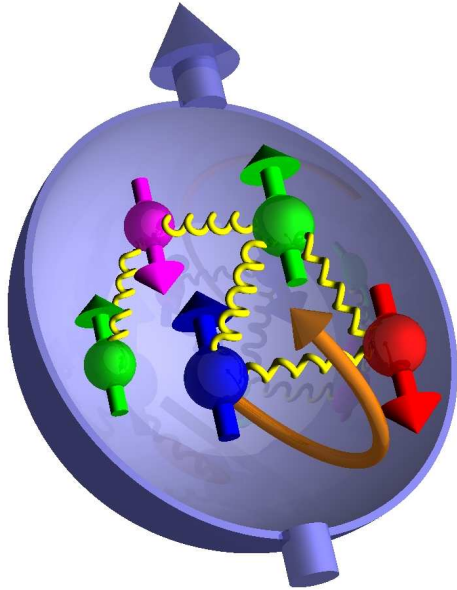


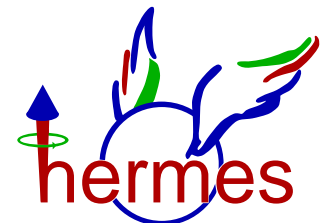
# New Results from HERMES



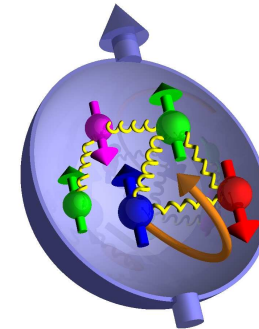
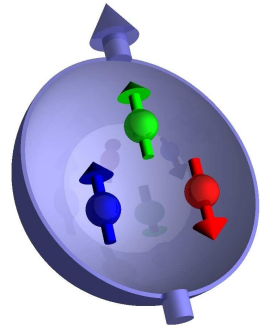
- ⇒ Inclusive Deep-Inelastic Scattering
- ⇒ NLO QCD analysis
- ⇒  $b_1(x)$  Measurement
- ⇒  $\Delta q$ -extraction
- ⇒ Double Spin Asymmetries in VM Production
- ⇒  $Q^2$ -Dependence of  $\rho^0$  Nuclear Transparency
- ⇒ Quark Fragmentation in Nuclei

**Michael Tytgat**  
**University of Gent**

on behalf of the HERMES Collaboration



# Spin Structure of the Nucleon



Naive Parton Model :

only **valence quarks** ( $\Delta u_v + \Delta d_v = 1$ )

EMC 1988 :  $\Delta\Sigma = 0.123 \pm 0.013 \pm 0.019$

☞ Include also **gluons**,  
**sea quarks**

& **orbital angular momentum**

$$S_z = \frac{1}{2}\hbar = \frac{1}{2} \left( \underbrace{\Delta u + \Delta \bar{u} + \Delta d + \Delta \bar{d} + \Delta s + \Delta \bar{s}}_{\Delta\Sigma} \right) + \Delta g + L_z^q + L_z^g$$

$$\Delta q = \int_0^1 dx \cdot \Delta q(x) : \text{first moments of helicity densities}$$

$\Delta\Sigma$  ☞ inclusive scattering

$\Delta q$  ☞ semi-inclusive scattering

$\Delta g$  ☞ NLO QCD analysis,  
high- $p_t$  hadrons

$L_{q,g}$  ☞ GPD's ?

# Polarized Deep Inelastic Scattering

$$\frac{d^2\sigma}{d\Omega dE^2} = \frac{\alpha^2 E'}{Q^2 E} L_{\mu\nu}(k, q, s) W^{\mu\nu}(P, q, S)$$

$L_{\mu\nu}$  : exactly calculable in QED

$$W^{\mu\nu} = -g^{\mu\nu} F_1(x, Q^2) + \frac{p^\mu p^\nu}{\nu} F_2(x, Q^2) \\ + i\epsilon^{\mu\nu\lambda\sigma} \frac{q_\lambda}{\nu} (S_\sigma g_1(x, Q^2) + \frac{1}{\nu} (p \cdot q S_\sigma - S \cdot q p_\sigma) g_2(x, Q^2))$$

Quark Parton Model :

$F_1, F_2$  : unpolarized structure functions  $\Rightarrow$  momentum distribution of quarks

