
Spin Structure of Nucleons

XXVI Physics in Collisions, Búzios, Brazil, July 6-9 2006

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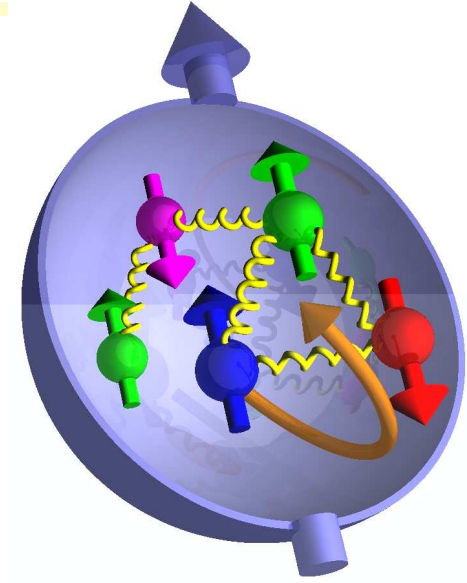
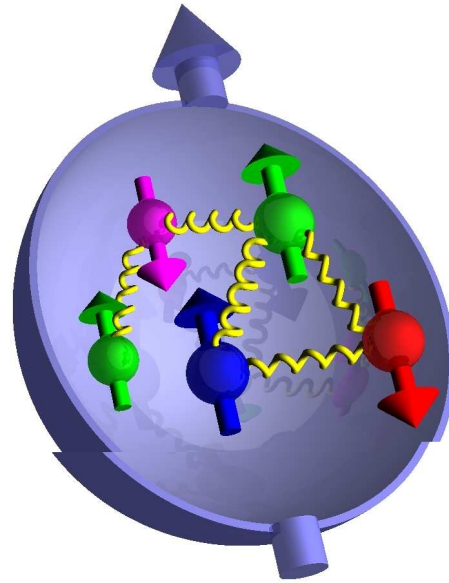
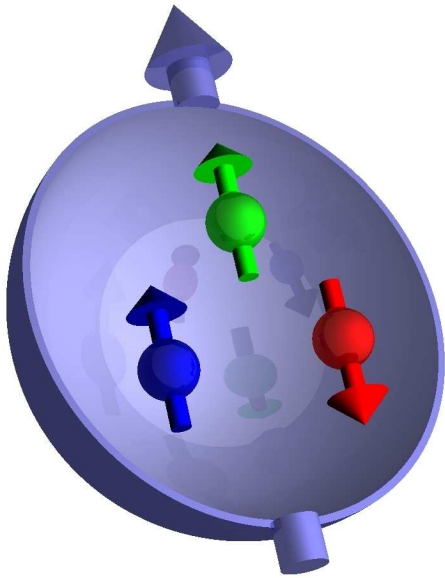
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Spin Budget of the Proton



Naive Quark-Parton Model:

● $\Delta q_u = \frac{4}{3} \quad \Delta q_d = -\frac{1}{3}$

$\Delta\Sigma = \Delta q_u + \Delta q_d + \Delta q_s = 1$

Relat. Quark-Parton Model:

● Quark spin: $\Delta\Sigma \approx 0.6$

EMC [PLB206(1988)364]:

$\Delta\Sigma = 0.060 \pm 0.047 \pm 0.069$

HERA collider results:

● Gluons are important

\implies **Measure $\Delta G!$**

at: COMPASS, HERMES, RHIC

Since: $\Delta q_f = \Delta q_f^{val} + \Delta q_f^{sea}$

\implies **Measure $\Delta q_f^{sea}!$**

at: HERMES, polar. RHIC

Proton spin budget:

● $J = \frac{1}{2} = J^Q(\mu) + J^G(\mu)$

● $J^G = \Delta G + L^G$

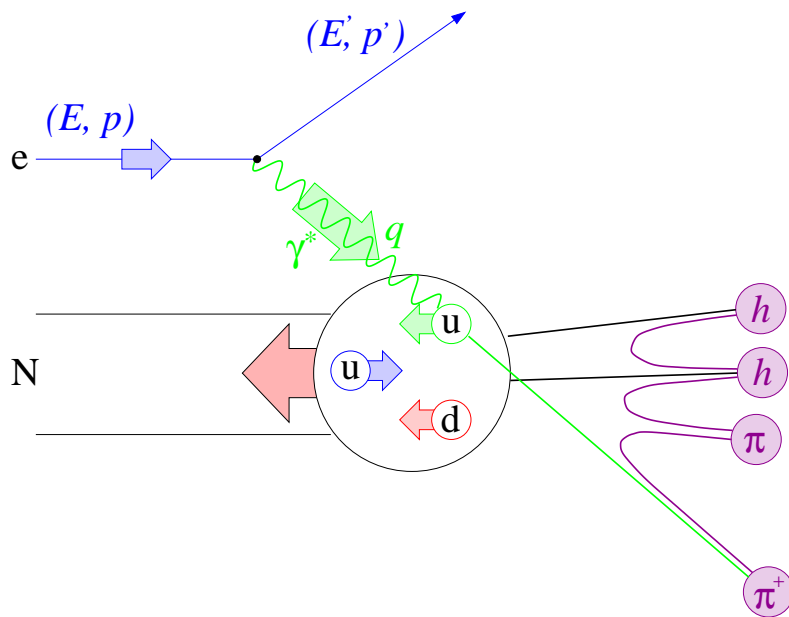
● $J^Q = \frac{1}{2}\Delta\Sigma + L^Q$

L^Q : Quark orb. ang. mom.

\implies **Measure J^Q : DVCS!**

at: HERMES, JLAB

DIS: Kinematics, Cross Sections, Asymmetry



Virtual-photon kinematics:

$$Q^2 = -q^2 \quad \nu = E - E'$$

Fraction of nucleon momentum

carried by struck quark: $x = \frac{Q^2}{2M\nu}$

fraction of virtual-photon energy

carried by produced hadron h : $z = \frac{E_h}{\nu}$

Hadron transverse momentum: $P_{h\perp}$

● Unpolarized cross section:

$$\sigma_{UU} \equiv \frac{1}{2} (\sigma^{\leftarrow\leftarrow} + \sigma^{\rightarrow\rightarrow})$$

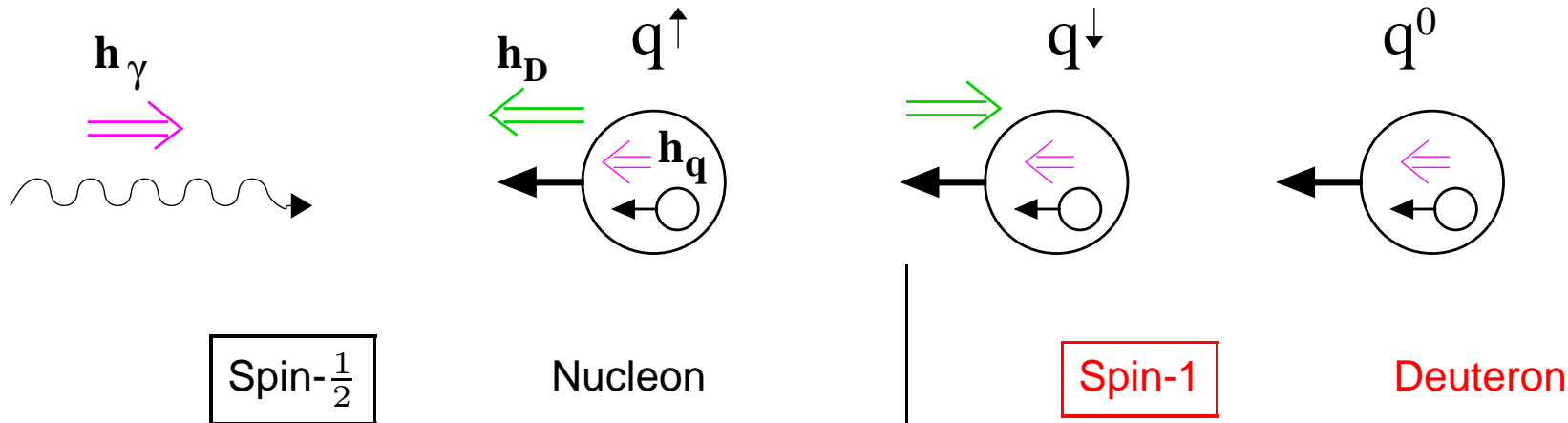
● Cross section (helicity) difference:

$$\sigma_{LL} \equiv \frac{1}{2} (\sigma^{\leftarrow\leftarrow} - \sigma^{\rightarrow\rightarrow})$$

● Double-spin asymmetry: $A_{||} \equiv \frac{\sigma_{LL}}{\sigma_{UU}} \simeq \frac{g_1}{F_1}$ (neglecting small g_2 contribution)

● Measured asymmetry: $A_{||} = \frac{1}{\langle P_T \rangle \langle P_B \rangle} \frac{(\frac{N}{L})^{\leftarrow\leftarrow} - (\frac{N}{L})^{\rightarrow\rightarrow}}{(\frac{N}{L})^{\leftarrow\leftarrow} + (\frac{N}{L})^{\rightarrow\rightarrow}}$

DIS Structure Functions in Quark-Parton Model



$$F_1^{p,n} = \frac{1}{2} \sum_f e_f^2 (q_f^{\rightarrow} + q_f^{\leftarrow}) = \frac{1}{2} \sum_f e_f^2 q_f$$

$$g_1^{p,n} = \frac{1}{2} \sum_f e_f^2 (q_f^{\rightarrow} - q_f^{\leftarrow}) = \frac{1}{2} \sum_f e_f^2 \Delta q_f$$

$$F_1^d = \frac{1}{3} \sum_f e_f^2 (q_f^{\rightarrow} + q_f^{\leftarrow} + q^0)$$

$$g_1^d = \frac{1}{2} \sum_f e_f^2 (q_f^{\rightarrow} - q_f^{\leftarrow})$$

$$b_1^d = \frac{1}{2} \sum_f e_f^2 (2q_f^0 - (q_f^{\rightarrow} + q_f^{\leftarrow}))$$

- g_1 measures a certain combination of quark + anti-quark helicity distributions $\Delta q_f = \Delta q_f^{val} + \Delta q_f^{sea}$
- ⇒ No new g_1 data published by HERMES or COMPASS during last 12 months
- b_1^d measures nuclear effects that make the deuteron look different from just the most simple proton-neutron system

