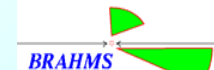
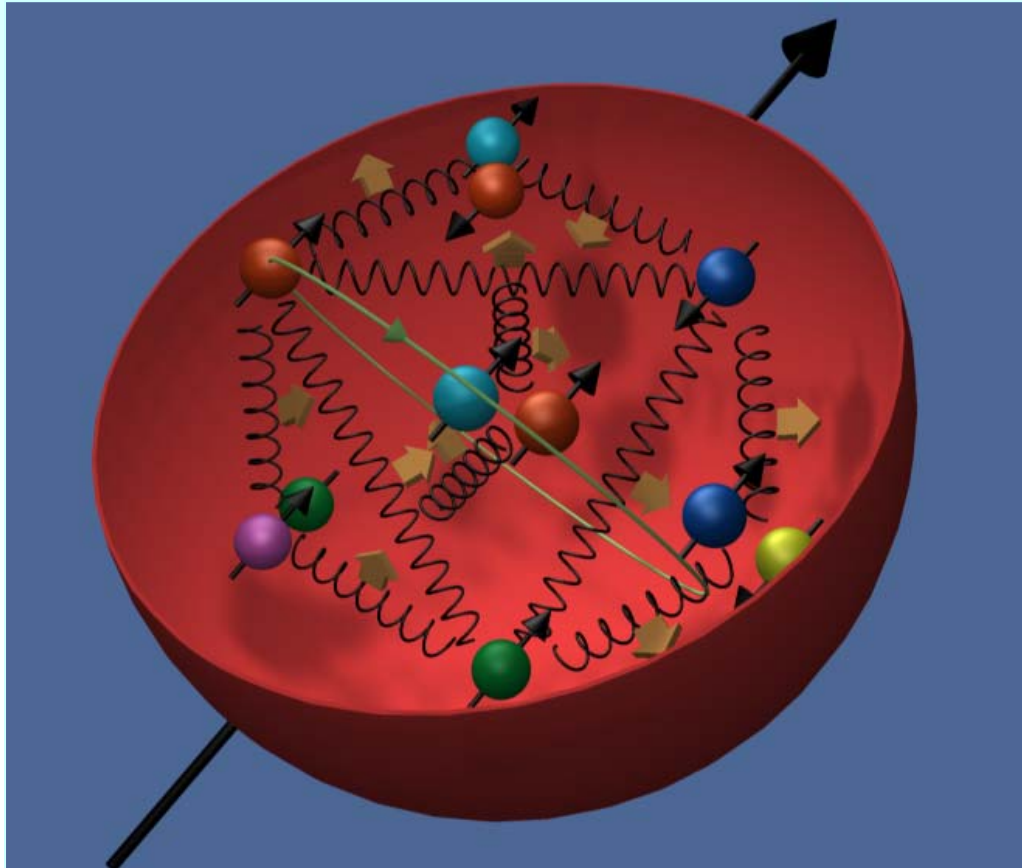


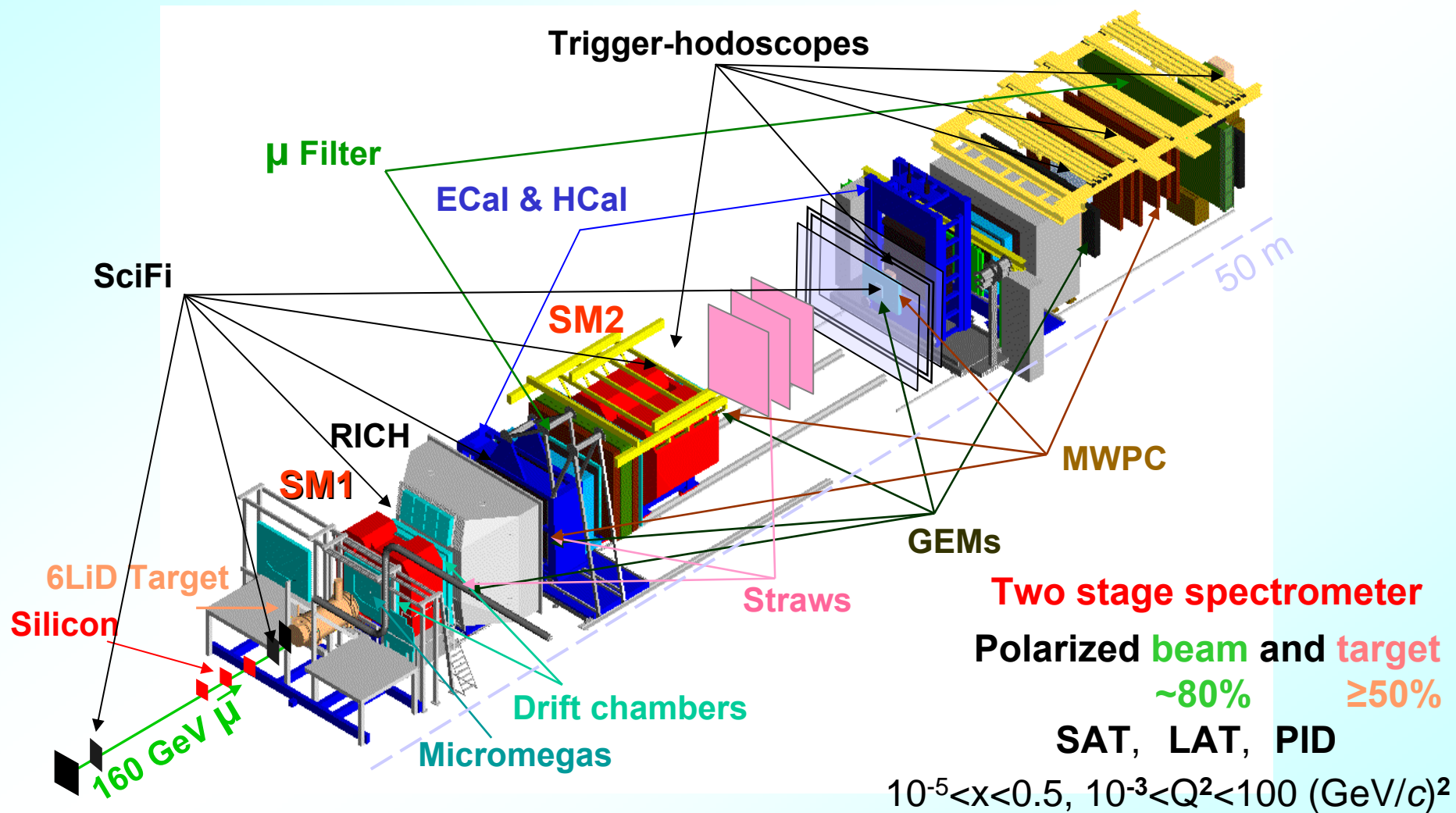
# Selected spin physics results from COMPASS, HERMES and RHIC

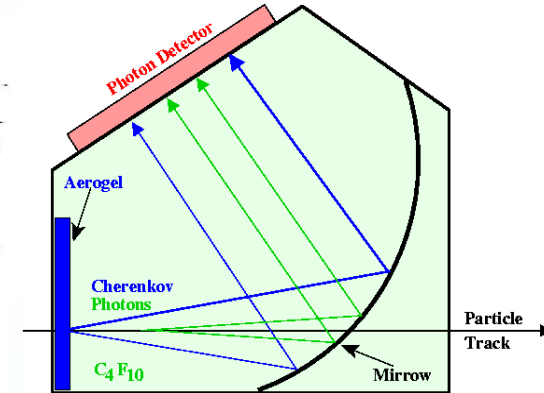
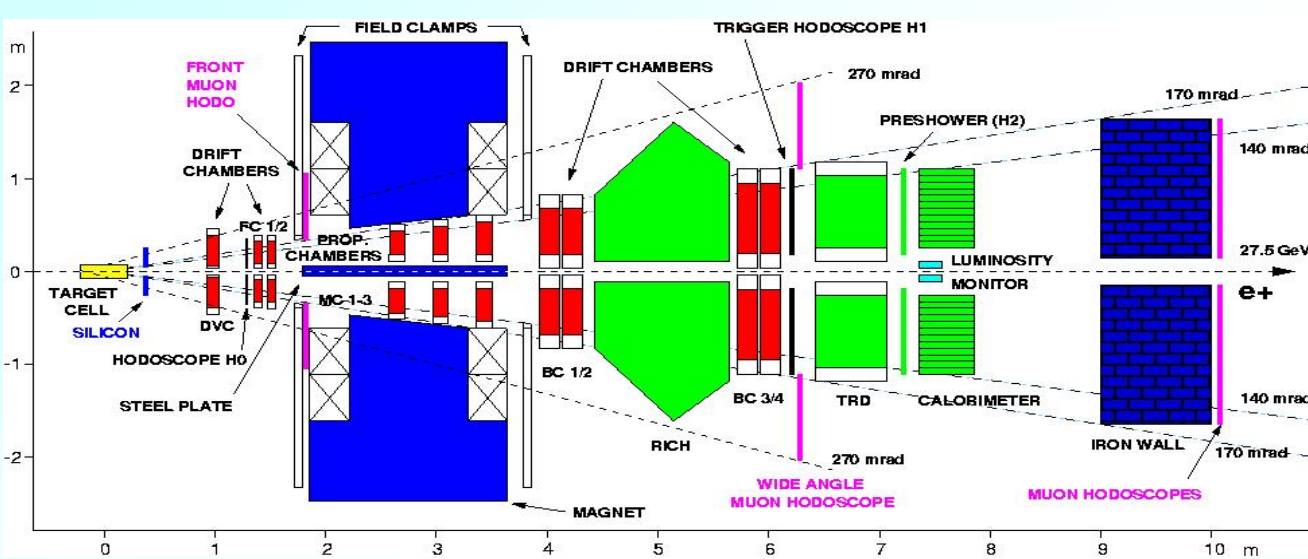
K. Rith, CIPANP06, 2.6.2006



$$S_z = \frac{1}{2} = J_q + J_g = \frac{1}{2}\Delta\Sigma + L_q + (\Delta G + L_g)$$

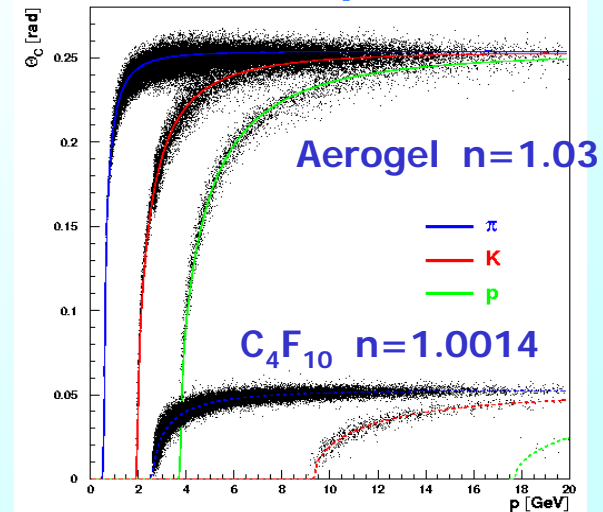
- The Experiments
- Inclusive Asymmetries
- Quark helicity distributions
- Gluon helicity distribution
- (Exclusive processes → GPDs) → M. Garcon
  - Transverse spin physics
    - Transversity - Collins fragmentation function
    - Sivers distribution function
    - $A_N$  in pp collisions
- Conclusions



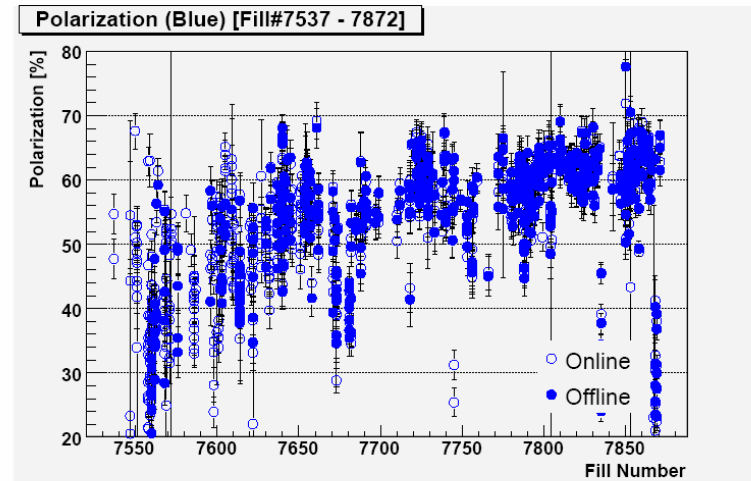
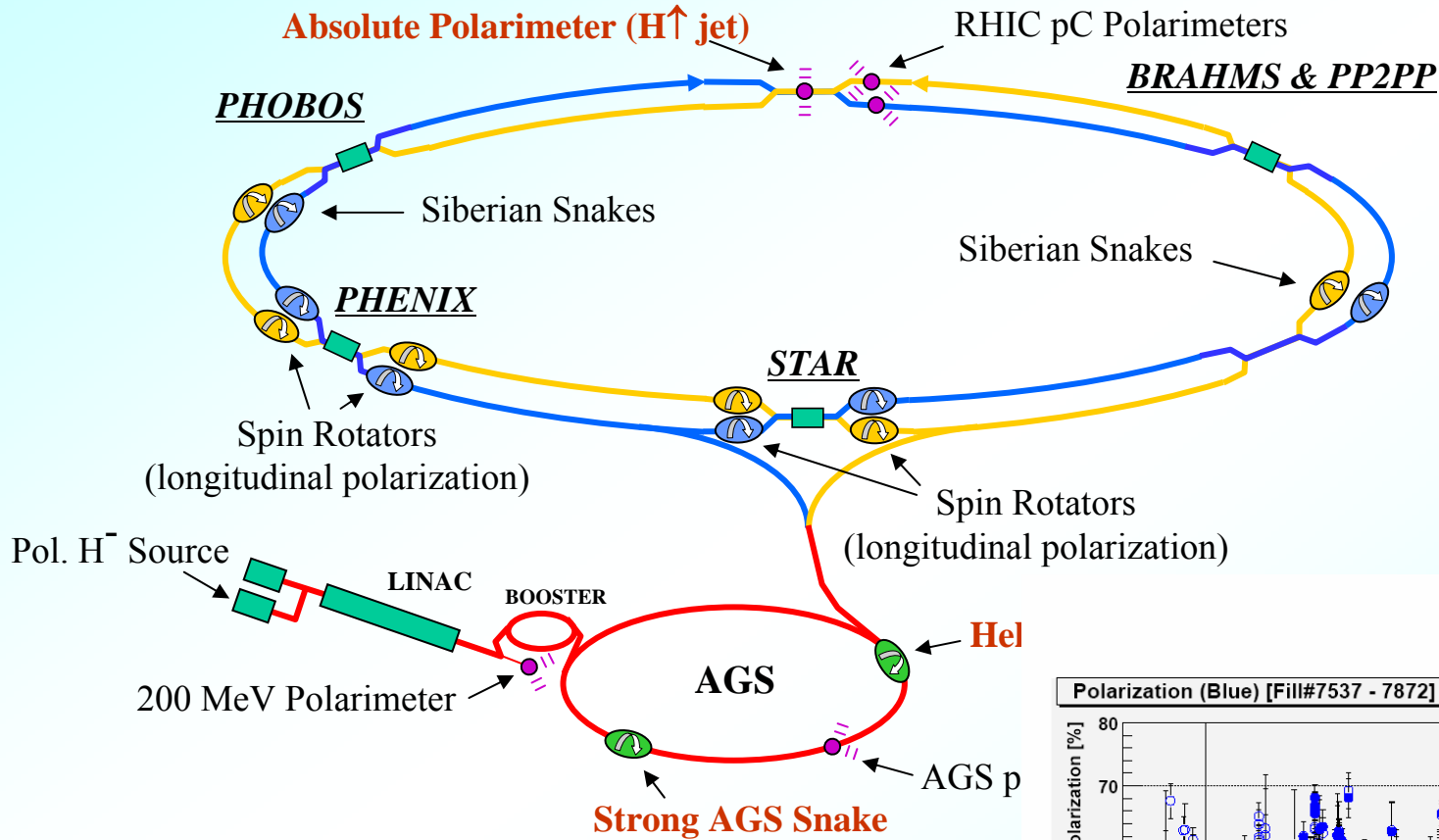


- HERA  $e^+/e^-$  beam of 27.6 GeV
- Polarized internal gas target (H, D,  $^3\text{He}$ )
- kinematics:  $0.02 < x < 0.6$ ,  $1.0 < Q^2 < 15 \text{ GeV}^2$
- tracking:  $\delta p/p \sim 2\%$ ,  $\delta\theta < 0.6 \text{ mrad}$ , 40-220 mrad
- PID: Calorimeter, Preshower, TRD, RICH

## hadron separation



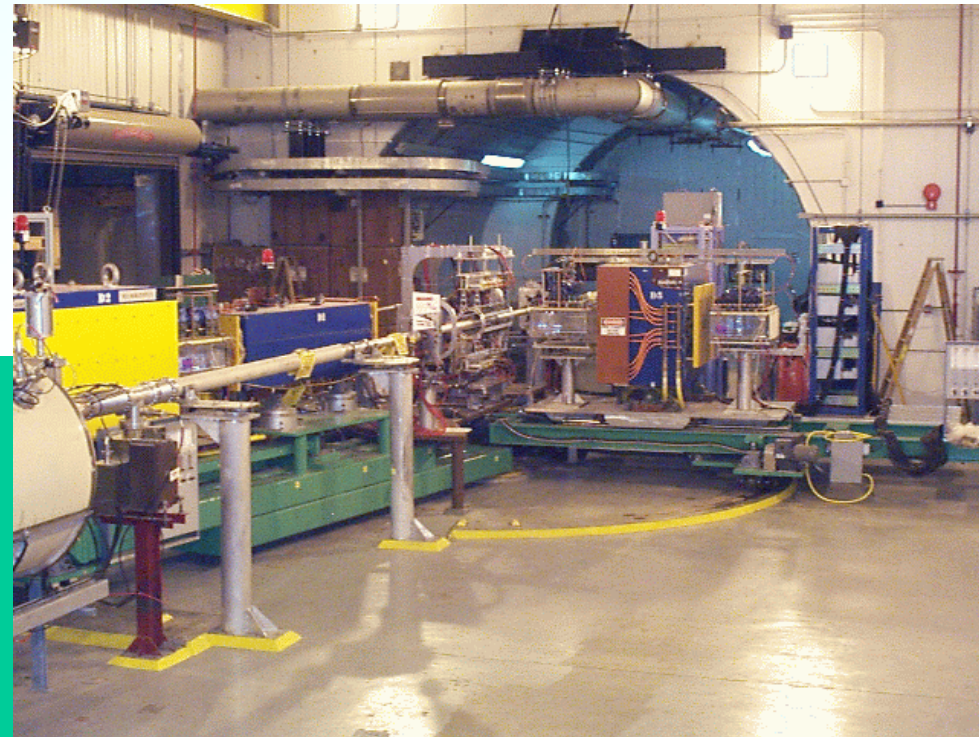
# RHIC-Polarized Collider



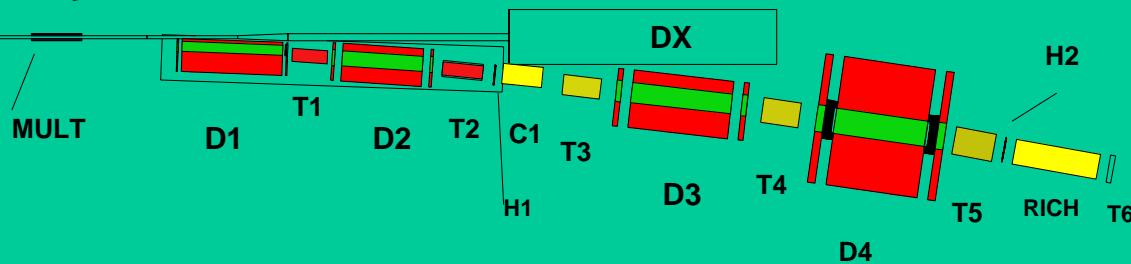
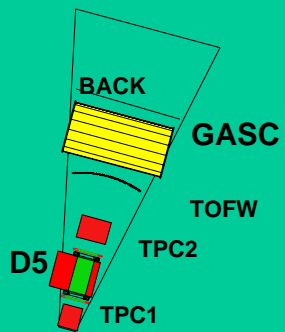
2006: 1 MHz collision rate;  $P \sim 0.6$

