

Study of GPDs at HERMES

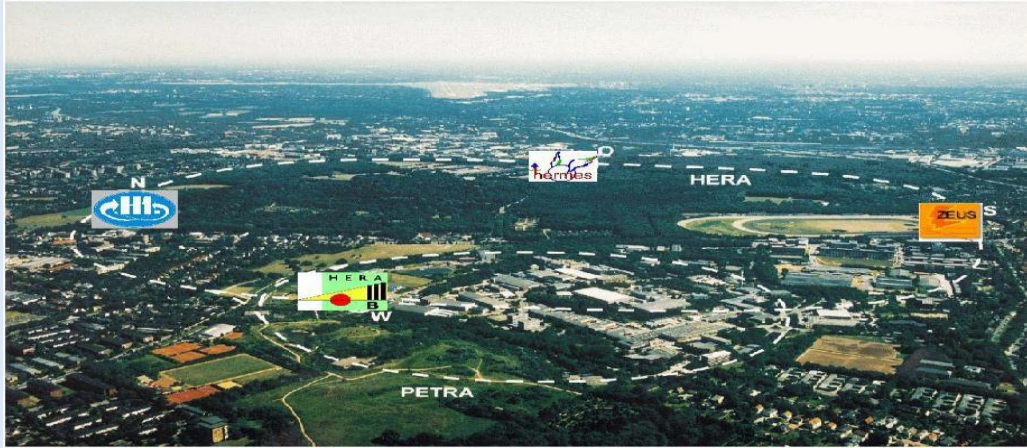
Hrachya Marukyan
AANL (Yerevan Physics Institute)
(on behalf of the HERMES Collaboration)

Correlations in Partonic and Hadronic Interactions 2020 (CPHI-20)
CERN, Geneva, Switzerland, Feb. 3-7, 2020

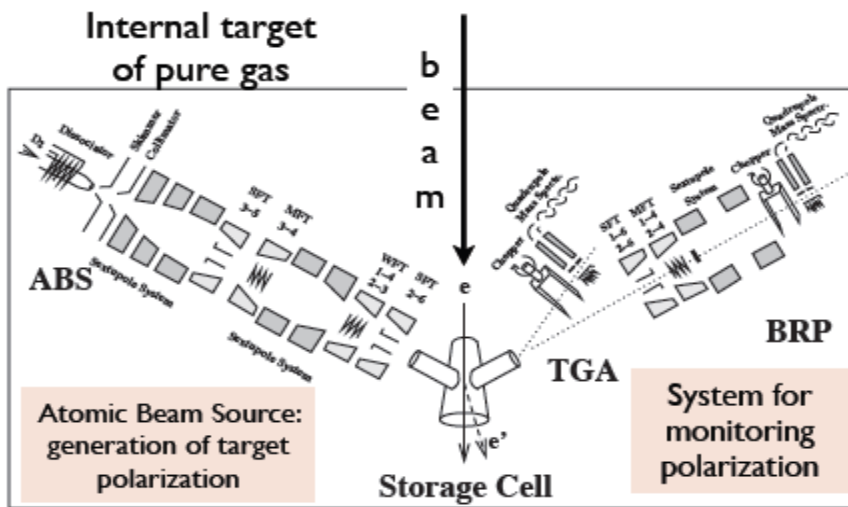
- HERMES experiment at HERA
- Exclusive reactions and GPDs
- DVCS: measurement of azimuthal asymmetries at HERMES
- Measurements of BSAs: use of Recoil Detector information
- Exclusive meson production and GPDs
- Summary



HERMES at DESY



Self-polarized e^+ and e^- beams
27.6 GeV
Helicity switched every few months

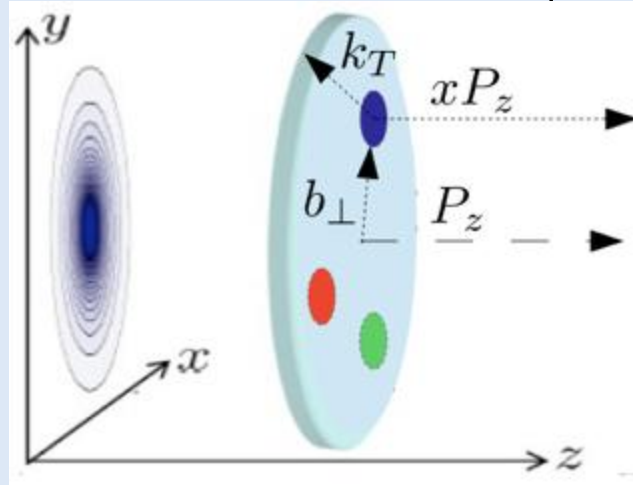


Polarized hydrogen (Long.,Trans.), deuterium (Long.)
Polarization flipped at 60-180 s time interval
Unpolarized *He,N,Ne,Kr,Xe*

3D picture of the nucleon

Wigner distributions $W(x, \vec{k}_T, \vec{b}_\perp)$

$$\int d^2 \vec{b}_\perp$$



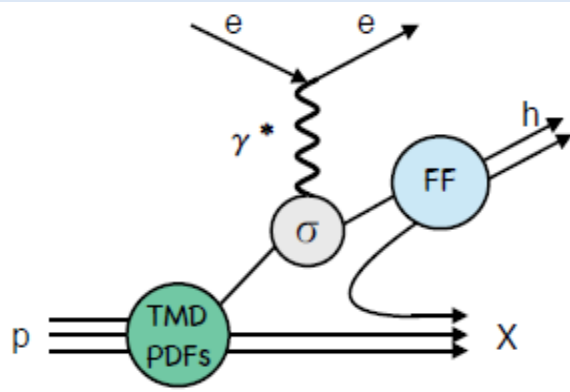
$$\int d^2 \vec{k}_T$$

TMD PDFs: $f_p^q(x, k_T), \dots$

GPDs: $H_p^q(x, \xi, t), \dots$

Semi-inclusive measurements
Direct info about momentum distribution

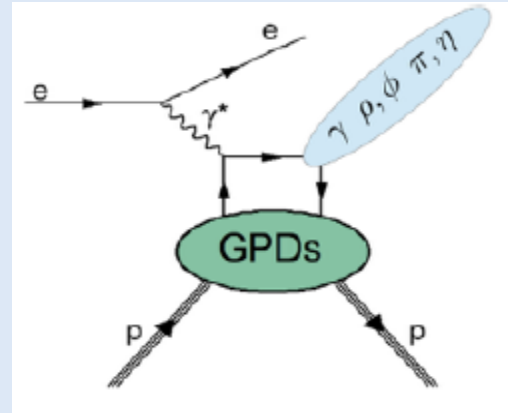
Exclusive Measurements
Direct info about spatial distribution



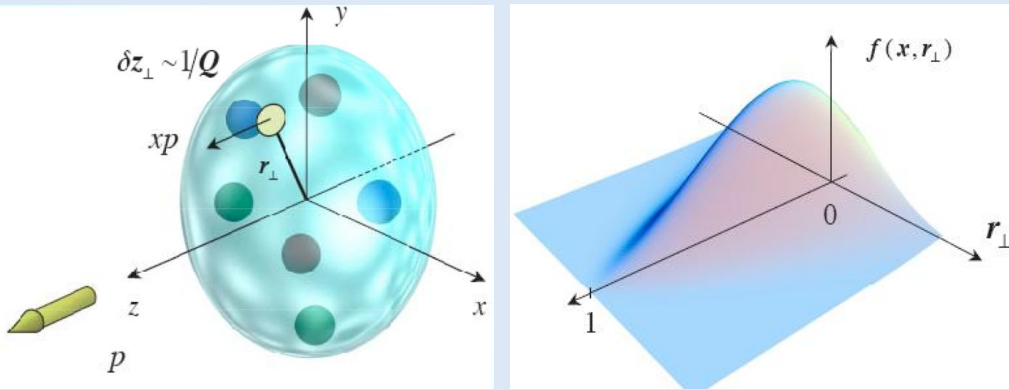
$$\int d^2 \vec{k}_T$$

$\xi=0, t=0$

PDFs $f_p^q(x), \dots$



Exclusive reactions & GPDs



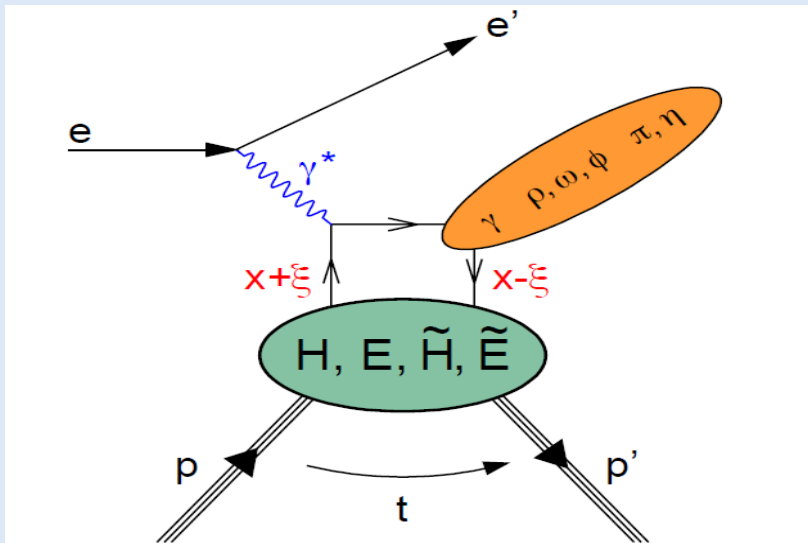
Correlated information about **longitudinal momentum xp** and **transverse spatial position r_{\perp}**

Ji sum rule \Rightarrow access OAM

$$J_q = \frac{1}{2} \lim_{t \rightarrow 0} \int dx x [H^q(x, \xi, t) + E^q(x, \xi, t)]$$

$$\frac{1}{2} = \frac{1}{2} \Delta \Sigma + L_q + J_q$$

H^q and E^q : quark **G**eneralized **P**arton **D**istributions (**GPDs**)



Spin-1/2 target: 4 chiral-even leading-twist quark **GPDs** $H, E, \tilde{H}, \tilde{E}$

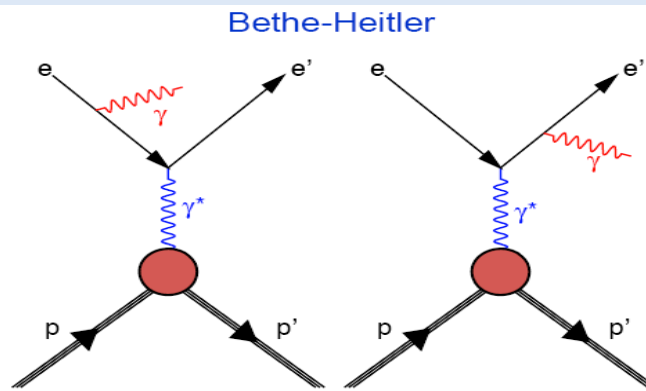
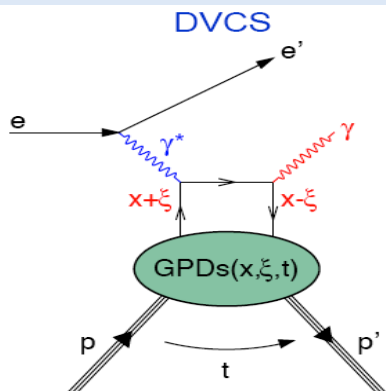
Final state sensitive to different **GPDs**

DVCS (γ) $H, E, \tilde{H}, \tilde{E}$

Vector mesons (ρ, ω, ϕ) $H, E,$

Pseudoscalar mesons (π, η) \tilde{H}, \tilde{E}

Deeply virtual Compton scattering & GPDs

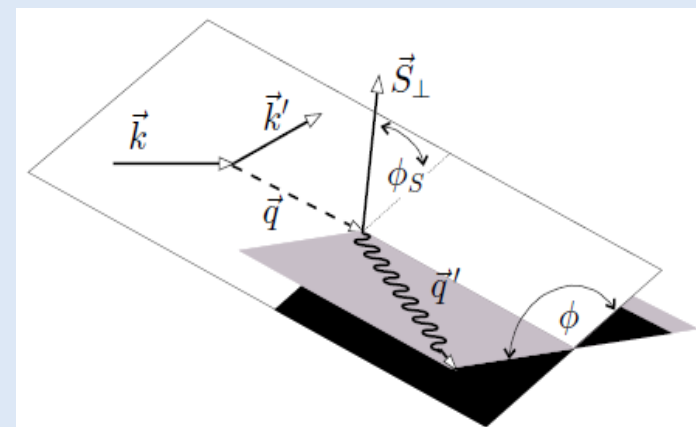
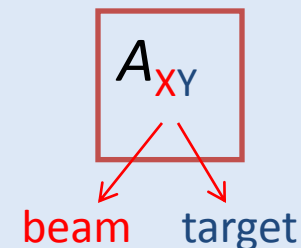


- Theoretically cleanest way to access **GPDs**
- Interference between **DVCS** and **Bethe-Heitler** amplitude
- $|\tau_{\text{DVCS}}| \ll |\tau_{\text{BH}}|$ at **HERMES**

Access to GPD combinations through azimuthal asymmetries

HERMES: Complete set of asymmetries

- Both **beam charges**
- Both **beam helicities**
- Unpolarized ^1H , ^2H , and **also nuclear** targets
- **Longitudinally polarized** ^1H and ^2H targets
- **Transversely polarized** ^1H target
- **Recoil detector**: unpolarized ^1H and ^2H



- **Beam-Charge Asymmetry**

$$\sigma(e^+, \phi) - \sigma(e^-, \phi) \propto \Re[F_1 \mathcal{H}]$$

- **Beam-Spin Asymmetry**

$$\sigma(\vec{e}, \phi) - \sigma(\vec{e}, \phi) \propto \Im[F_1 \mathcal{H}]$$

- **Longitudinal Target-Spin Asymmetry**

$$\sigma(\vec{P}, \phi) - \sigma(\vec{P}, \phi) \propto \Im[F_1 \tilde{\mathcal{H}}]$$

- **Longitudinal Double-Spin Asymmetry**

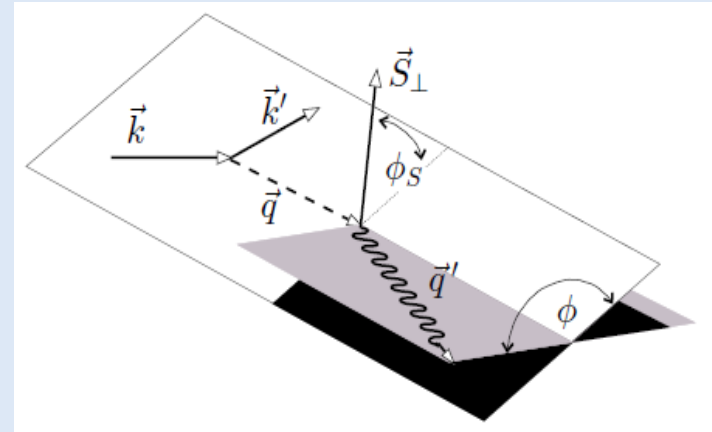
$$\sigma(\vec{P}, \vec{e}, \phi) - \sigma(\vec{P}, \vec{e}, \phi) \propto \Re[F_1 \tilde{\mathcal{H}}]$$

- **Transverse Target-Spin Asymmetry**

$$\sigma(\phi, \phi_S) - \sigma(\phi, \phi_S + \pi) \propto \Im[F_2 \mathcal{H} - F_1 \mathcal{E}]$$

- **Transverse Double-Spin Asymmetry**

$$\sigma(\vec{e}, \phi, \phi_S) - \sigma(\vec{e}, \phi, \phi_S + \pi) \propto \Re[F_2 \mathcal{H} - F_1 \mathcal{E}]$$



Compton Form Factors: convolutions of **GPDs** with hard scattering kernels

$$F(\xi, t) = \sum_q \int_{-1}^1 dx C_q^\mp(\xi, x) F^q(x, \xi, t) \longrightarrow \text{GPD}$$

DVCS without recoil detector

- Event with exactly **one** DIS-lepton and exactly one trackless cluster in the calorimeter.
- No recoil detection \rightarrow Exclusivity via missing mass: $M_X^2 = (q + P - q')^2$

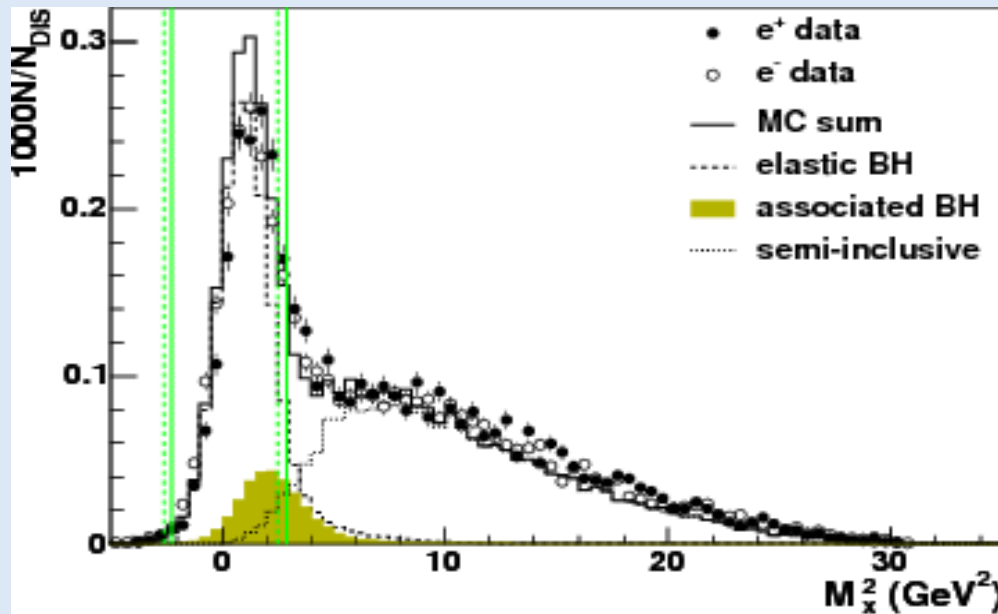
$$5 < \Theta_{\gamma^*\gamma} < 45 \text{ mrad}$$

$$-t < 0.7 \text{ GeV}^2, E_\gamma > 5 \text{ GeV}$$

$$0.03 < x_B < 0.35, 1 < Q^2 < 10 \text{ GeV}^2$$

$$W > 3 \text{ GeV}, \nu < 22 \text{ GeV}$$

MC for background and cuts,
systematic uncertainty



$$e p \rightarrow e' X \gamma$$

$e p \rightarrow e' p \gamma$; elastic BH

$e p \rightarrow e' \Delta^+ \gamma$; associated BH

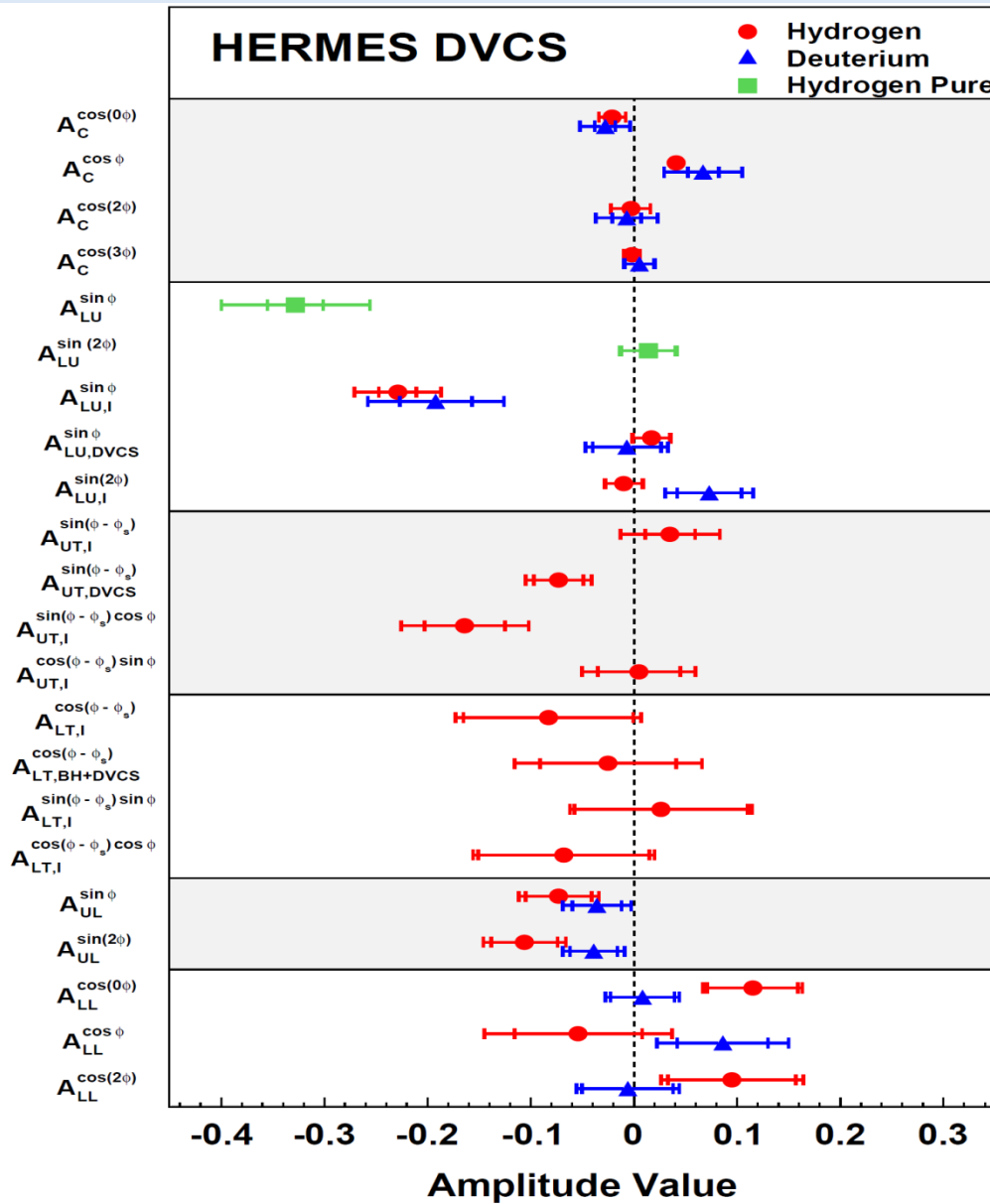
$e p \rightarrow e' \pi^0 X$; semi-inclusive

