

The (mysterious) Proton Spin

Klaus Rith

University of Erlangen -Nürnberg & DESY

Simposio Dalpiaz, October 17-18, 2008 - Ferrara

CERN/SPSC/74-78
SPSC P.18
1 July 1974

PROPOSED EXPERIMENTS AND EQUIPMENT
FOR A PROGRAMME OF MUON PHYSICS AT THE SPS

by

The European Muon Collaboration

1980-84:
19 joint publications

The European Muon Collaboration

British Participants: R. Clift, E. Gabathuler, H. Montgomery, P.R. Norton, J.C. Thompson (Daresbury Laboratory), T. Sloan (Lancaster Univ.), G.R. Court, R. Gamet, P. Hayman, J.R. Holt (Liverpool Univ.), W.S. Williams (Oxford Univ.), F. Combley (Sheffield Univ.) and F. Farley (R.M.C. Shrivenham).

CERN Participants: M. Borghini and J.H. Field.

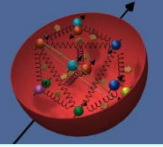
French Participants: J.J. Aubert, C. Broll, X. de Bouard, G. Coignet, J. Favier, H. de Kerrett, L. Massonnet, H. Pessard, F. Vannucci and M. Vivargent (Institut de Physique Nucléaire, Orsay).

German Participants: H.J. Behrend, F.W. Brasse, W. Flauger, J. Gayler, V. Korbel*, A. Ladage, J. May, P. Söding (Deutsches Elektronen-Synchrotron, Hamburg), U. Hahn, K. Moser, K. Rith, E. Schlösser, H.E. Stier (Freiburg Univ.), O.C. Allkofer (Kiel Univ.), K.H. Becks, J. Drees, U. Opara and H. Wahlen (Wuppertal Univ.).

* Now at CERN.

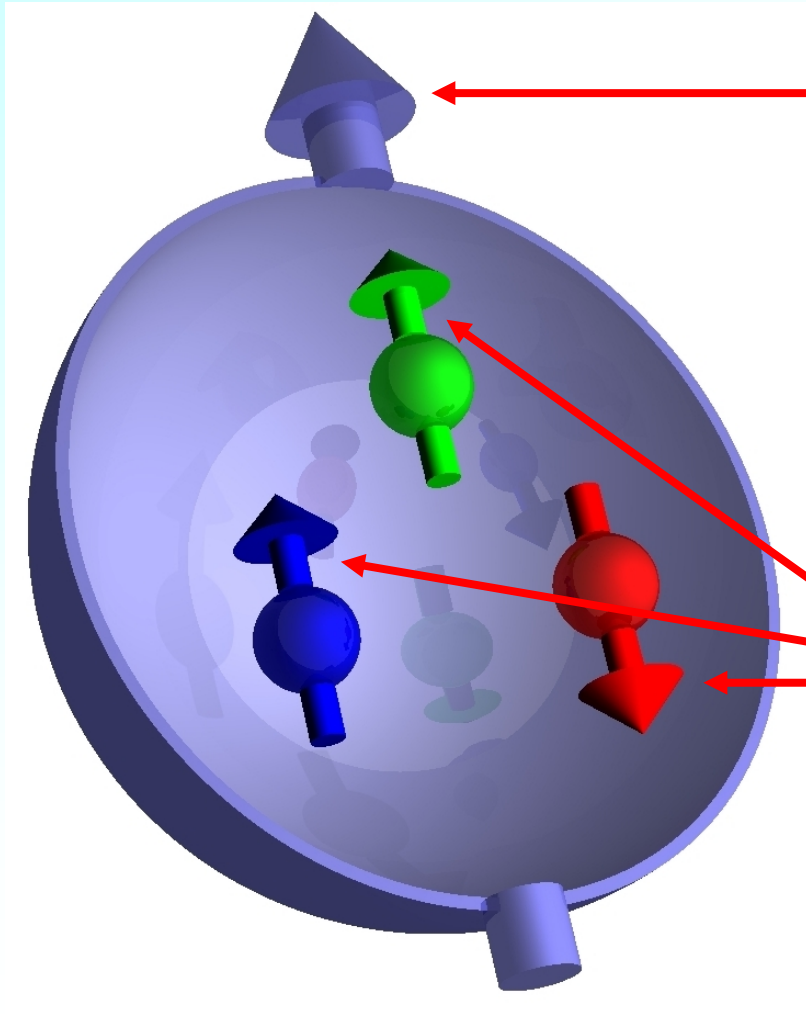
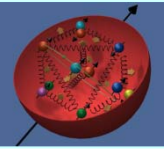
Italian Participants: P. Dalpiaz, P.F. Dalpiaz, M.I. Ferrero and C. Franzinetti (Turin Univ.).

Contactman: E. Gabathuler - present address NP-Division, CERN.



- Spin: extremely important quantity in quantum physics with properties of angular momentum
- Spin-1/2 particles:
fundamental constituents [quarks, leptons (e, μ, τ , neutrinos), proton, neutron,...]
- Spin-1/2 responsible for stability of matter (Pauli-principle):
No two Spin-1/2 particles can occupy a state where all quantum numbers are identical

Nucleon Spin: constituent quark model



Nucleon Spin

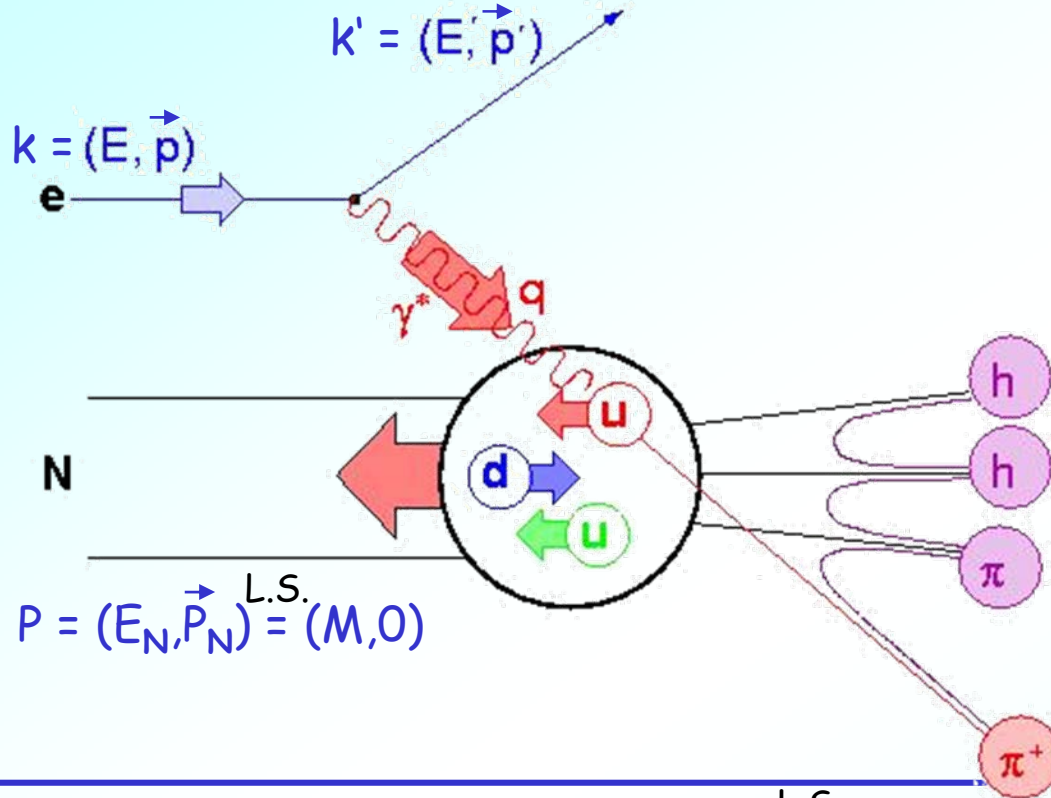
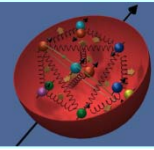
$$\frac{1}{2} = \frac{1}{2} \Delta\Sigma$$

Contribution of quark spins:

$$\Delta\Sigma = 1$$

Determination of $\Delta\Sigma$

Polarized deep-inelastic scattering



Asymmetries:

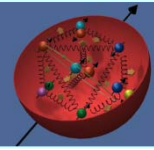
$$A = \frac{N \begin{matrix} \uparrow \downarrow \\ \downarrow \uparrow \end{matrix} - N \begin{matrix} \uparrow \uparrow \\ \downarrow \downarrow \end{matrix}}{N \begin{matrix} \uparrow \downarrow \\ \downarrow \uparrow \end{matrix} + N \begin{matrix} \uparrow \uparrow \\ \downarrow \downarrow \end{matrix}}$$

$$Q^2 = -q^2 = -(k - k')^2, \quad \nu = Pq/M \stackrel{\text{L.S.}}{=} E - E',$$

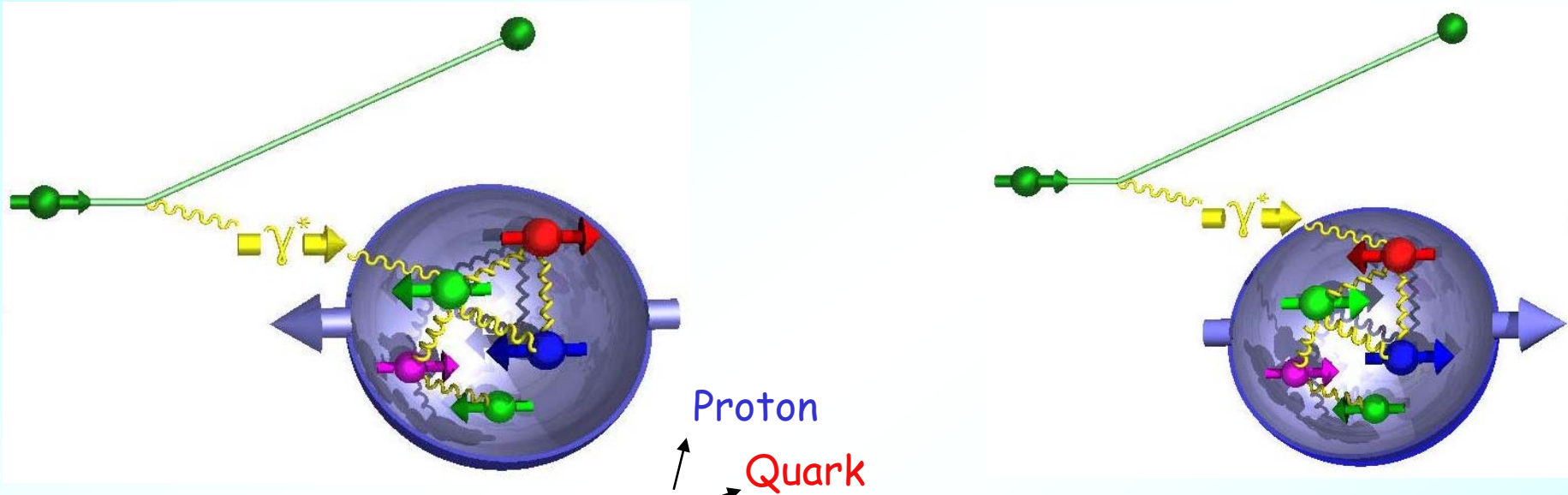
$x = Q^2/(2Pq)$ = fraction of nucleon's longitudinal momentum carried by struck quark

$q(x)$ = quark number density (quark momentum distribution)

Quark helicity distributions $\Delta q(x)$



More precisely: „helicity weighted momentum distributions“



$$q^+(x) = q^{\uparrow\uparrow}$$

$$q^-(x) = q^{\downarrow\uparrow}$$

$$\Delta q(x) = q^+(x) - q^-(x)$$

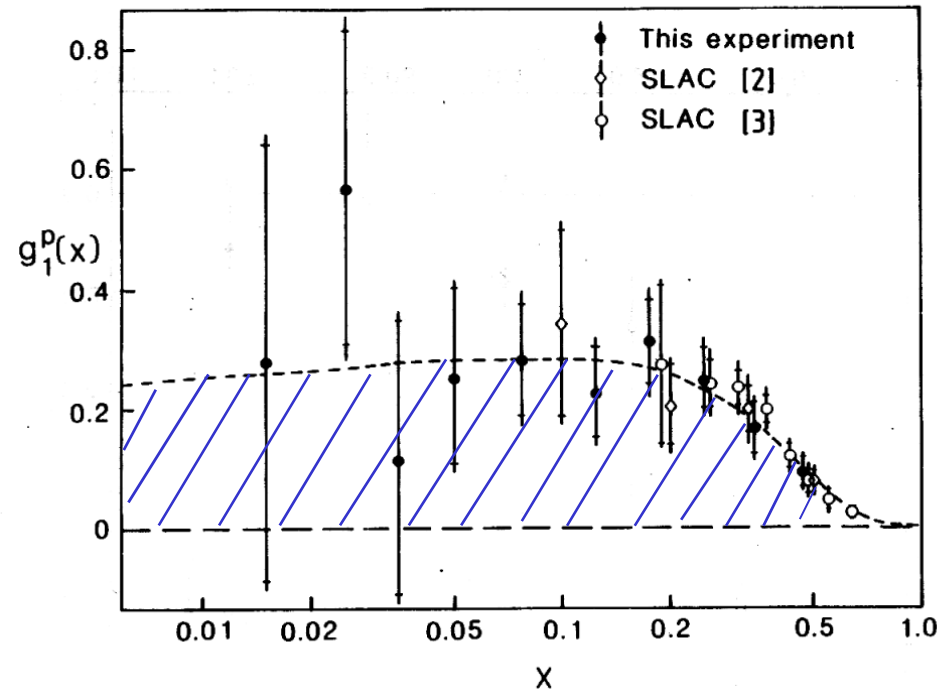
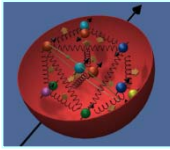
$$\Delta q = \int_0^1 \Delta q(x) dx$$

$$\Delta \Sigma = \sum_q \Delta q$$

$$g_1(x) = \frac{1}{2} \sum_q e_q^2 \Delta q(x)$$

$$\Gamma_1 = \int_0^1 g_1(x) dx$$

The EMC result for $g_1^p(x)$



$$\Gamma_1^p = 0,126 \pm 0,010 \pm 0,015$$

J. Ashman et al., PL B 206 (1988) 364 (1411 Cit.)

J. Ashman et al. Nucl. Phys. B 328 (1989) 1 (1212 Cit.)

Consequence (1987):

$$\Delta u \cong 0,78$$

$$\Delta d \cong -0,47$$

$$\Delta s \cong -0,19$$

1) Quark-'Sea' is negatively polarised

$$2) \Delta \Sigma = \Delta u + \Delta d + \Delta s = 0,12 \pm 0,09 \pm 0,14$$

Contribution of Quark Spins to Nucleon-Spin very small

Spin-'crises'

