppose  $\exists$  **PHASE SHIFT**  $e^{i\delta}$  between amplitudes ...

$$\sigma \sim |A_1 + e^{i\delta} A_2|^2 = 2 + 2\text{Re}(e^{i\delta} A_1^* A_2) = 2 + \cos \delta \cos \phi - \sin \delta \sin \phi$$

●  $e^{i\delta} \Rightarrow$  scattering phase shift, from **final / initial state interactions**

● ... but in high energy  $\pi$  production, surely **many** amplitudes contribute

significant  $\hat{T}$ -odd  
frag<sup>n</sup> function



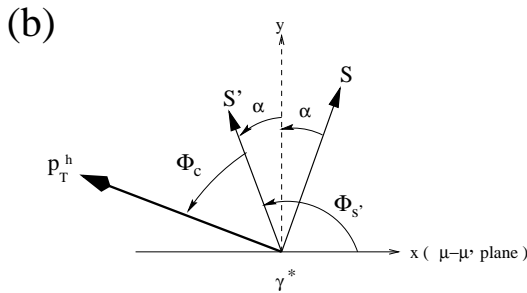
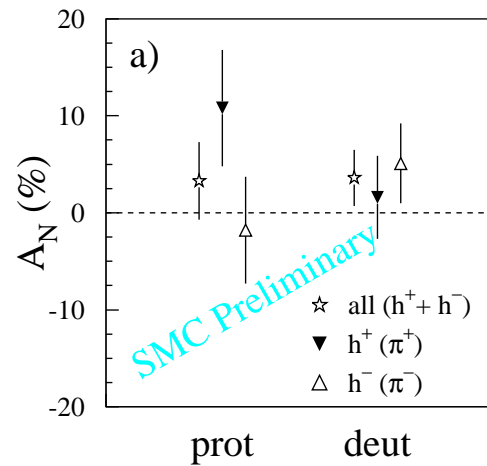
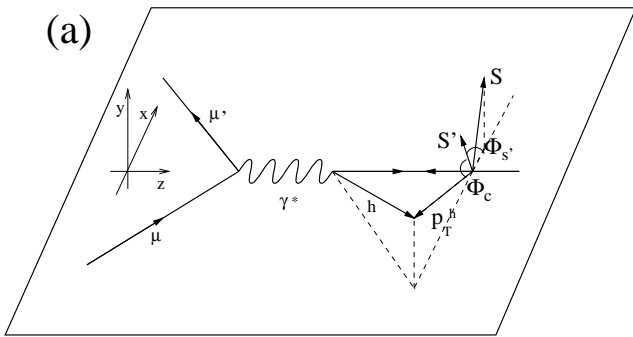
**phase coherence** in  
fragmentation!



# SMC: Azimuthal Asymmetry

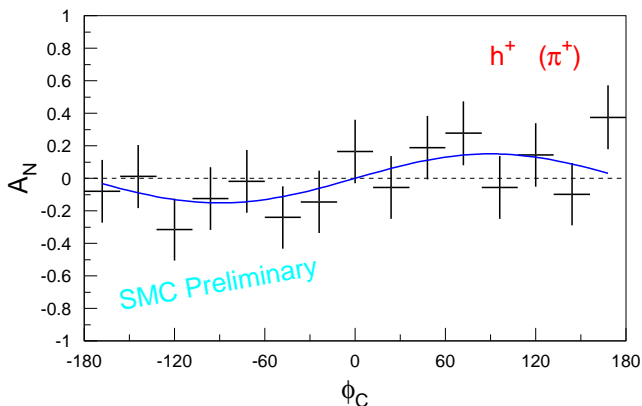
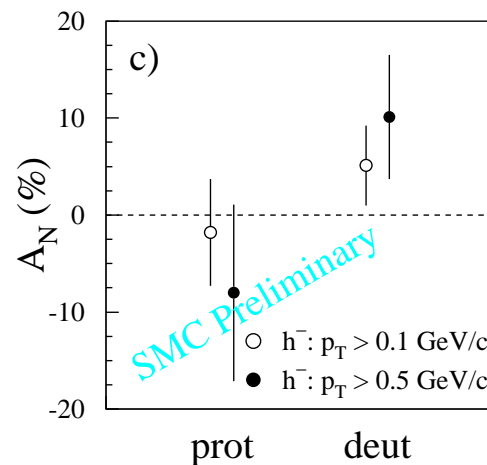
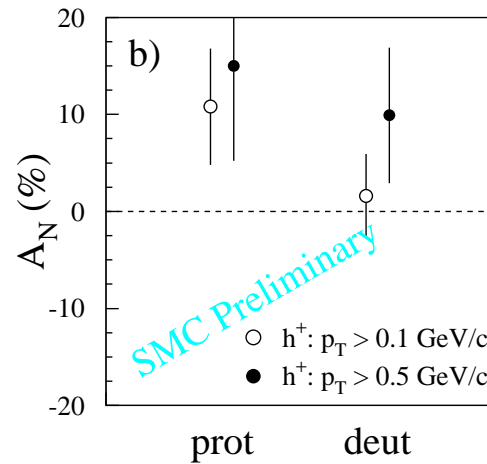