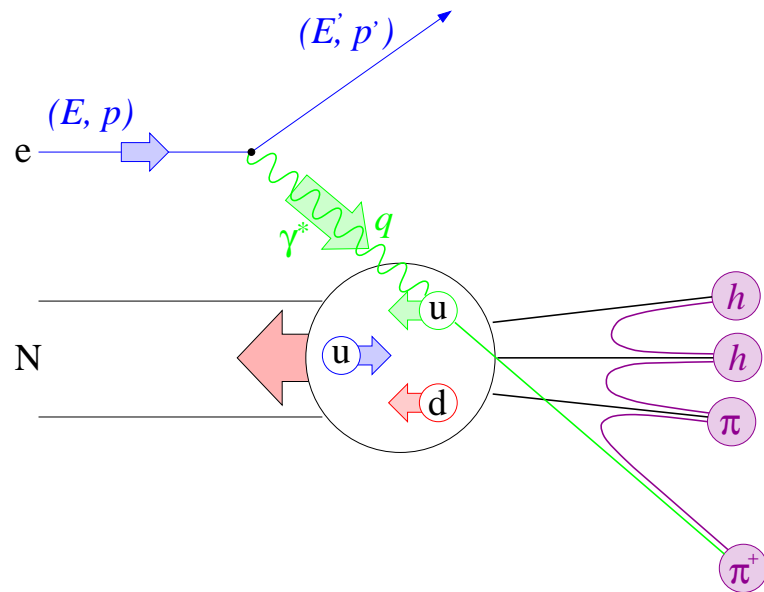
$$F_1(x) = \frac{1}{2} \sum_q e_q^2 [q^+(x) + q^-(x)] = \frac{1}{2} \sum_q e_q^2 q(x)$$

$$F_2(x) = 2x F_1(x)$$

$g_1, g_2$  : polarized structure functions  $\Rightarrow$  spin distribution of quarks

$$g_1(x) = \frac{1}{2} \sum_q e_q^2 [q^+(x) - q^-(x)] = \frac{1}{2} \sum_q e_q^2 \Delta q(x)$$

# Polarized Deep Inelastic Scattering



Measure **double spin asymmetries** :

$$A_{\parallel} = \frac{\sigma^{\uparrow\downarrow} - \sigma^{\uparrow\uparrow}}{\sigma^{\uparrow\downarrow} + \sigma^{\uparrow\uparrow}} = D (A_1 + \eta A_2)$$

