



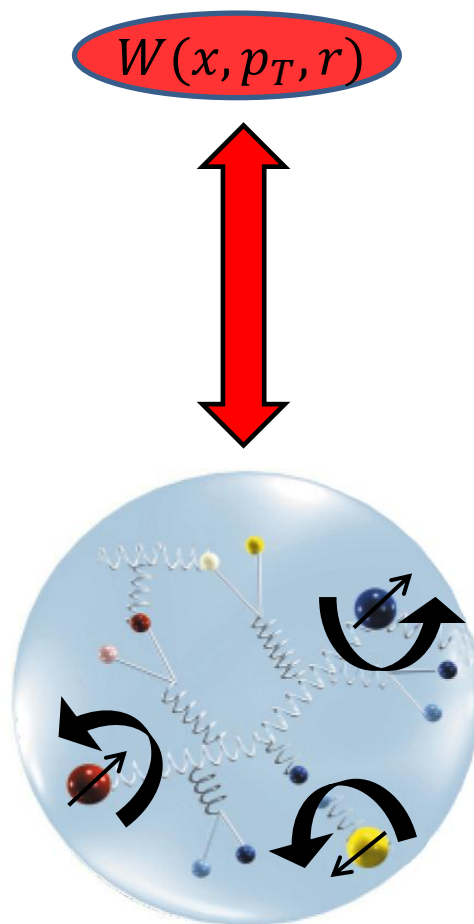
Recent Hermes results for SSAs and DSAs

Luciano L. Pappalardo

University of Ferrara

The phase-space distribution of partons

The full phase-space distribution of the partons encoded in the **Wigner function**

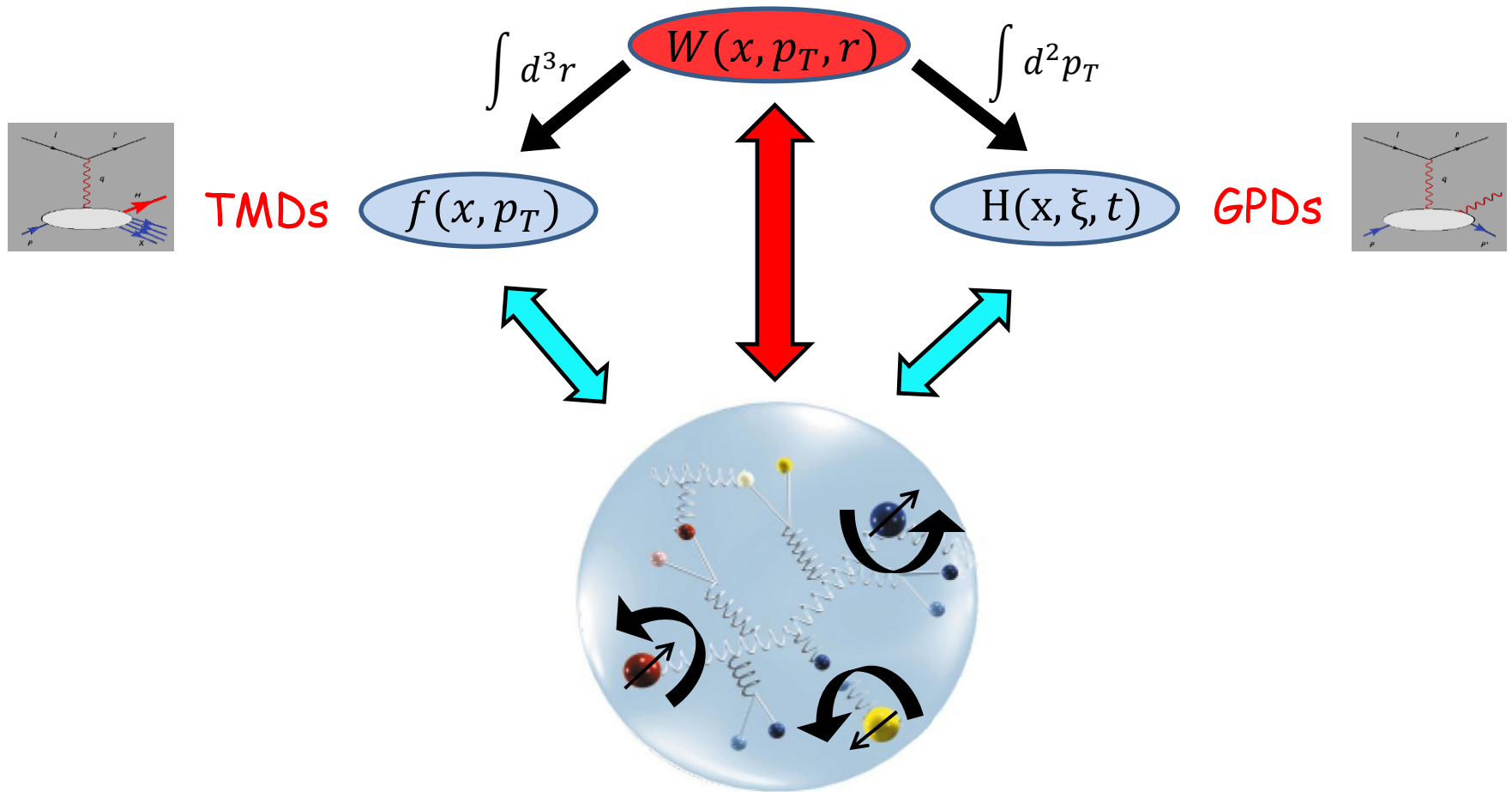


The phase-space distribution of partons

The full phase-space distribution of the partons encoded in the **Wigner function**

...but $\Delta x \Delta p \geq \frac{\hbar}{2} \rightarrow$ no simultaneous knowledge of momentum and position

cannot be directly accessed experimentally \rightarrow integrated quantities

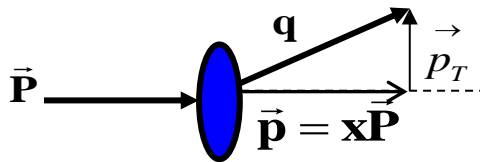
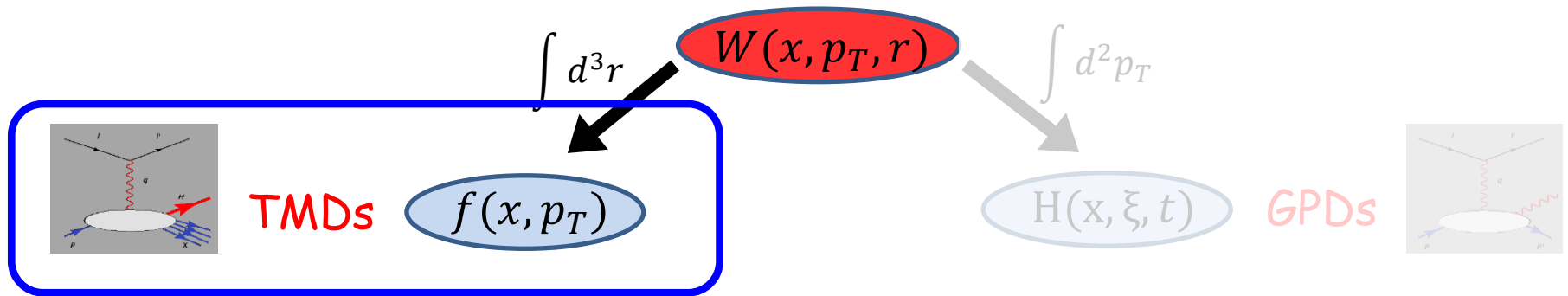


The non-collinear structure of the nucleon

The full phase-space distribution of the partons encoded in the **Wigner function**

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cannot be directly accessed experimentally \rightarrow integrated quantities



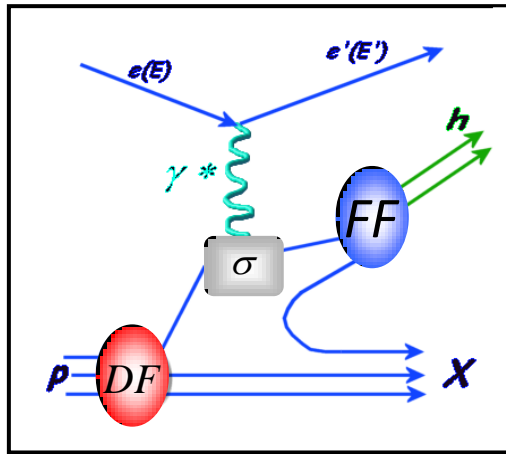
- TMDs depend on x and p_T
- Describe correlations between p_T and quark or nucleon spin (**spin-orbit correlations**)
- Provide a **3-dim picture** of the nucleon in momentum space (**nucleon tomography**)

		momentum	helicity	Boer-Mulders
nucleon	quark	U	L	T
	U	f_1		h_1^\perp
	L		g_1	h_{1L}^\perp
	T	f_{1T}^\perp	g_{1T}^\perp	h_{1T}^\perp

Additional labels: transversity (pointing to h_1^\perp), pretzelosity (pointing to h_{1T}^\perp), Sivers (pointing to f_{1T}^\perp), worm-gears (pointing to g_{1T}^\perp).

The non-collinear structure of the nucleon

Mostly investigated in **SIDIS**: detection of transverse momentum of produced hadrons gives access to p_T



$$\sigma^{ep \rightarrow ehX} = \sum_q \text{DF} \otimes \sigma^{eq \rightarrow eq} \otimes \text{FF}$$

- TMDs depend on x and p_T
- Describe correlations between p_T and quark or nucleon spin (**spin-orbit correlations**)
- Provide a **3-dim picture** of the nucleon in momentum space (**nucleon tomography**)

Fragmentation Functions (FF)				
		quark		
		U	L	T
h a d r o n	U	D_1		H_1^\perp
	L		G_{1L}	H_{1L}^\perp
	T	D_{1T}^\perp	G_{1T}^\perp	H_{1T}^\perp

Collins FF
chiral-odd

unpol. FF
chiral-even

				momentum	helicity	Boer-Mulders	
		quark					
		U	L	T			
n u c l e o n	U	f_1		h_1^\perp			
	L		g_1	h_{1L}^\perp			
	T	f_{1T}^\perp	g_{1T}^\perp	h_{1T}^\perp			

transversity

pretzelosity

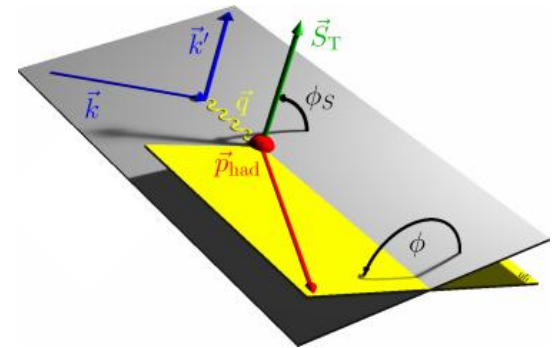
Sivers

worm-gears

The SIDIS cross-section

$$\frac{d\sigma^h}{dx dy d\phi_S dz d\phi d\mathbf{P}_{h\perp}^2} = \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x} \right)$$

$$\left\{ \begin{aligned} & \left[F_{UU,T} + \epsilon F_{UU,L} \right. \\ & \left. + \sqrt{2\epsilon(1+\epsilon)} \cos(\phi) F_{UU}^{\cos(\phi)} + \epsilon \cos(2\phi) F_{UU}^{\cos(2\phi)} \right] \\ & + \lambda_l \left[\sqrt{2\epsilon(1-\epsilon)} \sin(\phi) F_{LU}^{\sin(\phi)} \right] \\ & + S_L \left[\sqrt{2\epsilon(1+\epsilon)} \sin(\phi) F_{UL}^{\sin(\phi)} + \epsilon \sin(2\phi) F_{UL}^{\sin(2\phi)} \right] \\ & + S_L \lambda_l \left[\sqrt{1-\epsilon^2} F_{LL} + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi) F_{LL}^{\cos(\phi)} \right] \\ & + S_T \left[\sin(\phi - \phi_S) \left(F_{UT,T}^{\sin(\phi-\phi_S)} + \epsilon F_{UT,L}^{\sin(\phi-\phi_S)} \right) \right. \\ & \left. + \epsilon \sin(\phi + \phi_S) F_{UT}^{\sin(\phi+\phi_S)} + \epsilon \sin(3\phi - \phi_S) F_{UT}^{\sin(3\phi-\phi_S)} \right. \\ & \left. + \sqrt{2\epsilon(1+\epsilon)} \sin(\phi_S) F_{UT}^{\sin(\phi_S)} \right. \\ & \left. + \sqrt{2\epsilon(1+\epsilon)} \sin(2\phi - \phi_S) F_{UT}^{\sin(2\phi-\phi_S)} \right] \\ & + S_T \lambda_l \left[\sqrt{1-\epsilon^2} \cos(\phi - \phi_S) F_{LT}^{\cos(\phi-\phi_S)} \right. \\ & \left. + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi_S) F_{LT}^{\cos(\phi_S)} \right. \\ & \left. + \sqrt{2\epsilon(1-\epsilon)} \cos(2\phi - \phi_S) F_{LT}^{\cos(2\phi-\phi_S)} \right] \end{aligned} \right\}$$



$$F_{XY,Z} = F_{XY,Z}(x, y, z)$$

target polarization \uparrow
 beam polarization \downarrow virtual photon polarization \downarrow

The SIDIS cross-section

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$$+ \lambda_l \left[\sqrt{2\epsilon(1-\epsilon)} \sin(\phi) F_{LU}^{\sin(\phi)} \right]$$

$$+ S_L \left[\sqrt{2\epsilon(1+\epsilon)} \sin(\phi) F_{UL}^{\sin(\phi)} + \epsilon \sin(2\phi) F_{UL}^{\sin(2\phi)} \right]$$

$$+ S_L \lambda_l \left[\sqrt{1-\epsilon^2} F_{LL} + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi) F_{LL}^{\cos(\phi)} \right]$$

$$+ S_T \left[\begin{aligned} & \sin(\phi - \phi_S) \left(F_{UT,T}^{\sin(\phi-\phi_S)} + \epsilon F_{UT,L}^{\sin(\phi-\phi_S)} \right) \\ & + \epsilon \sin(\phi + \phi_S) F_{UT}^{\sin(\phi+\phi_S)} + \epsilon \sin(3\phi - \phi_S) F_{UT}^{\sin(3\phi-\phi_S)} \\ & + \sqrt{2\epsilon(1+\epsilon)} \sin(\phi_S) F_{UT}^{\sin(\phi_S)} \\ & + \sqrt{2\epsilon(1+\epsilon)} \sin(2\phi - \phi_S) F_{UT}^{\sin(2\phi-\phi_S)} \end{aligned} \right]$$

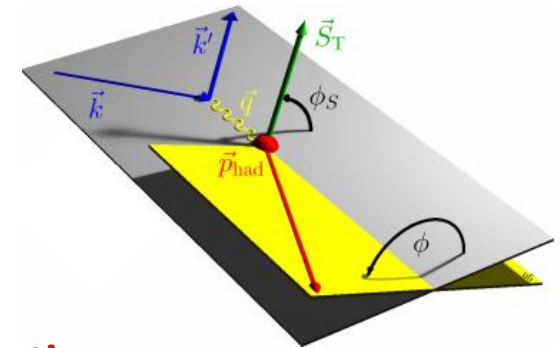
$$+ S_T \lambda_l \left[\begin{aligned} & \sqrt{1-\epsilon^2} \cos(\phi - \phi_S) F_{LT}^{\cos(\phi-\phi_S)} \\ & + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi_S) F_{LT}^{\cos(\phi_S)} \\ & + \sqrt{2\epsilon(1-\epsilon)} \cos(2\phi - \phi_S) F_{LT}^{\cos(2\phi-\phi_S)} \end{aligned} \right] \left. \right\}$$

unpolarized

beam polarization

target polarization

beam and target polarization



$$F_{XY,Z}^{\text{target polarization}} = F_{XY,Z}(x, y, z)$$

beam polarization \downarrow virtual photon polarization \downarrow

Selected leading-twist 1-hadron SIDIS results

Boer-Mulders function

$$\frac{d\sigma^h}{dx dy d\phi_S dz d\phi d\mathbf{P}_{h\perp}^2} = \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x} \right)$$

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$$+ S_T \lambda_l \left[\sqrt{1-\epsilon^2} \cos(\phi - \phi_S) F_{LT}^{\cos(\phi-\phi_S)} \right. \\ \left. + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi_S) F_{LT}^{\cos(\phi_S)} \right. \\ \left. + \sqrt{2\epsilon(1-\epsilon)} \cos(2\phi - \phi_S) F_{LT}^{\cos(2\phi-\phi_S)} \right] \left. \right\}$$

$$F_{UU}^{\cos 2\phi_h} = C \left[-\frac{2(\hat{h} \cdot \mathbf{k}_T)(\hat{h} \cdot \mathbf{p}_T) - \mathbf{k}_T \cdot \mathbf{p}_T}{MM_h} h_1^\perp H_1^\perp \right]$$

Describes correlation between quark transverse momentum and transverse spin in unpolarized nucleon

Distribution Functions

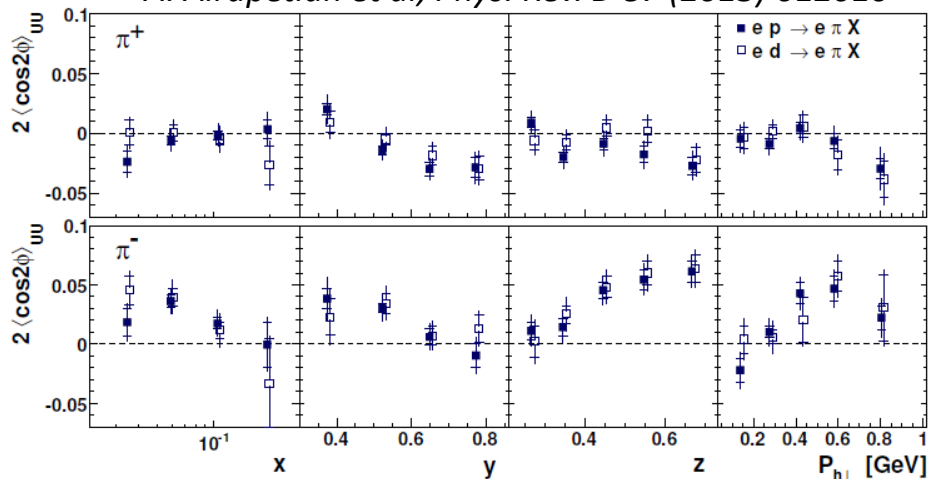
		quark		
		U	L	T
nucleon	U	f_1		h_1^\perp
	L		g_1	h_{1L}^\perp
	T	f_{1T}^\perp	g_{1T}^\perp	h_{1T}^\perp

Fragmentation Functions

		quark		
		U	L	T
h	U	D_1		H_1^\perp

The $\cos 2\phi$ amplitudes $\propto h_1^\perp(x, p_T^2) \otimes H_1^\perp(z, k_T^2)$

