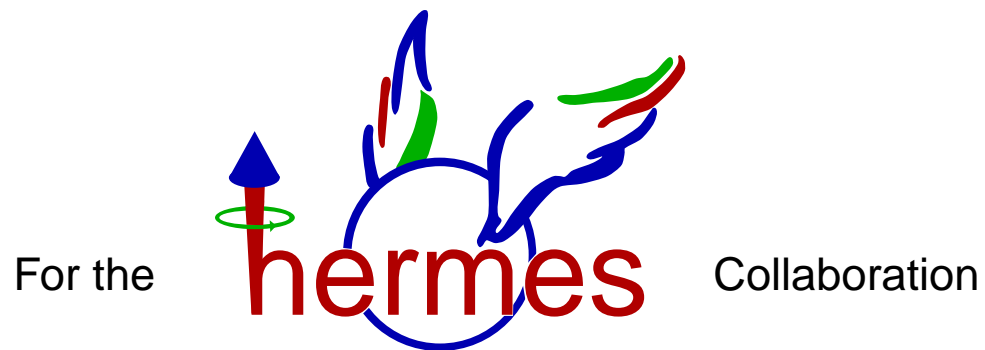


Transversity Measurements at HERMES

Gunar Schnell

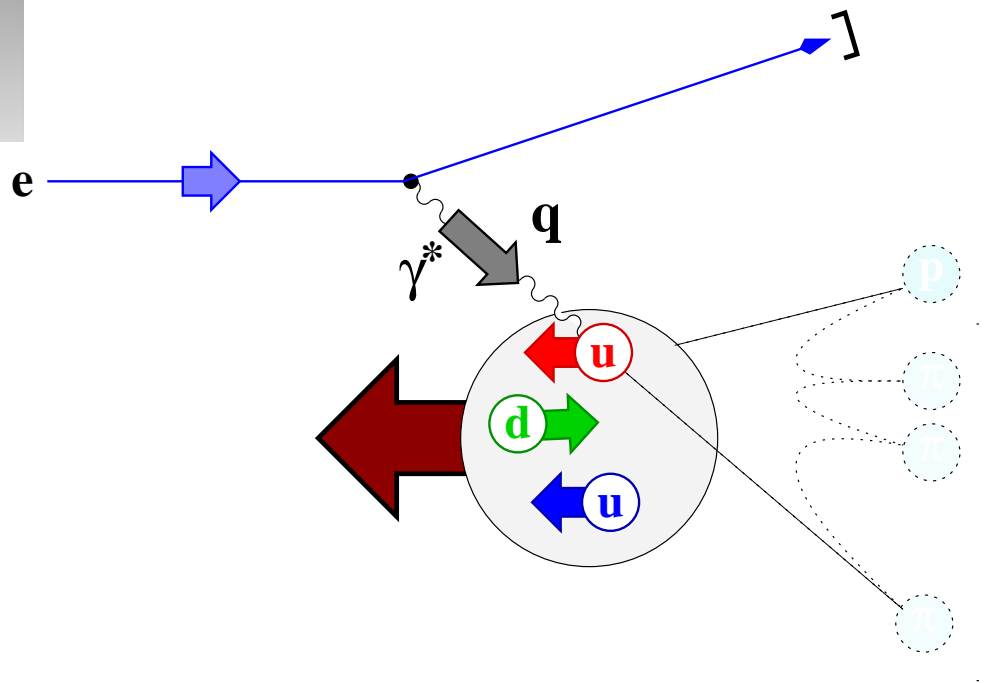
Tokyo Institute of Technology / DESY - Zeuthen

gunar.schnell@desy.de



Deep Inelastic Scattering

use well-known probe to study hadronic structure



$$Q^2 \stackrel{\text{lab}}{=} 4EE' \sin^2\left(\frac{\Theta}{2}\right)$$

$$\nu \stackrel{\text{lab}}{=} E - E'$$

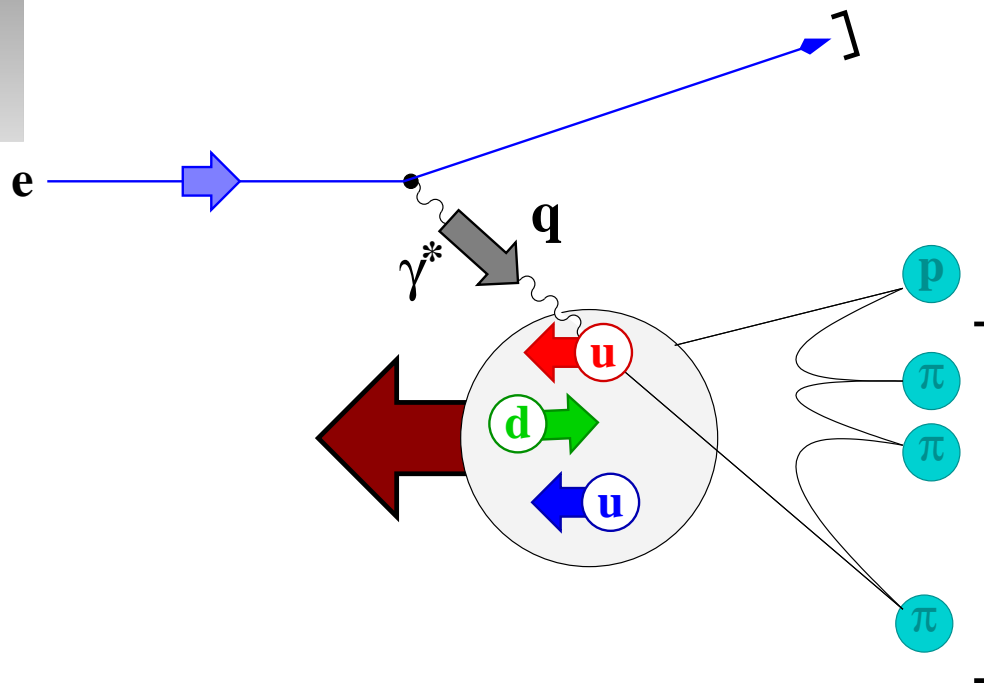
$$W^2 \stackrel{\text{lab}}{=} M^2 + 2M\nu - Q^2$$

$$y \stackrel{\text{lab}}{=} \frac{\nu}{E}$$

$$x \stackrel{\text{lab}}{=} \frac{Q^2}{2M\nu}$$

Deep Inelastic Scattering

use well-known probe to study hadronic structure



$$Q^2 \stackrel{\text{lab}}{=} 4EE' \sin^2\left(\frac{\Theta}{2}\right)$$

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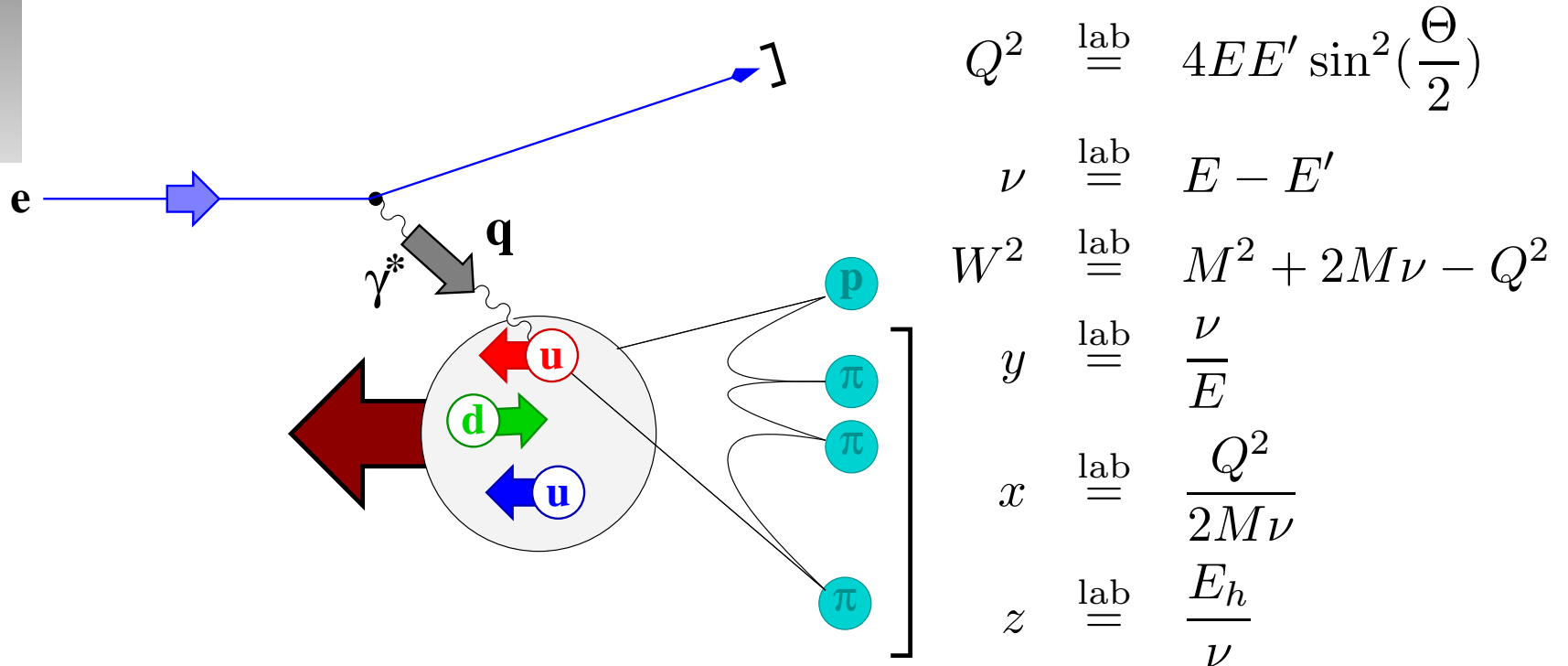
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$$x \stackrel{\text{lab}}{=} \frac{Q^2}{2M\nu}$$

$$z \stackrel{\text{lab}}{=} \frac{E_h}{\nu}$$

Deep Inelastic Scattering

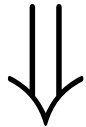
use well-known probe to study hadronic structure