**Congratulations!!!**

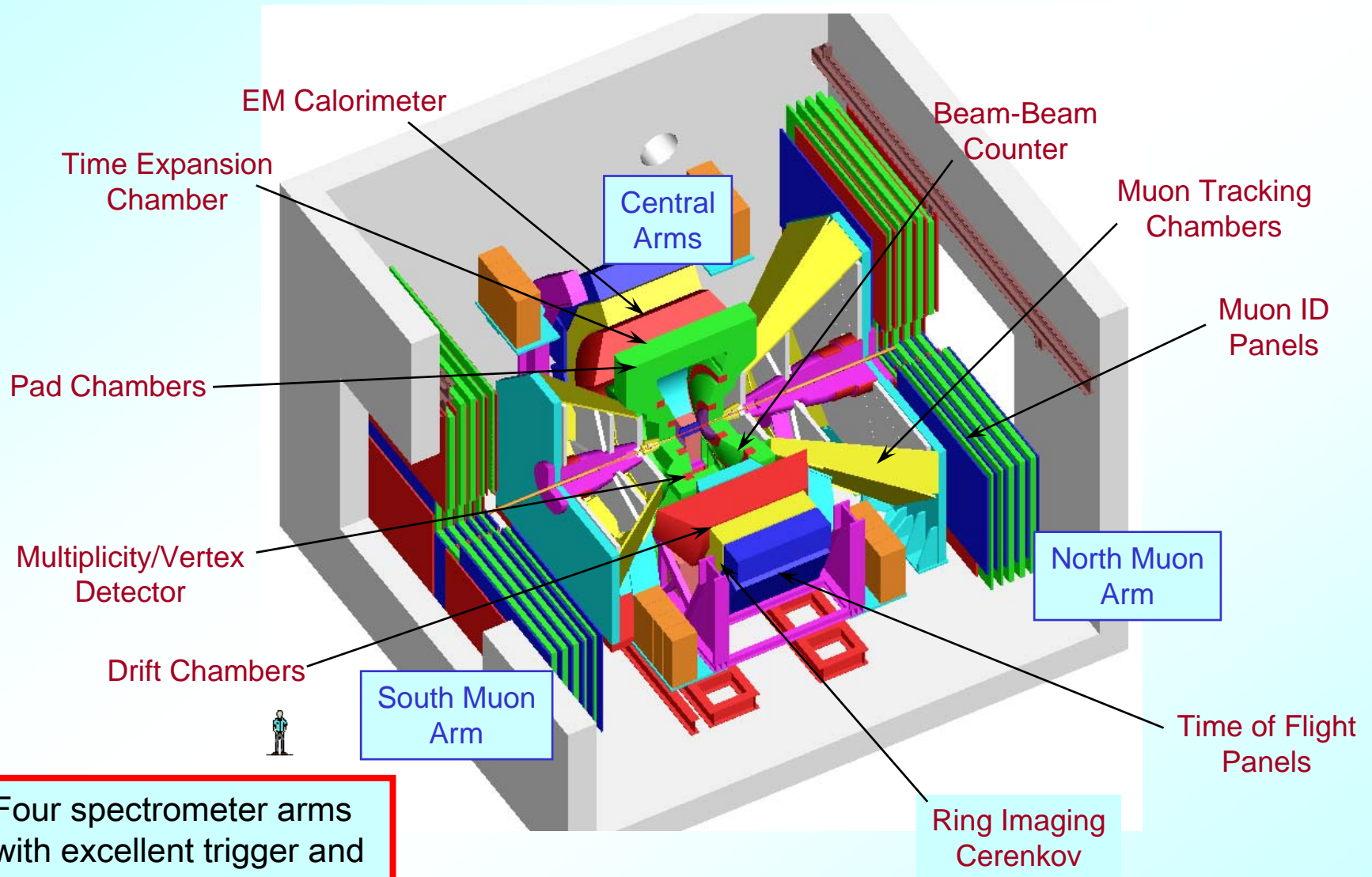
100% transverse spin!  
Two spectrometer arms  
with good particle ID at  
high momenta



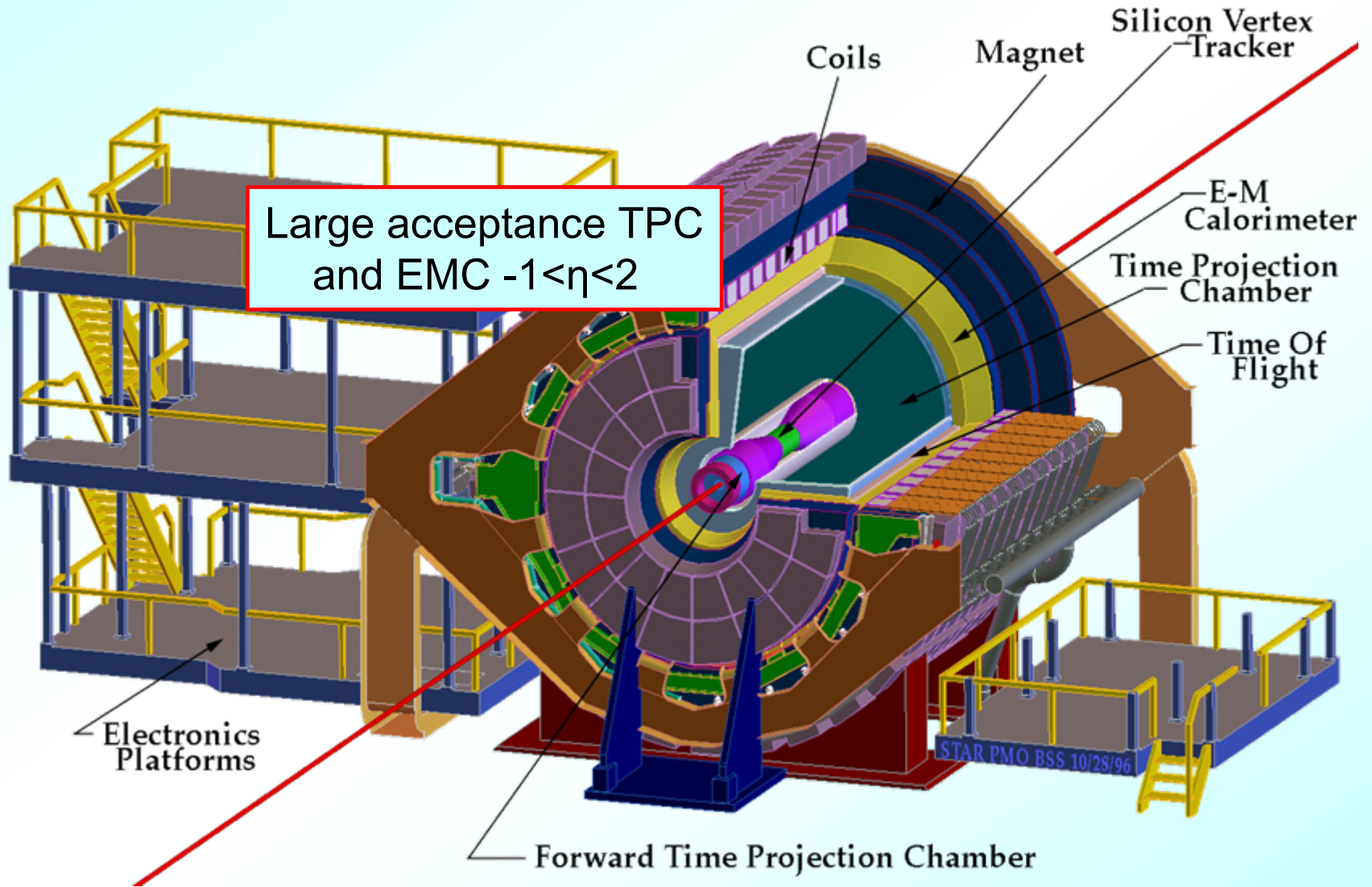
Mid rapidity spectrometer



Forward spectrometer

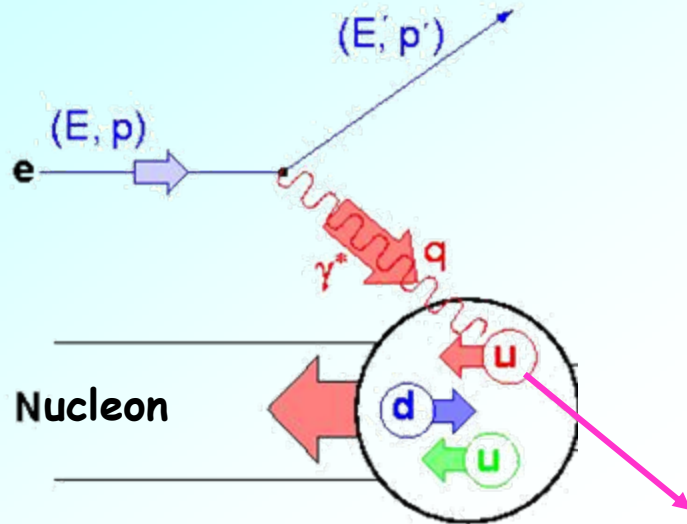


Four spectrometer arms with excellent trigger and DAQ capabilities.





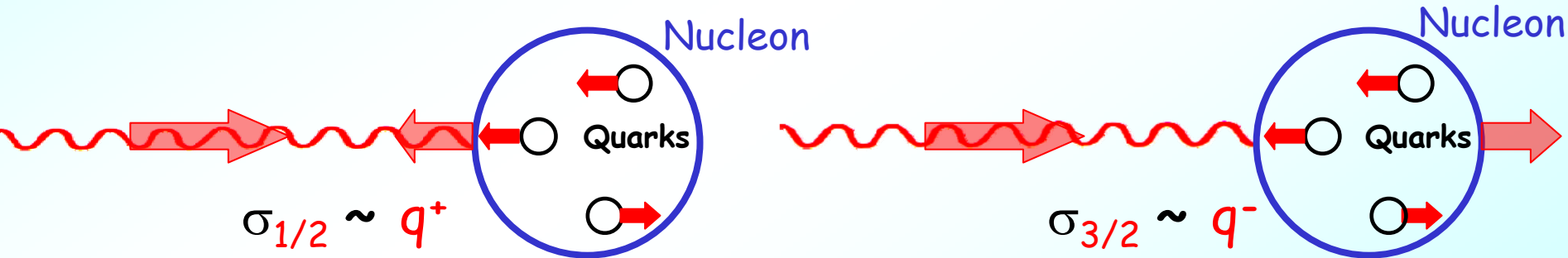
# Spin-dependent DIS



$$\nu = E - E'$$

$$Q^2 = -q^2$$

$x = Q^2 / (2M\nu)$  = fraction of nucleon's momentum carried by struck quark



Helicity DF:  $\Delta q(x) := q^+(x) - q^-(x)$

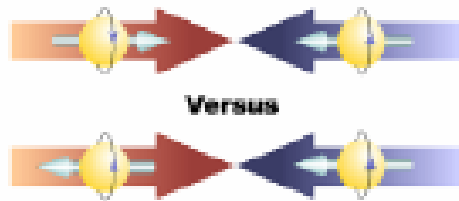
$$\text{Asymmetry: } A_1 = \frac{\sigma_{1/2} - \sigma_{3/2}}{\sigma_{1/2} + \sigma_{3/2}} \cong \frac{g_1}{F_1}$$

$$g_1(x) := \frac{1}{2} \sum_q z_q^2 \Delta q(x)$$

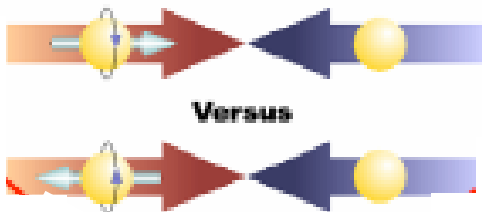
$$F_1(x) := \frac{1}{2} \sum_q z_q^2 q(x)$$

# Asymmetries in polarized pp collisions

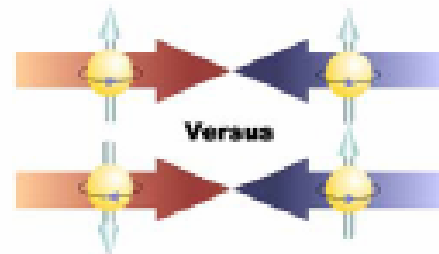
$$A_{LL} = \frac{\sigma(++)-\sigma(+ -)}{\sigma(++)+\sigma(+ -)}$$



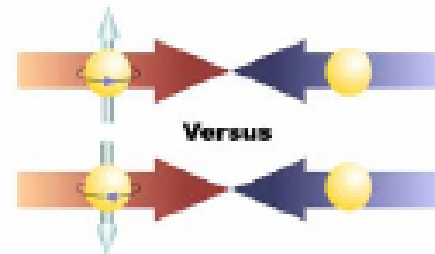
$$A_L = \frac{\sigma(+)-\sigma(-)}{\sigma(+)+\sigma(-)}$$



$$A_{TT} = \frac{\sigma(\uparrow\uparrow)-\sigma(\uparrow\downarrow)}{\sigma(\uparrow\uparrow)+\sigma(\uparrow\downarrow)}$$



$$A_T = \frac{\sigma(\uparrow)-\sigma(\downarrow)}{\sigma(\uparrow)+\sigma(\downarrow)}$$



# Parton helicity distributions from polarized pp

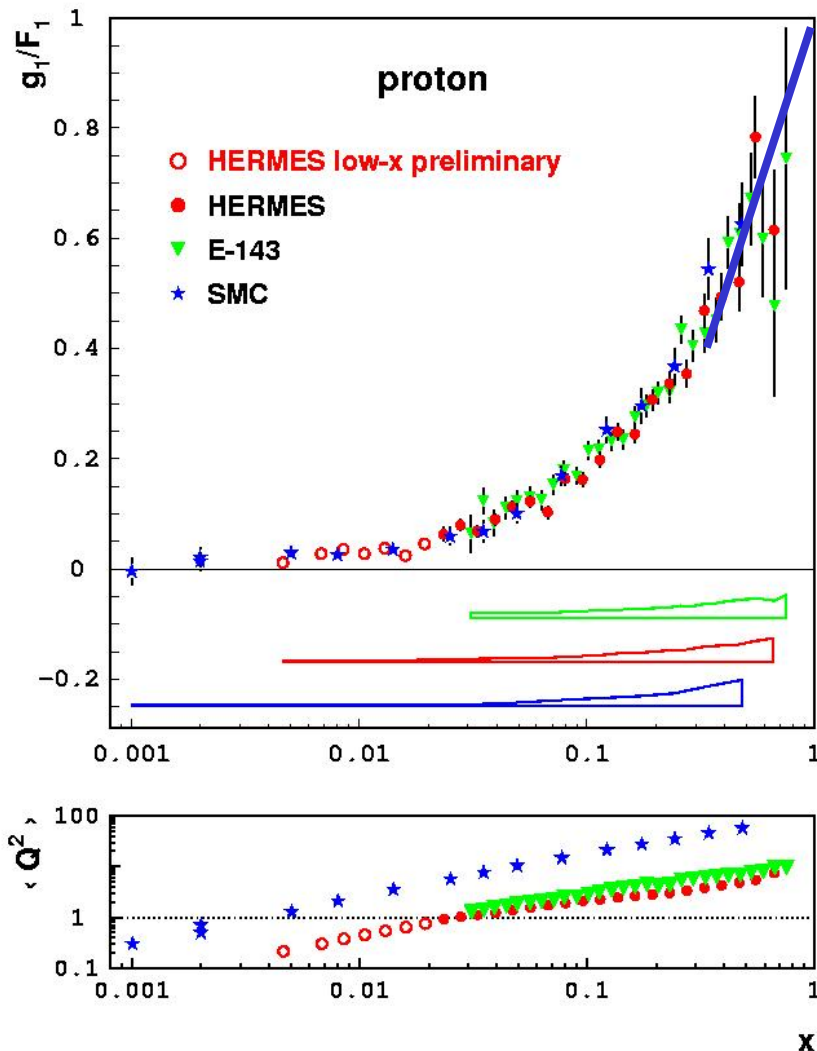
Reaction	Dom. partonic process	probes	LO Feynman diagram
<p>→ <math>\vec{p}\vec{p} \rightarrow \pi + X</math></p>	$\vec{g}\vec{g} \rightarrow gg$ $\vec{q}\vec{g} \rightarrow qg$	$\Delta g$	
<p>→ <math>\vec{p}\vec{p} \rightarrow \text{jet(s)} + X</math></p>	$\vec{g}\vec{g} \rightarrow gg$ $\vec{q}\vec{g} \rightarrow qg$	$\Delta g$	(as above)
<p>→ <math>\vec{p}\vec{p} \rightarrow \gamma + X</math>  <math>\vec{p}\vec{p} \rightarrow \gamma + \text{jet} + X</math>  <math>\vec{p}\vec{p} \rightarrow \gamma\gamma + X</math></p>	$\vec{q}\vec{g} \rightarrow \gamma q$ $\vec{q}\vec{g} \rightarrow \gamma q$ $\vec{q}\vec{q} \rightarrow \gamma\gamma$	$\Delta g$ $\Delta g$ $\Delta q, \Delta\bar{q}$	
<p><math>\vec{p}\vec{p} \rightarrow DX, BX</math></p>	$\vec{g}\vec{g} \rightarrow c\bar{c}, b\bar{b}$	$\Delta g$	
<p><math>\vec{p}\vec{p} \rightarrow \mu^+\mu^-X</math> (Drell-Yan)</p>	$\vec{q}\vec{q} \rightarrow \gamma^* \rightarrow \mu^+\mu^-$	$\Delta q, \Delta\bar{q}$	
<p>→ <math>\vec{p}\vec{p} \rightarrow (Z^0, W^\pm)X</math>  <math>p\vec{p} \rightarrow (Z^0, W^\pm)X</math></p>	$\vec{q}\vec{q} \rightarrow Z^0, \vec{q}'\vec{q} \rightarrow W^\pm$ $\vec{q}'\vec{q} \rightarrow W^\pm, q'\vec{q} \rightarrow W^\pm$	$\Delta q, \Delta\bar{q}$	

$\Delta g$

$\Delta q$

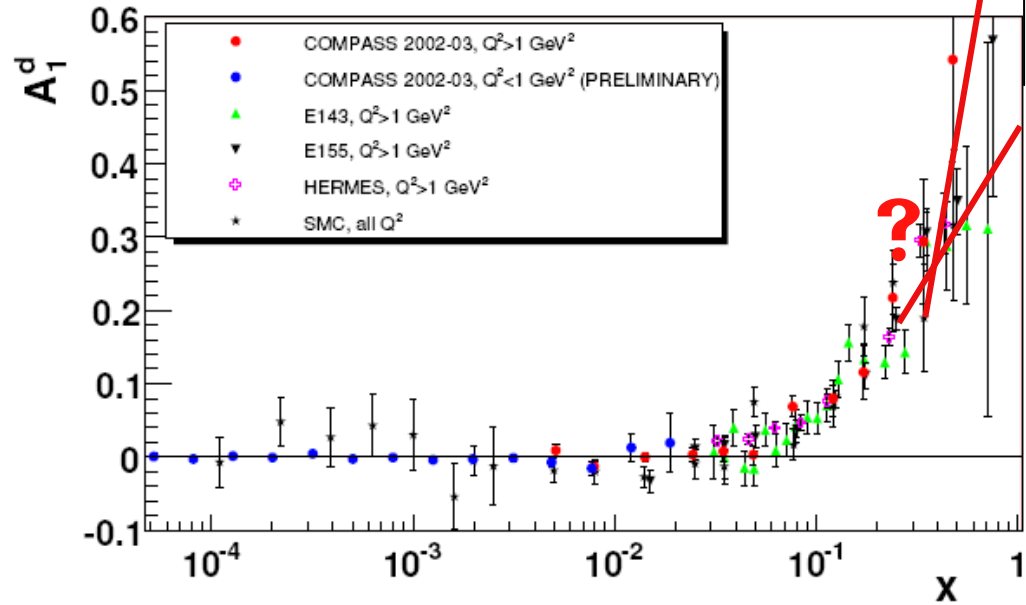
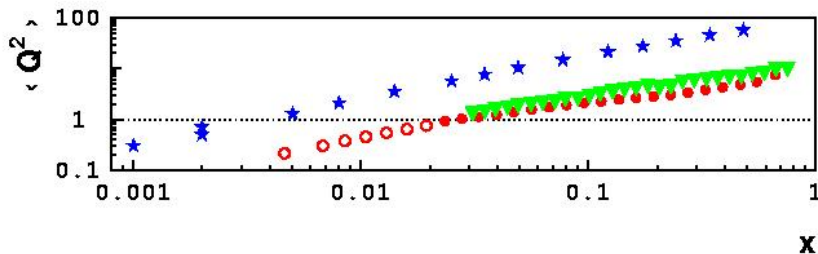
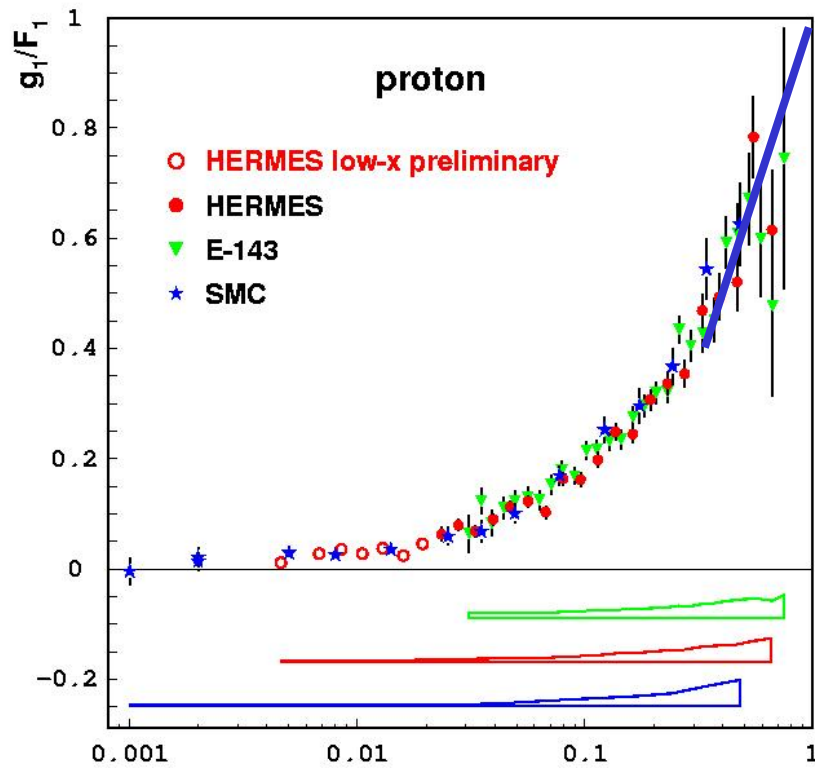
# Inclusive asymmetries in DIS