Correction; π^0 background ($\approx 3\%$)

Associated ($\approx 12\%$); **part of signal**

\rightarrow Exclusive bin ($-(1.5)^2 < M_X^2 < (1.7)^2 \text{ GeV}^2$)

DVCS asymmetries at HERMES



● Beam-charge asymmetry

GPD \tilde{H}

H: [PRL 87 \(2001\) 182001](#)

[PRD 75 \(2007\) 011103](#)

[JHEP 11 \(2009\) 083](#)

[JHEP 07 \(2012\) 032](#) [JHEP 10 \(2012\) 042](#)

D: [Nucl. Phys. B 829 \(2010\)1](#)

● Beam-spin asymmetry

GPD \tilde{H}

● Transverse target-spin asymmetry

GPD \tilde{E}

H: [JHEP 06 \(2008\) 066](#)

● Transverse double-spin asymmetry

GPD \tilde{E}

H: [Phys. Lett. B 704 \(2011\) 15](#)

● Longitudinal target spin asymmetry

GPD \tilde{H}

H: [JHEP 06 \(2010\) 019](#)

D: [Nucl. Phys. B 842 \(2011\) 265](#)

● Longitudinal double spin asymmetry

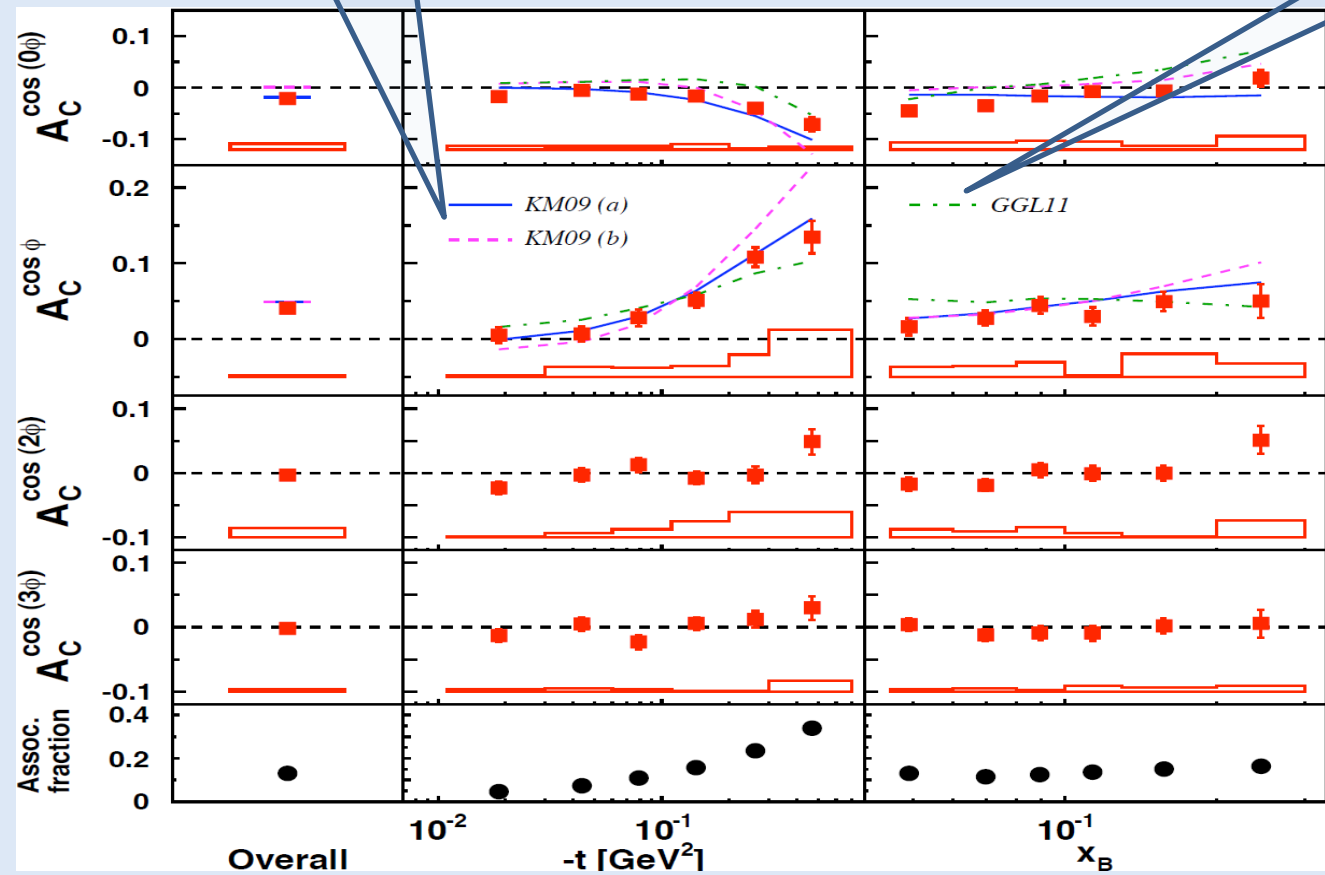
GPD \tilde{H}

Beam-charge asymmetry A_C

KM09:global fit
Including data from HERA
HERMES and Jlab
K. Kumerički, D. Müller
Nucl. Phys. **B 84** (2010) 1

JHEP 07 (2012) 032, arXiv:1203.6287

GGL11:model calculation
G. Goldstein, S. Liuti,
J. Hernandez
Phys. Rev. **D 84** 034007 (2010)



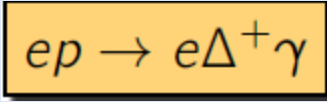
$$\propto -A_C^{\cos(\phi)}$$

$$\propto \text{Re} [F_1 \mathcal{H}]$$

← Higher twist

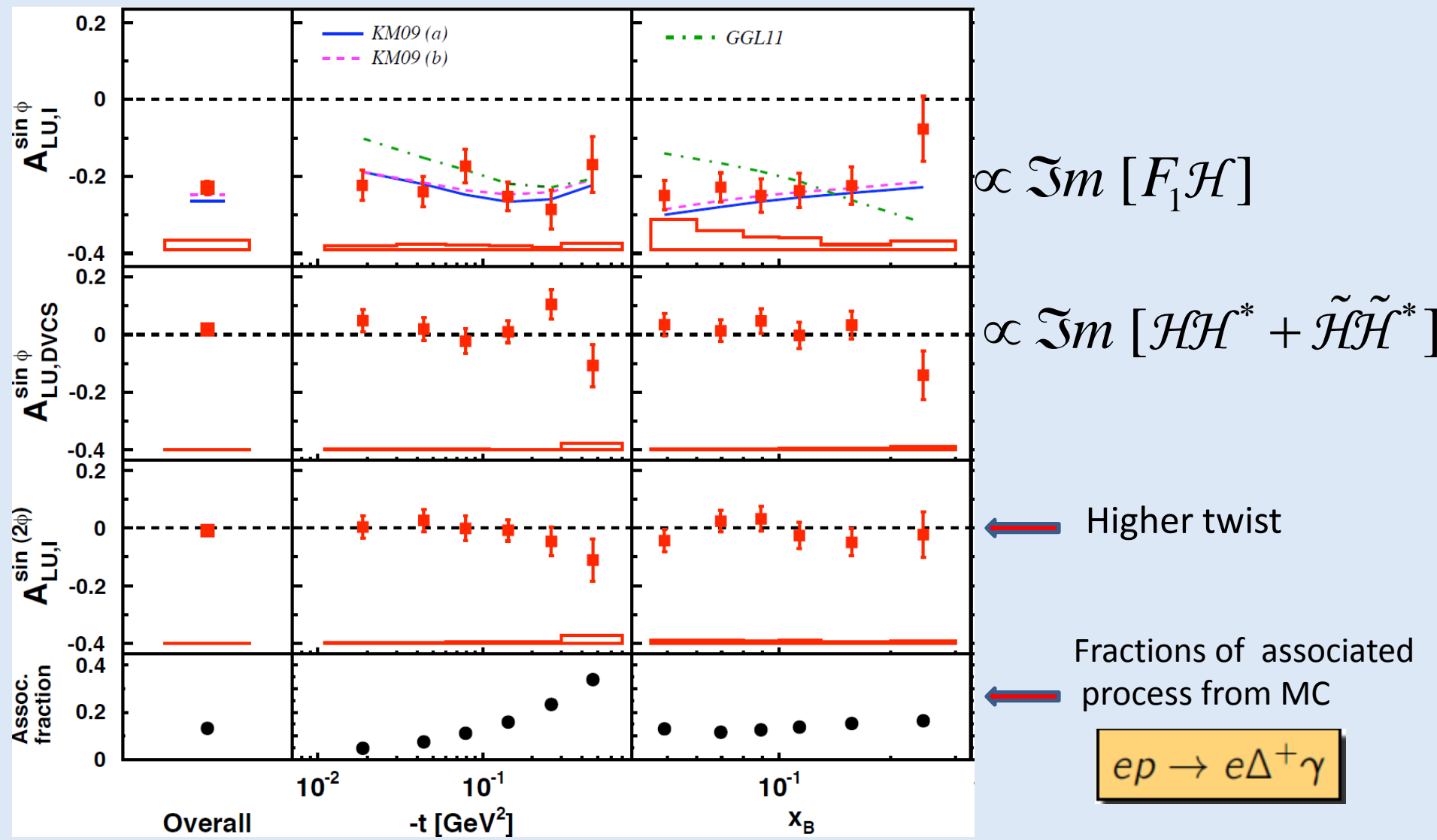
← Gluon leading twist

← Fractions of associated process from MC



Beam-charge-separated asymmetries $A_{LU,I}$ & $A_{LU,DVCS}$

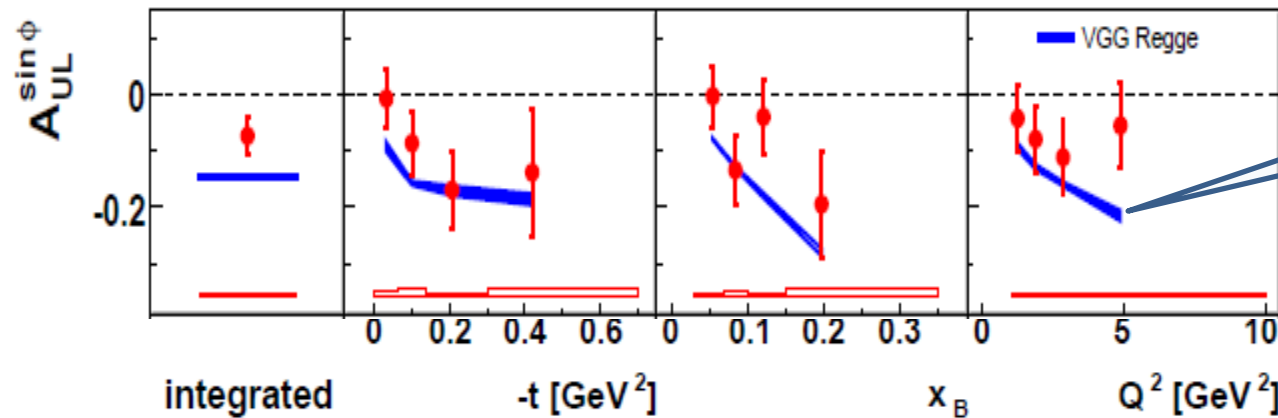
JHEP 07 (2012) 032, arXiv:1203.6287



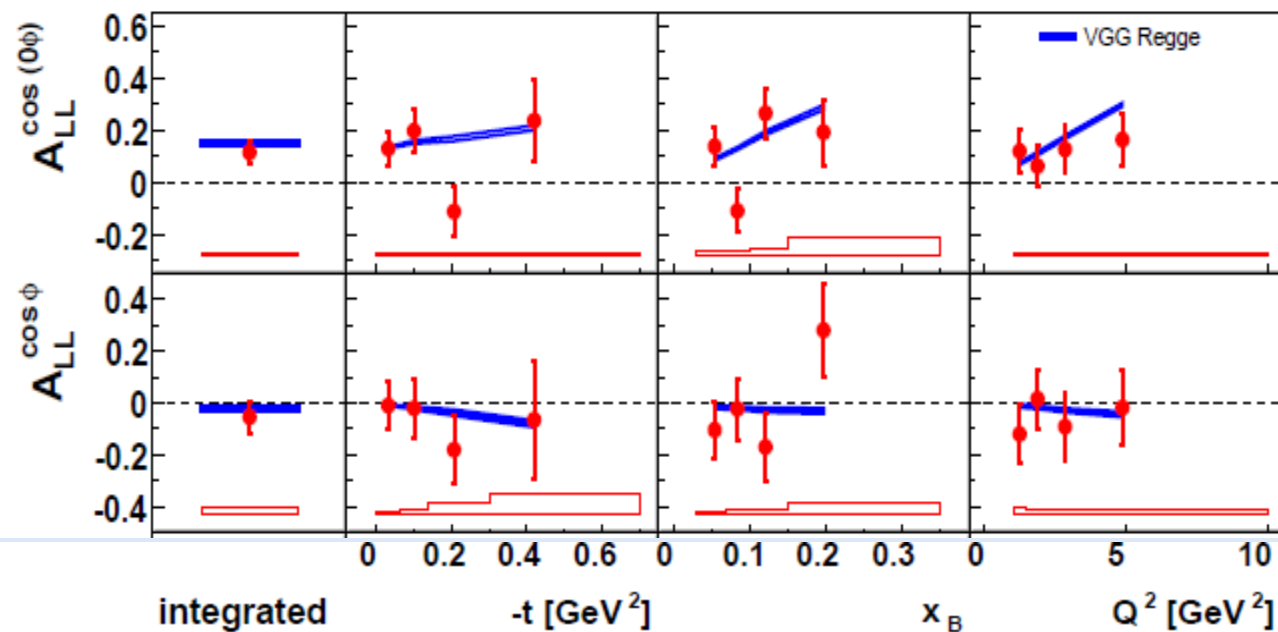
Longitudinal single- and double-spin asymmetries $A_{U(L)L}$

JHEP 06 (2010) 019, arXiv:1004.0177

VGG: model calculation
 M. Vanderhaeghen, P. Guichon,
 M. Guidal
 Phys. Rev. **D60** (1999) 0940177
 Prog. Nucl. Phys. **47** (2001) 401