Factorization $\Rightarrow \sigma^{ep \rightarrow ehX} = \sum_q f^{p \rightarrow q} \otimes \sigma^{eq \rightarrow eq} \otimes D^{q \rightarrow h}$

Quark Distribution Functions

$$f_1^q = \text{[Diagram: circle with black dot]}$$



Unpolarized
quarks and
nucleons

$q(x)$: spin averaged
(well known)

⇒ Vector Charge

$$g_1^q = \text{[Diagram: two circles with dots and arrows, one right one left, with a minus sign between them]} - \text{[Diagram: two circles with dots and arrows, one left one right, with a minus sign between them]}$$



Longitudinally
polarized quarks
and nucleons

$\Delta q(x)$: helicity
difference (known)

⇒ Axial Charge

$$h_1^q = \text{[Diagram: circle with dot and red arrow up, green arrow up]} - \text{[Diagram: circle with dot and red arrow down, green arrow up]}$$



Transversely
polarized quarks
and nucleons

$\delta q(x)$: helicity flip
(unmeasured!)

⇒ Tensor Charge

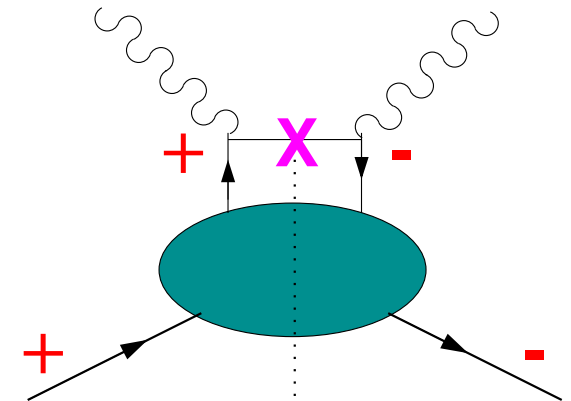
HERMES 1995-2000

HERMES 2002...

- Non-relativistic quarks: $\Delta q(x) = \delta q(x)$
 $\Rightarrow \delta q$ probes **relativistic nature** of quarks
- obvious bound: $|\delta q(x)| \leq q(x)$
- Soffer bound: $|\delta q(x)| \leq \frac{1}{2}[q(x) + \Delta q(x)]$
- Sum Rule: **fi rst moment** \rightarrow **tensor charge** reliably calculable in **lattice QCD** (i.e. at $Q^2 = 2GeV^2$):

$$\delta\Sigma = \sum_f \int_0^1 dx (\delta q_f - \delta \bar{q}_f) = 0.562 \pm 0.088$$
- no “gluon transversity”
- transversity distribution **CHIRAL ODD**

\hookrightarrow **No Access In Inclusive DIS**



How can one measure transversity?

Need another chiral-odd object!

Semi-Inclusive DIS \longrightarrow HERMES with **transversely** polarized target

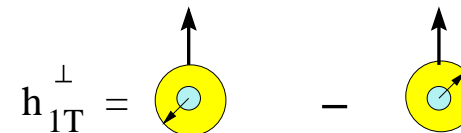
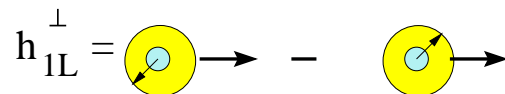
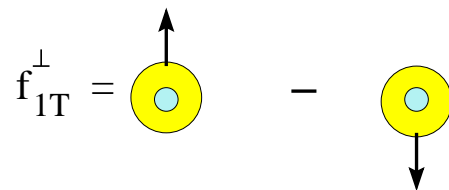
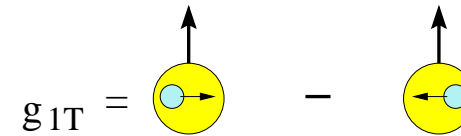
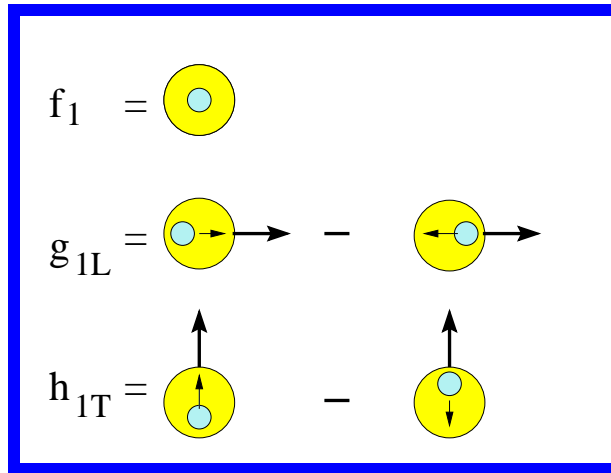
$$\sigma^{ep \rightarrow ehX} = \sum_q f^{H \rightarrow q} \otimes \sigma^{eq \rightarrow eq} \otimes D^{q \rightarrow h}$$

\Downarrow
chiral-odd
 DF

\Downarrow
chiral-odd
 FF

Twist-2 Quark Distribution Functions

Functions surviving integration over intrinsic transverse momentum



Twist-2 Quark Distribution Functions

Functions surviving integration over intrinsic transverse momentum

$$\begin{aligned}
 f_1 &= \text{circle with light blue center} \\
 g_{1L} &= \text{circle with light blue center and right arrow} - \text{circle with light blue center and left arrow} \\
 h_{1T} &= \text{circle with light blue center and up arrow} - \text{circle with light blue center and down arrow}
 \end{aligned}$$

$$g_{1T} = \text{circle with light blue center, right arrow, and up arrow} - \text{circle with light blue center, left arrow, and up arrow}$$

$$f_{1T}^\perp = \text{circle with light blue center and up arrow} - \text{circle with light blue center and down arrow}$$

$$h_1^\perp = \text{circle with light blue center and right arrow} - \text{circle with light blue center and left arrow}$$

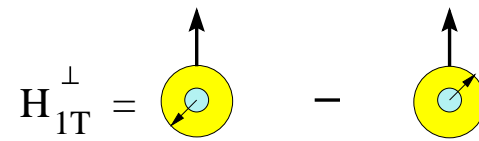
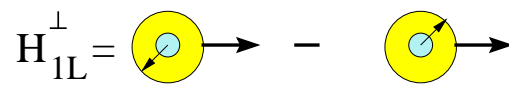
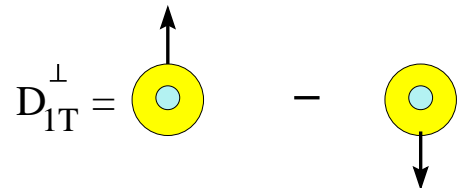
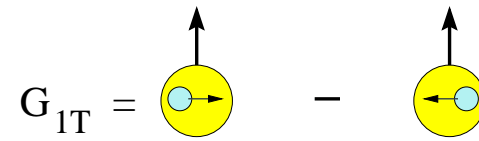
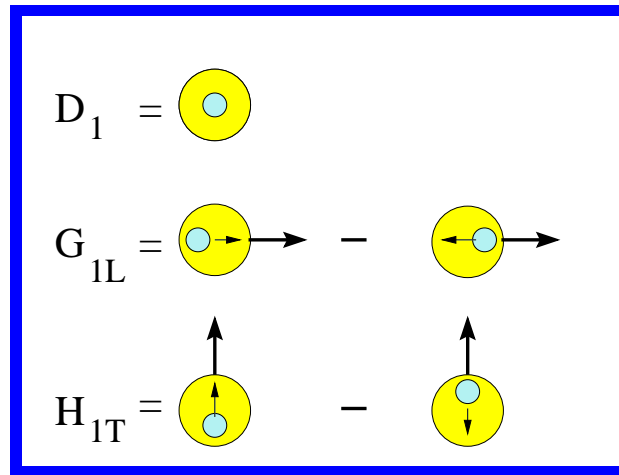
$$h_{1L}^\perp = \text{circle with light blue center, right arrow, and up arrow} - \text{circle with light blue center, right arrow, and down arrow}$$

Sivers Function

$$h_{1T}^\perp = \text{circle with light blue center, right arrow, and up arrow} - \text{circle with light blue center, left arrow, and up arrow}$$