# $A_1 \cong g_1/F_1$ - Proton



- $g_1^p/F_1^p$  well known for  $x \searrow 10^{-3}$
- Excellent agreement between all experiments
- $g_1^p/F_1^p$  (within errors) ,independent' of  $Q^2$ , accuracy still insufficient to confirm  $Q^2$  dependence predicted by QCD
- $\langle Q^2 \rangle = f(x)$
- Extrapolation to  $x \rightarrow 0$  for  $Q^2 = Q_0^2$  ?
- $g_1^p/F_1^p \rightarrow 1$  for  $x \rightarrow 1$

# $A_1 \cong g_1/F_1$ - Proton and Deuteron



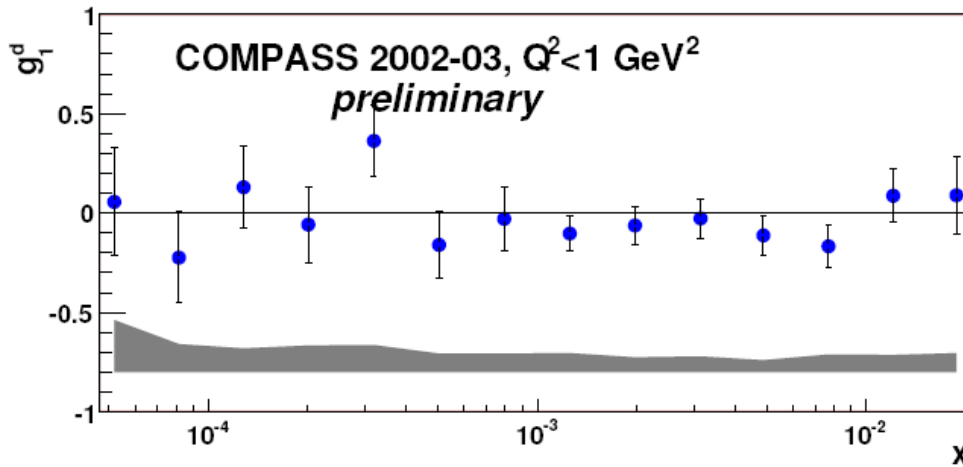
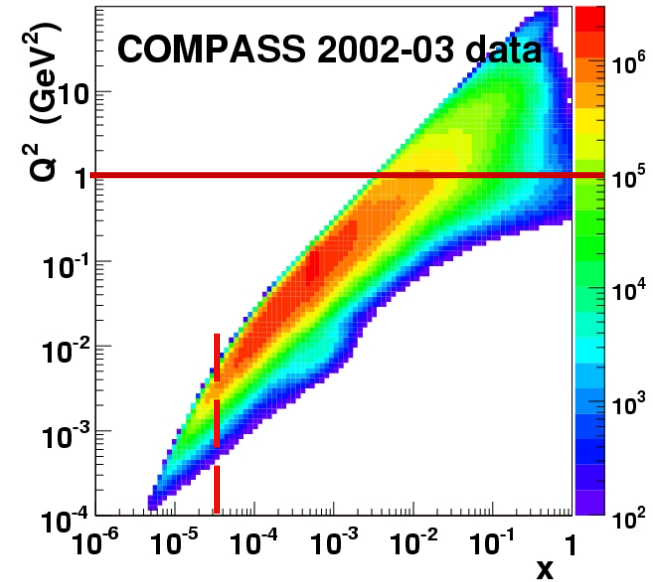
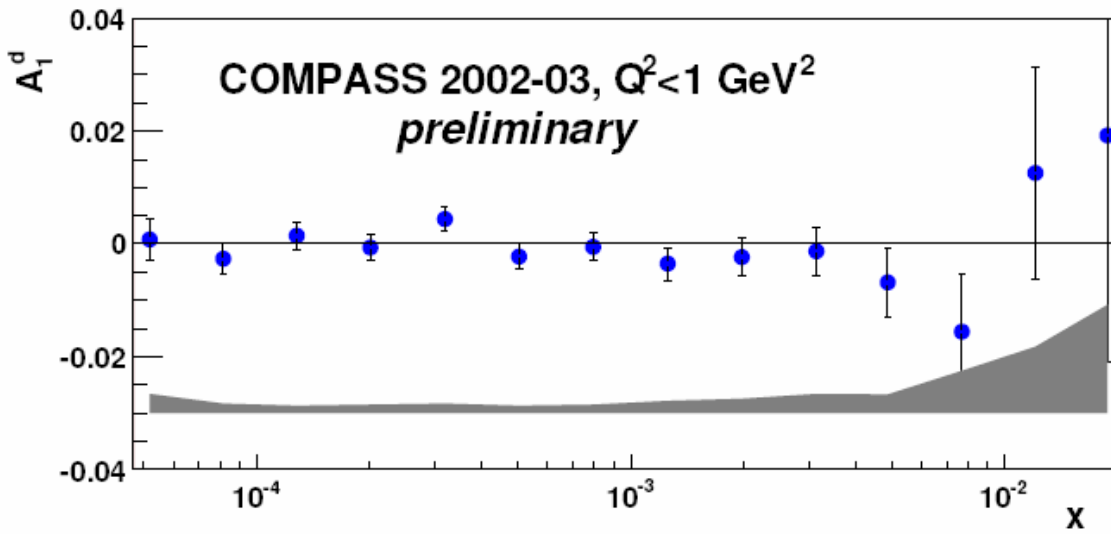
■  $A_1^d$  vanishes below  $x = 0.05$

■  $A_1^d \rightarrow ?$  for  $x \rightarrow 1$

■ High  $x$ : JLAB-12 GeV



# $A_1^d$ and $g_1^d$ at low $x$ and $Q^2$



■  $A_1^d$  compatible with 0 at low  $x$

■  $g_1^d$  compatible with 0 at low  $x$  and very low  $Q^2$

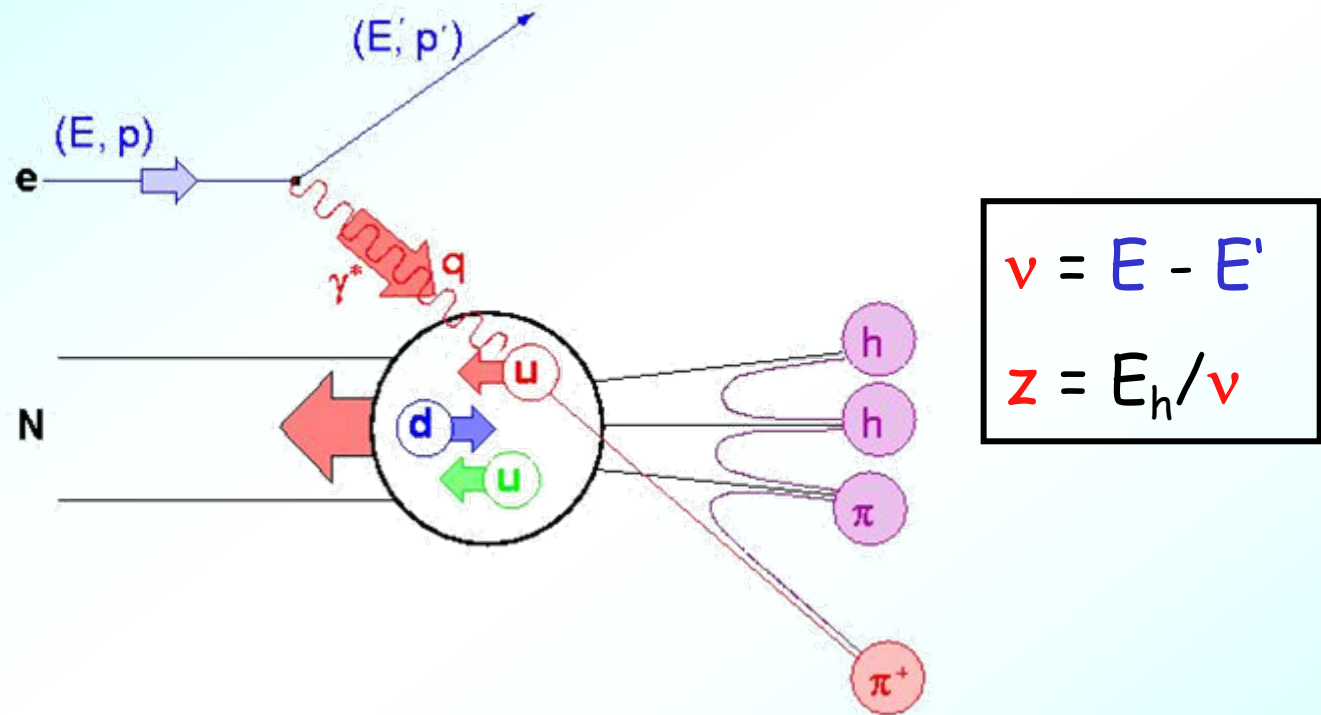
But:

■ What is the interpretation of  $g_1^d$  at these low values of  $Q^2$ ?

# Quark helicity distributions



# Quark helicity distributions from SIDIS



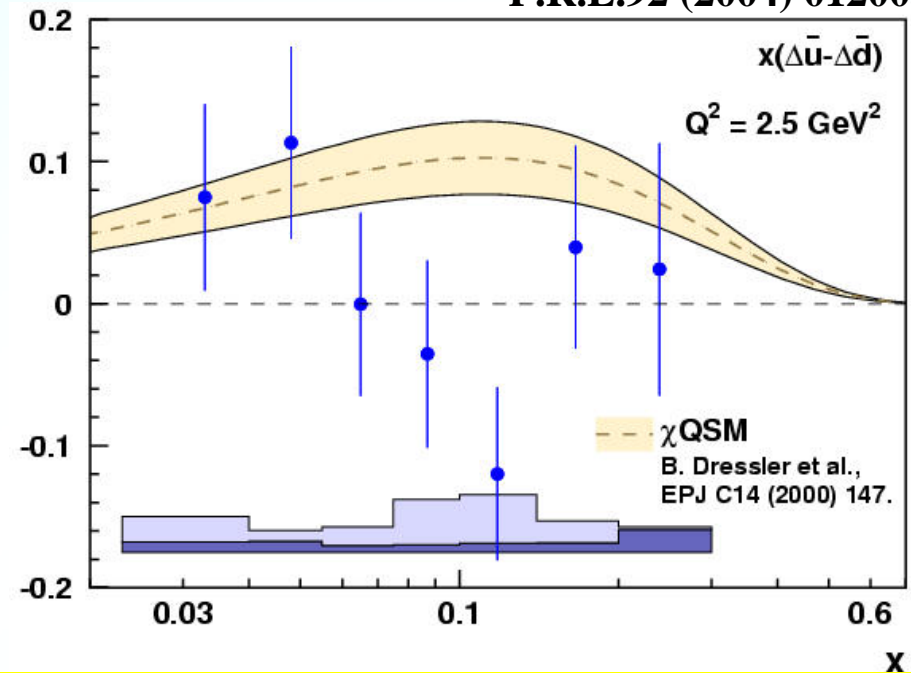
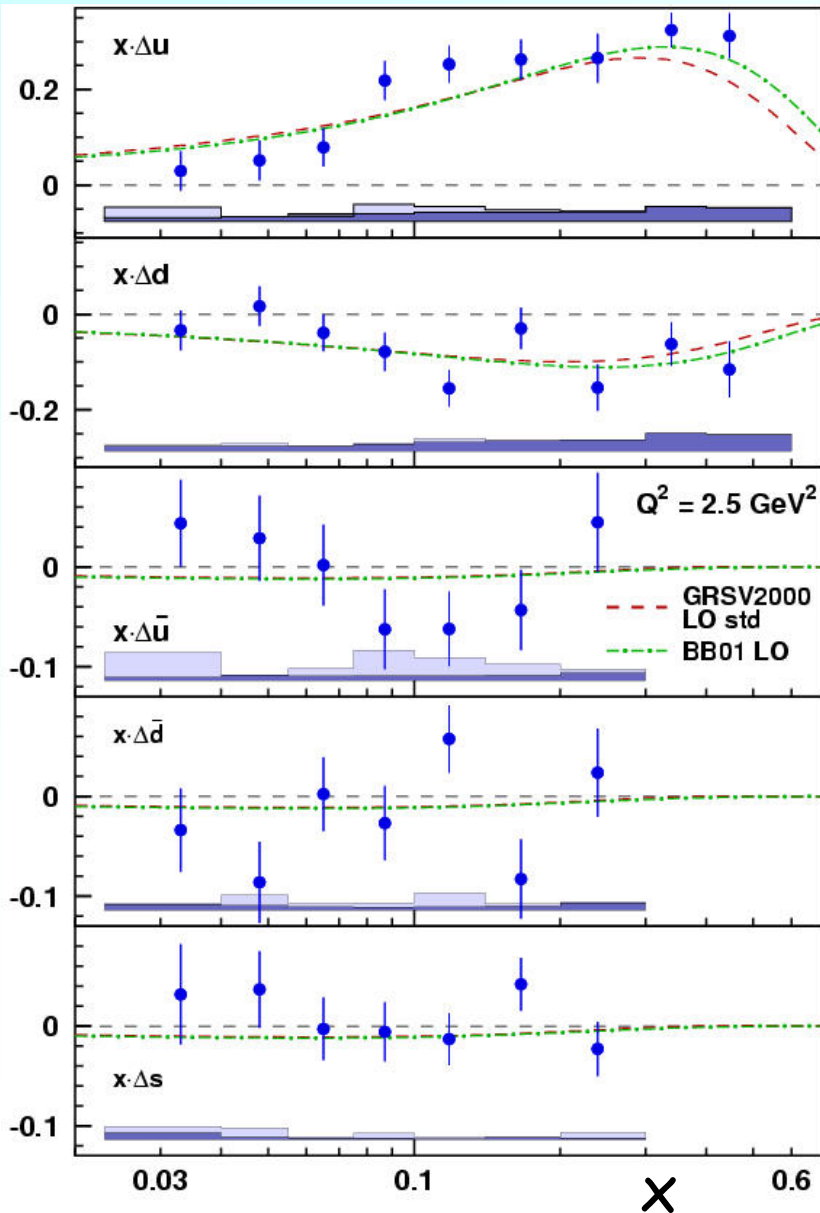
Leading **hadron** originates with large probability from **struck quark**

$D(z)$  := Fragmentation function (**FF**)

$q(x), \Delta q(x)$  := Distribution functions (**DF**)

Measure **hadron** asymmetries

$$A_1^h(x, z) = \frac{\sum_q z_q^2 \Delta q(x) D_q^h(z)}{\sum_q z_q^2 q(x) D_q^h(z)}$$



In measured range (0,023 - 0.6):

$$\int \Delta u(x) dx = +0.601 \pm 0.063$$

$$\int \Delta d(x) dx = -0.226 \pm 0.063$$

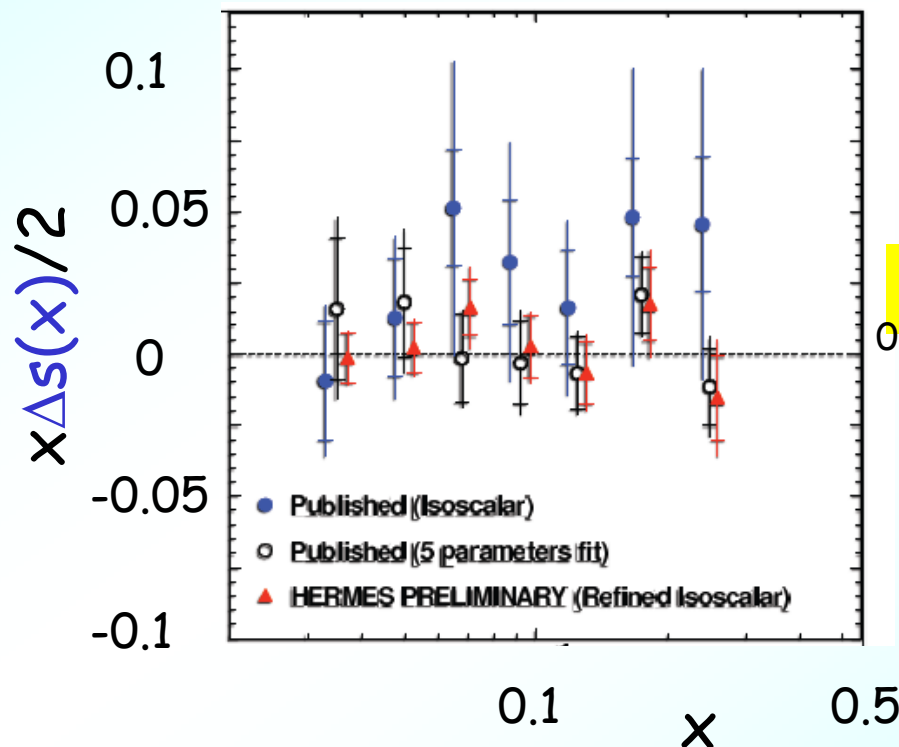
$$\int \Delta \bar{u}(x) dx = -0.002 \pm 0.043$$

$$\int \Delta \bar{d}(x) dx = -0.054 \pm 0.035$$

$$\int \Delta \bar{s}(x) dx = +0.028 \pm 0.034$$

## Inputs:

- Multiplicities for  $K^+$  and  $K^-$  with deuteron target
- Inclusive deuteron symmetry  $A_1^d$
- Asymmetries for  $K^+$  and  $K^-$  from deuteron:  $A_1^{K^+}$ ,  $A_1^{K^-}$



$$\int_{0.02}^1 \Delta s(x) dx = 0.006 \pm 0.029 \pm 0.007$$

# NLO QCD ( $\overline{\text{MS}}$ ) fits

Typical example: AAC06, hep-ph/0603213

## Assumptions:

Helicity distribution of sea quarks flavour symmetric

$\Delta u_V$  and  $\Delta d_V$  constraint by F and D (SU(3) symmetry)