$$A_N = \frac{1}{P_T f D_{NN}} \frac{1}{\langle \sin \phi_c \rangle} \frac{N(\phi_c) - N(\phi_c + \pi)}{N(\phi_c) + N(\phi_c + \pi)}$$

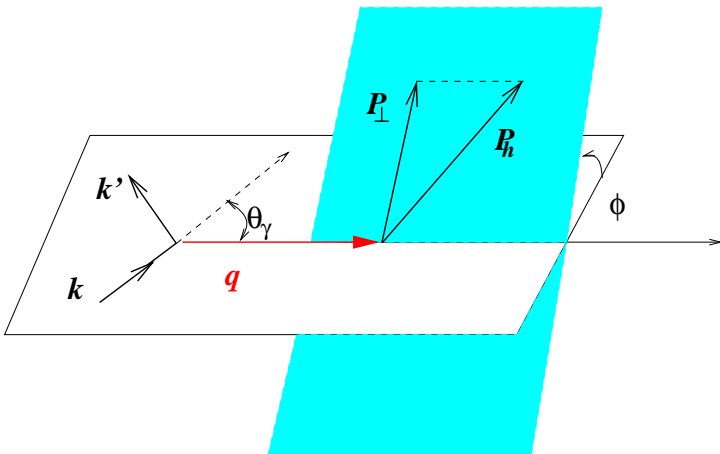


$$d\sigma \sim (1 + A_N \sin \phi_c) d\phi_c$$

Using transversely polarized target

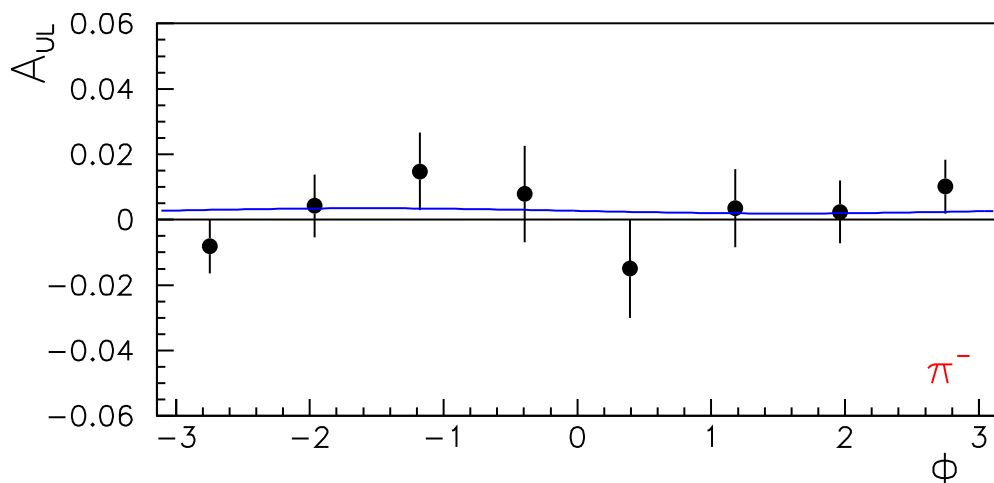
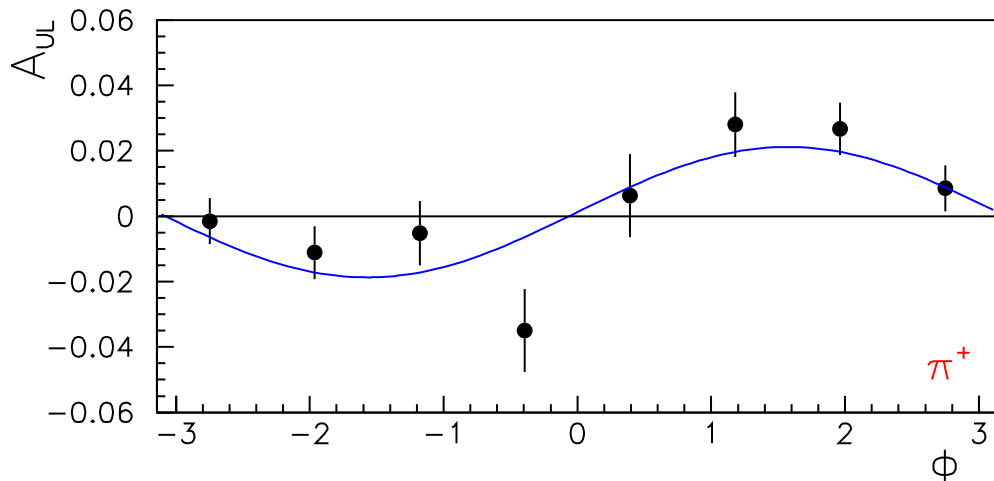