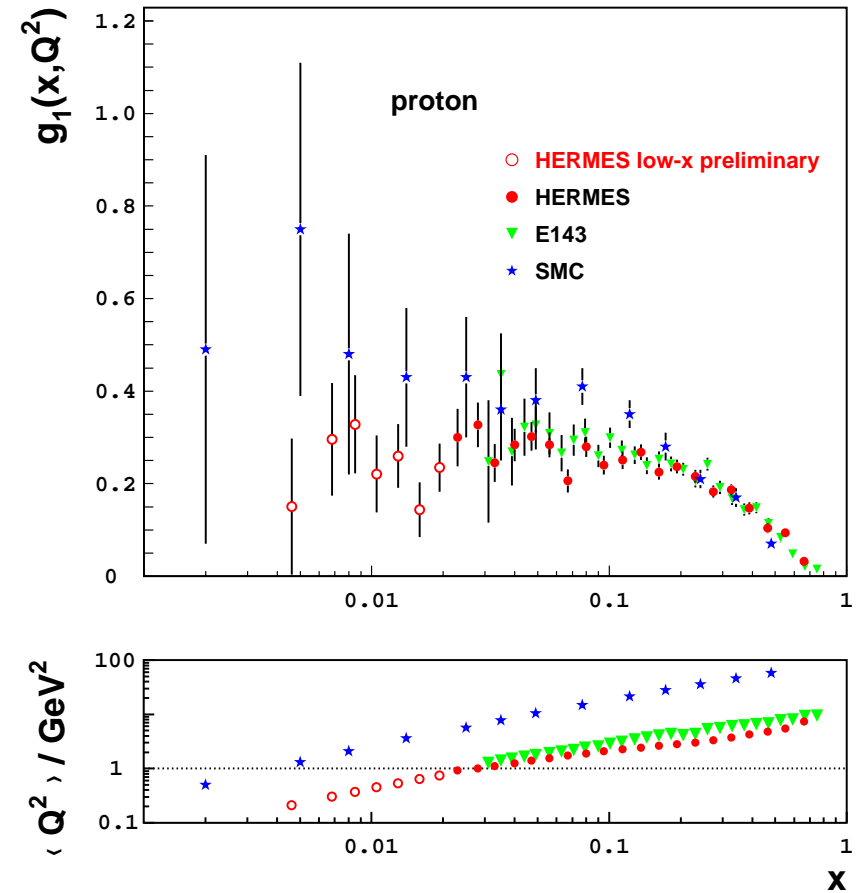
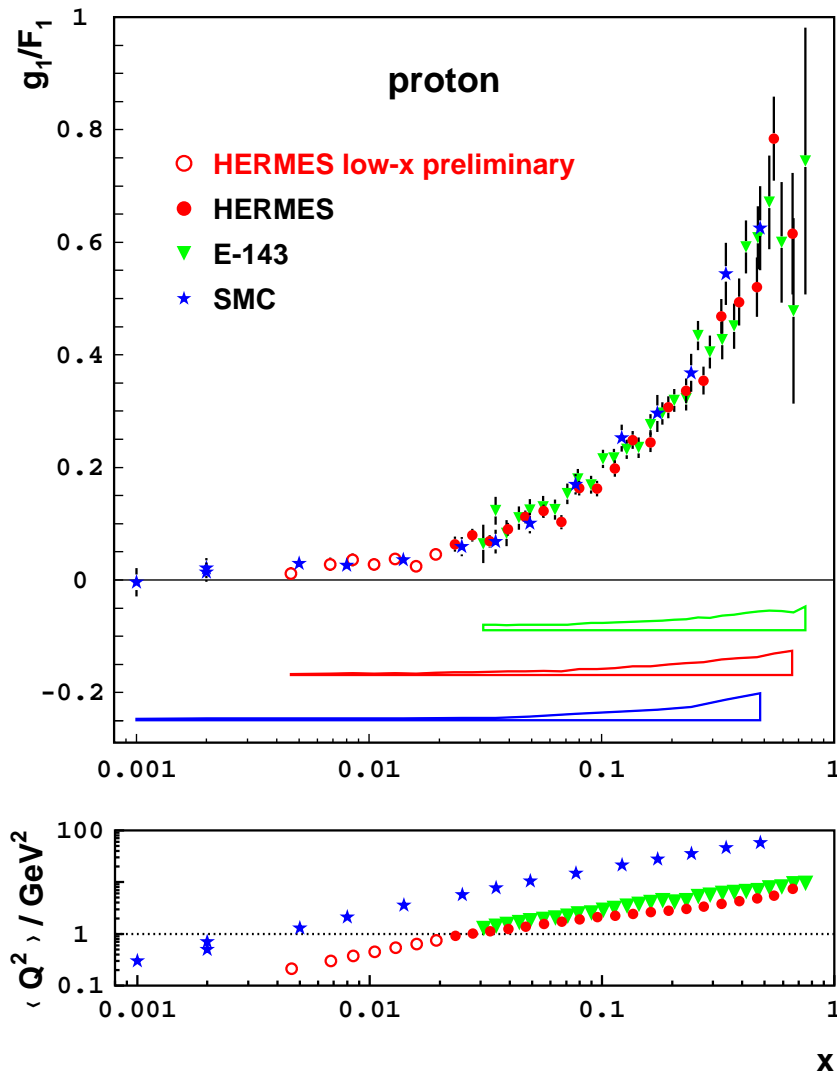
$$A_1 = \frac{\sigma^{1/2} - \sigma^{3/2}}{\sigma^{1/2} + \sigma^{3/2}} = \frac{g_1(x) - \gamma^2 g_2(x)}{F_1(x)},$$