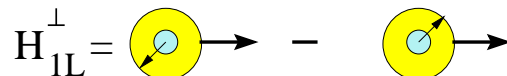
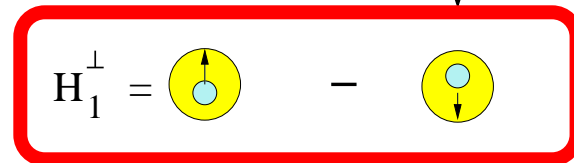
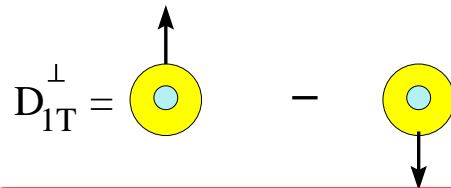
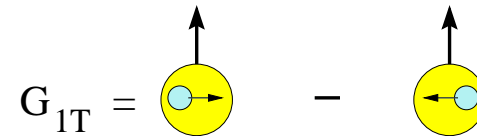
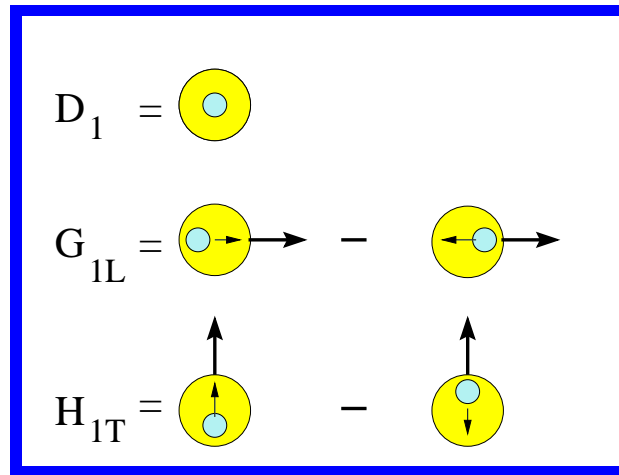
Twist-2 Fragmentation Functions

Functions surviving integration over intrinsic transverse momentum

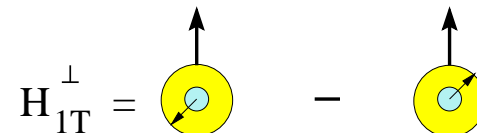


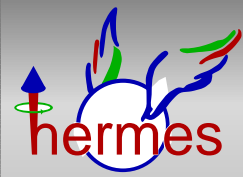
Twist-2 Fragmentation Functions

Functions surviving integration over intrinsic transverse momentum



Collins Function





The Need for Semi-Inclusive Measurements

- h_1 chiral odd
 - ⇒ not accessible in inclusive DIS
 - ⇒ need some sort of quark polarimetry
 - ⇒ **Collins Effect**: transverse spin of quark \rightsquigarrow transverse motion of produced hadron
- k_{\perp} -dependent distribution functions (besides f_1, g_1, h_1)
 - ⇒ vanish when integrating over k_{\perp} (i.e. inclusive DIS)
 - ⇒ need to access k_{\perp} -dependence

Azimuthal Single Spin Asymmetries in Semi-Inclusive DIS

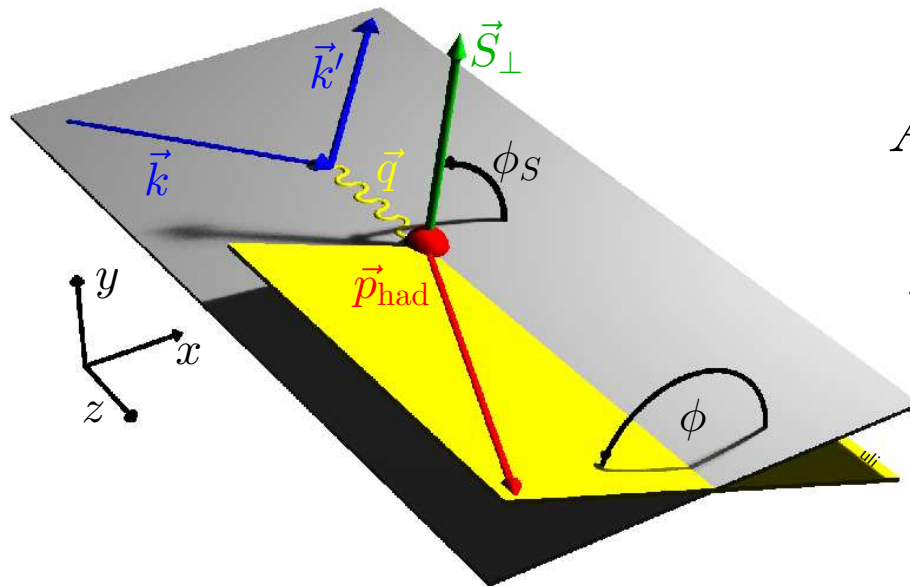
Single Spin Asymmetries

$$ep \longrightarrow e'\pi X$$

study azimuthal distribution of π 's:

$$A(\Phi) = \frac{1}{\langle P \rangle} \cdot \frac{N^+(\Phi) - N^-(\Phi)}{N^+(\Phi) + N^-(\Phi)}$$

with **transversely polarized target:**
(unpolarized beam)



$\Phi = \phi + \phi_S$ Collins angle

$$A_{UT}^{\sin \Phi} \propto \frac{\sum_q e_q^2 h_1^q(x) H_1^{\perp, q}(z)}{\sum_q e_q^2 f_1^q(x) D_1^q(z)}$$

Single Spin Asymmetries

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study azimuthal distribution of π 's:

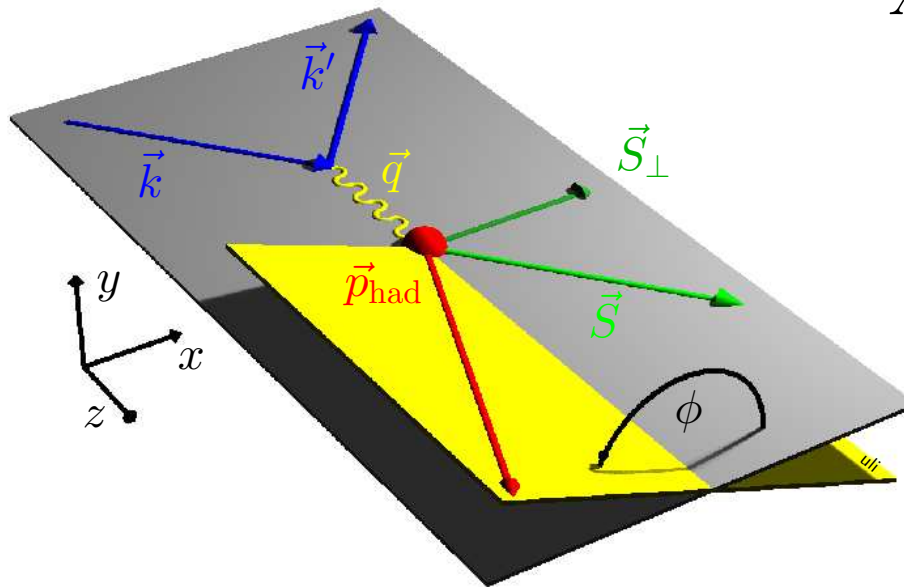
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with **longitudinally polarized target**:

$$A_{UL}^{\sin \Phi} \propto \dots$$



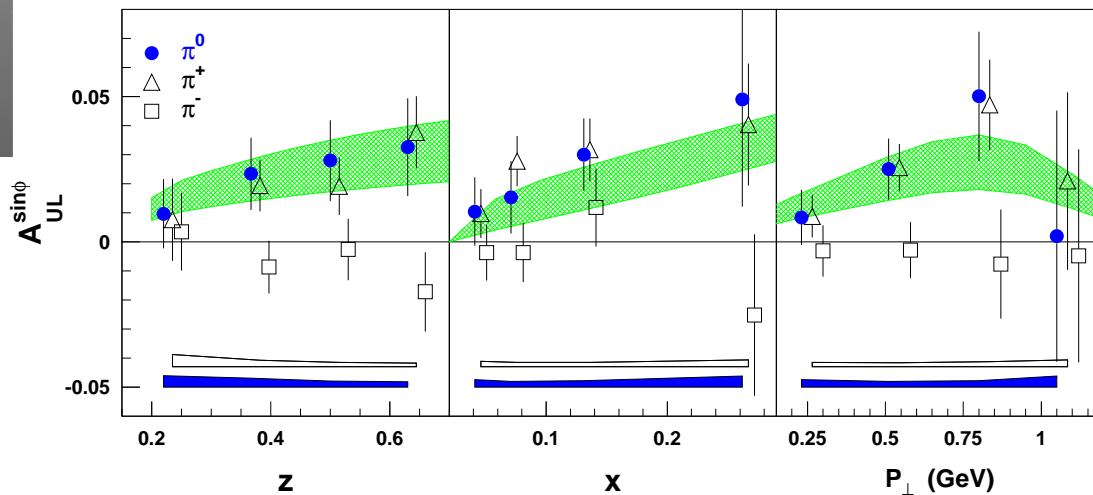
$\Phi = \phi$ Collins angle

Single Spin Asymmetries at HERMES

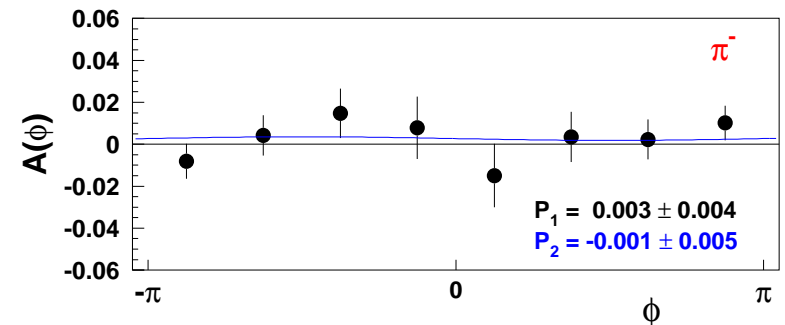
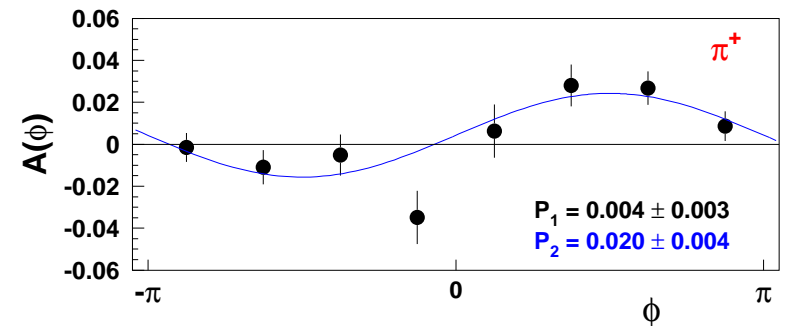
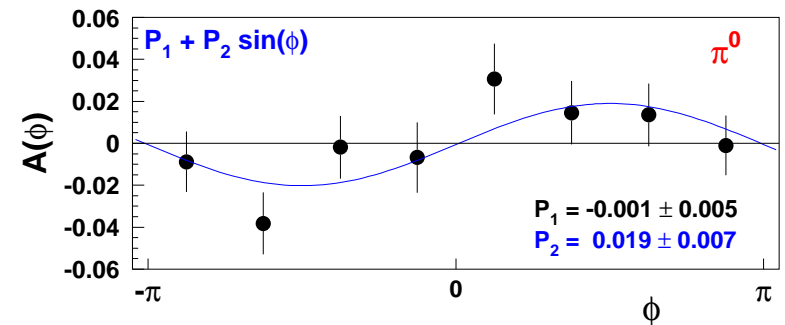
HERMES 1996/97: longitudinally polarized proton target

Longitudinal target SSA:

$$A_{UL}^{\sin\phi}(\phi) = \frac{1}{\langle P \rangle} \cdot \frac{N^+(\phi) - N^-(\phi)}{N^+(\phi) + N^-(\phi)}$$

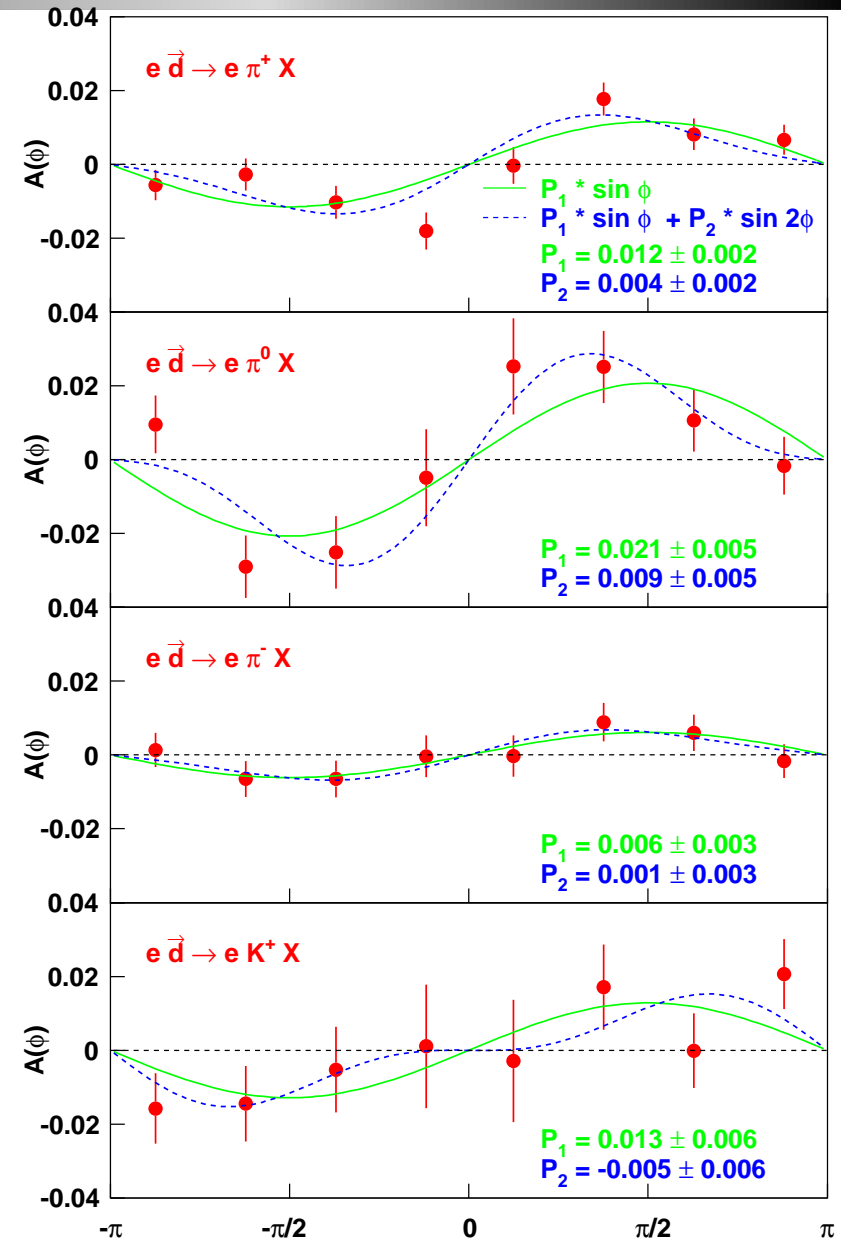


(green band: model calculation)



HERMES Results on *Deuteron Target*

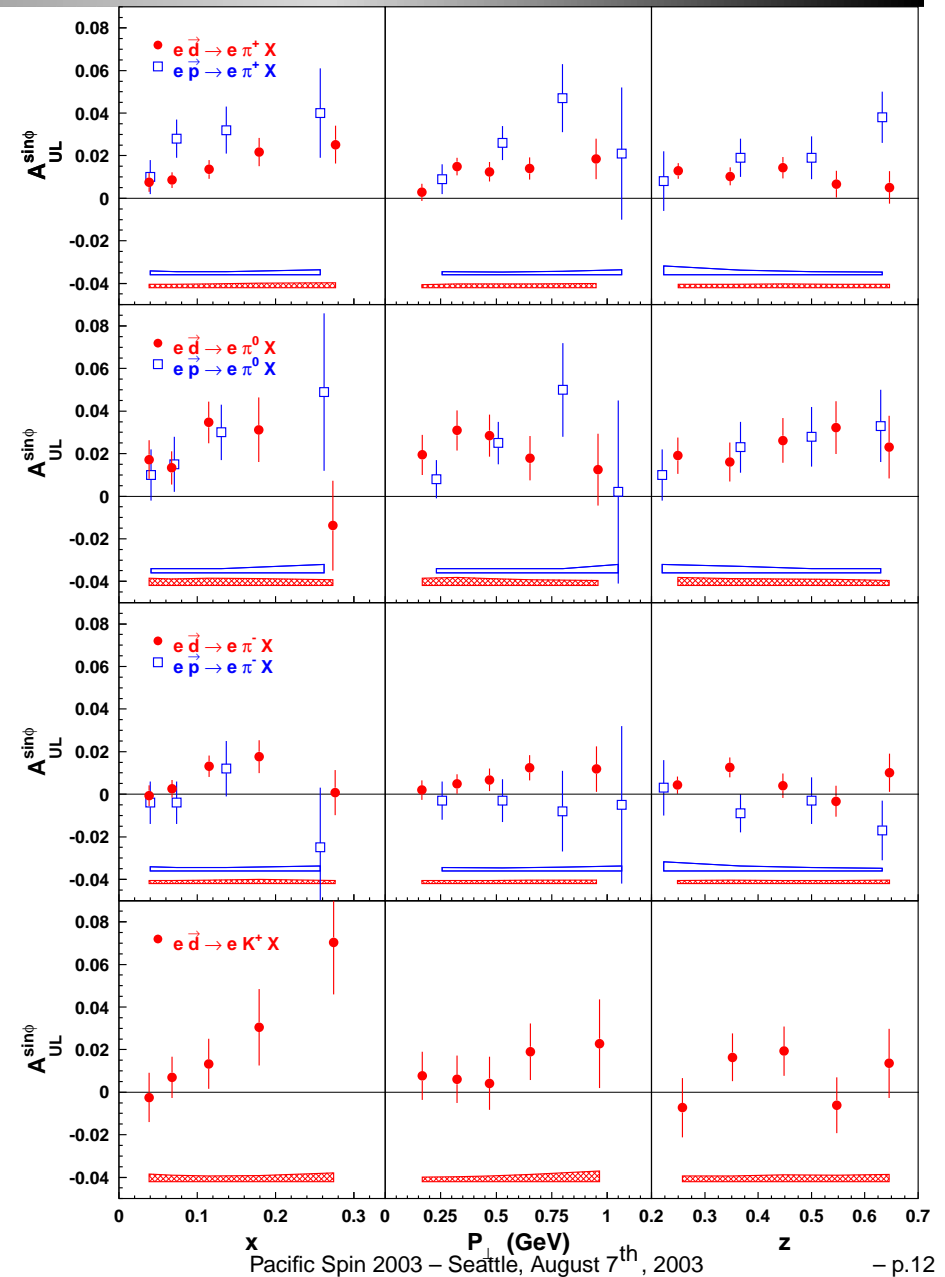
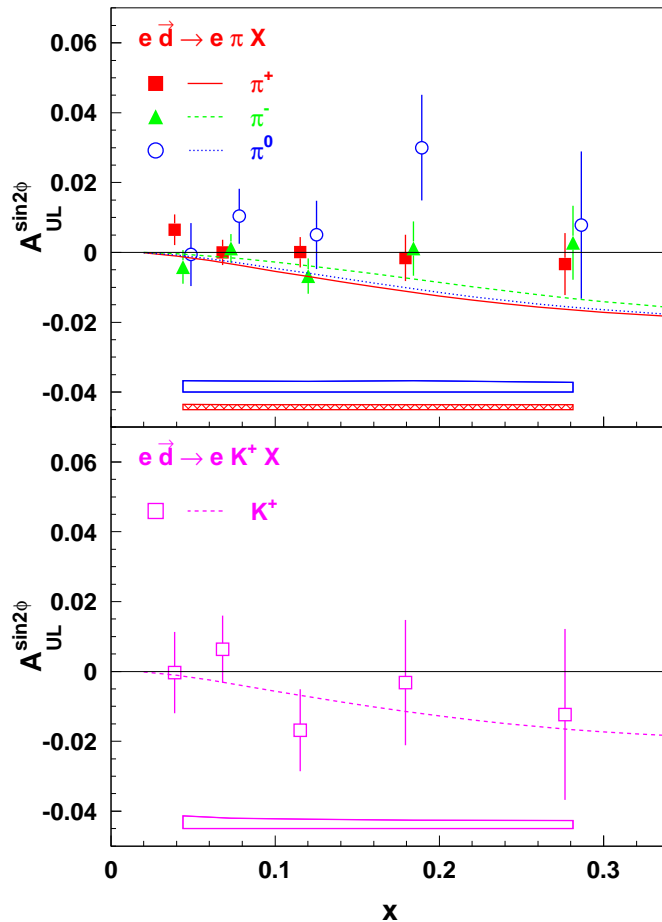
- HERMES 1998-2000: longitudinally polarized **deuteron** target
- High statistics: **~8 Million DIS**
- Good hadron identification due to RICH
- First measurement of Kaon **SSA**



