# **Overview of HERMES results**

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#### XVII WORKSHOP ON <u>HIGH ENERGY SPIN</u> PHYSICS DSPIN – 17 Sept. 11 – 15, Dubna, Russia

- **•** The HERMES experiment.
- **9** 3D picture of the nucleon:
  - **9**  $A_{UT} \& A_{LT}, A_{LU}$  in semi-inclusive DIS.
  - **ω**-meson production:
    - SDMEs & A<sub>UT</sub> from exclusive DIS;
    - **Solution** Extraction of  $\pi\omega$  transition form factor.
  - **ρ**<sup>0</sup>-meson production:
    - Measurement of helicity amplitude ratios;





#### **HERMES at DESY**







Polarized hydrogen (Long., Trans.), deuterium (Long.) Polarization flipped at 60-180 s time interval Unpolarized *H*, *D*, *He*, *N*, *Ne*, *Kr*, *Xe* 

#### **The HERMES Spectrometer**



PID: RICH, TRD, Preshower and Calorimeter; lepton-hadron > 98%

**•** Momentum resolution of charged particles:  $\delta P/P \simeq 1.5\%$ 

#### **3D picture of the nucleon**



# $A_{\text{UT}}$ & $A_{\text{LT}}$ , $A_{\text{LU}}$ in semi-inclusive DIS

- Unpolarized & longitudinally polarized e<sup>+</sup>/e<sup>-</sup> beam
- Transversely polarized H target
- Unpolarized H & D targets

### **Semi-inclusive DIS processes (SIDIS)**



#### SIDIS processes:

- Describe spin-orbit correlation: correlations between the hadron transverse momentum and quark or nucleon spin
- Sensitive to quark orbital angular momentum

#### **The SIDIS cross-section**

$$\frac{d\sigma^{h}}{dx \, dy \, d\phi_{S} \, dz \, d\phi \, d\mathbf{P}_{hL}^{2}} = \frac{\alpha^{2} \, y^{2}}{xyQ^{2} \, 2(1-\epsilon)} \left(1 + \frac{\gamma^{2}}{2x}\right)$$

$$\left\{ \begin{array}{c} \left[F_{UU,T} + \epsilon F_{UU,L} + \sqrt{2\epsilon(1+\epsilon)} \cos(\phi) F_{UU}^{\cos(\phi)} + \epsilon \cos(2\phi) F_{UU}^{\cos(2\phi)}\right] \\ + \lambda_{l} \left[\sqrt{2\epsilon(1-\epsilon)} \sin(\phi) F_{UU}^{\sin(\phi)}\right] \\ + S_{L} \left[\sqrt{2\epsilon(1-\epsilon)} \sin(\phi) F_{UL}^{\sin(\phi)} + \epsilon \sin(2\phi) F_{UL}^{\sin(2\phi)}\right] \\ + S_{L} \lambda_{l} \left[\sqrt{1-\epsilon^{2}} F_{LL} + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi) F_{LL}^{\cos(\phi)}\right] \\ + S_{T} \left[\sin(\phi - \phi_{S}) \left(F_{UT,T}^{\sin(\phi - \phi_{S})} + \epsilon F_{UT,L}^{\sin(\phi - \phi_{S})}\right) \\ + \epsilon \sin(\phi + \phi_{S}) F_{UT}^{\sin(\phi + \phi_{S})} + \epsilon \sin(3\phi - \phi_{S}) F_{UT}^{\sin(3\phi - \phi_{S})} \\ + \sqrt{2\epsilon(1+\epsilon)} \sin(\phi + \phi_{S}) F_{UT}^{\sin(\phi + \phi_{S})}\right] \\ + S_{T} \lambda_{l} \left[\sqrt{1-\epsilon^{2}} \cos(\phi - \phi_{S}) F_{UT}^{\sin(\phi + \phi_{S})}\right] \\ + S_{T} \lambda_{l} \left[\sqrt{1-\epsilon^{2}} \cos(\phi - \phi_{S}) F_{UT}^{\cos(\phi - \phi_{S})} \\ + \sqrt{2\epsilon(1+\epsilon)} \sin(2\phi - \phi_{S}) F_{UT}^{\cos(\phi - \phi_{S})}\right] \\ + S_{T} \lambda_{l} \left[\sqrt{1-\epsilon^{2}} \cos(\phi - \phi_{S}) F_{UT}^{\cos(\phi - \phi_{S})} \\ + \sqrt{2\epsilon(1-\epsilon)} \cos(\phi + \phi_{S}) F_{UT}^{\cos(\phi - \phi_{S})}\right] \right\}$$

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#### **Transversely polarized quarks: Collins effect for pions**



#### Phys. Lett. B 693 (2010) 11



- Opposite in sign for charged pions
- Disfavored Collins FF large and opposite in sign to favored one