$$\propto \Im [F_1 \tilde{H}]$$

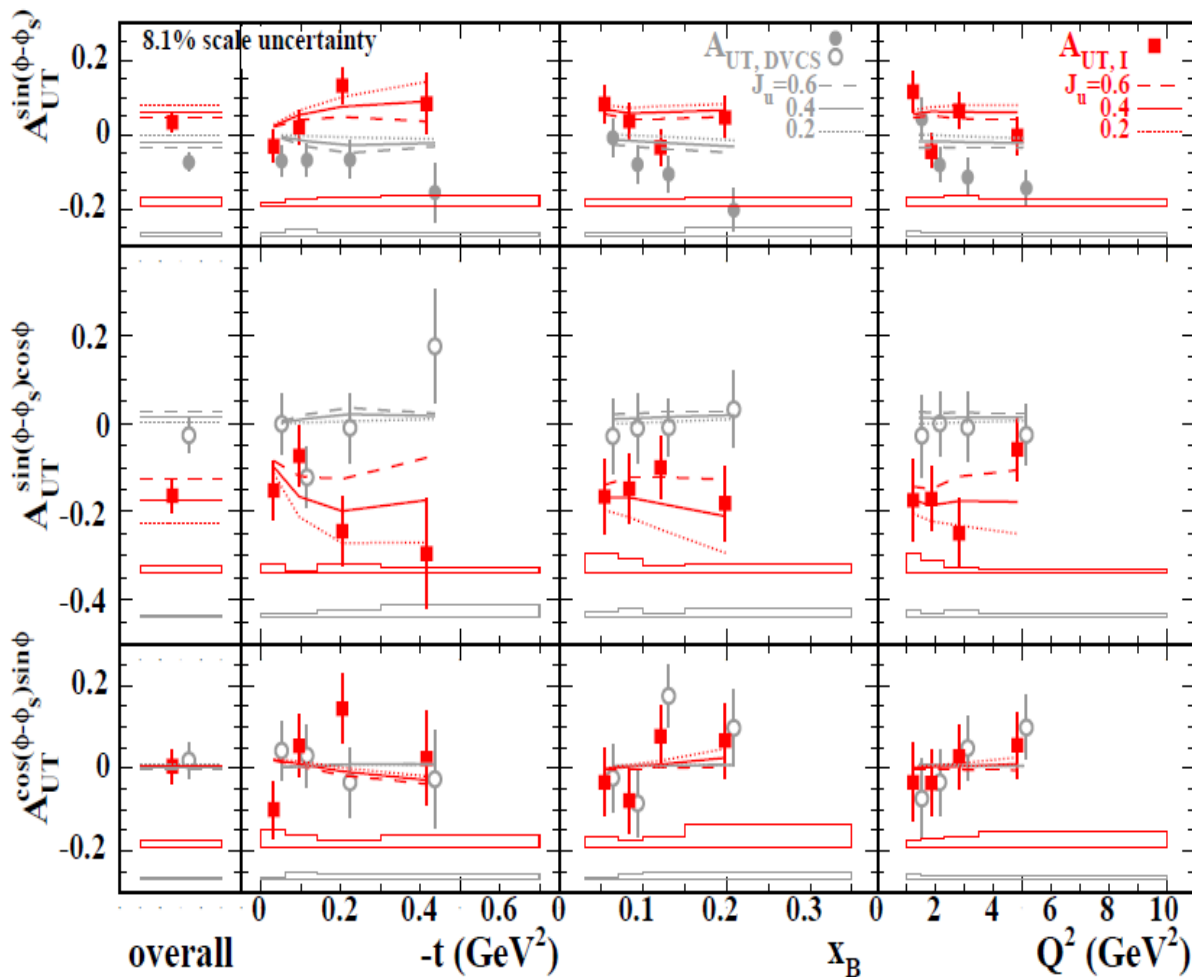


Relatively large BH
 contribution to these
 asymmetries

$$\propto \Re [F_1 \tilde{H}]$$

DVCS: Transverse target-spin asymmetry A_{UT}

Sensitive to **GPD E** JHEP 06 (2008) 066, arXiv:0802.2499



Sensitive to J_u

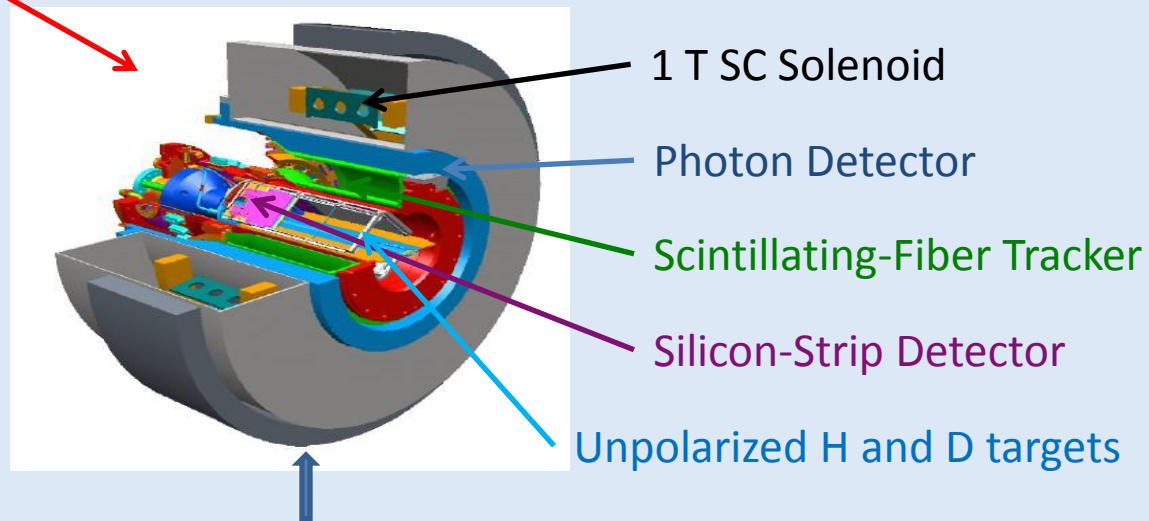
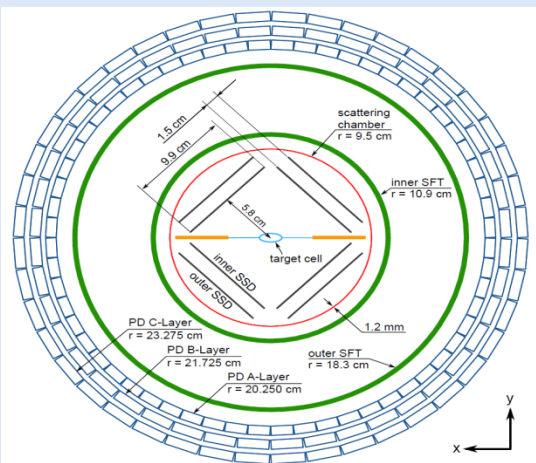
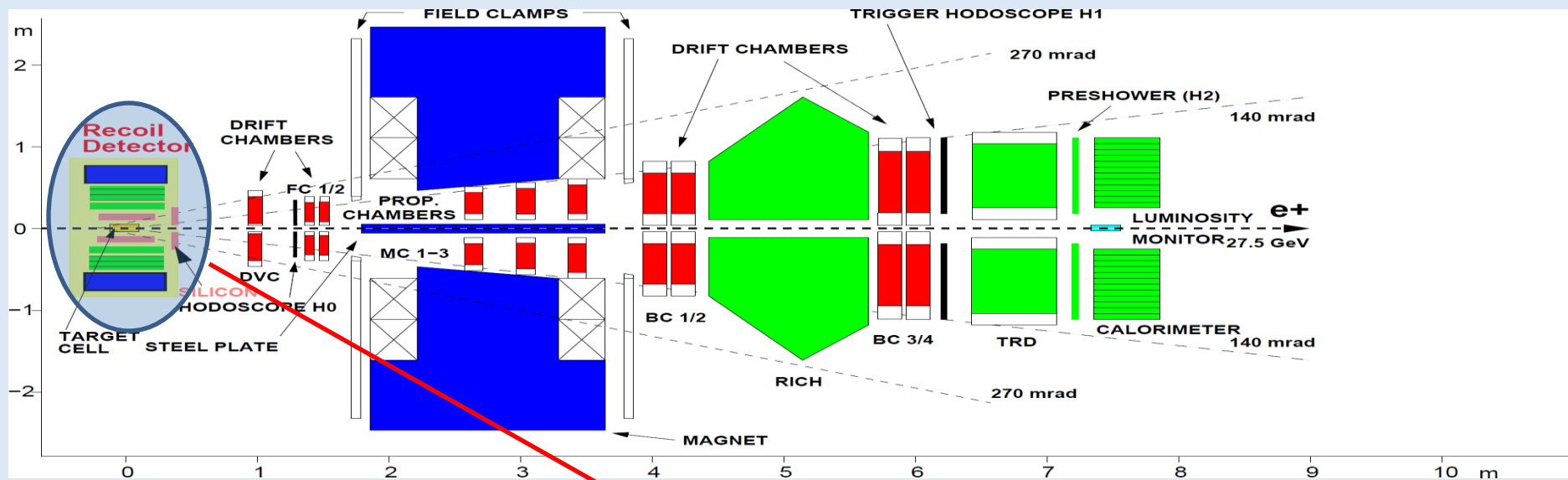
$$\propto \Im [F_2 \mathcal{H} - F_1 \mathcal{E}]$$

Not sensitive to J_u

$$\propto \Im [F_2 \tilde{\mathcal{H}} - (F_1 + \xi F_2) \tilde{\mathcal{E}}]$$

Model: VGG with variation of J_u , while $J_d=0$

DVCS with recoil detector



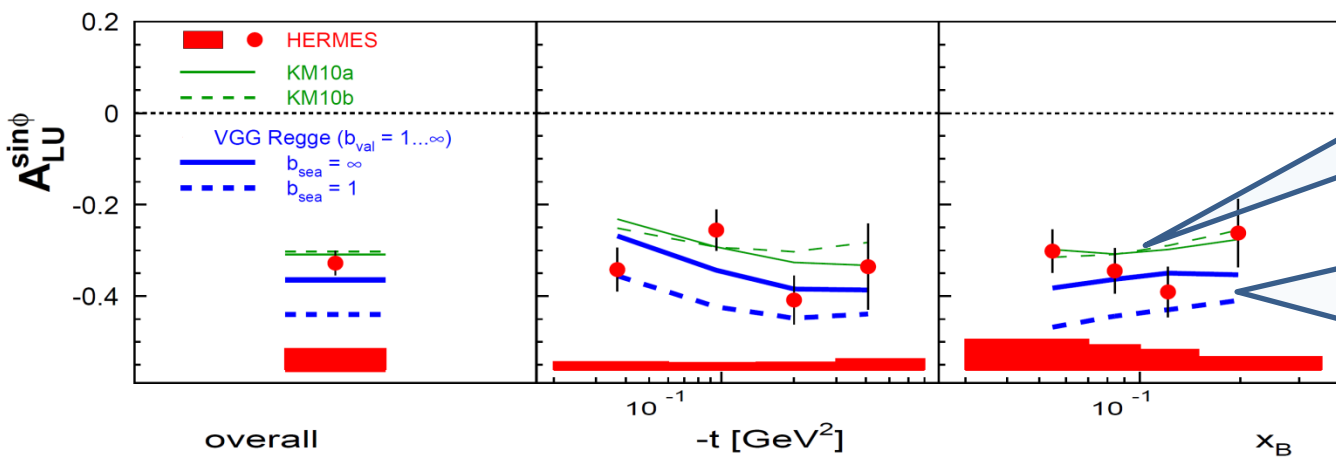
Recoil Detector to tag exclusivity

A. Airapetian et al., JINST B (2013) P05012

JHEP 10 (2012) 042, arXiv:1206.5683

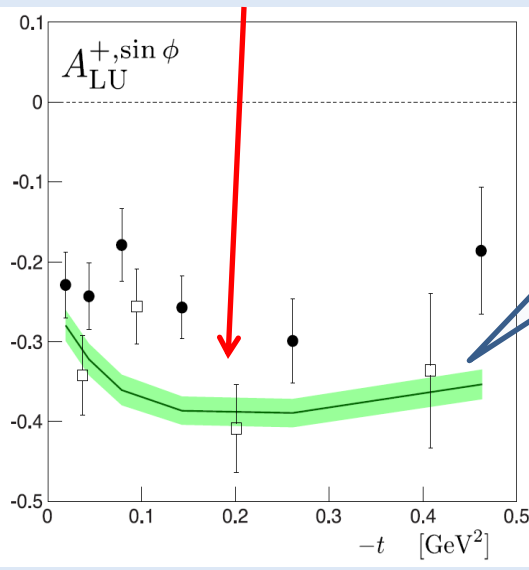
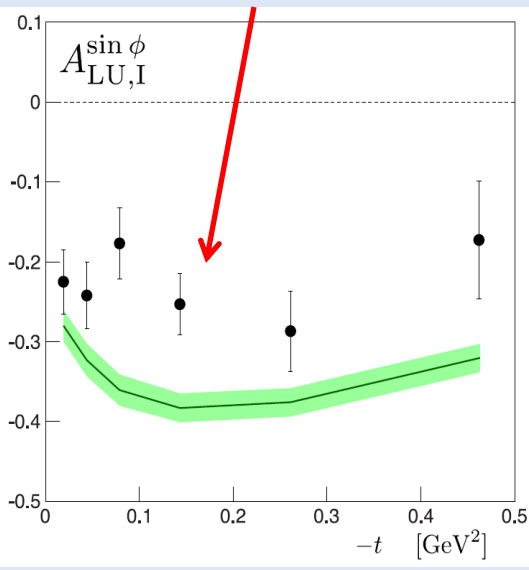
KM10: global fit
Including data from HERA
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Nucl. Phys. **B 84** (2010) 1

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JHEP 07 (2012) 032

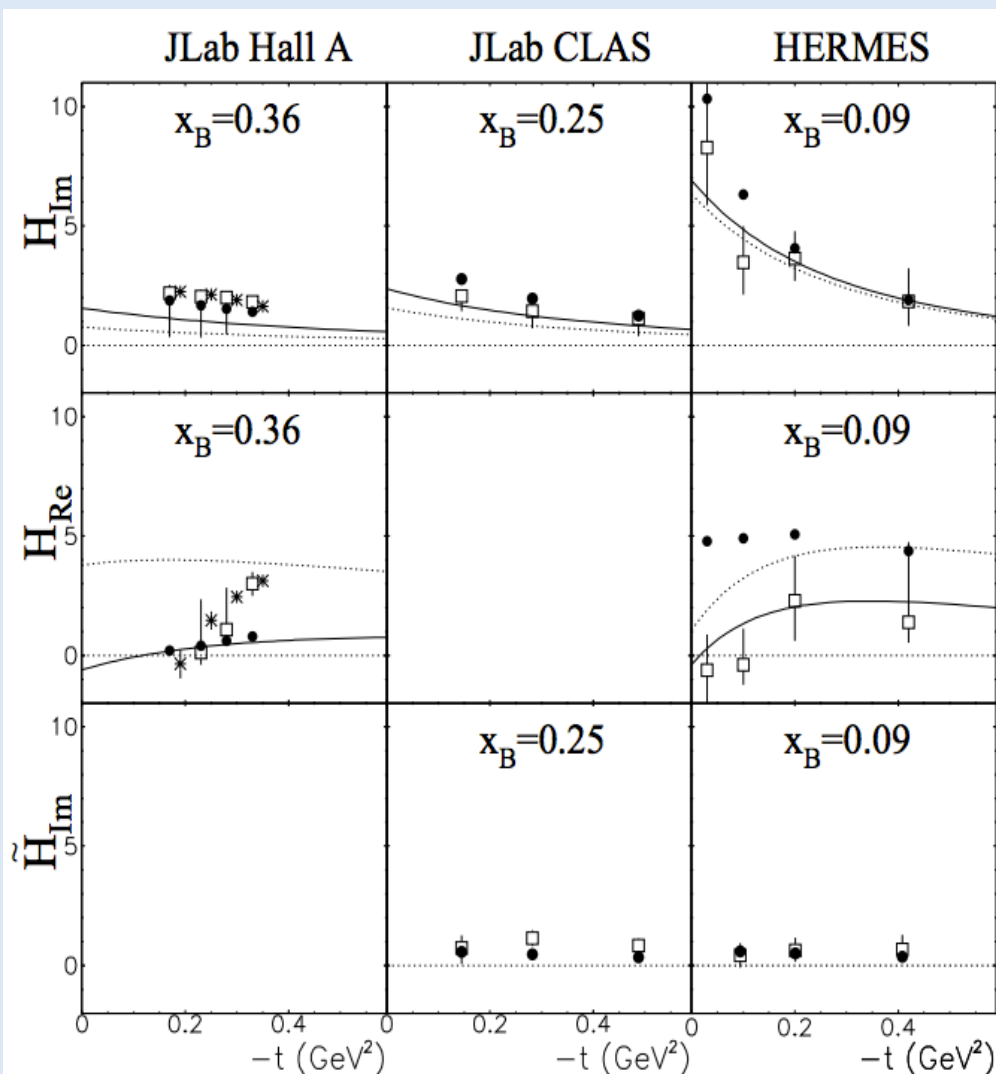
JHEP 10 (2012) 042



KMS: model calculation
GPDs are extracted from HEMP.
P. Kroll, H Moutarde, F. Sabatie,
Eur. Phys. J. C **73** (2001) 2278

The leading amplitude for pure elastic process is well described by recent fits to previously published data and by KMS model fit to exclusive meson data.

M. Guidal ICHEP Proc. (2010) 148



CFFs are extracted from experimental measurements

- VGG model:
GPD H in this model is not consistent with experimental results.

□ M. Guidal, ICHEP Proc. (2010) 148

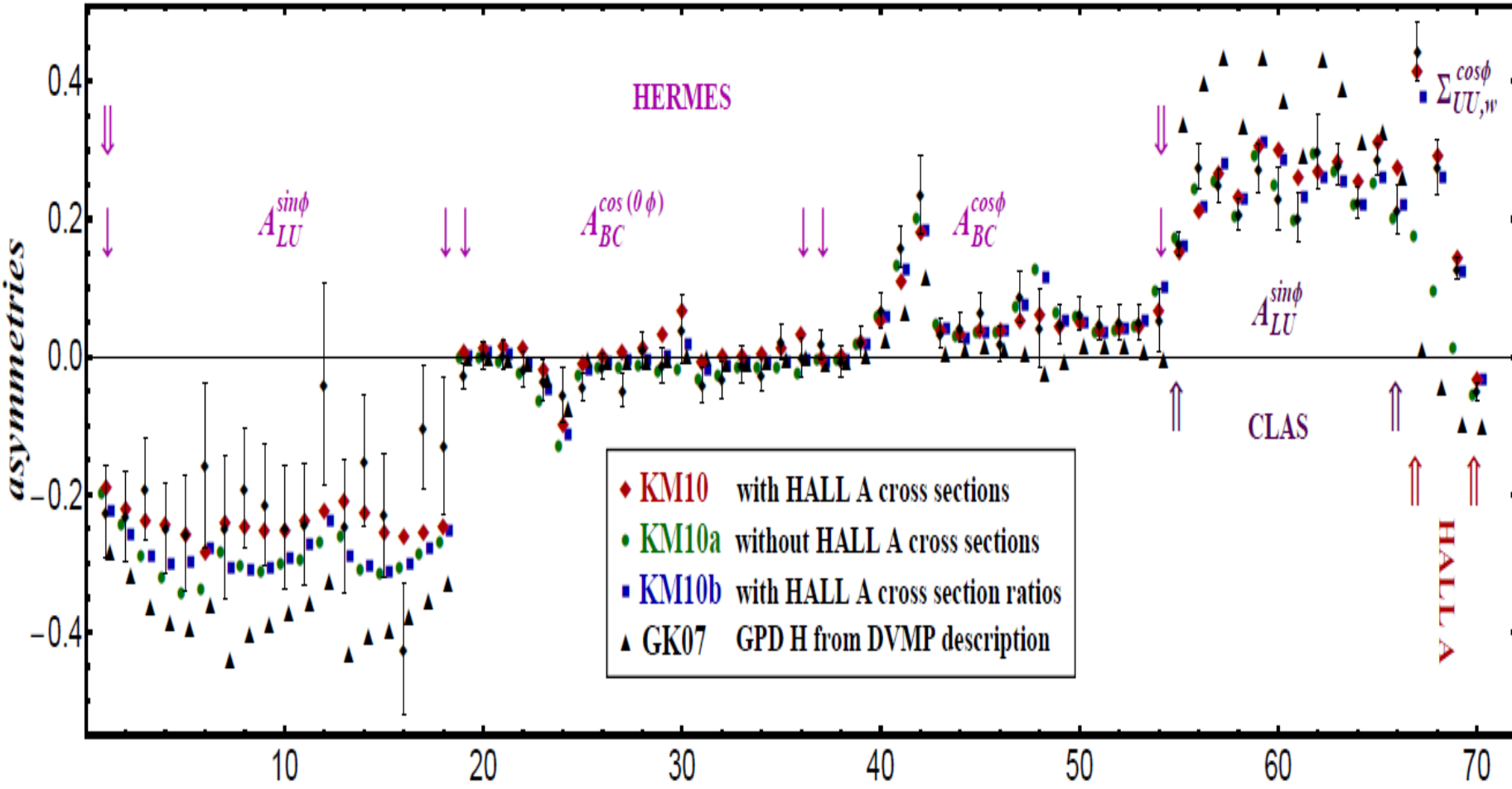
★ H. Moutarde, Phys. Rev. **D** 79 (2009)

Curves:

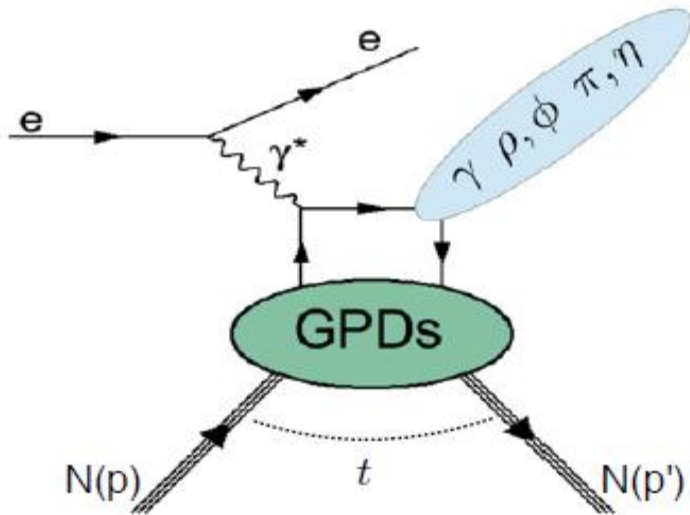
K. Kumericki, D. Muller
Nucl. Phys. **B** 841 (2010)

Results of different fits

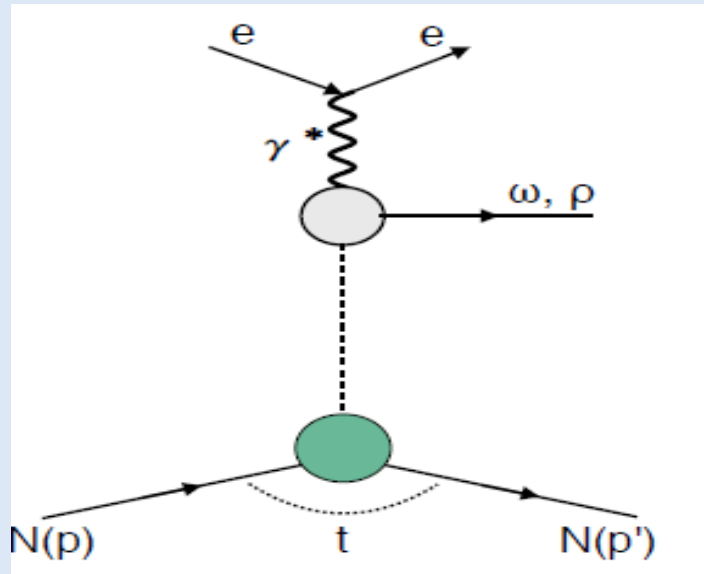
D. Müller: Few Body Syst. 55 (2014) 317-337



Exclusive meson production



- Probes various types of GPDs with different sensitivity and different flavour combinations
- Complementary to DVCS process
- Unpolarized target:
nucleon-helicity-non-flip GPDs H, \tilde{H} and $\bar{E}_T = 2\tilde{H}_T + E_T$.
- Transversely polarized target:
nucleon-helicity-flip GPDs E, \tilde{E} and H_T .