QPM:

$$4/3$$

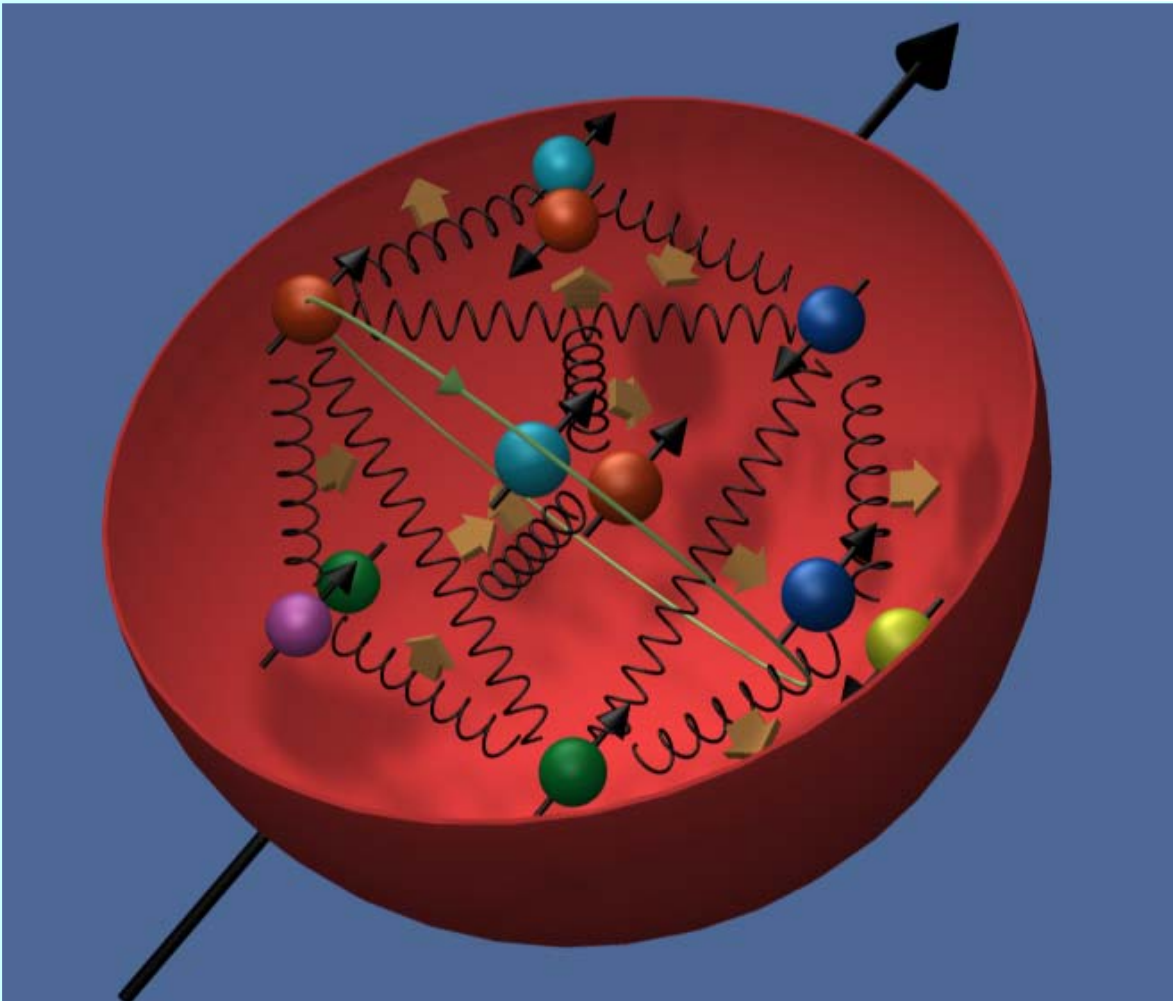
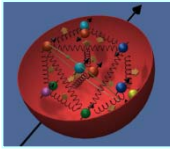
$$-1/3$$

$$0$$

1

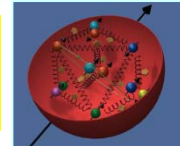


Nucleon Spin: QCD picture

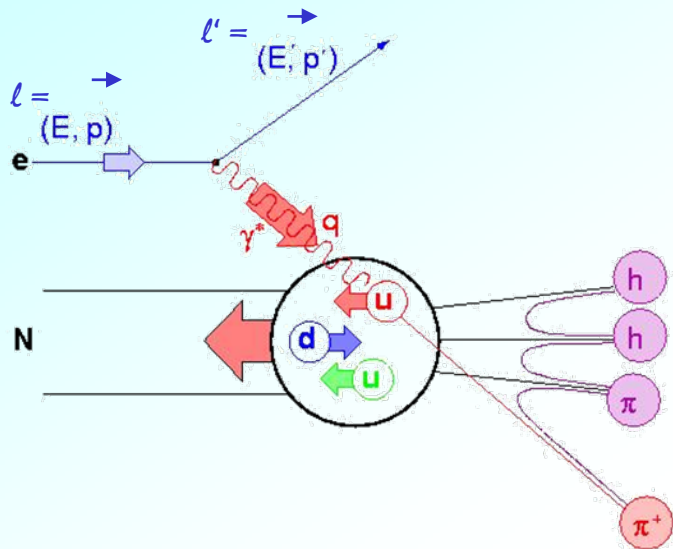


$$\begin{aligned} \frac{1}{2} &= \frac{1}{2} \Delta\Sigma \text{ (Quark spins)} \\ &+ \Delta G \text{ (Gluon spins)} \\ &+ L_q + L_g \\ &\text{(Orbital angular momenta)} \end{aligned}$$

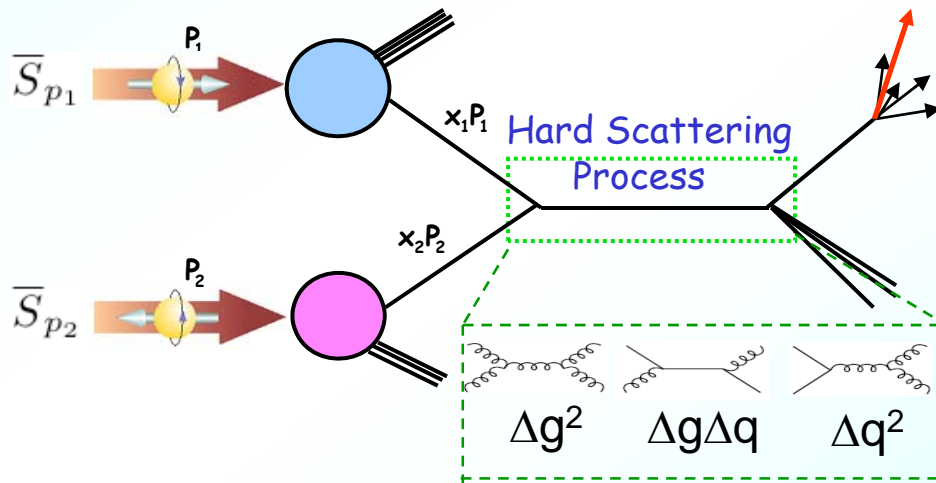
Nucleon Spin - Tools



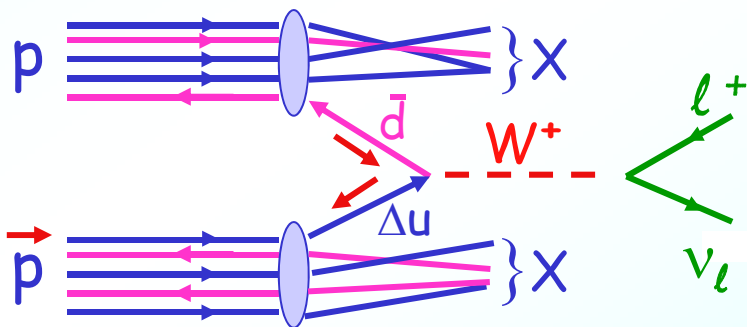
Polarised DIS



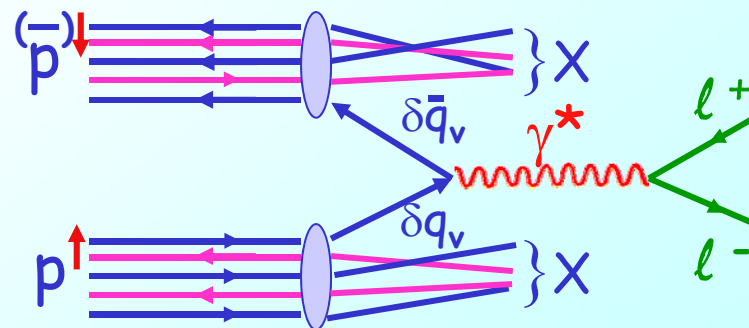
π^0 or jet production in $\vec{p}\vec{p}$



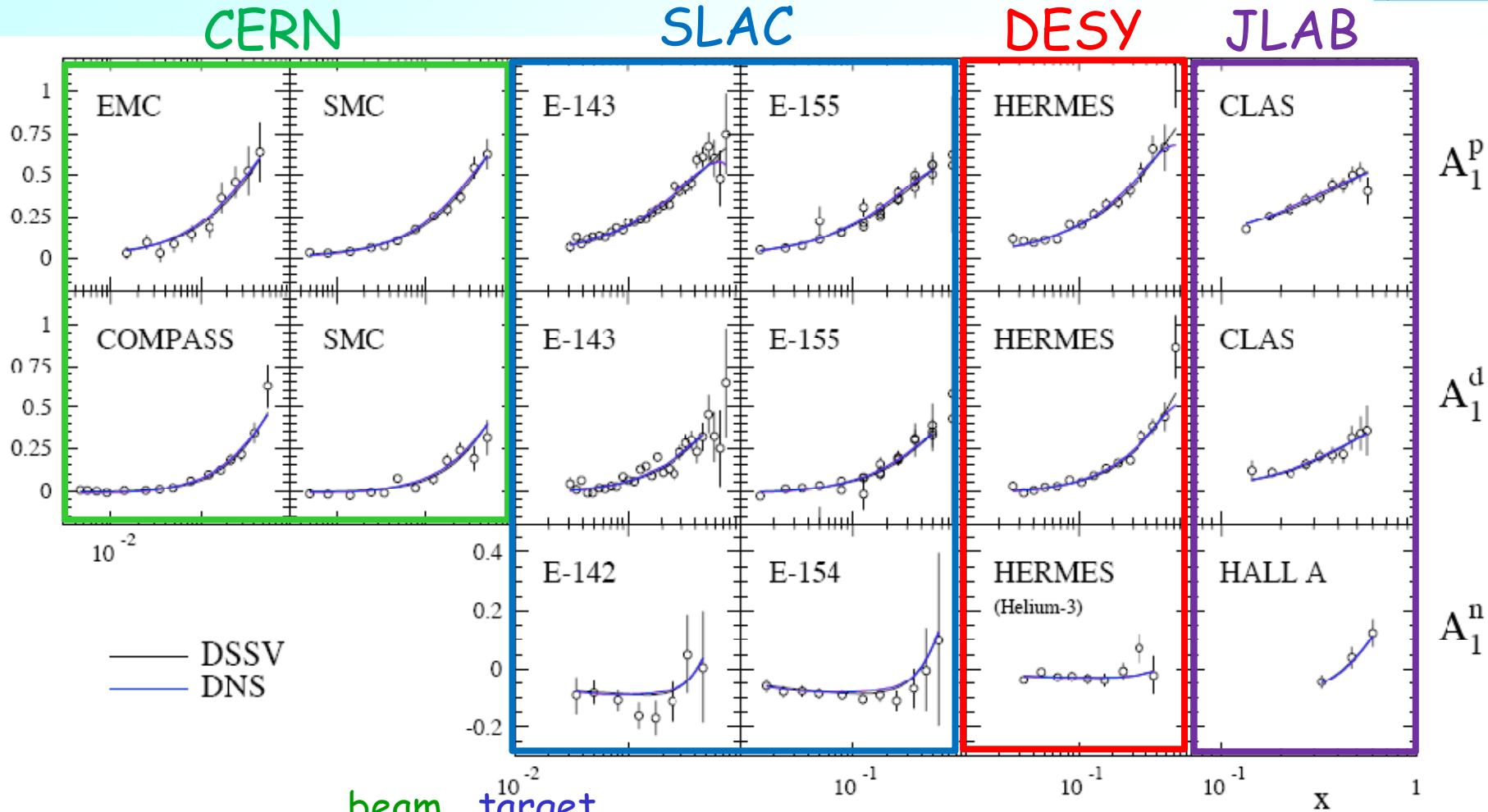
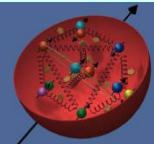
W^\pm -production



Drell-Yan



Asymmetries in polarized DIS



beam target

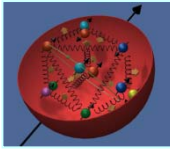
$$A_1(x) \cong \frac{\sigma^{\uparrow\downarrow} - \sigma^{\uparrow\uparrow}}{\sigma^{\uparrow\downarrow} + \sigma^{\uparrow\uparrow}} \stackrel{\text{L.O.}}{\cong} \frac{\sum_q e_q^2 \Delta q(x)}{\sum_q e_q^2 q(x)} = \frac{g_1(x)}{F_1(x)}$$

From W. Vogelsang

HERMES

HERA MEasurement of Nucleon Spin

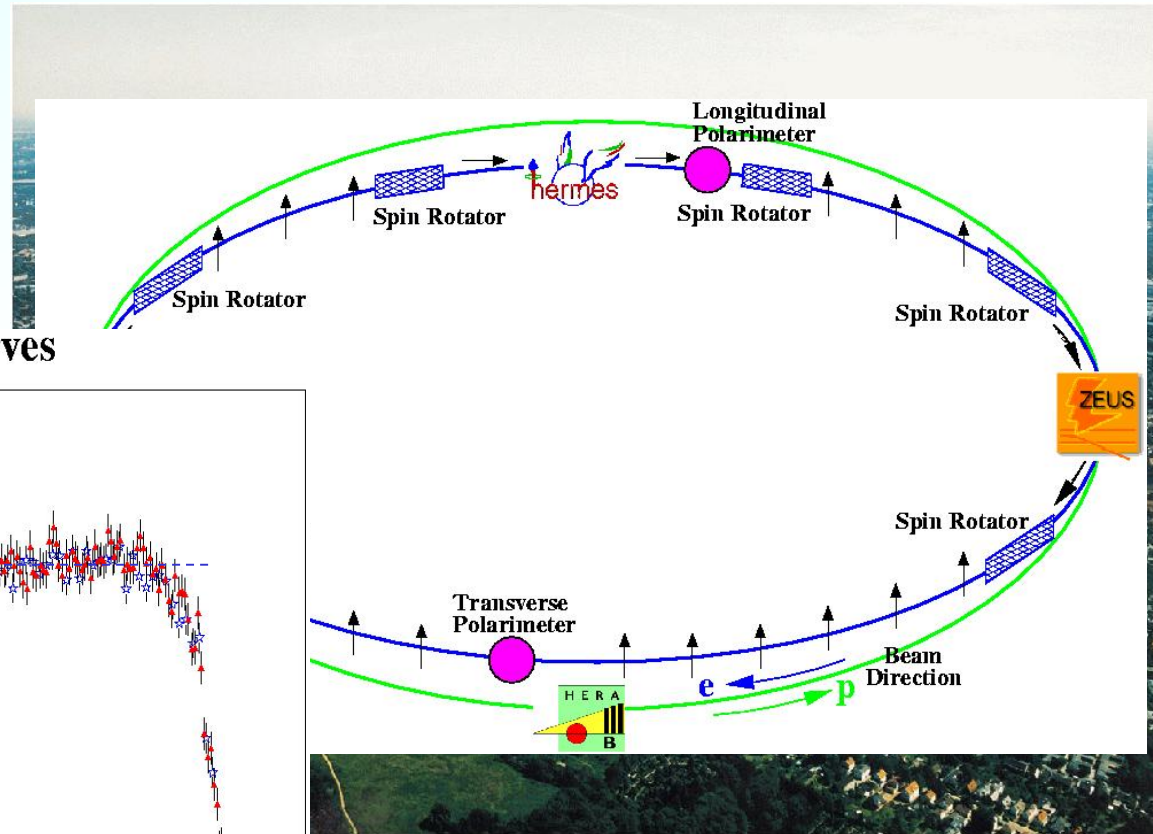
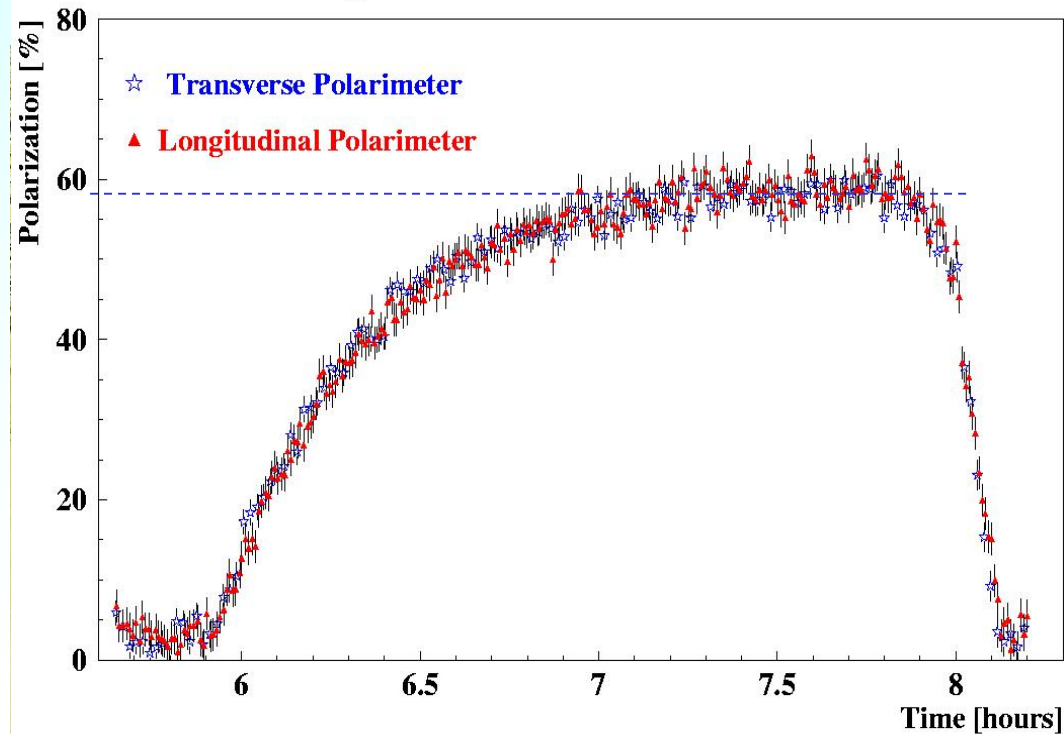
Ferrara group: 20 collaboration members in total