Tensor Asymmetry in DIS on Deuteron

$$\frac{d^2\sigma_{\text{meas}}}{dx dQ^2} = \frac{d^2\sigma_{\text{unpol}}}{dx dQ^2} \left[1 - P_z P_B D A_1 + \frac{1}{2} P_{zz} A_{zz} \right]$$

- $\sigma_{\text{unpol}} = \sigma^{\uparrow\uparrow} + \sigma^{\uparrow\downarrow} + \sigma^0$

- $P_{zz} = \frac{n^+ + n^- - 2n^0}{n^+ + n^- + n^0}$

$$A_{zz} = \frac{(\sigma^{\uparrow\uparrow} + \sigma^{\uparrow\downarrow}) - 2\sigma^0}{3\sigma_{\text{unpol}} P_{zz}^0}$$

	vector term	tensor term
$\sigma^{\uparrow\uparrow}$	$+ P_z \cdot P_B $	$+P_{zz}^0$
$\sigma^{\uparrow\downarrow}$	$- P_z \cdot P_B $	$+P_{zz}^0$
σ_0	< 0.01	$-2P_{zz}^0$

$$|P_z \cdot P_B| = 0.45 \pm 0.04$$

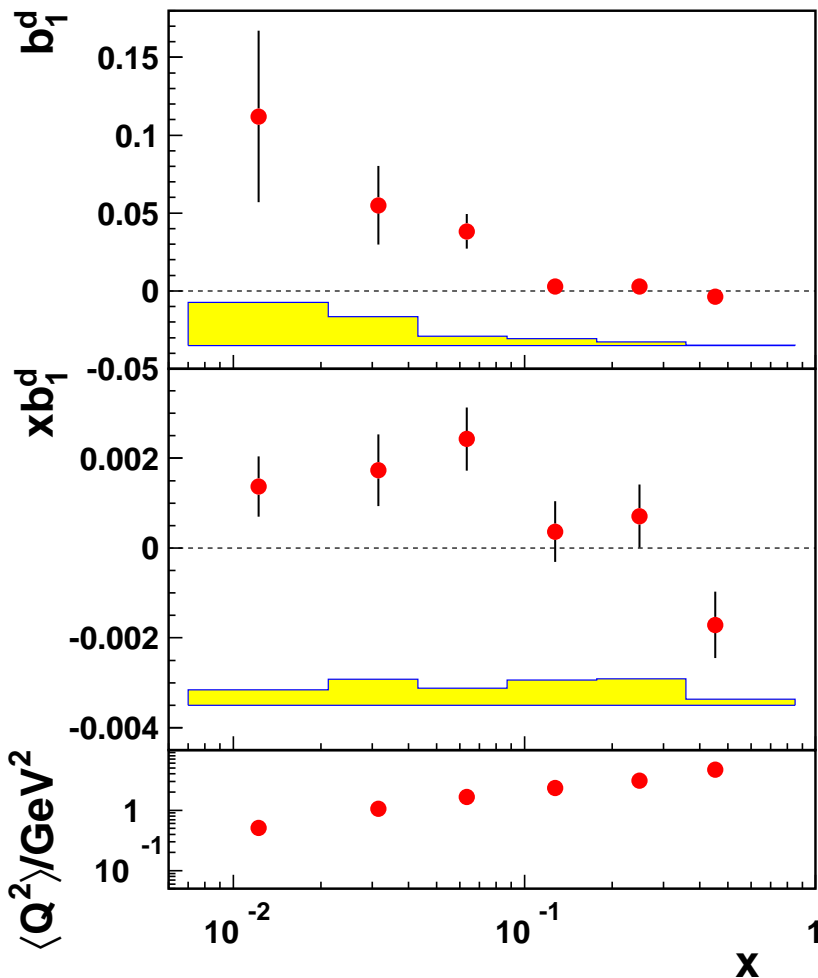
$$P_{zz}^0 = 0.83 \pm 0.03$$

Tensor structure function b_1 from tensor asymmetry A_{zz} :

$$b_1^d = -\frac{3}{2} A_{zz}^d F_1^d$$

$$F_1^d = \frac{(1 + Q^2/\nu^2) F_2^d}{2x(1+R)}$$

Tensor Structure Function $b_1^d(\mathbf{x})$



← HERMES result [PRL95 (2005) 242001]

Theory work < 1997:

- binding&Fermi motion effects at $x \geq 0.2$

Theory \geq 1997: Double scattering

- diffr.nucl.shadowing+pion excess mech. Nikolaev et al., PLB 398, 245 (1997)
- coherent double scattering Edelman et al., PRC 57, 3392 (1998)
- double scattering through VMD Bora & Jaffe, PRD 57, 6906 (1998)

↪ observe significant enhancement of b_1 at small x_B :

▷ Close-Kumano sum rule $\int dx b_1(x, Q^2) = 0$ violated ??

▷ interpretable as tensor polarization of the quark sea ?

Sea Quark Flavor Asymmetry

⇐ HERMES: 5-parameter flavor separation

[PRD 71(2005) 012003]: semi-inclusive pion & kaon and inclusive asymmetries:

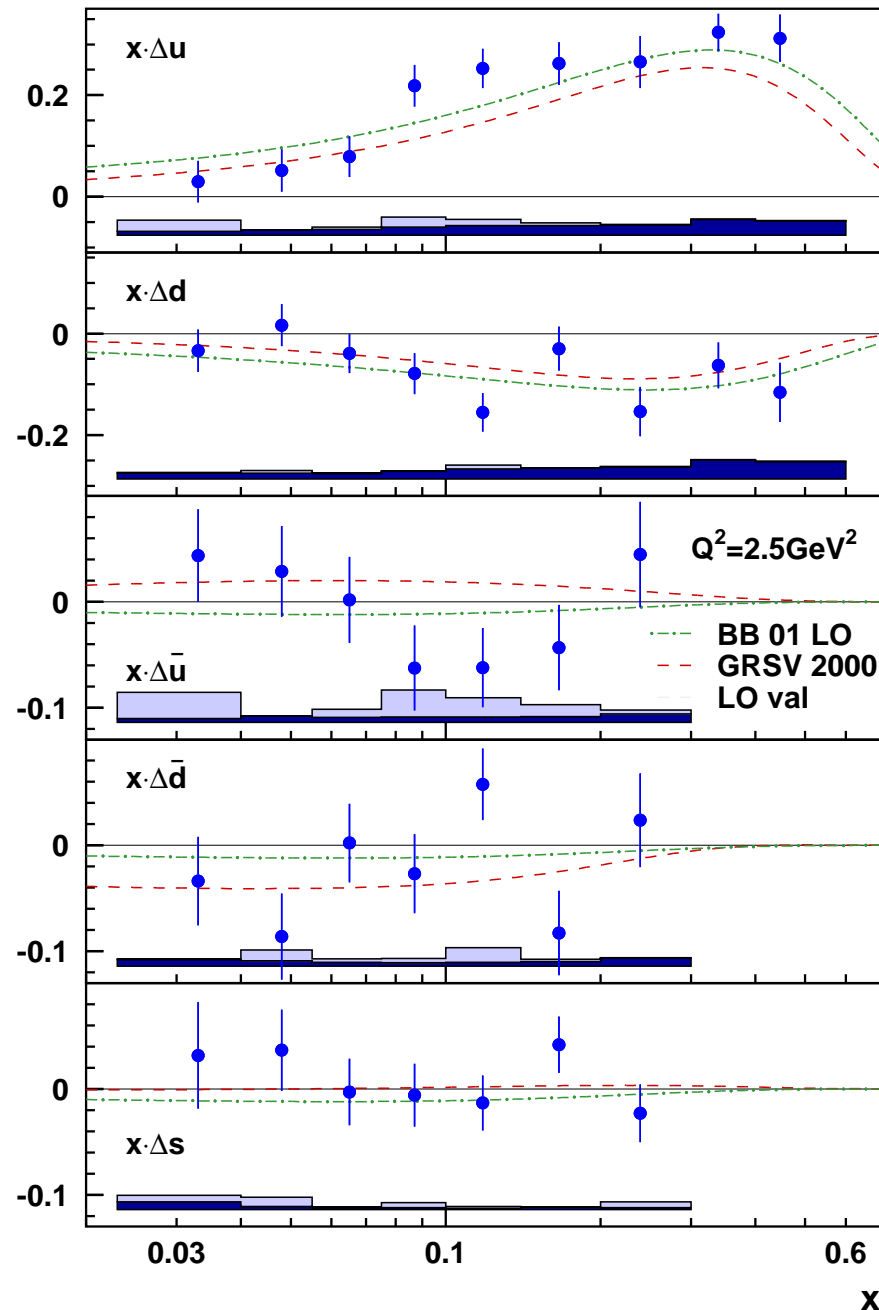
$$A_1^h(x, z) \propto \frac{\sum_f e_f^2 \Delta q_f(x) D_f^h(z)}{\sum_f e_f^2 q_f(x) D_f^h(z)}$$

with $D_f^h(z)$: Fragmentation function

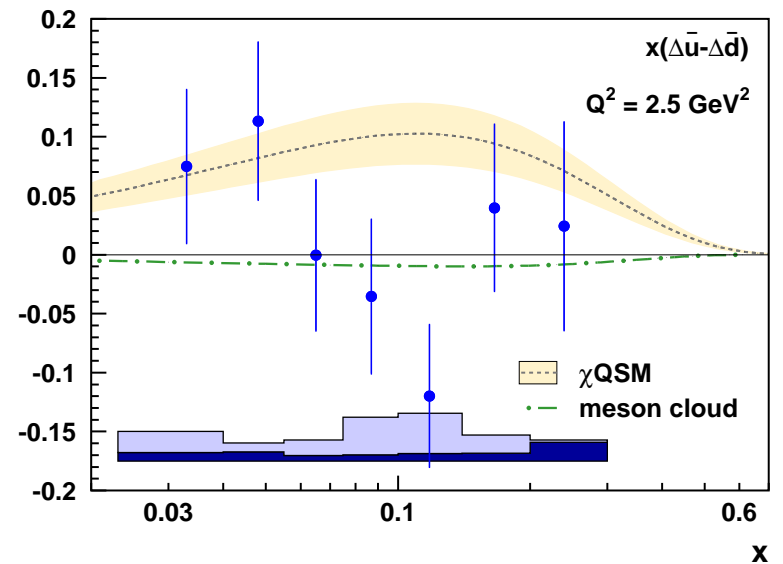
● HERMES: Sea quark flavor asymmetry:

$$\int_{0.023}^{0.3} (\Delta q_u(x) - \Delta q_d(x)) dx = 0.05 \pm 0.06 \pm 0.03$$