#### **Transversely polarized quarks: Collins effect for pions**



- Opposite in sign for charged pions
- Disfavored Collins FF large and opposite in sign to favored one
- 3D projections allow to constrain global fits in a more profound way
- $\bullet$   $\pi^-$  amplitudes increasing with x at large  $P_{h\perp}$

### **Collins effect for kaons and (anti) protons**

 $F_{UT}^{\sin(\phi_h+\phi_S)} \propto h_1(x,p_T^2) \otimes H_1^{\perp}(z,k_T^2)$ Phys. Lett. B 693 (2010) 11 0.3 0.15 ⟨sin(∳+∲<sub>S</sub>))<sup>K</sup>UT ⟨sin(∳-∲<sub>S</sub>)⟩<sub>U⊥</sub> K⁺ PRELIMINARY HERMES 0.25 7.3% scale uncertainty 0.2 p 0.1 0.15 0.1 0.05 0.05 2 -0 0 -0.05 -0.1 2 -0.15 -0.05 -0.2 0.35 K 0.1 0.3 0.25 p 0.05 0.2 0.15 0 0.1 0.05 -0.05 -0 -0.05 -0.1 -0.1 -1 0.4 0.6 0.5 -0.15 10  $\mathbf{P}_{h\perp}^{0.5}$  [GeV] 0.1 0.2 0.2 0.4 0.6 0 P<sub>h⊥</sub> [GeV] Х Ζ Х Ζ

- Positive Collins SSA amplitude for positive kaons
- Consistent with zero for negative kaons and (anti)protons
- Vanishing sea-quark transversity?

#### **Sivers amplitudes for mesons**

Phys. Lett. B 693 (2010) 11

$$F_{UT}^{\sin(\phi_h-\phi_S)} \propto f_{1T}^{\perp}\left(x, p_T^2\right) \otimes D_1\left(z, k_T^2\right)$$



Larger amplitudes for positive kaons vs. pions

#### **Sivers amplitudes for baryons**

Phys. Lett. B 693 (2010) 11







 Similar amplitudes for positive pions and protons

u-quark dominance (and not a FF effect)?

#### The SIDIS cross-section: A<sub>LU</sub> amplitudes

$$\begin{split} \frac{d\sigma}{dx\,dy\,d\psi\,dz\,d\phi_{h}\,dP_{h\perp}^{2}} &= \\ \frac{\alpha^{2}}{xyQ^{2}}\frac{y^{2}}{2\left(1-\varepsilon\right)}\left(1+\frac{\gamma^{2}}{2x}\right)\left\{F_{UU,T}+\varepsilon F_{UU,L}+\sqrt{2\,\varepsilon(1+\varepsilon)}\,\cos\phi_{h}\,F_{UU}^{\cos\phi_{h}}\right.\\ &+\varepsilon\cos(2\phi_{h})\,F_{UU}^{\cos2\phi_{h}}+\lambda_{e}\,\sqrt{2\,\varepsilon(1-\varepsilon)}\,\sin\phi_{h}F_{LU}^{\sin\phi_{h}}\right.\\ &+S_{\parallel}\left[\sqrt{2\,\varepsilon(1+\varepsilon)}\,\sin\phi_{h}\,F_{UL}^{\sin\phi_{h}}+\varepsilon\sin(2\phi_{h})\,F_{UL}^{\sin2\phi_{h}}\right] \\ &+S_{\parallel}\lambda_{e}\left[\sqrt{1-\varepsilon^{2}}\,F_{LL}+\sqrt{2\,\varepsilon(1-\varepsilon)}\,\cos\phi_{h}\,F_{LL}^{\cos\phi_{h}}\right] \\ &+|S_{\perp}|\left[\sin(\phi_{h}-\phi_{S})\left(F_{UT,T}^{\sin(\phi_{h}-\phi_{S})}+\varepsilon\,F_{UT,L}^{\sin(\phi_{h}-\phi_{S})}\right)\right.\\ &+\varepsilon\sin(\phi_{h}+\phi_{S})\,F_{UT}^{\sin(\phi_{h}+\phi_{S})}+\varepsilon\,\sin(3\phi_{h}-\phi_{S})\,F_{UT}^{\sin(3\phi_{h}-\phi_{S})} \\ &+\sqrt{2\,\varepsilon(1+\varepsilon)}\,\sin\phi_{S}\,F_{UT}^{\sin\phi_{S}}+\sqrt{2\,\varepsilon(1+\varepsilon)}\,\sin(2\phi_{h}-\phi_{S})\,F_{UT}^{\sin(2\phi_{h}-\phi_{S})} \\ &+|S_{\perp}|\lambda_{e}\left[\sqrt{1-\varepsilon^{2}}\,\cos(\phi_{h}-\phi_{S})\,F_{LT}^{\cos(\phi_{h}-\phi_{S})}+\sqrt{2\,\varepsilon(1-\varepsilon)}\,\cos\phi_{S}\,F_{LT}^{\cos\phi_{S}}\right.\\ &+\left.\left.\left.\left.\left.\left.\left(\sqrt{1-\varepsilon^{2}}\,\cos(\phi_{h}-\phi_{S})\,F_{LT}^{\cos(2\phi_{h}-\phi_{S})}\right)\right.\right.\right.\right.\right\}, \end{split}$$