HERMES Results on Longitudinally Polarized Deuteron

$\sin(\phi)$ -moment \Rightarrow

$\sin(2\phi)$ -moment $\sim h_{1L}^\perp H_1^\perp$



Longitudinally Polarized Target

transverse component S_T of target spin (w.r.t. virtual photon):

$$S_T \propto \sin \Theta_\gamma \simeq \frac{2Mx}{Q} \sqrt{1-y} \sim 0.15$$

$$A_U^{\sin \phi} \underset{L}{\sim} S_L \langle \sin \phi \rangle - S_T \langle \sin \phi \rangle \underset{T}{\sim}$$

Longitudinally polarized in experiment

(along beam direction)

L/T polarized in theory

(along virtual gamma direction)

Longitudinally Polarized Target

transverse component S_T of target spin (w.r.t. virtual photon):

$$S_T \propto \sin \Theta_\gamma \simeq \frac{2Mx}{Q} \sqrt{1-y} \sim 0.15$$

$$A_{UL}^{\sin \phi} \sim S_L \langle \sin \phi \rangle_{UL} - S_T \langle \sin \phi \rangle_{UT}$$

$$\langle \sin \phi \rangle_{UL} \sim \frac{1}{Q} \sum_q e_q^2 (h_L^q(x) H_1^{\perp(1),q}(z) - \frac{1}{z} h_{1L}^{\perp(1),q}(x) \tilde{H}(z))$$

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$$\langle \sin \phi \rangle_{UT} \sim \sum_q e_q^2 h_1^q(x) H_1^{\perp(1),q}(z) \quad (\text{but } S_T \sim \frac{1}{Q} \text{ like twist-3})$$

Longitudinally Polarized Target

transverse component S_T of target spin (w.r.t. virtual photon):

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$$\langle \sin \phi \rangle_{UT} \sim \sum_q e_q^2 h_1^q(x) H_1^{\perp(1),q}(z) \quad \text{Collins}$$

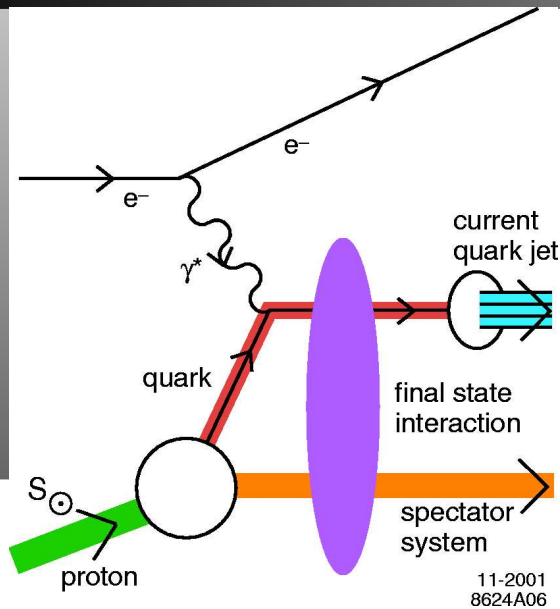
$$\langle \sin \phi \rangle_{UT} \sim \sum_q e_q^2 f_{1T}^{\perp(1),q} D_1^q(z) \quad \text{Sivers}$$

Contributions to $A_{UL}^{\sin \phi}$ hard to disentangle

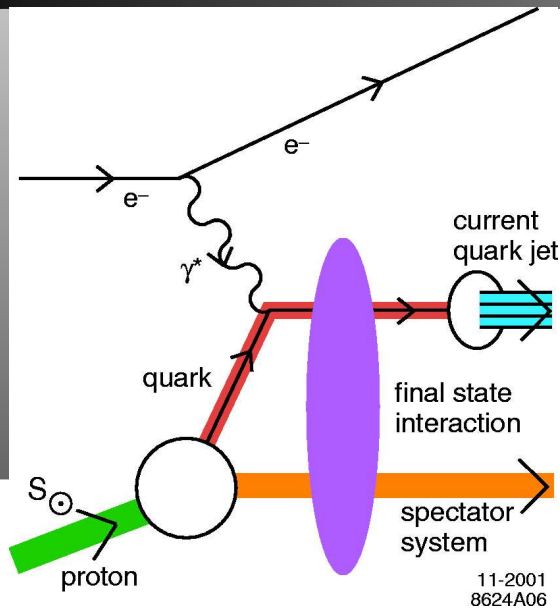
Some words about **Sivers Effect**

thanks to Brodsky, Hwang, Schmidt:

- quark rescattering
- can generate SSA
- leading twist effect
- requires L_z of quarks



Some words about **Sivers Effect**



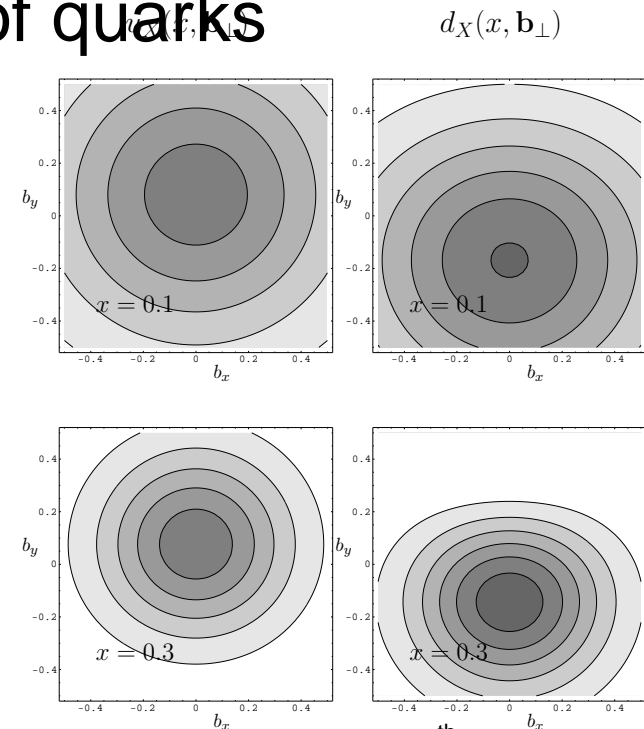
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different approach by Burkardt:

spatial distortion of q-distribution

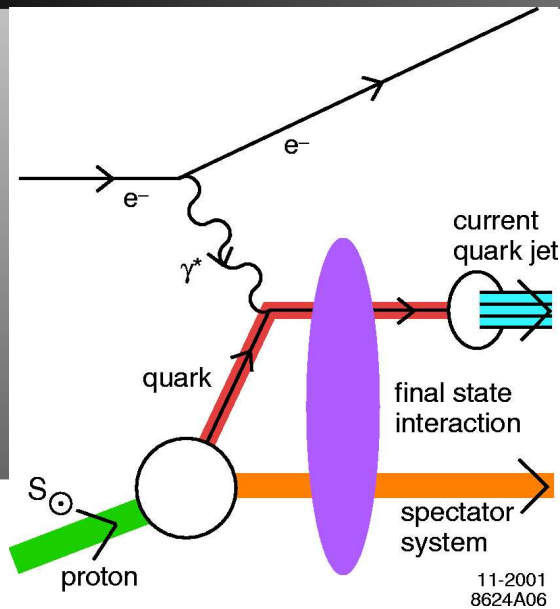
(consequence of anom. magn. moments
& impact parameter dependent PDFs)