## Results for $Q_0^2 = 1 \text{ GeV}^2$ :

$$\Delta\Sigma = 0.25 \pm 0.10$$

$$\Delta G = 0.47 \pm 1.08$$

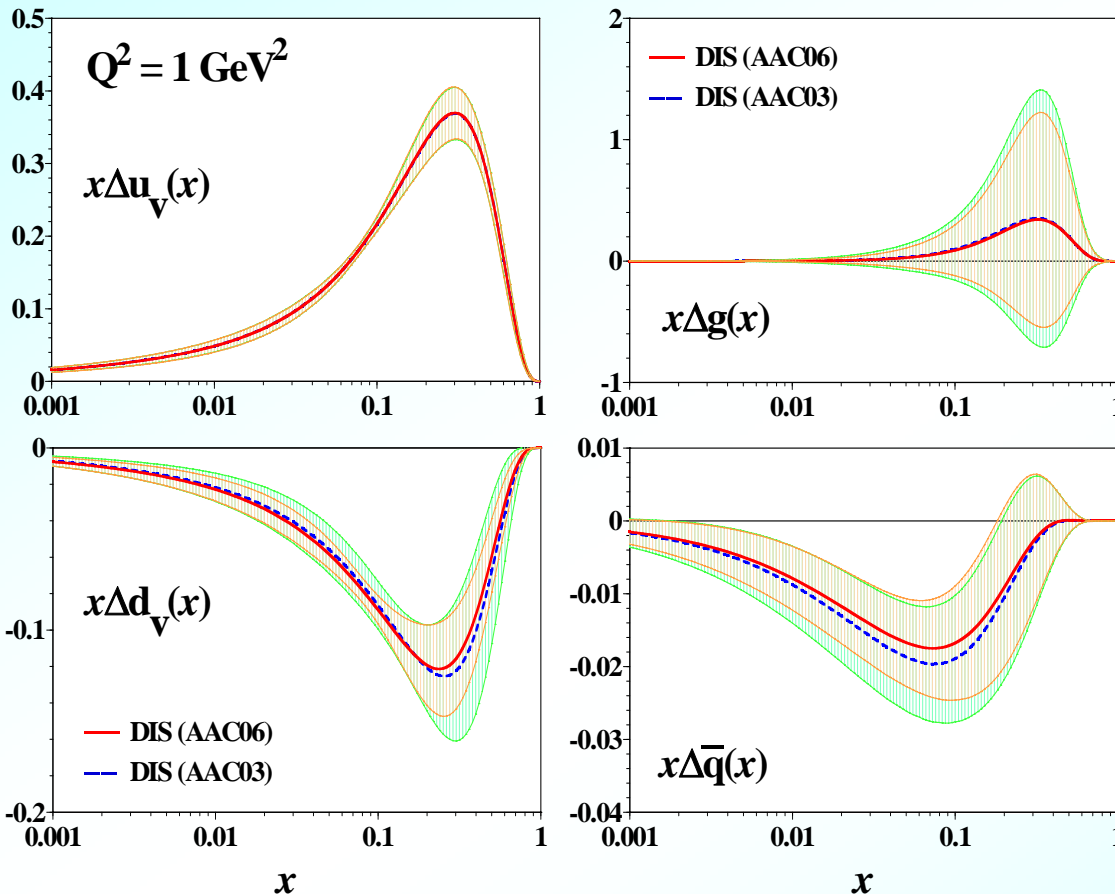
$\Delta G$  undetermined by only DIS

## Note: From $g_1^d$

$$\Delta\Sigma(0.01 < x < 1)_{\text{exp}} \cong 0.35 \pm 0.03$$

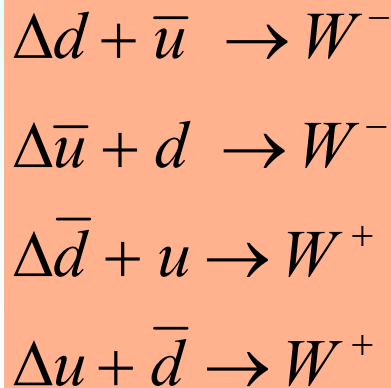
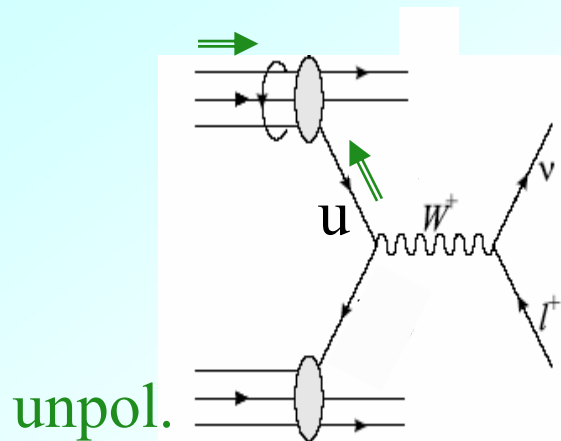
From NLO fits

$$\Delta\Sigma(0 < x < 0.01)_{\text{fit}} \cong -0.13 \pm 0.11$$



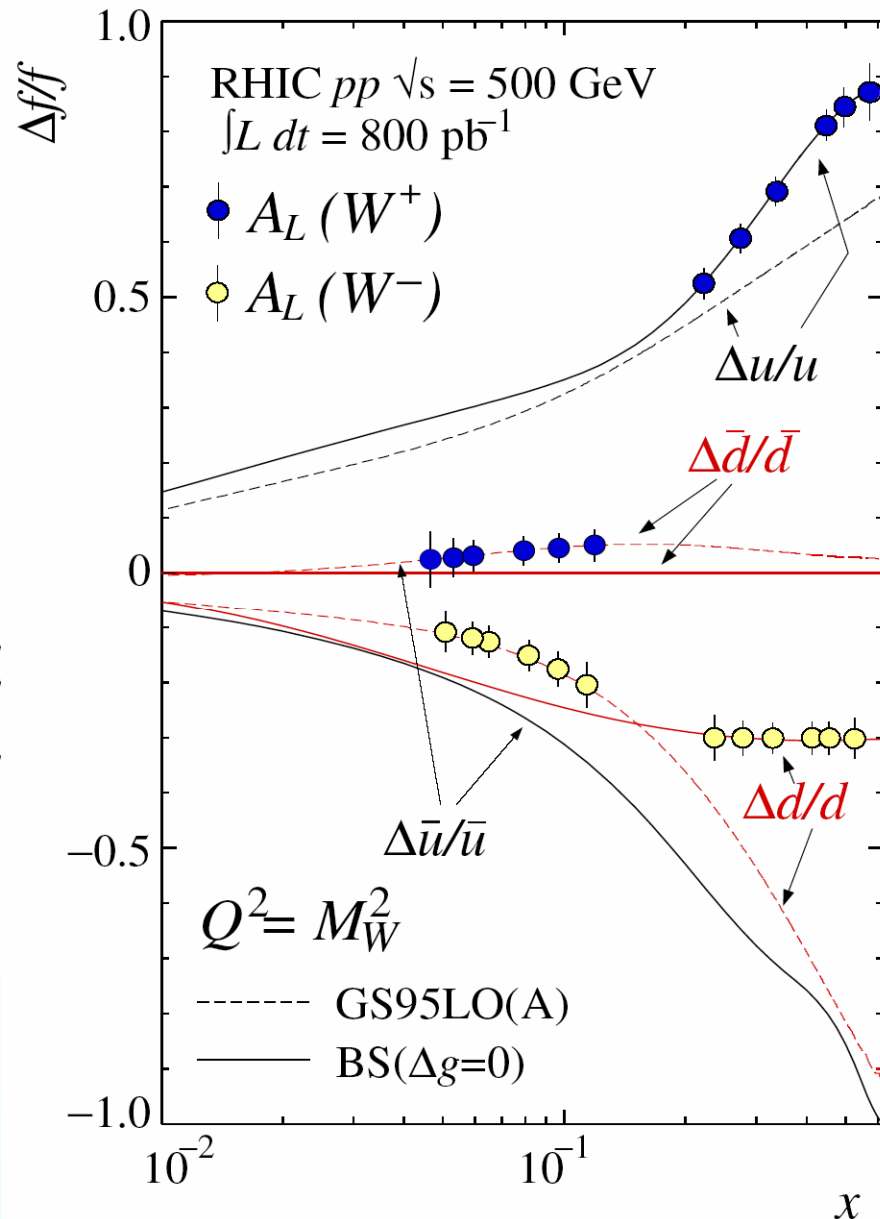
● Low- $x$  data urgently needed  $\rightarrow$  e-RHIC

# $\Delta q - \Delta \bar{q}$ at RHIC via $W$ production



$$\mathbf{A_L} = \frac{\sigma_+ - \sigma_-}{\sigma_+ + \sigma_-}$$

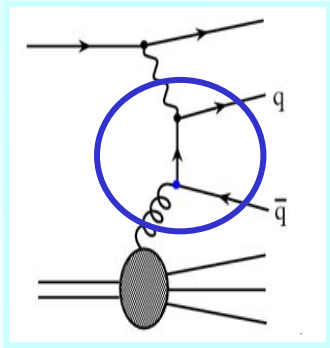
**Expected start: 2009**



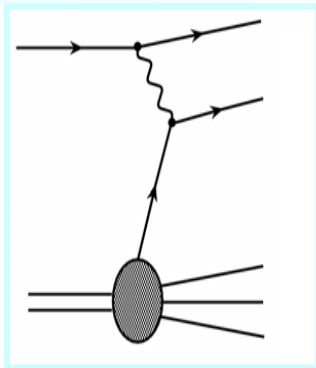
# The Gluon helicity distribution

# $\Delta G/G$ from high $p_T$ hadron pairs

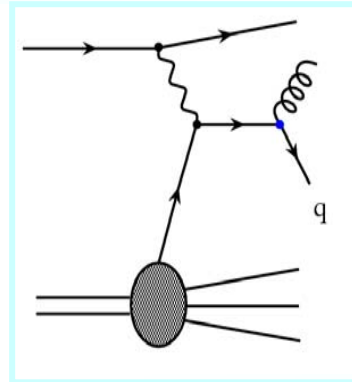
$$A_{||} = R_{PGF} \times a_{LL}^{PGF} \times \left( \frac{\Delta G}{G} \right) + A_{Bkg}$$



Photon  
Gluon  
Fusion

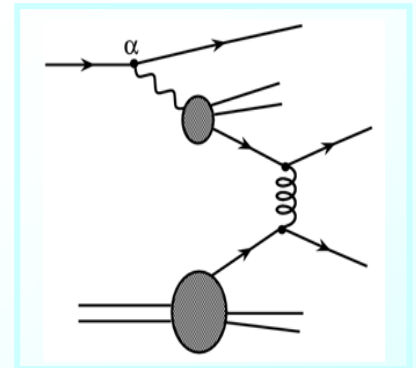


Leading  
Order



QCD  
Compton

+



Resolved  $\gamma$   
 $Q^2 < 1 \text{ (GeV/c)}^2$

$a_{LL}$  : calculable partonic asymmetries

$R_{PGF}$  : Monte Carlo is required to calculate  $R_{PGF}$



# $\Delta G/G$ from high $p_T$ hadron pairs

Two high  $p_T$  hadrons,  $p_T > 0.7 \text{ GeV}/c$ ,  $\Sigma p_T^2 > 2.5 (\text{GeV}/c)^2$

- $Q^2 < 1 (\text{GeV}/c)^2$  analysis - **large statistics** (PL B612 (2005) 154)
  - perturbative QCD scale from  $\Sigma p_T^2$
  - **PHYTIA MC** used to evaluate physical Bkg, low  $p_T$ , resolved  $\gamma$ ,
- $Q^2 > 1 (\text{GeV}/c)^2$  analysis - **lower statistics**
  - perturbative QCD scale from  $Q^2$ ,
  - **LEPTO MC** used to evaluate Bkg, better controlled

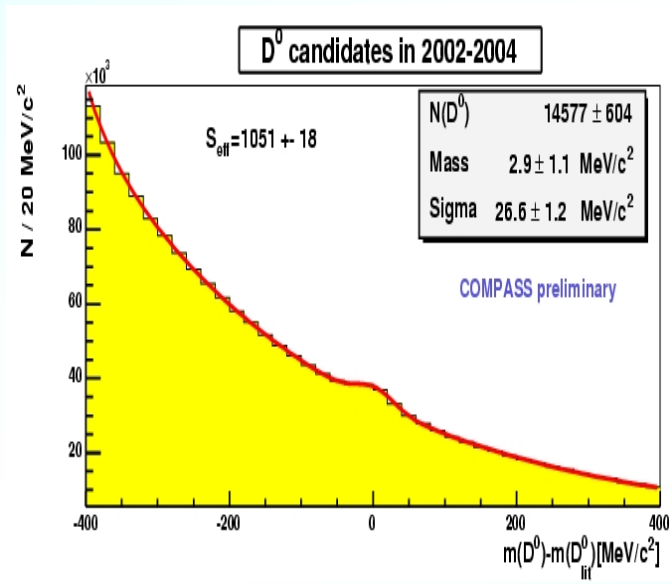
**Different data sets and analysis. Independent results**



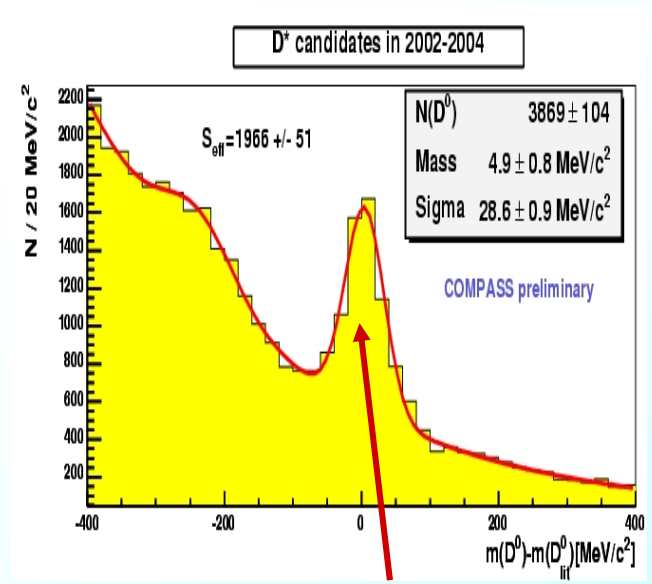


# $\Delta G/G$ from open charm

$D^0 \rightarrow K + \pi$   
untagged

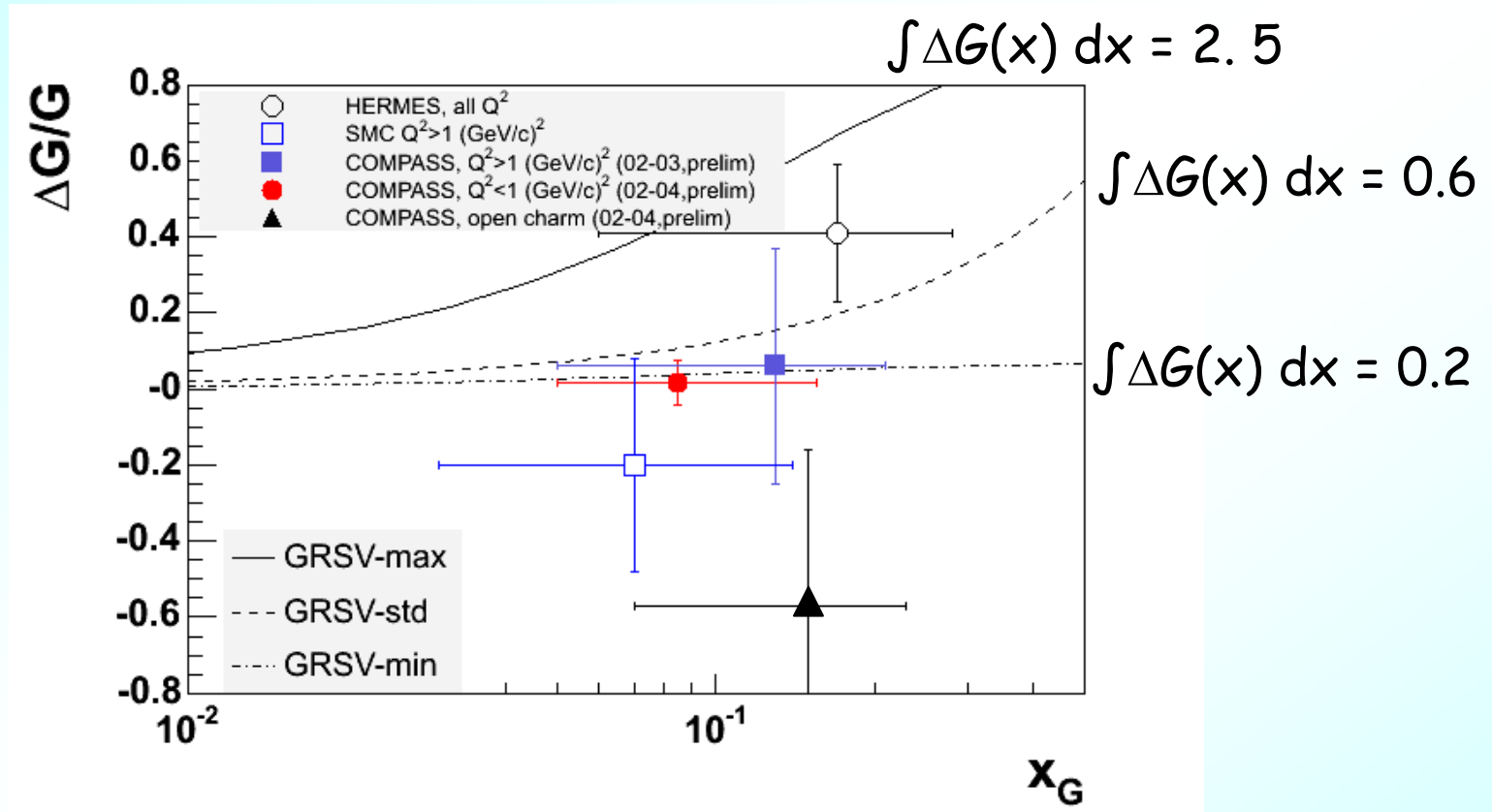


$D^* \rightarrow D^0 + \pi_s \rightarrow K + \pi + \pi$   
tagged



We have now estimate for  $\sigma$  (nb)

# $\Delta G/G$ from high $p_T$ hadron pairs and open charm



High  $p_T$  hadron pairs,  $Q^2 > 1 \text{ GeV}^2$ :  $\Delta G/G = 0.06 \pm 0.31$  (stat)  $\pm 0.06$  (syst)  $\langle x_g \rangle \sim 0.13$

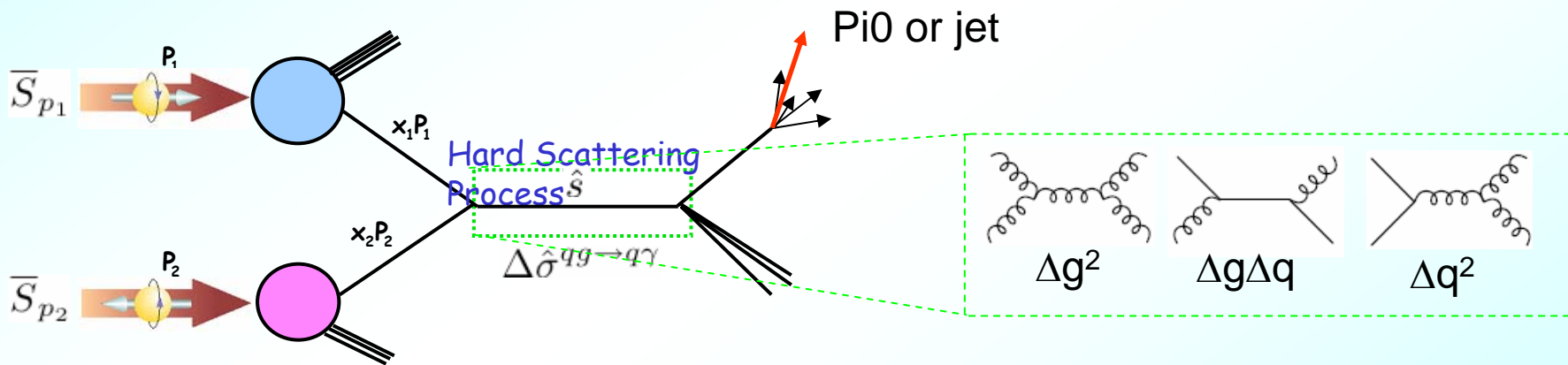
High  $p_T$  hadron pairs,  $Q^2 < 1 \text{ GeV}^2$ :  $\Delta G/G = 0.016 \pm 0.058$  (stat)  $\pm 0.055$  (syst)  $\langle x_g \rangle \sim 0.085$

Open charm:  $\Delta G/G = -0.57 \pm 0.41$   $\langle x_g \rangle \sim 0.15$

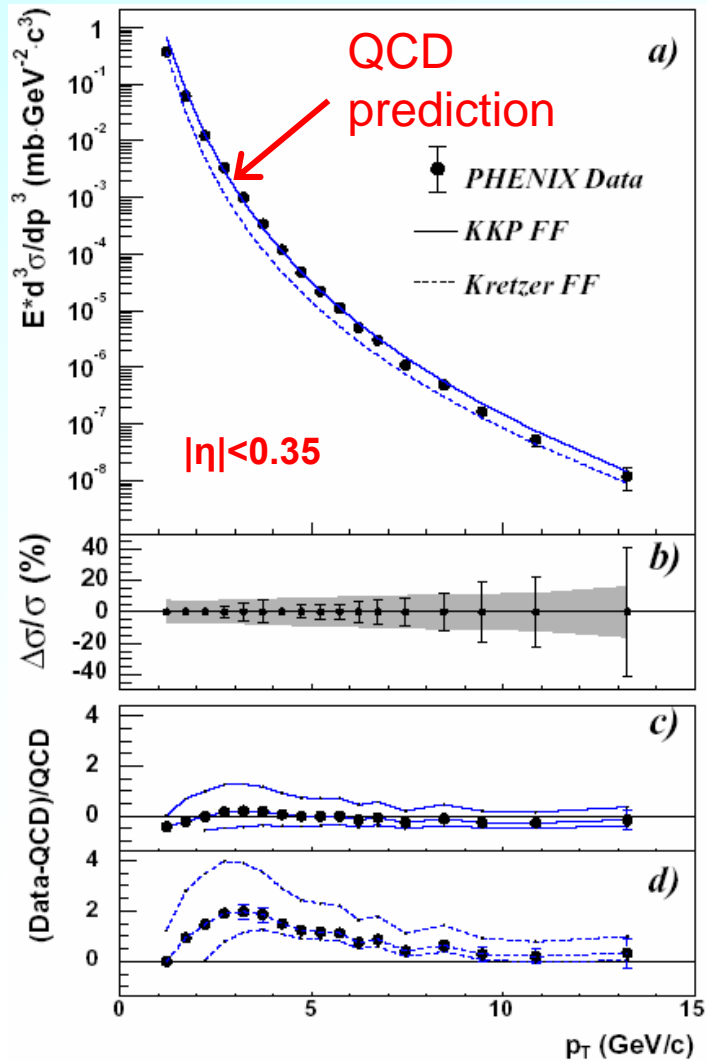
$\Delta G/G$  ( $x_g \approx 0.1$ ) is small