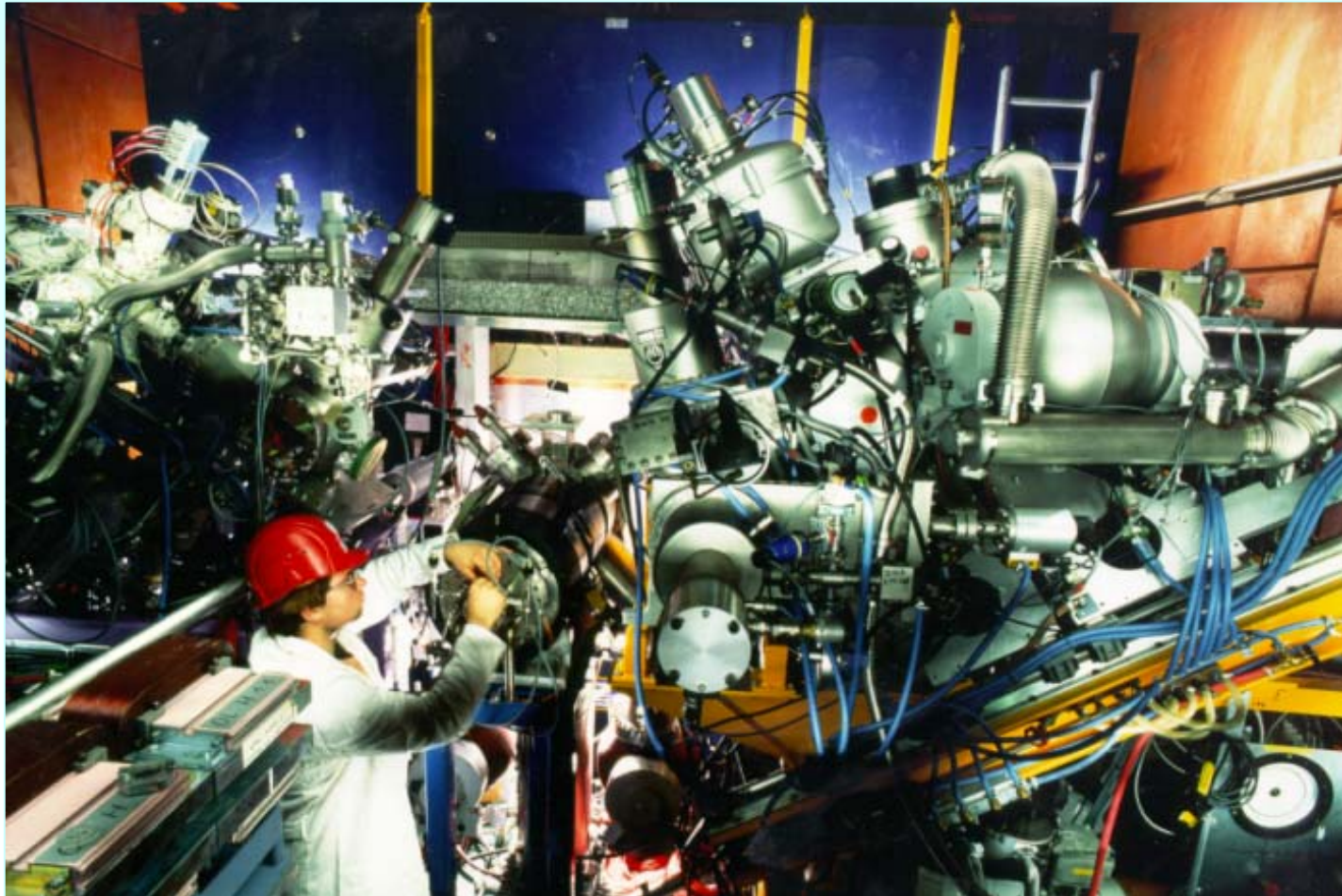
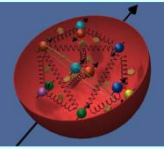
Electron beam:

$$E = 27.6 \text{ GeV}, I_e < 50 \text{ mA}$$

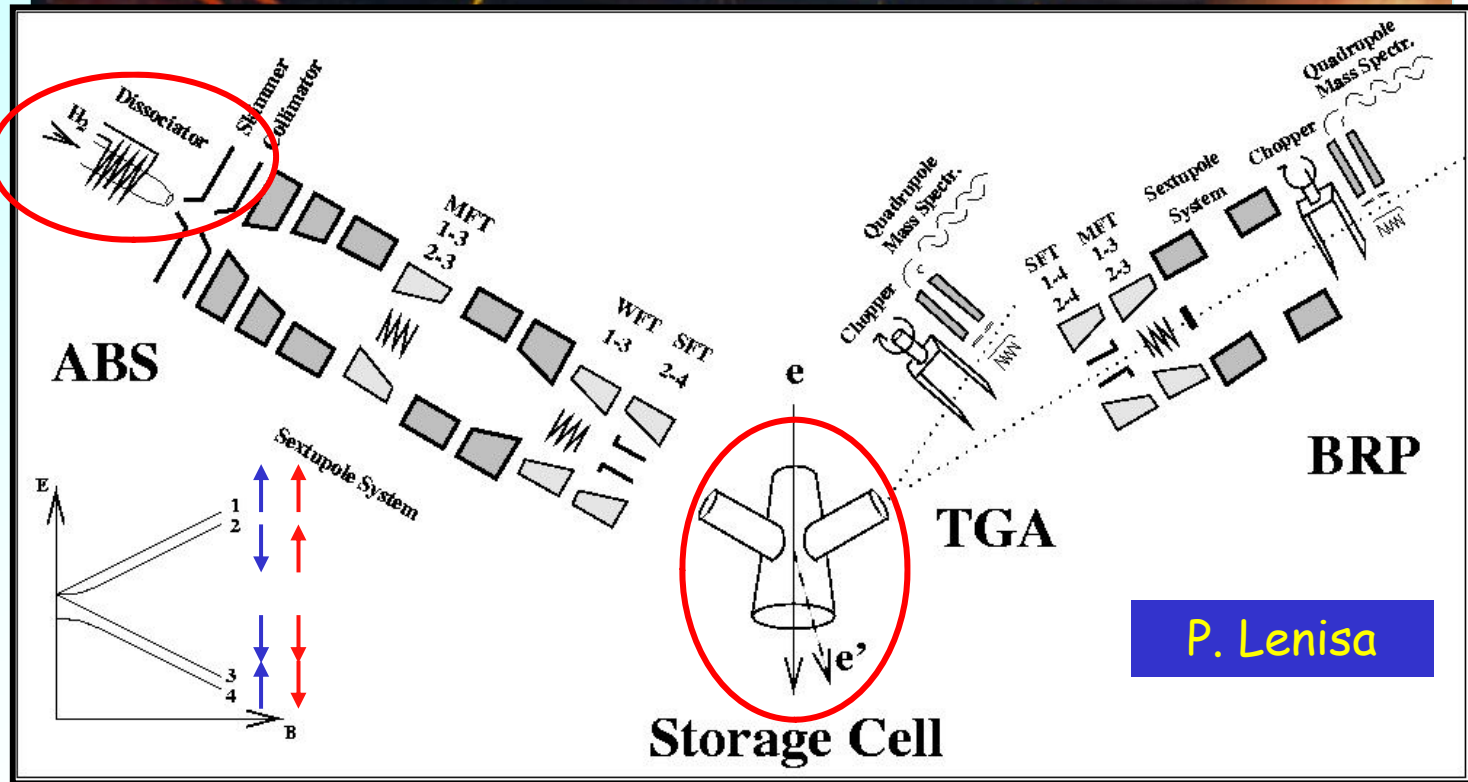
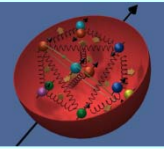
Comparison of rise time curves



Internal polarized storage-cell gas target



Internal polarized storage-cell gas target

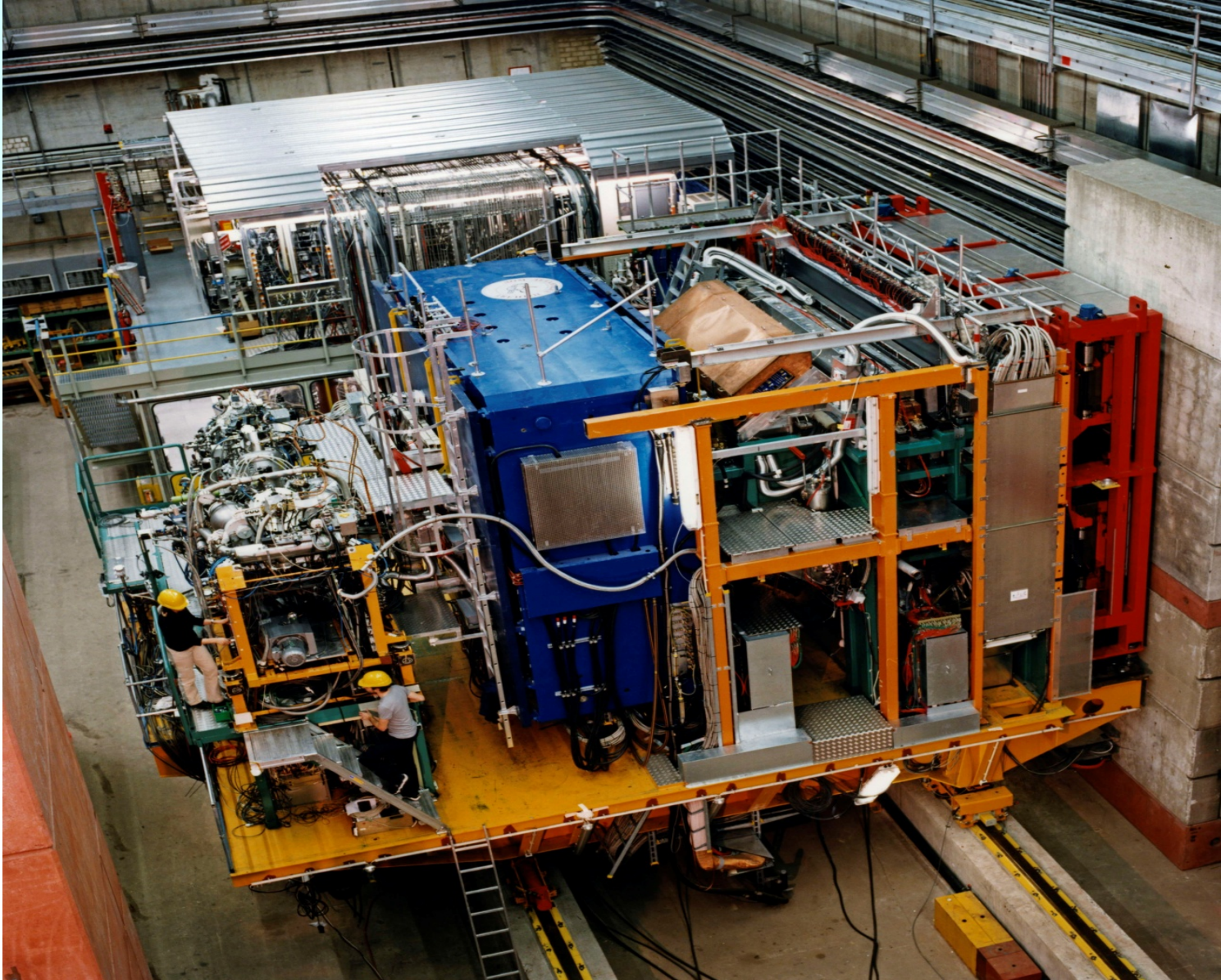
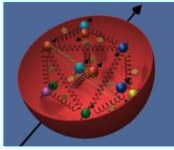


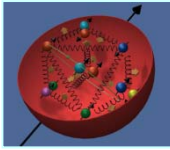
Principle: Stern-Gerlach separation of HF-states + RF-transitions

Target polarisation: $P_T \approx 0.85$, Dilution factor: $f=1$

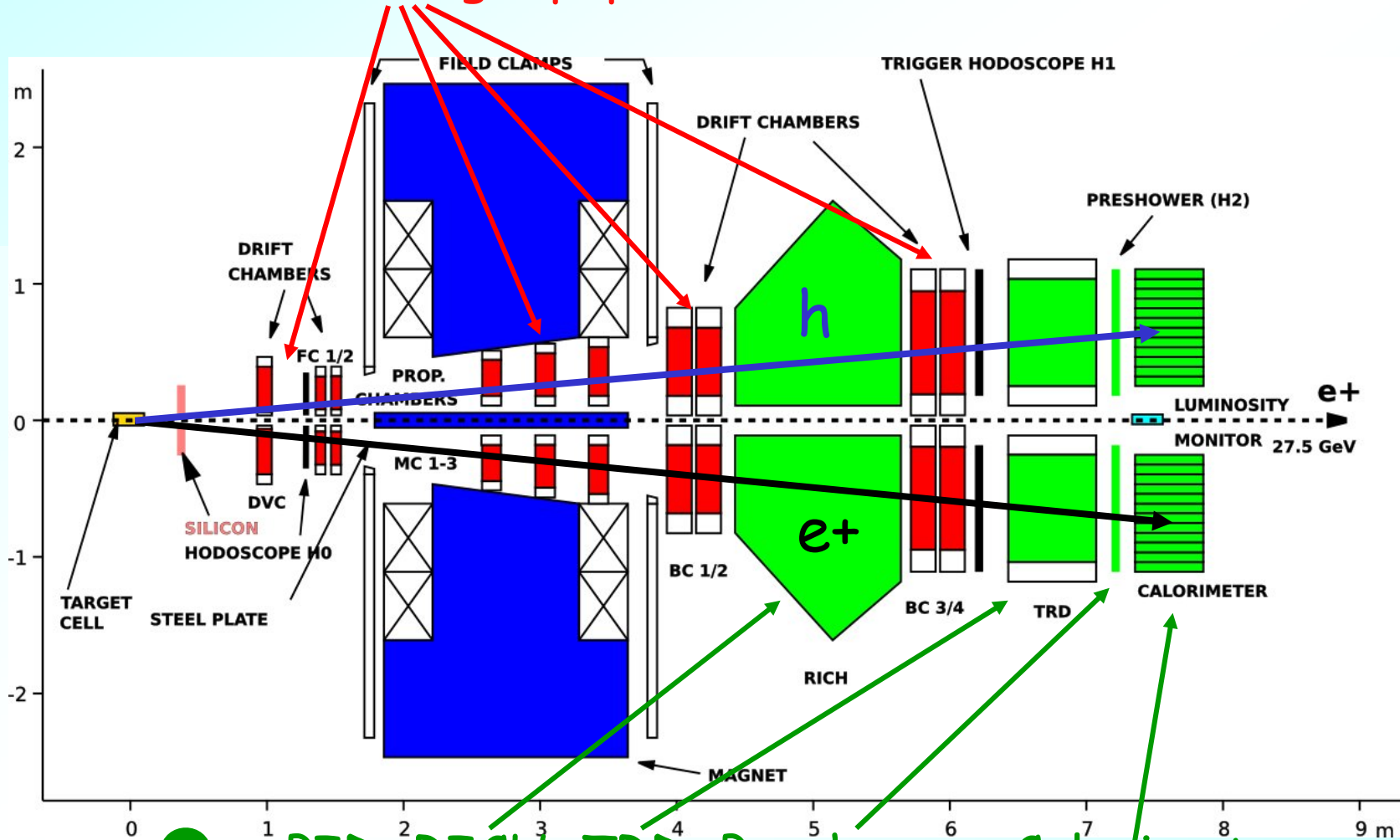


HERMES Spectrometer

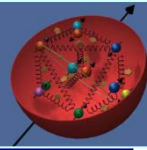




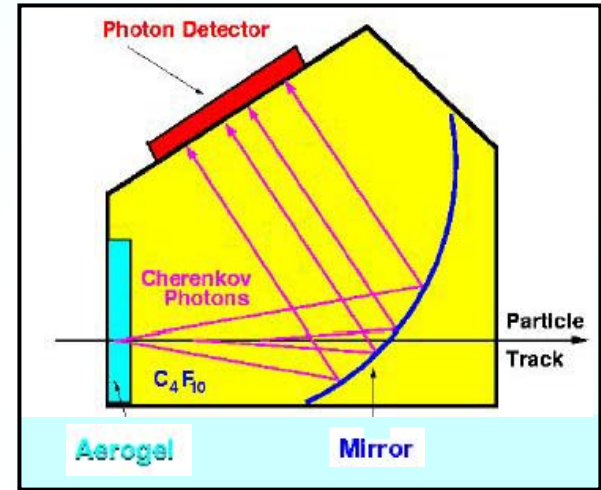
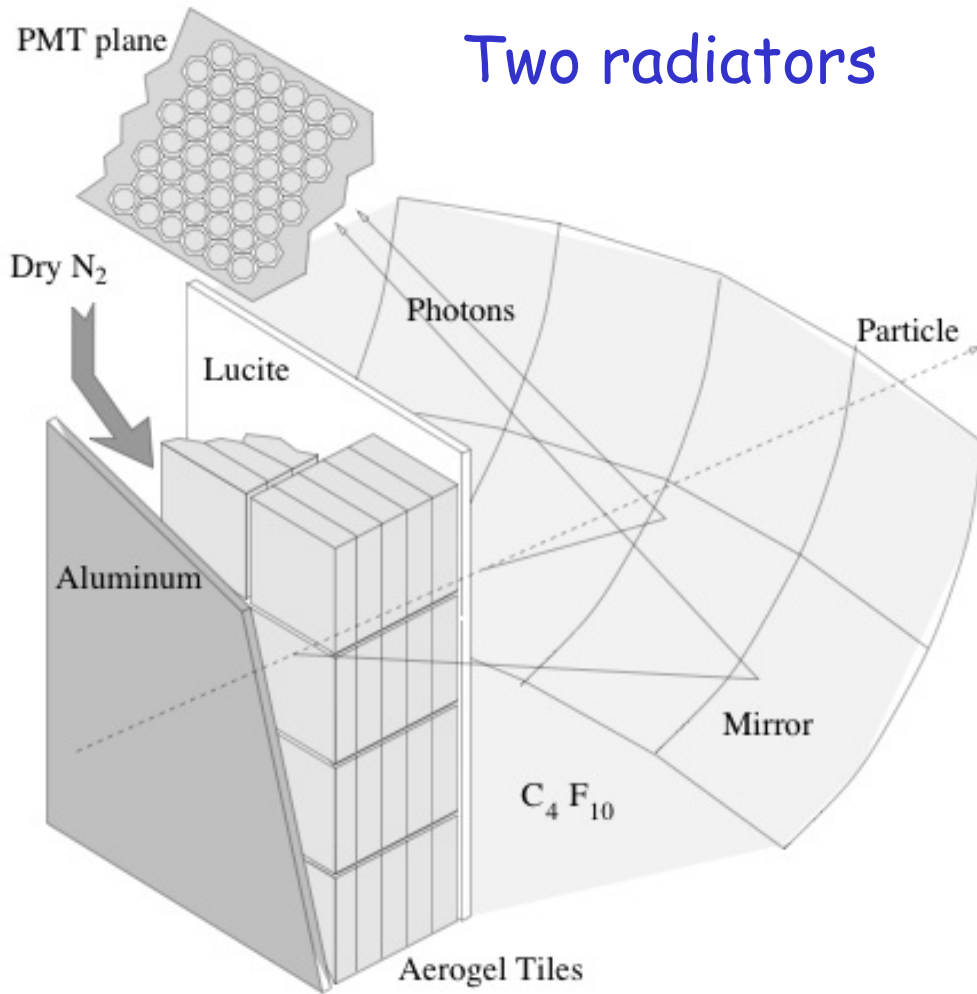
● tracking: $\delta p/p \sim 2\%$, $\delta \Theta < 0.6$ mrad, 40-220 mrad