[PRL 92 (2004) 012005]



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Spin Contribution of Strange Quarks

HERMES 'isoscalar' extraction method uses only deuterium data:

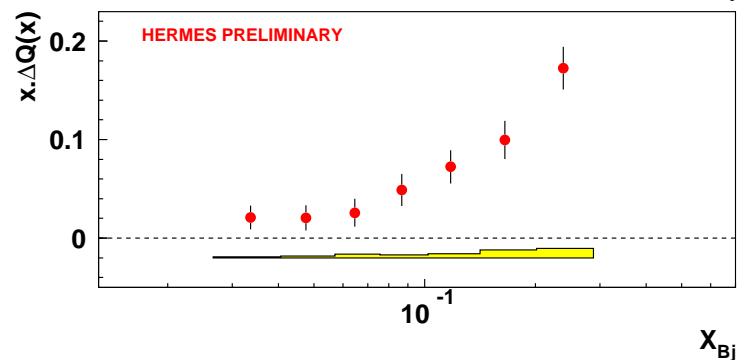
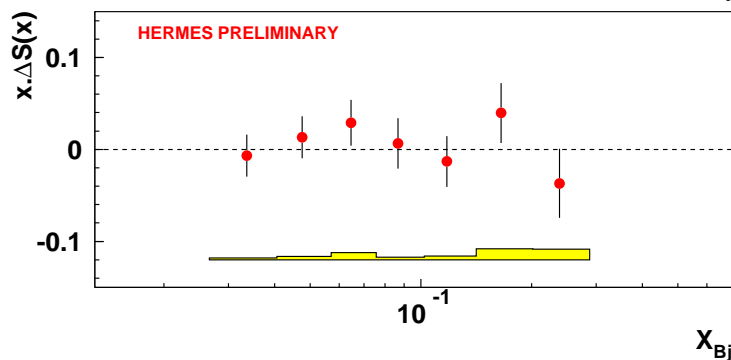
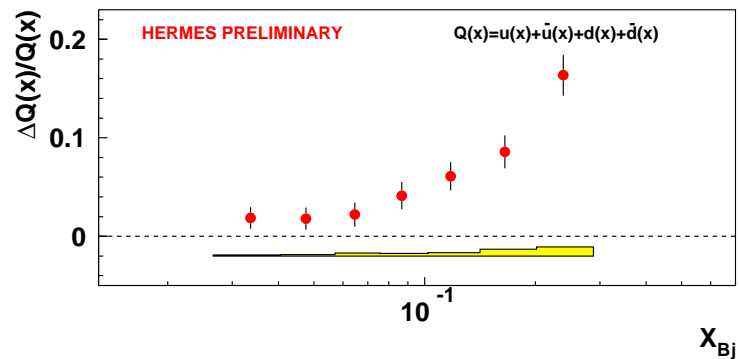
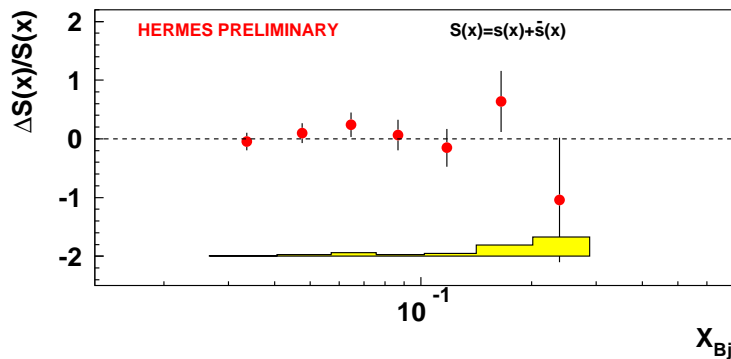
● K^+ & K^- multiplicities, inclusive asymmetry A_1^d , kaon asymmetries $A_1^{K^+}$, $A_1^{K^-}$

⇒ Fit parameters: $\Delta S(x) = q_s(x) + \bar{q}_s(x)$; $\Delta Q(x) = q_u(x) + \bar{q}_u(x) + q_d(x) + \bar{q}_d(x)$

$$\int_{0.02}^{0.6} \Delta S(x) dx = 0.006 \pm 0.029 \pm 0.007 \quad [\text{preliminary 2005}]$$

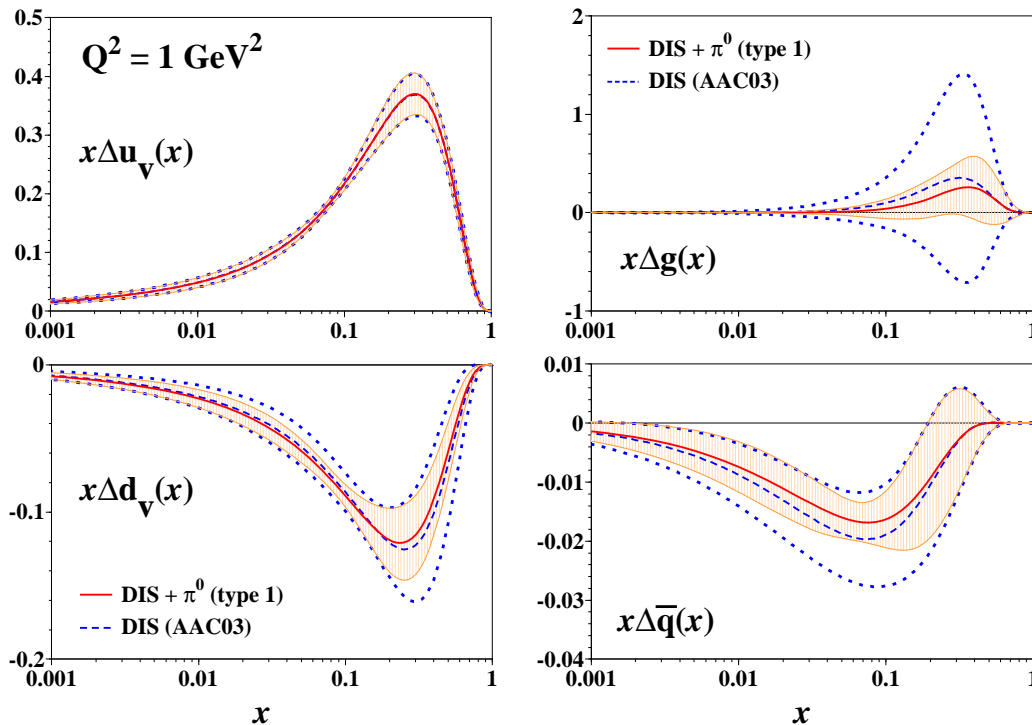
⇒ small ΔG ? (suggested: gluon splitting into strange sea through axial anomaly)

● Note: uncertainties very sensitive to fragmentation function input



Next-to-leading Order QCD Fits

Typical (and most recent) results by AAC [hep-ph/0603213]: NLO in α_s , \overline{MS} scheme



Assumptions:

- Flavor-symmetric Δq_{sea}
- Integrals of Δq_u^{val} and Δq_d^{val} fixed by weak decay constants F and D

Input experimental data:

- $A_1^{p,d}$ from COMPASS, JLAB, HERMES
- $A_{LL}^{\pi^0}$ from PHENIX

Results at $Q^2 = 1 \text{ GeV}^2$: $\Delta\Sigma = 0.25 \pm 0.10$

$\Delta G = 0.47 \pm 1.08$ (DIS alone); $\Delta G = 0.31 \pm 0.32$ (DIS+PHENIX)

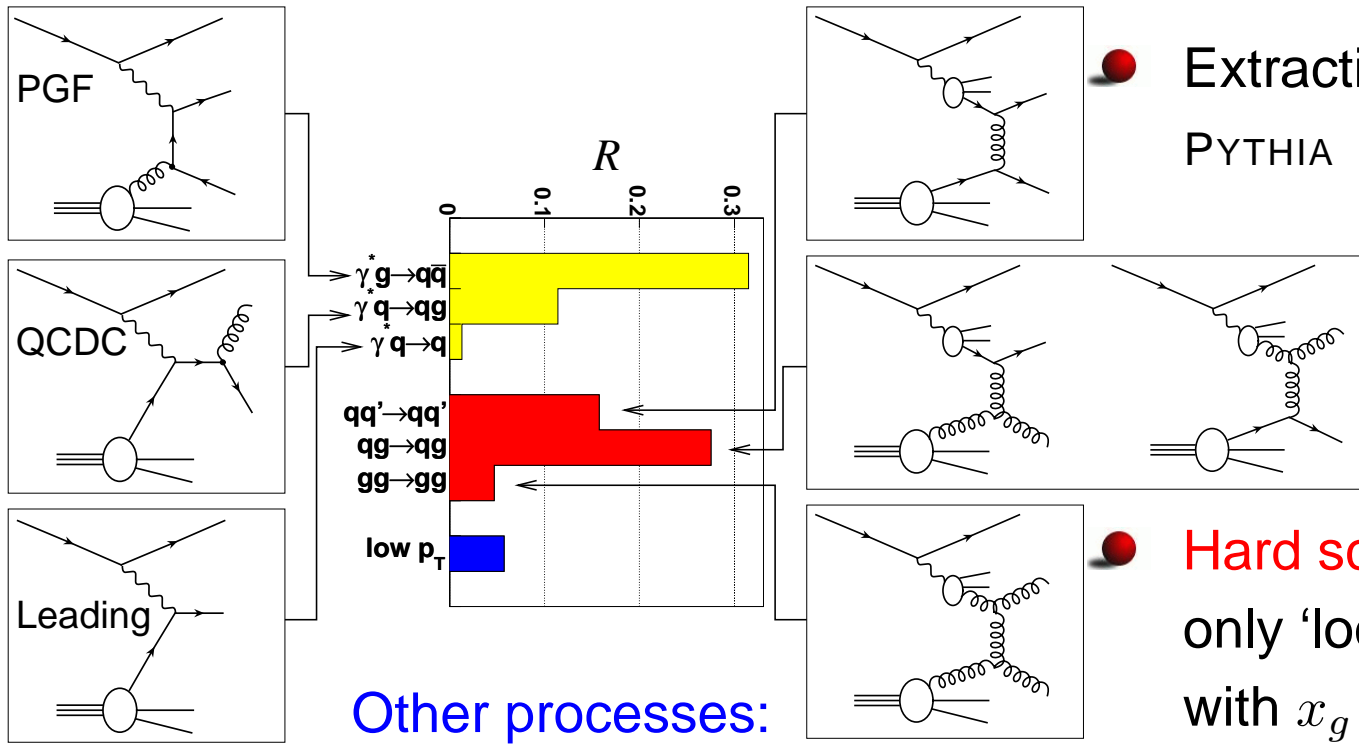
NOTE: From g_d^1 : $\Delta\Sigma_{0.01 < x < 1}^{exp} \approx 0.35 \pm 0.03$, while $\Delta\Sigma_{0 < x < 0.01}^{fit} \approx -0.13 \pm 0.11$ is obtained for low- x 'extrapolation' (due to stiff shape of PDF parameterizations)

ALSO: low- x data urgently needed to constrain $g_1^{p,d}$ (E-RHIC, ELIC)

Determination of Gluon Contribution to Nucleon Spin

- Process: High- p_t hadron pairs in quasi-real photoprod.: $\langle Q^2 \rangle \approx 0.1 \text{ GeV}^2$
- Sensitivity through $\gamma^* g$ 'direct' hard scattering or 'resolved-photon' process

left graphs: direct processes; right graphs: resolved-photon processes [COMPASS analysis]



- Extraction heavily relies on PYTHIA simulation (LO only !)