# $\Delta G/G$ from polarized pp collisions

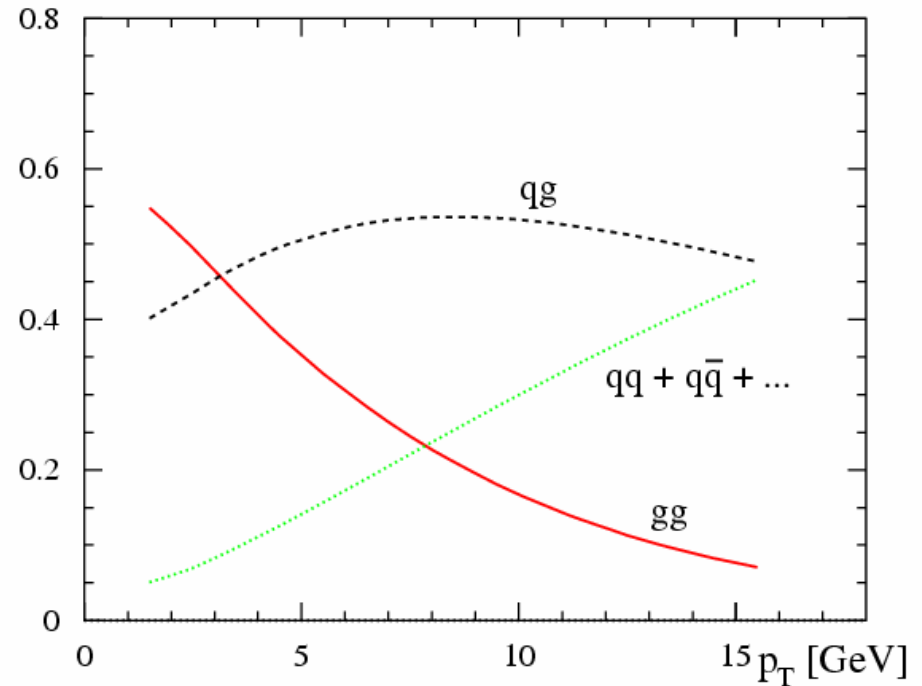
How to measure  $\Delta g$ :

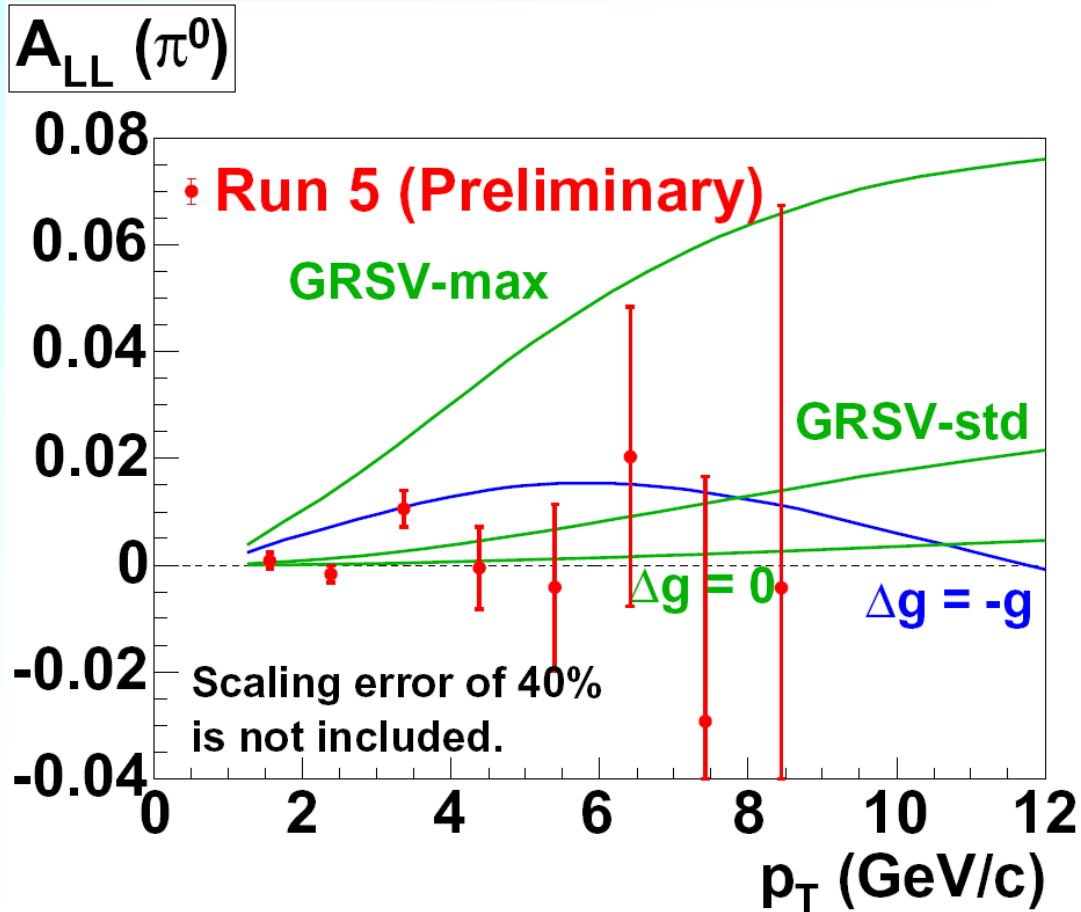


$$A_{LL}^{\pi^0} = \frac{\sigma_{++} - \sigma_{+-}}{\sigma_{++} + \sigma_{+-}} \sim a_{gg} * \Delta g^2 + b_{gq} * \Delta g + c_{qq}$$



## Mid-rapidity: PHENIX



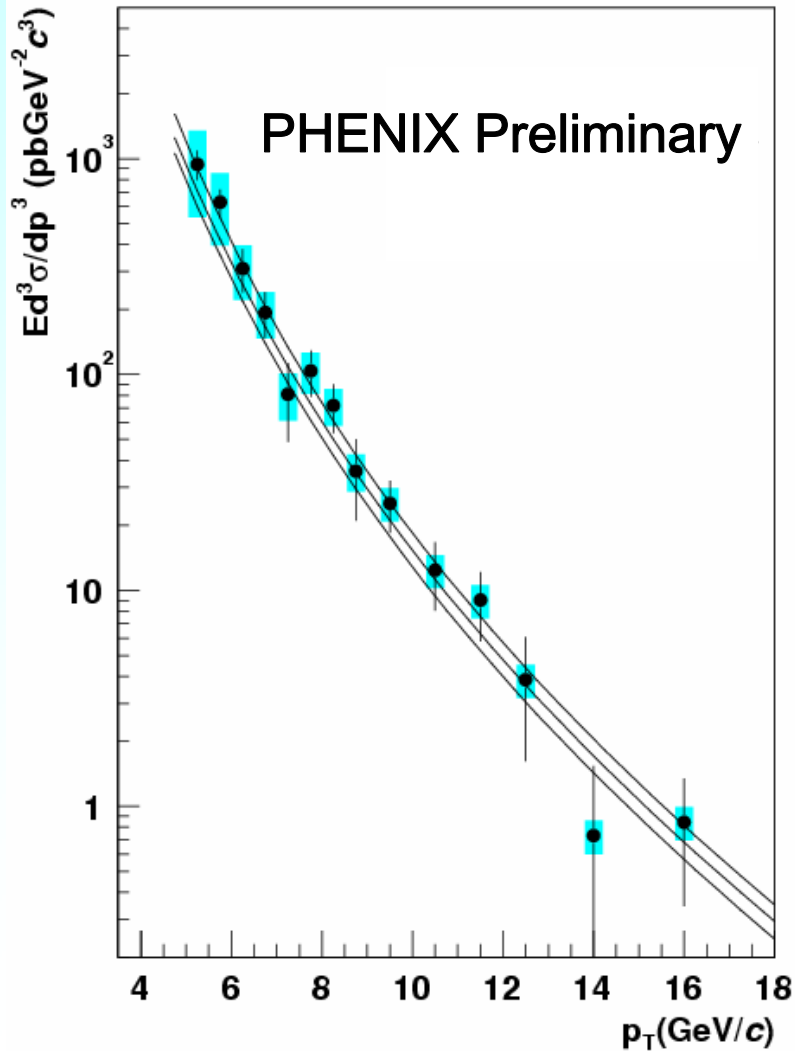


Theory model	C.L. (%)
GRSV-std	21.7-17.1
*GRSV-max ( $\Delta g = g$ )	0.0-0.0
*GRSV $\Delta g = 0$	16.7-18.4
*GRSV $\Delta g = -g$	0.7-0.0

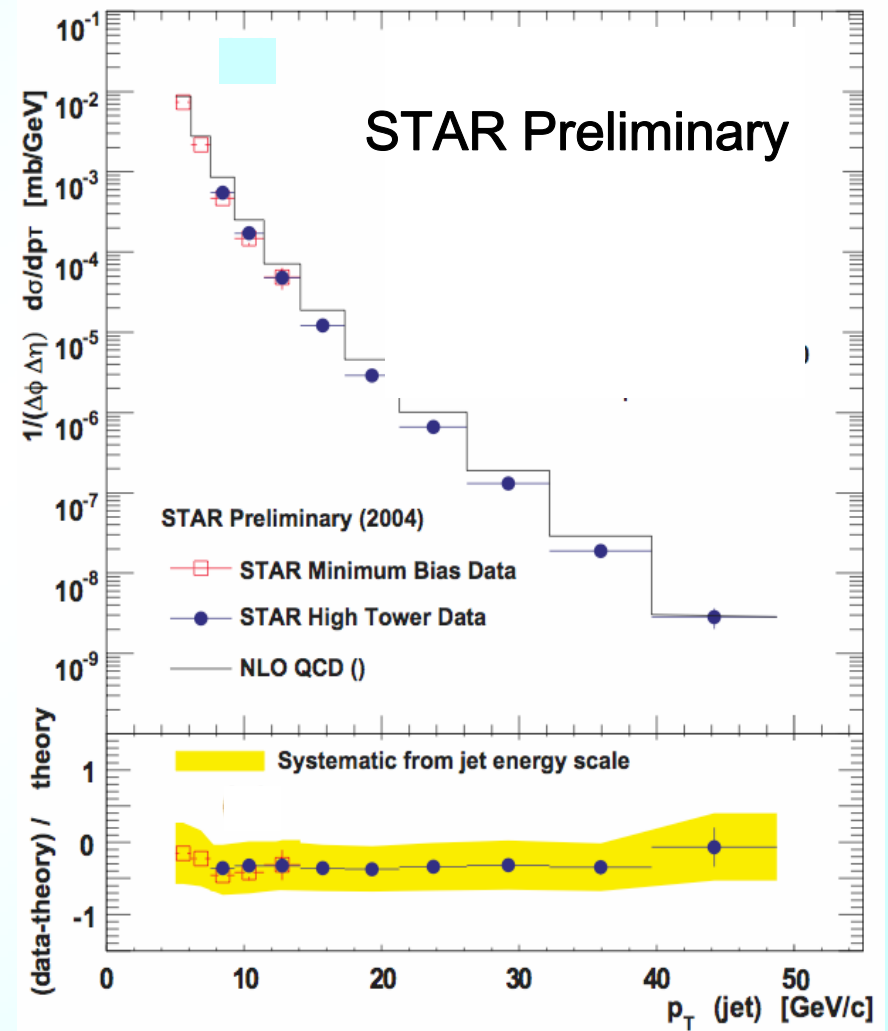
GRSV: M. Glück, E. Reya, M. Stratmann, and W. Vogelsang, Phys. Rev. D 53 (1996) 4775.

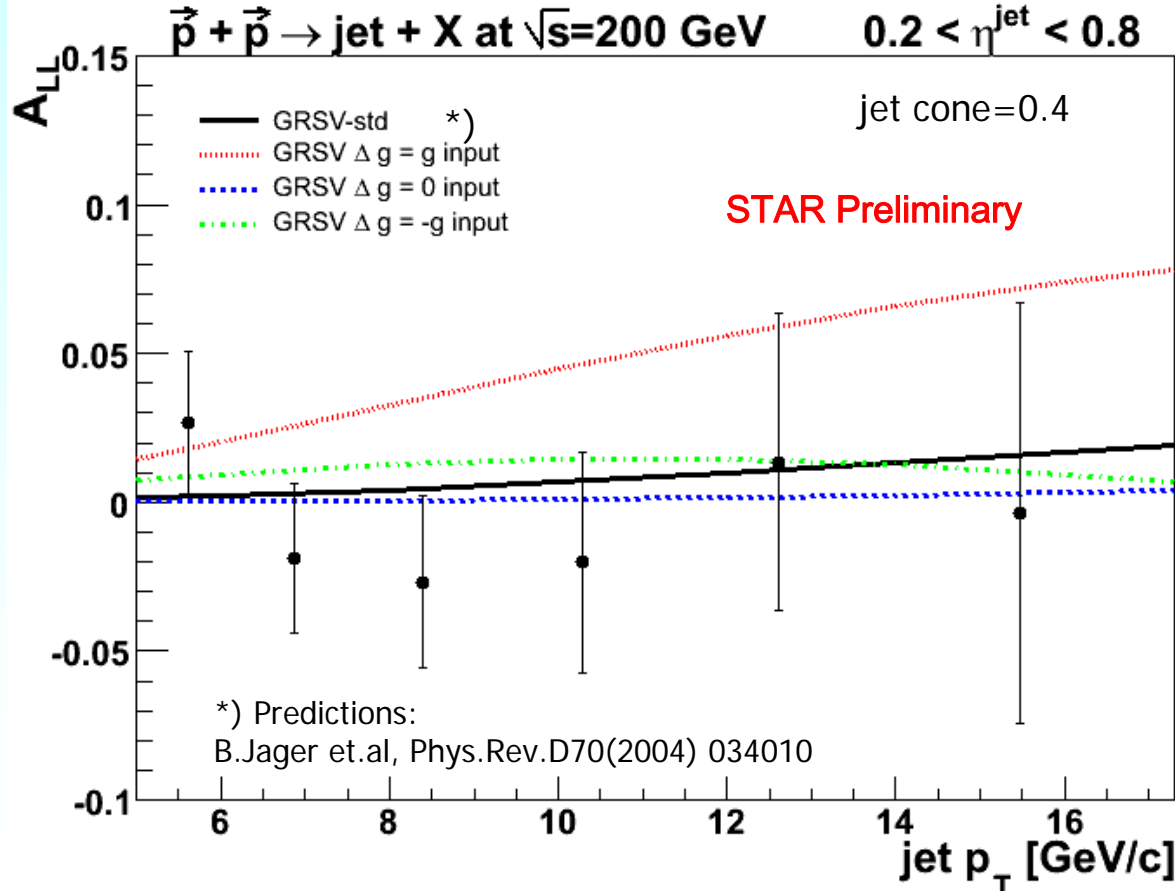
\* At input scale:  
 $Q^2 = .4 \text{ GeV}$

### Direct Photon Cross section



### Inclusive Jet Cross section



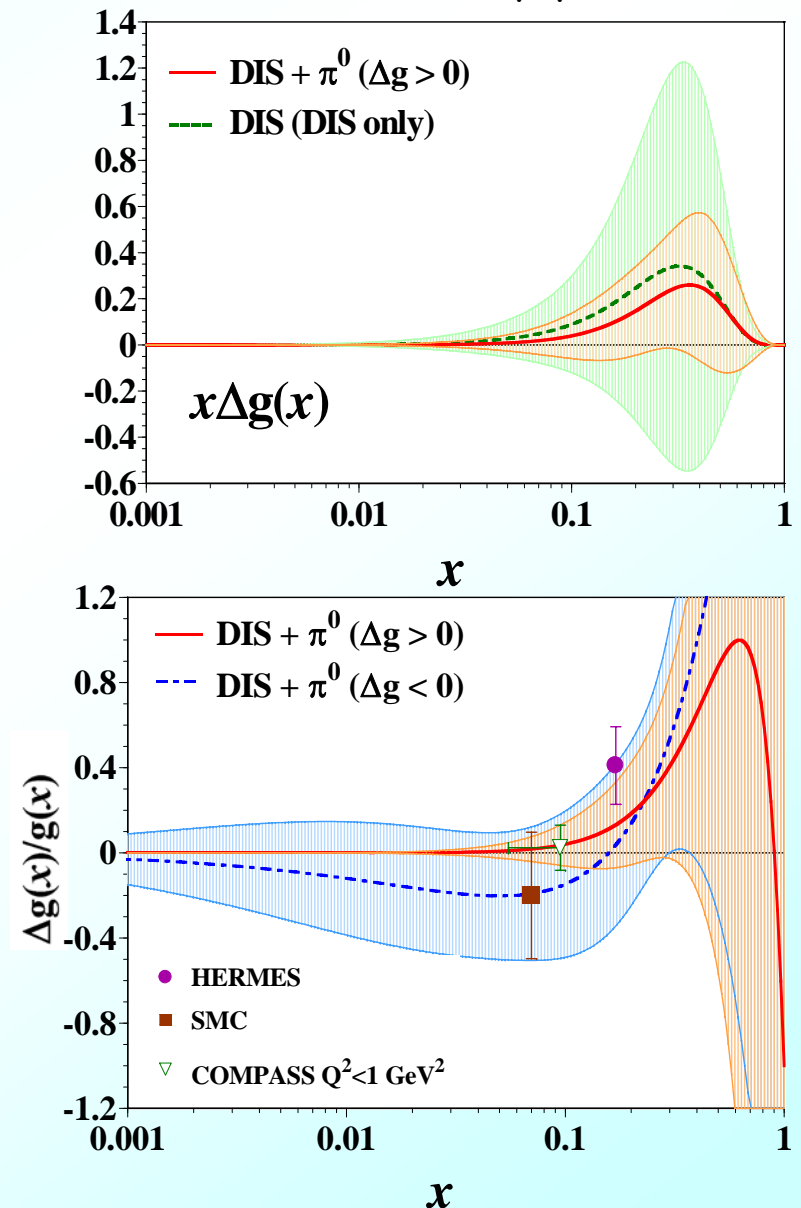


- Results limited by statistical precision
- Total systematic uncertainty  $\sim 0.01$  (STAR) + beam pol. (RHIC)
- GRSV-max gluon polarization scenario disfavored

- Significant reduction of  $\Delta G$  uncertainty  
 $\Delta G = 0.31 \pm 0.32$  (DIS+p $^0$ )  
 $\Delta G = 0.47 \pm 1.08$  (DIS only)

- Sign problem : gg dominates  
 Similar  $\chi^2$  for ( $\Delta G(x) > 0$ ) and ( $\Delta G(x) < 0$ )

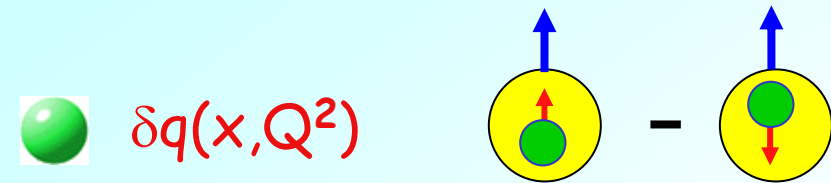
- Consistent results for partial 1<sup>st</sup> moment ( $0.1 < x < 1$ )  
 $\Delta G(x) > 0$ :  $0.30 \pm 0.30$   
 $\Delta G(x) < 0$ :  $0.32 \pm 0.42$





# Transverse Spin physics

# Transversity DF $\delta q(x)$ and Sivers DF $f_{1T}^{\perp q}(p_T^2)$ ( $p_T^2$ )

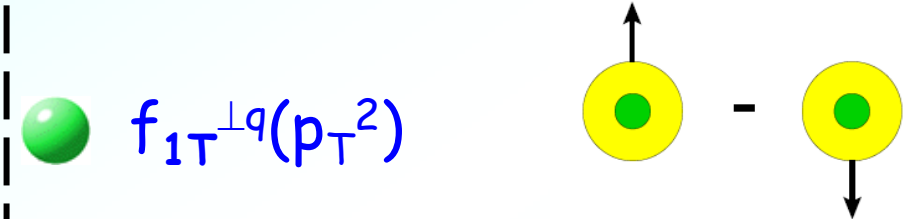
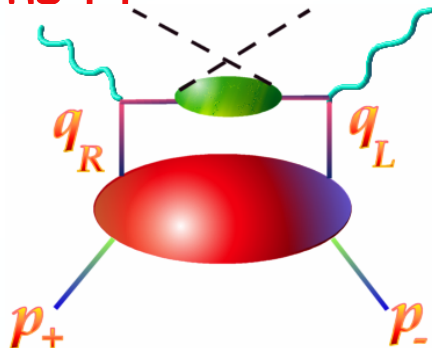


● DF of transv. polarized quarks in a transv. polarized nucleon

● 3<sup>rd</sup> leading twist DF. As important as  $q(x)$  and  $\Delta q(x)$

●  $\delta q$  is chiral-odd: not accessible in DIS

● Need 2<sup>nd</sup> chiral-odd object Collins FF



● DF of unpolarised quark with transv. momentum  $p_T$  in a transv. polarised nucleon.