# Spin-Azimuthal Asymmetry



Longitudinal target spin asymmetry:

$$A(\phi) = \frac{1}{P} \frac{N^+(\phi) - N^-(\phi)}{N^+(\phi) + N^-(\phi)}$$

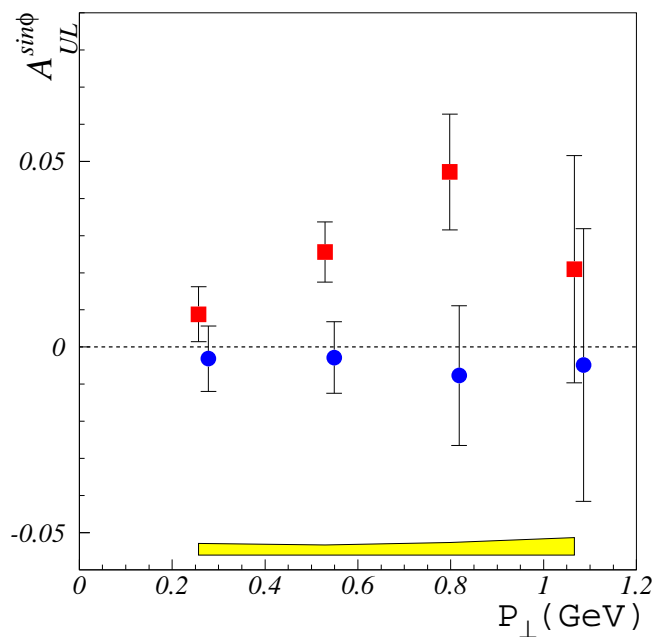
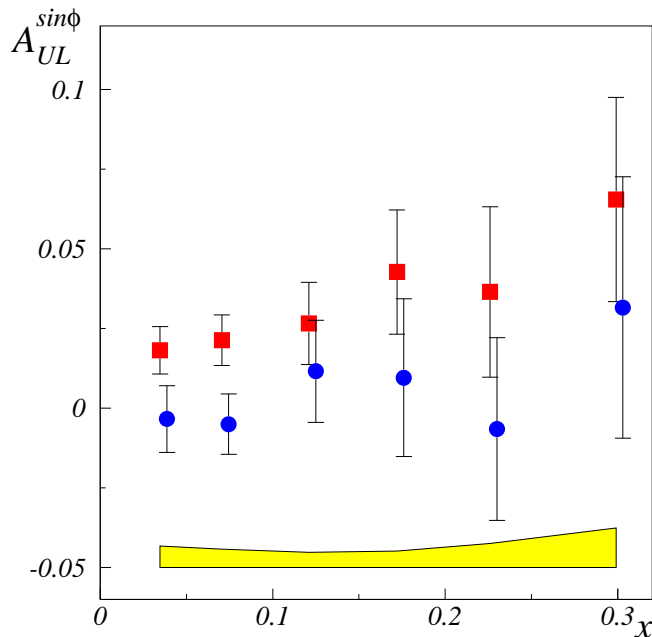


Effect observable even with longitudinally polarized target  
 $\Rightarrow$  good promise for future **transverse target program**  
 at HERMES

$A_{UL}^{\sin\phi} = \langle \sin\phi \rangle$  moment of longitudinal target asymmetry  
 → related to product of  $h_1(x)$  and  $H_1^\perp(z)$

Red squares (blue circles) =  $\pi^+$  ( $\pi^-$ ).