$$A_2 = \frac{\sigma_{TL}}{\sigma_T} = \frac{\gamma(g_1(x) + g_2(x))}{F_1(x)}$$

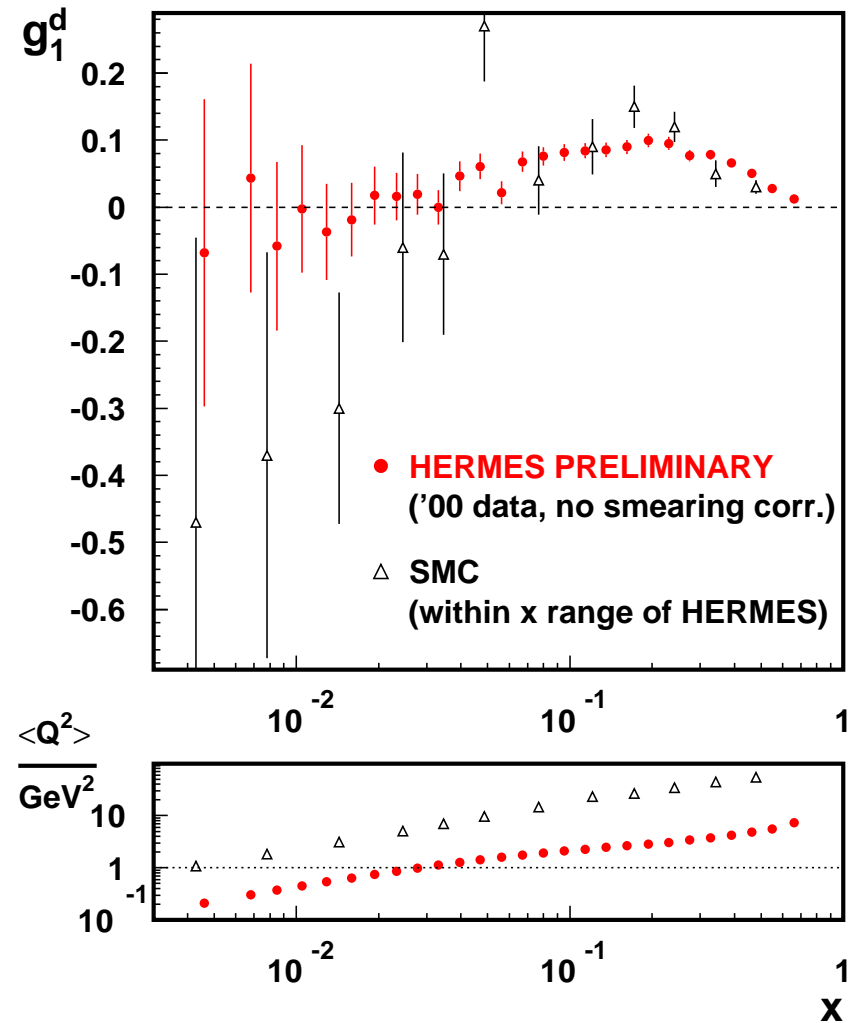
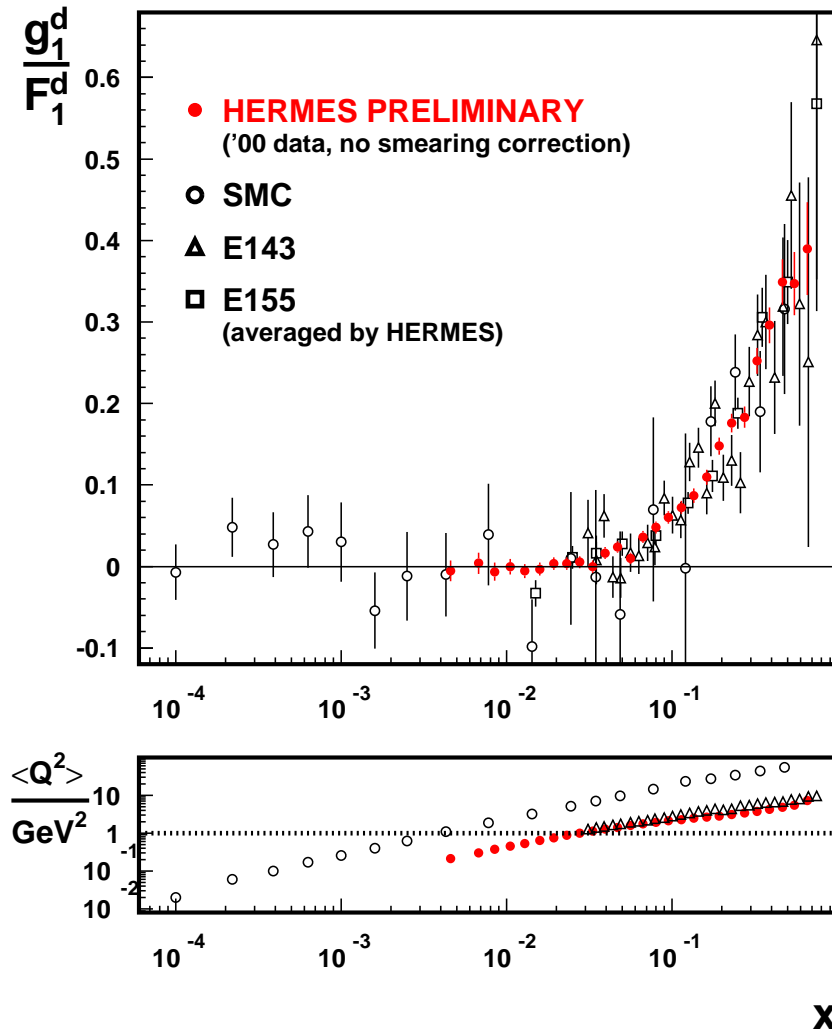
$$g_1(x) = \frac{F_1(x)}{1 + \gamma^2} \left[ \frac{A_{\parallel}(x)}{D} + (\gamma - \eta) A_2 \right]$$