● Non-zero Sivers DF requires non-vanishing orbital angular momentum in nucleon WF

● Chiral-even & naive T-odd

# Azimuthal angular asymmetries in SIDIS

$$A_{UT}(\phi, \phi_S) = \frac{1}{S_{\perp}} \frac{N^{\uparrow}(\phi, \phi_S) - N^{\downarrow}(\phi, \phi_S)}{N^{\uparrow}(\phi, \phi_S) + N^{\downarrow}(\phi, \phi_S)}$$

U: unpol. beam

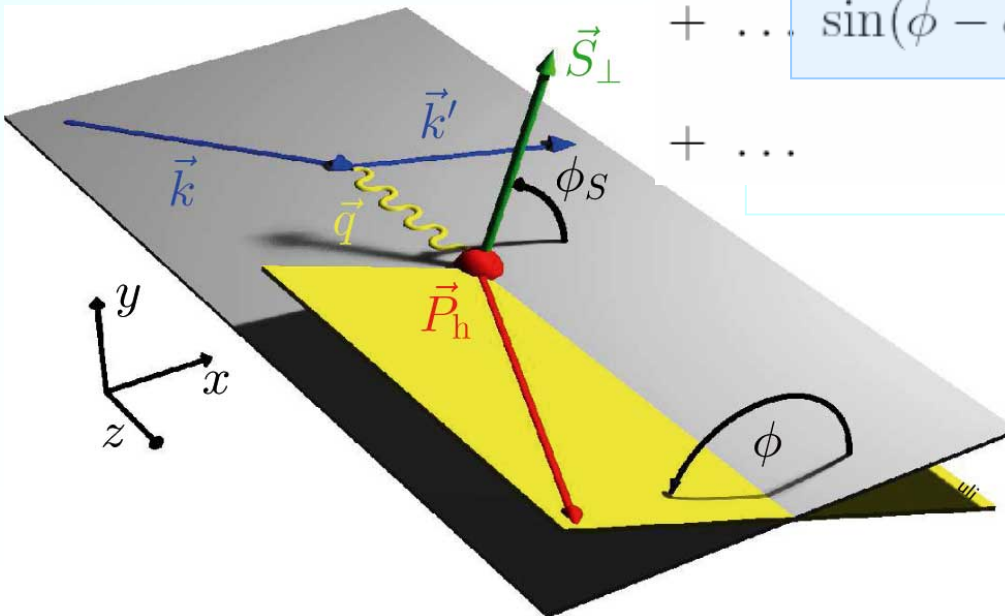
T: transv. pol. Target

$$A_{UT}(\phi, \phi_S) \sim \dots \sin(\phi + \phi_S) \frac{\sum_q e_q^2 \mathcal{I} \left[ \dots \delta q(x, \vec{p}_T^2) \cdot H_1^{\perp q}(z, \vec{k}_T^2) \right]}{\sum_q e_q^2 q(x) \cdot D_1^q(z)}$$

Collins

$$+ \dots \sin(\phi - \phi_S) \frac{\sum_q e_q^2 \mathcal{I} \left[ \dots f_{1T}^{\perp q}(x, \vec{p}_T^2) \cdot D_1^q(z, \vec{k}_T^2) \right]}{\sum_q e_q^2 q(x) \cdot D_1^q(z)}$$

Sivers

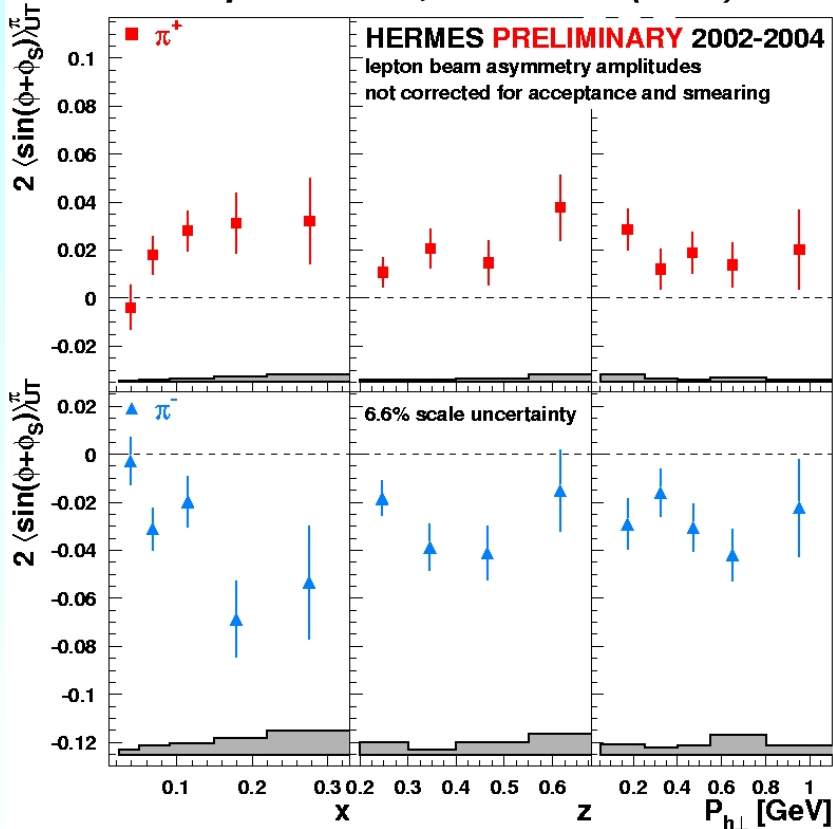


$\mathcal{I}[\dots]$ : convolution integral over quark transverse momenta  $\vec{p}_T$  and  $\vec{k}_T$

# Collins amplitudes for $\pi^{+/-}$ (proton)

$$A_{UT}^{\sin(\phi+\phi_S)} \sim \delta q(x) \cdot H_1^{\perp(1/2)}(z)$$

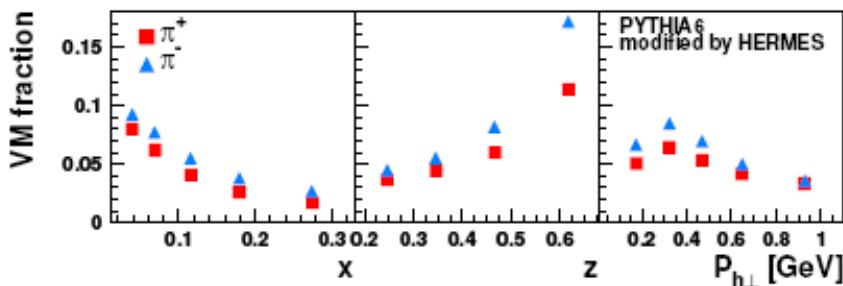
also: A. Airapetian et al, P. R. L. 94 (2005) 012002



- Non-zero Collins effect
- Both Collins FF and transversity DF sizeable
- Surprisingly large  $\pi^-$  asymmetry
- Possible source: large contribution (with opposite sign) from unfavored fragmentation, i.e.  $u \rightarrow \pi^-$

$$H_{1,disf} \approx -H_{1,fav}$$

- Substantial contribution to pion sample from exclusively produced vector mesons (PYTHIA)

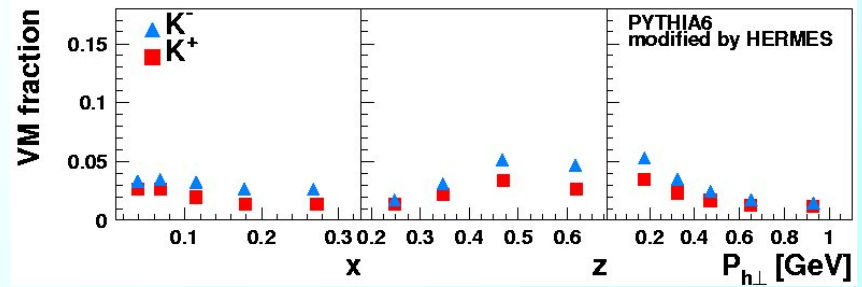
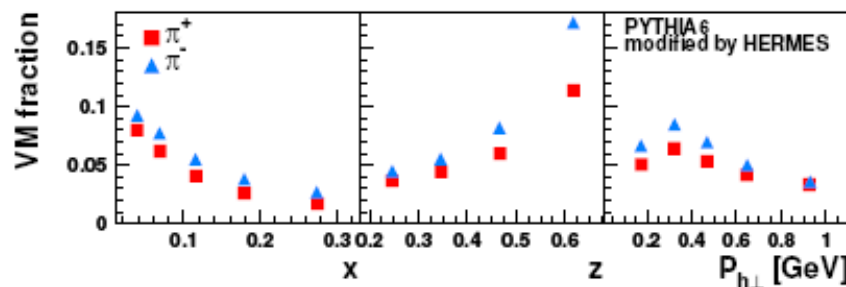
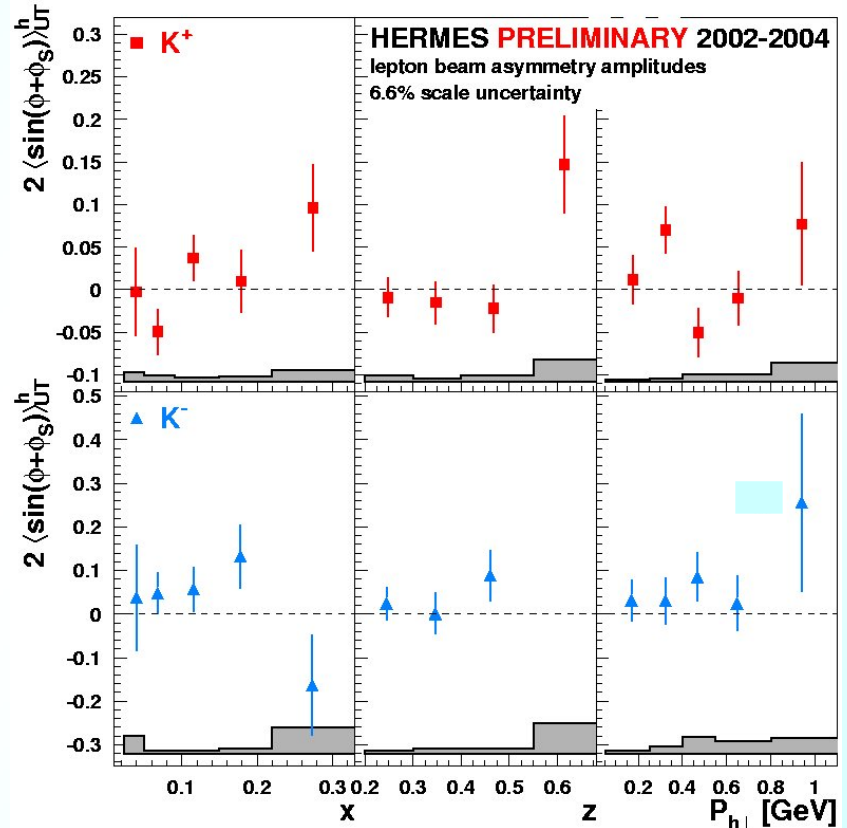
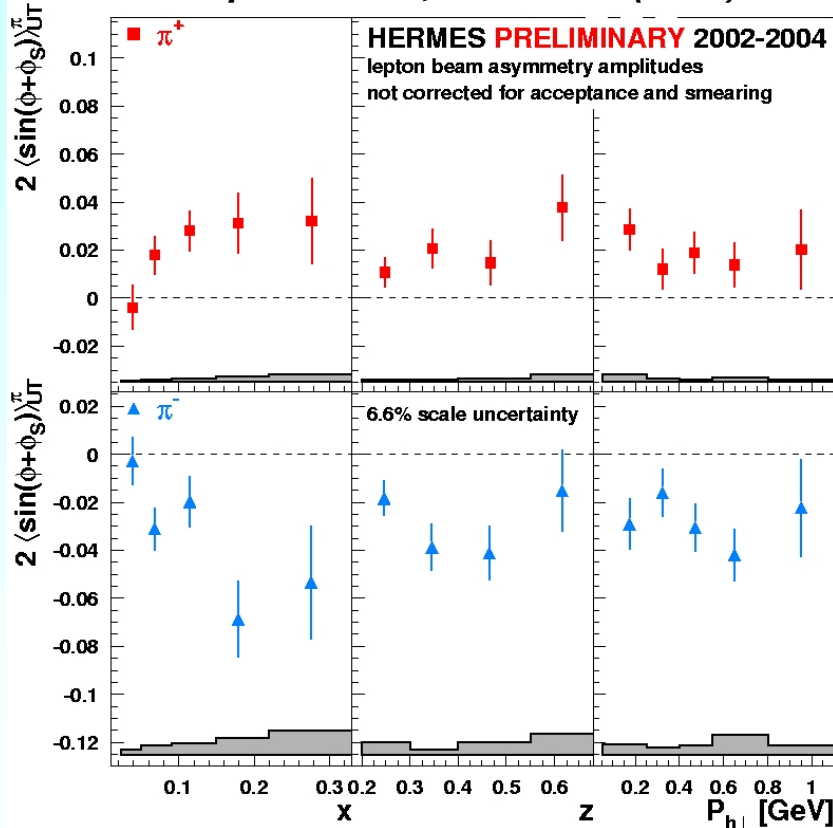




# Collins amplitudes for $\pi^{+/-}$ and $K^{+/-}$

$$A_{UT}^{\sin(\phi+\phi_S)} \sim \delta q(x) \cdot H_1^{\perp(1/2)}(z)$$

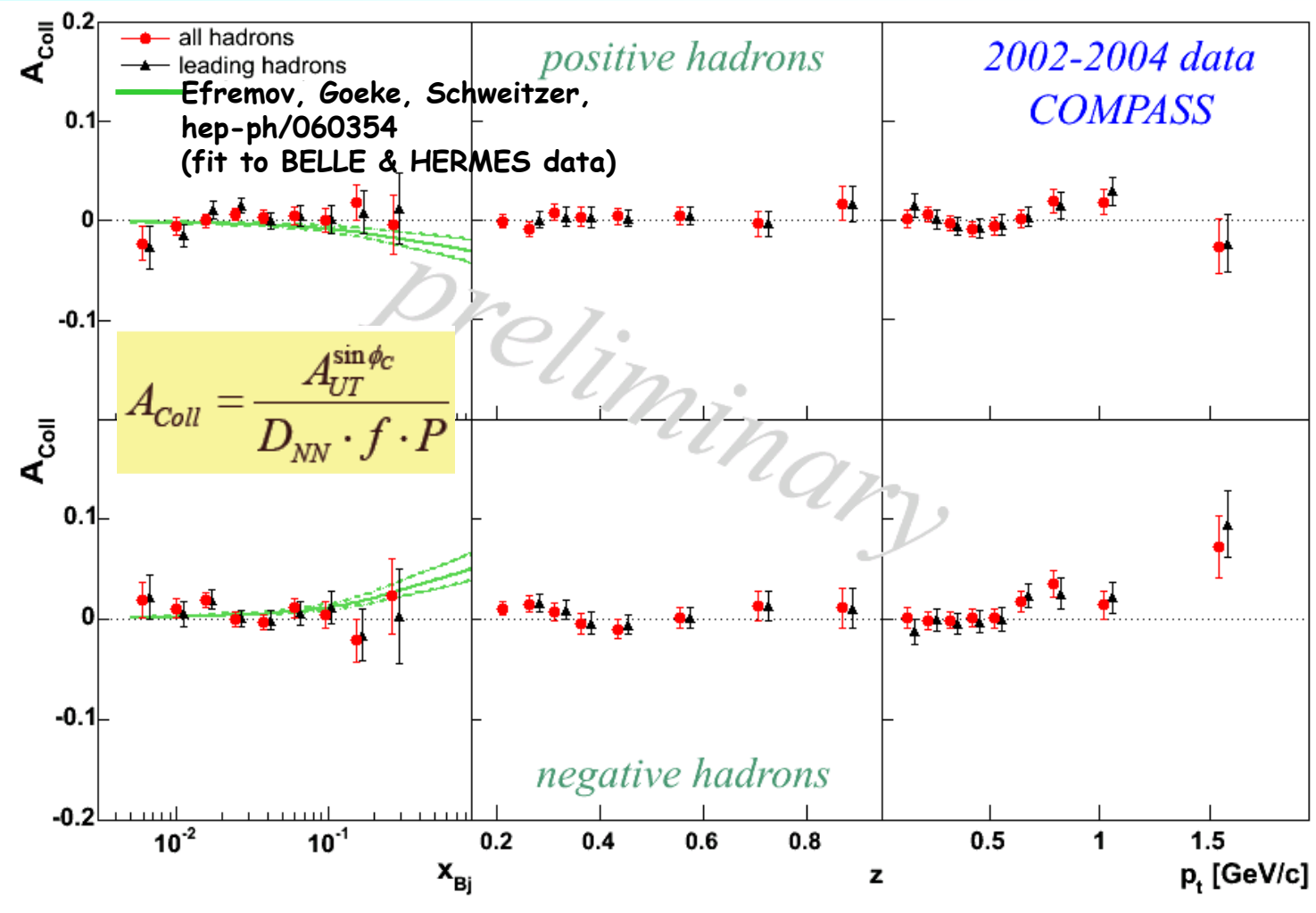
also: A. Airapetian et al, P. R. L. 94 (2005) 012002





# Collins Asymmetries - D target

Note: different convention :  $\phi_{Coll} = \phi + \phi_S - \pi$  also: V. Yu. Alexakhin et al, PRL 94 (2005) 202002

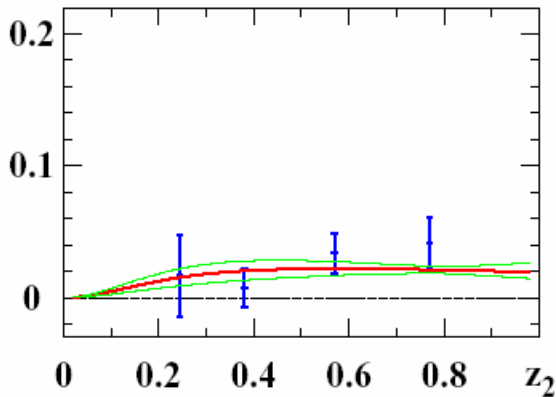


Consistent with zero. Cancellation due to **deuteron** target?