In case of longitudinal beam (L) and unpolarized target (U) only target spin-independent parts can contribute to the asymmetry. The structure function of interest :



#### **A<sub>LU</sub> amplitudes: Subleading twist**



Significant positive amplitudes for (in particular positive) pions

#### **A<sub>LU</sub> amplitudes: Subleading twist**

 $F_{LU}^{\sin(\phi_h)} \propto \frac{M_h}{M_z} h_1^{\perp} E \oplus xg^{\perp} D_1 \oplus \frac{M_h}{M_z} f_1 G^{\perp} \oplus xeH_1^{\perp} \quad \text{Convolution of twist-2 \& twist-3}$ 



Mostly consistent with zero for other hadrons (except maybe K<sup>+</sup>)

#### **A<sub>LU</sub>** amplitudes: Subleading twist; 3D extraction





**9** 3D projections allow to constrain global fits in a more profound way

#### **A<sub>LU</sub>** amplitudes: Subleading twist





- Opposite behavior at HERMES/CLAS negative pions in z projection due to x-range probed in different experiments.
- CLAS is more sensitive to e(x) Collins term due to higher x? Hrachya Marukyan, 11.09.2017, DSPIN-17, Dubna, Russia

#### **A<sub>LU</sub>** amplitudes: Subleading twist





Consistent behavior for charged pions (hadrons) at HERMES/COMPASS for isoscalar targets

# ω-meson production from exclusive DIS: SDMEs & A<sub>UT</sub>

- Unpolarized & longitudinally polarized e<sup>+</sup>/e<sup>-</sup> beam
- Unpolarized H & D targets
- Transversely polarized H targets

#### **Exclusive meson production**



- Probes various types of GPDs with different sensitivity and different flavour combinations
- Complementary to DVCS process
- Unpolarized target: nucleon-helicity-non-flip GPDs H,  $\tilde{H}$  and  $\bar{E}_{T}=2\tilde{H}_{T}+E_{T}$ .
  - Transversely polarized target: nucleon-helicity-flip GPDs  $E, \tilde{E}$  and  $H_{T}$ .



NPE  $(J^P = 0^+, 1^-, 2^+ ...)$  (two-gluon exchange = pomeron,  $\rho$ ,  $\omega$ ,  $f_2$ ,  $a_2$ , ... reggeons =  $\overline{q}q$  exchange). UPE  $(J^P = 0^-, 1^+, ...)$  ( $\pi$ ,  $a_1$ ,  $b_1$ ,... reggeons =  $\overline{q}q$  exchange)

## **Angular distribution and extraction of SDMEs**

Photon SDMEs

Three-dimensional angular distribution  $W^{U+L}(\Phi, \phi, \cos \Theta)$ depends linearly on SDMEs –  $r^{\alpha}_{\lambda_{v}\lambda'_{v}}$  and beam polarization  $P_{b}$ 

 $\mathbf{r}^{\alpha}_{\lambda_{\mathbf{v}}\lambda_{\mathbf{v}}'} \sim \rho_{\lambda_{\mathbf{v}}\lambda_{\mathbf{v}}'} = \frac{1}{2N} \sum_{\lambda_{\mathbf{v}}\lambda_{\mathbf{v}}'\lambda_{\mathbf{v}}} F_{\lambda_{\mathbf{v}}\lambda_{\mathbf{v}}'\lambda_{\mathbf{v}}} \sum_{\lambda_{\mathbf{v}}\lambda_{\mathbf{v}}'\lambda_{\mathbf{v}}'\lambda_{\mathbf{v}}'\lambda_{\mathbf{v}}'} F_{\lambda_{\mathbf{v}}'\lambda_{\mathbf{v}'}'\lambda_{\mathbf{v}'}'\lambda_{\mathbf{v}'}'\lambda_{\mathbf{v}}'\lambda_{\mathbf{v}}'\lambda_{\mathbf{v}}'\lambda_{\mathbf{v}}'\lambda_{\mathbf{v}}'\lambda_{\mathbf{v}'}$ 



- Helicity amplitudes are the fundamental quantities to be compared with theory.
- They form a basis for the SDMEs.
- For longitudinally polarized beam and unpolarized target there are 23 SDMEs:
   15 unpolarized and 8 polarized.
- The SDMEs are extracted by fitting the angular distribution  $W^{U+L}(\Phi, \phi, \cos \Theta)$  to the experimental angular distribution of pions from  $\omega$  decay using unbinned Maximum Likelihood method.