A. Airapetian et al, Phys. Rev. D 87 (2013) 012010



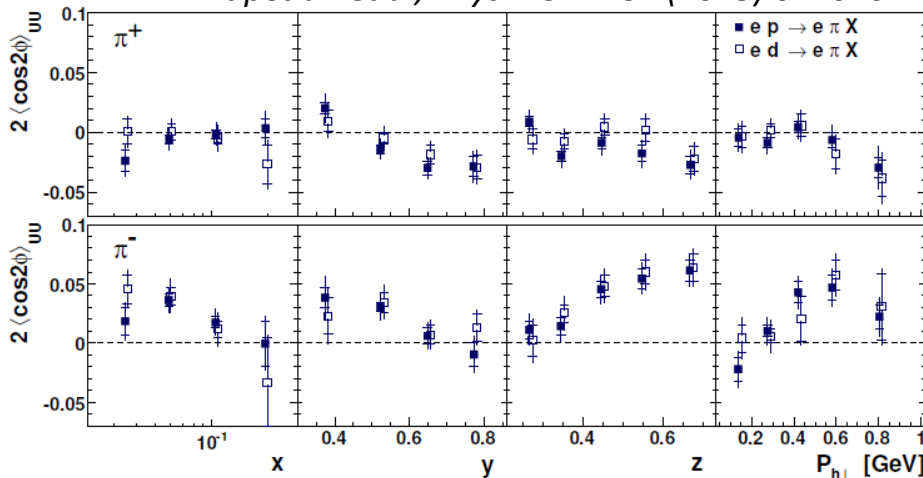
negative

positive

- Amplitudes are significant
→ clear evidence of BM effect
- similar results for H & D indicate $h_1^{\perp,u} \approx h_1^{\perp,d}$
- Opposite sign for π^+/π^- consistent with opposite signs of fav/unfav Collins

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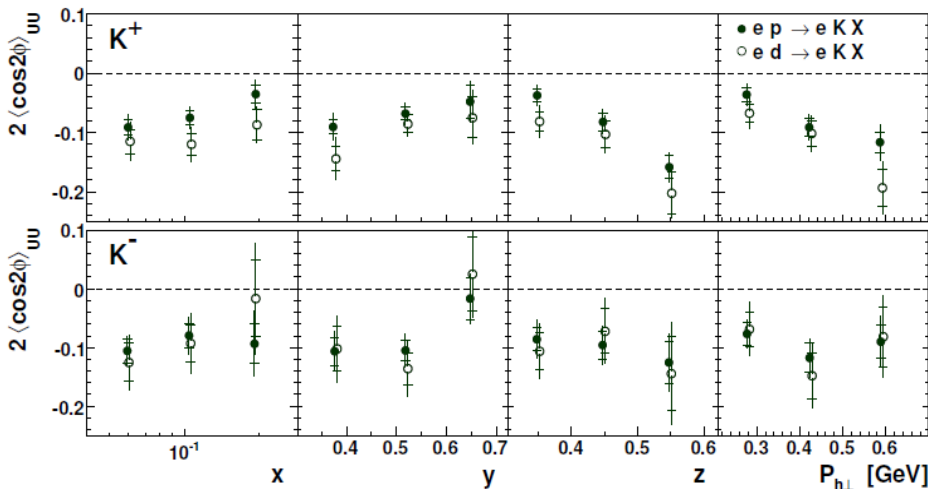
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indicate $h_1^{\perp,u} \approx h_1^{\perp,d}$

- Opposite sign for π^+/π^-
consistent with opposite signs
of fav/unfav Collins



Large
and
negative

Large
and
negative

- K^+/K^- amplitudes are larger
than for pions, have different
kinematic dependencies than
pions and have same sign

- different role of Collins FF for
pions and kaons?

- Significant contribution from
scattering off strange quarks?

Analysis multi-dimensional in $x, y, z,$ and P_t

Create your own projections of results through: <http://www-hermes.desy.de/cosnphi/>

Transversity

$$\frac{d\sigma^h}{dx dy d\phi_S dz d\phi d\mathbf{P}_{h\perp}^2} = \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x} \right)$$

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$$F_{UT}^{\sin(\phi_h + \phi_S)} = C \left[-\frac{\hat{h} \cdot \mathbf{k}_T}{M_h} h_1 H_1^\perp \right]$$

Describes probability to find transversely polarized quarks in a transversely polarized nucleon

Distribution Functions

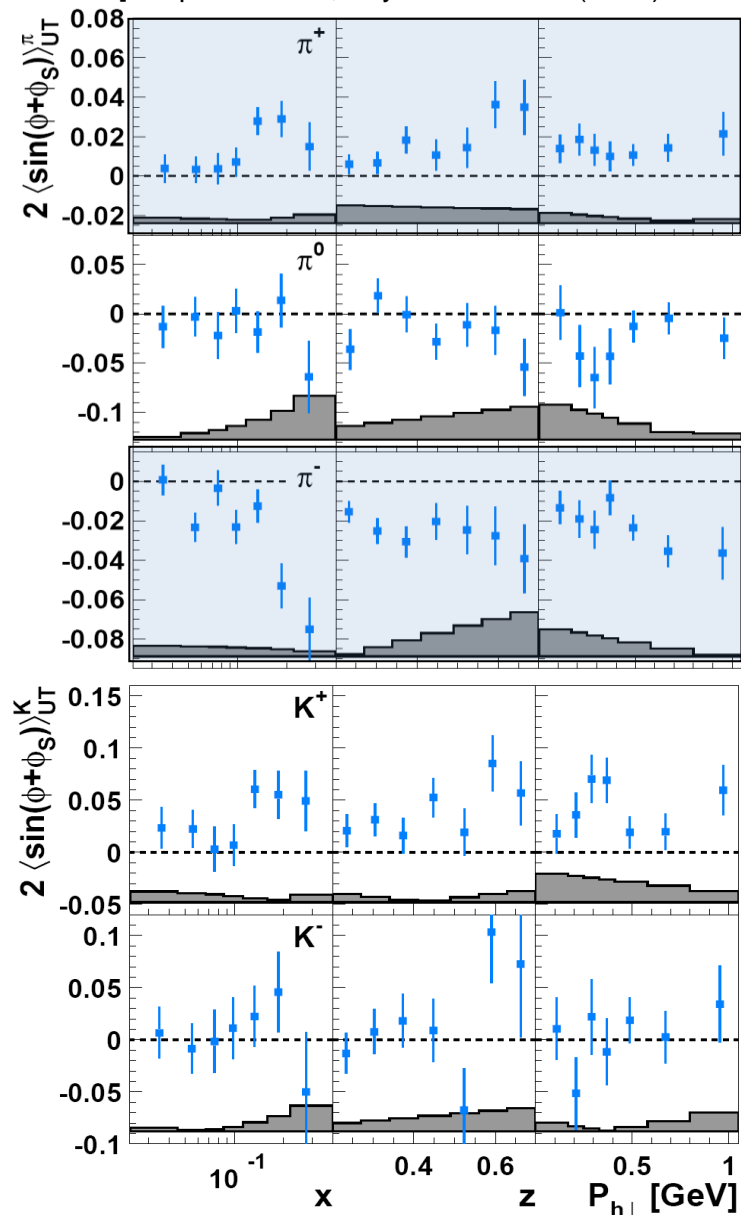
		quark		
		U	L	T
nucleon	U	f_1		h_1^\perp
	L		g_1	h_{1L}^\perp
	T	f_{1T}^\perp	g_{1T}^\perp	h_1 h_{1T}^\perp

Fragmentation Functions

		quark		
		U	L	T
h	U	D_1		H_1^\perp

Collins amplitudes $\propto h_1(x, p_T^2) \otimes H_1^\perp(z, k_T^2)$

[Airapetian et al., Phys. Lett. B 693 (2010) 11-16]



positive

consistent with zero
(isospin-symmetry)

large and negative!

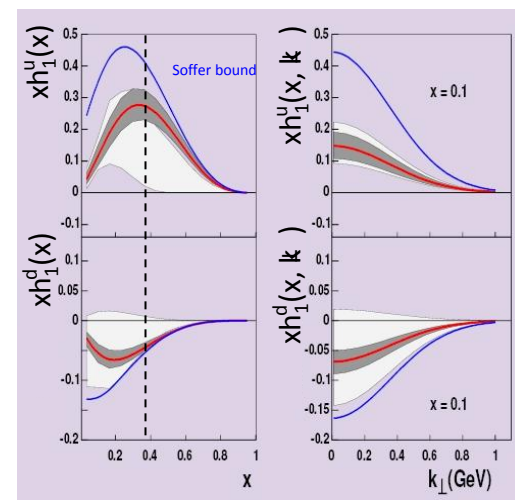
significantly positive

consistent with zero

$$\begin{array}{cc}
 \left[\begin{array}{l} u \rightarrow \pi^- \\ d \rightarrow \pi^+ \end{array} \right. & \left[\begin{array}{l} u \rightarrow \pi^+ \\ d \rightarrow \pi^- \end{array} \right. \\
 \uparrow & \uparrow \\
 H_1^{\perp, unfav}(z) \approx -H_1^{\perp, fav}(z) &
 \end{array}$$

Consistent with Belle/BaBar measurements in e^+e^-

$$e^+e^- \rightarrow \pi_{jet1}^+ \pi_{jet2}^- X$$



Anselmino et al. Phys. Rev. D 75 (2007)



Sivers function

$$\frac{d\sigma^h}{dx dy d\phi_S dz d\phi d\mathbf{P}_{h\perp}^2} = \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x} \right) \left\{ \begin{aligned} & \left[F_{UU,T} + \epsilon F_{UU,L} \right. \\ & \left. + \sqrt{2\epsilon(1+\epsilon)} \cos(\phi) F_{UU}^{\cos(\phi)} + \epsilon \cos(2\phi) F_{UU}^{\cos(2\phi)} \right] \\ & + \lambda_L \left[\sqrt{2\epsilon(1-\epsilon)} \sin(\phi) F_{LU}^{\sin(\phi)} \right] \\ & + S_L \left[\sqrt{2\epsilon(1+\epsilon)} \sin(\phi) F_{UL}^{\sin(\phi)} + \epsilon \sin(2\phi) F_{UL}^{\sin(2\phi)} \right] \\ & + S_L \lambda_L \left[\sqrt{1-\epsilon^2} F_{LL} + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi) F_{LL}^{\cos(\phi)} \right] \\ & + S_T \left[\sin(\phi - \phi_S) \left(F_{UT,T}^{\sin(\phi-\phi_S)} + \epsilon F_{UT,L}^{\sin(\phi-\phi_S)} \right) \right. \\ & \left. + \epsilon \sin(\phi + \phi_S) F_{UT}^{\sin(\phi+\phi_S)} + \epsilon \sin(3\phi - \phi_S) F_{UT}^{\sin(3\phi-\phi_S)} \right. \\ & \left. + \sqrt{2\epsilon(1+\epsilon)} \sin(\phi_S) F_{UT}^{\sin(\phi_S)} \right. \\ & \left. + \sqrt{2\epsilon(1+\epsilon)} \sin(2\phi - \phi_S) F_{UT}^{\sin(2\phi-\phi_S)} \right] \\ & + S_T \lambda_L \left[\sqrt{1-\epsilon^2} \cos(\phi - \phi_S) F_{LT}^{\cos(\phi-\phi_S)} \right. \\ & \left. + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi_S) F_{LT}^{\cos(\phi_S)} \right. \\ & \left. + \sqrt{2\epsilon(1-\epsilon)} \cos(2\phi - \phi_S) F_{LT}^{\cos(2\phi-\phi_S)} \right] \end{aligned} \right\}$$

$$F_{UT,T}^{\sin(\phi_h - \phi_S)} = C \left[-\frac{\hat{h} \cdot \mathbf{p}_T}{M} f_{1T}^\perp D_1 \right]$$

Describes correlation between quark transverse momentum and nucleon transverse polarization

Distribution Functions

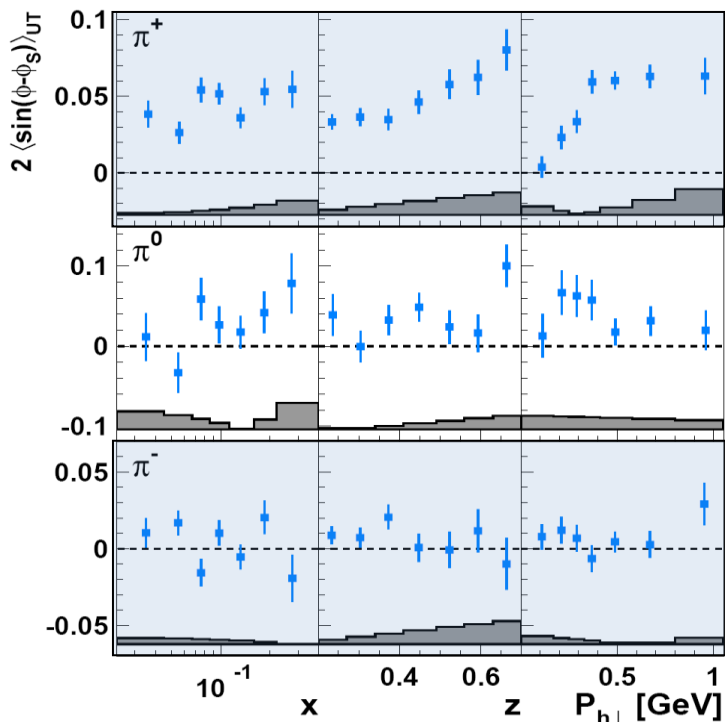
		quark		
		U	L	T
n u c l e o n	U	f_1		h_1^\perp
	L		g_1	h_{1L}^\perp
	T	f_{1T}^\perp	g_{1T}^\perp	h_1

Fragmentation Functions

		quark		
		U	L	T
h	U	D_1		H_1^\perp

Sivers amplitudes $\propto f_{1T}^\perp(x, p_T^2) \otimes D_1(z, k_T^2)$

[Airapetian et al., Phys. Rev. Lett. 103 (2009) 152002]

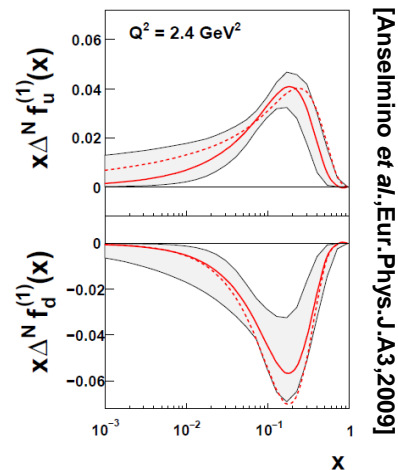


significantly positive

slightly positive
(isospin-symmetry)

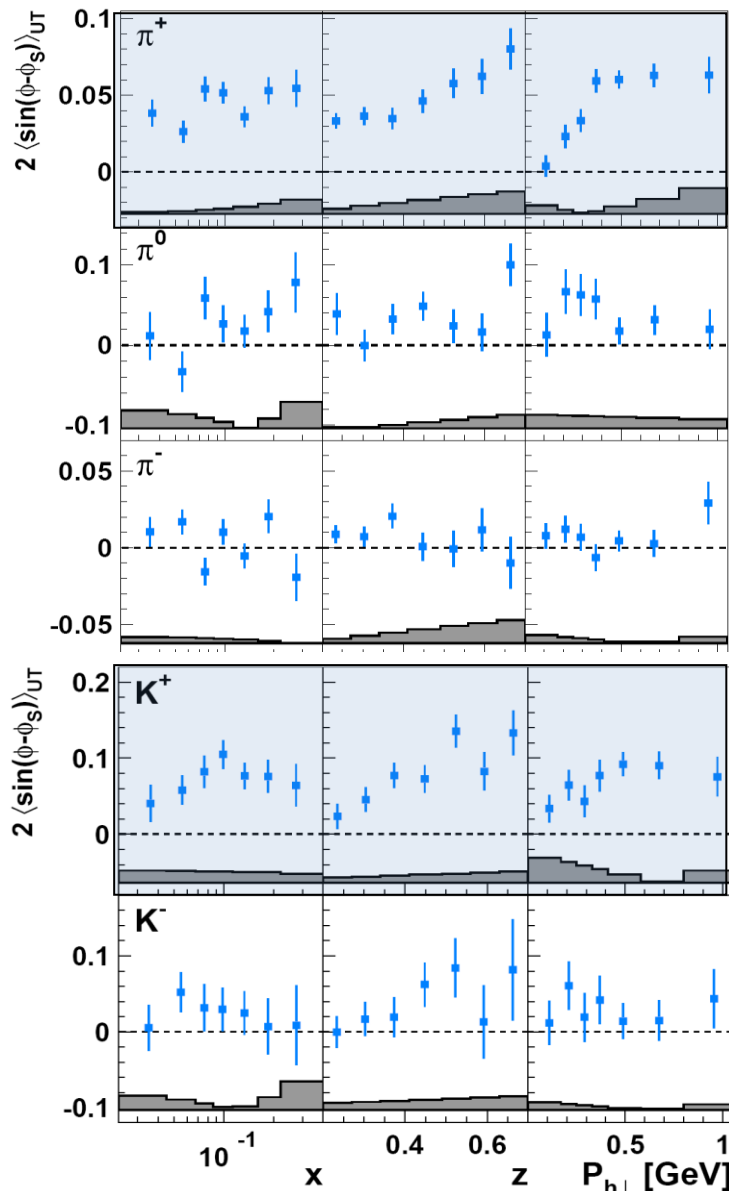
consistent with zero

consistent with Sivers func. of opposite sign for u and d quarks



Sivers amplitudes $\propto f_{1T}^\perp(x, p_T^2) \otimes D_1(z, k_T^2)$

[Airapetian et al., Phys. Rev. Lett. 103 (2009) 152002]



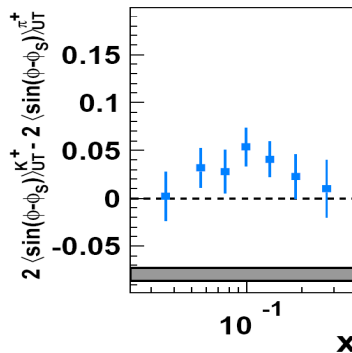
☞ significantly positive

☞ slightly positive
(isospin-symmetry)

☞ consistent with zero

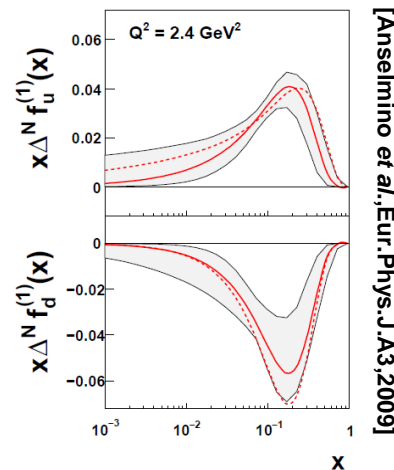
☞ Larger than π^+ !!

- role of sea quarks ?

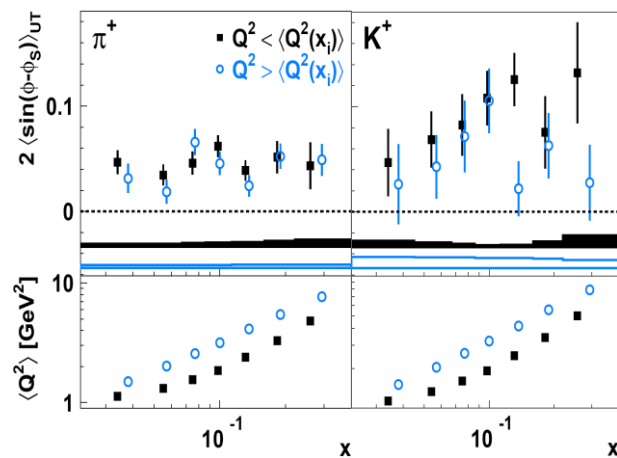


diff. comes from low Q^2

consistent with Sivers func. of opposite sign for u and d quarks

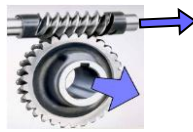


[Anselmino et al., Eur. Phys. J. A3, 2009]



- Higher-twist contrib for K^+ ?