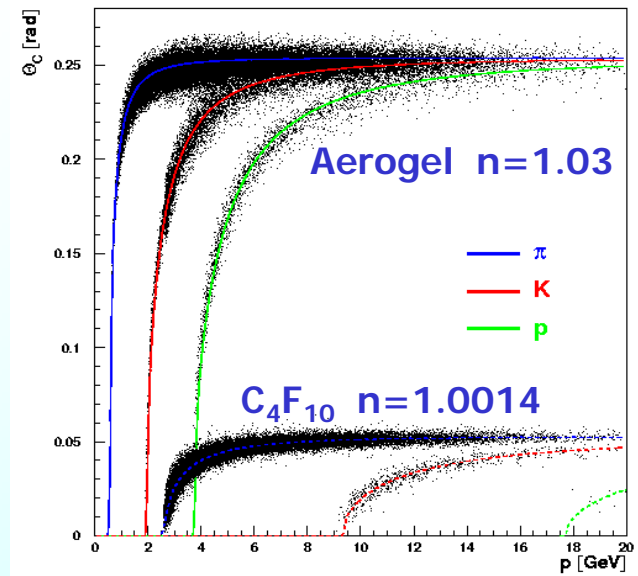
● PID: RICH, TRD, Preshower, Calorimeter
lepton-hadron separation > 98%



Two radiators



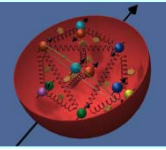
hadron separation



Hadron: $\pi \sim 98\%$, $K \sim 88\%$, $P \sim 85\%$



Data taking



1995-2000: Longitudinal target polarisation

(1995: $^3\vec{\text{He}}$, 1996-97 $\vec{\text{H}}$, 1998-2000 $\vec{\text{D}}$)

+ unpolarised targets (H_2 , D_2 , ^4He , N_2 , ^{20}Ne , ^{84}Kr , ^{131}Xe)

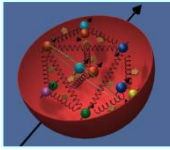
2002-2005: Transverse target polarisation (H^\uparrow)

+ unpolarised targets

2006-30/06/2007: Recoil detector (H_2 , D_2)

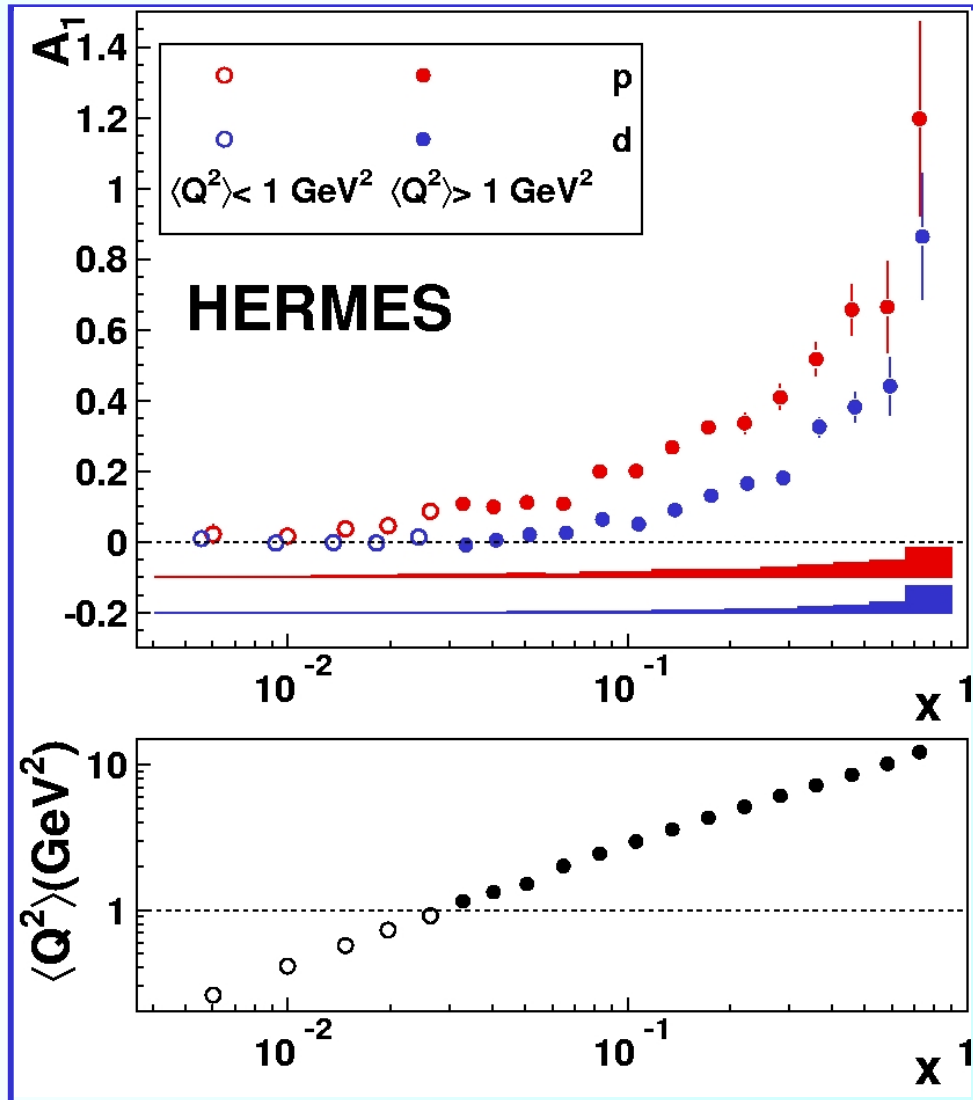
exclusive reactions

The Asymmetry $A_1 \cong g_1/F_1$

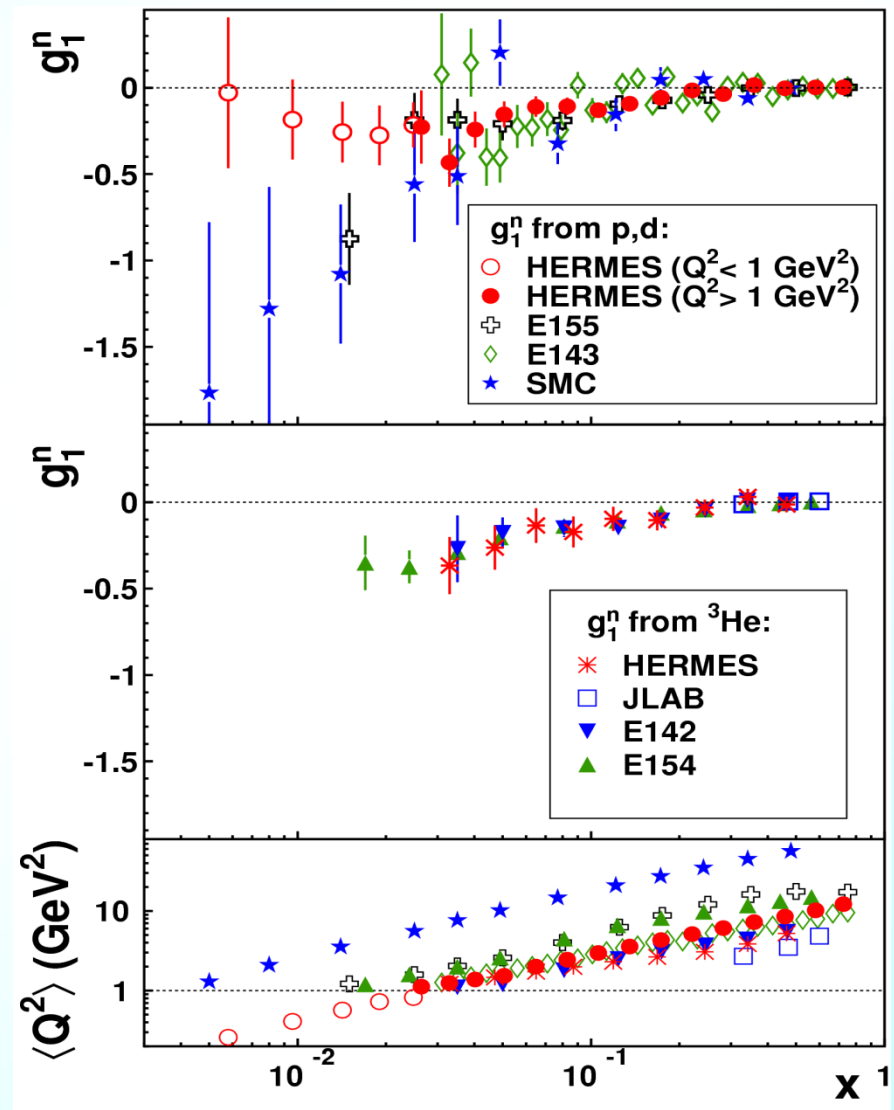
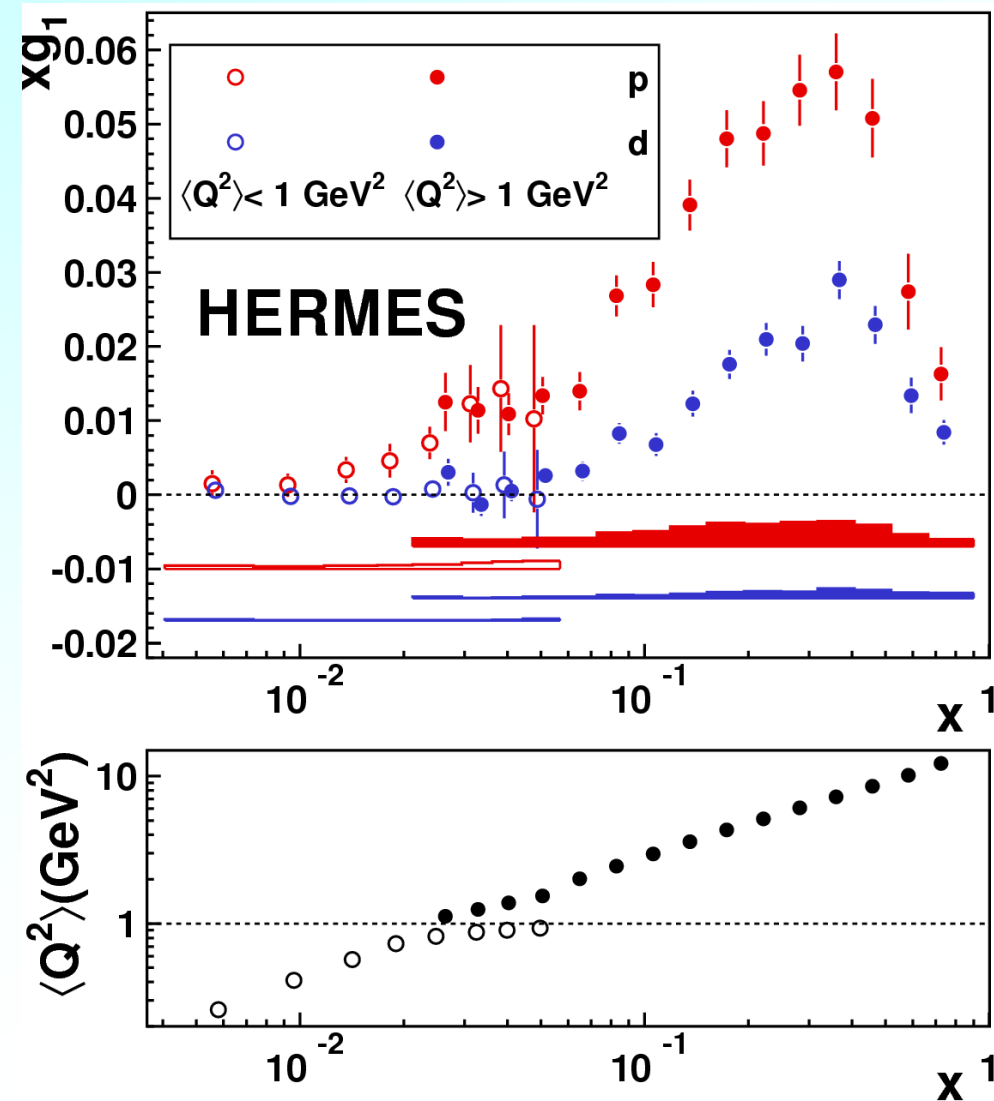


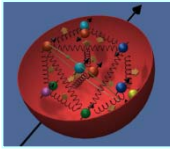
P. R. D 75 (2007) 012007

$$\begin{aligned}
 A_1(x) &\cong \frac{\sigma^{\uparrow\downarrow} - \sigma^{\uparrow\uparrow}}{\sigma^{\uparrow\downarrow} + \sigma^{\uparrow\uparrow}} \\
 &\cong \frac{\sum_q e_q^2 \Delta q(x)}{\sum_q e_q^2 q(x)} \\
 &= \frac{g_1(x)}{F_1(x)}
 \end{aligned}$$



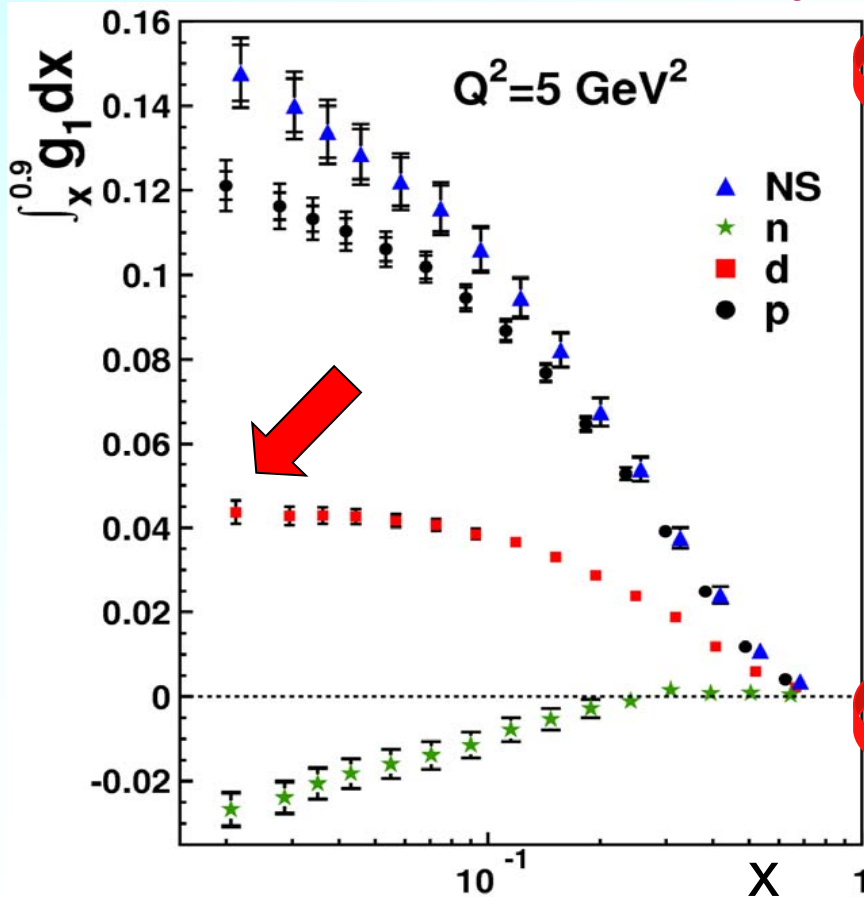
P. R. D 75 (2007) 012007





Most precise determination of $\Delta\Sigma$

[$Q^2 > 1 \text{ GeV}^2$ data only]