$$\left\{ \begin{array}{l} F_1 = \frac{(1 + \gamma^2)}{2x(1 + R)} F_2 \\ \text{Use } A_2^n = 0 \text{ or fit to } A_2^p \text{ data or } A_2^d = A_2^{WW} \end{array} \right.$$

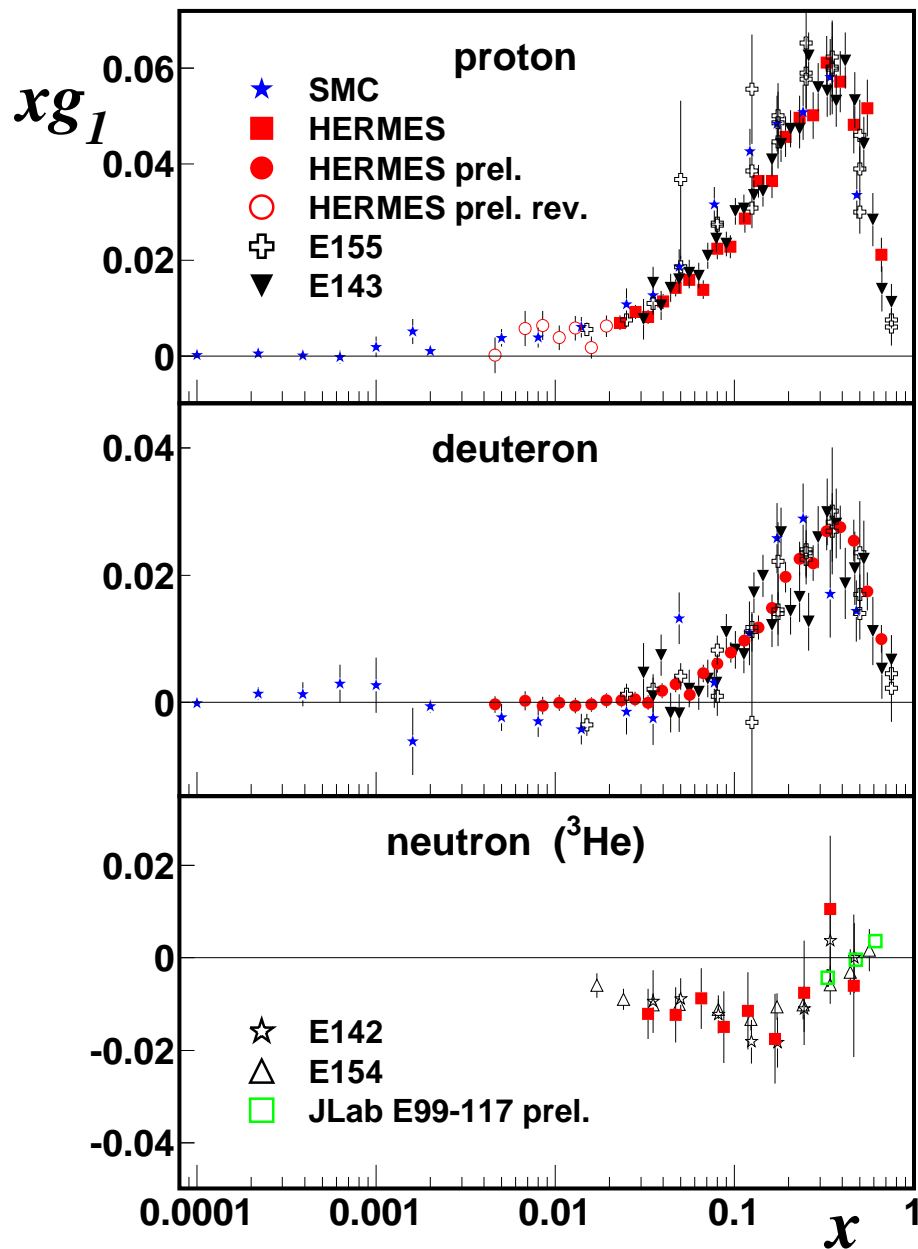
# $g_1^p(x)$ from Hydrogen



# $g_1^d(x)$ from Deuterium



# World Data on $xg_1(x)$



$$g_1^p > g_1^d > g_1^n$$

Neglecting sea quark contributions :

$$p : 2 \cdot \frac{4}{9} \Delta u_p + \frac{1}{9} \Delta d_p$$

$$d : p + n$$

$$n : 2 \cdot \frac{1}{9} \Delta d_n + \frac{4}{9} \Delta u_n$$

$$\text{or } 2 \cdot \frac{1}{9} \Delta u_p + \frac{4}{9} \Delta d_p$$

$$\Delta u_p > 0$$

$$\Delta d_p < 0$$

# NLO QCD Fit

---

- 0th order :  $g_1^0(x) = \frac{1}{2} \sum_q e_q^2 \Delta q(x)$ , no  $Q^2$  dependence
- LO : gluon radiation, photon-gluon fusion

☞ Redefinition of quark distributions including  $\Delta g$

$$g_1^{LO}(x, Q^2) = \frac{1}{2} \sum_q e_q^2 \Delta q(x, Q^2)$$

- NLO :