Worm-gear g_{1T}^\perp



$$\frac{d\sigma^h}{dx dy d\phi_S dz d\phi d\mathbf{P}_{h\perp}^2} = \frac{\alpha^2 y^2}{xyQ^2 2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x} \right)$$

$$\left\{ \begin{aligned} & \left[F_{UU,T} + \epsilon F_{UU,L} \right. \\ & \left. + \sqrt{2\epsilon(1+\epsilon)} \cos(\phi) F_{UU}^{\cos(\phi)} + \epsilon \cos(2\phi) F_{UU}^{\cos(2\phi)} \right] \\ + \lambda_l & \left[\sqrt{2\epsilon(1-\epsilon)} \sin(\phi) F_{LU}^{\sin(\phi)} \right] \\ + S_L & \left[\sqrt{2\epsilon(1+\epsilon)} \sin(\phi) F_{UL}^{\sin(\phi)} + \epsilon \sin(2\phi) F_{UL}^{\sin(2\phi)} \right] \\ + S_L \lambda_l & \left[\sqrt{1-\epsilon^2} F_{LL} + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi) F_{LL}^{\cos(\phi)} \right] \\ + S_T & \left[\sin(\phi - \phi_S) \left(F_{UT,T}^{\sin(\phi-\phi_S)} + \epsilon F_{UT,L}^{\sin(\phi-\phi_S)} \right) \right. \\ & + \epsilon \sin(\phi + \phi_S) F_{UT}^{\sin(\phi+\phi_S)} + \epsilon \sin(3\phi - \phi_S) F_{UT}^{\sin(3\phi-\phi_S)} \\ & + \sqrt{2\epsilon(1+\epsilon)} \sin(\phi_S) F_{UT}^{\sin(\phi_S)} \\ & \left. + \sqrt{2\epsilon(1+\epsilon)} \sin(2\phi - \phi_S) F_{UT}^{\sin(2\phi-\phi_S)} \right] \end{aligned} \right.$$

$$\left. \left\{ \begin{aligned} + S_T \lambda_l & \left[\sqrt{1-\epsilon^2} \cos(\phi - \phi_S) F_{LT}^{\cos(\phi-\phi_S)} \right. \right. \\ & + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi_S) F_{LT}^{\cos(\phi_S)} \\ & \left. \left. + \sqrt{2\epsilon(1-\epsilon)} \cos(2\phi - \phi_S) F_{LT}^{\cos(2\phi-\phi_S)} \right] \right\} \right.$$

$$F_{LT}^{\cos(\phi_h - \phi_S)} = C \left[\frac{\hat{h} \cdot p_T}{M} g_{1T} D_1 \right]$$

Describes the probability to find longitudinally polarized quarks in a transversely polarized nucleon!

- requires interference between wave funct. components that differ by 1 unit of **OAM**
- Can be accessed in **LT DSAs**

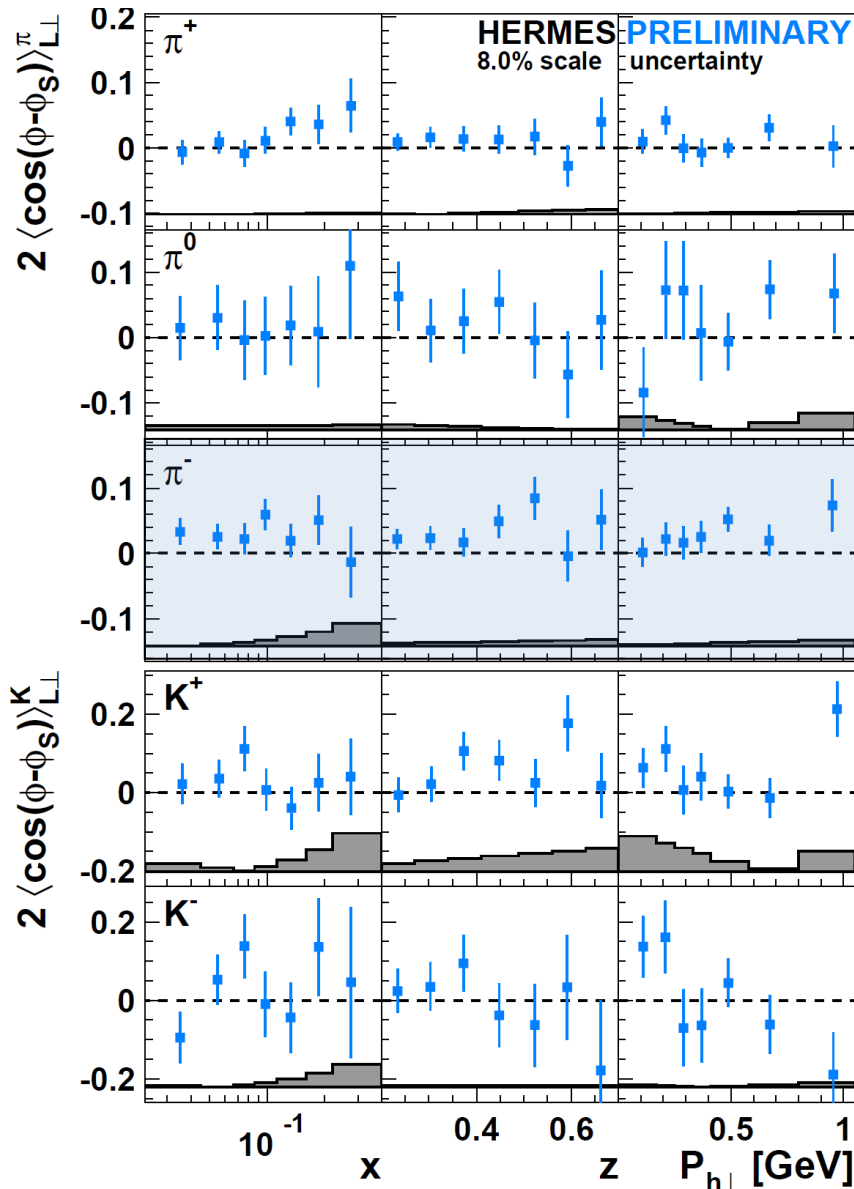
Distribution Functions

		quark		
		U	L	T
nucleon	U	f_1		h_1^\perp
	L		g_1	h_{1L}^\perp
	T	f_{1T}^\perp	g_{1T}^\perp	h_1 h_{1T}^\perp

Fragmentation Functions

		quark		
		U	L	T
h	U	D_1		H_1^\perp

The $\cos(\phi-\phi_S)$ amplitudes $\propto g_{1T}^\perp(x, p_T^2) \otimes D_1(z, k_T^2)$



☞ slightly positive ?

☞ consistent with zero

☞ positive!!

similar observations from Hall-A and COMPASS

☞ slightly positive ?

☞ consistent with zero

Selected higher-twist 1-hadron SIDIS results

Subleading twist

$$\frac{d\sigma^h}{dx dy d\phi_S dz d\phi d\mathbf{P}_{h\perp}^2} = \frac{\alpha^2 y^2}{xyQ^2 2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x} \right)$$

$$\left\{ \begin{aligned} & \left[F_{UU,T} + \epsilon F_{UU,L} \right. \\ & \left. + \sqrt{2\epsilon(1+\epsilon)} \cos(\phi) F_{UU}^{\cos(\phi)} + \epsilon \cos(2\phi) F_{UU}^{\cos(2\phi)} \right] \end{aligned} \right.$$

$$+ \lambda_l \left[\sqrt{2\epsilon(1-\epsilon)} \sin(\phi) F_{LU}^{\sin(\phi)} \right]$$

$$+ S_L \left[\sqrt{2\epsilon(1+\epsilon)} \sin(\phi) F_{UL}^{\sin(\phi)} + \epsilon \sin(2\phi) F_{UL}^{\sin(2\phi)} \right]$$

$$+ S_L \lambda_l \left[\sqrt{1-\epsilon^2} F_{LL} + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi) F_{LL}^{\cos(\phi)} \right]$$














$$+ S_T \left[\begin{aligned} & \sin(\phi - \phi_S) \left(F_{UT,T}^{\sin(\phi-\phi_S)} + \epsilon F_{UT,L}^{\sin(\phi-\phi_S)} \right) \\ & + \epsilon \sin(\phi + \phi_S) F_{UT}^{\sin(\phi+\phi_S)} + \epsilon \sin(3\phi - \phi_S) F_{UT}^{\sin(3\phi-\phi_S)} \\ & + \sqrt{2\epsilon(1+\epsilon)} \sin(\phi_S) F_{UT}^{\sin(\phi_S)} \\ & + \sqrt{2\epsilon(1+\epsilon)} \sin(2\phi - \phi_S) F_{UT}^{\sin(2\phi-\phi_S)} \end{aligned} \right]$$

$$+ S_T \lambda_l \left[\begin{aligned} & \sqrt{1-\epsilon^2} \cos(\phi - \phi_S) F_{LT}^{\cos(\phi-\phi_S)} \\ & + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi_S) F_{LT}^{\cos(\phi_S)} \\ & + \sqrt{2\epsilon(1-\epsilon)} \cos(2\phi - \phi_S) F_{LT}^{\cos(2\phi-\phi_S)} \end{aligned} \right] \left. \right\}$$

$$F_{UT}^{\sin\phi_S} = \frac{2M}{Q} \mathcal{C} \left\{ \left(x f_T D_1 - \frac{M_h}{M} h_1 \frac{\tilde{H}}{z} \right) - \frac{k_T \cdot p_T}{2MM_h} \left[\left(x h_T H_1^\perp + \frac{M_h}{M} g_{1T} \frac{\tilde{G}^\perp}{z} \right) - \left(x h_T^\perp H_1^\perp - \frac{M_h}{M} f_{1T}^\perp \frac{\tilde{D}^\perp}{z} \right) \right] \right\}$$

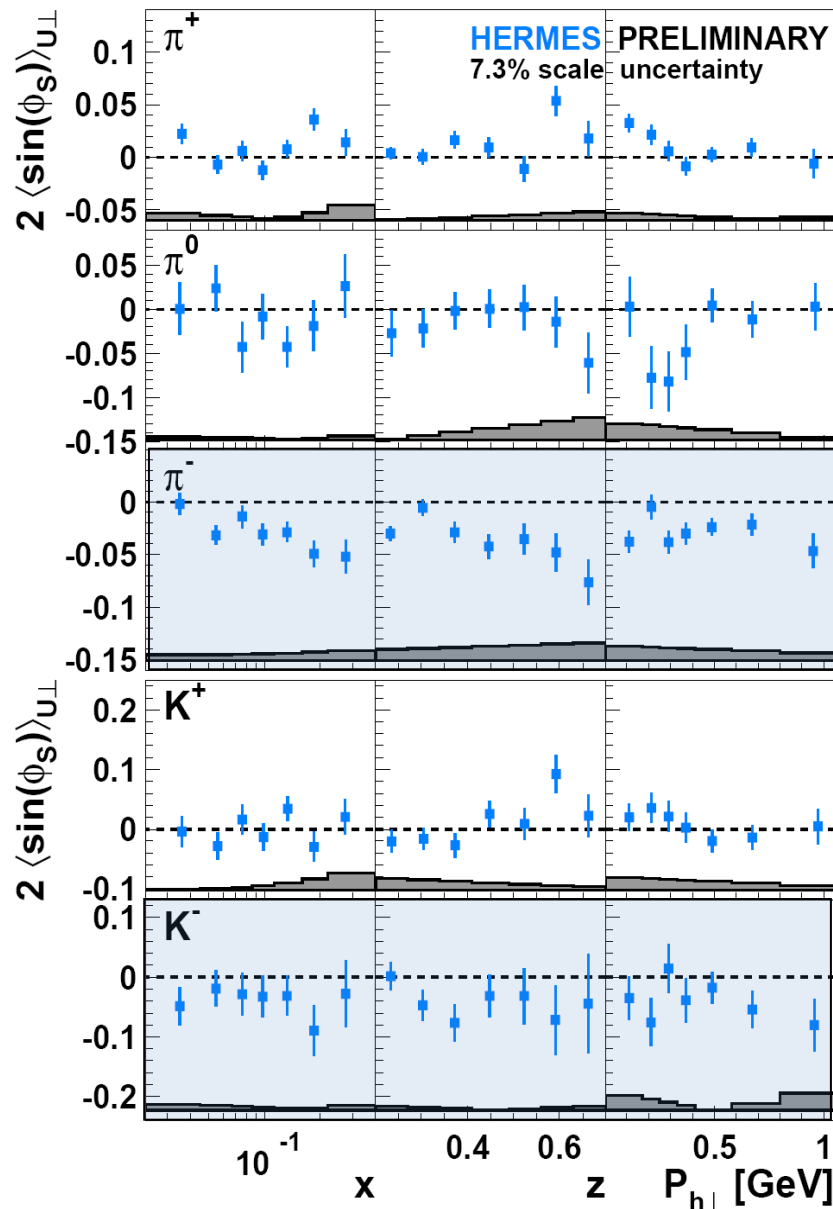
Sensitive to worm-gear g_{1T}^\perp , sivers, transversity + higher-twist DF and FF

Distribution Functions

		quark		
		U	L	T
nucleon	U	f_1 		h_1^\perp  - 
	L		g_1  - 	h_{1L}^\perp  - 
	T	f_{1T}^\perp  - 	g_{1T}^\perp  - 	h_{1T}^\perp  - 

Subleading-twist $\sin(\phi_S)$ Fourier component

- sensitive to **worm-gear** g_{1T}^\perp , **Sivers function**, **Transversity**, etc
- **significant non-zero signal for π^- and K^- !**

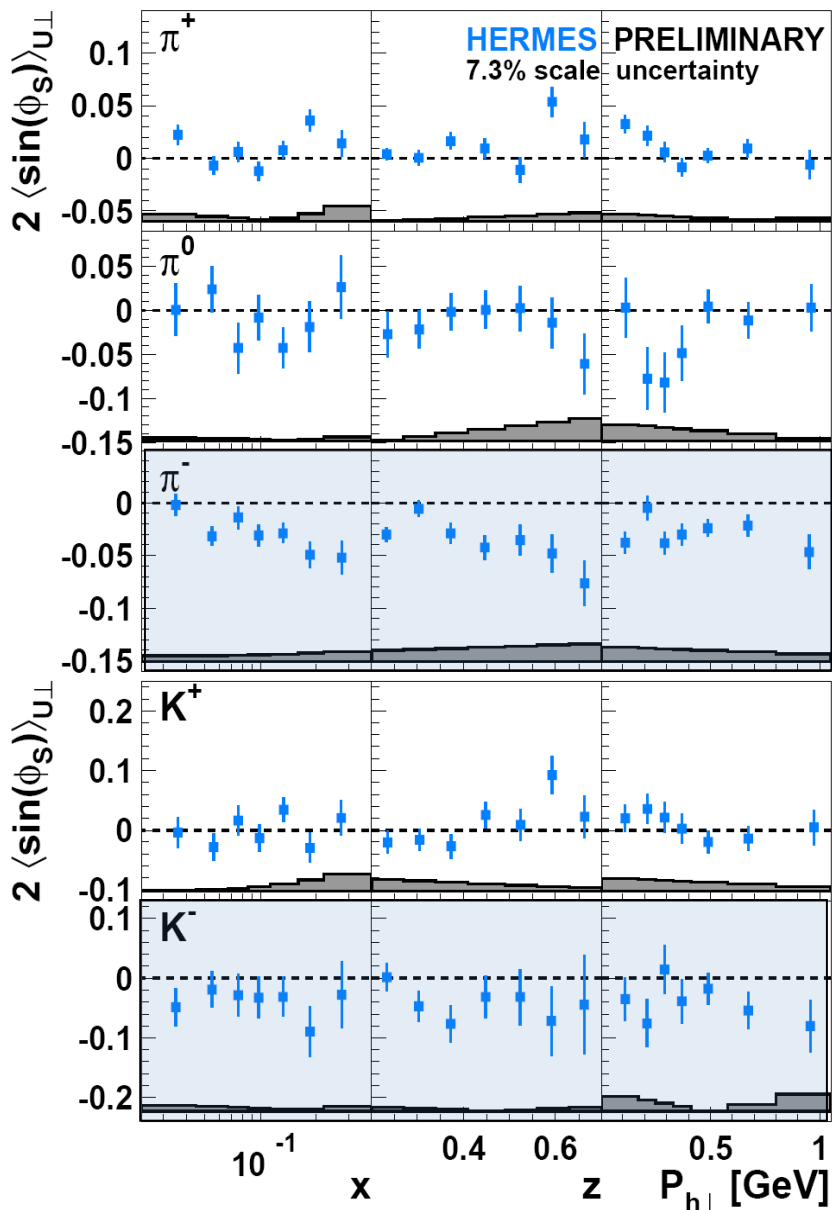


Large and negative

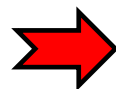
negative

Subleading-twist $\sin(\phi_S)$ Fourier component

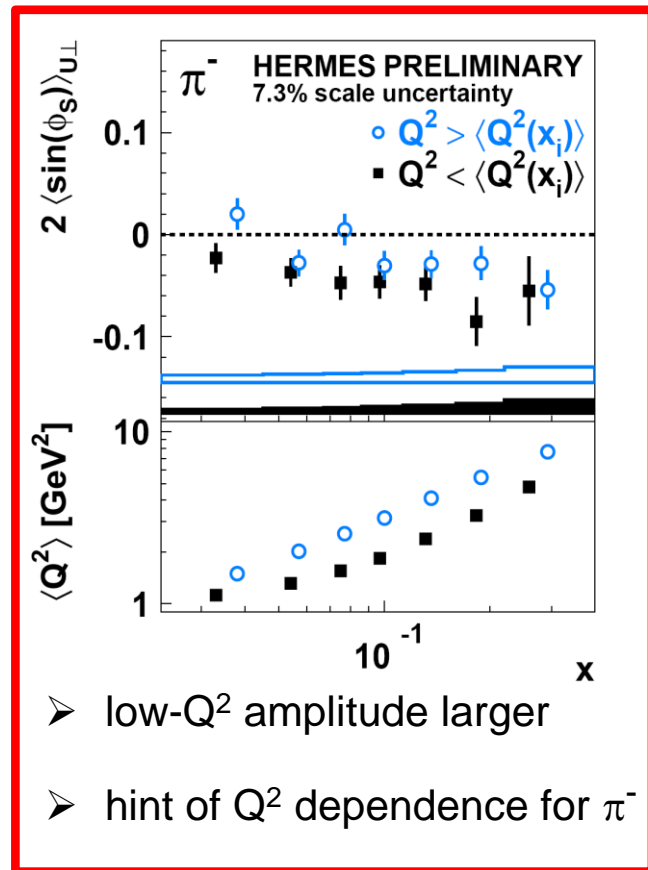
- sensitive to **worm-gear** g_{1T}^\perp , **Sivers function**, **Transversity**, etc
- **significant non-zero signal for π^- and K^- !**