M. Contalbrigo

Assumption: Γ_1^d saturates for $x < 0.05$

$$\Gamma_1^d = 0,042 \pm 0,001^{(\text{stat})} \pm 0,003^{(\text{sys})}$$

$$\Delta\Sigma = \frac{1}{\Delta C_S} \left[\frac{9\Gamma_1^d}{\left(1 - \frac{3}{2}\omega_D\right)} - \frac{1}{4} a_s \Delta C_{NS} \right]$$

D-state probability in deuteron wave function

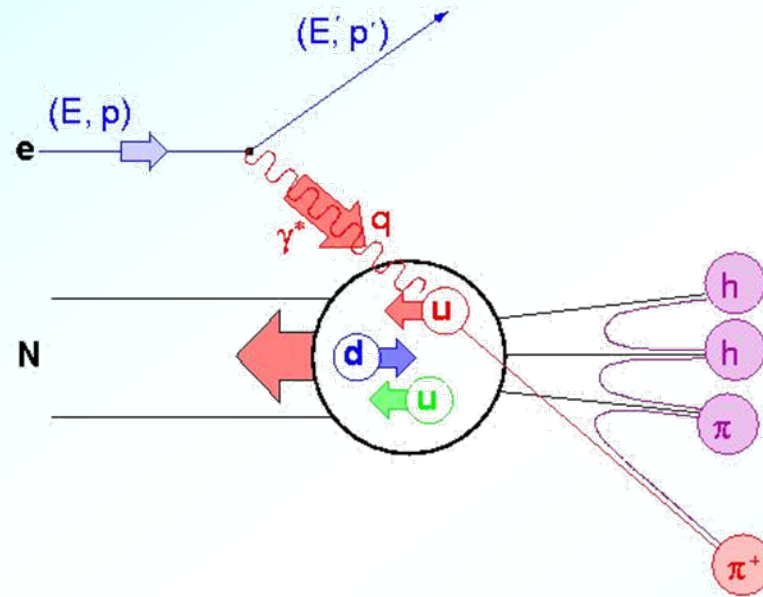
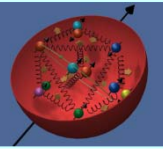
SU(3)

$$\overline{\Delta\Sigma} = 0,330 \pm 0,025 \pm 0,011 \pm 0,028$$

(exp) (theory) (evol.)

$$\text{EMC: } \Delta\Sigma = 0,12 \pm 0,09 \pm 0,14$$

Quark helicity distributions from SIDIS



Leading **hadron** originates with large probability from **struck quark**

$D_q^h(z)$:= Fragmentation function (FF)

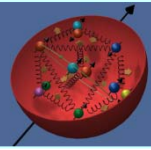
$$z = E_h / \nu$$

Measure hadron asymmetries

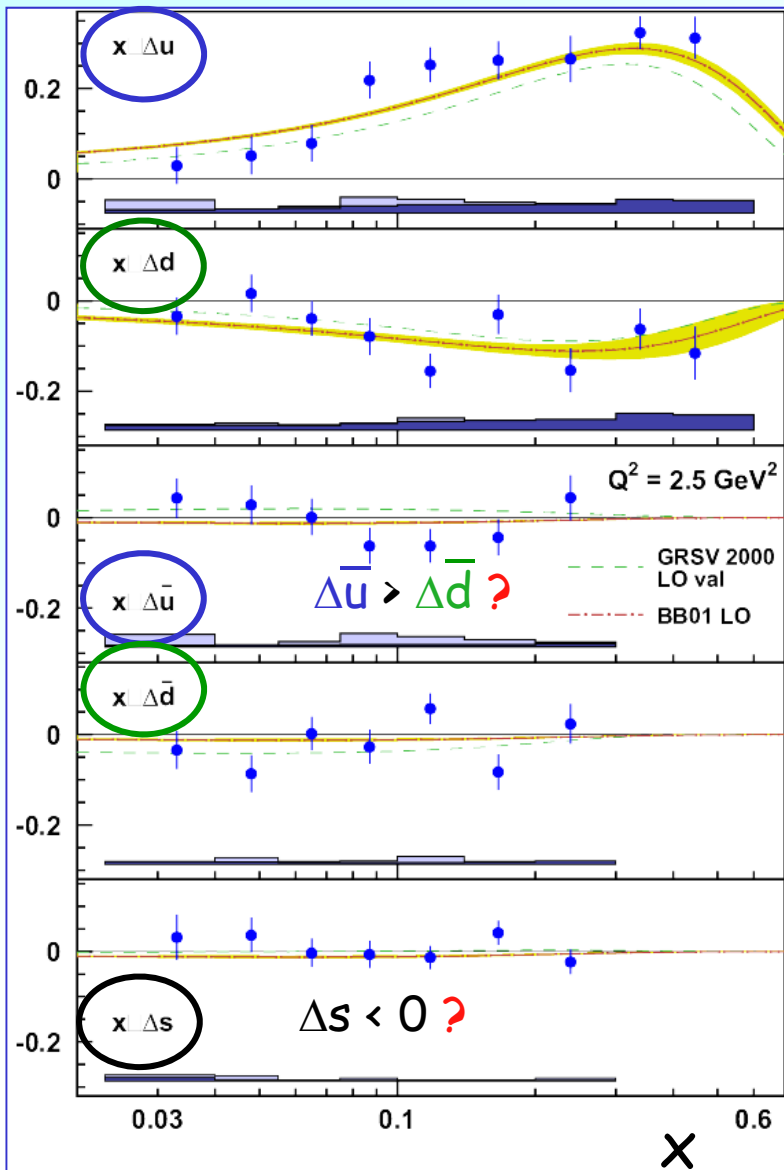
$$A_1^h(x, z) = \frac{\sum_q z_q^2 \Delta q(x) D_q^h(z)}{\sum_q z_q^2 q(x) D_q^h(z)}$$

Targets: \vec{H}, \vec{D} ; $h = \pi^\pm, K^\pm, p$

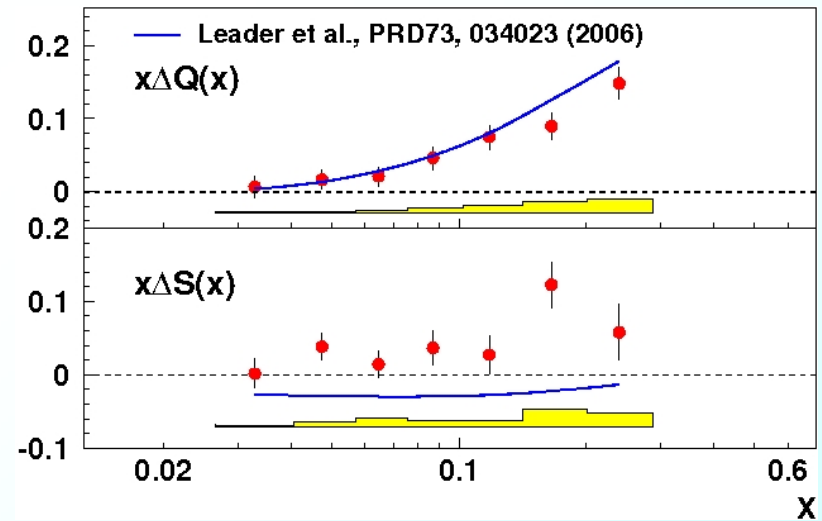
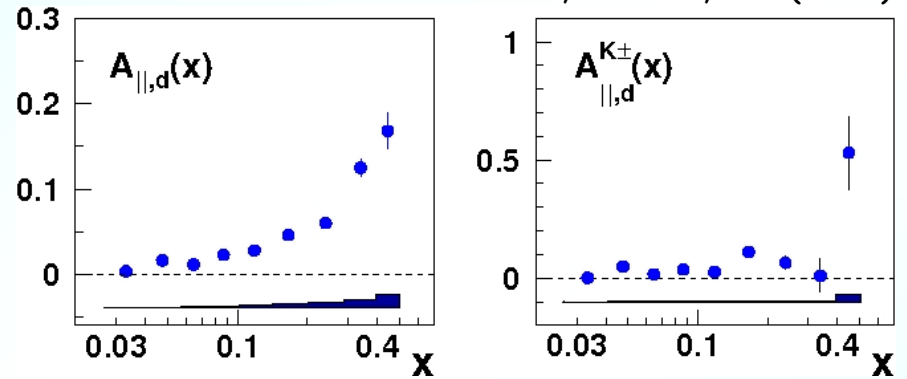
Quark helicity distributions



HERMES, PRL 92 (2004) 012005, PRD 71 (2005) 012003



HERMES, PLB 666, 446 (2008)

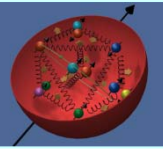


$$\Delta S = 0.037 \pm 0.019(\text{stat.}) \pm 0.027(\text{syst.})$$

(inclusive data and SU(3):

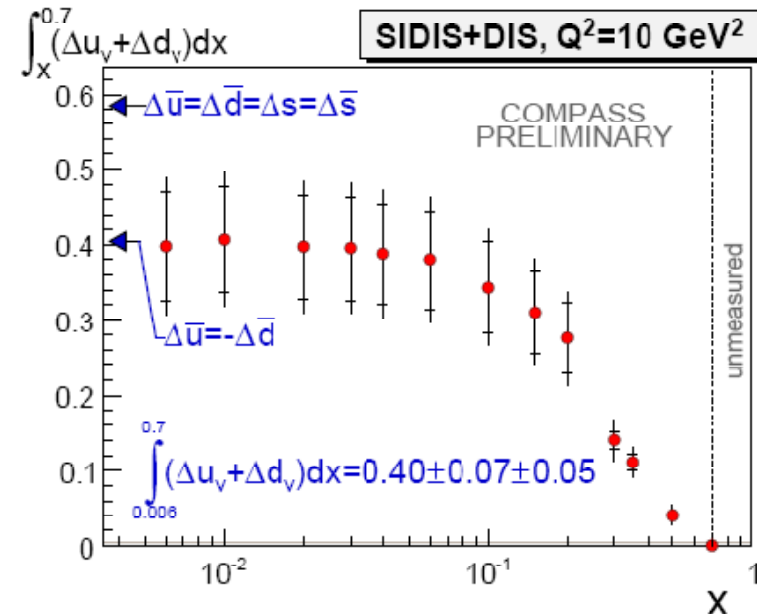
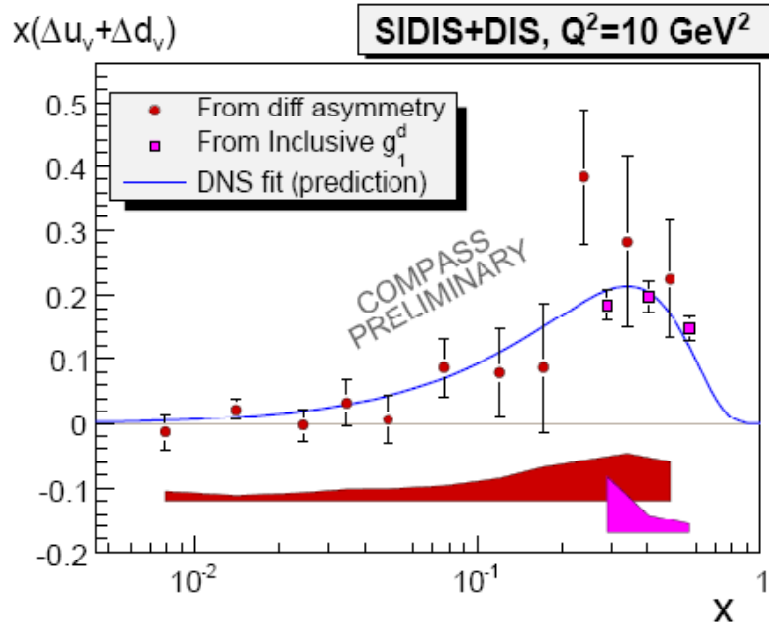
$$\Delta S = -0.085 \pm 0.013(\text{stat.}) \pm 0.012(\text{syst.})$$

Valence-quark helicity distributions



$$A_d^{\pi^+-\pi^-}(x) \stackrel{\text{L.O.}}{=} A_d^{K^+-K^-}(x) \stackrel{\text{L.O.}}{=} \frac{\Delta u_v(x) + \Delta d_v(x)}{u_v(x) + d_v(x)}$$

COMPASS, PLB 660 (2008) 458



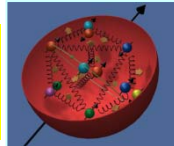
$$\Delta \bar{u} + \Delta \bar{d} = 3\Gamma_1^N - \frac{1}{2}\Gamma_1^v + a_8/12$$