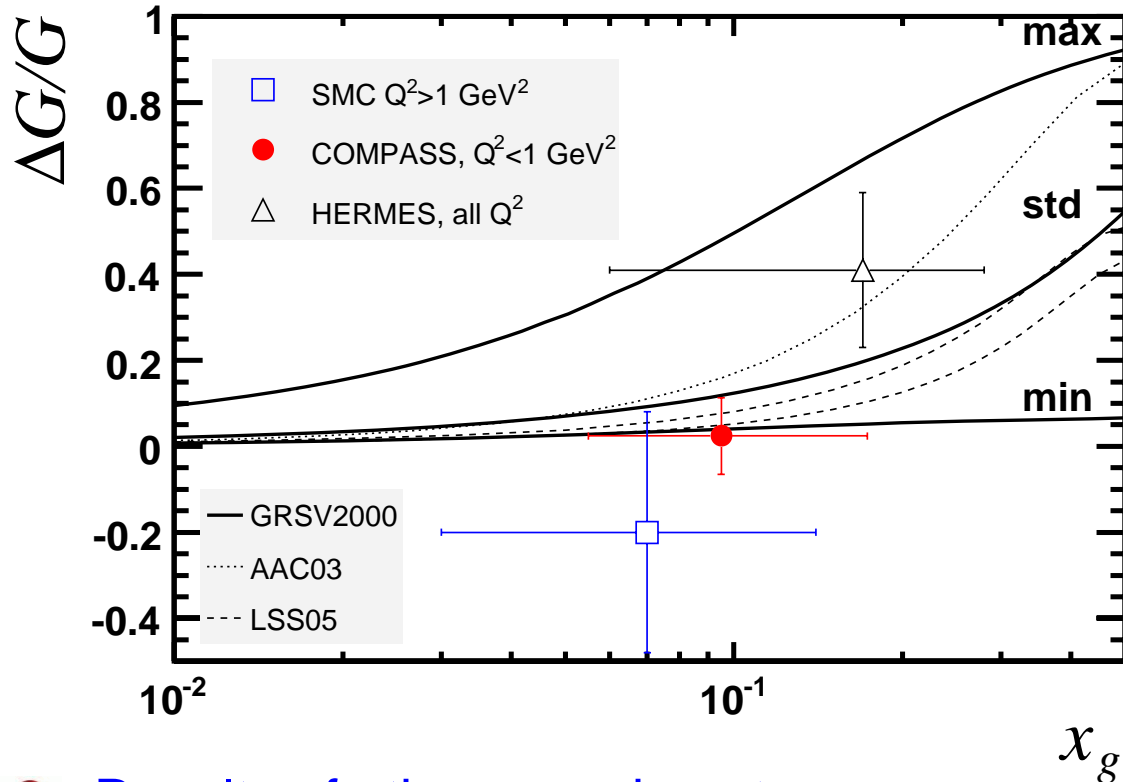
- Hard scale $\mu^2 \simeq 3 \text{ GeV}^2$ only 'loosely' correlated with x_g ($\langle x_g \rangle \simeq 0.1$)

- COMPASS: Open-charm production ($\gamma^* g \rightarrow c\bar{c}$)
- HERMES: Quasi-real photoproduction of single high- p_t hadrons
- RHIC: A_{LL} in inclusive direct γ & π^0 production, inclusive jet production

Results on Gluon Distribution $\frac{\Delta g}{g}(\mathbf{x}_g)$

● Most precise result from high- p_t hadron pairs

↓ COMPASS ↓



$Q^2 < 1 \text{ GeV}^2$ ($\langle x_g \rangle \simeq 0.085$):
 $\frac{\Delta g}{g} = 0.016 \pm 0.058_{stat} \pm 0.055_{syst}$
 [PLB 612,154 (2005)]

$Q^2 > 1 \text{ GeV}^2$ ($\langle x_g \rangle \simeq 0.13$) [prel.]:
 $\frac{\Delta g}{g} = 0.06 \pm 0.31_{stat} \pm 0.06_{syst}$

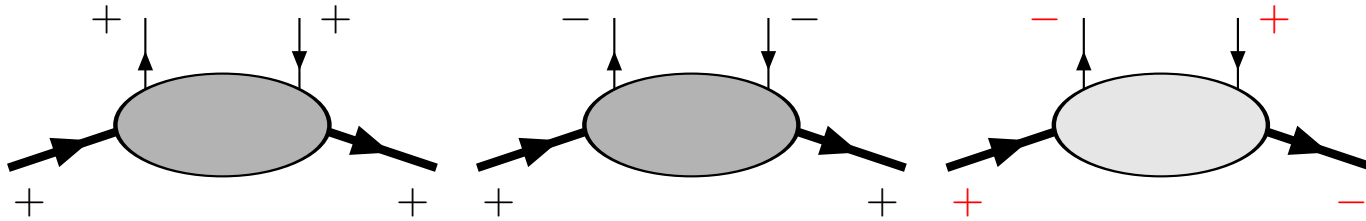
Open charm ($\langle x_g \rangle \simeq 0.15$) [prel.]:
 $\frac{\Delta g}{g} = -0.57 \pm 0.31_{stat}$

● Results of other experiments:

● HERMES high- p_t hadron pairs (all Q^2 , $\langle x_g \rangle \simeq 0.17$) [PRL84 (2000) 2584]
 $\frac{\Delta g}{g} = 0.41 \pm 0.18_{stat} \pm 0.03_{exp-syst}$

● PHENIX: Presently only confidence limits for different $\frac{\Delta g}{g}$ assumptions
 [PANIC05 talk]

The third twist-2 PDF: Transversity



Optical theorem: $\left\| \begin{array}{c} \text{wavy } q \\ \text{--- } P \end{array} \right\|^2 \sim \text{Im} \left\{ \begin{array}{c} q \text{ wavy } q \\ \text{--- } P \quad \text{--- } P \end{array} \right\}$

$$q_f(x) = q_f^{\vec{\rightarrow}}(x) + q_f^{\vec{\leftarrow}}(x) \sim \text{Im}(\mathcal{A}_{++,++} + \mathcal{A}_{+-,+-})$$

$$\Delta q_f(x) = q_f^{\vec{\rightarrow}}(x) - q_f^{\vec{\leftarrow}}(x) \sim \text{Im}(\mathcal{A}_{++,++} - \mathcal{A}_{+-,+-})$$

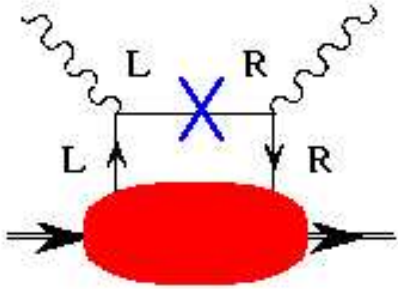
$$\delta q_f(x) \quad \text{alias} \quad h_1(x) \quad \sim \text{Im} \mathcal{A}_{+-, -+}$$

Positivity limit & Soffer bound:

$$|\delta q_f(x)| < q_f(x)$$

$$|\delta q_f(x)| < \frac{1}{2} (q_f(x) + \Delta q_f(x))$$

How to Measure Transversity?



- Hard interactions conserve chirality
- ⇐ In DIS: chirality-flip diagram suppressed by quark mass
- The transversity distribution function is chiral-odd
⇒ not accessible in DIS!

Semi-inclusive DIS: $\sigma^{eH \rightarrow ehX} \propto \sum_q \mathcal{D}^{H \rightarrow q} \otimes \sigma^{eq \rightarrow eq} \otimes \mathcal{F}^{q \rightarrow h}$

where \mathcal{D} denotes a distribution function and \mathcal{F} a fragmentation function
(Factorization not yet proven for transv.-mom.-dependent subleading $1/Q$ terms)

Need another chiral-odd object: **Collins fragmentation function H_1^\perp**

- also 'T-odd' (=odd under naive time reversal)
- represents interference of 2 amplitudes with different imaginary parts
⇒ H_1^\perp can generate a single-spin asymmetry

NOTE: SIDIS alone can not independently determine δq and H_1^\perp (only shapes!)

- Collins function from BELLE e^+e^- data: 1st result! [hep-ex/0507063, acc. by PRL]
- Drell-Yan can yield transversity: upgraded RHIC, PAX? (only large x , 2012 ?)