Large and negative



negative



$F_{LU}^{\sin \phi}$

$$F_{LU}^{\sin \phi_h} = \frac{2M}{Q} c \left[-\frac{\hat{h} \cdot \mathbf{k}_T}{M_h} \left(x e H_1^\perp + \frac{M_h}{M} f_1 \frac{\tilde{G}^\perp}{z} \right) + \frac{\hat{h} \cdot \mathbf{p}_T}{M} \left(x g^\perp D_1 + \frac{M_h}{M} h_1^\perp \frac{\tilde{E}}{z} \right) \right]$$

$$\frac{d\sigma^h}{dx dy d\phi_S dz d\phi d\mathbf{P}_{h\perp}^2} = \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x} \right)$$

$$\left\{ \begin{aligned} & \left[F_{UU,T} + \epsilon F_{UU,L} \right. \\ & \left. + \sqrt{2\epsilon(1+\epsilon)} \cos(\phi) F_{UU}^{\cos(\phi)} + \epsilon \cos(2\phi) F_{UU}^{\cos(2\phi)} \right] \end{aligned} \right.$$

$$+ \lambda_l \left[\sqrt{2\epsilon(1-\epsilon)} \sin(\phi) F_{LU}^{\sin(\phi)} \right]$$

$$+ S_L \left[\sqrt{2\epsilon(1+\epsilon)} \sin(\phi) F_{UL}^{\sin(\phi)} + \epsilon \sin(2\phi) F_{UL}^{\sin(2\phi)} \right]$$

$$+ S_L \lambda_l \left[\sqrt{1-\epsilon^2} F_{LL} + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi) F_{LL}^{\cos(\phi)} \right]$$

$$+ S_T \left[\begin{aligned} & \sin(\phi - \phi_S) \left(F_{UT,T}^{\sin(\phi-\phi_S)} + \epsilon F_{UT,L}^{\sin(\phi-\phi_S)} \right) \\ & + \epsilon \sin(\phi + \phi_S) F_{UT}^{\sin(\phi+\phi_S)} + \epsilon \sin(3\phi - \phi_S) F_{UT}^{\sin(3\phi-\phi_S)} \\ & + \sqrt{2\epsilon(1+\epsilon)} \sin(\phi_S) F_{UT}^{\sin(\phi_S)} \\ & + \sqrt{2\epsilon(1+\epsilon)} \sin(2\phi - \phi_S) F_{UT}^{\sin(2\phi-\phi_S)} \end{aligned} \right]$$

$$+ S_T \lambda_l \left[\begin{aligned} & \sqrt{1-\epsilon^2} \cos(\phi - \phi_S) F_{LT}^{\cos(\phi-\phi_S)} \\ & + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi_S) F_{LT}^{\cos(\phi_S)} \\ & + \sqrt{2\epsilon(1-\epsilon)} \cos(2\phi - \phi_S) F_{LT}^{\cos(2\phi-\phi_S)} \end{aligned} \right] \left. \right\}$$

Sensitive to f_1 , Boer-Mulders + higher-twist DF and FF

Distribution Functions

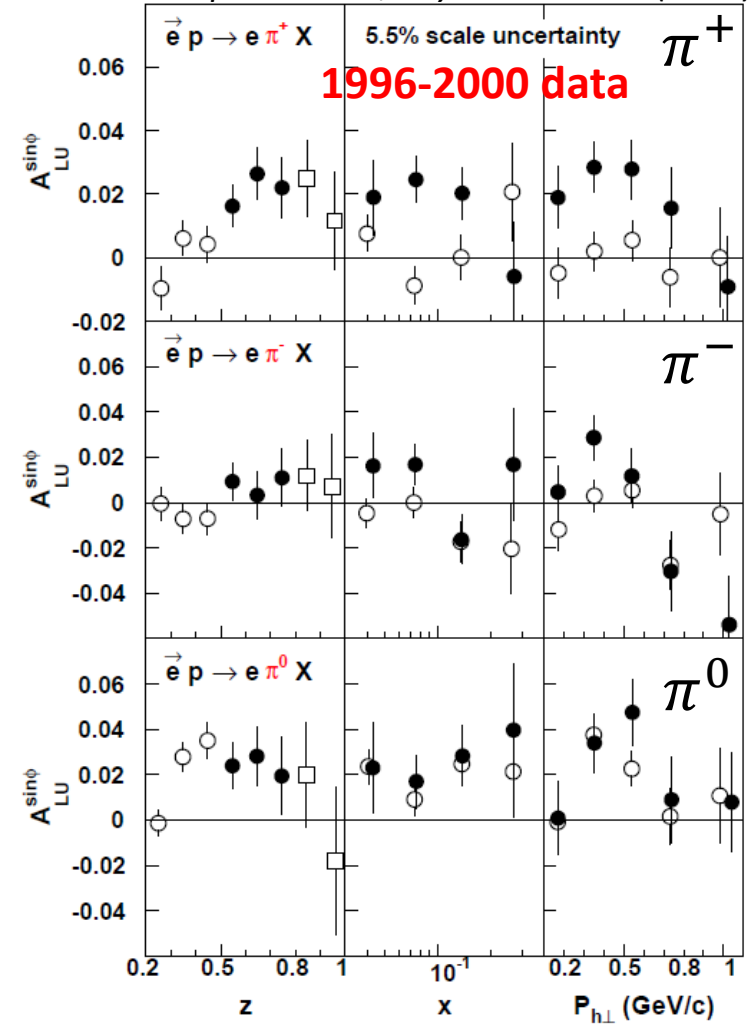
		quark		
		U	L	T
nucleon	U	f_1		h_1^\perp
	L		g_1	h_{1L}^\perp
	T	f_{1T}^\perp	g_{1T}^\perp	h_{1T}^\perp

$F_{LU} \sin \phi$

$$F_{LU}^{\sin \phi_h} = \frac{2M}{Q} c \left[-\frac{\hat{h} \cdot \mathbf{k}_T}{M_h} \left(x e H_1^\perp + \frac{M_h}{M} f_1 \frac{\tilde{G}^\perp}{z} \right) + \frac{\hat{h} \cdot \mathbf{p}_T}{M} \left(x g^\perp D_1 + \frac{M_h}{M} h_1^\perp \frac{\tilde{E}}{z} \right) \right]$$

$$\frac{d\sigma^h}{dx dy d\phi_S dz d\phi d\mathbf{P}_{h\perp}^2} = \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x} \right) \left\{ \begin{aligned} & \left[F_{UU,T} + \epsilon F_{UU,L} \right. \\ & \left. + \sqrt{2\epsilon(1+\epsilon)} \cos(\phi) F_{UU}^{\cos(\phi)} + \epsilon \cos(2\phi) F_{UU}^{\cos(2\phi)} \right] \\ & + \lambda_l \left[\sqrt{2\epsilon(1-\epsilon)} \sin(\phi) F_{LU}^{\sin(\phi)} \right] \\ & + S_L \left[\sqrt{2\epsilon(1+\epsilon)} \sin(\phi) F_{UL}^{\sin(\phi)} + \epsilon \sin(2\phi) F_{UL}^{\sin(2\phi)} \right] \\ & + S_L \lambda_l \left[\sqrt{1-\epsilon^2} F_{LL} + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi) F_{LL}^{\cos(\phi)} \right] \\ & + S_T \left[\sin(\phi - \phi_S) \left(F_{UT,T}^{\sin(\phi-\phi_S)} + \epsilon F_{UT,L}^{\sin(\phi-\phi_S)} \right) \right. \\ & \left. + \epsilon \sin(\phi + \phi_S) F_{UT}^{\sin(\phi+\phi_S)} + \epsilon \sin(3\phi - \phi_S) F_{UT}^{\sin(3\phi-\phi_S)} \right. \\ & \left. + \sqrt{2\epsilon(1+\epsilon)} \sin(\phi_S) F_{UT}^{\sin(\phi_S)} \right. \\ & \left. + \sqrt{2\epsilon(1+\epsilon)} \sin(2\phi - \phi_S) F_{UT}^{\sin(2\phi-\phi_S)} \right] \\ & + S_T \lambda_l \left[\sqrt{1-\epsilon^2} \cos(\phi - \phi_S) F_{LT}^{\cos(\phi-\phi_S)} \right. \\ & \left. + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi_S) F_{LT}^{\cos(\phi_S)} \right. \\ & \left. + \sqrt{2\epsilon(1-\epsilon)} \cos(2\phi - \phi_S) F_{LT}^{\cos(2\phi-\phi_S)} \right] \end{aligned} \right\}$$

A. Airapetian et al, Phys. Lett. B 648 (2007)

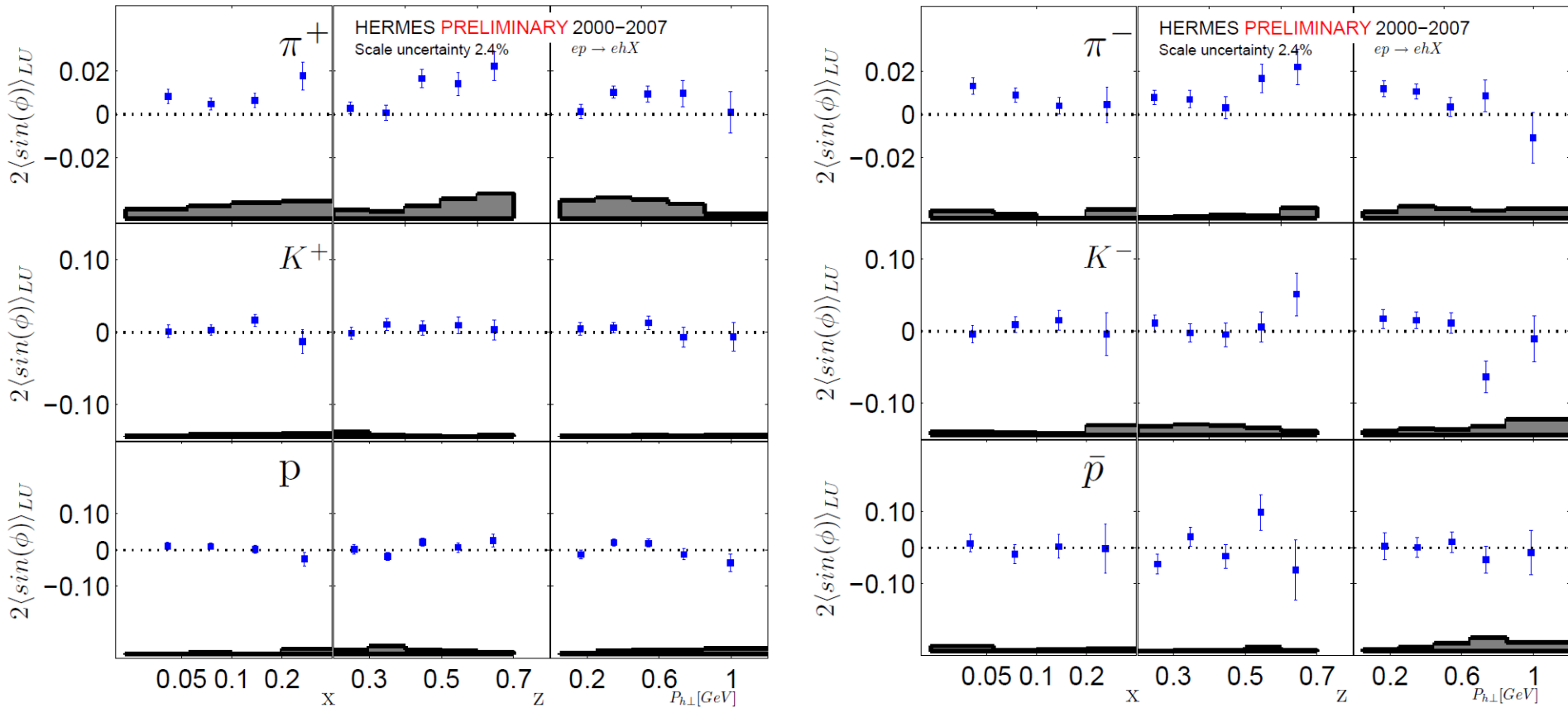


open circles $0.2 < z < 0.5$
 full circles $0.5 < z < 0.8$
 open squares: $0.8 < z < 1.0$

$F_{LU}^{\sin \phi}$

$$F_{LU}^{\sin \phi_h} = \frac{2M}{Q} c \left[-\frac{\hat{h} \cdot \mathbf{k}_T}{M_h} \left(x e H_1^\perp + \frac{M_h}{M} f_1 \frac{\tilde{G}^\perp}{z} \right) + \frac{\hat{h} \cdot \mathbf{p}_T}{M} \left(x g^\perp D_1 + \frac{M_h}{M} h_1^\perp \frac{\tilde{E}}{z} \right) \right]$$

H target, 2000-2007 data $0.2 < z < 0.7$

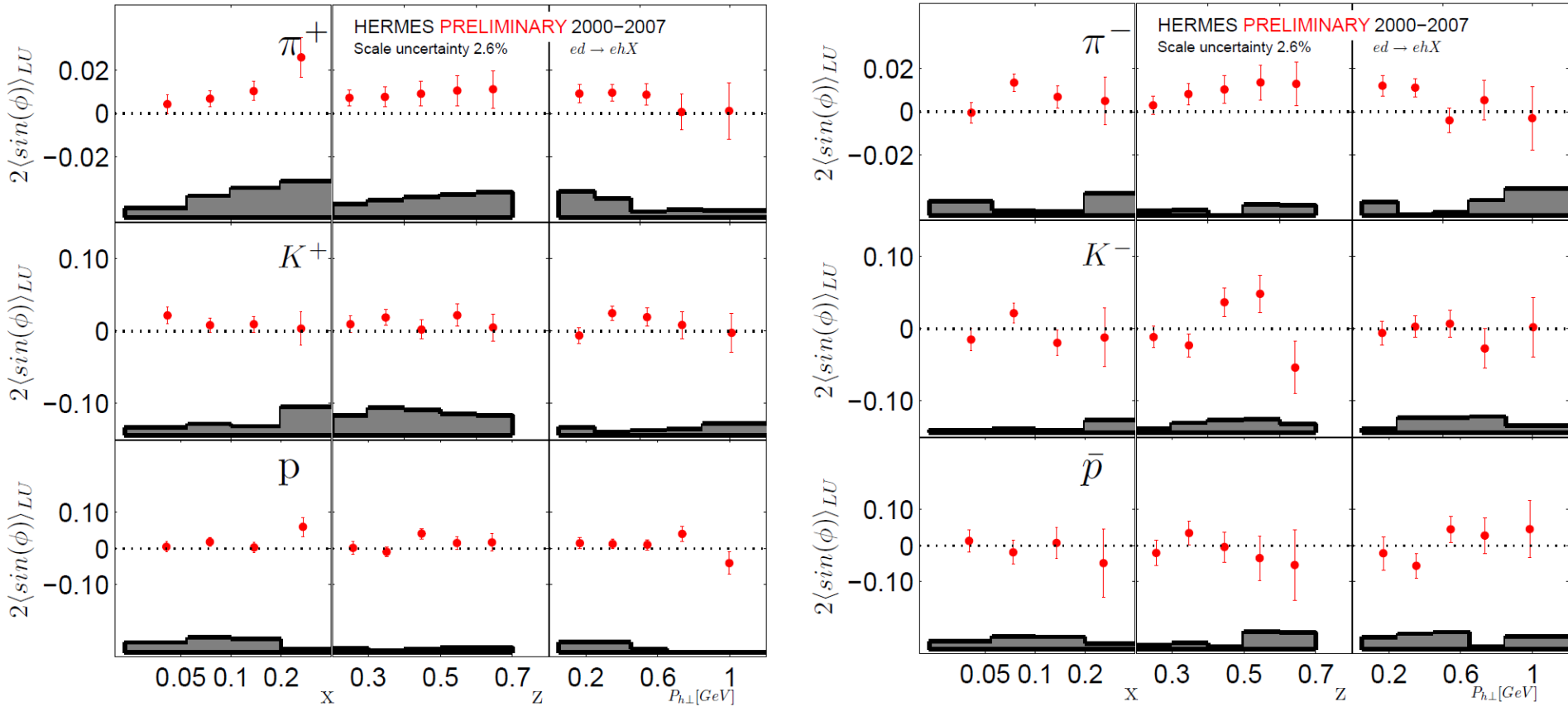


Released yesterday!!

$F_{LU} \sin \phi$

$$F_{LU}^{\sin \phi_h} = \frac{2M}{Q} c \left[-\frac{\hat{h} \cdot \mathbf{k}_T}{M_h} \left(x e H_1^\perp + \frac{M_h}{M} f_1 \frac{\tilde{G}^\perp}{z} \right) + \frac{\hat{h} \cdot \mathbf{p}_T}{M} \left(x g^\perp D_1 + \frac{M_h}{M} h_1^\perp \frac{\tilde{E}}{z} \right) \right]$$

D target, 2000-2007 data $0.2 < z < 0.7$



Released yesterday!!