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Helicity amplitudes

#### **Exclusive ω - meson production at HERMES**



#### SDMEs in exclusive *w* production



#### **Extraction of \pi\omega transition form factor**

$$u_1 = 1 - r_{00}^{04} + 2r_{1-1}^{04} - 2r_{11}^1 - 2r_{1-1}^1$$

#### Eur. Phys. J. C 74 (2014) 3110





Only the magnitude of the  $\pi\omega$  transition form factor (not the sign) can be evaluated.

- The solid line show the calculation of the GK model with pion-pole contribution Dashed line are the model results without the pion-pole.
- The pion-pole contribution seems to account comletely for UPE.

#### Exclusive $\omega$ - meson production: A<sub>UT</sub> asymmetry

$$e(k) + N(p) \rightarrow e(k') + N(p') + \omega$$
$$\omega \rightarrow \pi^{+} \pi^{-} \pi^{0}, \pi^{0} \rightarrow 2\gamma$$

#### Angular dependent part

$$w(\phi, \phi_{S}) = 1 + A_{UU}^{\cos(\phi)} \cos(\phi) + A_{UU}^{\cos(2\phi)} \cos(2\phi) + S_{\perp} \left[ A_{UT}^{\sin(\phi+\phi_{S})} \sin(\phi+\phi_{S}) + A_{UT}^{\sin(\phi-\phi_{S})} \sin(\phi-\phi_{S}) + A_{UT}^{\sin(\phi+\phi_{S})} \sin(\phi_{S}) + A_{UT}^{\sin(2\phi-\phi_{S})} \sin(2\phi-\phi_{S}) + A_{UT}^{\sin(3\phi-\phi_{S})} \sin(3\phi-\phi_{S}) \right]$$
$$w(\phi, \phi_{S}, \theta) = \frac{3}{2} r_{00}^{04} \cos^{2}(\theta) w_{L}(\phi, \phi_{S}) + \frac{3}{4} (1 - r_{00}^{04}) \sin^{2}(\theta) w_{T}(\phi, \phi_{S})$$

$$w_{L}(\phi,\phi_{S}) = 1 + A_{UU,L}(\phi) + S_{\perp}A_{UT,L}(\phi,\phi_{S})$$
$$w_{T}(\phi,\phi_{S}) = 1 + A_{UU,T}(\phi) + S_{\perp}A_{UT,T}(\phi,\phi_{S})$$

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Fit angular distributions of  $\omega$ -decay pions

 $S_1$ 

## Exclusive ω - meson production: amplitudes of A<sub>UT</sub>



- **The solid (dash-dotted) lines show the calculation of the GK model** for a positive (negative)  $\pi\omega$  transition form factor
- Dashed lines are the model results without the pion pole.

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# ρ<sup>0</sup> –meson production from exclusive DIS: Ratios of helicity amplitudes

Transversely polarized H target

## Exclusive $\rho^0$ – meson production , helicity ratios

$$\begin{aligned} \mathbf{e}(\mathbf{k}) + \mathbf{N}(\mathbf{p}) &\rightarrow \mathbf{e}(\mathbf{k}') + \mathbf{N}(\mathbf{p}') + \rho^{0} \\ \rho^{0} &\rightarrow \pi^{+} \pi^{-} \end{aligned}$$



#### **Exclusive ρ<sup>0</sup> – meson production: helicity ratios**



#### **Summary**

- **9** 3D picture of the nucleon:
  - A<sub>UT</sub> and A<sub>LT</sub> in semi-inclusive DIS: 3D extraction, including protons: contribute to understanding of various TMD PDFs @ twist 2 and twist 3.
  - A<sub>LU</sub> in semi-inclusive DIS: 3D extraction.
- **\_** Measurement of ω –meson SDMEs & A<sub>UT</sub> asymmetry amplitudes from exclusive DIS: good model description with inclusion of pion pole.
  - $\checkmark$  The sign of the  $\pi\omega$  transition form factor
- Measurement of helicity ratios from exclusive ρ<sup>0</sup> –meson production in DIS: model description with inclusion of pion pole.

## Thank You

#### **Backup slides**

# **Backup Slides**

#### **Sivers amplitudes**



**•**  $\pi^+$  amplitudes positive;  $\pi^-$  amplitudes  $\approx 0$ 

 $\bullet$   $\pi^+$  amplitudes increasing with x at large  $P_{h\perp}$ 

#### **Sivers amplitudes**



- $\bullet$  K<sup>+</sup> amplitudes positive, larger than  $\pi^+$
- Non-trivial role of sea quarks?

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## A<sub>LU</sub> amplitudes: K<sup>±</sup>





#### A<sub>LU</sub> amplitudes: p & p<sup>bar</sup>