NPE ($J^P = 0^+, 1^-, 2^+ \dots$) (two-gluon exchange = pomeron, $\rho, \omega, f_2, a_2, \dots$ reggeons = $\bar{q}q$ exchange):

GPDs H and E

UPE ($J^P = 0^-, 1^+, \dots$) (π, a_1, b_1, \dots reggeons = $\bar{q}q$ exchange):

GPDs \tilde{H} and \tilde{E}

Angular distribution and extraction of SDMEs

Three-dimensional angular distribution $W^{U+L}(\Phi, \phi, \cos \Theta)$ depends linearly on SDMEs – $r^\alpha_{\lambda_V \lambda'_V}$ and beam polarization P_b

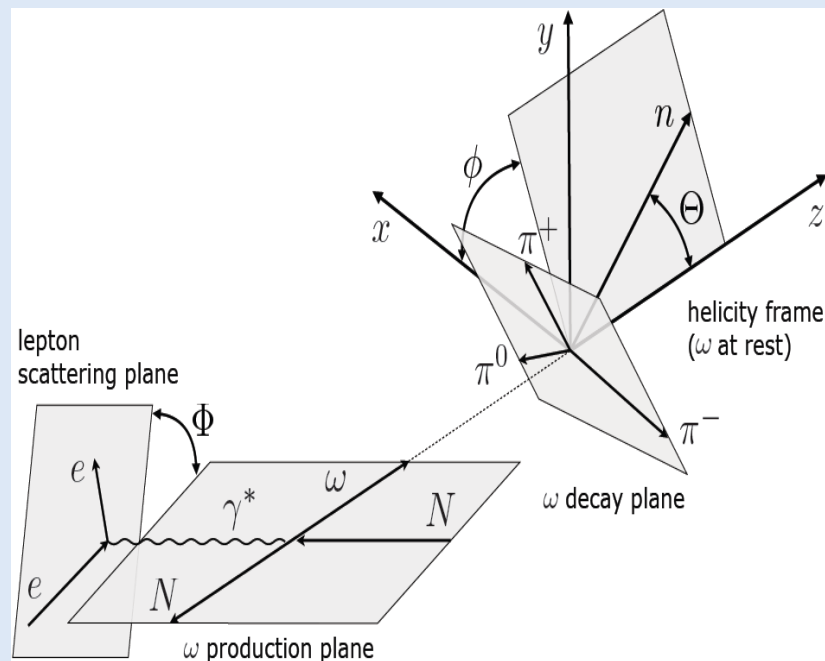
$$r^\alpha_{\lambda_V \lambda'_V} \sim \rho_{\lambda_V \lambda'_V} = \frac{1}{2N} \sum_{\lambda_\gamma \lambda'_\gamma \lambda_N \lambda'_N} F_{\lambda_V \lambda'_N \lambda_\gamma \lambda_N} \sum_{\lambda_\gamma \lambda'_\gamma}^\alpha F_{\lambda'_V \lambda'_N \lambda'_\gamma \lambda_N}^*$$

$$\gamma^*(\lambda_\gamma) + N(\lambda_N) \rightarrow V(\lambda_V) + N(\lambda'_N)$$

Photon SDMEs

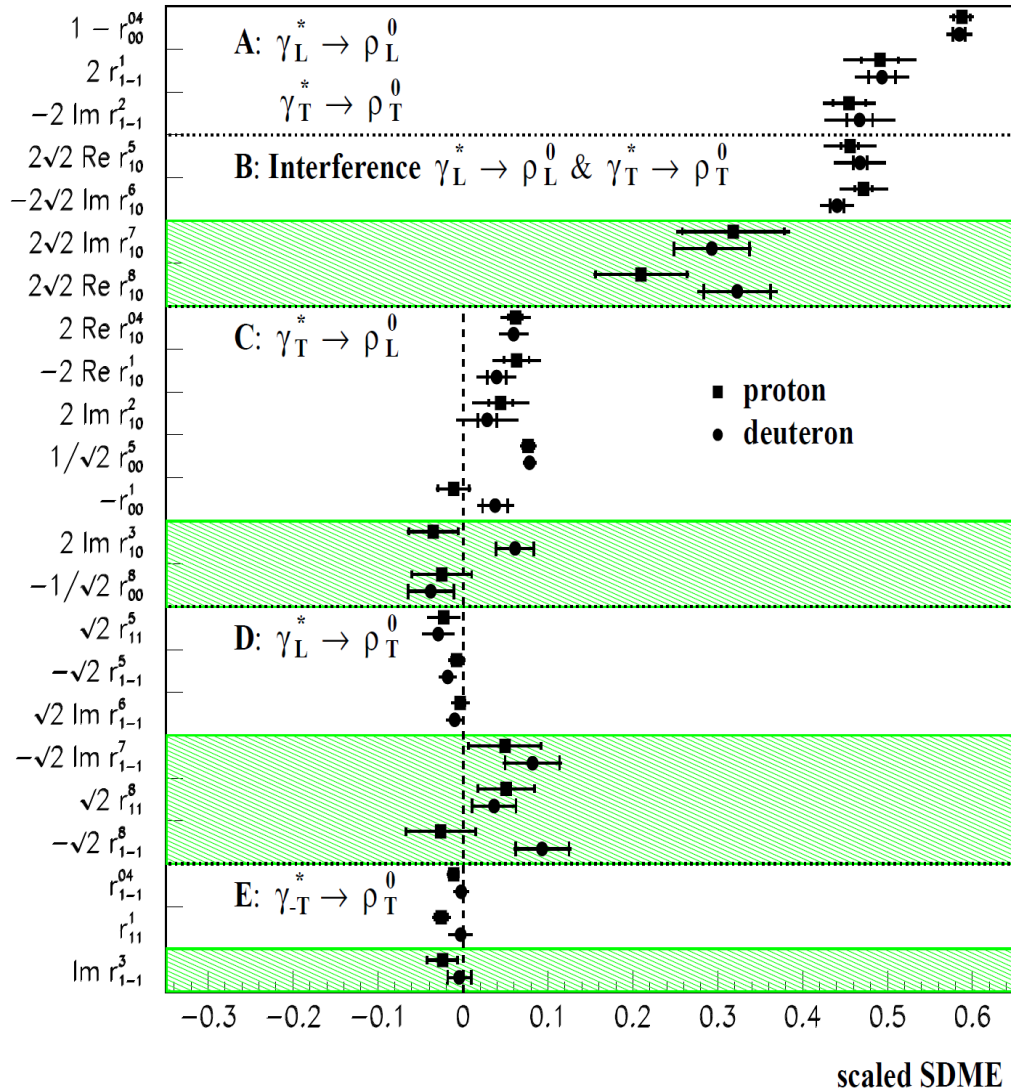
Helicity amplitudes

- Helicity amplitudes are the fundamental quantities to be compared with theory.
- They form a basis for the SDMEs.
- For longitudinally polarized beam and unpolarized target there are 23 SDMEs: 15 unpolarized and 8 polarized.
- The SDMEs are extracted by fitting the angular distribution $W^{U+L}(\Phi, \phi, \cos \Theta)$ to the experimental angular distribution of pions from ω -decay using unbinned Maximum Likelihood method.

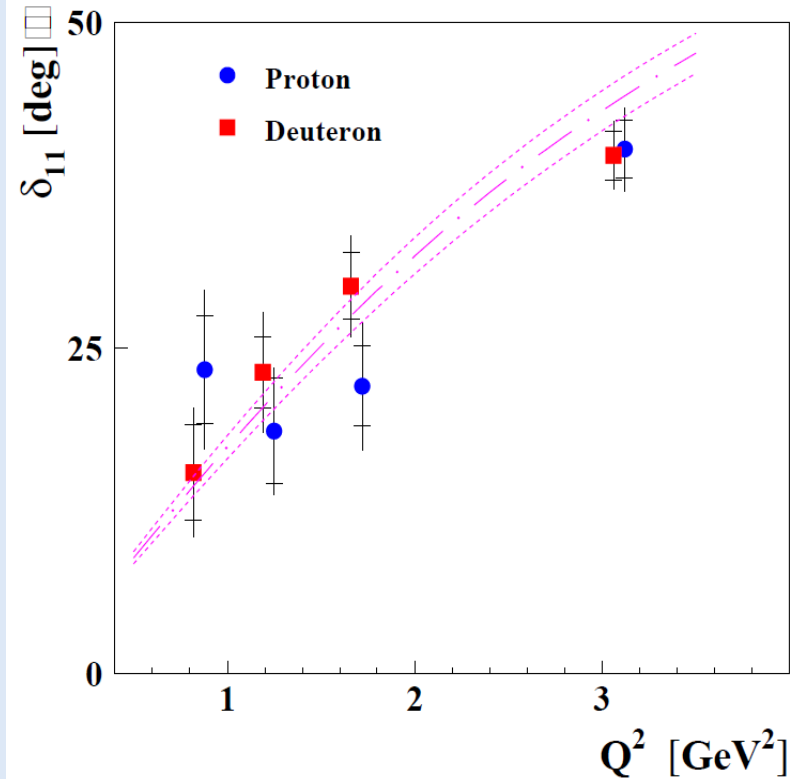


ρ^0 – meson production: SDMEs

Eur. Phys. J. C 62 (2009) 659



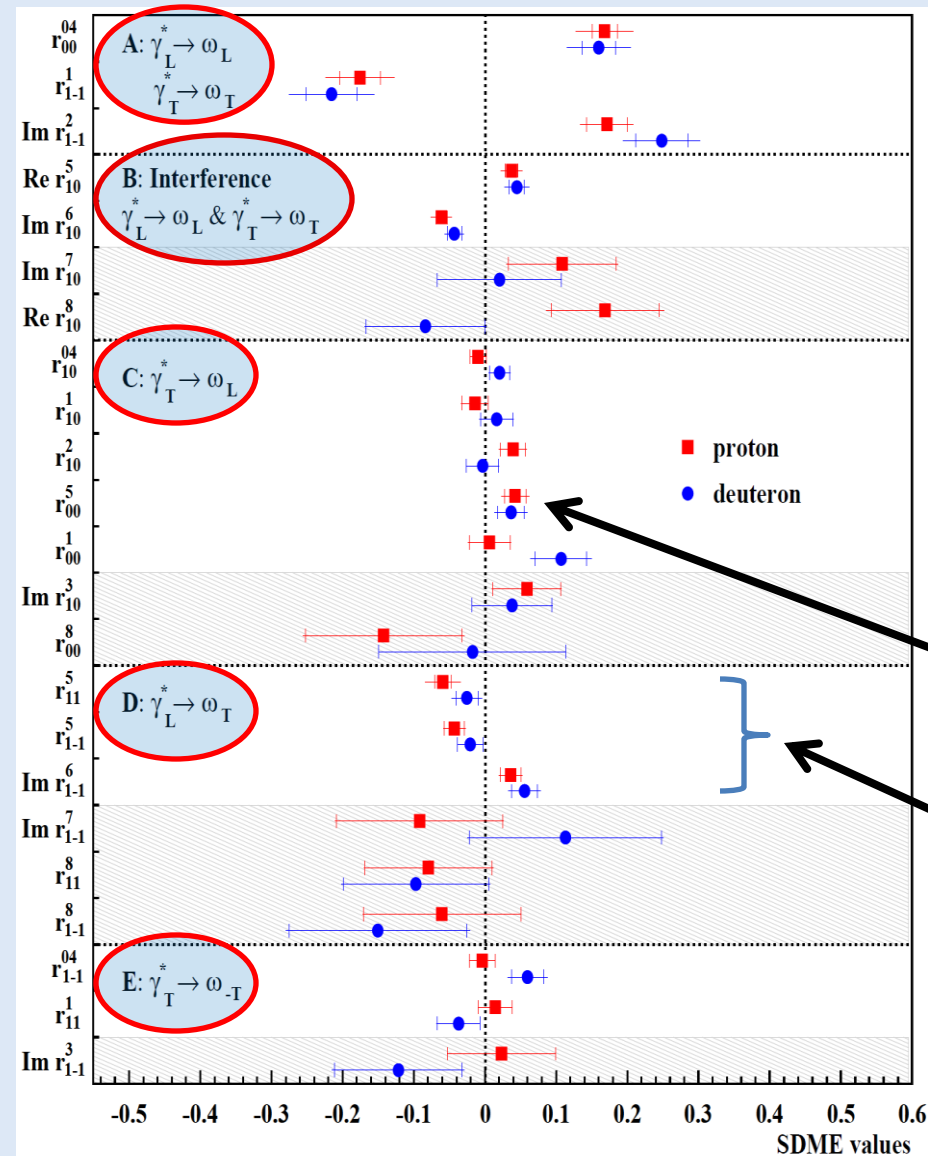
Eur. Phys. J. C 71 (2011) 1609



Extraction of SDMEs and helicity amplitude ratios at HERMES for ρ^0 – mesons challenges GPD-based calculations (giving small values).

SDMEs in exclusive ω production

Eur. Phys. J. C 74 (2014) 3110



- 5 classes of SDMEs
- Unpolarized and polarized SDMEs
- Similar magnitudes of SDMEs on **proton** & **deuteron**
- SCHC (S-Channel Helicity Conservation)**: holds for **class – A** & **class – B** SDMEs:

$$\longrightarrow \begin{cases} r_{1-1}^1 = -\text{Im } r_{1-1}^2 \\ \text{Re } r_{10}^5 = -\text{Im } r_{10}^6 \\ \text{Im } r_{10}^7 = \text{Re } r_{10}^8 \end{cases}$$

- SCHC**: slightly violated for **class – C**

$$r_{00}^5 \neq 0 \text{ by } 3(2) \sigma \text{ for } p(d)$$

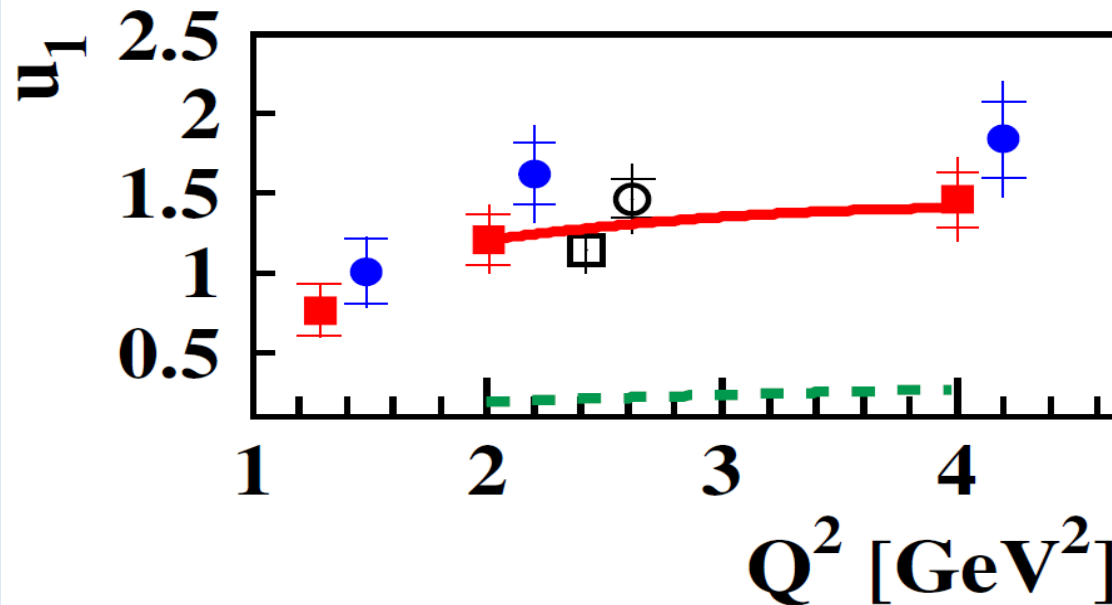
- SCHC**: slightly violated for **class – D**

$$r_{11}^5 + r_{1-1}^5 - \text{Im } r_{1-1}^6 \neq 0 \text{ by } 3(2.5) \sigma \text{ for } p(d)$$

Extraction of $\pi\omega$ transition form factor

$$u_1 = 1 - r_{00}^{04} + 2r_{1-1}^{04} - 2r_{11}^1 - 2r_{1-1}^1$$

Eur. Phys. J. C 74 (2014) 3110

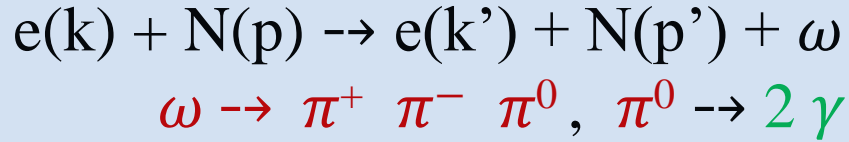


GK model
S. Goloskokov & P. Kroll,
Eur. Phys. J. A 50 (2014) 146

Only the magnitude of the $\pi\omega$ transition form factor (not the sign) can be evaluated.

- The **solid** line show the calculation of the **GK model with pion-pole contribution**
- **Dashed line** are the model results **without the pion-pole**.
- The **pion-pole contribution** seems to account completely for UPE.