2-hadron SIDIS results

Following formalism developed by **Steve Gliske**

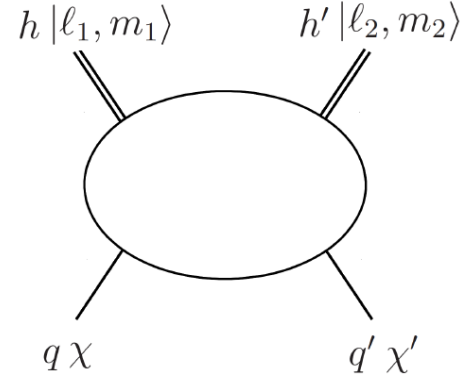
Find details in

Transverse Target Moments of Dihadron Production in Semi-inclusive Deep Inelastic Scattering at HERMES
S. Gliske, PhD thesis, University of Michigan, 2011

A short digression on di-hadron fragmentation functions

Standard definition of di-hadron FF assume no polarization of final state hadrons (pseudo-scalar mesons) or define mixtures of certain partial waves as new FFs

In the **new formalism** there are only two di-hadron FFs. Names and symbols are entirely associated with the quark spin states (D_1 for $\chi = \chi'$ and H_1^\perp (*generalized Collins*) for $\chi \neq \chi'$), whereas the partial waves of the produced hadrons ($|\ell_1 m_1\rangle, |\ell_2 m_2\rangle$) are associated with partial waves of FFs.



$$D_1 = \sum_{\ell=1}^{\infty} \sum_{m=-\ell}^{\ell} P_{\ell,m}(\cos \vartheta) e^{im(\phi_R - \phi_k)} D_1^{|\ell,m\rangle}(z, M_h, |\mathbf{k}_T|)$$

$$H_1^\perp = \sum_{\ell=1}^{\infty} \sum_{m=-\ell}^{\ell} P_{\ell,m}(\cos \vartheta) e^{im(\phi_R - \phi_k)} H_1^{\perp|\ell,m\rangle}(z, M_h, |\mathbf{k}_T|)$$

The cross-section is identical to the ones in literature, the only difference is the interpretation of the FFs:

$$D_1^{[0,0]} = D_{1,OO} = \left(\frac{1}{4} D_{1,OO}^s + \frac{3}{4} D_{1,OO}^p \right)$$

$$H_1^{\perp[0,0]} = H_{1,OO}^\perp = \frac{1}{4} H_{1,OO}^{\perp s} + \frac{3}{4} H_{1,OO}^{\perp p}$$

$$H_1^{\perp[2,0]} = \frac{1}{2} H_{1,LL}^\perp$$

$$D_1^{[1,0]} = D_{1,OL}$$

$$H_1^{\perp[1,1]} = H_{1,OT}^\perp + \frac{|\mathbf{R}|}{|\mathbf{k}_T|} \bar{H}_{1,OT}^\perp = \frac{|\mathbf{R}|}{|\mathbf{k}_T|} H_{1,OT}^\perp$$

$$H_1^{\perp[2,-1]} = \frac{1}{2} H_{1,LT}^\perp$$

$$D_1^{[1,\pm 1]} = D_{1,OT} \mp \frac{|\mathbf{k}_T| |\mathbf{R}|}{M_h^2} G_{1,OT}^\perp$$

$$H_1^{\perp[1,0]} = H_{1,OL}^\perp$$

$$H_1^{\perp[2,-2]} = H_{1,TT}^\perp$$

$$D_1^{[2,0]} = \frac{1}{2} D_{1,LL}$$

$$H_1^{\perp[1,-1]} = H_{1,OT}^\perp$$

$$D_1^{[2,\pm 1]} = \frac{1}{2} \left(D_{1,LT} \mp \frac{|\mathbf{k}_T| |\mathbf{R}|}{M_h^2} G_{1,LT}^\perp \right)$$

$$H_1^{\perp[2,2]} = H_{1,TT}^\perp + \frac{|\mathbf{R}|}{|\mathbf{k}_T|} \bar{H}_{1,TT}^\perp = \frac{|\mathbf{R}|}{|\mathbf{k}_T|} H_{1,TT}^\perp$$

$$D_1^{[2,\pm 2]} = D_{1,TT} \mp \frac{1}{2} \frac{|\mathbf{k}_T| |\mathbf{R}|}{M_h^2} G_{1,TT}^\perp$$

$$H_1^{\perp[2,1]} = \frac{1}{2} H_{1,LT}^\perp + \frac{1}{2} \frac{|\mathbf{R}|}{|\mathbf{k}_T|} \bar{H}_{1,LT}^\perp = \frac{1}{2} \frac{|\mathbf{R}|}{|\mathbf{k}_T|} H_{1,LT}^\perp$$

The di-hadron SIDIS cross-section

$$\begin{aligned}
 d\sigma_{UT} = & \frac{\alpha^2 M_h P_{h\perp}}{2\pi xy Q^2} \left(1 + \frac{\gamma^2}{2x}\right) |\mathbf{S}_\perp| \\
 & \times \sum_{\ell=0}^2 \sum_{m=-\ell}^{\ell} \left\{ A(x, y) \left[P_{\ell, m} \sin((m+1)\phi_h - m\phi_R - \phi_S) \right. \right. \\
 & \quad \times \left. \left(F_{UT,T}^{P_{\ell, m} \sin((m+1)\phi_h - m\phi_R - \phi_S)} + \epsilon F_{UT,L}^{P_{\ell, m} \sin((m+1)\phi_h - m\phi_R - \phi_S)} \right) \right] \\
 & + B(x, y) \left[P_{\ell, m} \sin((1-m)\phi_h + m\phi_R + \phi_S) F_{UT}^{P_{\ell, m} \sin((1-m)\phi_h + m\phi_R + \phi_S)} \right. \\
 & \quad \left. + P_{\ell, m} \sin((3-m)\phi_h + m\phi_R - \phi_S) F_{UT}^{P_{\ell, m} \sin((3-m)\phi_h + m\phi_R - \phi_S)} \right] \\
 & + V(x, y) \left[P_{\ell, m} \sin(-m\phi_h + m\phi_R + \phi_S) F_{UT}^{P_{\ell, m} \sin(-m\phi_h + m\phi_R + \phi_S)} \right. \\
 & \quad \left. + P_{\ell, m} \sin((2-m)\phi_h + m\phi_R - \phi_S) F_{UT}^{P_{\ell, m} \sin((2-m)\phi_h + m\phi_R - \phi_S)} \right] \left. \right\}.
 \end{aligned}$$

l and m correspond to the l and m in $|lm\rangle$ angular momentum state of the hadron

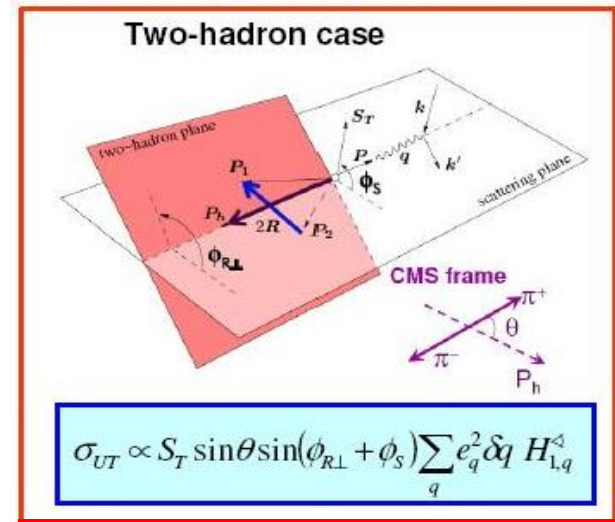
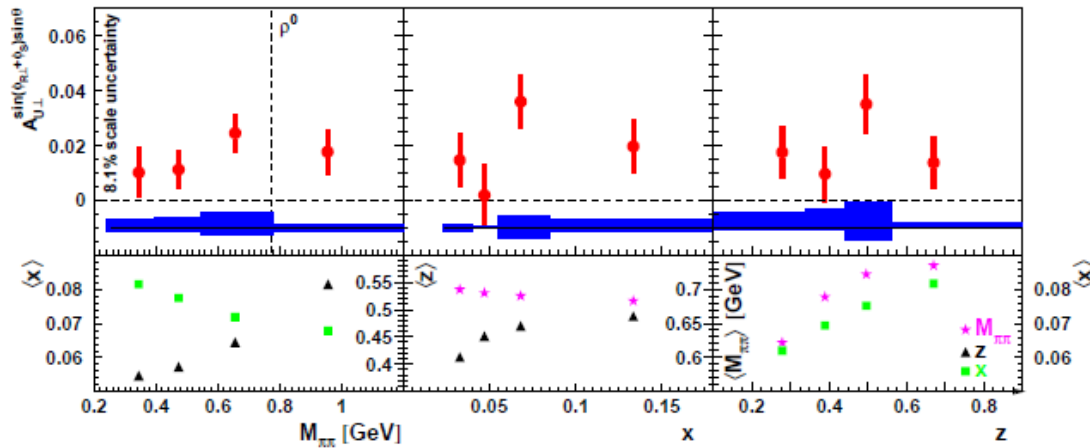
Considering all terms ($d\sigma_{UU}, d\sigma_{LU}, d\sigma_{UL}, d\sigma_{LL}, d\sigma_{UT}, d\sigma_{LT}$) there are **144 non-zero structure functions** at twist-3 level. The most known is

$$F_{UT}^{P_{\ell, m} \sin((1-m)\phi_h + m\phi_R + \phi_S)} = -\mathcal{I} \left[\frac{|\mathbf{k}_T|}{M_h} \cos((m-1)\phi_h - \phi_p - m\phi_k) h_1 H_1^{\perp|\ell, m} \right]$$

which for $l = 1$ and $m = 1$ reduces to the well known colliner $F_{UT}^{\sin \vartheta \sin(\phi_R + \phi_S)}$ related to transversity

The di-hadron SIDIS cross-section

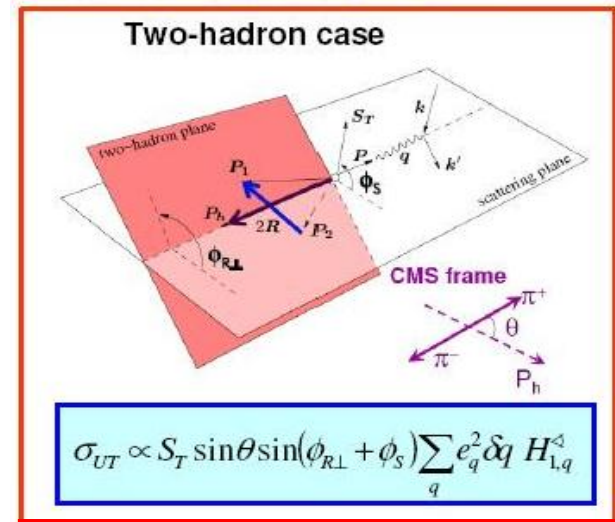
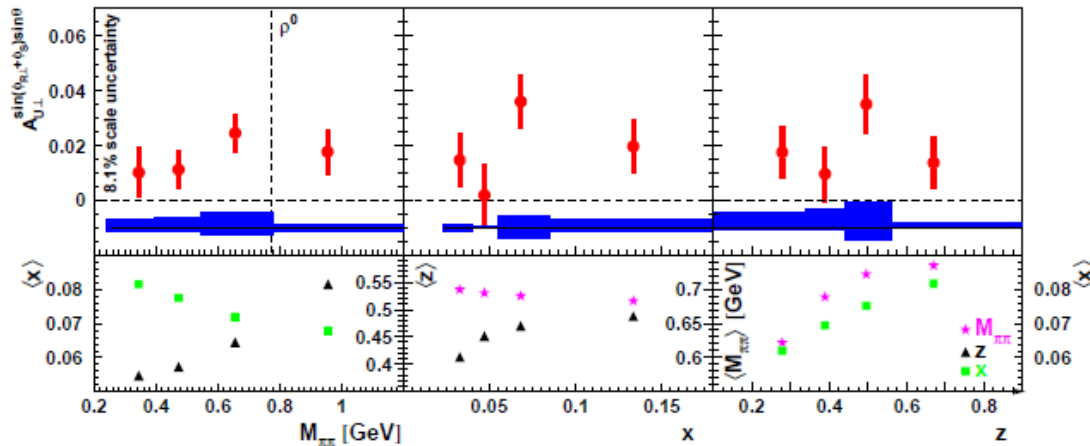
Published $\pi^+\pi^-$ Results



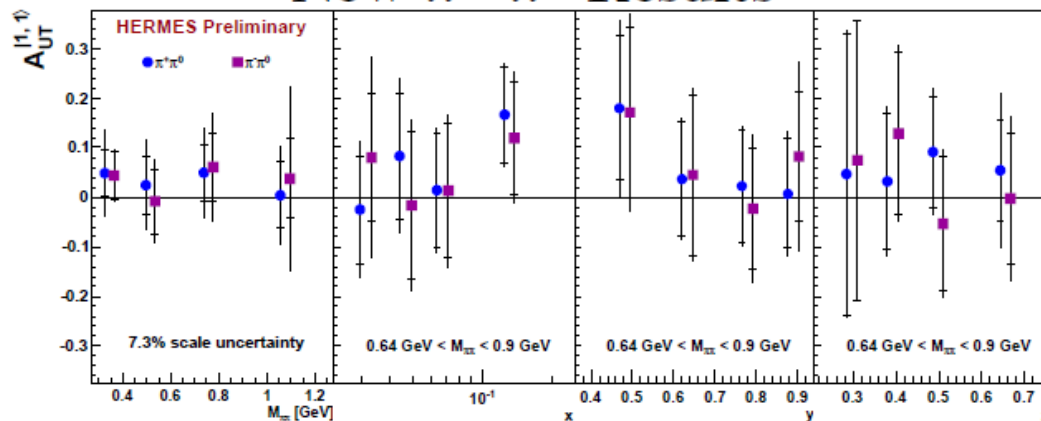
- independent way to access transversity
- significantly positive amplitudes
- 1st evidence of non zero dihadron FF
- no convolution integral involved
- limited statistical power (v.r.t. 1 hadron)

The di-hadron SIDIS cross-section

Published $\pi^+\pi^-$ Results



New $\pi^\pm\pi^0$ Results



- New tracking, new PID, use of ϕ_R rather than ϕ_{RL}
- Different fitting procedure and function
- Acceptance correction

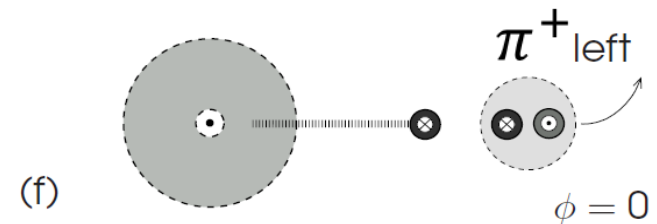
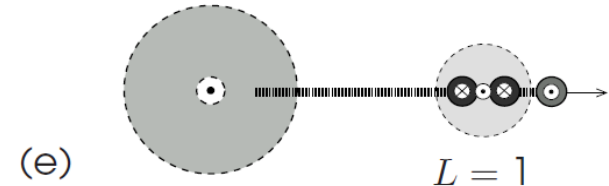
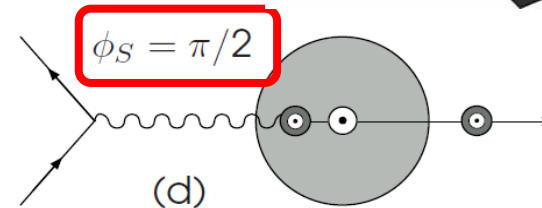
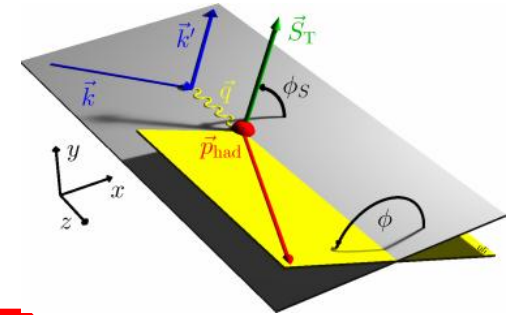
- independent way to access transversity
- significantly positive amplitudes
- 1st evidence of non zero dihadron FF
- no convolution integral involved
- limited statistical power (v.r.t. 1 hadron)
- signs are consistent for all $\pi\pi$ species
- statistics much more limited for $\pi^\pm\pi^0$
- despite uncertainties may still help to constrain global fits and may assist in $u - d$ flavor separation

A short digression on the Lund/Artru string fragmentation model

(a phenomenological explanation of the Collins effect)

In the cross-section the Collins FF is always paired with a distrib. function involving a transv. pol. quark.

1. Assume u quark and proton have (transverse) spin aligned in the direction $\phi_S = \pi/2$. The model assumes that the struck quark is initially connected with the remnant via a gluon-flux tube (string)
2. When the string breaks, a $q\bar{q}$ pair is created with vacuum quantum numbers $J^P = 0^+$. The positive parity requires that the spins of q and \bar{q} are aligned, thus an OAM $L = 1$ has to compensate the spins
3. This OAM generates a transverse momentum of the produced pseudo-scalar meson (e.g. π^+) and deflects the meson to the **left side** w.r.t. the struck quark direction, generating left-right azimuthal asymmetries



A short digression on the Lund/Artru string fragmentation model

Relative to the proton transv. spin, the fragmenting quark can have spin parallel or antiparallel to $\left| \frac{1}{2}, \pm \frac{1}{2} \right\rangle$

Then combining the spins of the formed di-quark systems one can get:

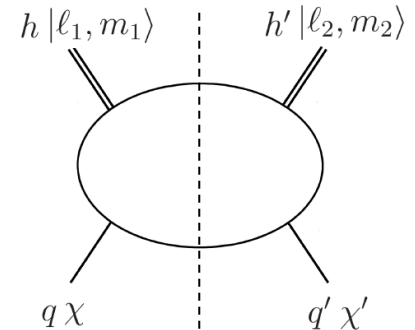
$$\frac{1}{2} \otimes \frac{1}{2} = 1 \oplus 0 \Rightarrow \begin{cases} 1 \text{ spin } 0 \text{ state } |0, 0\rangle & 1 \text{ pseudo-scalar meson (PSM)} \\ 3 \text{ spin } 1 \text{ states } \begin{cases} |1, 0\rangle & 1 \text{ Longitudinal VM} \\ |1, \pm 1\rangle & 2 \text{ transv. VM} \end{cases} \end{cases}$$

Lund/Artru prediction at the amplitude level: the asymmetry for PSM has opposite sign to that for transversely polarized VM (left vs. right side), and the amplitude for $|1, 0\rangle$ is 0

Lund/Artru model makes predictions for the individual di-hadrons, but the Collins function includes pairs of di-hadrons

→ to make predictions for the Collins function one needs to consider the cross-section level, i.e. the sum of contributing amplitudes times their complex conjugate

Using the Clebsch-Gordan algebra one obtains: $|1, \pm 1\rangle |1, \pm 1\rangle \equiv |2, \pm 2\rangle$

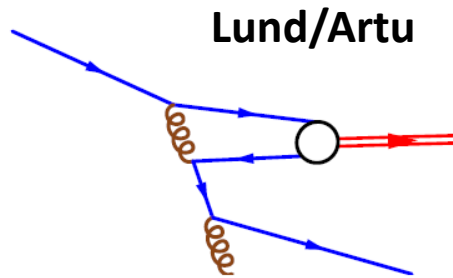


Lund/Artru prediction at the cross-section level: the $|2, \pm 2\rangle$ partial waves of the Collins func. for SIDIS VM production have the opposite sign as the respective PS Collins func.

“gluon radiation model” vs. Lund/Artru model

The Lund/Artru model only accounts for favored Collins fragmentation. An extension of the model (the **gluon radiation model**), elaborated by **S. Gliske** accounts for the disfavored case

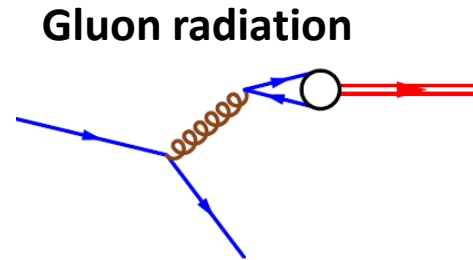
1. Struck quark emits a gluon in such a way that most of its momentum is transferred to the gluon
2. The struck quark then becomes part of the remnant
3. The radiated gluon produces a $q\bar{q}$ pair that eventually converts into a meson
4. For PSM the di-quark must interact further with the remnant to get the PSM quantum numbers. In case of VM the di-quark directly forms the meson



Lund/Artru

- Di-quark has q.n. of vacuum
- **Struck quark** joins the anti-quark in the final state → **favored fragment.**

Prediction: the $|2, \pm 2\rangle$ partial wave of the Collins funct. for SIDIS VM production have the opposite sign as the respective PS Collins function



Gluon radiation

- Di-quark has q.n. of observed final state
- **Produced quark** joins the anti-quark in the final state → **disfavored fragment.**

Prediction: the disfavored $|2, \pm 2\rangle$ Collins frag. also is expected to have opposite sign as the respective PS Collins function.