$$g_1^{NLO}(x, Q^2) = \frac{1}{2} \sum_q e_q^2 [\Delta q + \Delta q(x, Q^2) \otimes C_q + \Delta g(x, Q^2) \otimes C_g]$$

2 independent NS distributions +  $\Delta\Sigma$  +  $\Delta g$  :

$$\Delta q_{NS}^p = \frac{1}{2}(2\Delta u - \Delta d - \Delta s), \quad \Delta q_{NS}^n = \frac{1}{2}(2\Delta d - \Delta u - \Delta s)$$

$$\Delta\Sigma = \Delta u + \Delta d + \Delta s$$



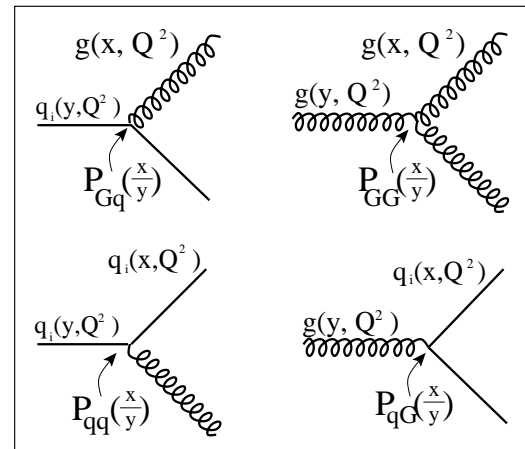
# NLO QCD Fit

$Q^2$  evolution :

$$\frac{d}{d \ln Q^2} \Delta q^{NS}(x, Q^2) = \frac{\alpha_s(Q^2)}{2\pi} P_{qq} \otimes \Delta q^{NS}$$

$$\frac{d}{d \ln Q^2} \begin{pmatrix} \Delta \Sigma(x, Q^2) \\ \Delta g(x, Q^2) \end{pmatrix} = \frac{\alpha_s(Q^2)}{2\pi} \begin{pmatrix} P_{qq} & 2 N_f P_{qg} \\ P_{gq} & P_{gg} \end{pmatrix} \otimes \begin{pmatrix} \Delta \Sigma \\ \Delta g \end{pmatrix}$$

Splitting Functions



Parametrization of parton distributions at input scale  $Q_0^2$  :

$$x \Delta q_i(x, Q_0^2) = \eta_i A_i x^{a_i} (1-x)^{b_i} (1 + \gamma_i x + \rho_i x^{1/2})$$