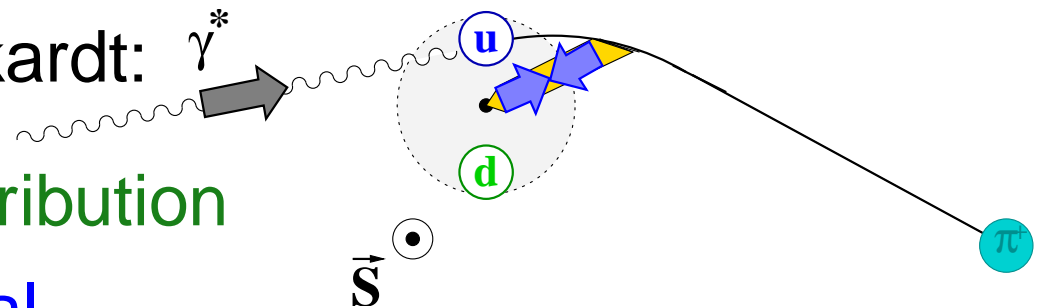
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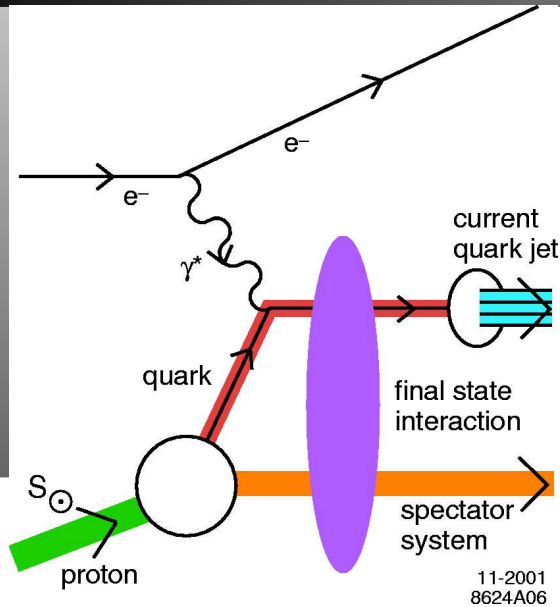


spatial distortion of q-distribution

+ attractive QCD potential

(gluon exchange)

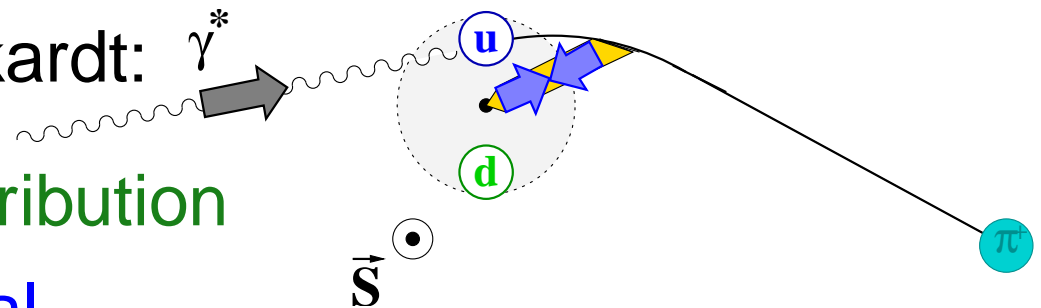
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different approach by Burkardt:



spatial distortion of q-distribution

+ attractive QCD potential

⇒ transverse asymmetries

Longitudinally polarized target \Rightarrow Sivers and Collins effects indistinguishable

Transversely polarized target

\swarrow
Sivers

$\langle \sin(\phi - \phi_s) \rangle$ moment

\downarrow
 $f_{1T}^\perp(x)$

\swarrow
Collins

$\langle \sin(\phi + \phi_s) \rangle$ moment

\downarrow
 $h_1(x), H_1^\perp(z)$

Additionally: $\langle \sin(3\phi - \phi_s) \rangle$ moment $\Rightarrow h_{1T}^\perp(x), H_1^\perp(z)$
and others

What do theorists expect?

Not much is known about the Collins FF:

$$\left| \frac{\langle H_1^\perp \rangle}{\langle D_1 \rangle} \right| = 6.3\%$$

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$$\left| \frac{\langle H_1^\perp \rangle}{\langle D_1 \rangle} \right| = 6.3\%, 12.5\%, \sim 4\% \dots ???$$

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Even less for the Sivers DF:

$$f_{1T}^{\perp,u} \neq 0$$

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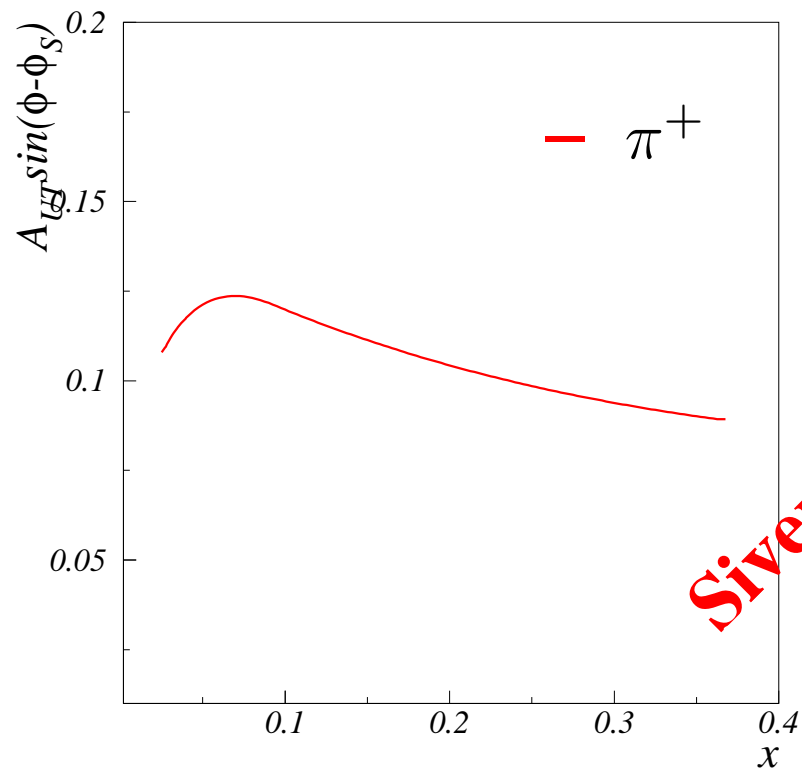
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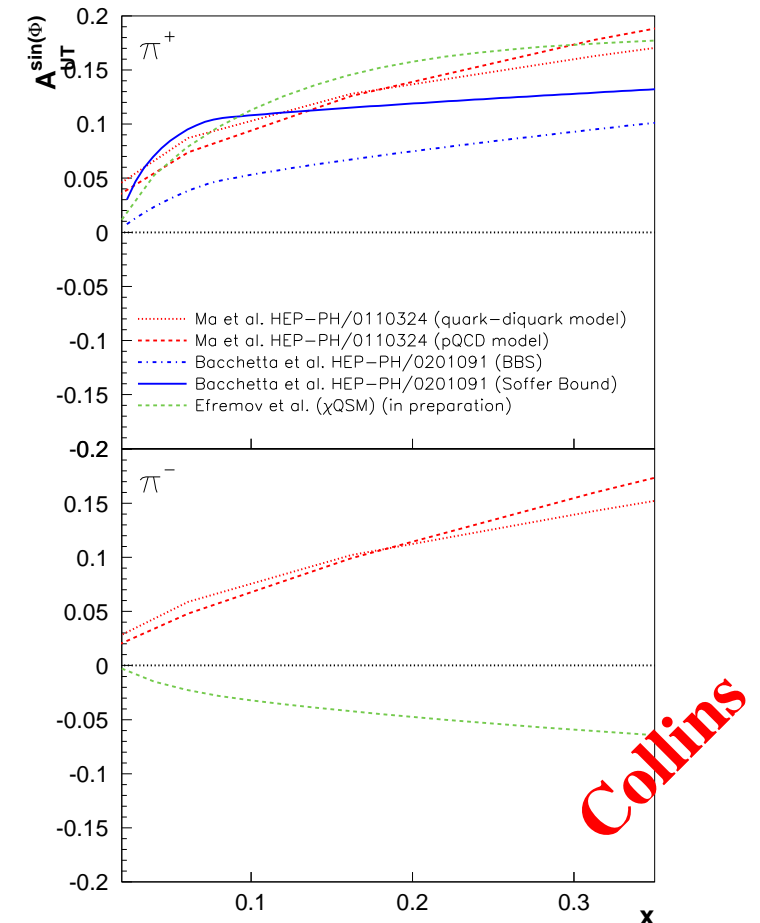
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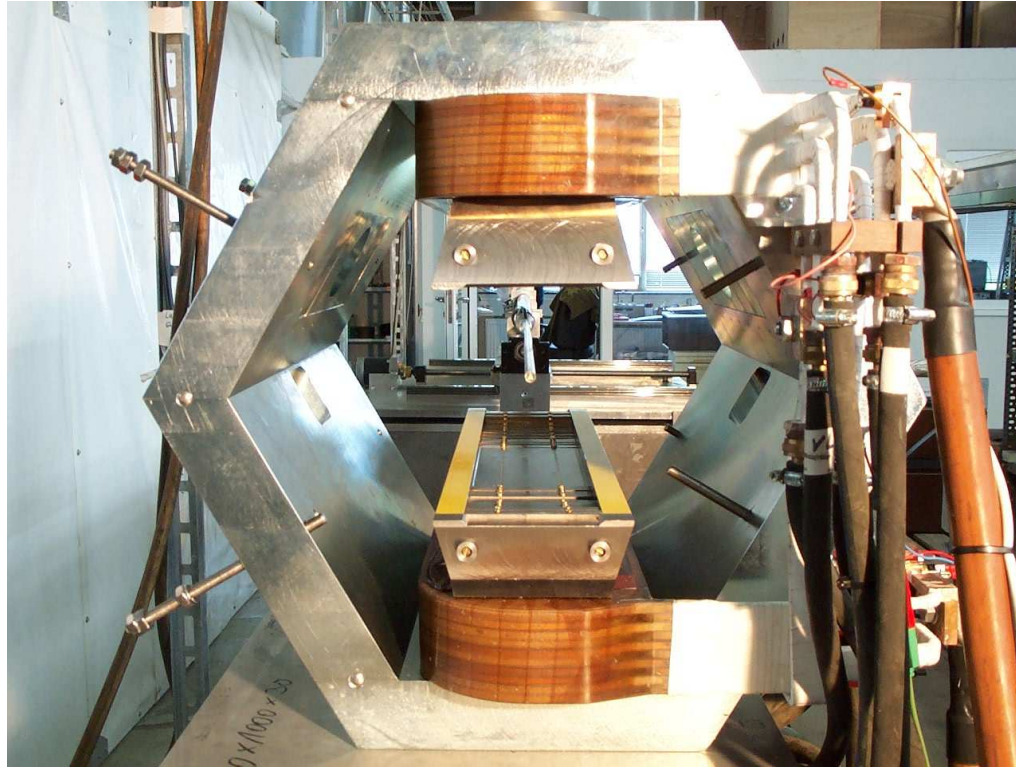
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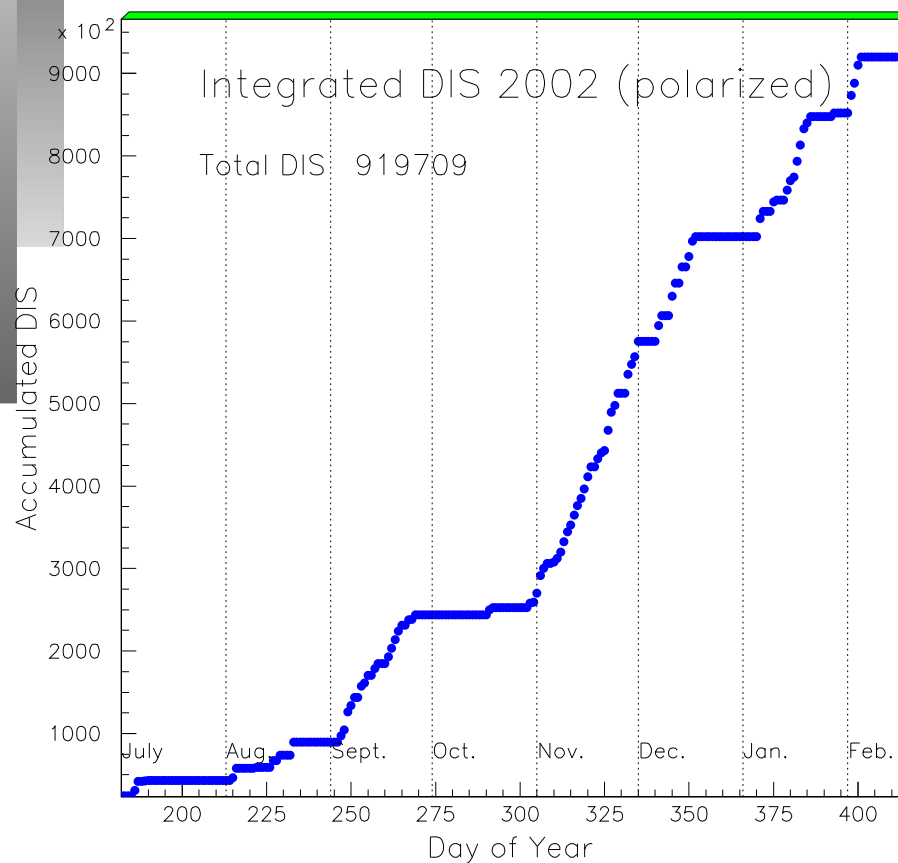
Gamberg et al. HEP-PH/0301018



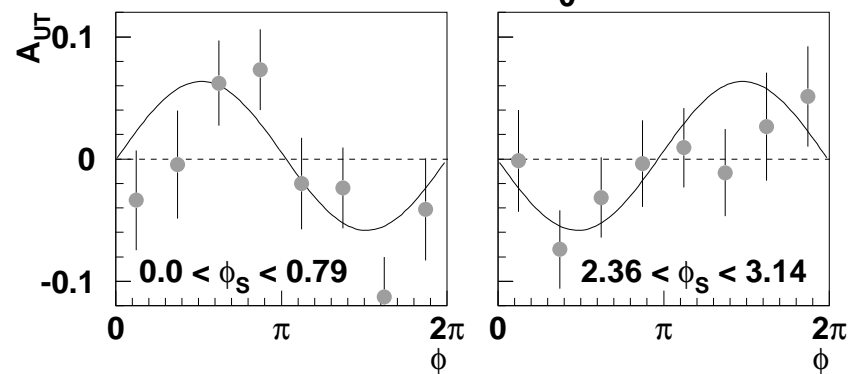
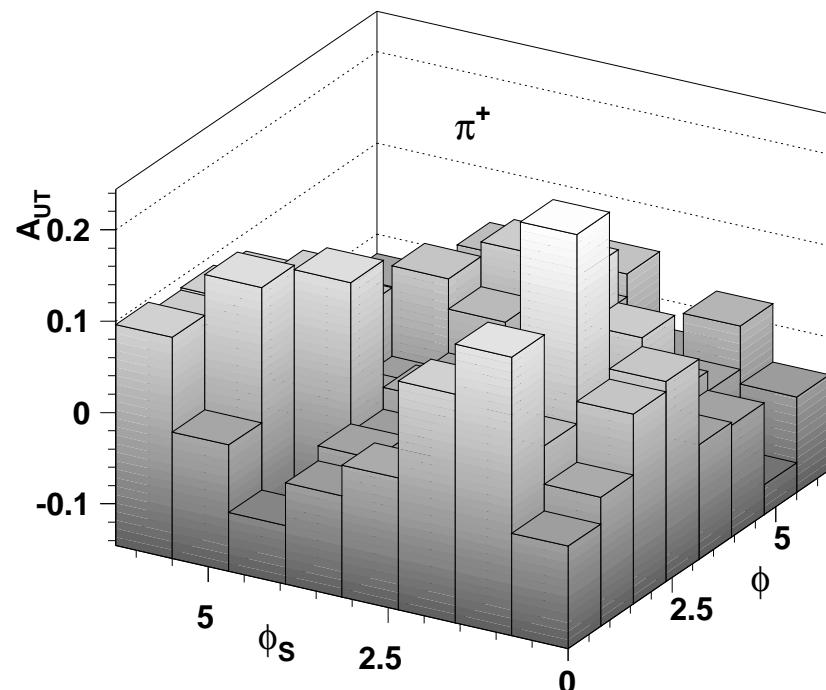
New Transverse Target HERMES



- **Transverse target magnet ($B = 0.295T$)**
- **High uniformity along beam direction: $\Delta B \leq 4.5 \cdot 10^{-5}T$**
- **Transversely polarized hydrogen**
- **Target polarization around 75%**