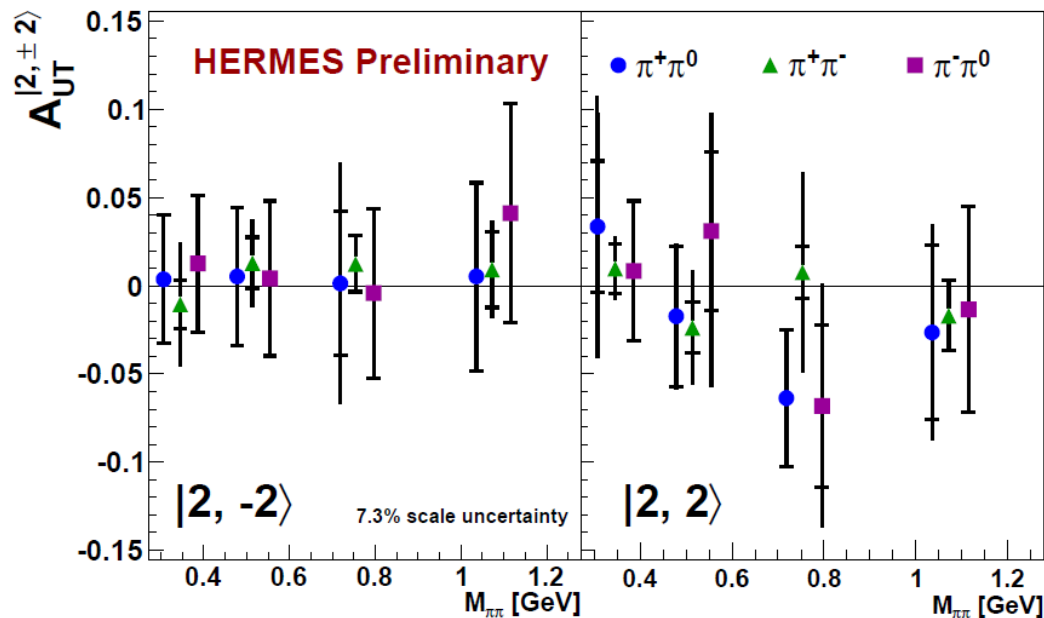
⇒ { Models predict: fav = disfav for VM
Data say: fav \cong - disfav for PSM (Collins π^+ vs. π^-)

...and now let's look at the results

	Fragment. process	Fav/disfav	Deflection	Sign of amplitude	
u dominance	$u \rightarrow \pi^+$	fav PSM	left ($\phi_h \rightarrow 0$)	> 0 (Collins π^+)	from data
	$u \rightarrow \pi^-$	disfav PSM	right ($\phi_h \rightarrow \pi$)	< 0 (Collins π^-)	
	$u \rightarrow \rho^+ \rightarrow \pi^+\pi^0$	fav VM	right ($\phi_h \rightarrow \pi$)	< 0	from models
	$u \rightarrow \rho^- \rightarrow \pi^-\pi^0$	disfav VM	right ($\phi_h \rightarrow \pi$)	< 0	
	$u \rightarrow \rho^0 \rightarrow \pi^+\pi^-$	mixed VM	right ($\phi_h \rightarrow \pi$)	0 or < 0	

...and now let's look at the results

	Fragment. process	Fav/disfav	Deflection	Sign of amplitude	
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	$u \rightarrow \pi^-$	disfav PSM	right ($\phi_h \rightarrow \pi$)	< 0 (Collins π^-)	
	$u \rightarrow \rho^+ \rightarrow \pi^+\pi^0$	fav VM	right ($\phi_h \rightarrow \pi$)	< 0	from models
	$u \rightarrow \rho^- \rightarrow \pi^-\pi^0$	disfav VM	right ($\phi_h \rightarrow \pi$)	< 0	
	$u \rightarrow \rho^0 \rightarrow \pi^+\pi^-$	mixed VM	right ($\phi_h \rightarrow \pi$)	0 or < 0	



$[2, -2]$ consistent with zero for all flavors
 Not in contradiction with models: if the transversity function causes the fragmenting quark to have positive polarization than Collins $[2, -2]$ must be zero as this partial wave requires fragmenting quark with negative polarization

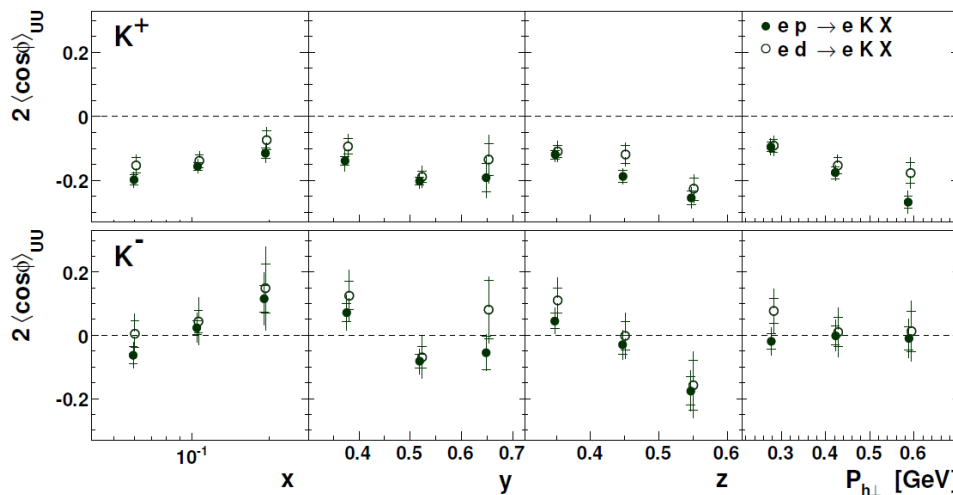
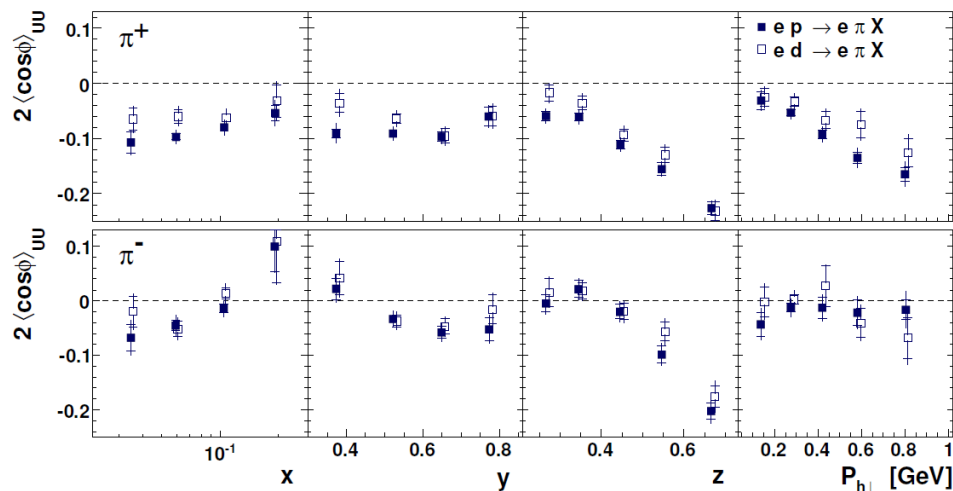
$[2, +2]$ consistent with model expect:

- No signal outside ρ -mass bin
 \rightarrow no non-resonant pion-pairs in p-wave
- Negative for ρ^\pm (model predictions)
- very small for ρ^0 (consistent with small Collins π^0)

Back-up

The $\cos\phi$ amplitudes

A. Airapetian et al, Phys. Rev. D 87 (2013) 012010



Analysis multi-dimensional in x , y , z , and P_t

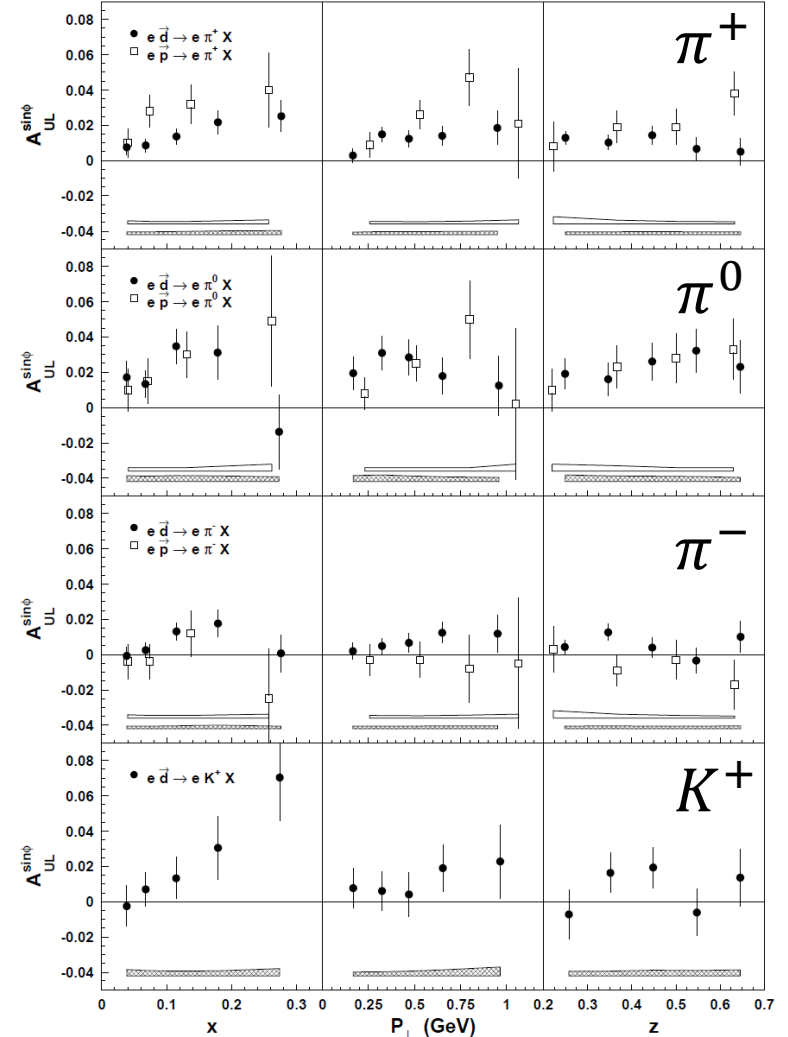
Create your own projections of results through: <http://www-hermes.desy.de/cosnphi/>

$F_{UL} \sin \phi$

$$F_{UL}^{\sin \phi_h} = \frac{2M}{Q} c \left[-\frac{\hat{h} \cdot \mathbf{k}_T}{M_h} \left(x h_L H_1^\perp + \frac{M_h}{M} g_{1L} \frac{\tilde{G}^\perp}{z} \right) + \frac{\hat{h} \cdot \mathbf{p}_T}{M} \left(x f_L^\perp D_1 - \frac{M_h}{M} h_{1L}^\perp \frac{\tilde{H}}{z} \right) \right]$$

$$\frac{d\sigma^h}{dx dy d\phi_S dz d\phi d\mathbf{P}_{h\perp}^2} = \frac{\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x} \right) \left\{ \begin{aligned} & \left[F_{UU,T} + \epsilon F_{UU,L} \right. \\ & \left. + \sqrt{2\epsilon(1+\epsilon)} \cos(\phi) F_{UU}^{\cos(\phi)} + \epsilon \cos(2\phi) F_{UU}^{\cos(2\phi)} \right] \\ & + \lambda_l \left[\sqrt{2\epsilon(1-\epsilon)} \sin(\phi) F_{LU}^{\sin(\phi)} \right] \\ & + S_L \left[\sqrt{2\epsilon(1+\epsilon)} \sin(\phi) F_{UL}^{\sin(\phi)} + \epsilon \sin(2\phi) F_{UL}^{\sin(2\phi)} \right] \\ & + S_L \lambda_l \left[\sqrt{1-\epsilon^2} F_{LL} + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi) F_{LL}^{\cos(\phi)} \right] \\ & + S_T \left[\sin(\phi - \phi_S) \left(F_{UT,T}^{\sin(\phi-\phi_S)} + \epsilon F_{UT,L}^{\sin(\phi-\phi_S)} \right) \right. \\ & + \epsilon \sin(\phi + \phi_S) F_{UT}^{\sin(\phi+\phi_S)} + \epsilon \sin(3\phi - \phi_S) F_{UT}^{\sin(3\phi-\phi_S)} \\ & + \sqrt{2\epsilon(1+\epsilon)} \sin(\phi_S) F_{UT}^{\sin(\phi_S)} \\ & \left. + \sqrt{2\epsilon(1+\epsilon)} \sin(2\phi - \phi_S) F_{UT}^{\sin(2\phi-\phi_S)} \right] \\ & + S_T \lambda_l \left[\sqrt{1-\epsilon^2} \cos(\phi - \phi_S) F_{LT}^{\cos(\phi-\phi_S)} \right. \\ & + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi_S) F_{LT}^{\cos(\phi_S)} \\ & \left. + \sqrt{2\epsilon(1-\epsilon)} \cos(2\phi - \phi_S) F_{LT}^{\cos(2\phi-\phi_S)} \right] \end{aligned} \right\}$$

A. Airapetian et al, Phys. Lett. B562 (2003)



Worm-gear h_{1L}^\perp

$$\frac{d\sigma^h}{dx dy d\phi_S dz d\phi d\mathbf{P}_{h\perp}^2} = \frac{\alpha^2 y^2}{xyQ^2 2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x} \right)$$

$$\left\{ \begin{aligned} & \left[F_{UU,T} + \epsilon F_{UU,L} \right. \\ & \left. + \sqrt{2\epsilon(1+\epsilon)} \cos(\phi) F_{UU}^{\cos(\phi)} + \epsilon \cos(2\phi) F_{UU}^{\cos(2\phi)} \right] \end{aligned} \right.$$

$$+ \lambda_l \left[\sqrt{2\epsilon(1-\epsilon)} \sin(\phi) F_{LU}^{\sin(\phi)} \right]$$

$$+ S_L \left[\sqrt{2\epsilon(1+\epsilon)} \sin(\phi) F_{UL}^{\sin(\phi)} + \epsilon \sin(2\phi) F_{UL}^{\sin(2\phi)} \right]$$

$$+ S_L \lambda_l \left[\sqrt{1-\epsilon^2} F_{LL} + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi) F_{LL}^{\cos(\phi)} \right]$$

$$+ S_T \left[\begin{aligned} & \sin(\phi - \phi_S) \left(F_{UT,T}^{\sin(\phi-\phi_S)} + \epsilon F_{UT,L}^{\sin(\phi-\phi_S)} \right) \\ & + \epsilon \sin(\phi + \phi_S) F_{UT}^{\sin(\phi+\phi_S)} + \epsilon \sin(3\phi - \phi_S) F_{UT}^{\sin(3\phi-\phi_S)} \\ & + \sqrt{2\epsilon(1+\epsilon)} \sin(\phi_S) F_{UT}^{\sin(\phi_S)} \\ & + \sqrt{2\epsilon(1+\epsilon)} \sin(2\phi - \phi_S) F_{UT}^{\sin(2\phi-\phi_S)} \end{aligned} \right]$$

$$+ S_T \lambda_l \left\{ \begin{aligned} & \left[\sqrt{1-\epsilon^2} \cos(\phi - \phi_S) F_{LT}^{\cos(\phi-\phi_S)} \right. \\ & + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi_S) F_{LT}^{\cos(\phi_S)} \\ & \left. + \sqrt{2\epsilon(1-\epsilon)} \cos(2\phi - \phi_S) F_{LT}^{\cos(2\phi-\phi_S)} \right] \end{aligned} \right\}$$

$$F_{UL}^{\sin 2\phi_h} = C \left[-\frac{2(\hat{h} \cdot \mathbf{k}_T)(\hat{h} \cdot \mathbf{p}_T) - \mathbf{k}_T \cdot \mathbf{p}_T}{MM_h} h_{1L}^\perp H_1^\perp \right]$$

Describes the probability to find transversely polarized quarks in a longitudinally polarized nucleon

Distribution Functions

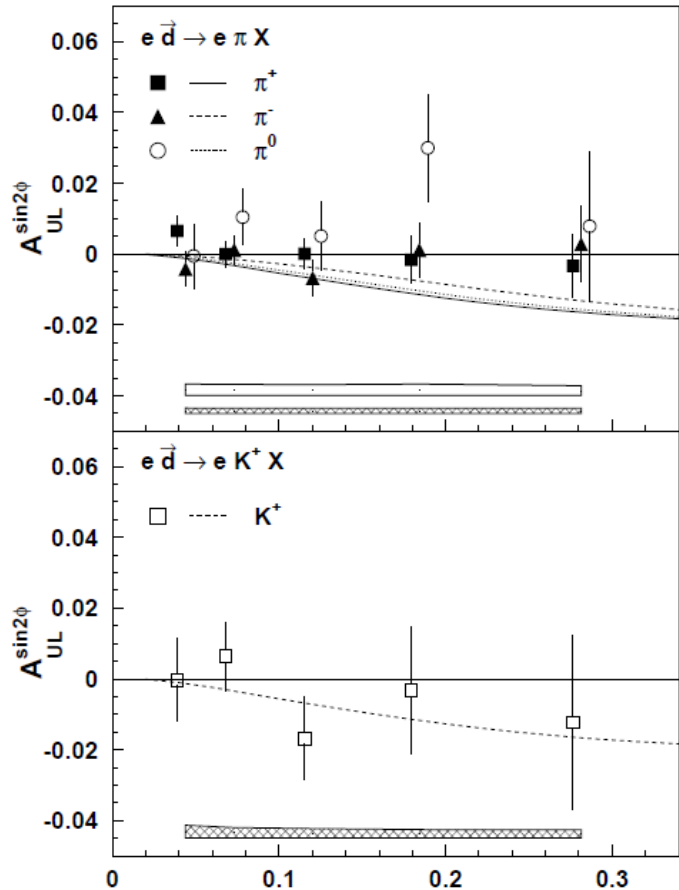
		quark		
		U	L	T
nucleon	U	f_1		h_1^\perp
	L		g_1	h_{1L}^\perp
	T	f_{1T}^\perp	g_{1T}^\perp	h_{1T}^\perp

Fragmentation Functions

		quark		
		U	L	T
h	U	D_1		H_1^\perp

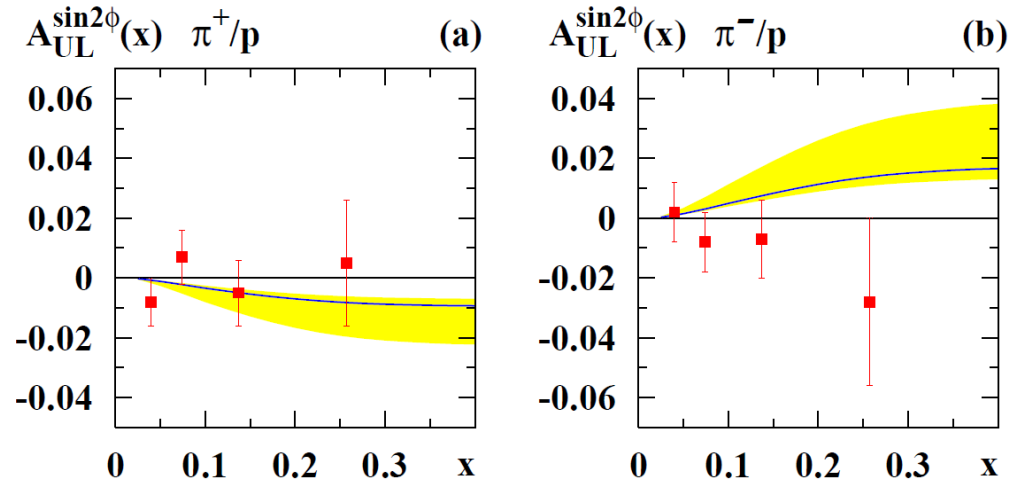
The $\sin(2\phi)$ amplitude $\propto h_{1L}^\perp(x, p_T^2) \otimes H_1^\perp(z, k_T^2)$