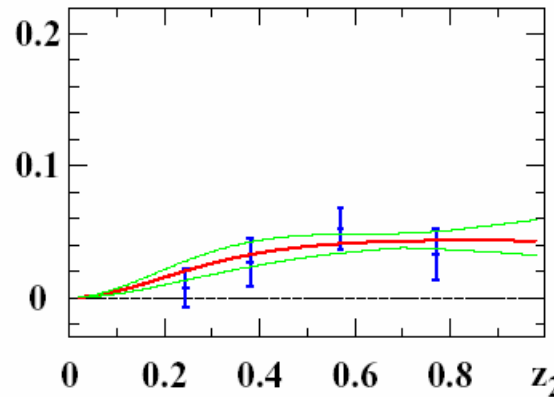
# LO-QCD Analysis of HERMES and BELLE Results

(Efremov, Goeke, Schweitzer, hep-ph/0603054)

$P(z_1, z_2)$  for  $0.2 < z_1 < 0.3$  (a)

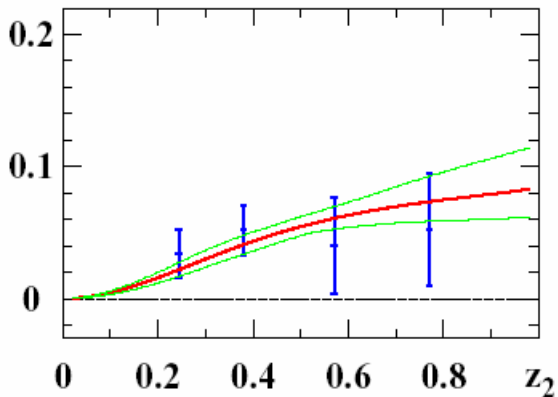


$P(z_1, z_2)$  for  $0.3 < z_1 < 0.5$  (b)

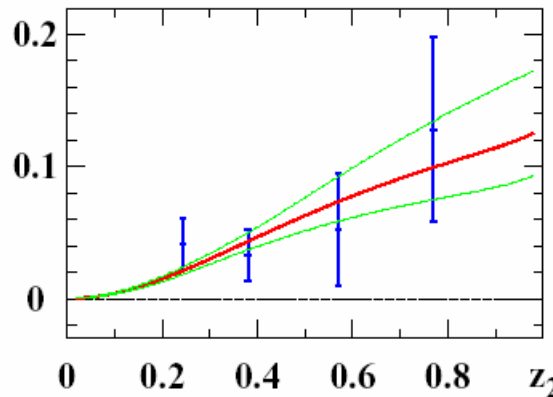


## BELLE PRELIMINARY

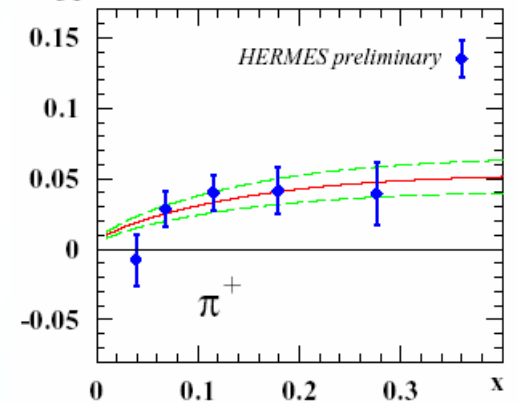
$P(z_1, z_2)$  for  $0.5 < z_1 < 0.7$  (c)



$P(z_1, z_2)$  for  $0.7 < z_1 < 1$  (d)

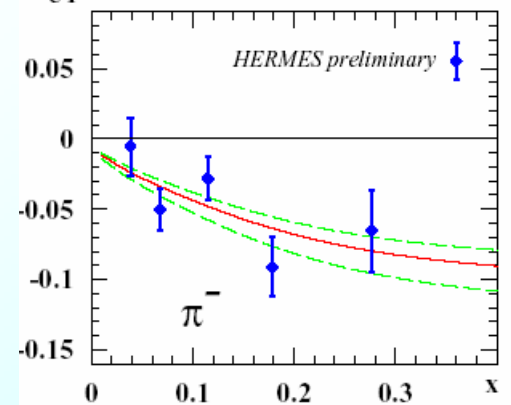


$A_{UT}^{\sin(\phi+\phi_S)}(x)$  for proton (a)



## HERMES PRELIMINARY

$A_{UT}^{\sin(\phi+\phi_S)}(x)$  for proton (b)

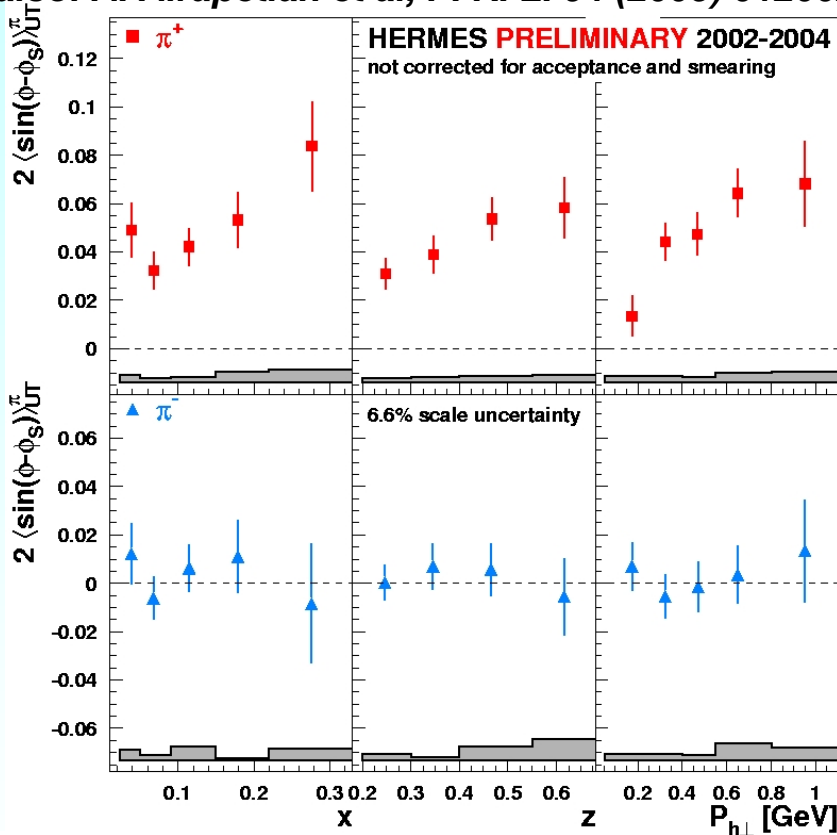


Combined fit to **Hermes** asymmetries (Transversity x Collins-FF) and **Belle** asymmetries (Collins-FF<sup>2</sup>) → Excellent agreement!

# Sivers amplitudes for $\pi^{+/-}$ (2002-2004)

$$A_{UT}^{\sin(\phi-\phi_S)} \sim f_{1T}^{\perp(1/2)}(x) \cdot D_1(z)$$

also: A. Airapetian et al, P. R. L. 94 (2005) 012002



$\pi^+$  asymmetry significantly different from zero and positive

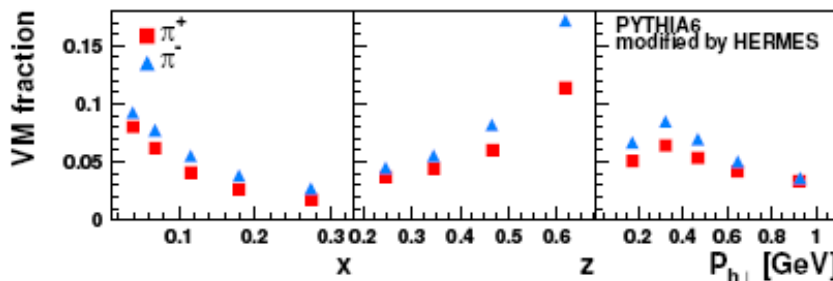
→ First hint of naive T-odd DF from DIS

→ orbital angular momentum  $L_z^q$

But: Contribution of  $L_z^q$  to nucleon spin unclear

$\pi^-$  asymmetry consistent with zero

Substantial contribution to pion sample from exclusively produced vector mesons (PYTHIA)



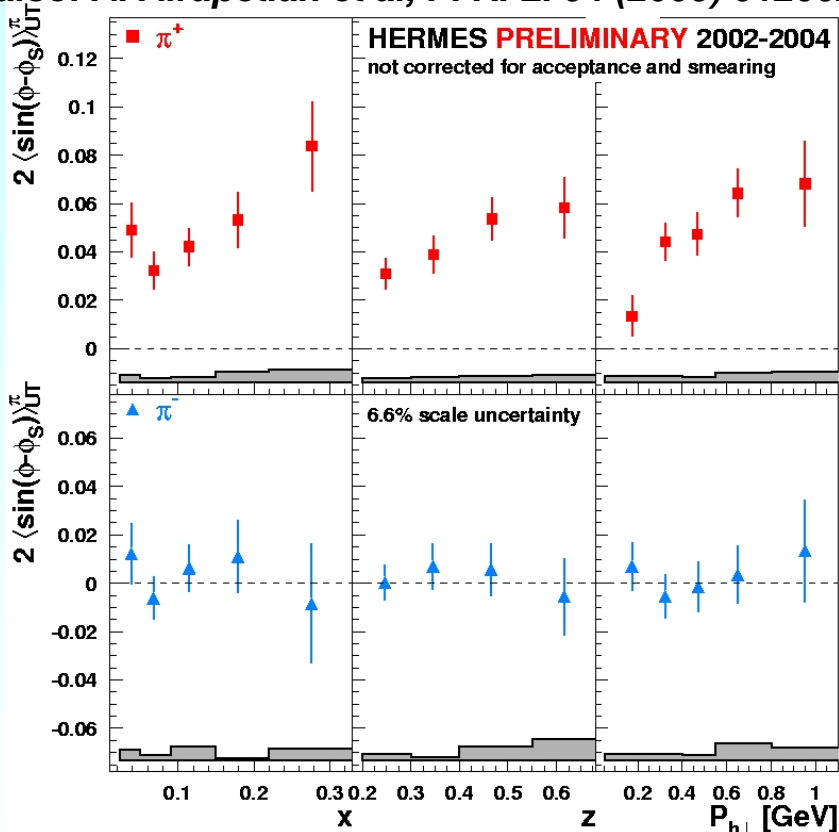




# Sivers amplitudes for $\pi^{+/-}$ and $K^{+/-}$

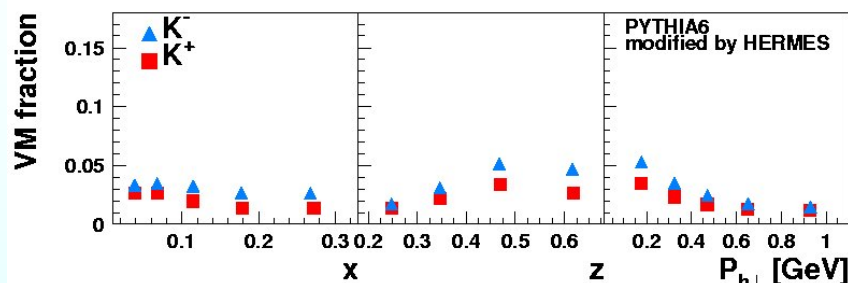
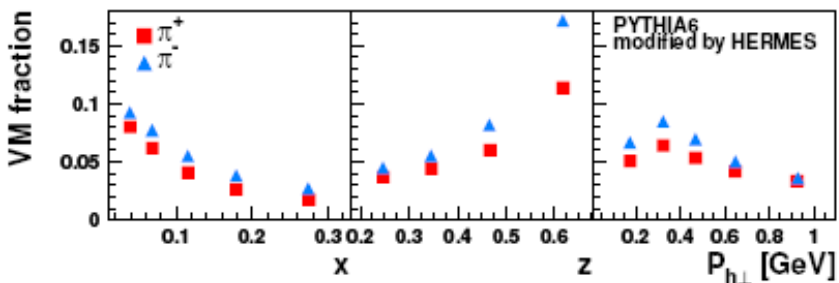
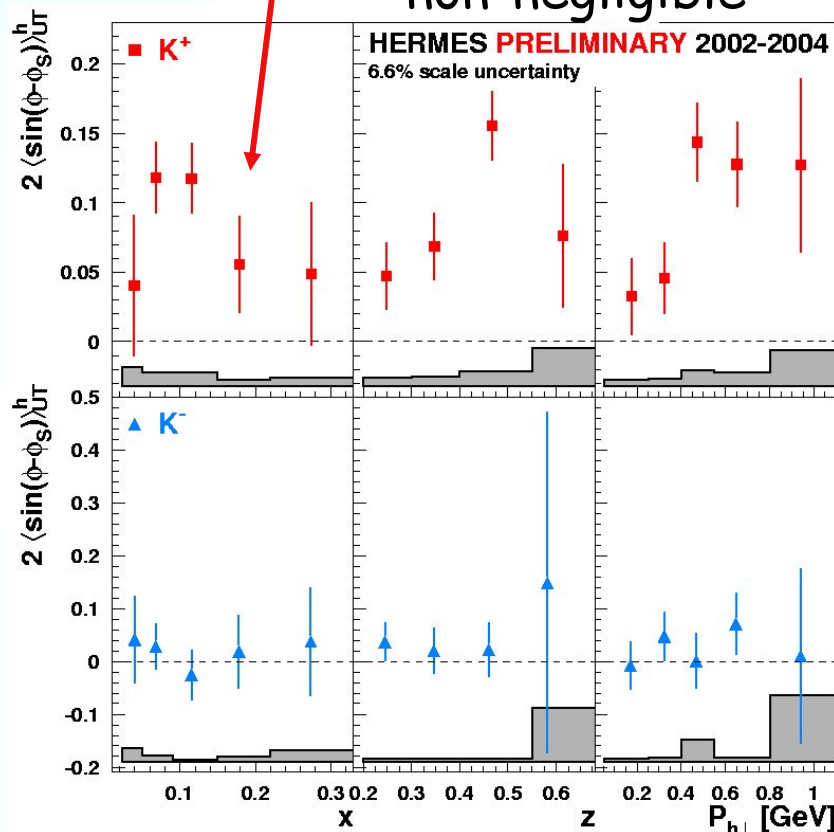
$$A_{UT}^{\sin(\phi-\phi_S)} \sim f_{1T}^{\perp(1/2)}(x) \cdot D_1(z)$$

also: A. Airapetian et al, P. R. L. 94 (2005) 012002



large!

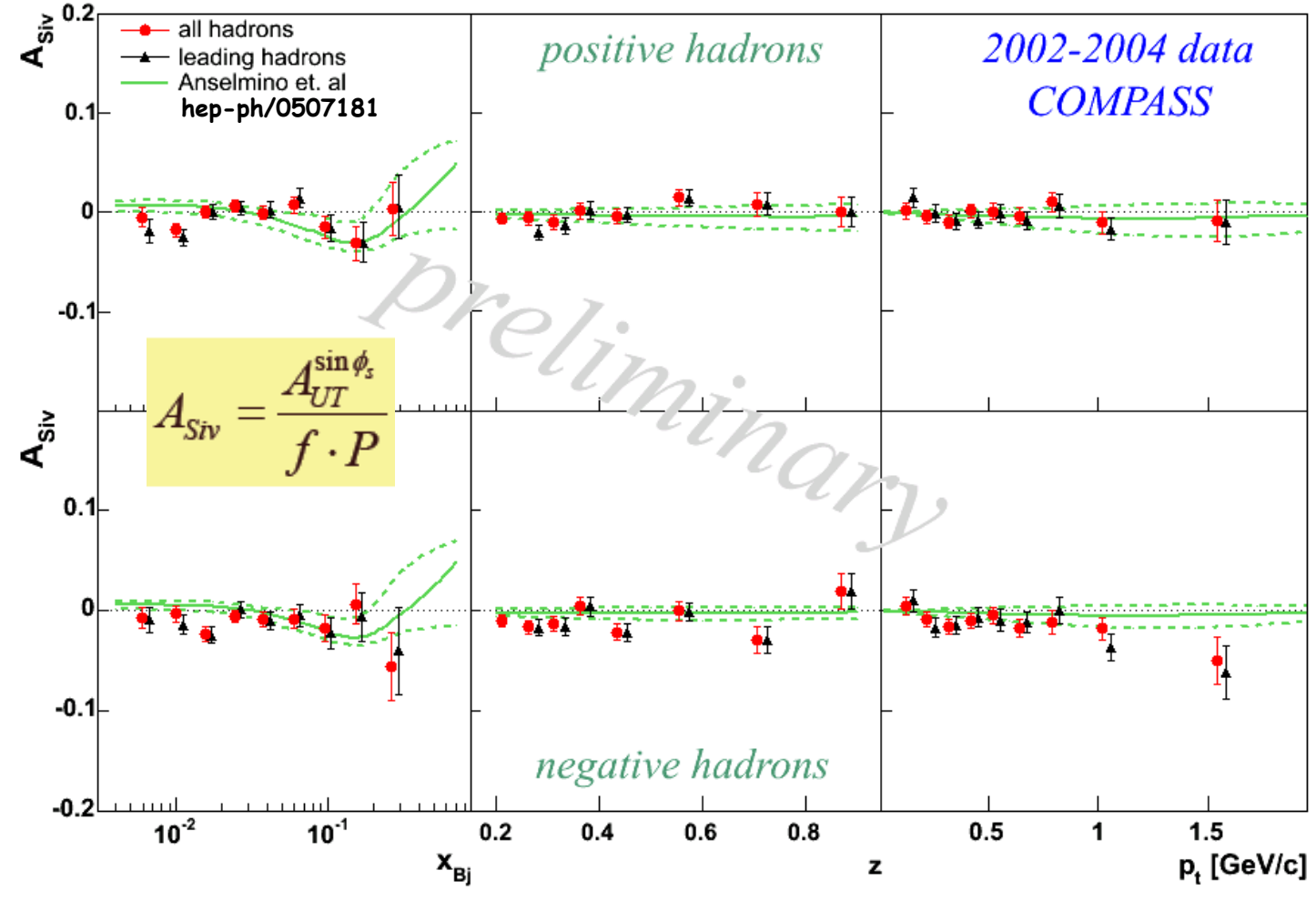
Sea contribution non-negligible





# Sivers Asymmetry - D target

also: V. Yu. Alexakhin et al, P R L 94 (2005) 202002



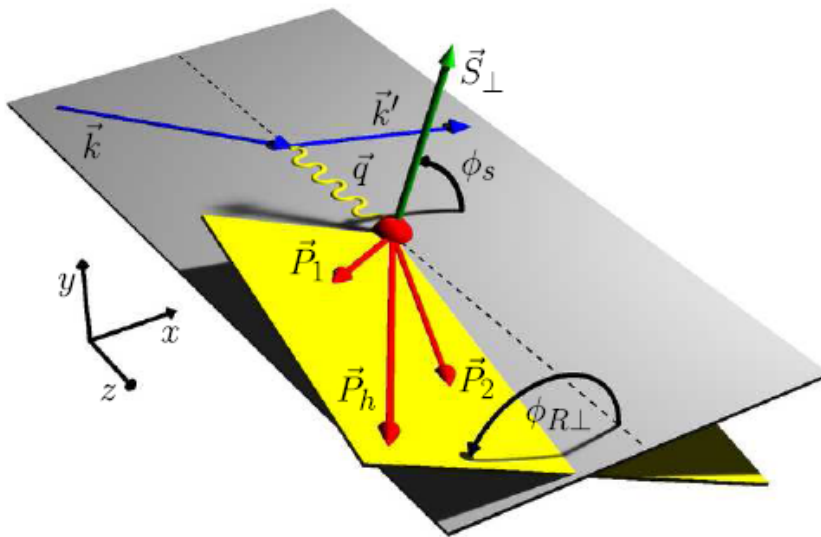
Consistent with zero. Cancellation due to deuteron target?