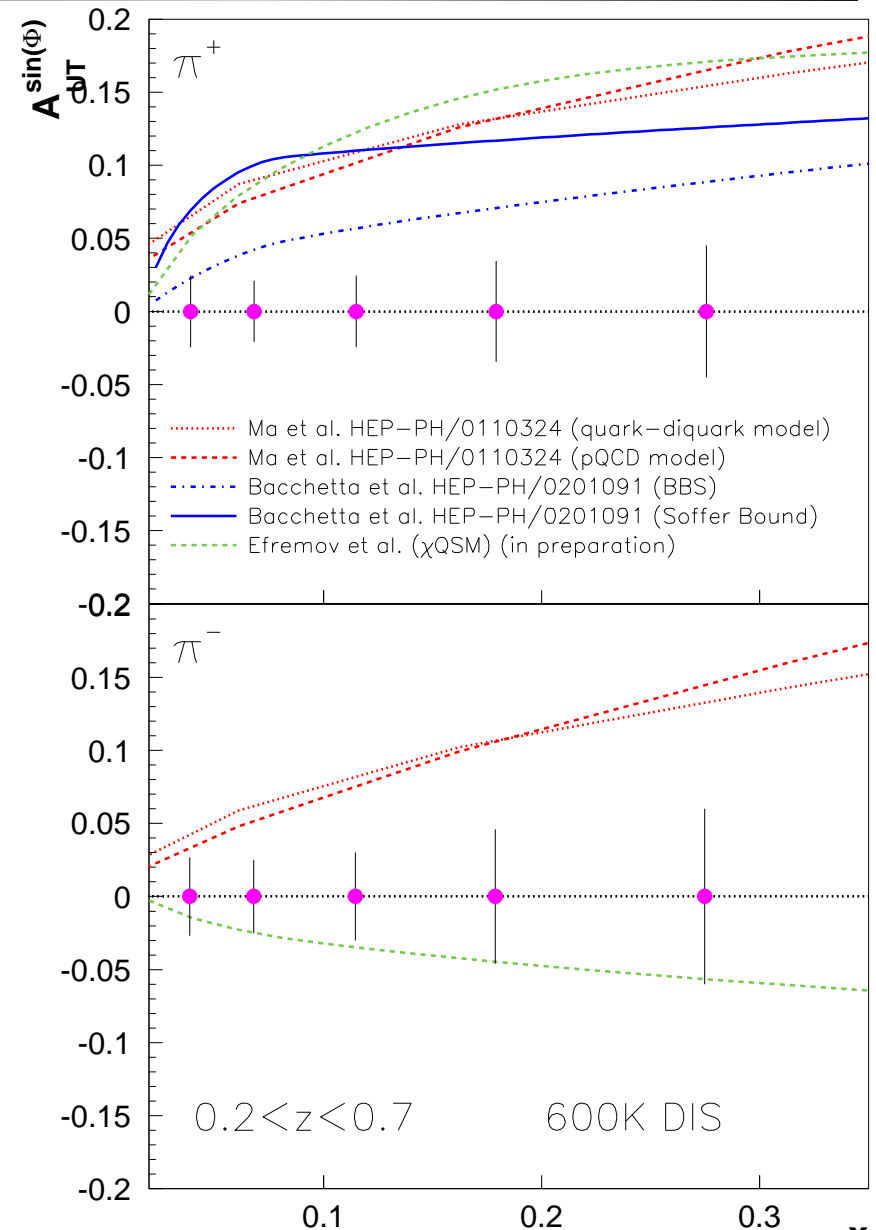
Integrated Luminosity 2002/03
(before data quality cuts)



Transverse Asymmetry $A_{UT}(\phi, \phi_S)$

Expected precision in comparison with model calculations for Collins Asymmetry

- After data quality: $\sim 600\text{K}$ DIS events
- charged and neutral π asymmetries
- statistics good enough to (dis)favour various model calculation



- **additional data taking** starting fall of 2003
 - **detector upgrade** (Λ -Wheels)
- ⇒ additional statistics allows analysis of different channels to access transversity:
- 2-Meson-Correlations ⇒ Interference FF

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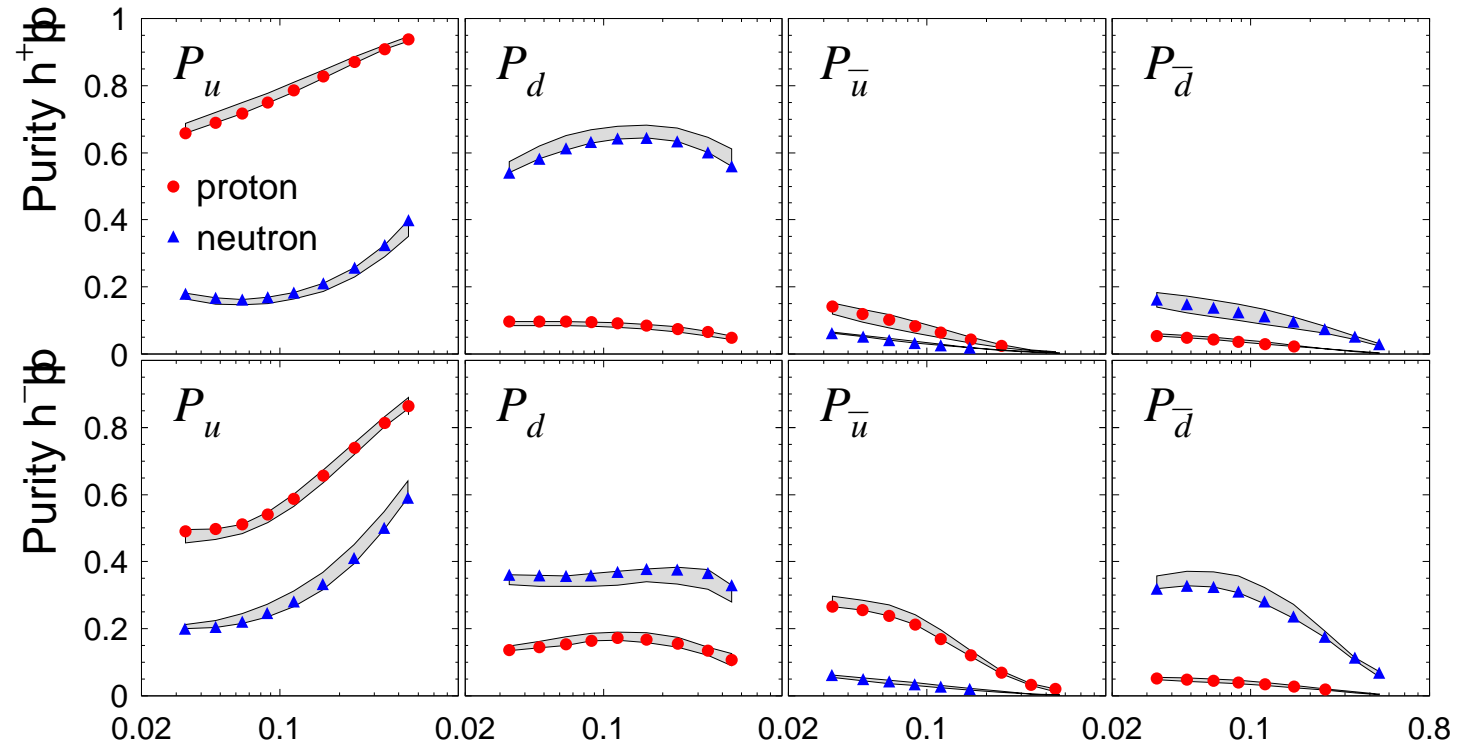
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- **polarized beam** ⇒ A_{LT} in π production
(measurement of twist-3 fragmentation function and transversity)

Extracting Quark Distributions – Purity Formalism

$$\begin{aligned}
 A_{UT}^{\sin(\phi-\phi_S),h}(x) &= \frac{\int dy S_T \frac{1+(1-y)^2}{2} \sum_q e_q^2 f_{1T}^{\perp,q}(x) \int dz D_1^{q,h}(z) \mathcal{A}(x,z)}{\int dy \frac{1+(1-y)^2}{2} \sum_{q'} e_{q'}^2 f_1^{q'}(x) \int dz D_1^{q',h}(z) \mathcal{A}(x,z)} \\
 &= c \cdot \sum_q \frac{e_q^2 f_1^q(x) \mathcal{D}_1^{q,h}(x)}{\sum_{q'} e_{q'}^2 f_1^{q'}(x) \mathcal{D}_1^{q',h}(x)} \cdot \frac{f_{1T}^{\perp,q}(x)}{f_1^q(x)} \\
 &= c \cdot \sum_q \mathcal{P}_q^h(x) \cdot \frac{f_{1T}^{\perp,q}(x)}{f_1^q(x)}
 \end{aligned}$$

- purities are completely unpolarized objects → present Monte Carlo-tunes can be used
- probabilistic interpretation of purities possible
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Extracting Quark Distributions – Purity Formalism



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Extracting Quark Distributions – Purity Formalism

$$\begin{aligned}
 A_{UT}^{\sin(\phi+\phi_S),h}(x) &= \frac{\int dy S_T(1-y) \sum_q e_q^2 h_1^q(x) \int dz H_1^{\perp,q,h}(z) \mathcal{A}(x,z)}{\int dy \frac{1+(1-y)^2}{2} \sum_{q'} e_{q'}^2 f_1^{q'}(x) \int dz D_1^{q',h}(z) \mathcal{A}(x,z)} \\
 &= \mathcal{C} \cdot \sum_q \frac{e_q^2 f_1^q(x) \mathcal{H}_1^{\perp,q,h}(x)}{\sum_{q'} e_{q'}^2 f_1^{q'}(x) \mathcal{D}_1^{q',h}(x)} \cdot \frac{h_1^q}{f_1^q}(x) \\
 &= \mathcal{C} \cdot \sum_q \mathcal{P}_q^h(x) \cdot \frac{h_1^q}{f_1^q}(x)
 \end{aligned}$$

- **purities** are completely **unpolarized** objects → present Monte Carlo-tunes can be used
- **probabilistic interpretation** of purities possible
- “easy”: Sivers ← fragmentation function (D_1) known
- Collins: these purities still **depend on parametrization** of Collins FF function

- HERMES measured SSA on **longitudinally polarized hydrogen and deuterium** targets
- HERMES has taken data with a **transversely polarized hydrogen** target
- Presently more than **600k** DIS events after data quality cuts
- **Transverse Asymmetries** \Rightarrow disentangle Sivers and Collins contributions
- **Purity** formalism \Rightarrow extraction of quark distributions $f_{1T}^{\perp,q}$ and h_1^q ($q = u, d$)
- IFF on longitudinal/transversely polarized target
- . . .