Deuterium target



A. Airapetian et al, *Phys. Lett. B* 562 (2003)

Hydrogen target



A. Airapetian et al, *Phys. Rev. Lett.* 84 (2000)

Amplitudes consistent with zero for all mesons and for both H and D targets

Pretzelosity

$$F_{UT}^{\sin(3\phi_h - \phi_S)} = C \left[\frac{2(\hat{h} \cdot p_T)(p_T \cdot k_T) + p_T^2(\hat{h} \cdot k_T) - 4(\hat{h} \cdot p_T)^2(\hat{h} \cdot k_T)}{2M^2 M_h} h_{1T}^\perp H_1^\perp \right]$$

$$\frac{d\sigma^h}{dx dy d\phi_S dz d\phi dP_{h\perp}^2} = \frac{\alpha^2 y^2}{xyQ^2 2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x} \right) \left\{ \begin{aligned} & \left[F_{UU,T} + \epsilon F_{UU,L} \right. \\ & \quad \left. + \sqrt{2\epsilon(1+\epsilon)} \cos(\phi) F_{UU}^{\cos(\phi)} + \epsilon \cos(2\phi) F_{UU}^{\cos(2\phi)} \right] \\ & + \lambda_L \left[\sqrt{2\epsilon(1-\epsilon)} \sin(\phi) F_{LU}^{\sin(\phi)} \right] \\ & + S_L \left[\sqrt{2\epsilon(1+\epsilon)} \sin(\phi) F_{UL}^{\sin(\phi)} + \epsilon \sin(2\phi) F_{UL}^{\sin(2\phi)} \right] \\ & + S_L \lambda_L \left[\sqrt{1-\epsilon^2} F_{LL} + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi) F_{LL}^{\cos(\phi)} \right] \\ & + S_T \left[\sin(\phi - \phi_S) \left(F_{UT,T}^{\sin(\phi - \phi_S)} + \epsilon F_{UT,L}^{\sin(\phi - \phi_S)} \right) \right. \\ & \quad + \epsilon \sin(\phi + \phi_S) F_{UT}^{\sin(\phi + \phi_S)} + \epsilon \sin(3\phi - \phi_S) F_{UT}^{\sin(3\phi - \phi_S)} \\ & \quad + \sqrt{2\epsilon(1+\epsilon)} \sin(\phi_S) F_{UT}^{\sin(\phi_S)} \\ & \quad \left. + \sqrt{2\epsilon(1+\epsilon)} \sin(2\phi - \phi_S) F_{UT}^{\sin(2\phi - \phi_S)} \right] \\ & + S_T \lambda_L \left[\sqrt{1-\epsilon^2} \cos(\phi - \phi_S) F_{LT}^{\cos(\phi - \phi_S)} \right. \\ & \quad + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi_S) F_{LT}^{\cos(\phi_S)} \\ & \quad \left. + \sqrt{2\epsilon(1-\epsilon)} \cos(2\phi - \phi_S) F_{LT}^{\cos(2\phi - \phi_S)} \right] \end{aligned} \right\}$$

Describes correlation between quark transverse momentum and transverse spin in a transversely pol. nucleon

➤ Sensitive to **non-spherical shape** of the nucleon

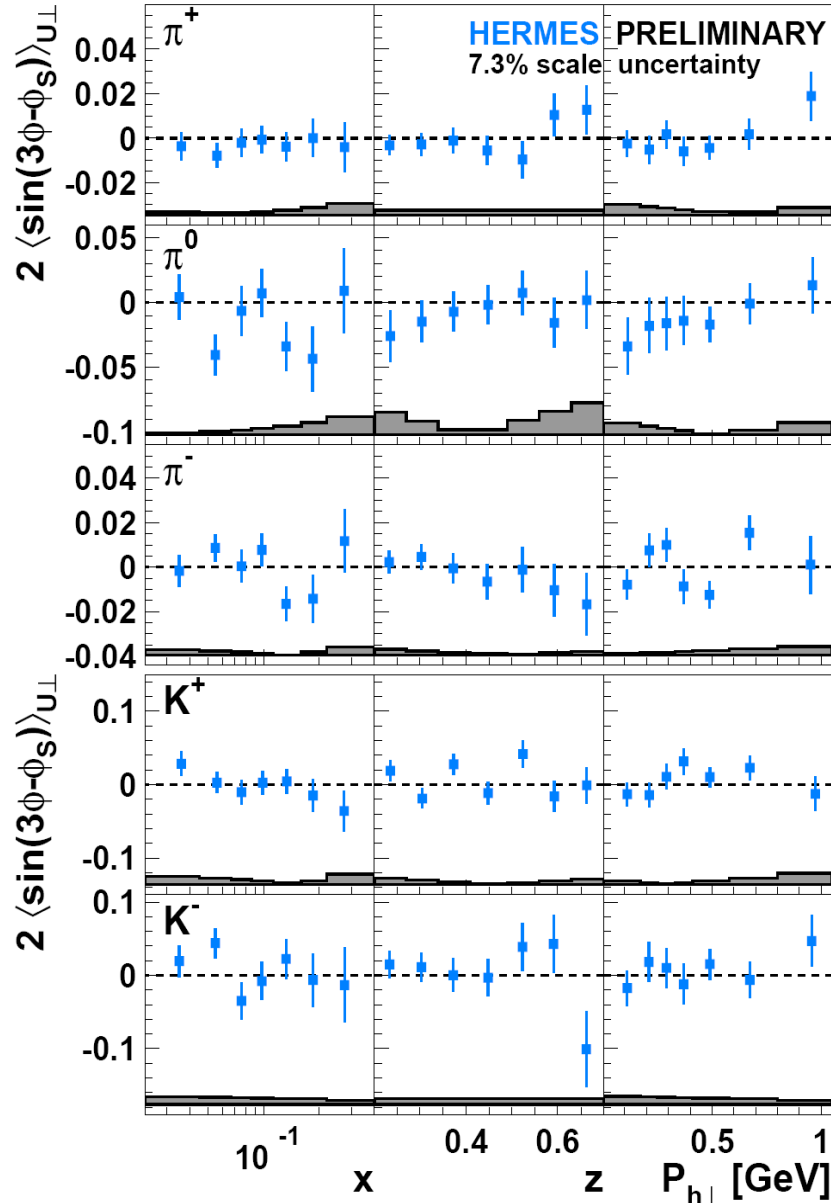
Distribution Functions

		quark		
		U	L	T
nucleon	U	f_1		h_1^\perp
	L		g_1	h_{1L}^\perp
	T	f_{1T}^\perp	g_{1T}^\perp	h_1 h_{1T}^\perp

Fragmentation Functions

		quark		
		U	L	T
h	U	D_1		H_1^\perp

The $\sin(3\phi - \phi_s)$ amplitude $\propto h_{1T}^\perp(x, p_T^2) \otimes H_1^\perp(z, k_T^2)$

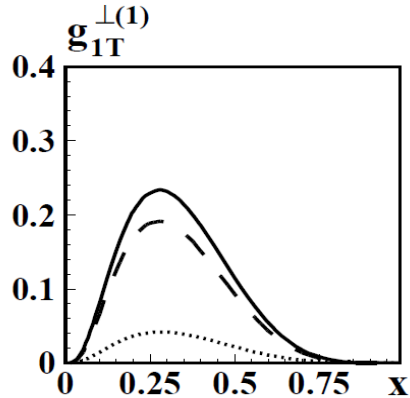


All amplitudes consistent with zero

...suppressed by two powers of $P_{h\perp}$
w.r.t. Collins and Sivers amplitudes

The worm-gear g_{1T}^\perp

- The only TMD that is both **chiral-even** and **naïve-T-even**
- requires interference between wave funct. components that differ by 1 unit of OAM



S. Boffi et al. (2009)
 Phys. Rev. D 79 094012
Light cone constituent quark model
 flavorless
 dashed line: interf. L=0, L=1
 dotted line: interf L=1, L=2

		quark		
		U	L	T
n u c l e o n	U	f_1		h_1^\perp
	L		g_1	h_{1L}^\perp
	T	f_{1T}^\perp	g_{1T}^\perp	h_{1T}^\perp

⇒ related to quark orbital motion inside nucleons

- Many models support simple relations among g_{1T}^\perp and other TMDs:

- $g_{1T}^q = -h_{1L}^{\perp q}$ (also supported by Lattice QCD and first data)

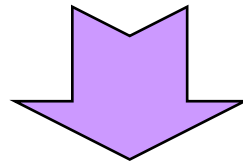
- $g_{1T}^{q(1)}(x) \stackrel{WW\text{-type}}{\approx} x \int_x^1 \frac{dy}{y} g_1^q(y)$ (Wandzura-Wilczek appr.)

Probing g_{1T}^\perp through Double Spin Asymmetries

$$F_{LT}^{\cos(\phi_h - \phi_s)} = c \left[\frac{\hat{h} \cdot \mathbf{p}_T}{M} g_{1T} D_1 \right]$$

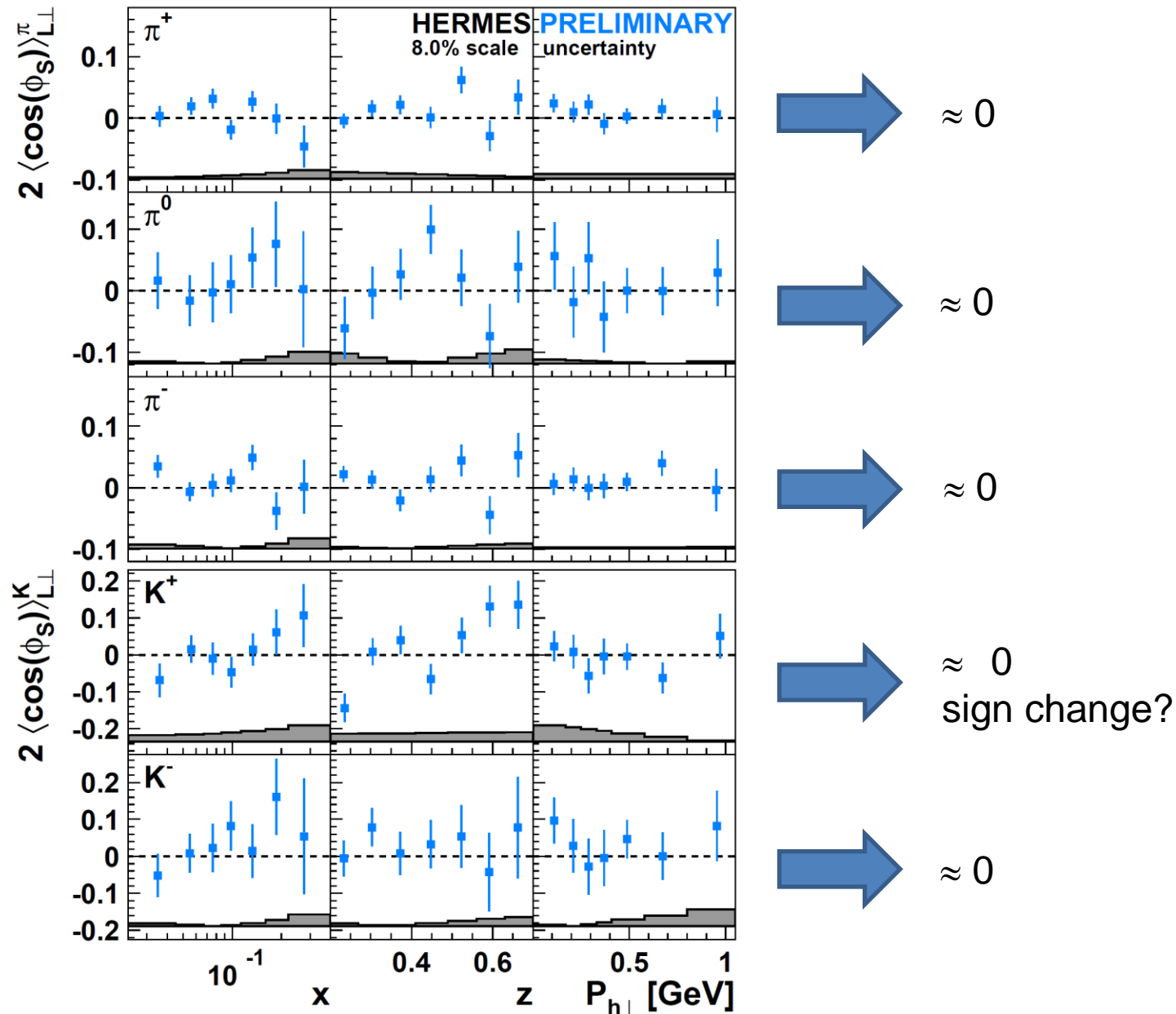
$$F_{LT}^{\cos \phi_s} = \frac{2M}{Q} c \left\{ - \left(x g_T D_1 + \frac{M_h}{M} h_1 \frac{\tilde{E}}{z} \right) + \frac{\mathbf{k}_T \cdot \mathbf{p}_T}{2MM_h} \left[\left(x e_T H_1^\perp - \frac{M_h}{M} g_{1T} \frac{\tilde{D}^\perp}{z} \right) + \left(x e_T^\perp H_1^\perp + \frac{M_h}{M} f_{1T}^\perp \frac{\tilde{G}^\perp}{z} \right) \right] \right\}$$

$$F_{LT}^{\cos(2\phi_h - \phi_s)} = \frac{2M}{Q} c \left\{ - \frac{2(\hat{h} \cdot \mathbf{p}_T)^2 - \mathbf{p}_T^2}{2M^2} \left(x g_T^\perp D_1 + \frac{M_h}{M} h_{1T}^\perp \frac{\tilde{E}}{z} \right) + \frac{2(\hat{h} \cdot \mathbf{k}_T)(\hat{h} \cdot \mathbf{p}_T) - \mathbf{k}_T \cdot \mathbf{p}_T}{2MM_h} \left[\left(x e_T H_1^\perp - \frac{M_h}{M} g_{1T} \frac{\tilde{D}^\perp}{z} \right) - \left(x e_T^\perp H_1^\perp + \frac{M_h}{M} f_{1T}^\perp \frac{\tilde{G}^\perp}{z} \right) \right] \right\}$$

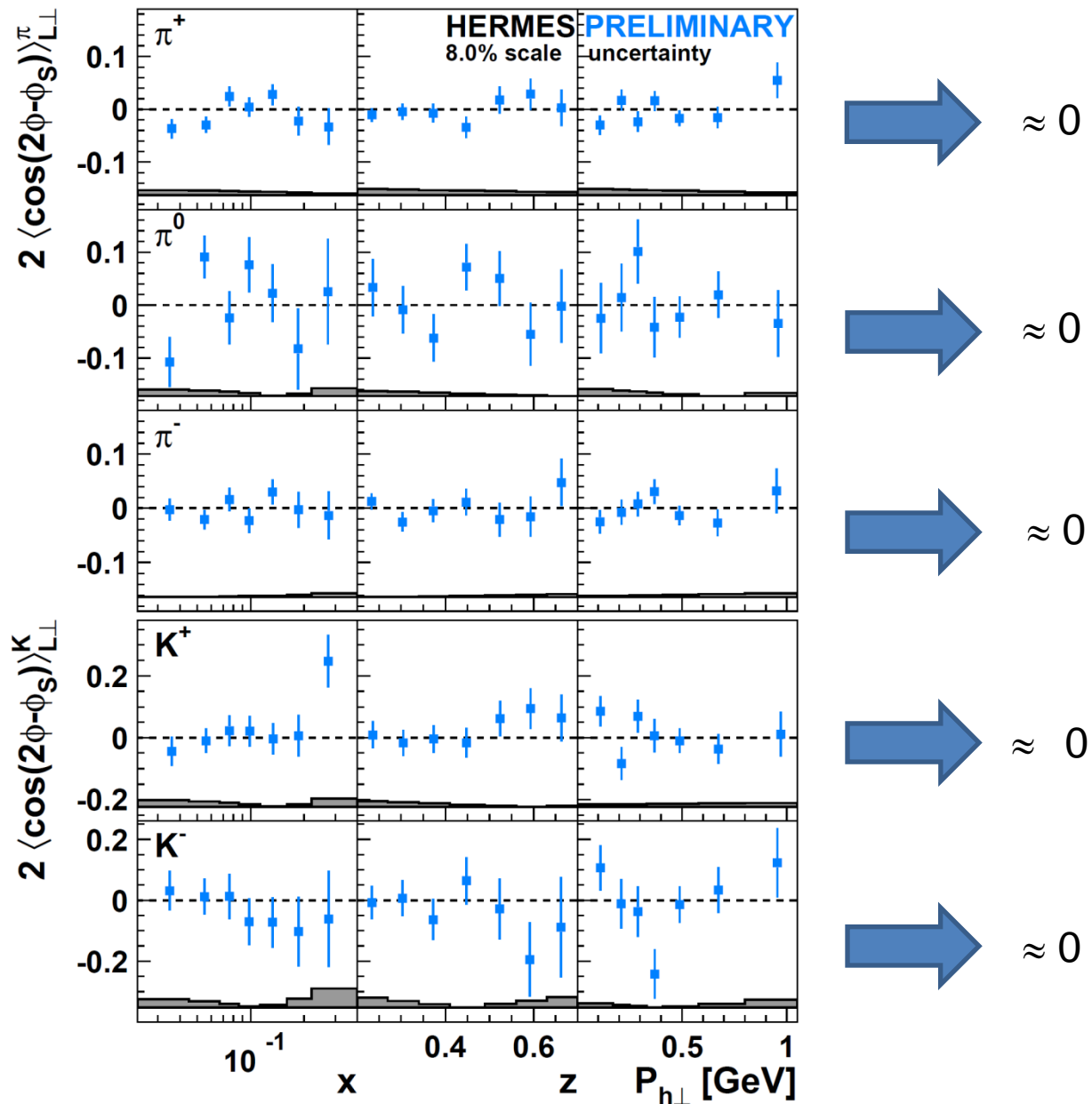


The simplest way to probe worm-gear g_{1T}^\perp is through the $\cos(\phi - \phi_s)$ Fourier component