HERMES, hep-ex/9910062



## Original Predictions of Collins

Collins, NP B396 (1993) 161

- Effect should peak at  $x \simeq 0.3$  (valence region)
- Effect should be stronger for  $\pi^+$  than  $\pi^-$  ( $u$ -quark dominance)
- Effect should grow with  $p_T$  and peak at  $p_T \simeq 1$  GeV/c

## Future Measurements of Transversity

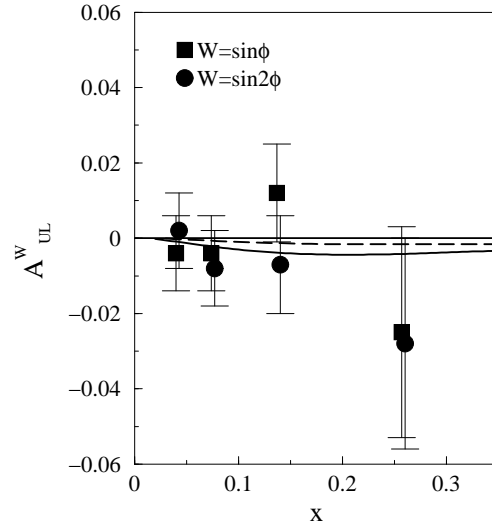
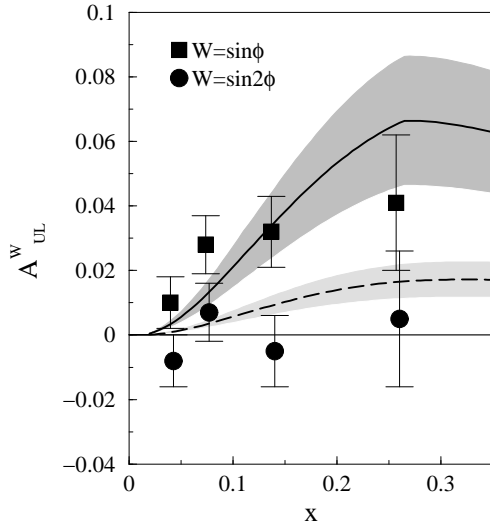
This effect is essentially a **transverse** one ... the fact that it is already visible using a longitudinally polarized target  $\Rightarrow$  good promise for future **transverse target programs**, e.g. at HERMES and COMPASS.