SIDIS: Two contrasting T-odd Phenomena

A single-spin asymmetry can arise from some (naive) **T-odd mechanism**

With transverse target polarization two mechanisms become distinguishable

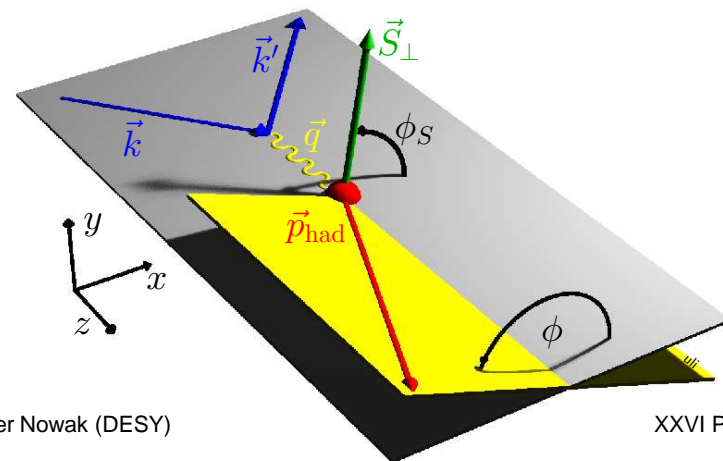
Transversity + T-odd Collins FF

- **Transversity:** polarizations of quark and nucleon correlated

- Photoabsorption flips quark polarization component in lepton scattering plane

- Quark polarization correlates with fragmentation $k_T \rightarrow \mathbf{P}_{h\perp}$ i.e. hadron production plane

⇒ Single **T**arget **S**pin **A**symmetry $\propto \sin(\phi + \phi_S)$



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T-odd Sivers distrib. function f_{1T}^\perp

- p_T of UNpolarized struck quark correlated with target polariz.

- p_T survives fragmentation, inherited by hadron $\mathbf{P}_{h\perp}$

⇒ Orientation of lepton scattering plane is irrelevant

⇒ Single **T**arget **S**pin **A**symmetry $\propto \sin(\phi - \phi_S)$

Extraction of Sivers & Collins Azimuthal Moments

Study azimuthal distributions of hadrons in: $e^\pm p^\uparrow \longrightarrow e^\pm \pi^\pm + X$
 unpol. beam (U), **transv. pol. target (T)**

$$\begin{aligned}
 A_{UT}^\ell(\phi, \phi_S) &= \frac{1}{\langle S_T \rangle} \frac{N_\pi^{\uparrow\uparrow}(\phi, \phi_S) - N_\pi^{\downarrow\downarrow}(\phi, \phi_S)}{N_\pi^{\uparrow\uparrow}(\phi, \phi_S) + N_\pi^{\downarrow\downarrow}(\phi, \phi_S)} \\
 &\sim \sin(\phi - \phi_S) \sum_q e_q^2 \mathcal{I} \left[w_{Siv}(p_T, P_{h_\perp}) f_{1T}^{\perp,q}(x, p_T^2) D_1^q(z, k_T^2) \right] \\
 &+ \sin(\phi + \phi_S) \sum_q e_q^2 \mathcal{I} \left[w_{Coll}(k_T, P_{h_\perp}) h_{1T}^q(x, p_T^2) H_1^{\perp,q}(z, k_T^2) \right] + \dots
 \end{aligned}$$

[...] : convol. integral over initial^q (p_T) and final (k_T) quark transverse momenta

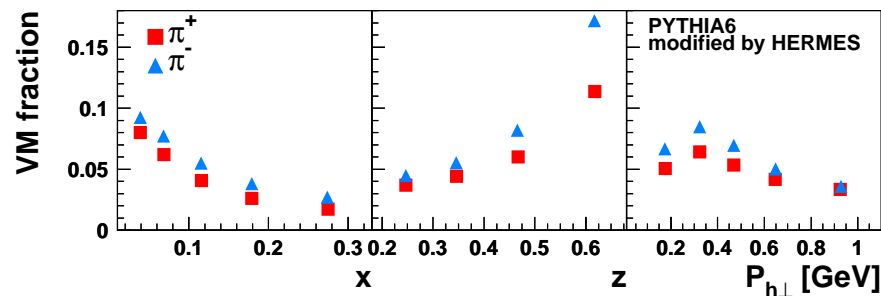
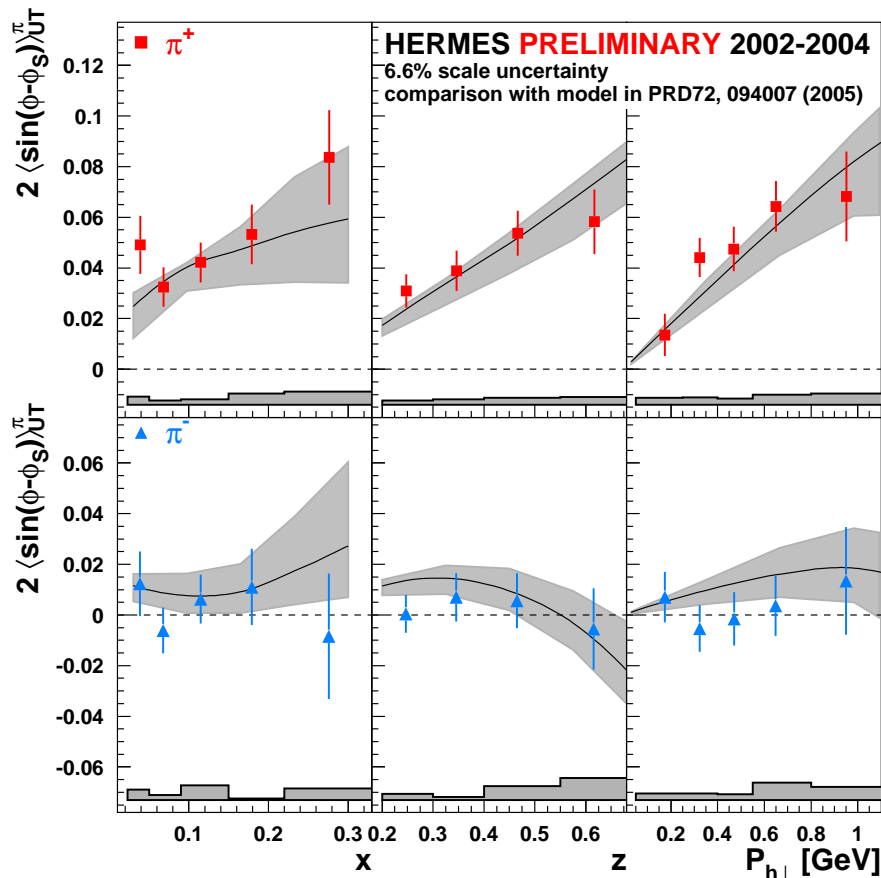
⇒ **can NOT DIRECTLY** extract transverse-momentum-dependent functions !
 ⇒ **Determine (simultaneously) Sivers** and **Collins** convolution integrals by a fit:

$$A_{UT}^\ell(\phi, \phi_S) = 2 \left\langle \sin(\phi - \phi_S) \right\rangle_{UT}^\ell \sin(\phi - \phi_S) + 2 \left\langle \sin(\phi + \phi_S) \right\rangle_{UT}^\ell \sin(\phi + \phi_S)$$

NOTE: asymmetry weighting by $P_{h_\perp} / (zM_h)$ makes convolution integral calculable (involves acceptance dependence)

Results on Sivers Moments from 2002-2004 data

$$2 \left\langle \sin(\phi - \phi_S) \right\rangle_{UT}^{\ell} \approx 2 \left\langle \sin(\phi - \phi_S) \right\rangle_{UT}^{\gamma^*} \propto - \sum_q e_q^2 \mathcal{I} \left[w_{Siv} f_{1T}^{\perp,q}(x, p_T^2) D_1^q(z) \right]$$



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⇐ 1st measurement: HERMES (proton target)

● π^+ : positive; π^- : consistent with zero

⇐ well described by phenomenol. model

● first unambiguous evidence for a non-zero T-odd distribution fct. in DIS !

⇒ a signature for quark orbital angular momentum

● $f_{1T}^{\perp,u}$ negative (using Trento convention)

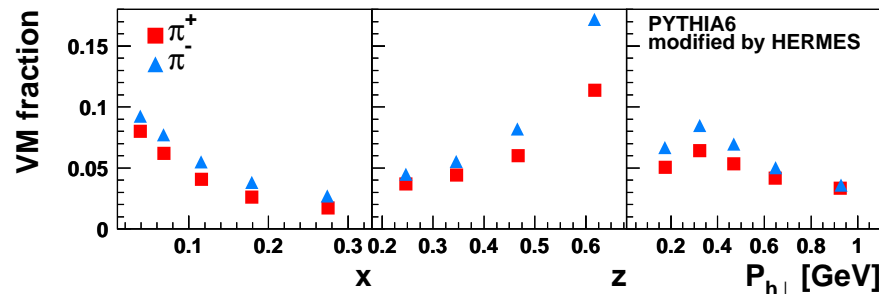
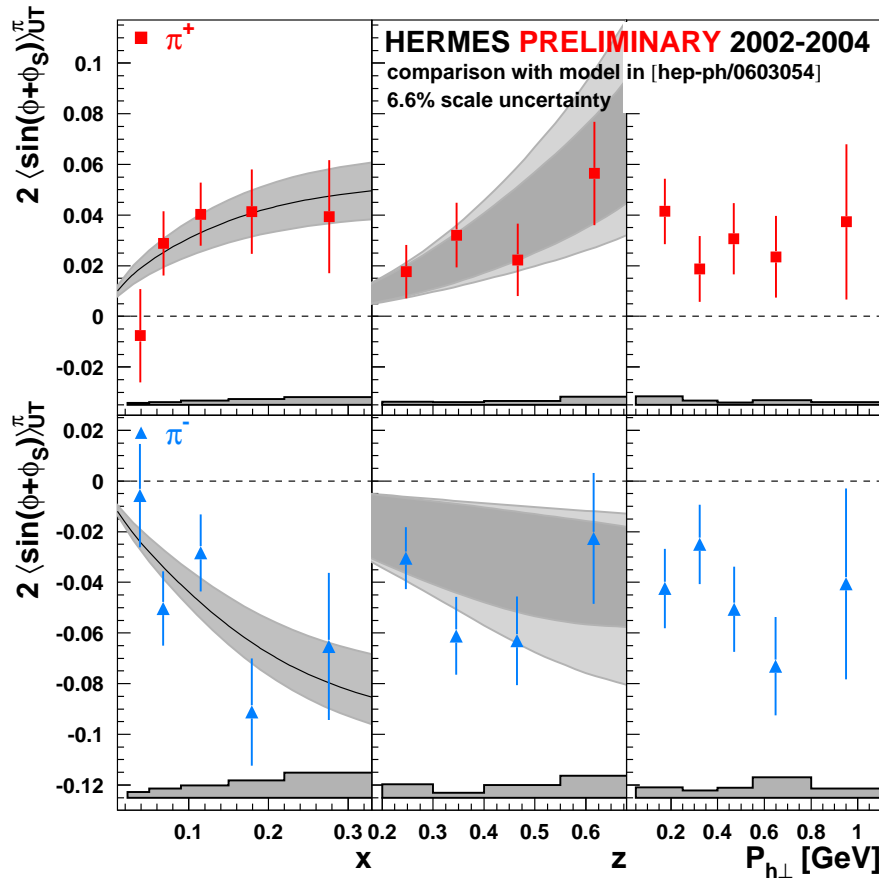
⇒ consistent with Burkhardt's picture of 'Chromodynamic lensing' !