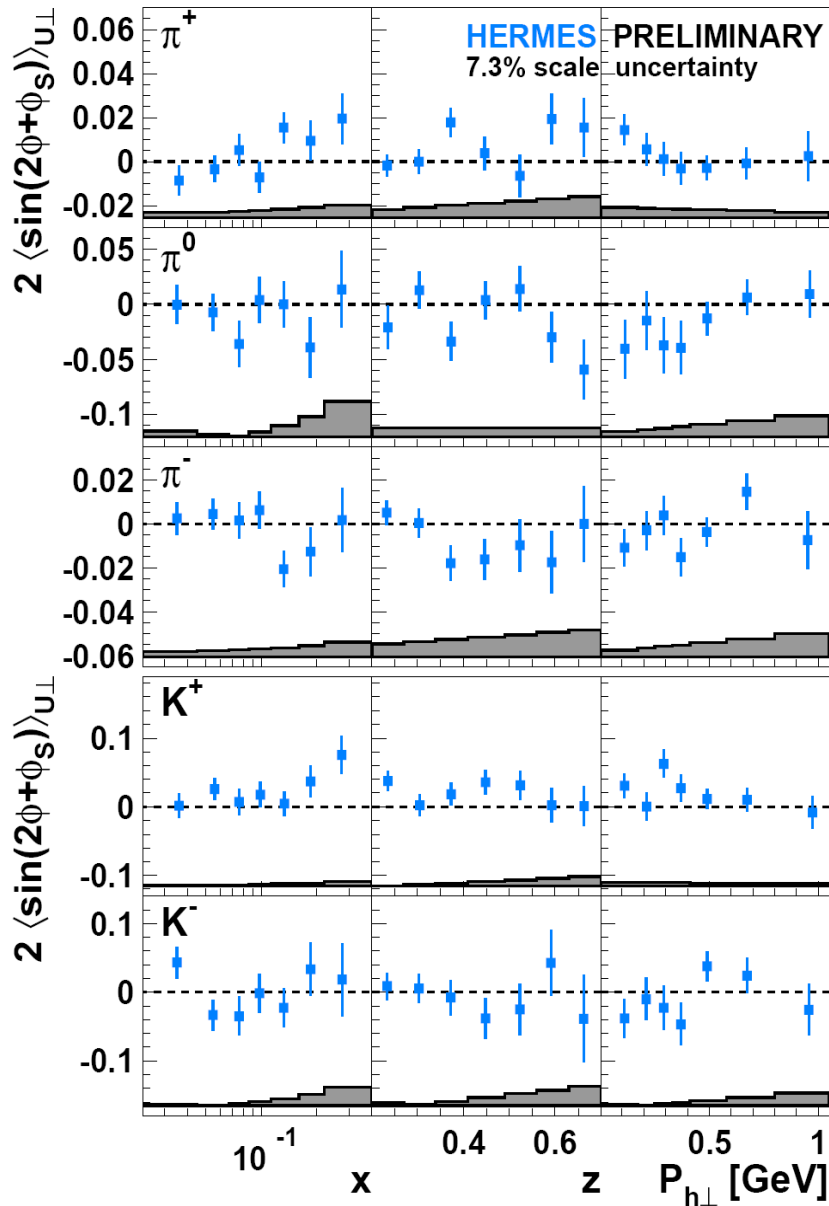
The $\cos(\phi_S)$ Fourier component



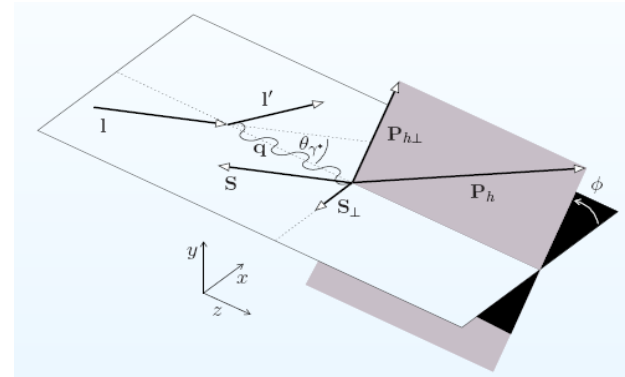
The $\cos(2\phi - \phi_S)$ Fourier component



The $\sin(2\phi + \phi_S)$ Fourier component



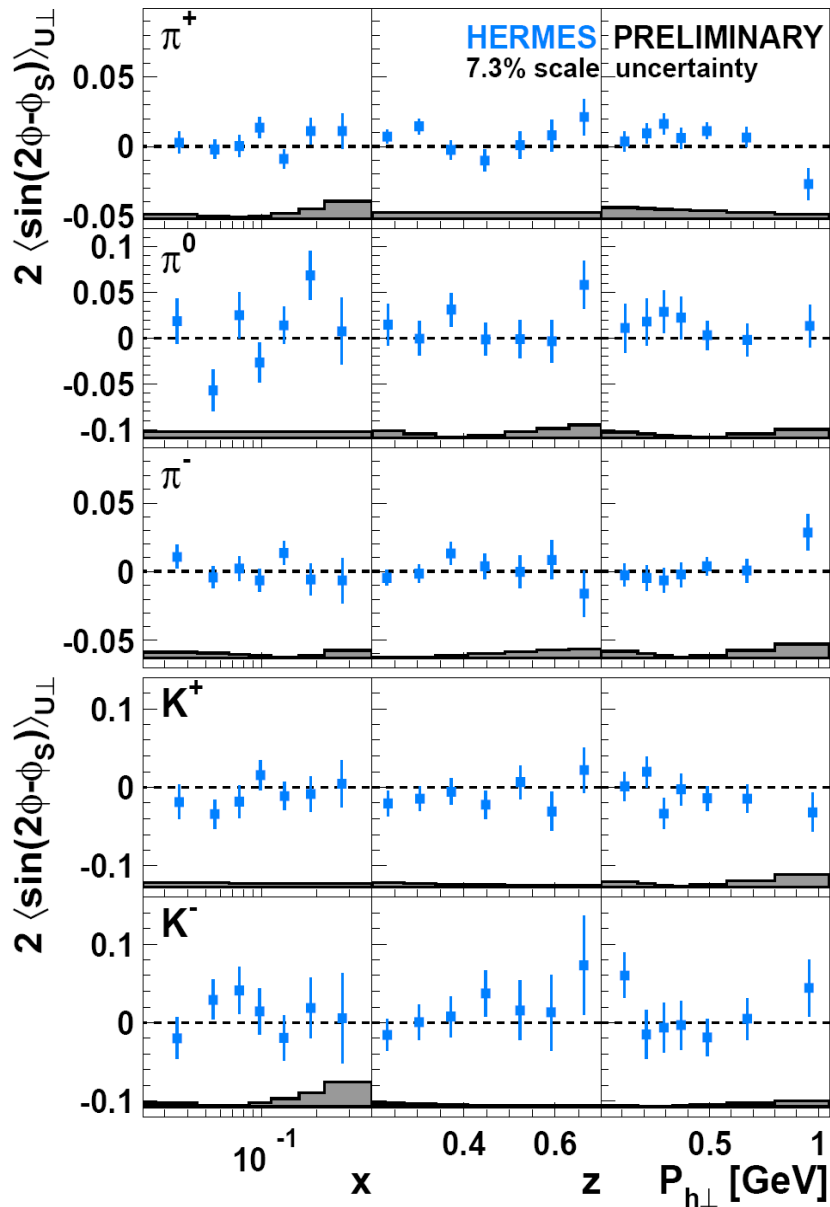
- arises solely from longitudinal (w.r.t. virtual photon direction) component of the target spin



- related to $\langle \sin(2\phi) \rangle_{UL}$ Fourier comp:

$$2 \langle \sin(2\phi + \phi_S) \rangle_{UT}^h \propto \frac{1}{2} \sin(\mathcal{G}_{l\gamma^*}) 2 \langle \sin(2\phi) \rangle_{UL}^h$$
- sensitive to **worm-gear** h_{1L}^\perp
- suppressed by one power of $P_{h\perp}$ w.r.t. Collins and Sivers amplitudes
- **no significant signal observed (except maybe for K+)**

The subleading-twist $\sin(2\phi-\phi_S)$ Fourier component



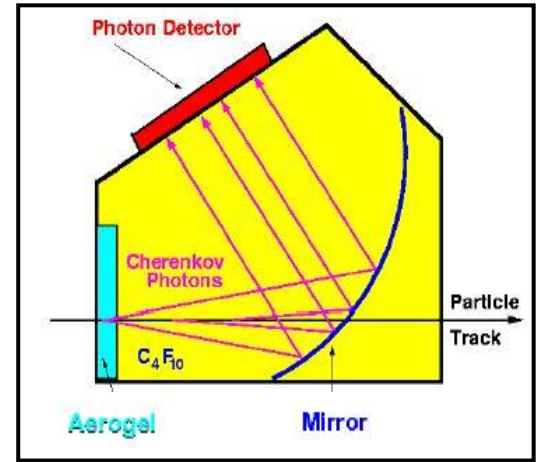
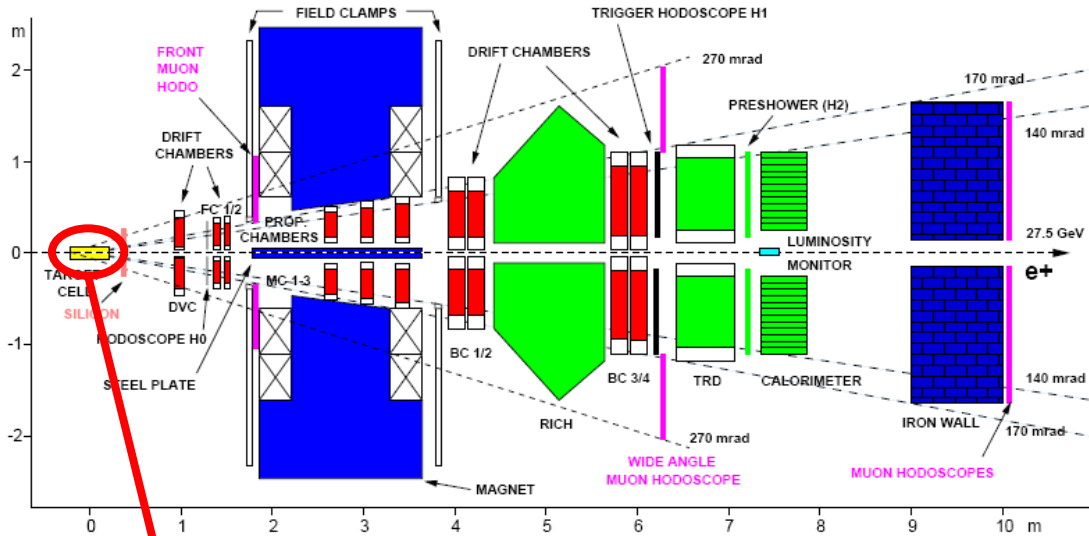
- sensitive to **worm-gear** g_{1T}^\perp , **Pretzelosity** and **Sivers function**:

$$\propto W_1(p_T, k_T, P_{h\perp}) \left(x f_T^\perp D_1 - \frac{M_h}{M} h_{1T}^\perp \frac{\tilde{H}}{z} \right) - W_2(p_T, k_T, P_{h\perp}) \left[\left(x h_T H_1^\perp + \frac{M_h}{M} g_{1T} \frac{\tilde{G}^\perp}{z} \right) + \left(x h_T^\perp H_1^\perp - \frac{M_h}{M} f_{1T}^\perp \frac{\tilde{D}^\perp}{z} \right) \right]$$

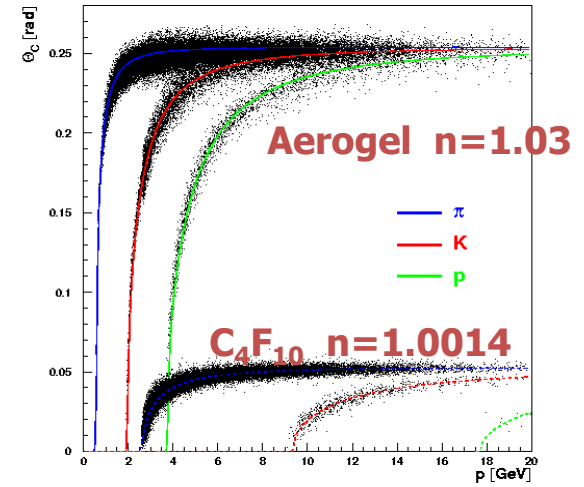
- suppressed by one power of $P_{h\perp}$ w.r.t. Collins and Sivers amplitudes

- **no significant non-zero signal observed**

The HERMES experiment at HERA

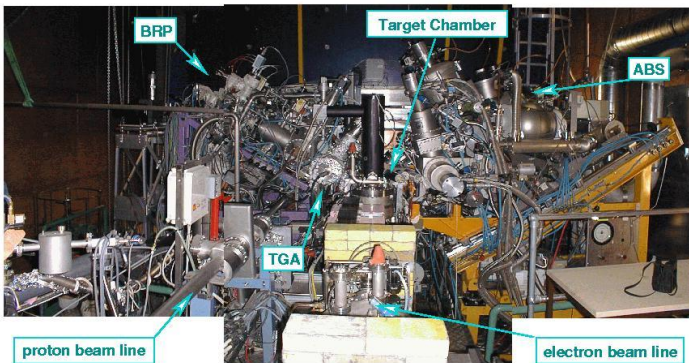
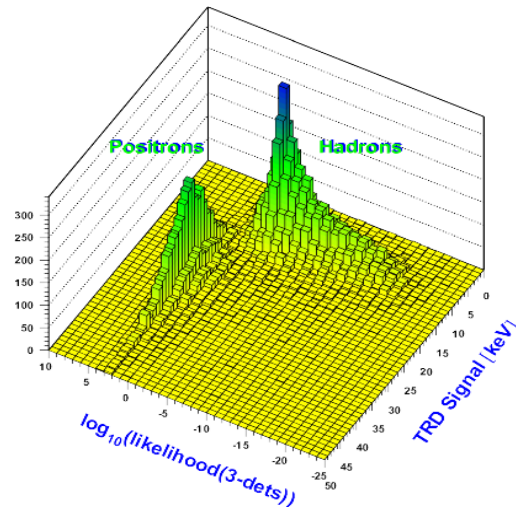


hadron separation

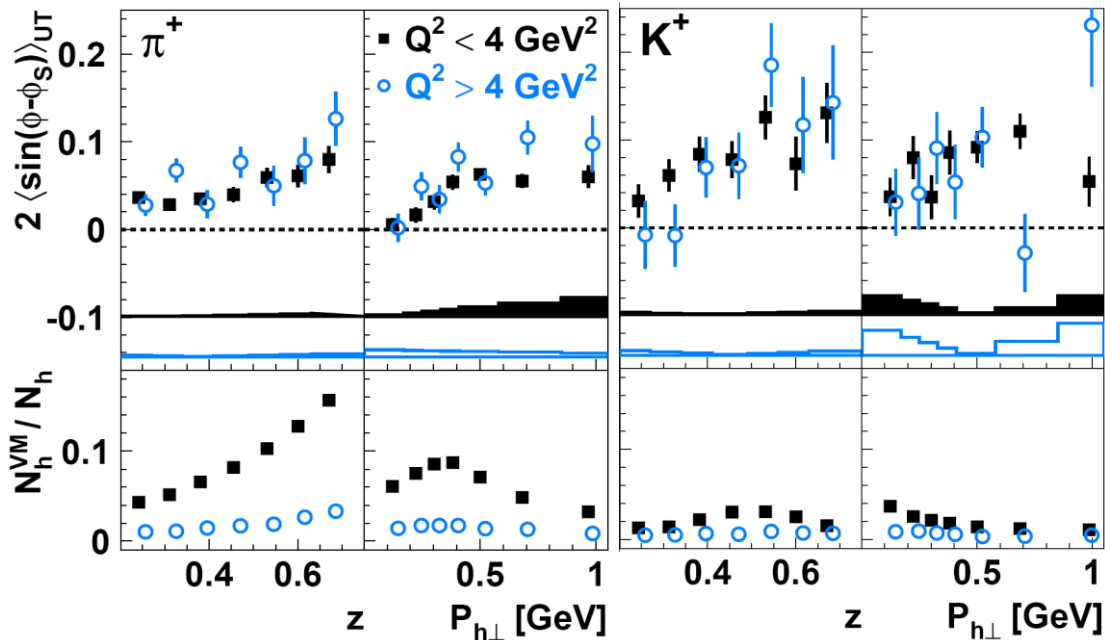


$\pi \sim 98\%$, $K \sim 88\%$, $P \sim 85\%$

TRD, Calorimeter,
preshower, RICH:
lepton-hadron > 98%



Siver amplitudes: additional studies

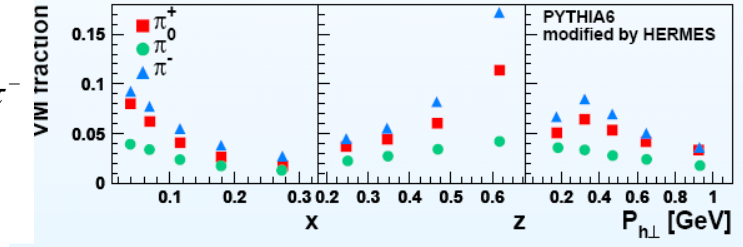
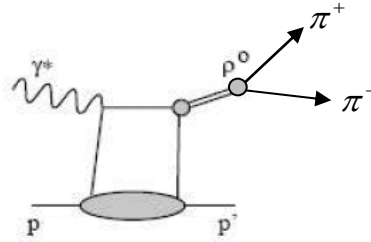


No systematic shifts observed between high and low Q^2 amplitudes for both π^+ and K^+

No indication of important contributions from exclusive VM

The pion-difference asymmetry

Contribution by decay of exclusively produced vector mesons (ρ^0, ω, ϕ) is not negligible (6-7% for pions and 2-3% for kaons), though substantially limited by the requirement $z < 0.7$.

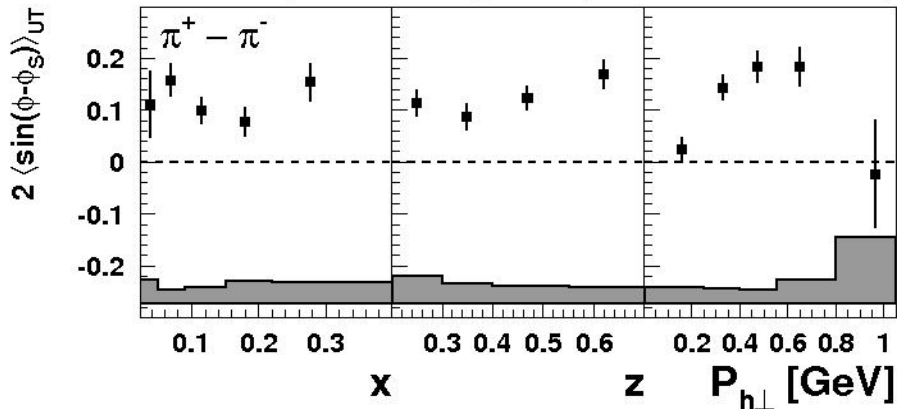


a new observable

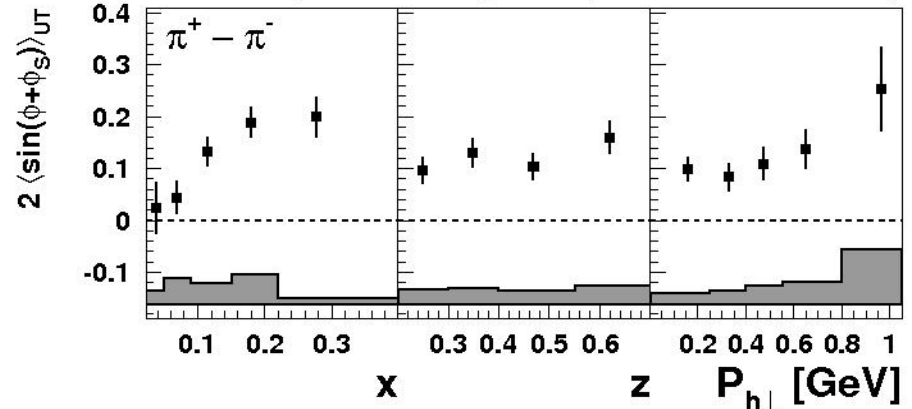
$$A_{UT}^{\pi^+ - \pi^-}(\phi, \phi_S) \equiv \frac{1}{P_T} \frac{(\sigma_{U\uparrow}^{\pi^+} - \sigma_{U\uparrow}^{\pi^-}) - (\sigma_{U\downarrow}^{\pi^+} - \sigma_{U\downarrow}^{\pi^-})}{(\sigma_{U\uparrow}^{\pi^+} - \sigma_{U\uparrow}^{\pi^-}) + (\sigma_{U\downarrow}^{\pi^+} - \sigma_{U\downarrow}^{\pi^-})}$$

Contribution from exclusive ρ^0 largely cancels out!

HERMES PRELIMINARY 2002-2005
lepton beam amplitudes, 8.1% scale uncertainty



HERMES PRELIMINARY 2002-2005
lepton beam amplitudes, 8.1% scale uncertainty



- significantly positive Sivers and Collins amplitudes are obtained
- measured amplitudes are not generated by exclusive VM contribution