Exclusive ω - meson production: A_{UT} asymmetry



Angular dependent part

$$w(\phi, \phi_S) = 1 + A_{UU}^{\cos(\phi)} \cos(\phi) + A_{UU}^{\cos(2\phi)} \cos(2\phi)$$

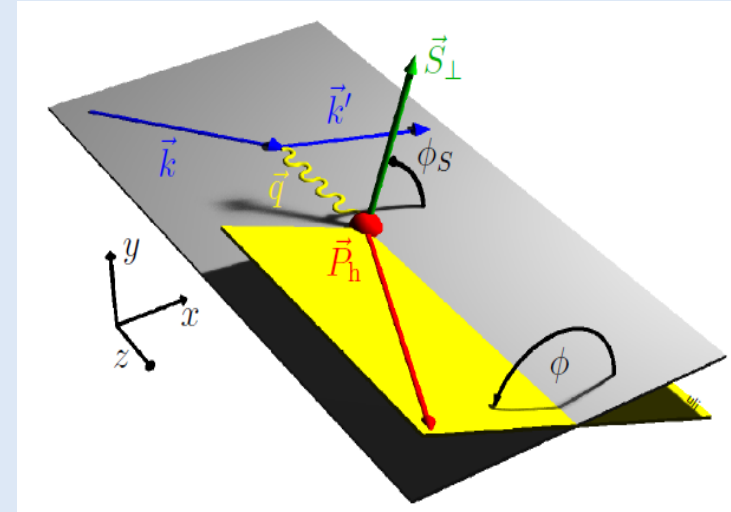
$$+ S_{\perp} \left[A_{UT}^{\sin(\phi+\phi_S)} \sin(\phi+\phi_S) + A_{UT}^{\sin(\phi-\phi_S)} \sin(\phi-\phi_S) \right.$$

$$\left. + A_{UT}^{\sin(\phi_S)} \sin(\phi_S) + A_{UT}^{\sin(2\phi-\phi_S)} \sin(2\phi-\phi_S) + A_{UT}^{\sin(3\phi-\phi_S)} \sin(3\phi-\phi_S) \right]$$

$$w(\phi, \phi_S, \theta) = \frac{3}{2} r_{00}^{04} \cos^2(\theta) w_L(\phi, \phi_S) + \frac{3}{4} (1 - r_{00}^{04}) \sin^2(\theta) w_T(\phi, \phi_S)$$

$$w_L(\phi, \phi_S) = 1 + A_{UU,L}(\phi) + S_{\perp} A_{UT,L}(\phi, \phi_S)$$

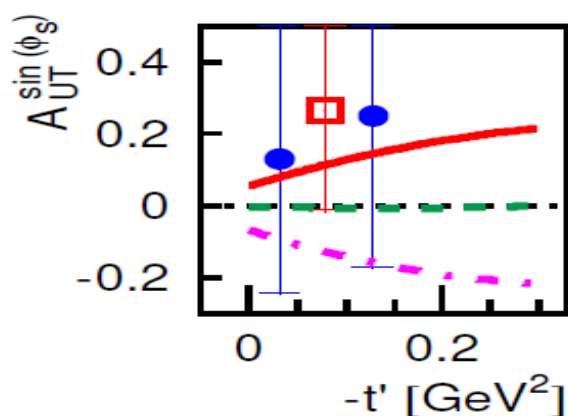
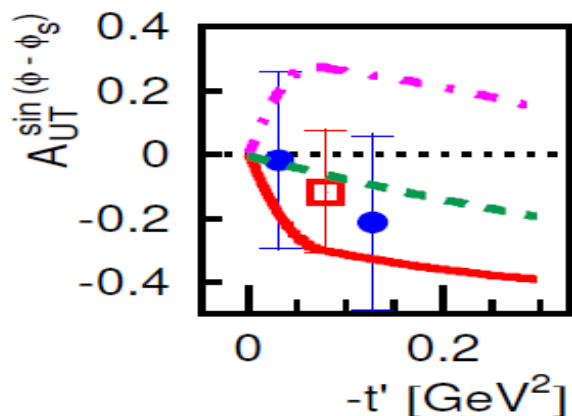
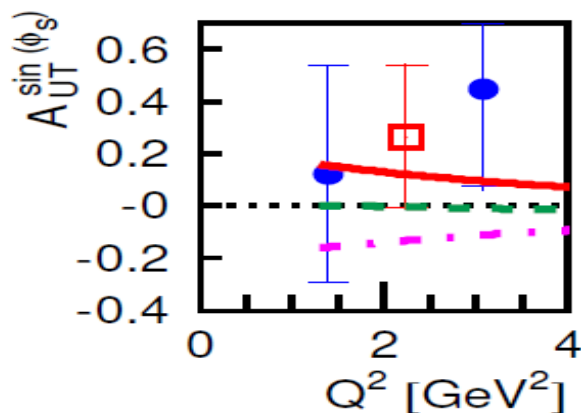
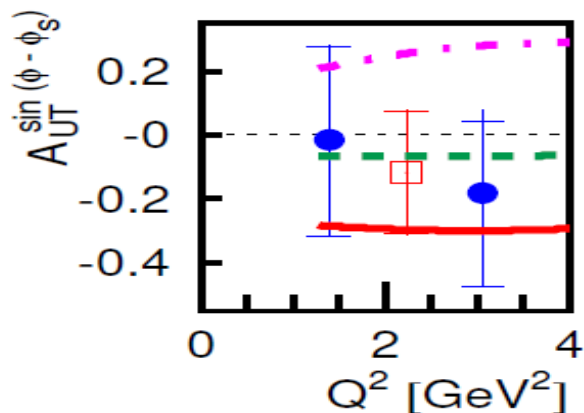
$$w_T(\phi, \phi_S) = 1 + A_{UU,T}(\phi) + S_{\perp} A_{UT,T}(\phi, \phi_S)$$



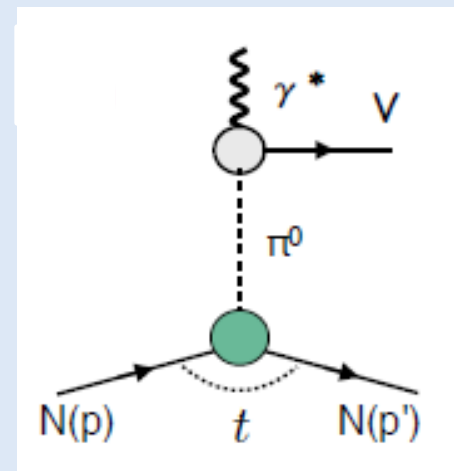
Fit angular distributions
of ω -decay pions

Exclusive ω - meson production: amplitudes of A_{UT}

Eur. Phys. J. C 75 (2015) 600



GK model
S. Goloskokov & P. Kroll,
Eur. Phys. J. A 50 (2014) 146



Pion pole

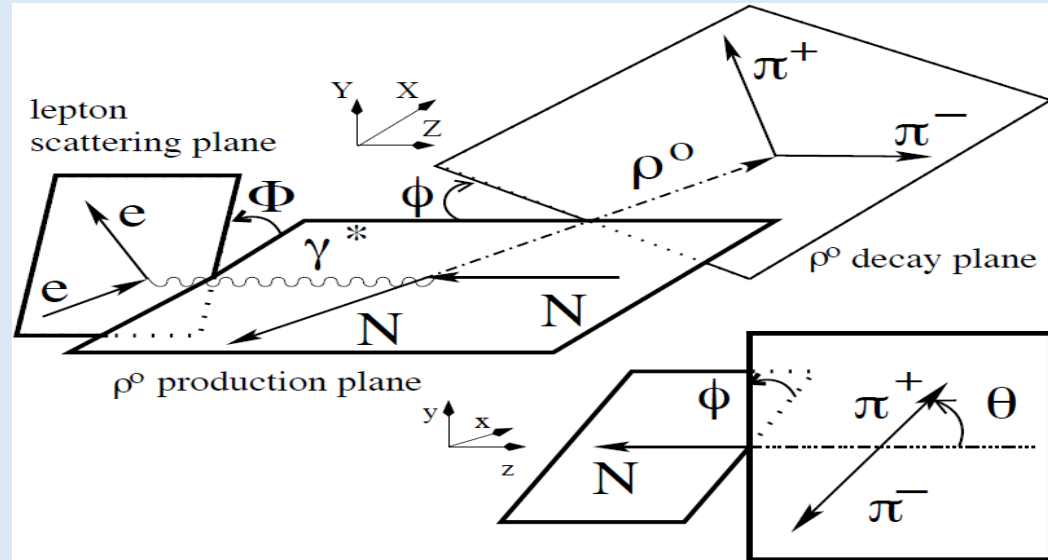
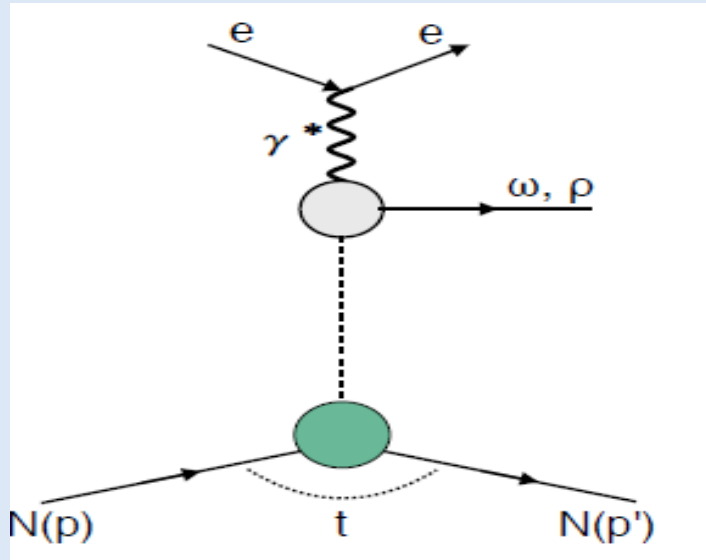
$$\left(\propto \frac{1}{t - m_\pi^2} \right)$$

- The **solid** (**dash-dotted**) lines show the calculation of the **GK model** for a **positive** (**negative**) $\pi\omega$ transition form factor
- Dashed lines** are the model results **without the pion pole**.

Exclusive ρ^0 – meson production: helicity ratios

$$e(k) + N(p) \rightarrow e(k') + N(p') + \rho^0$$

$$\rho^0 \rightarrow \pi^+ \pi^-$$



$$\gamma^* (\lambda_\gamma) + N (\lambda_N) \rightarrow V(\lambda_V) + N(\lambda'_N)$$

$$F_{\lambda_V \lambda'_N \lambda_\gamma \lambda_N} = T_{\lambda_V \lambda'_N \lambda_\gamma \lambda_N} + U_{\lambda_V \lambda'_N \lambda_\gamma \lambda_N}$$

Helicity amplitude ratios:

$$t_{\lambda_V \lambda_\gamma}^{(n)} = T_{\lambda_V \lambda_\gamma}^{(n)} / T_{0\frac{1}{2}0\frac{1}{2}}$$

$$u_{\lambda_V \lambda_\gamma}^{(n)} = U_{\lambda_V \lambda_\gamma}^{(n)} / T_{0\frac{1}{2}0\frac{1}{2}}$$

$$n=1 \quad \lambda_N = \lambda'_N$$

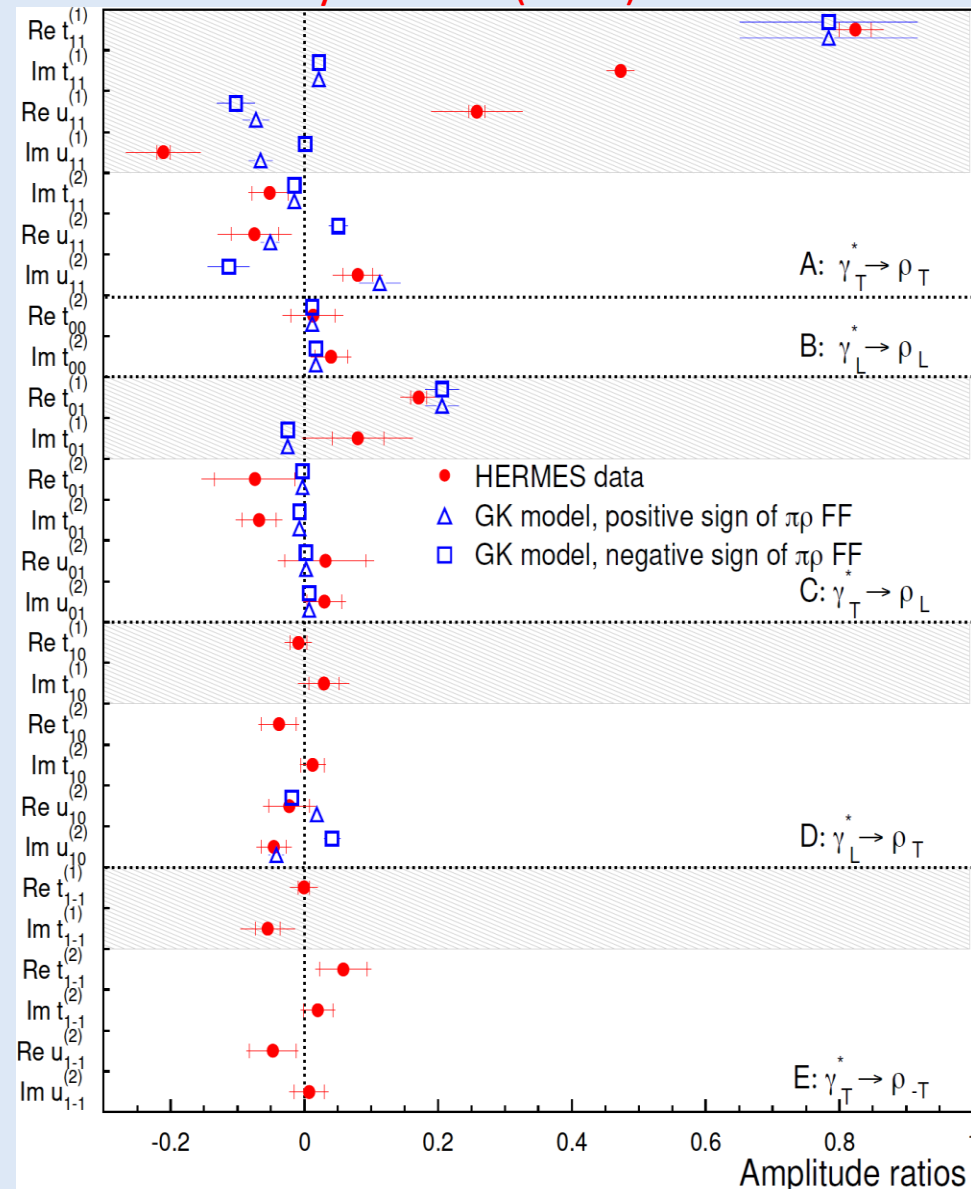
$$n=2 \quad \lambda_N \neq \lambda'_N$$

$T_{\lambda_V \lambda_\gamma}^{(n)}$ – NPE Amplitude

$U_{\lambda_V \lambda_\gamma}^{(n)}$ – UPE Amplitude

Exclusive ρ^0 – meson production: helicity ratios

Eur. Phys. J. C 77 (2017) 378



- Comparison with GK model:
Eur. Phys. J. A 50 (2014) 146
- Where missing, set to zero in GK model
- Two set of calculations using opposite signs for the $\pi\rho$ transition form factors
- Data clearly favors positive sign
- Good agreement for most ratios, but clearly off for some
- Problem with phases known already

- 3D picture of the nucleon:
 - HERMES measured “full set” of DVCS-related asymmetries on proton and nuclear targets.
 - Data with recoil-proton detection allows clean separation of DVCS/BH contribution in a signal.
 - Indication of larger amplitude for pure sample.
 - Associated DVCS results consistent with zero and also with model prediction.
- Measurement of ρ^0 / ω –meson SDMEs & A_{UT} asymmetry amplitudes from exclusive DIS: good model description based on GPDs with inclusion of pion pole.
 - The sign of the $\pi\omega$ transition form factor
- Measurement of helicity ratios from exclusive ρ^0 –meson production in DIS: model description with inclusion of pion pole.

Backup Slides

Azimuthal dependences in DVCS

Unpolarized proton target

$$\frac{d^4\sigma}{dQ^2 dx_B dt d\phi} \propto \left(|\tau_{\text{BH}}|^2 + |\tau_{\text{DVCS}}|^2 + \text{I} \right)$$

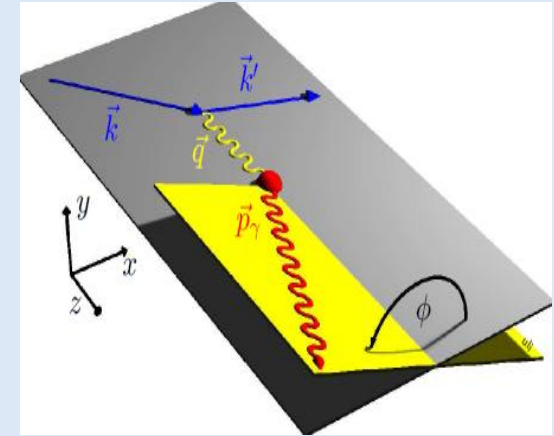
$$|\tau_{\text{BH}}|^2 = \frac{K_{\text{BH}}}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \sum_{n=0}^2 \mathcal{C}_n^{\text{BH}} \cos(n\phi)$$

$$|\tau_{\text{DVCS}}|^2 = K_{\text{DVCS}} \left\{ \sum_{n=0}^2 \mathcal{C}_n^{\text{DVCS}} \cos(n\phi) + \sum_{n=1}^2 \mathcal{S}_n^{\text{DVCS}} \sin(n\phi) \right\}$$

$$\text{I} = -\frac{e_l K_{\text{I}}}{\mathcal{P}_1(\phi)\mathcal{P}_2(\phi)} \left\{ \sum_{n=0}^3 \mathcal{C}_n^{\text{I}} \cos(n\phi) + \sum_{n=1}^3 \mathcal{S}_n^{\text{I}} \sin(n\phi) \right\}$$

Fourier coefficients are related to certain linear or bi-linear combinations of Compton Form Factors (CFFs):

$$\mathcal{F}(\xi, t) = \sum_q \int_{-1}^1 dx C_q^{\mp}(\xi, x) F^q(x, \xi, t) \longrightarrow \text{GPD}$$

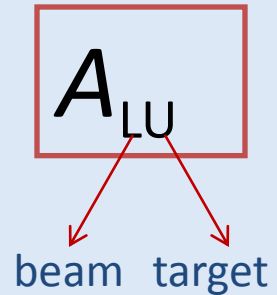


Azimuthal asymmetries in DVCS off unpolarized targets

$$\sigma_{LU}(\phi, P_l, e_l) = \sigma_{UU} [1 + e_l A_C(\phi) + e_l P_l A_{LU}^I(\phi) + P_l A_{LU}^{DVCS}(\phi)]$$

Charge-difference beam-helicity asymmetry:

$$A_{LU}^I(\phi) = \frac{(\sigma^{+\rightarrow} - \sigma^{+\leftarrow}) - (\sigma^{-\rightarrow} - \sigma^{-\leftarrow})}{(\sigma^{+\rightarrow} + \sigma^{+\leftarrow}) + (\sigma^{-\rightarrow} + \sigma^{-\leftarrow})} = -\frac{1}{D(\phi)} \frac{x_B}{y} \sum_{n=1}^2 S_n^I \sin(n\phi)$$



Charge-averaged beam-helicity asymmetry:

$$A_{LU}^{DVCS}(\phi) = \frac{(\sigma^{+\rightarrow} - \sigma^{+\leftarrow}) + (\sigma^{-\rightarrow} - \sigma^{-\leftarrow})}{(\sigma^{+\rightarrow} + \sigma^{+\leftarrow}) + (\sigma^{-\rightarrow} + \sigma^{-\leftarrow})} = \frac{1}{D(\phi)} \cdot \frac{x_B^2 t \mathcal{P}_1(\phi) \mathcal{P}_2(\phi)}{Q^2} S_1^{DVCS} \sin(\phi)$$

Beam-Charge asymmetry:

$$A_C(\phi) = \frac{(\sigma^{+\rightarrow} + \sigma^{+\leftarrow}) - (\sigma^{-\rightarrow} + \sigma^{-\leftarrow})}{(\sigma^{+\rightarrow} + \sigma^{+\leftarrow}) + (\sigma^{-\rightarrow} + \sigma^{-\leftarrow})} = -\frac{1}{D(\phi)} \frac{x_B}{y} \sum_{n=0}^3 C_n^I \cos(n\phi)$$

- Measurement with both **beam helicity** and both beam charges
 → **separate** contributions from DVCS and Interference term
- This **separation** is impossible in measurements of single-charge beam-helicity asymmetry $A_{LU}(\phi) = (\sigma^{\rightarrow} - \sigma^{\leftarrow}) / (\sigma^{\rightarrow} + \sigma^{\leftarrow})$

Asymmetries on longitudinally polarized targets

Single-charge target-spin asymmetry (Hydrogen/Deuterium):

$$A_{UL}(\phi, e_l) = \frac{[\sigma^{\rightarrow\rightarrow}(\phi, e_l) + \sigma^{\leftarrow\rightarrow}(\phi, e_l)] - [\sigma^{\rightarrow\leftarrow}(\phi, e_l) + \sigma^{\leftarrow\leftarrow}(\phi, e_l)]}{[\sigma^{\rightarrow\rightarrow}(\phi, e_l) + \sigma^{\leftarrow\rightarrow}(\phi, e_l)] + [\sigma^{\rightarrow\leftarrow}(\phi, e_l) + \sigma^{\leftarrow\leftarrow}(\phi, e_l)]}$$