Flavor asymmetric polarized sea ($\Delta \bar{u} = -\Delta \bar{d}$) favoured

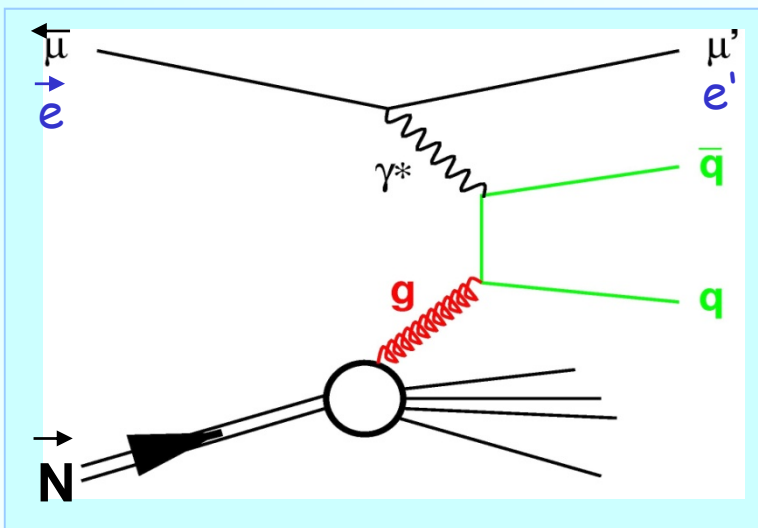
Gluon helicity distribution

$$\Delta g(x)$$

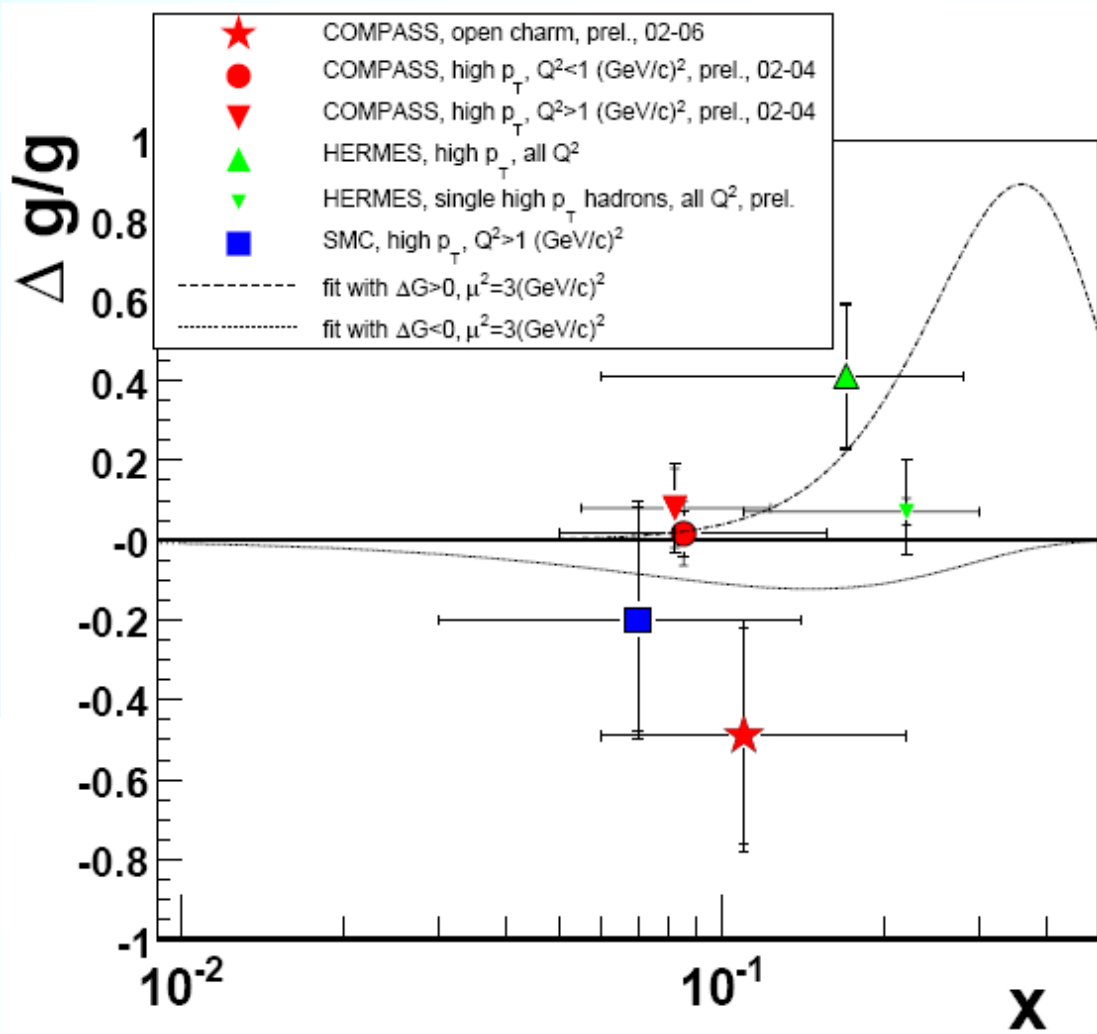
Gluon helicity distribution



Photon-gluon fusion

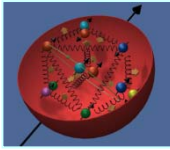


- Charm production
- Hadrons with high p_t

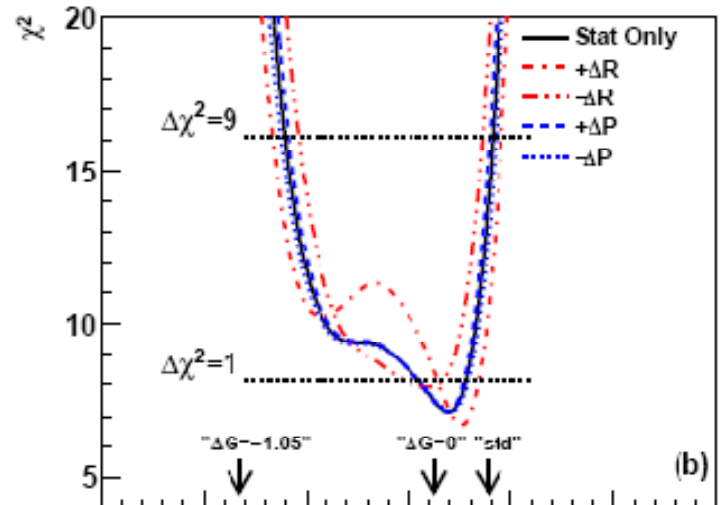
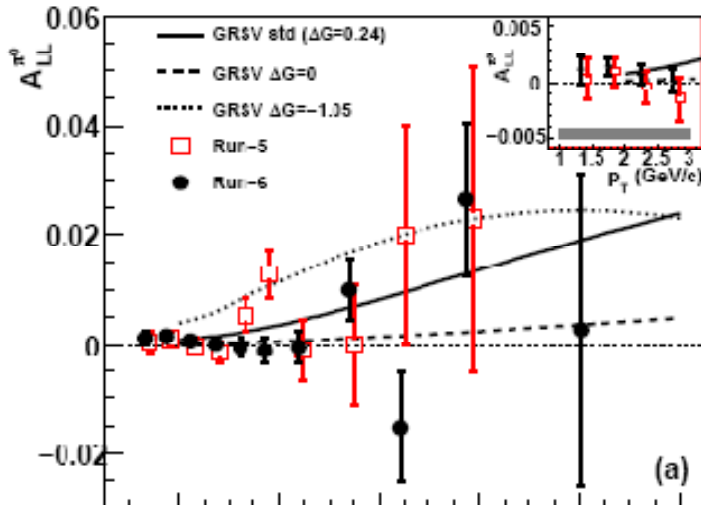


L.O. analyses

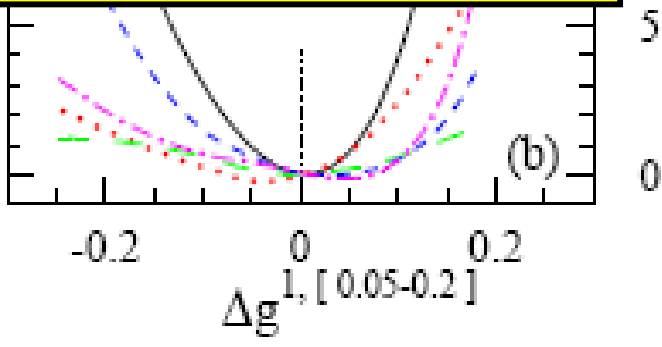
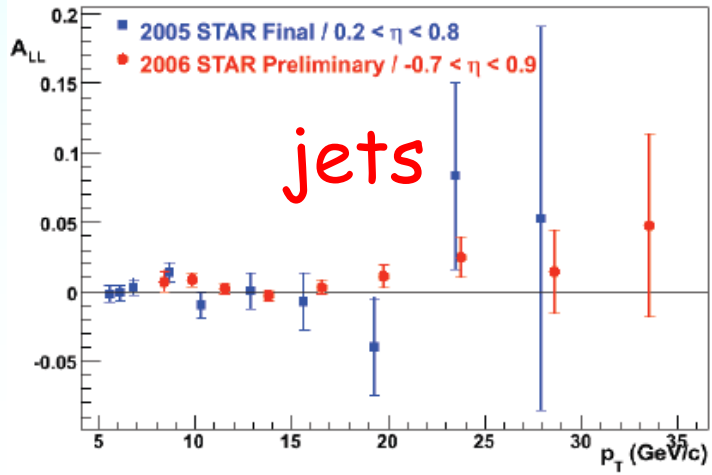
ΔG from $pp \rightarrow \pi^0$ (jet) X



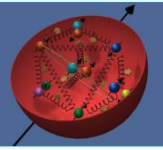
A. Adare et al. (PHENIX); arXiv:0810.0694



Δg seems to be rather small !!



NLO analysis (without data from previous slide)

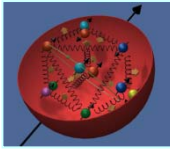


- Origin of nucleon spin still unclear:
Where do the missing 65% come from?
X. Ji: 'Dark Spin'
- Is there a substantial contribution of Δg and/or $\Delta \bar{q}$ at *very low x*?
→ EIC
- What is the contribution of *orbital angular momenta*
 $L_q, L_g ???$

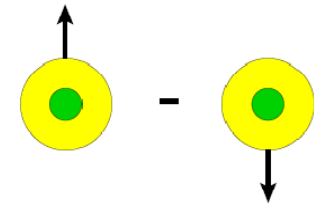
Quark orbital angular momentum

L_q

The Sivers distribution function f_{1T}

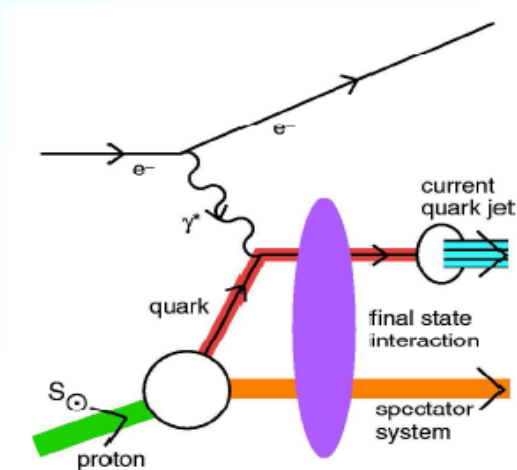


- Describes correlation between intrinsic quark p_T and **transverse nucleon spin**



- $f_{1T}^{\perp q}(p_T^2)$ describes probability to find an unpolarised quark with transverse momentum in a transversely polarised nucleon

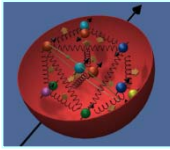
Chiral - even & **naive T - odd**



requires a quark rescattering via soft gluon exchange (gauge link) (Brodsky, Hwang, Schmidt)

- Non-zero **Sivers DF** requires **non-vanishing orbital angular momentum** in the nucleon wave function

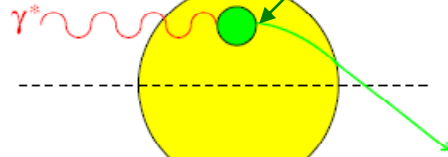
The Sivers effect



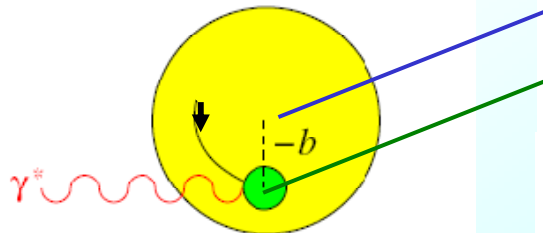
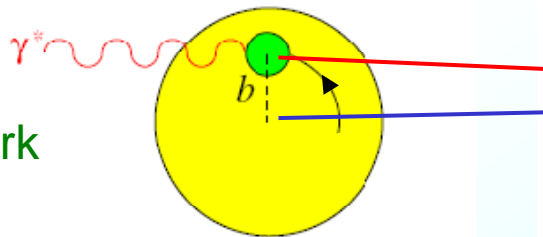
- Attractive **FSI** deflects quark inwards
- Left-right distribution asymmetry is converted into right-left momentum asymmetry
- Impact parameter formalism (M. Burkardt hep-ph/030926)
 - Orbital angular momentum of quarks
 - Virtual photon sees different x for different b
 - Quark distributions depend on b

lensing effect

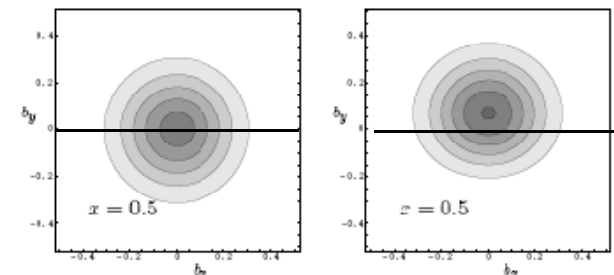
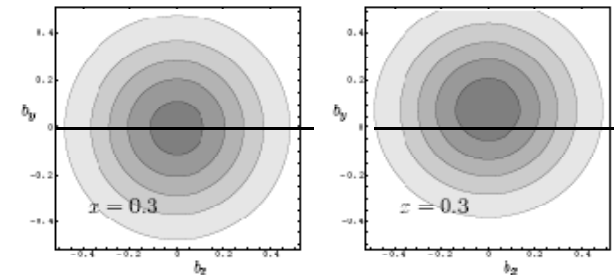
green quark



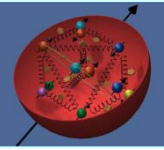
anti-green remnant



$u(x, b)$



Azimuthal angular distributions



Amplitude has 2 components:

Transversity DF

$$2\langle \sin(\phi + \phi_S) \rangle_{UT}^h \sim \delta q(x) \cdot H_1^{\perp q}(z)$$

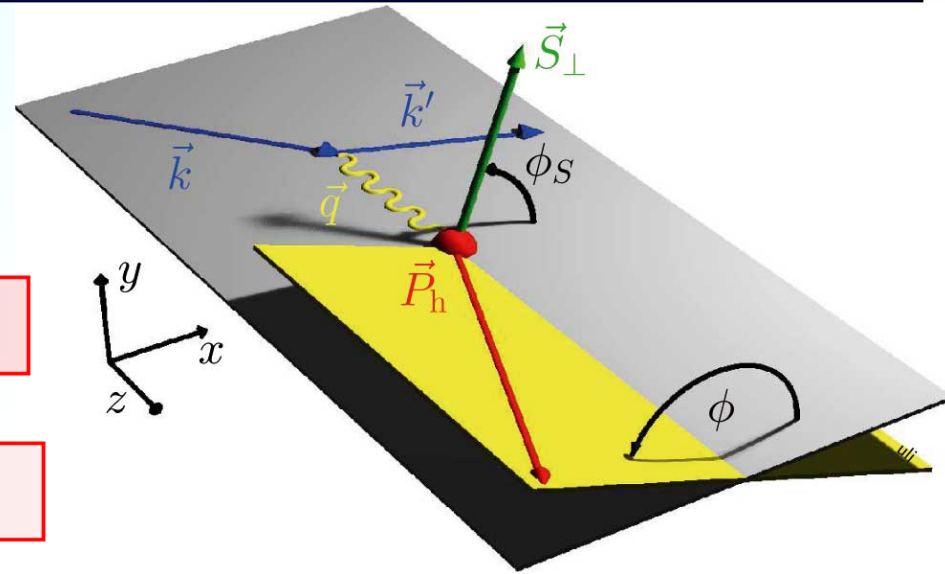
Collins Fragmentation Function

Unpolarised FF

$$2\langle \sin(\phi - \phi_S) \rangle_{UT}^h \sim f_{1T}^{\perp q}(x) \cdot D_1^q(z)$$

Sivers DF

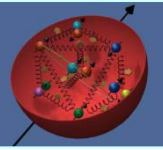
(Requires non-vanishing orbital angular momenta L_q of quarks)



U: unpol. e^\pm -beam

T: transv. pol. Target

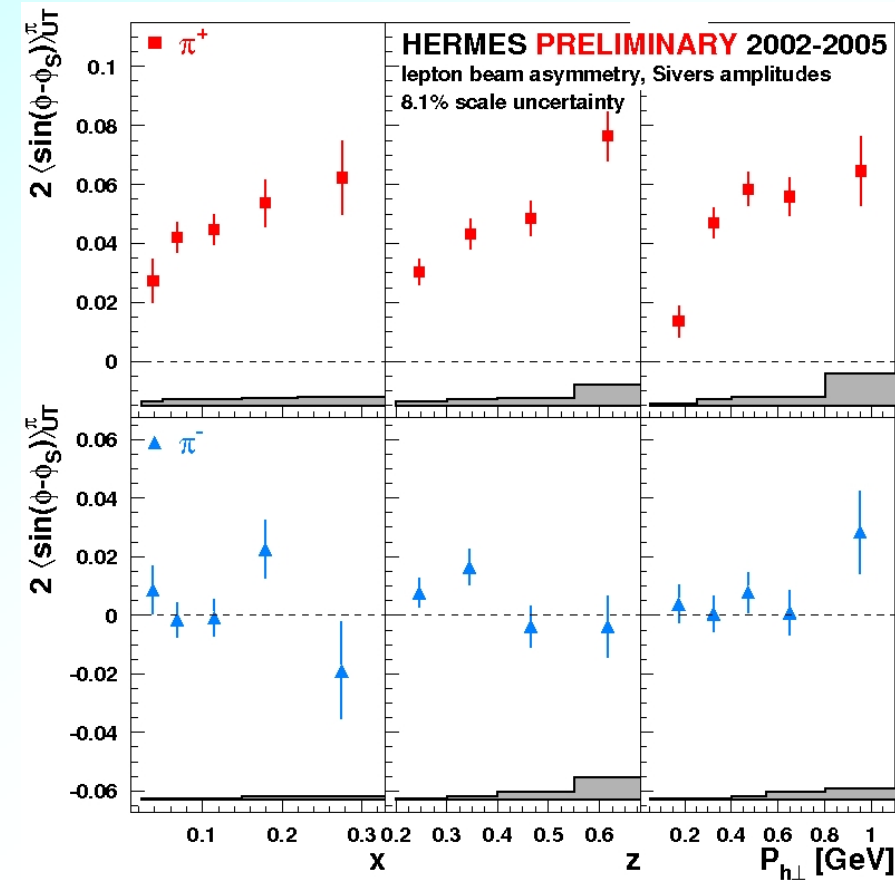
$$z = E_h/v$$



$$2\langle \sin(\phi - \phi_S) \rangle_{UT}^{\pi} \sim f_{1T}^{\perp q}(x) \otimes D_1^q(z)$$

M. Dieffenthaler @ DIS07, hep-ex 0706.2242

(also HERMES, P. R. L. 94 (2005) 012002)