● COMPASS: 'zero' results (deuteron target!)

⇐ NOTE: Contamination (2-16%) by decay of exclusively produced vector mesons

Results on Collins Moments from 2002-2004 data

$$2 \left\langle \sin(\phi + \phi_S) \right\rangle_{UT}^{\ell} \approx 2 \left\langle \sin(\phi + \phi_S) \right\rangle_{UT}^{\gamma^*} \propto \sum_q e_q^2 \mathcal{I} \left[w_{Coll} h_{1T}^q(x, p_T^2) H_1^{\perp, q}(z, k_T^2) \right]$$



● **pos. HERMES π^+ results** – no surprise: u-quark domin. and $\delta q > 0$ as $\Delta q > 0$

● **negative HERMES π^- results** were a surprise – now understood to require disfavored Collins function be large and opposite in sign (Artru fragm. model)

⇐ grey bands: predictions [hep-ph/0603054] of **chiral quark soliton model**:

▷ **x-dependence**: mean Collins function fitted and found to be x-independent

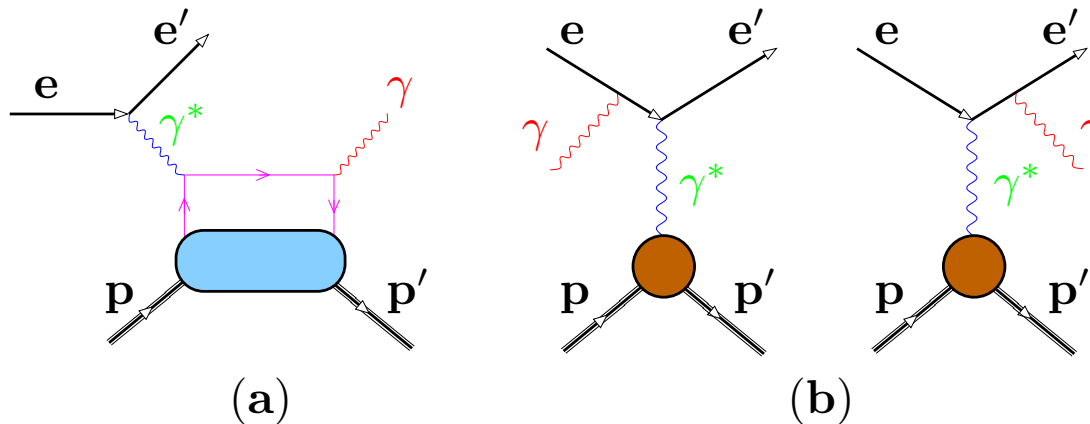
▷ **z-dependence**: **Collins fct.** extracted from **BELLE e^+e^- data** [hep-ex/0507063]

● COMPASS: ‘zero’ results (on deuteron!)

⇒ **HERMES, COMPASS and BELLE compatible**

● COMPASS will take proton data in 2006

Deeply Virtual Compton Scattering



- Same final state in **DVCS** and **Bethe-Heitler** \Rightarrow **Interference!**

$$d\sigma(eN \rightarrow eN\gamma) \propto |\mathcal{T}_{BH}|^2 + |\mathcal{T}_{DVCS}|^2 + \underbrace{\mathcal{T}_{BH}\mathcal{T}_{DVCS}^* + \mathcal{T}_{BH}^*\mathcal{T}_{DVCS}}_{\mathcal{I}}$$
- \mathcal{T}_{BH} is calculable in QED and parameterized in terms of Dirac and Pauli Form Factors F_1, F_2
- \mathcal{T}_{DVCS} is parameterized in terms of **Compton form factors** $\mathcal{H}, \mathcal{E}, \tilde{\mathcal{H}}, \tilde{\mathcal{E}}$ (which are convolutions of resp. **GPDs** $H, E, \tilde{H}, \tilde{E}$)
- (Certain Parts of) **interference term** \mathcal{I} can be **filtered out** by forming certain **cross section** differences (or **asymmetries**)
 \Rightarrow **GPDs** $H, E, \tilde{H}, \tilde{E}$ **indirectly** accessible via **interference term** \mathcal{I}

Azimuthal Asymmetries in DVCS

DVCS–Bethe-Heitler Interference term \mathcal{I}

induces azimuthal asymmetries in cross-section:

- **Beam-charge asymmetry $A_C(\phi)$ [BCA]** :

$$d\sigma(e^+, \phi) - d\sigma(e^-, \phi) \propto \text{Re}[F_1 \mathcal{H}] \cdot \cos \phi$$

- **Beam-spin asymmetry $A_{LU}(\phi)$ [BSA]** :

$$d\sigma(\vec{e}, \phi) - d\sigma(\overleftarrow{e}, \phi) \propto \text{Im}[F_1 \mathcal{H}] \cdot \sin \phi$$

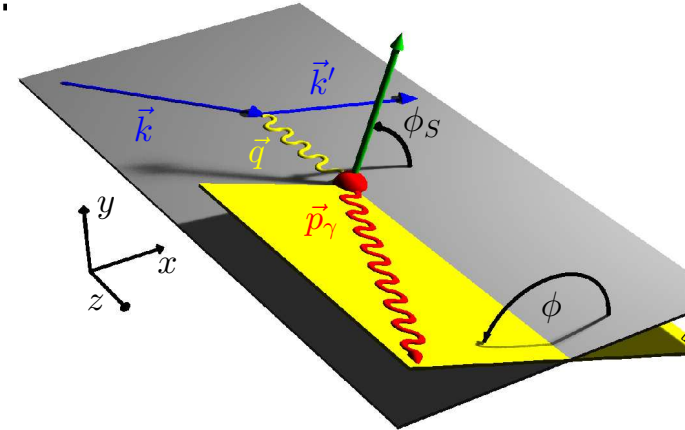
- **Long. target-spin asymmetry $A_{UL}(\phi)$:**

$$d\sigma(\overleftarrow{P}, \phi) - d\sigma(\overrightarrow{P}, \phi) \propto \text{Im}[F_1 \tilde{\mathcal{H}}] \cdot \sin \phi \quad \text{[LTSA]}$$

- **Transverse target-spin asymmetry $A_{UT}(\phi, \phi_S)$ [TTSA]:**

$$d\sigma(\phi, \phi_S) - d\sigma(\phi, \phi_S + \pi) \propto \text{Im}[F_2 \mathcal{H} - F_1 \mathcal{E}] \cdot \sin(\phi - \phi_S) \cos \phi \\ + \text{Im}[F_2 \tilde{\mathcal{H}} - F_1 \xi \tilde{\mathcal{E}}] \cdot \cos(\phi - \phi_S) \sin \phi$$

(F_1, F_2 are the Dirac and Pauli elastic nucleon form factors)



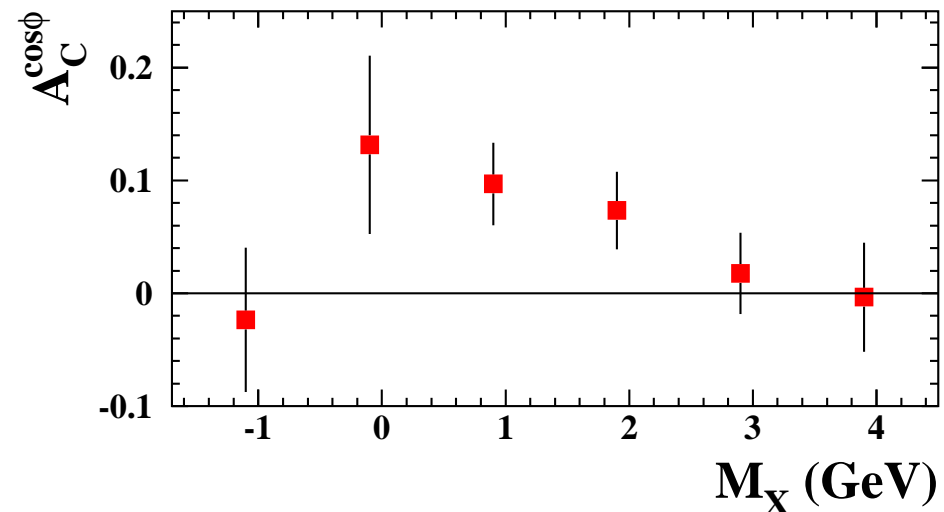
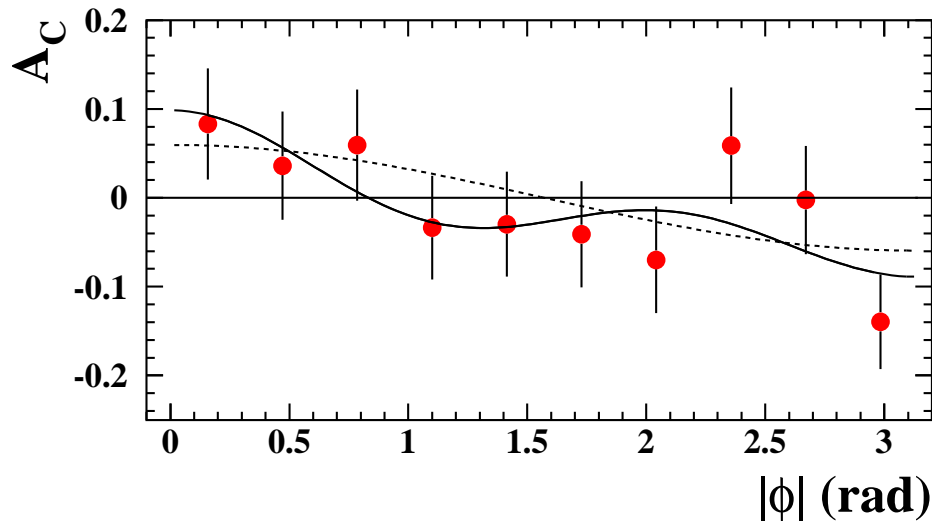
First Data on Beam-charge Asymmetry

$$A_C(\phi) = \frac{d\sigma^+(\phi) - d\sigma^-(\phi)}{d\sigma^+(\phi) + d\sigma^-(\phi)} \propto \text{Im}F_1 \mathcal{H} \cdot \cos \phi + \dots$$