Single-charge double-spin asymmetry (Hydrogen/Deuterium):

$$A_{LL}(\phi, e_l) = \frac{[\sigma^{\rightarrow\rightarrow}(\phi, e_l) + \sigma^{\leftarrow\leftarrow}(\phi, e_l)] - [\sigma^{\leftarrow\rightarrow}(\phi, e_l) + \sigma^{\rightarrow\leftarrow}(\phi, e_l)]}{[\sigma^{\rightarrow\rightarrow}(\phi, e_l) + \sigma^{\leftarrow\leftarrow}(\phi, e_l)] + [\sigma^{\leftarrow\rightarrow}(\phi, e_l) + \sigma^{\rightarrow\leftarrow}(\phi, e_l)]}$$

Single-charge beam-helicity asymmetry (Deuterium):

$$A_{L\leftarrow}(\phi, e_l) = \frac{[\sigma^{\rightarrow\rightarrow}(\phi, e_l) + \sigma^{\rightarrow\leftarrow}(\phi, e_l)] - [\sigma^{\leftarrow\rightarrow}(\phi, e_l) + \sigma^{\leftarrow\leftarrow}(\phi, e_l)]}{[\sigma^{\rightarrow\rightarrow}(\phi, e_l) + \sigma^{\rightarrow\leftarrow}(\phi, e_l)] + [\sigma^{\leftarrow\rightarrow}(\phi, e_l) + \sigma^{\leftarrow\leftarrow}(\phi, e_l)]}$$

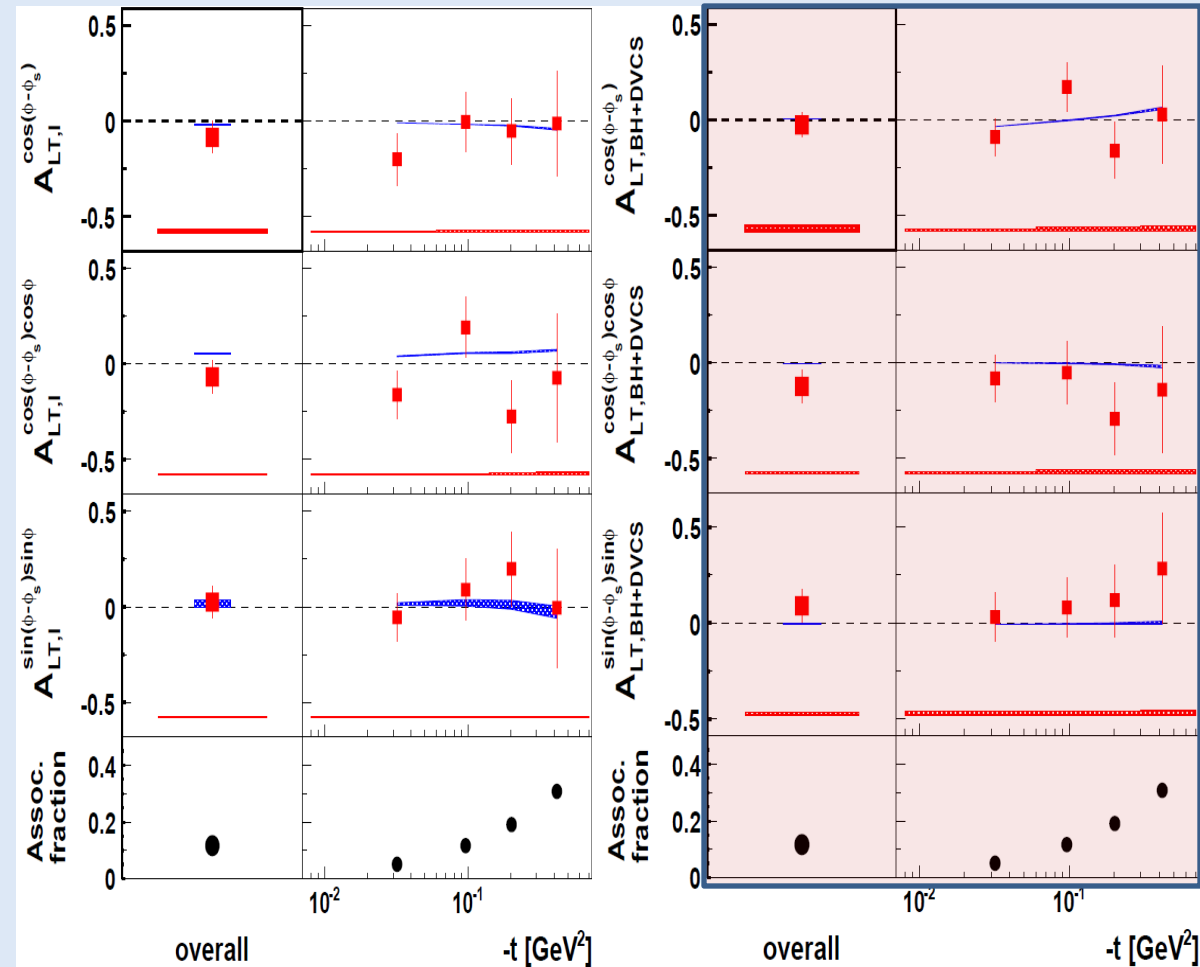
Single-helicity (\leftarrow) beam-charge asymmetry (Deuterium):

$$A_{C\leftarrow}(\phi) = \frac{[\sigma^{+\rightarrow}(\phi) + \sigma^{+\leftarrow}(\phi)] - [\sigma^{-\rightarrow}(\phi) + \sigma^{-\leftarrow}(\phi)]}{[\sigma^{+\rightarrow}(\phi) + \sigma^{+\leftarrow}(\phi)] + [\sigma^{-\rightarrow}(\phi) + \sigma^{-\leftarrow}(\phi)]}$$

DVCS: Transverse double-spin asymmetry A_{LT}

Phys Lett. B704 (2011) 15, arXiv:1106.2990

Full set of data: e+/e- beams;
both helicities; target
polarization - positive/negative.



$$\propto A_{LT}^{\cos(\phi-\phi_S)\cos(\phi)}$$

$$\propto \text{Re} [F_2 \tilde{H} - (F_1 + \xi F_2) \tilde{E}]$$

$$\propto \text{Re} [\mathcal{H}E^* - \mathcal{E}H^* - \xi (\tilde{H}\tilde{E}^* - \tilde{E}\tilde{H}^*)]$$

$$\propto \text{Re} [F_2 \mathcal{H} - F_1 \mathcal{E}]$$

$$\propto \text{Re} [-\tilde{H}E^* - \tilde{H}^*E + \xi (\mathcal{H}\tilde{E}^* + \tilde{E}\mathcal{H}^*)]$$

Sensitive to both GPDs
entering the Ji sum rule

Consistent with zero, cancellations between E and H
Sensitivity to J_u is suppressed by kinematic factors

Deuterium (Hydrogen): unpolarized target

JHEP 11 (2009) 083

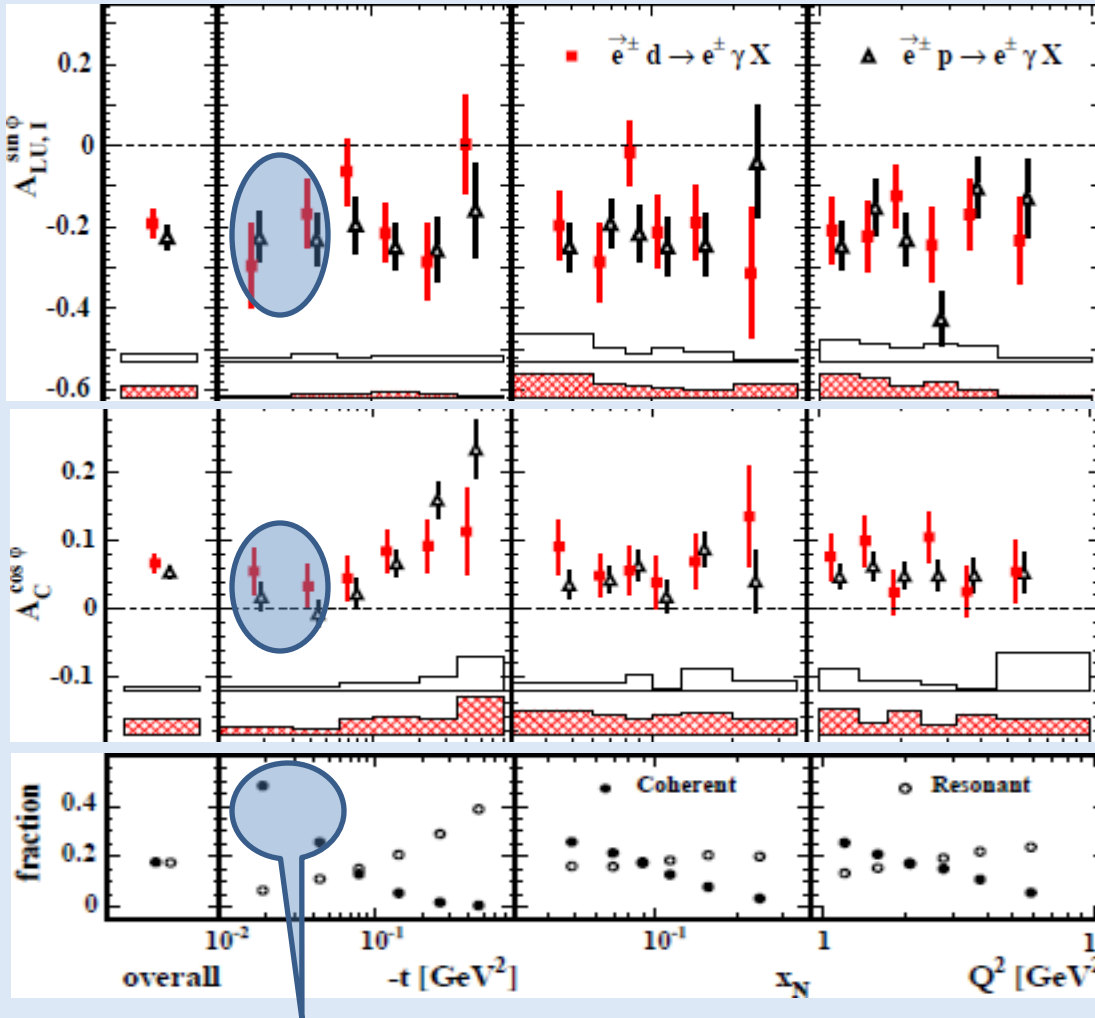
Nucl. Phys. B 829 (2010) 1

$\Im m(\mathcal{H})$

$\Im m(\mathcal{H}_1)$

$\Re e(\mathcal{H})$

$\Re e(\mathcal{H}_1)$

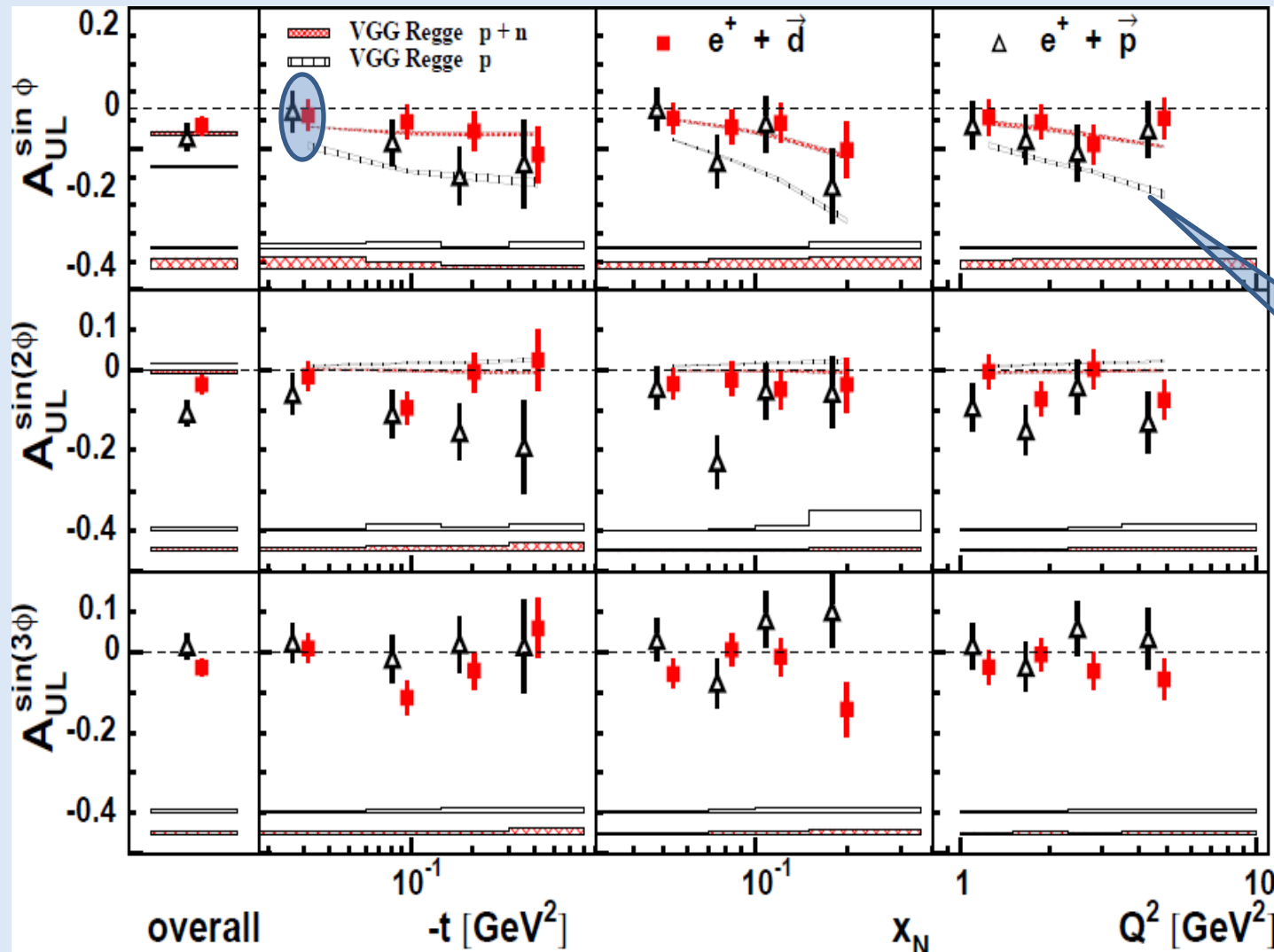


- $A_{LU,I,Coh}^{\sin \phi} = -0.29 \pm 0.18 \text{ (stat)} \pm 0.03 \text{ (syst)}$
- $A_{C,Coh}^{\cos \phi} = 0.11 \pm 0.07 \text{ (stat)} \pm 0.03 \text{ (syst)}$

Deuterium (Hydrogen): target-spin asymmetry

JHEP 11 (2009) 083

Nucl. Phys. B 842 (2011) 265



$\Im m(\tilde{H})$

$\Im m(\tilde{H}_1)$

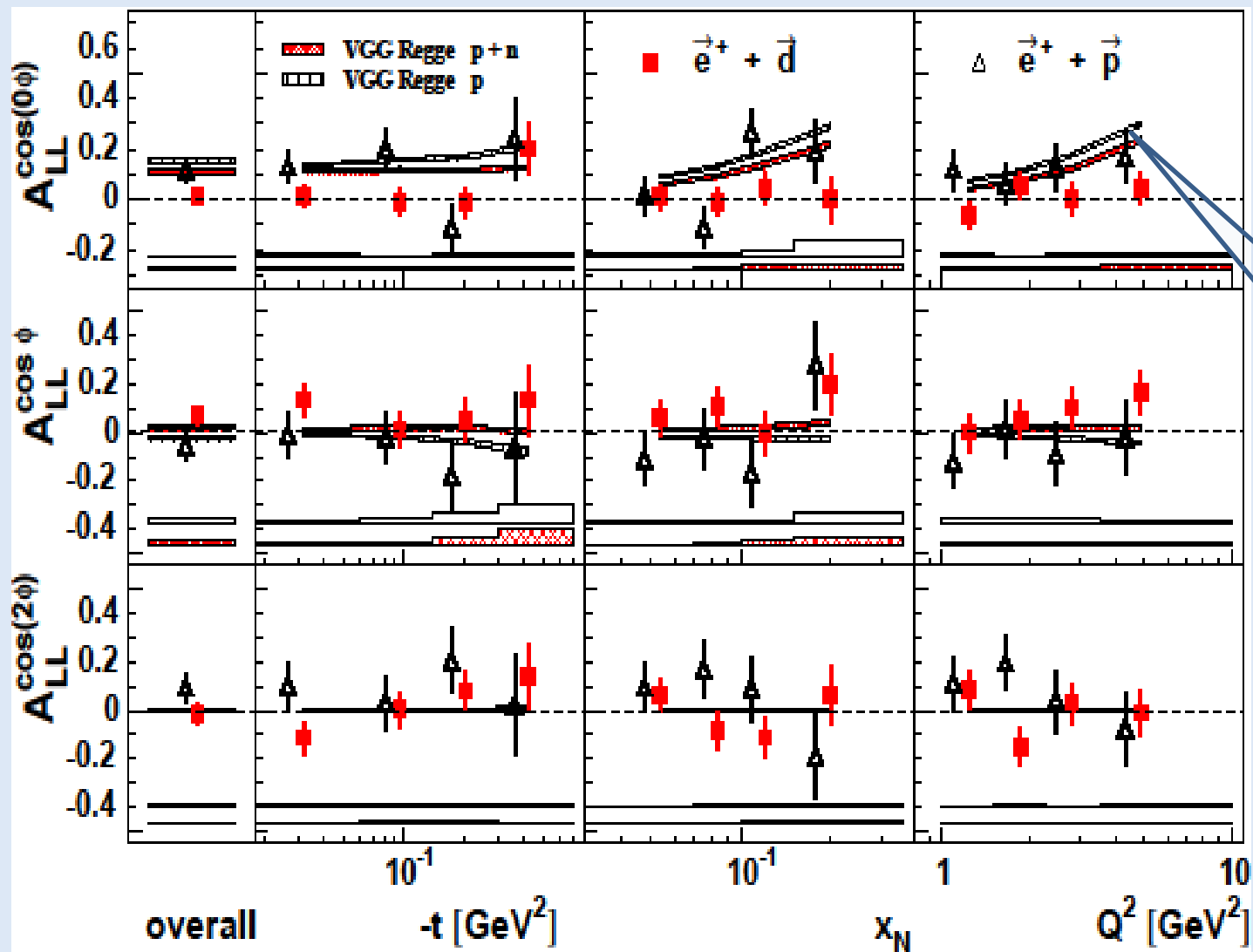
VGG:

Phys. Rev. D60
(1999) 0940177
&
Prog. Nucl. Phys.
47 (2001) 401

Deuterium (Hydrogen): double-spin asymmetry

JHEP 11 (2009) 083

Nucl. Phys. B 842 (2011) 265

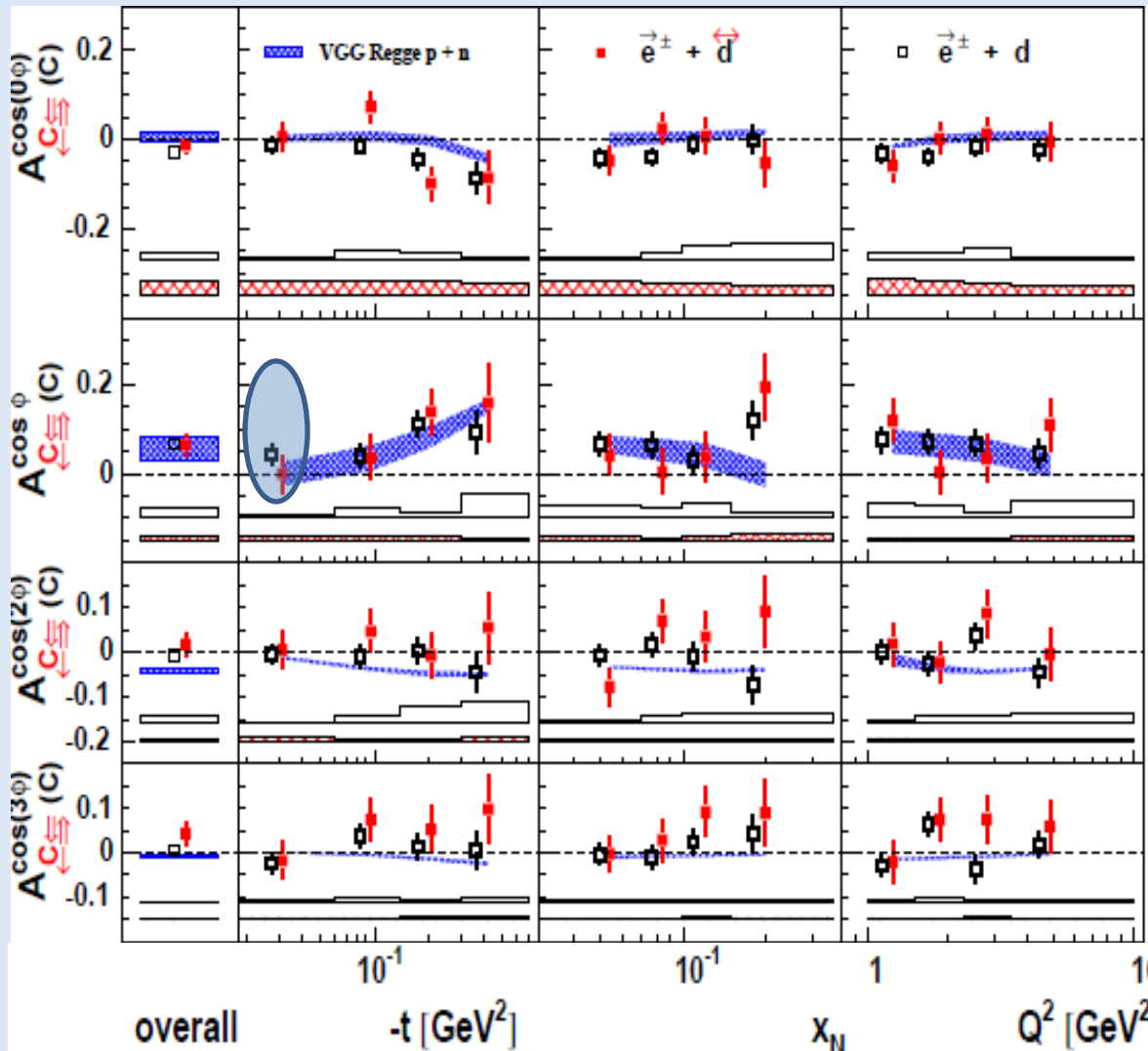


$\propto (BH)$

VGG:
 Phys. Rev. D60
 (1999) 0940177
 &
 Prog. Nucl. Phys.
 47 (2001) 401

$A_C (A_{C\leftrightarrow})$ on (un)polarized Deuterium

Nucl. Phys. B 842 (2011) 265



For coherent scattering

$$\Re(\mathcal{H}_1)$$

$$\Re(\mathcal{H}_1 - \frac{1}{3}\mathcal{H}_5)$$

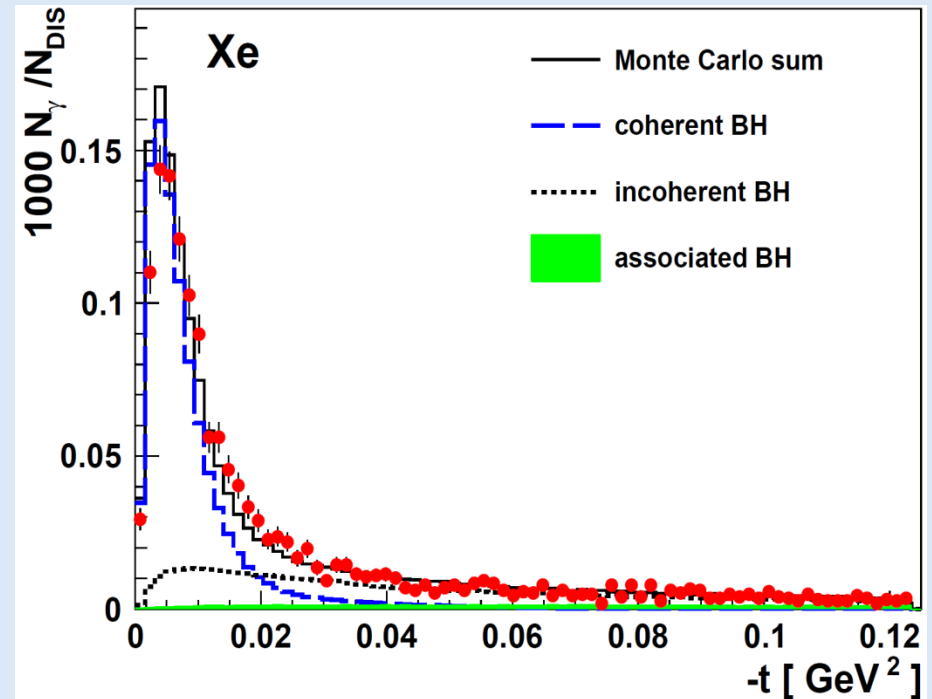
$$\Im(H_5)$$

A_{LZZ} sin ϕ amplitude:
 $0.074 \pm 0.196 \pm 0.022$
 ($-t < 0.06 \text{ GeV}^2$, 40% coherent)

Beam-charge /spin asymmetries on heavier nuclei

Phys. Rev. C 81 (2010) 035202

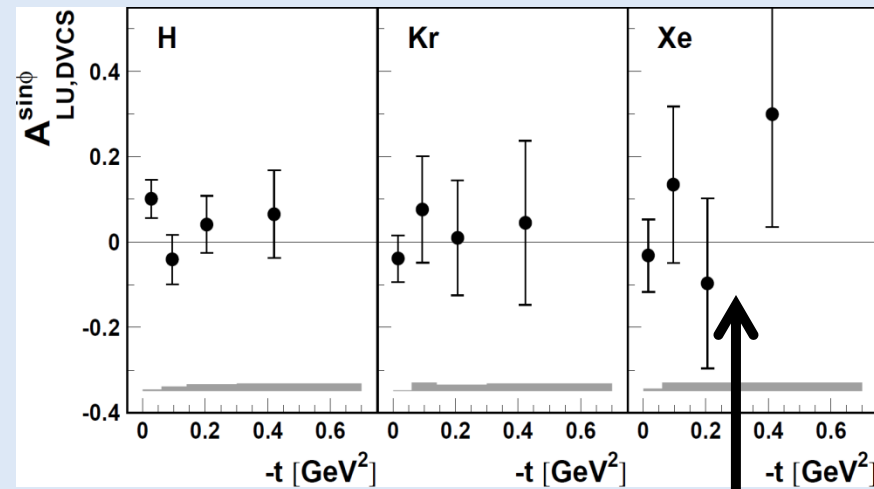
Target	Spin	L (pb ⁻¹)
¹ H	1/2	227
He	0	32
N	1	51
Ne	0	86
Kr	0	77
Xe	0, 1/2, 3/2	47



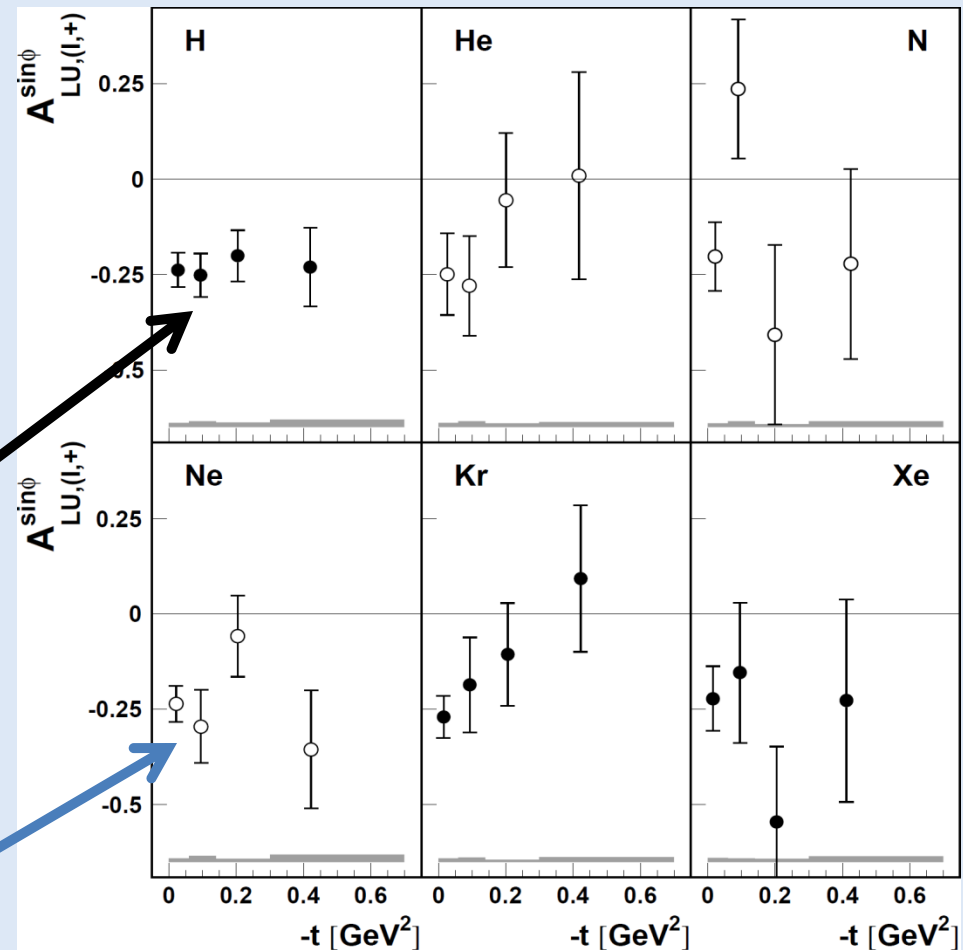
- Separation of coherent-enriched and incoherent-enriched data samples by t -cutoffs : similar average kinematics
- Coherent-enriched samples: $\approx 65\%$
- Incoherent enriched samples: $\approx 60\%$

Leading amplitudes of asymmetries on nuclei

Leading amplitude of
Beam-charge asymmetry



Leading amplitudes of
Beam-helicity asymmetry

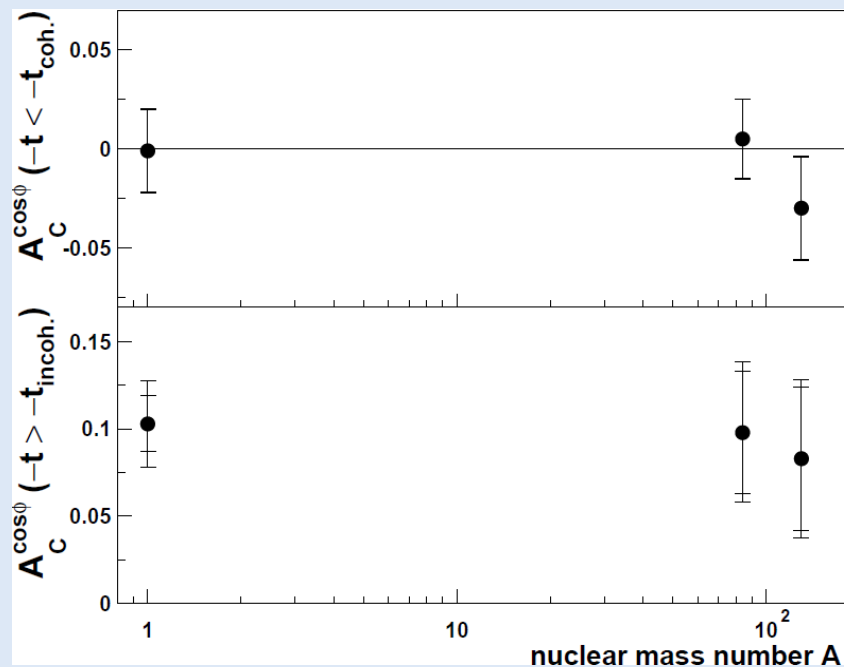


● Two beam charges available

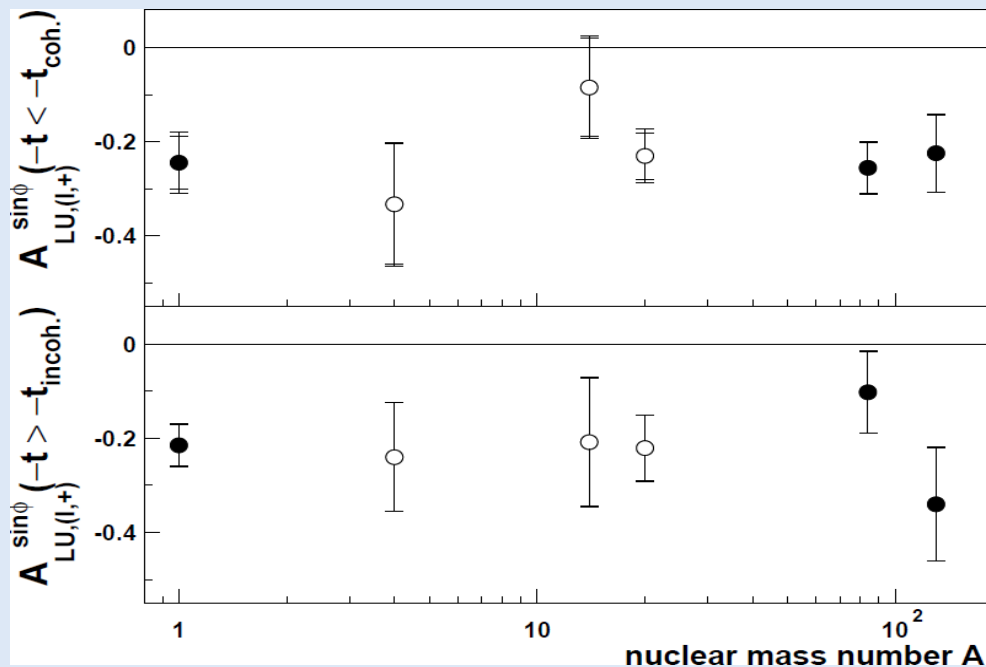
○ Only one beam charge available:
single-charge asymmetry without
entanglement of squared DVCS
and Interference terms

Nuclear-mass dependence of asymmetries

$A_C^{\cos\phi}$ vs. A



$A_{LU}^{\sin\phi}$ vs. A



$$A_{LU}^A / A_{LU}^H$$



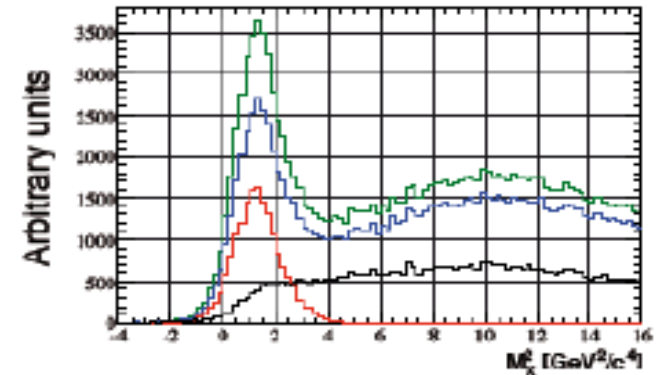
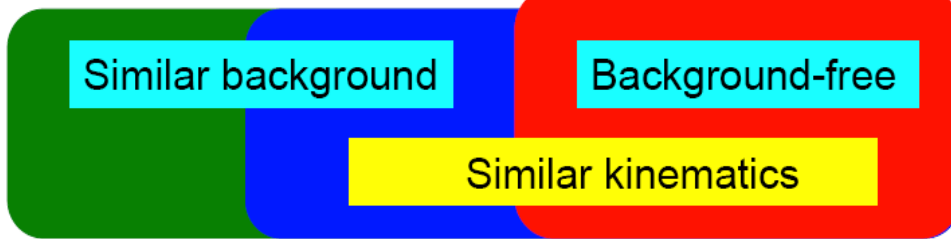
Coherent-enriched: 0.91 ± 0.19
 Incoherent-enriched: 0.93 ± 0.23

DVCS with recoil detector

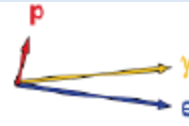
Without Recoil Detector

In Recoil Detector acceptance

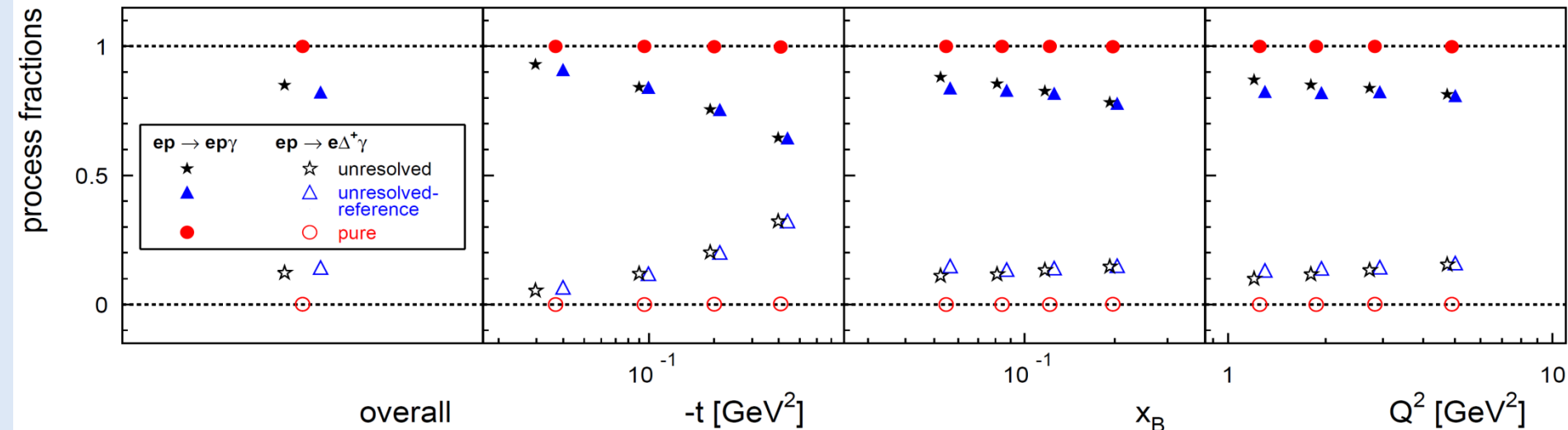
With Recoil Detector



Kinematic event fitting technique: all 3 particles
In the final state detected should satisfy
4-constraints on energy-momentum conservation



- No requirement for Recoil
- Charged recoil track in acceptance
- Kinematic fit probability > 1 %
- Kinematic fit probability < 1 %