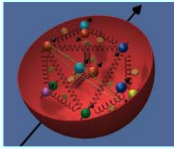


● First observation of non-zero Sivers distribution function in DIS

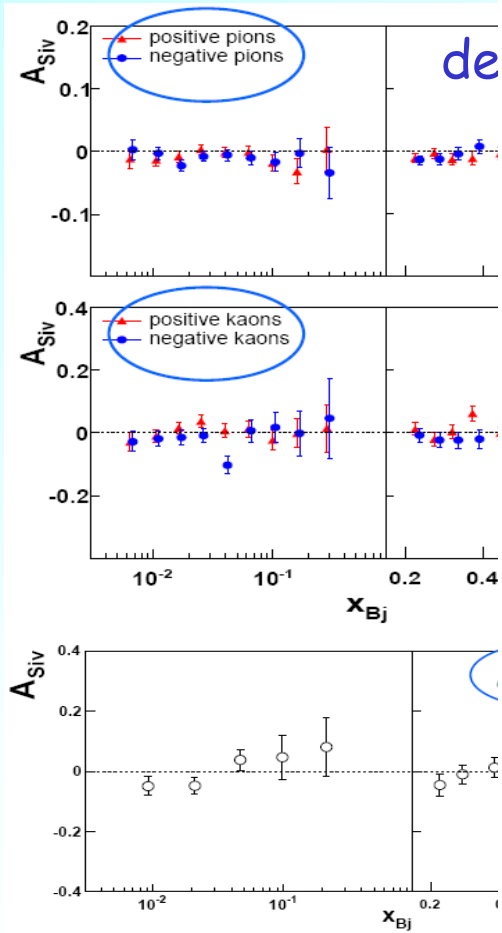
→ Experimental evidence for orbital angular momentum L_q of quarks

But: Quantitative contribution of L_q to nucleon spin still unclear

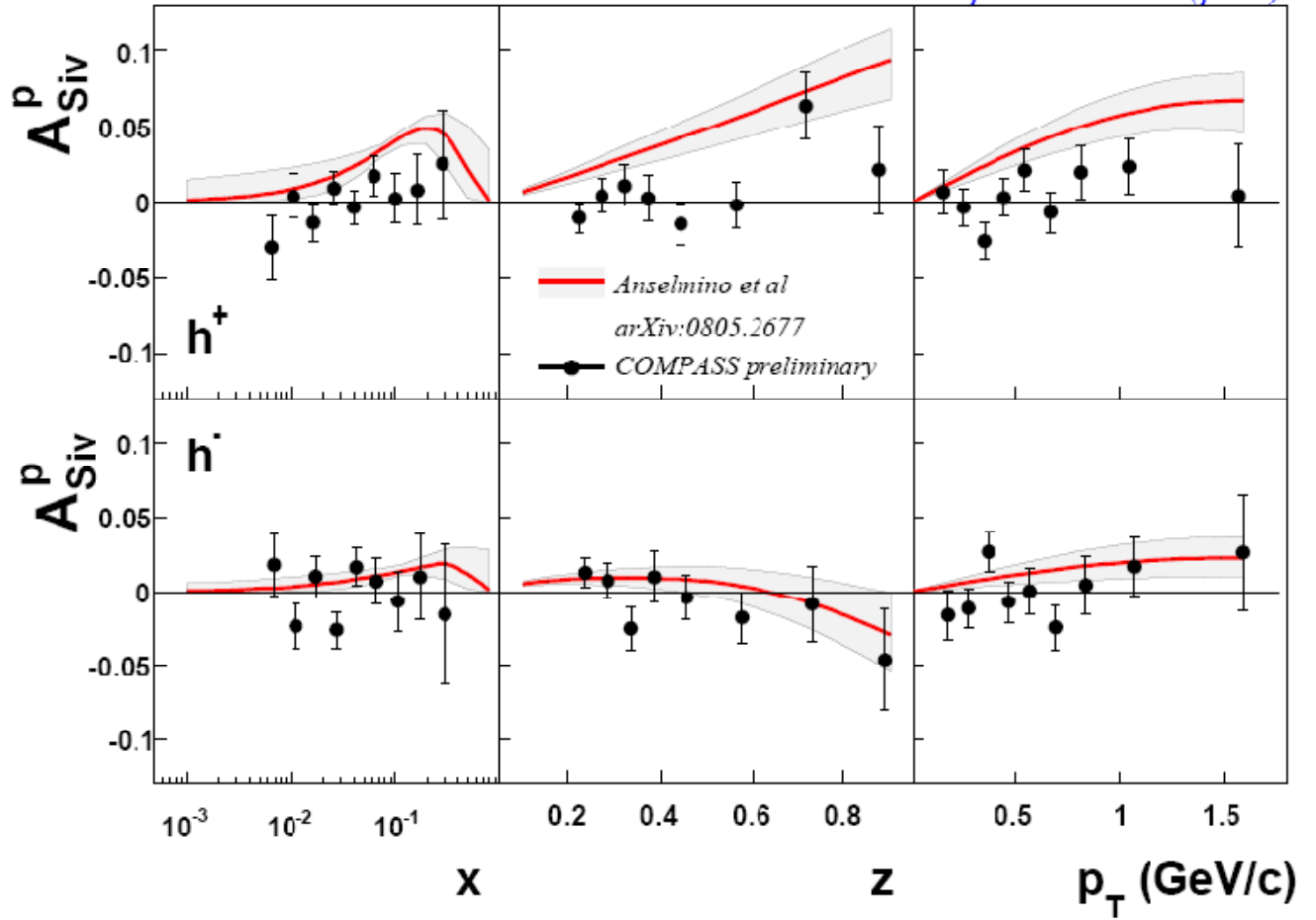
Sivers ampl. (d + p)



COMPASS, hep-ex/0802.2160



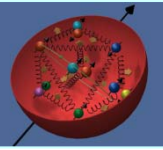
COMPASS 2007 transverse proton data (part)



Compatible with zero

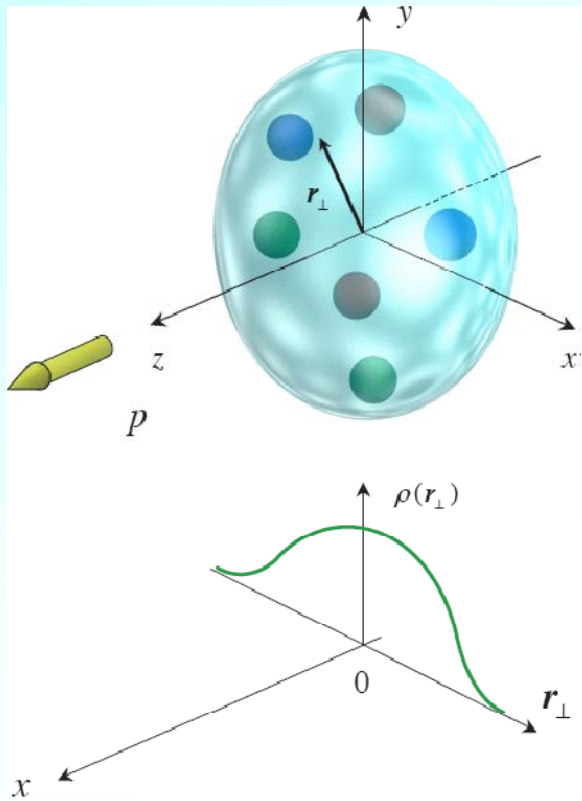
Still compatible with zero

Determination of L_q - GPDs



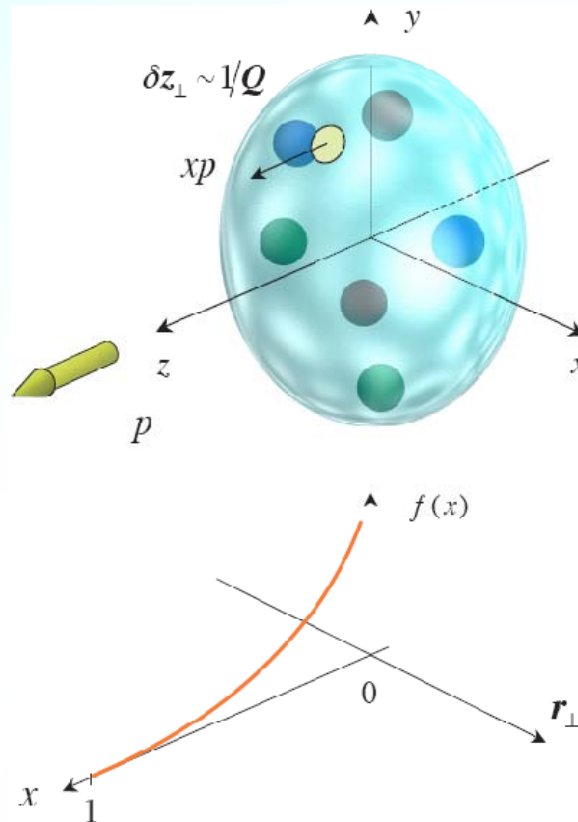
Tool: Generalised Parton Distributions

Formfactors:



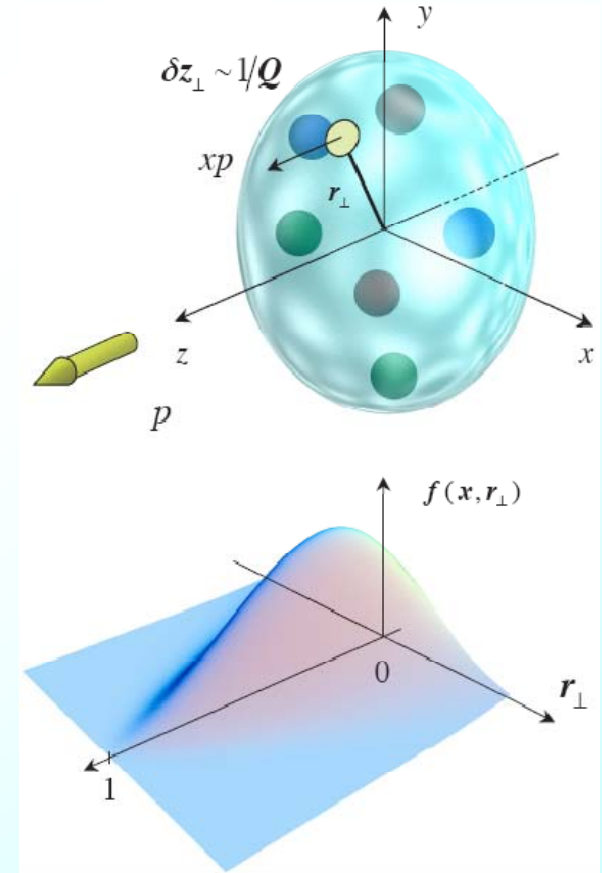
Fouriertransform of e.g. a radial charge distribution

PDFs:



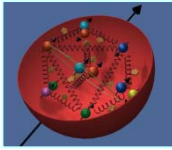
Number density of quarks with longitudinal momentum fraction x

GPDs:



Generalised description in 2+1 dimensions

Determination of L_q

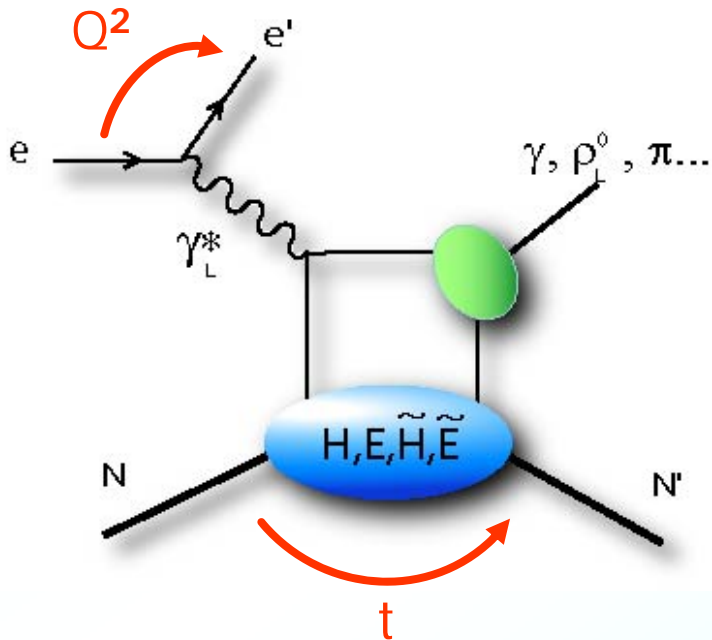


Ji relation:

$$J_q = 1/2 \Delta \Sigma + L_q = \lim_{t \rightarrow 0} \int_{-1}^1 dx x [H(x, \zeta, t) + E(x, \zeta, t)]$$

$H(x, \zeta, t), E(x, \zeta, t)$: Generalised Parton Distributions (GPDs)