# Azimuthal Asymmetry in the Chiral Quark Soliton Model



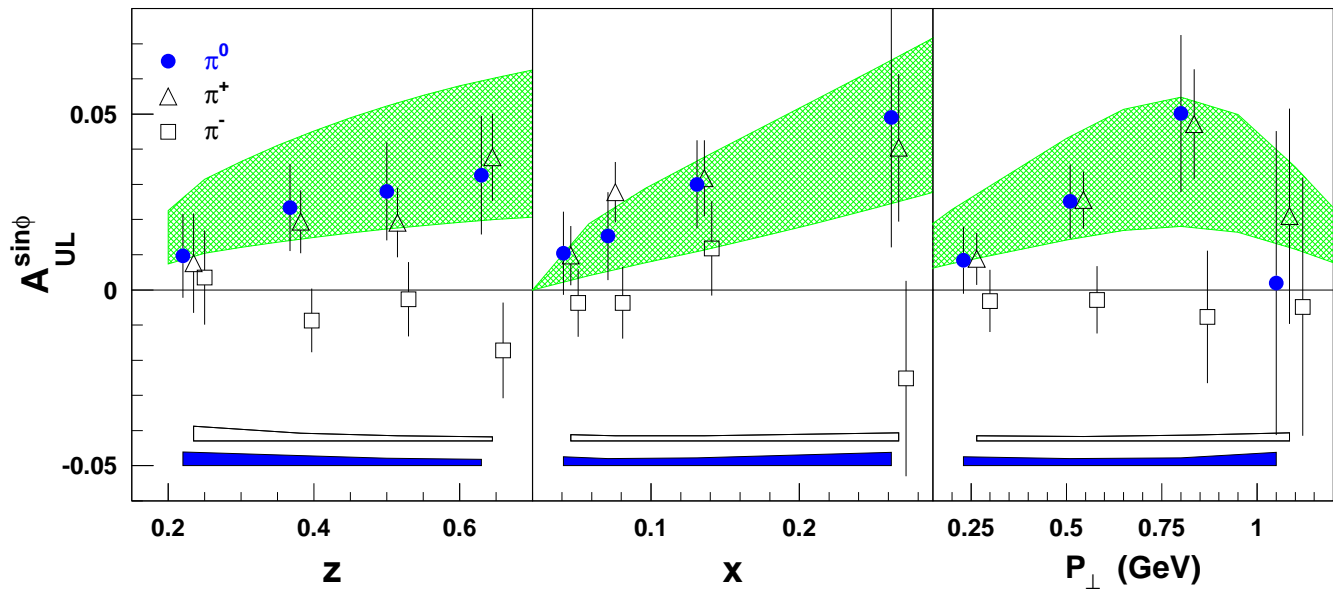
## Charged Pion Asymmetry $A_{UL}^W$

HERMES, PRL 84 (2000) 4047



## New: Neutral Pion Asymmetry

HERMES, hep-ph/0104005



## Calculation:

Efremov et al, hep-ph/0001119

- only favoured fragmentation functions  $D_1^{a/\pi}$  and  $H_1^{\perp a/\pi}$
- $\langle H_1^{\perp}(z)/z \rangle = \langle H_1^{\perp}(z) \rangle / \langle z \rangle$  with  $\langle z \rangle = 0.41$
- $\langle P_{h\perp} \rangle \approx \langle p_T \rangle \approx 0.4$  GeV
- GRV parametrization for  $f_1^a(x)$
- $h_1$  calculated in chiral soliton model

# Size of Collins Function

## • DELPHI

*Efremov et al., hep-ph/9812522*



Transverse  $q, \bar{q}$  polarization small but ANTI-CORRELATED (@  $\sim 50\%$  level)

$$\Rightarrow \left| \frac{H_1^\perp}{D_1} \right| = 6.3 \pm 1.7\%$$

## • HERMES / SMC

*Efremov et al., hep-ph/0108213*

Fit experimental data for  $H_1^\perp$ , taking  $h_1(x)$  from Chiral Quark Soliton Model ( $\chi$ QSM)

$$\Rightarrow \left| \frac{H_1^\perp}{D_1} \right| = \begin{cases} 6.1 \pm 0.9 \pm 0.8\% \\ \text{(HERMES)} \\ 10 \pm 5\% \text{ (SMC)} \end{cases}$$

## • E704

*Boglione & Mulders, PRD 60 (1999) 054007*

Fit experimental data, assuming ONLY Collins effect contributes

$$\Rightarrow \left| \frac{H_1^\perp}{D_1} \right| = 7.6\%$$

*There seems to be general agreement*

*(although results depend on  $z$ -range over which averaging performed)*

## What about the Sivers Function?

• Note: fit to E704 assuming ONLY Sivers effect contributes:

$$\Rightarrow \left| \frac{f_{1T}^\perp}{f_1} \right| = 8.3\% \quad \left( \begin{array}{l} \text{"max"} \\ \text{size} \end{array} \right)$$

• MORE DATA NEEDED ... e.g. DIS w transverse target

$$A_{UT} \text{ has term } \sim f_{1T}^\perp D_1 \sin(\phi_h^l + \phi_s^l)$$

# Summary

## Quark & Gluon Polarization

- **Semi-inclusive** data critical to constraining  $\Delta\bar{u}$ ,  $\Delta\bar{d}$ 
  - some indication already that  $\Delta\bar{u} > 0$
  - wait: HERMES analysis of 2000 data ... new data upcoming from RHICspin, COMPASS, HERMES Run II
- **Gluon polarization** not constrained by  $g_1$  data
  - need direct meas. of photon-gluon-fusion process
  - wait: RHICspin, COMPASS, SLAC, HERMES Run II
- Longitudinal spin transfer in  **$\Lambda$  production** high  $z$  may provide information on  $\Delta q^\Lambda / q^\Lambda$  as  $x \rightarrow 1$

## New Structures

- **Transversity**: first data on  $h_1$  in rather good agreement with models
- First clear evidence of T-odd **Collins Fragmentation Func<sup>n</sup>** obtained
  - strong phase coherence in fragmentation?
- More data required to constrain **Sivers Function  $f_{1T}^\perp$** 
  - sensitive to orbital angular momentum?