Missing mass distribution: exclusivity with RD

Without Recoil Detector

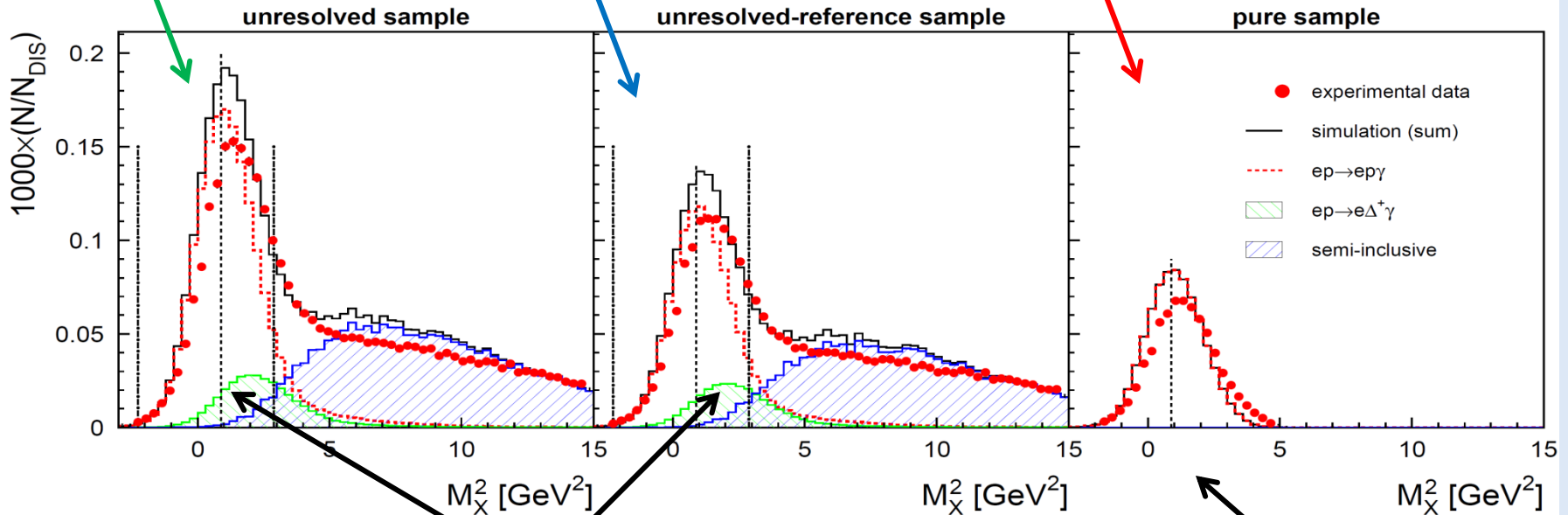
In Recoil Detector acceptance

With Recoil Detector

Similar background

Background-free

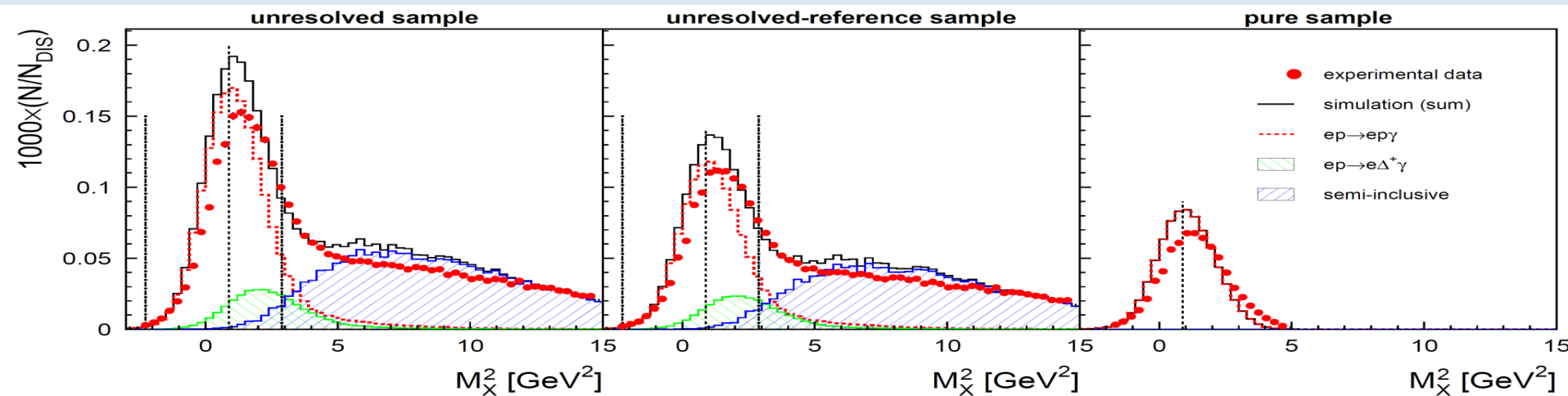
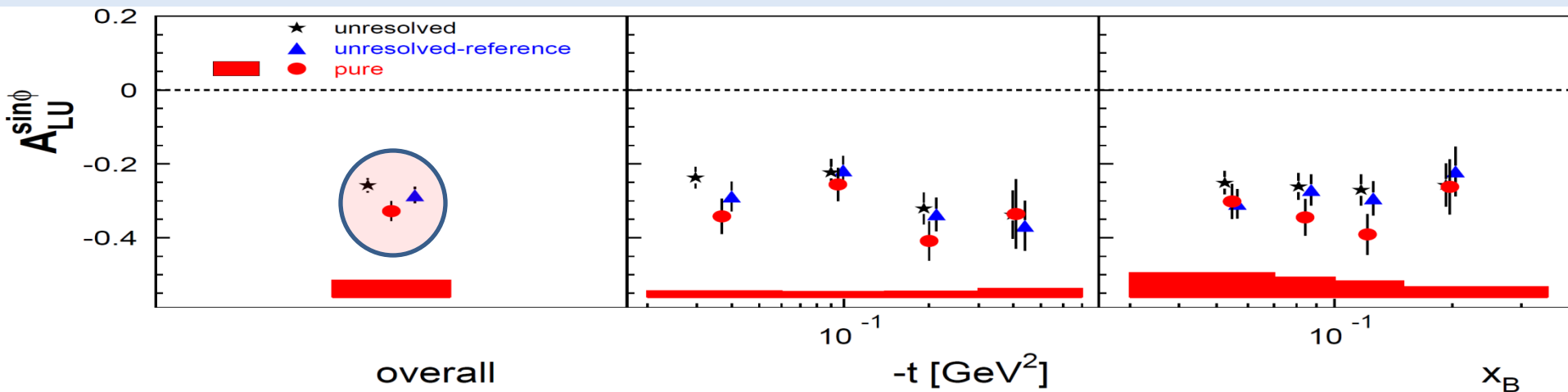
Similar kinematics



Associated processes (e p → e' γ Δ⁺)

Pure e p → e' γ p

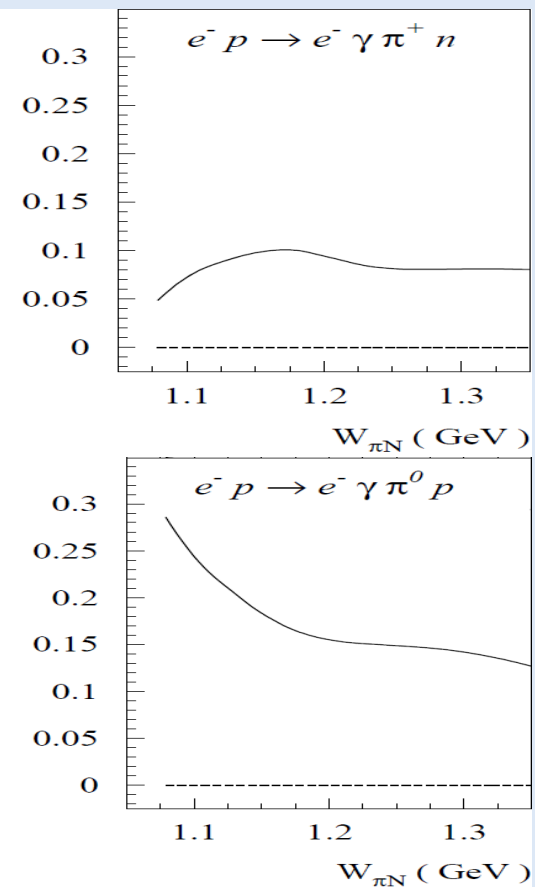
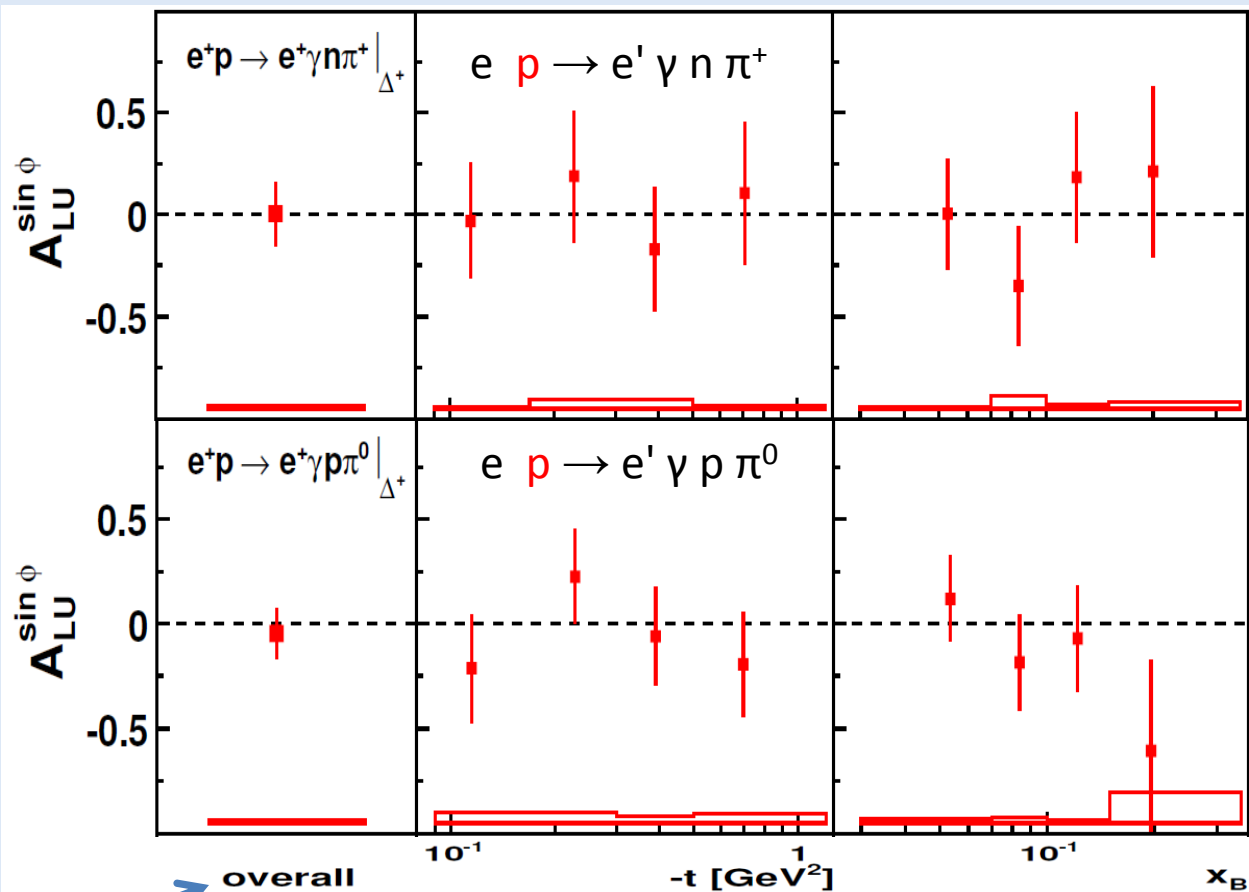
$$\text{Missing mass: } M_X^2 = (q + P - q')^2 = M^2 + 2M(v - E_\gamma + t)$$



- Practically no contamination of associated process.
- Indication that leading amplitude for pure elastic process is larger (0.054 ± 0.016) than for unresolved signal (elastic+associated).

Beam-spin asymmetry in „associated“ DVCS : $ep \rightarrow e\gamma\Delta^+$

JHEP 01 (2014) 077, arXiv:1206.5683



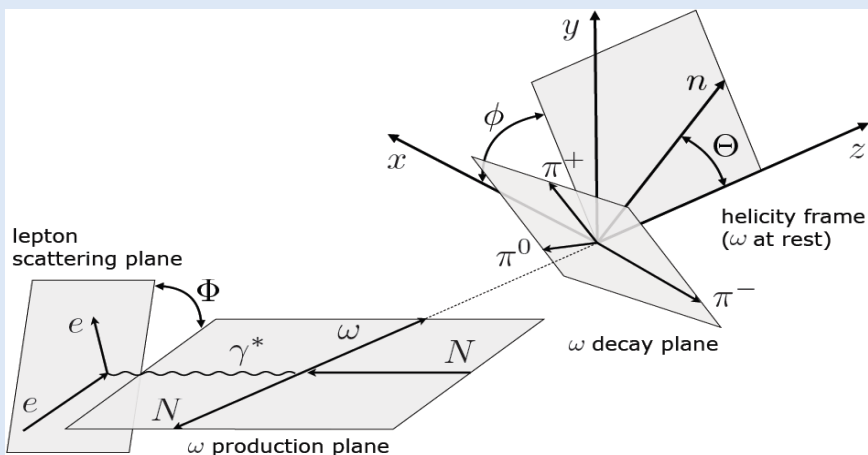
- **Associated DVCS/BH:** ($77 \pm 2\%$ for $n\pi^+$ & $85 \pm 1\%$ for $p\pi^0$)
- **Correction: π^0 SIDIS background:** ($23 \pm 3\%$ for $p\pi^0$ & $11 \pm 1\%$ for $n\pi^+$ channel);
- **Elastic:** ($0.2 \pm 0.1\%$ for $n\pi^+$ & $4.6 \pm 0.1\%$ for $p\pi^0$)

P. Guichon et al.,
PRD 68 (2003) 034018

Exclusive ω - meson production at HERMES

$$e(k) + N(p) \rightarrow e(k') + N(p') + \omega$$

$$\omega \rightarrow \pi^+ \pi^- \pi^0, \quad \pi^0 \rightarrow 2\gamma$$



Kinematic conditions:

$$1 \text{ GeV}^2 < Q^2 < 10 \text{ GeV}^2,$$

$$0.01 < x_B < 0.35,$$

$$3.0 \text{ GeV} < W < 6.3 \text{ GeV},$$

$$0 \leq -t' = -(t - t_{\min}) < 0.2 \text{ GeV}^2$$

Two photon invariant mass:

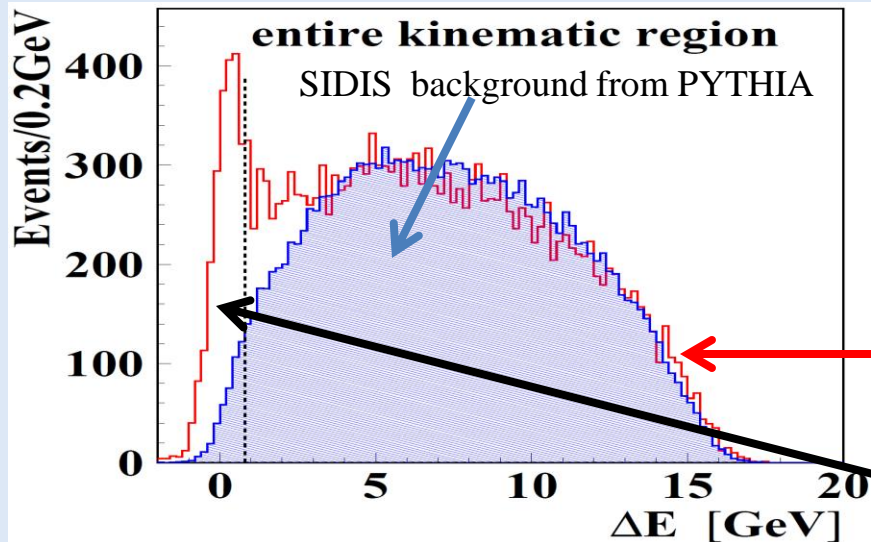
$$0.11 \text{ GeV} < M(\gamma\gamma) < 0.16 \text{ GeV}$$

Three-pion invariant mass:

$$0.71 \text{ GeV} < M(\pi^+ \pi^- \pi^0) < 0.87 \text{ GeV}$$

Missing energy:

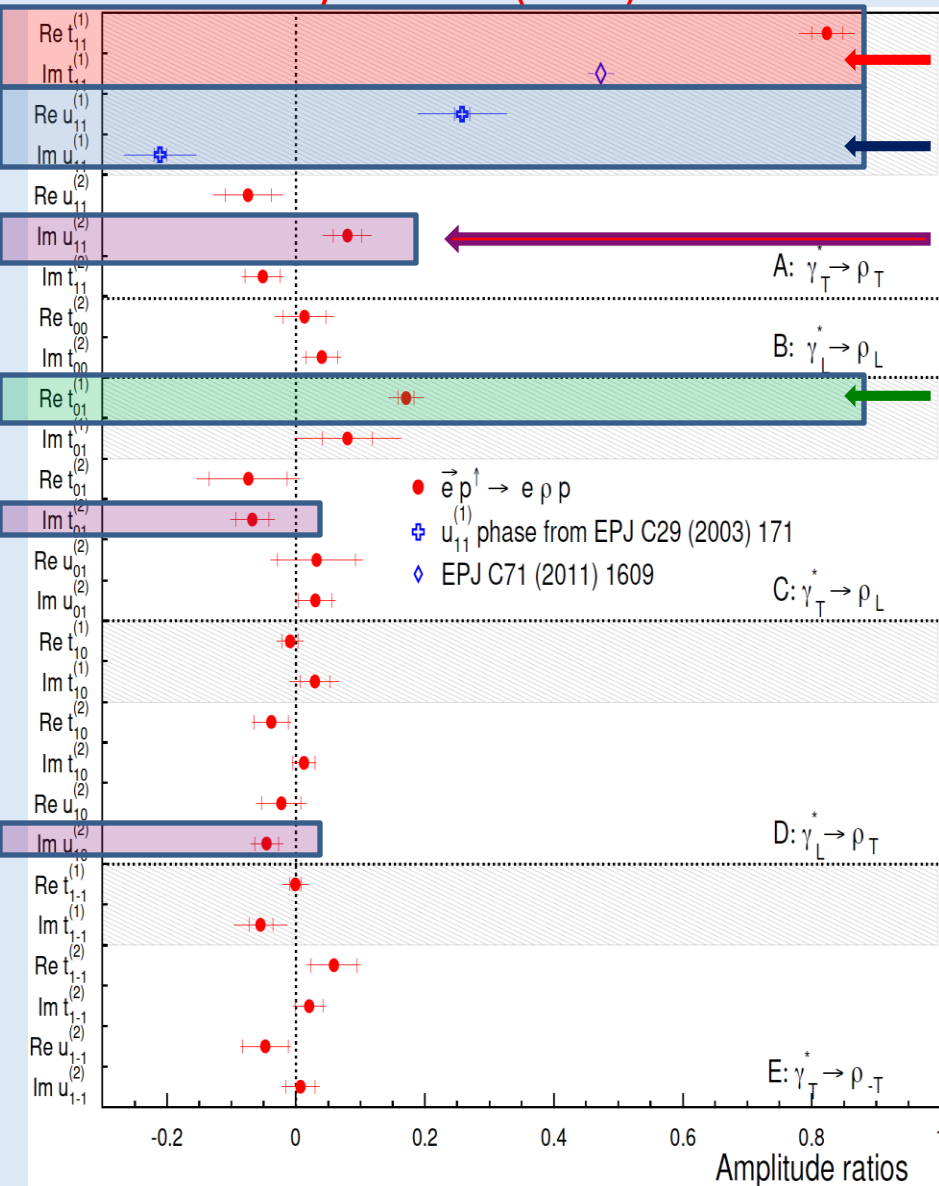
$$\Delta E = \frac{M_X^2 - M_p^2}{2M_p}, \quad M_X^2 = (p + q - p_{\pi^+} - p_{\pi^-} - p_{\pi^0})^2$$



Exclusive region: $-1.0 \text{ GeV} < \Delta E < 0.8 \text{ GeV}$

Exclusive ρ^0 – meson production: helicity ratios

Eur. Phys. J. C 77 (2017) 378



- Dominant amplitude: NPE nucleon-helicity non-flip $t_{11}^{(1)} \neq 0$ by $> 5\sigma$
- UPE nucleon-helicity non-flip $u_{11}^{(1)} \neq 0$ by $> 4\sigma$
- Nucleon-helicity flip $\text{Im } t_{01}^{(2)}, \text{Im } u_{11}^{(2)}, \text{Im } u_{10}^{(2)} \neq 0$ by 2σ
- Significant nucleon-helicity non-flip $\text{Re } t_{01}^{(1)} \neq 0$ by $> 5\sigma$
- Overall good agreement between direct extraction of SDMEs (Eur. Phys. J. C 71 (2011) 1609) and SDMEs via helicity amplitude ratios (not shown here).