Access: exclusive processes



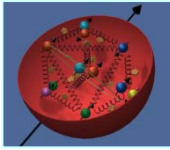
Final state sensitive to different GPDs

Vector mesons (ρ, ω, ϕ) H, E

Pseudoscalar mesons (π, η) \tilde{H}, \tilde{E}

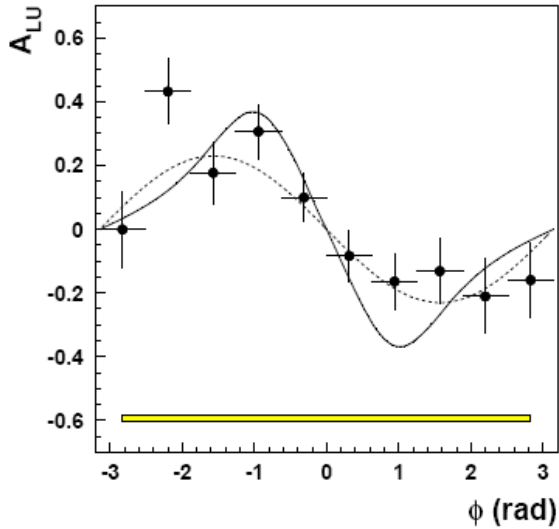
DVCS (γ) $H, E, \tilde{H}, \tilde{E}$

Azimuthal asymmetries

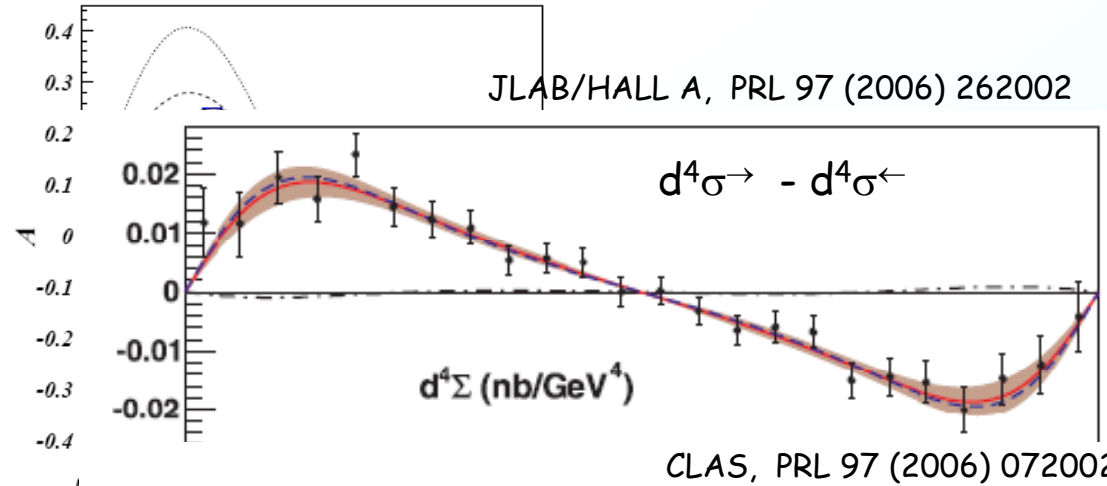


DVCS: Beam-spin asymmetry

HERMES, PRL 87 (2001) 182001

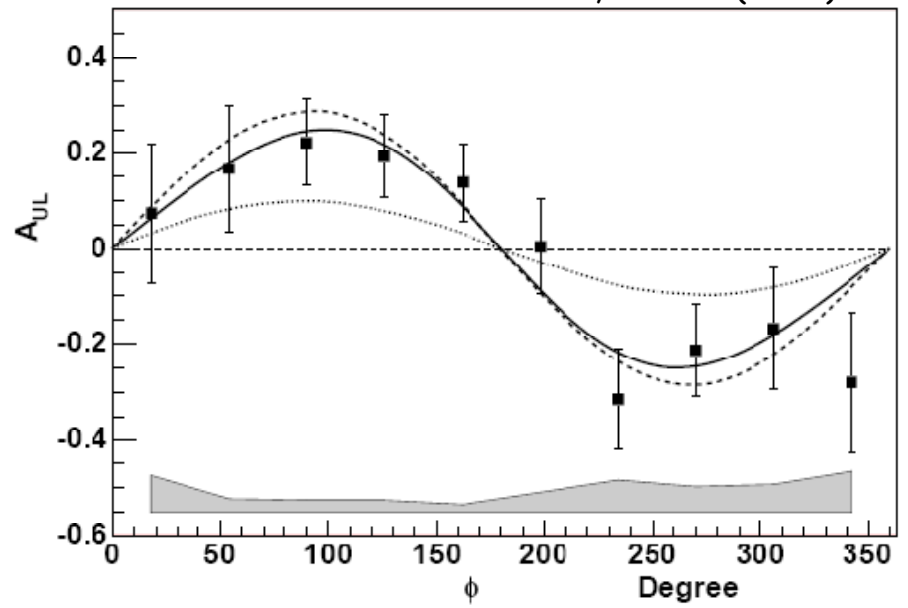


CLAS, PRL 87 (2001) 182002

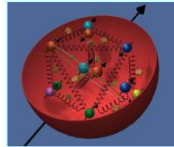


CLAS, PRL 97 (2006) 072002

DVCS: Longitudinal target-spin asymmetry



Hard exclusive processes - L_q



DVCS: Beam charge asymmetry

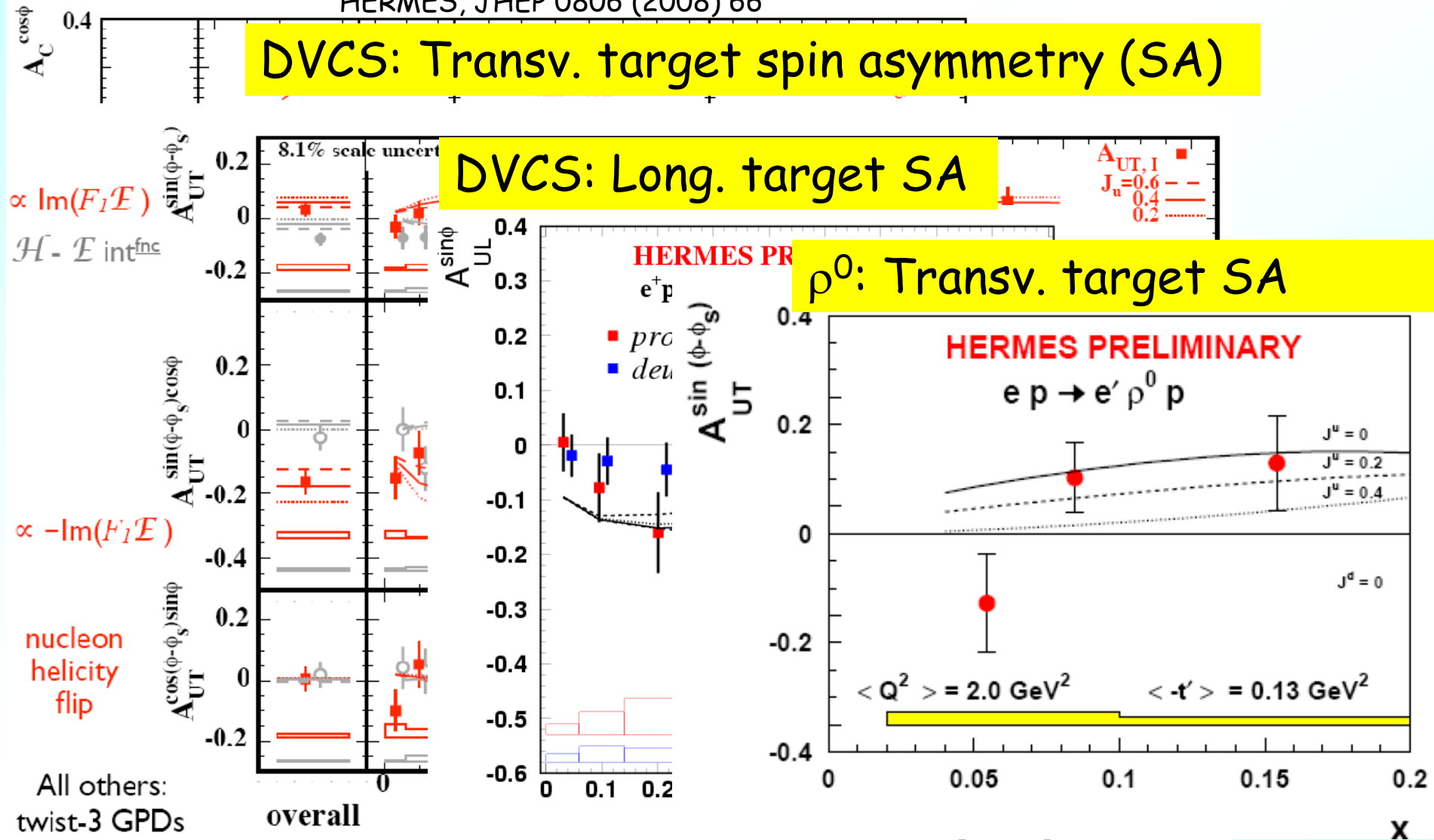
Pioneer measurements

HERMES, JHEP 0806 (2008) 66

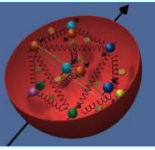
DVCS: Transv. target spin asymmetry (SA)

DVCS: Long. target SA

ρ^0 : Transv. target SA

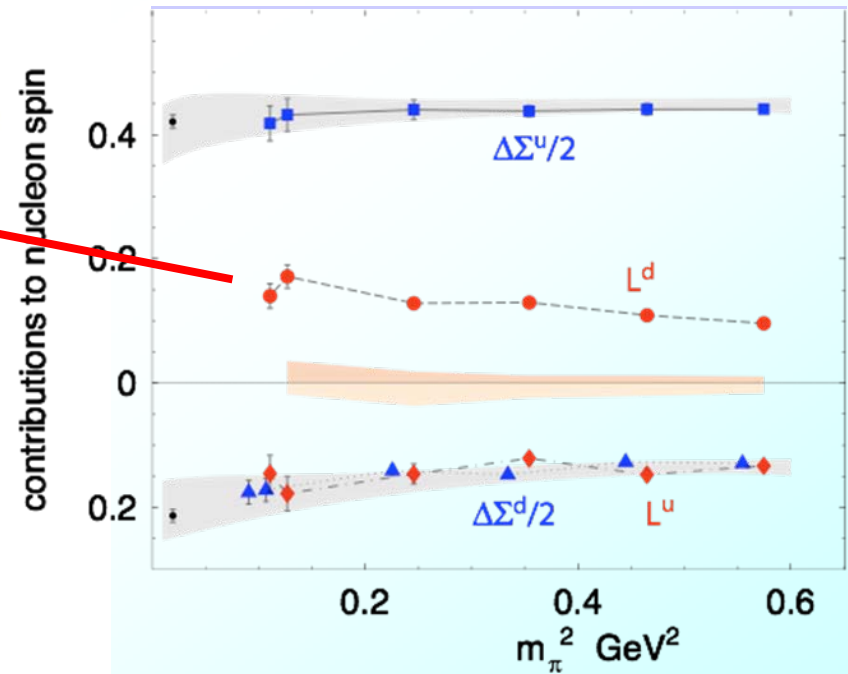
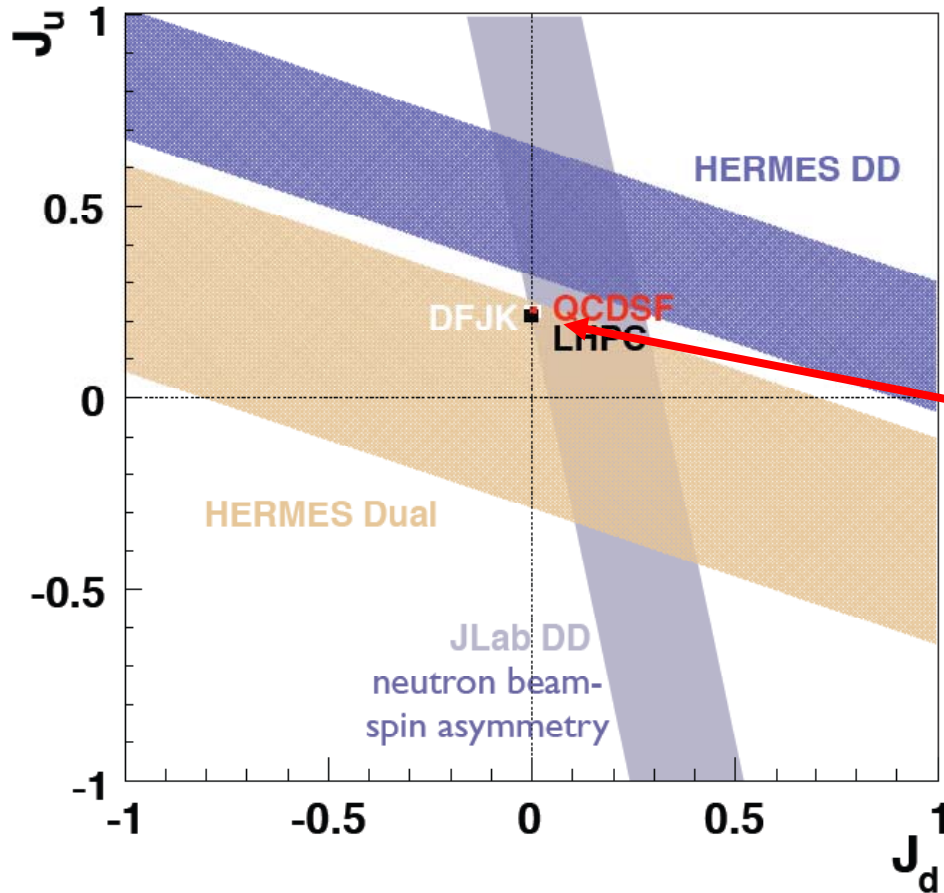


Determination of J_q

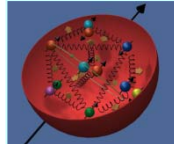


First model dependent attempt:

HERMES, JHEP 06 (2008) 066;
JLAB/HALL A, PRL 99 (2007) 242501

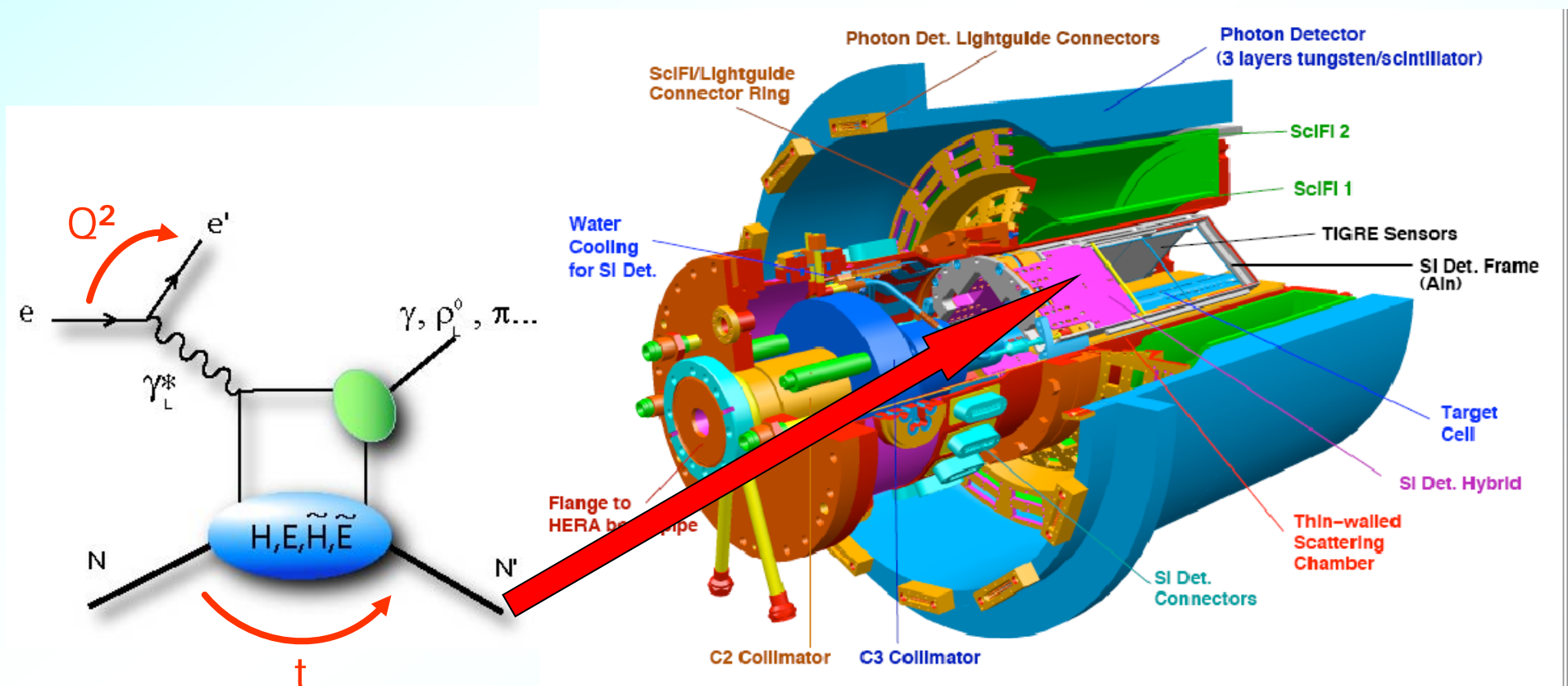


Lattice: $L_d \approx -L_u \approx 0.2$
 $L_d + \Delta d/2 \approx 0$!??

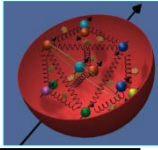


2006 - 2007:

Detailed study of *exclusive processes* with **Recoil-Detector**:



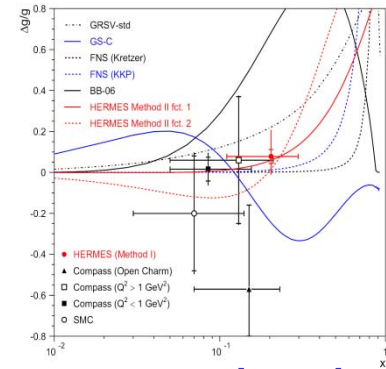
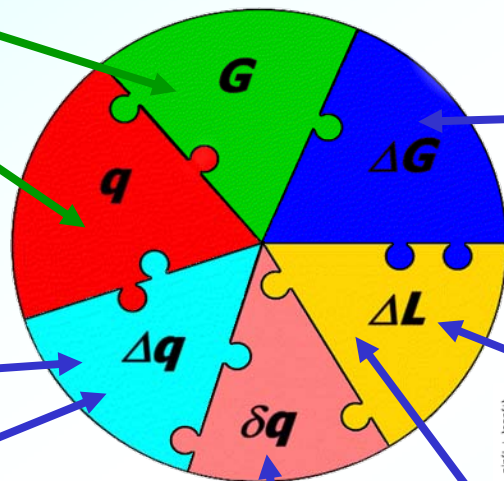
Nucleon Spin Structure & HERMES



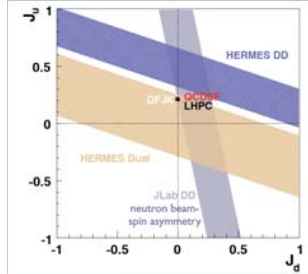
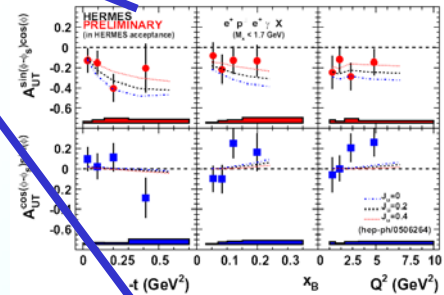
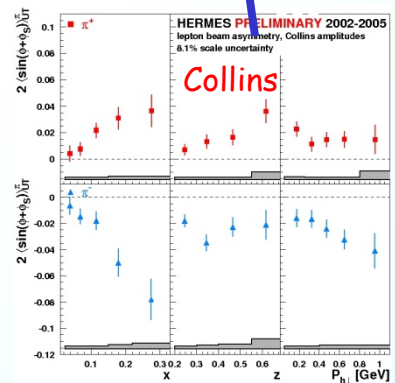
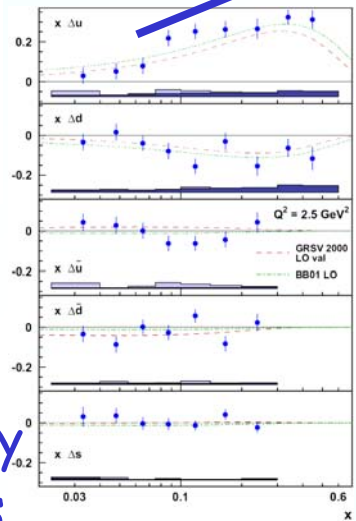
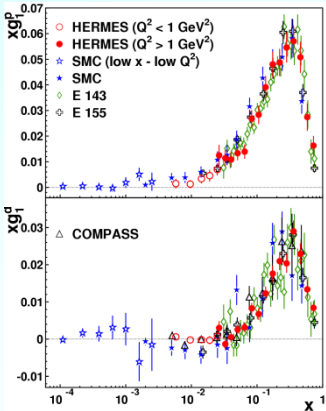
Unpolarised DIS
SLAC, BCDMS, NMC, HERA...

$$\rightarrow \Delta g/g = 0.071 \pm 0.035(\text{exp})$$

$$\rightarrow \Delta \Sigma = 0.330 \pm 0.025(\text{exp})$$



→ Signals for GPDs → $J_u + J_d$



→ individual quark helicity distributions

$$\rightarrow \delta q(x) \neq 0$$

$$\rightarrow L_q \neq 0$$

After Delia Hasch, Spin06, Kyoto