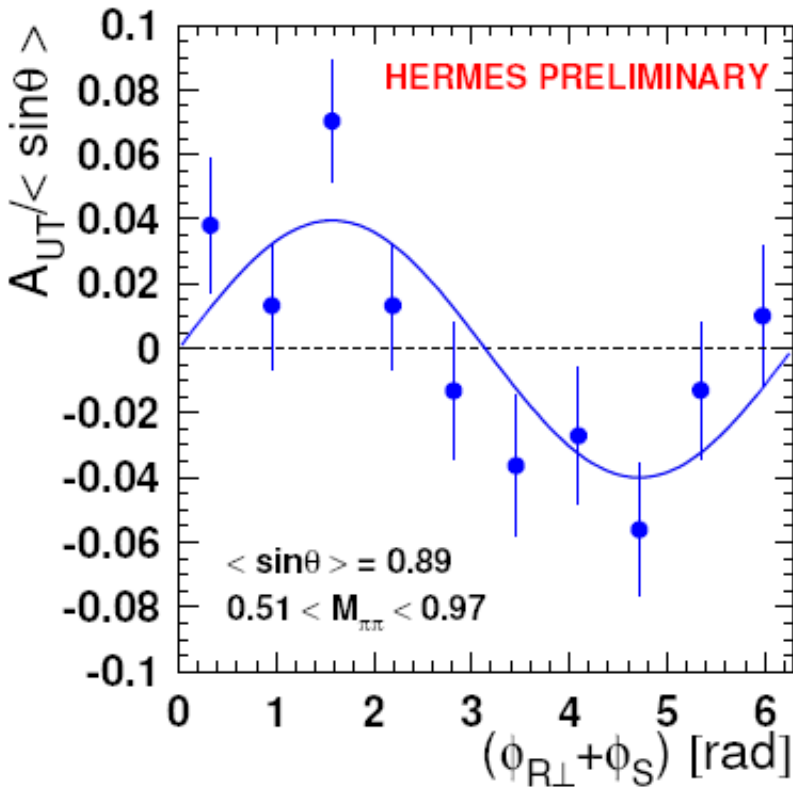
Detection of two final state pions with opposite charge:

$$A_{\text{UT}}(\phi_{R\perp}, \phi_S) \sim \dots \sin(\phi_{R\perp} + \phi_S) \frac{\sum_q e_q^2 \delta q(x) \cdot H_1^{\Delta q}(z, M_{\pi\pi}^2)}{\sum_q e_q^2 q(x) \cdot D_1^q(z, M_{\pi\pi}^2)} + \dots$$

$H_1^{\Delta q}(z, M_{\pi\pi}^2)$ ,  $D_1(z, M_{\pi\pi}^2)$ : two pion fragmentation functions

- no assumptions for  $\vec{p}_T$  and  $\vec{k}_T$  distributions necessary
- completely independent from single pion analysis

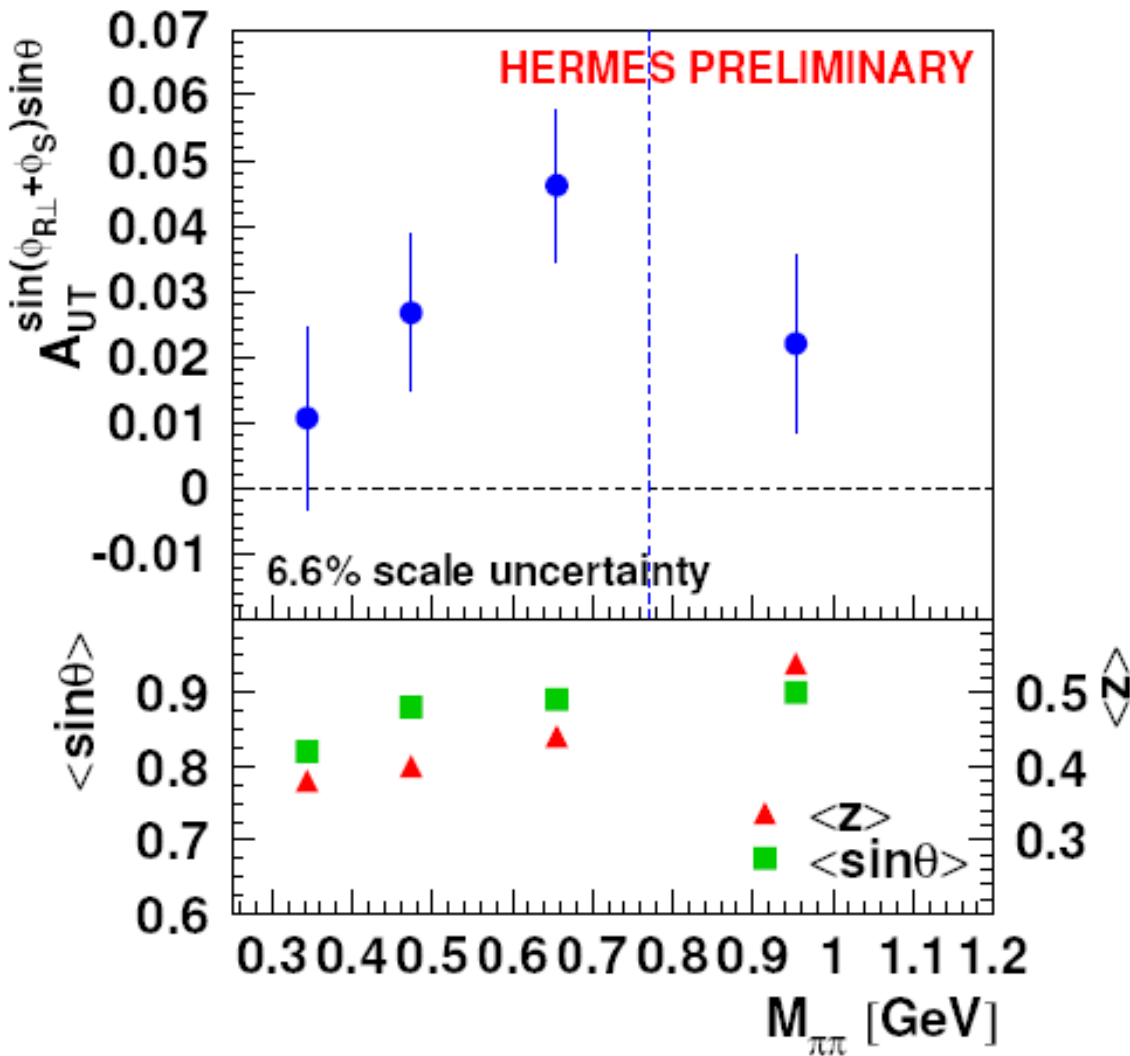




- hadrons assumed to be pions
- fit  $A_{UT}(\phi_{R\perp} + \phi_S) / \langle \sin \theta \rangle$  with  $p_1 + p_2 \sin(\phi_{R\perp} + \phi_S)$
- significant  $\sin(\phi_{R\perp} + \phi_S)$  behaviour!
- extract  $A_{UT}^{\sin(\phi_{R\perp} + \phi_S) \sin \theta}$  from  $A_{UT}(\phi_{R\perp}, \phi_S, \theta)$  by three dimensional fit

$$A_{UT}^{\sin(\phi_{R\perp} + \phi_S) \sin \theta} = 0.040 \pm 0.009 \text{ (stat)} \pm 0.003 \text{ (syst)}$$

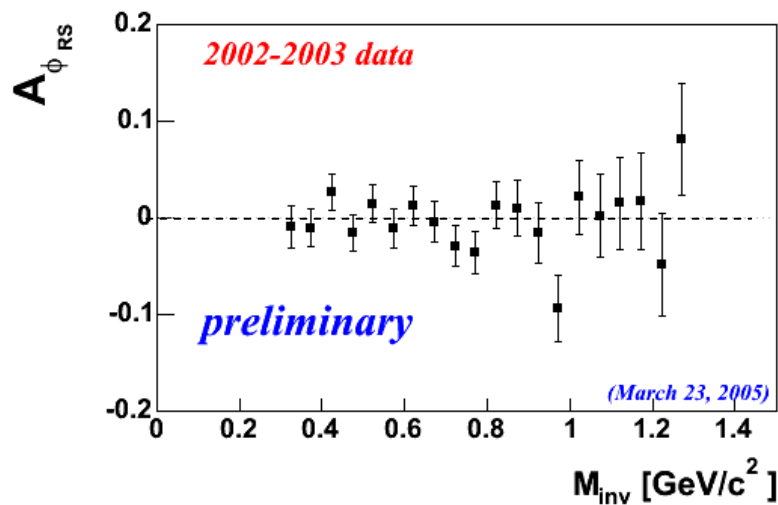
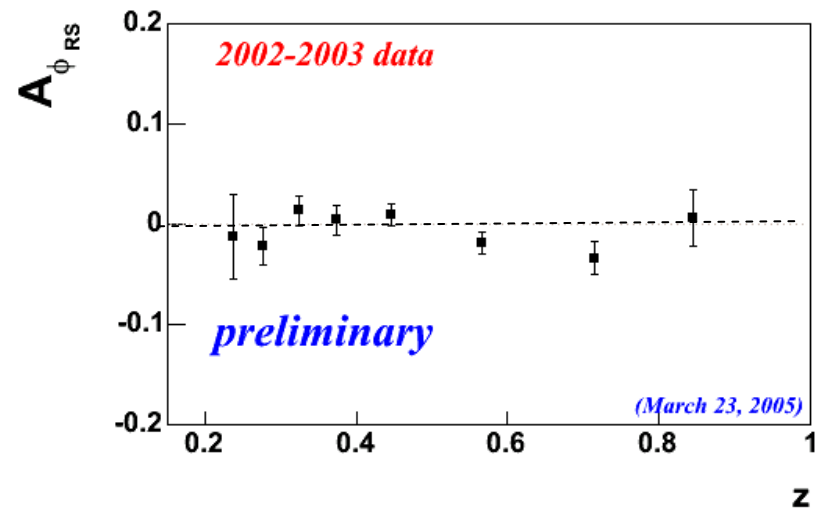
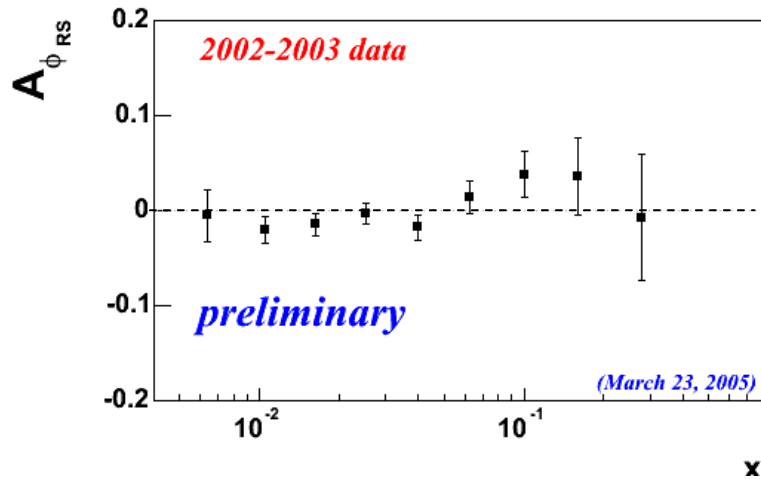
# Two-pion Asymmetries - H target



- positive asymmetry amplitudes in all bins
- no sign change at  $m_{\rho^0}$ !
- significant result for  $A_{UT}^{\sin(\phi_{R\perp} + \phi_S) \sin \theta}$   
→ non-zero IFF!



# Two-hadron Asymmetries - D target

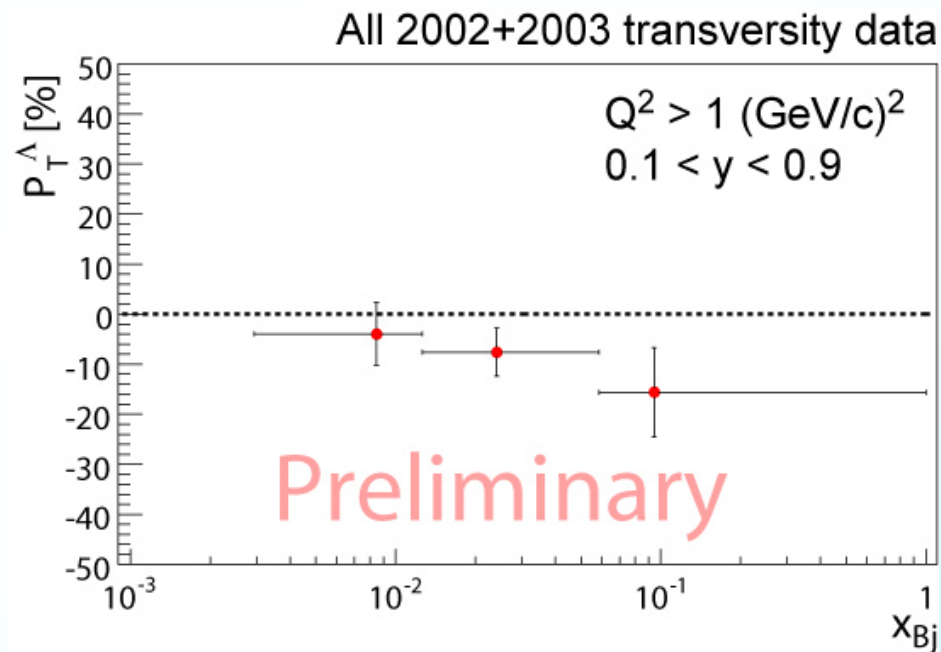
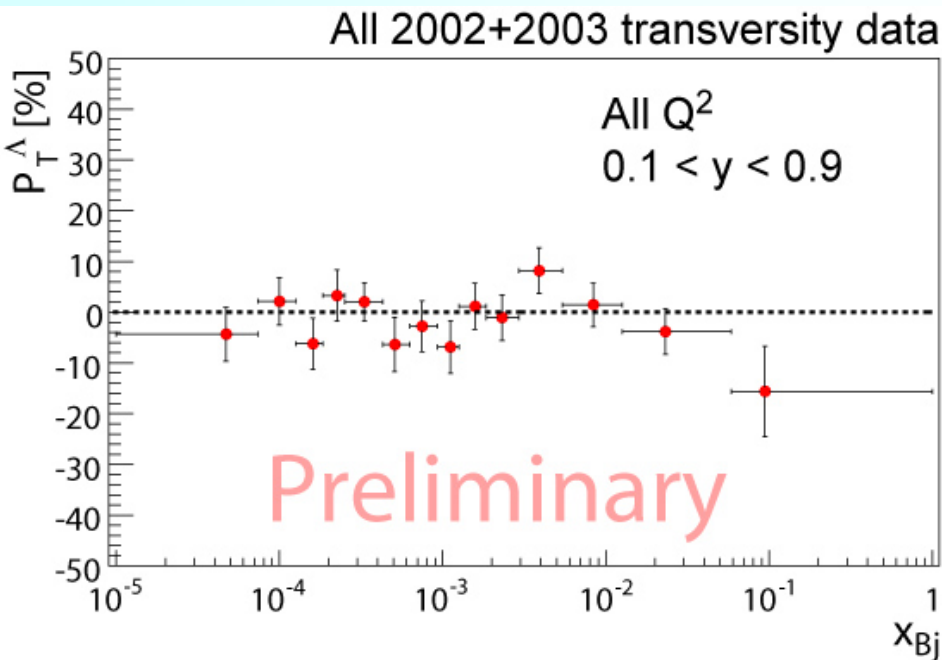


- Asymmetries compatible with zero
- Results from 2004 data analysis about to be released. Event sample has doubled



# Transversity from transverse $\Lambda$ polarisation

$$P_T^\Lambda = f P_T D \frac{\sum_q e_q^2 \times \Delta_T q \times \Delta D_q^\Lambda}{\sum_q e_q^2 \times q \times D_q^\Lambda}$$

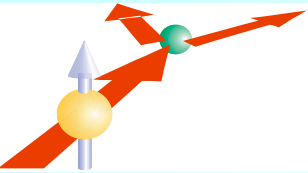


Negative trend for  $Q^2 > 1 \text{ GeV}^2$ , but deviation from zero not significant

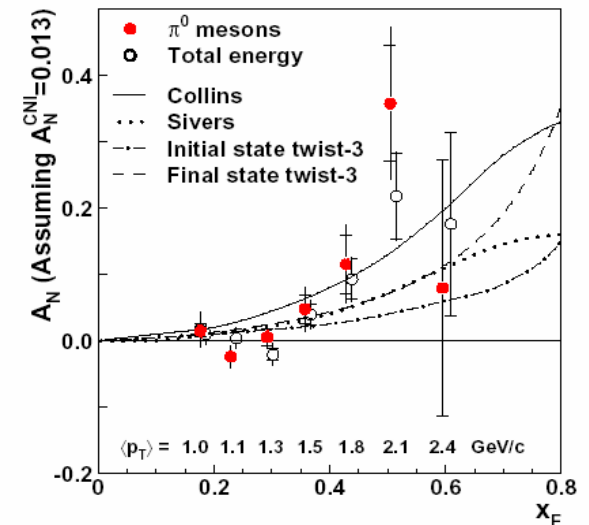
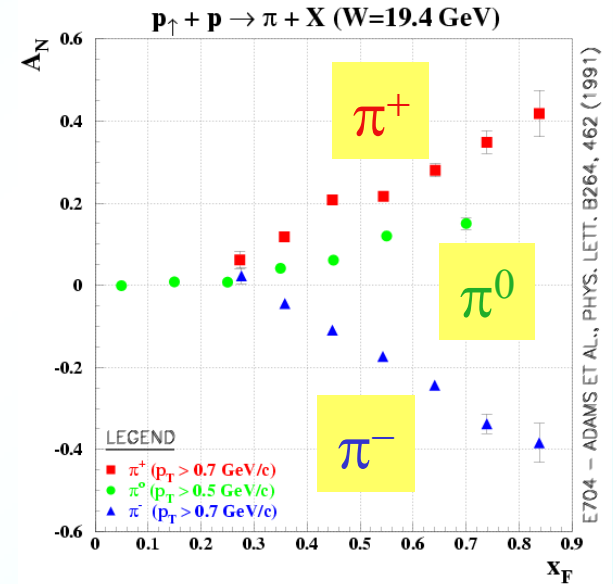
Statistics will double with 2004 data

But: HERMES data for quasi-real photoproduction from unpolarized and longt. polarized target:  $p_T^\Lambda \sim +5\%$

# Single transverse Spin Asymmetry $A_N$ in pp

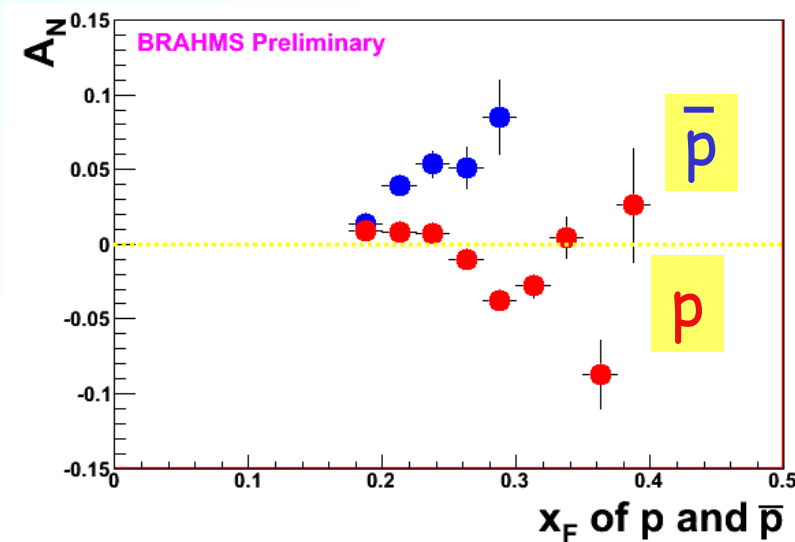
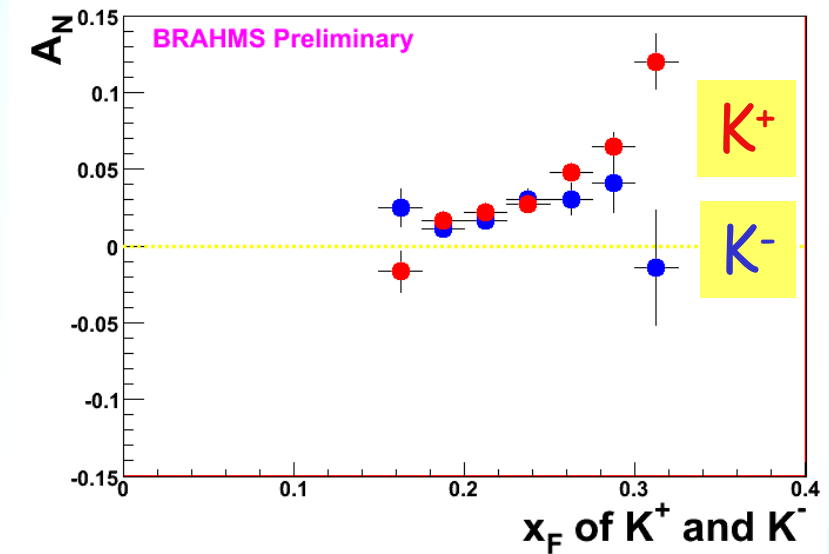
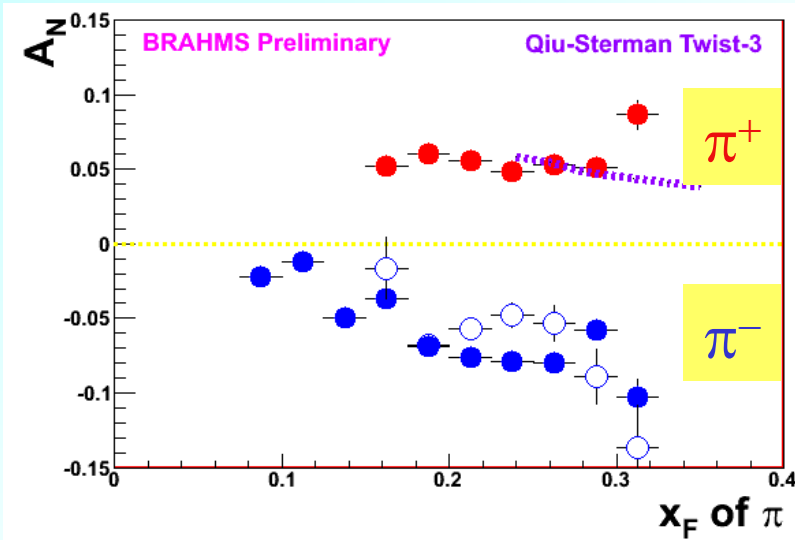


- Large  $A_N$  has been observed at forward rapidities in hadronic reactions: E704 and STAR
- Possible origins:
  - Collins FF
  - Sivers DF
  - Twist-3
  - Combinations of above
- Possible connection to **orbital angular momentum  $L$**  ?
- For consistent partonic description: Need flavor dependent  $A_N(E, x_F, p_T)$ ,





# $A_N$ for identified hadrons



- $A_N(\pi^+)$  positive  $\sim A_N(\pi^-)$  negative
- $A_N(K^+) \sim A_N(K^-)$  positive  
(in disagreement with expectation from valence quark fragmentation)
- $A_N(p) \sim 0$ ,  $A_N(\bar{p})$  positive
- More theoretical input needed

# Conclusions

- Plenty of new data from **COMPASS**, **HERMES**, **RHIC** improve our understanding of nucleon **spin structure**
- **Gluon** and **sea quark** polarisations small. Further improvements expected soon, especially from **RHIC**
- First results on **transverse spin physics** (**Transversity DF**, **Collins FF**, **Sivers DF**,  $A_N$ ) very promising

Stay tuned ...  
New exiting results will come soon!

Special thanks to G. Bunce and A. Magnon