⇒ extract 'amplitudes' by fitting in every ϕ -bin

$$A_C(\phi) = \text{const.} + A_C^{\cos \phi} \cos \phi + A_C^{\cos 2\phi} \cos 2\phi + A_C^{\cos 3\phi} \cos 3\phi$$

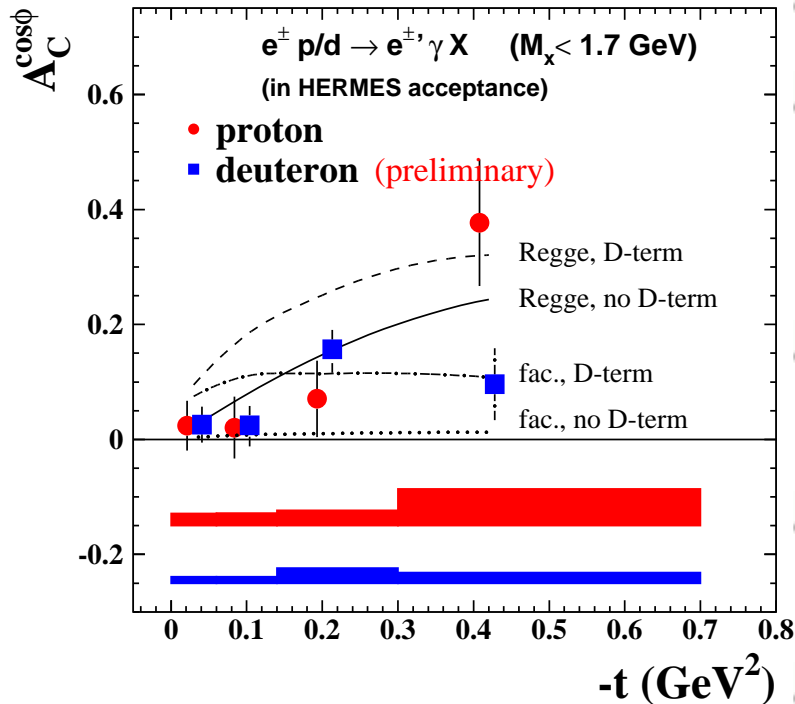
- First measurement by HERMES (unpolar. proton target) [hep-ex/0605108, subm. to PRL]:



- use symmetrization ($\phi \rightarrow |\phi|$) to get rid of sinusoidal terms
- $A_C^{\cos \phi} = 0.060 \pm 0.027$, other contributions insignificant (dashed = pure $\cos \phi$)
- asymmetry only in exclusive and 'associate' M_X region (\rightarrow resol. smearing)
- preliminary deuteron data (not shown) completely consistent

First Conclusion on GPD Models ?

BCA t -dependence can distinguish different GPD model versions:



- $A_C^{\cos \phi}$: elastic + associated production
- d-data: contributions per t -bin of associated production: 5,11,18,29% \Rightarrow highest t -bin mostly affected
- GPD H dominates, \tilde{H} and E suppressed [Goeke, Polyakov, Vanderhaeghen, PPNP 47(2001)401]
- Curves (code [Vanderhaeghen, Guichon, Guidal]) calculated for 4 different parameter sets
- BCA insensitive to profile fct. parameters

● HERMES HERA-I data disfavor Regge-inspired t -dependence with D-term

● 5 times more precise BCA data on HERMES disk from HERA-II

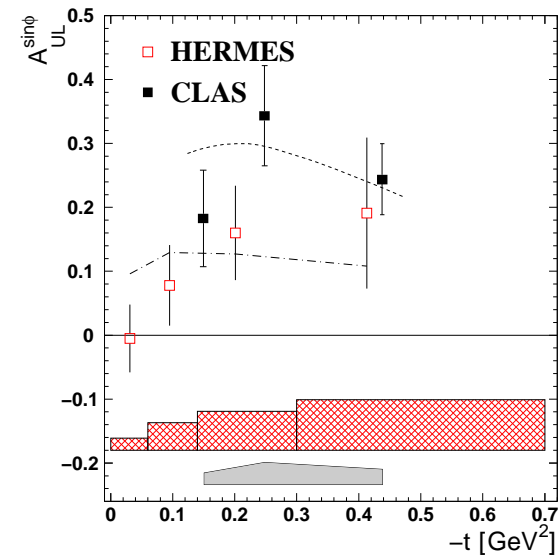
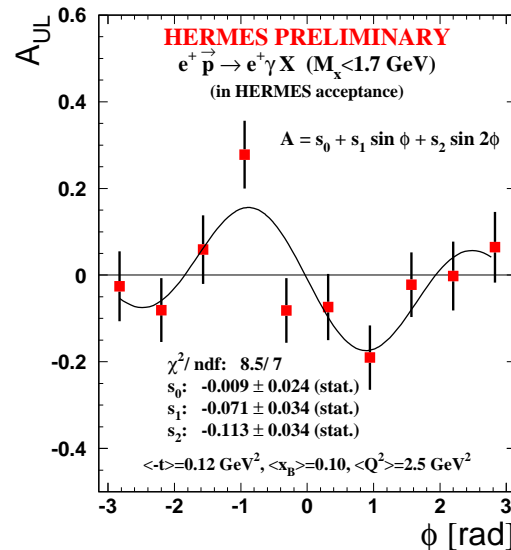
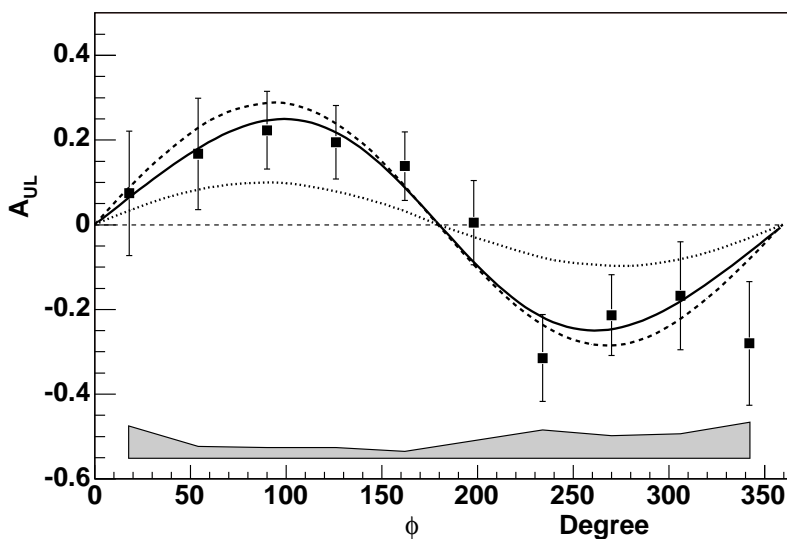
(this data may benefit from recoil detector, presently being commissioned)

● Further BCA data only in far future (COMPASS > 2010 ?, JLAB > 2015 ???)

Longitudinal Target-spin Asymmetry

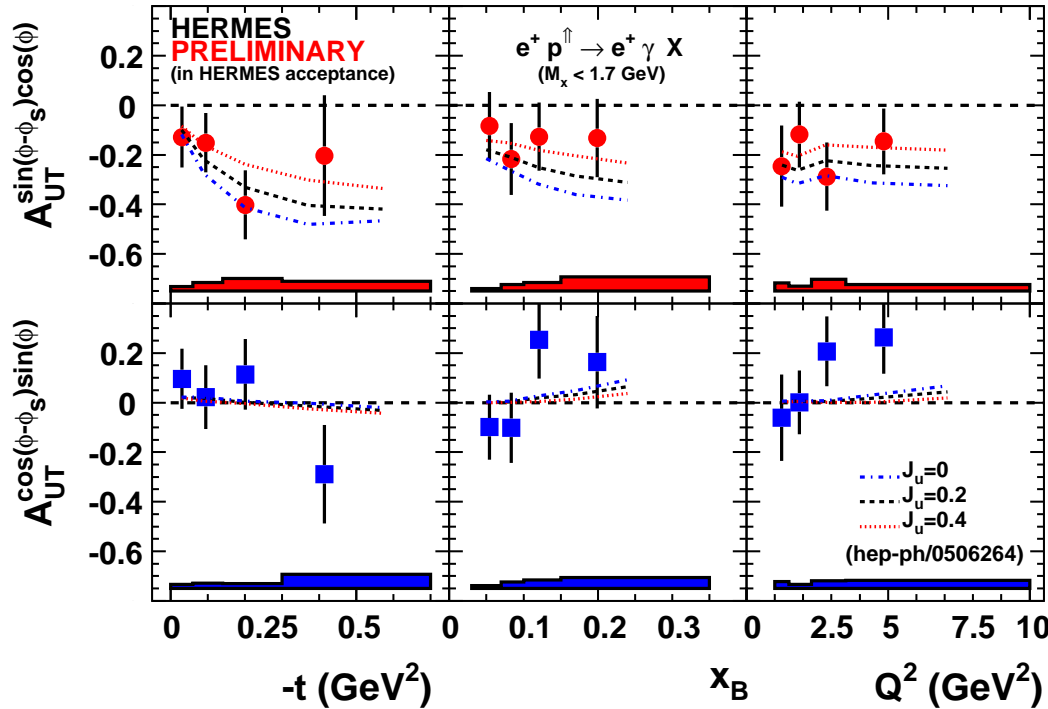
$$A_{UL}(\phi) = \frac{1}{\langle |P_L| \rangle} \cdot \frac{d\sigma^{\rightarrow}(\phi) - d\sigma^{\leftarrow}(\phi)}{d\sigma^{\rightarrow}(\phi) + d\sigma^{\leftarrow}(\phi)} \propto \text{Im}\{F_1 \tilde{\mathcal{H}} + \xi(F_1 + F_2)\mathcal{H} + \dots\} \sin \phi$$

⇒ extract 'amplitudes' fitting per ϕ -bin $A_{UL}(\phi) = c + A_{UL}^{\sin \phi} \sin \phi + A_{UL}^{\sin 2\phi} \sin 2\phi$



- 1st published measurement: CLAS 2000-01 proton data [hep-ex/0605012]
- May 2005 prel. HERMES results (1996-2000 proton and deuteron data)
- both data sets have similar statistics and show expected $\sin \phi$ behaviour
- HERMES can approach lower t -values
- CLAS vs GPD model [PRD60,094017(1999)]: large contribution from GPD $\tilde{\mathcal{H}}$!

Transverse Target-spin Asymmetry: Sensitivity to J_u



$$A_{UT}(\phi, \phi_S) = \frac{1}{\langle |P_T| \rangle}$$

$$\cdot \frac{d\sigma(\phi, \phi_S) - d\sigma(\phi, \phi_S + \pi)}{d\sigma(\phi, \phi_S) + d\sigma(\phi, \phi_S + \pi)} =$$

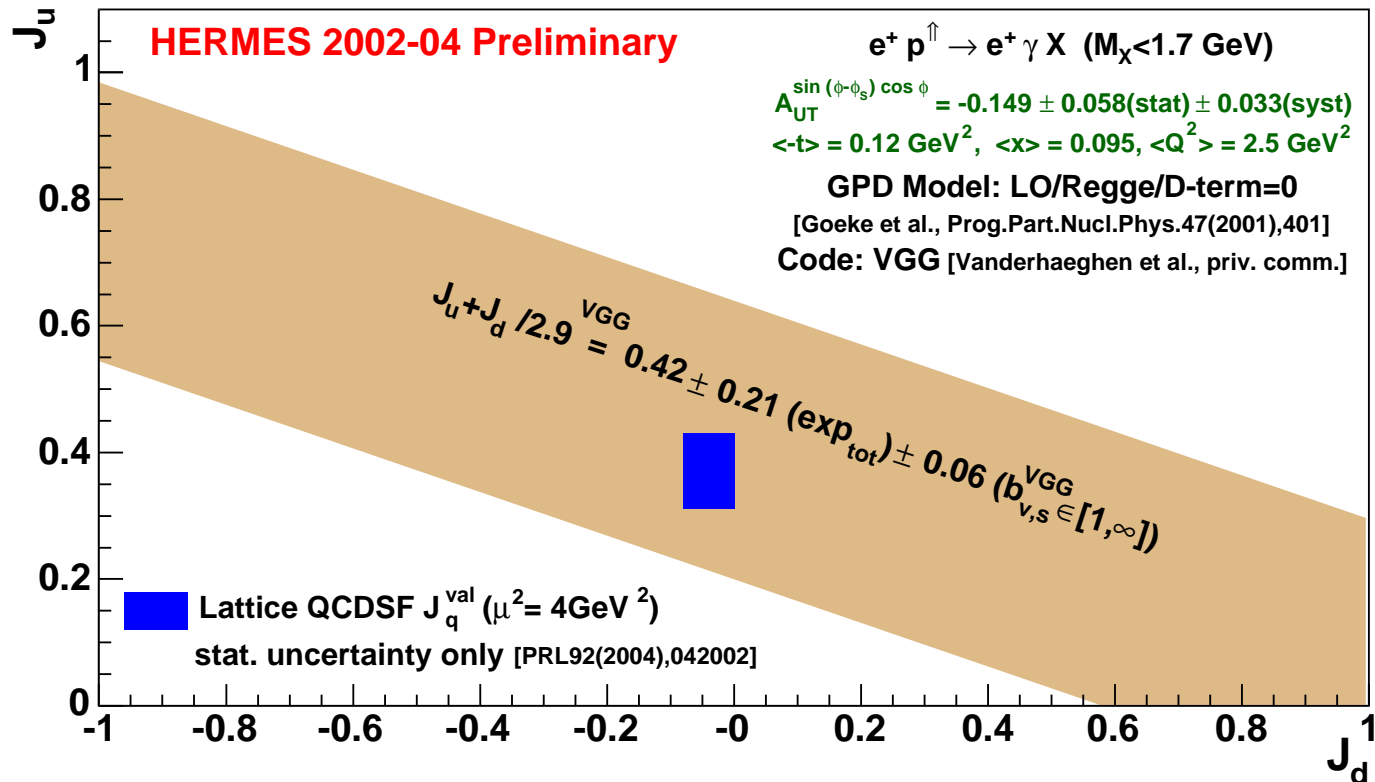
$$A_{UT}^{\sin(\phi-\phi_S)\cos\phi} \cdot \sin(\phi-\phi_S)\cos\phi$$

$$+ A_{UT}^{\cos(\phi-\phi_S)\sin\phi} \cdot \cos(\phi-\phi_S)\sin\phi$$

- First A_{UT} measurement by HERMES (U:unpolar. beam, T:transv. pol. target) (twice more HERMES statistics on disk)
- JLAB: transv. target ≥ 2008 ?, COMPASS: plans for 2010
- GPD E can be modeled in forward limit by $e(x) = Aq_{val}(x) + B\delta(x)$ acc. to χ QSM model [Prog.Part.Nucl.Phys.47(2001)401]
- $A_{UT}^{\sin(\phi-\phi_S)\cos\phi}$ sensitive to J_u , not to the other parameters [hep-ph/0506264]

Model-dependent Constraint on J_u vs J_d

Unbinned maximum likelihood fit to $A_{UT}^{\sin(\phi-\phi_S)\cos\phi}$ at average kinematics (fitting prel. HERMES data against VGG-model based calculations), leaving J_u and J_d as free parameters \Rightarrow model-dependent 1- σ constraint on J_u vs. J_d :



- Quenched **lattice calculation** done with pion masses 1070, 870, and 640 MeV, and then extrapolated linearly in m_π^2 to the physical value
- Uncertainties on VGG model parameters shown as separate uncertainty (± 0.06)

Summary and Outlook

Improvement over last 4 years:

● **Spin-independent & helicity PDFs**

- COMPASS: $\frac{\Delta g}{g}$
- HERMES: $\Delta q_u, \Delta q_d, \Delta q_s$
- JLAB: $\Delta q_u, \Delta q_d$ at large x

⇒ more: COMPASS, HERMES, RHIC

● **Transversity & TMD-PDFs:**

- HERMES: Sivers function
- BELLE: Collins (fragm.) function

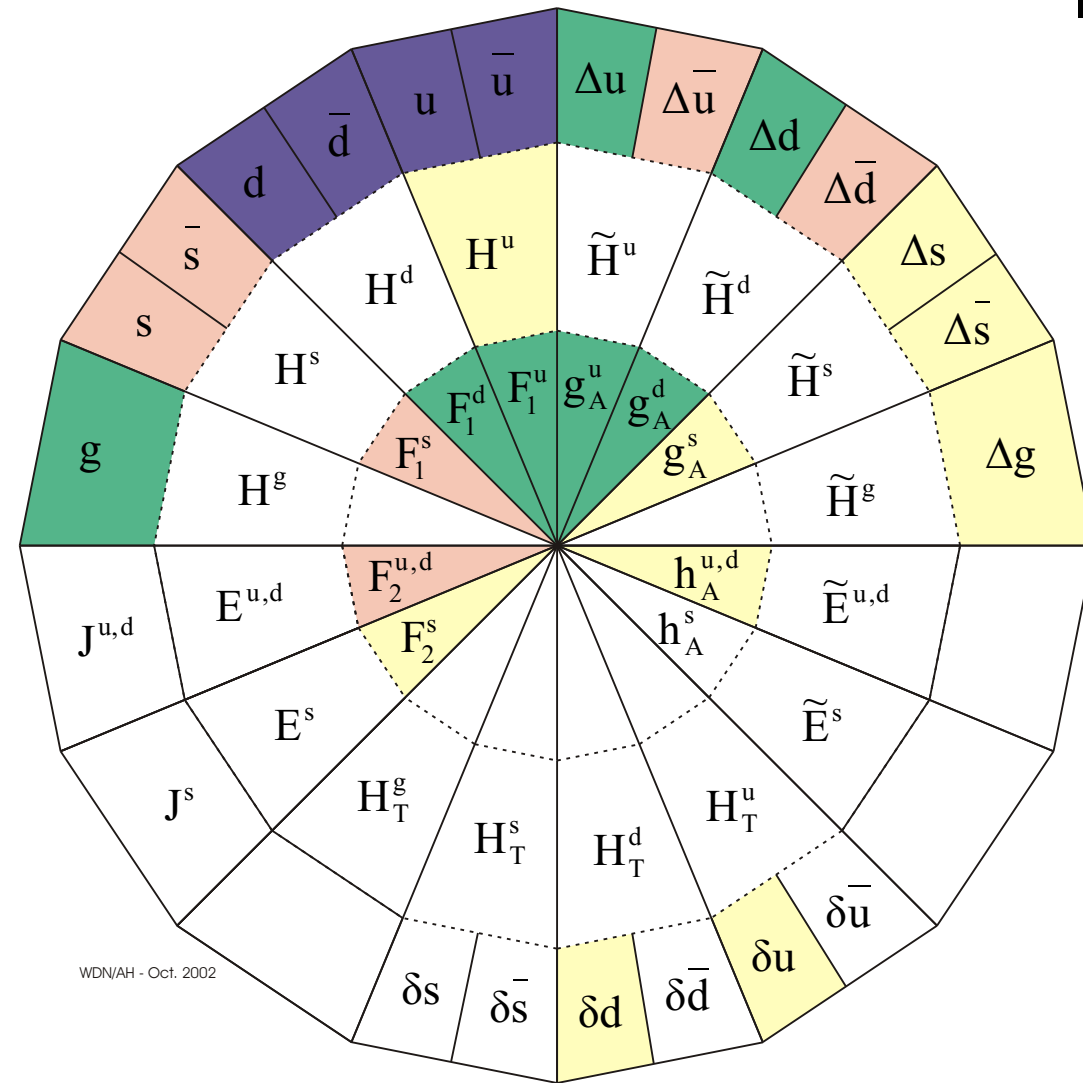
⇒ more: BELLE, COMPASS, HERMES
transversity, Sivers & Boer-Mulders fct., ...

● **GPDs:**

finishing pioneering phase ...

⇒ **much more to come:**

HERMES, JLAB, COMPASS, JLAB-12 GeV



WDN/AH - Oct. 2002

- well known
- known
- measured with large uncertainties
- to be measured in next years
- future measurements