# NLO QCD Fit

## Choice of Parameters

$$x\Delta q_i(x, Q_0^2) = \eta_i A_i x^{a_i} (1-x)^{b_i} (1 + \gamma_i x + \rho_i x^{\frac{1}{2}})$$

☞ Use  $g_1/F_1$  or  $A_1$  data on  $p$ ,  $d$  and  $n$

from EMC, E142, HERMES, E154,

SMC, E143, E155

with  $Q^2 > 1.0 \text{ GeV}^2$  cut

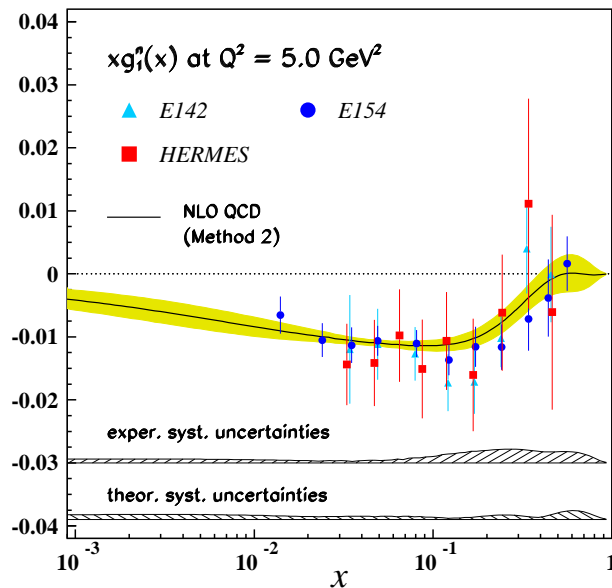
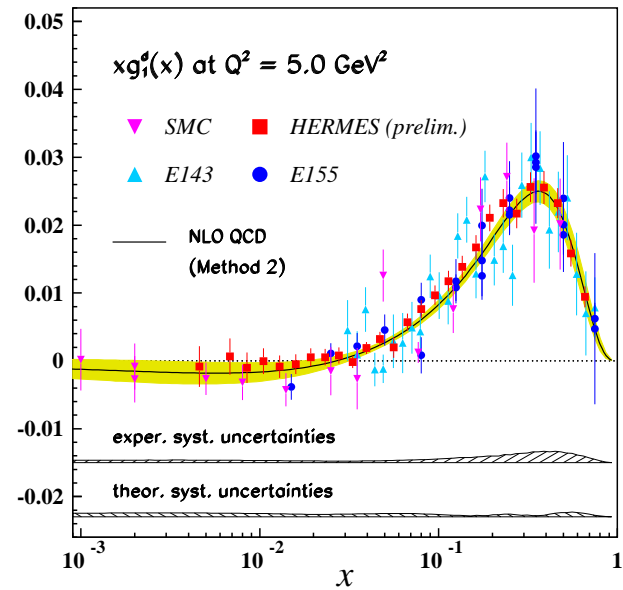
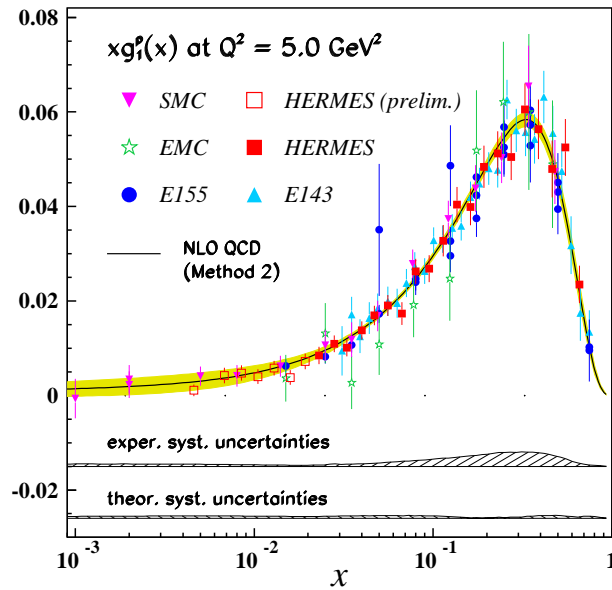
☞ 2 independent methods :

## Mellin Transform & Finite Differences

Method 1	Method 2
$\overline{MS}$	$\overline{MS}$
Mellin Transform	Finite differences
$\Delta u_v, \Delta d_v, \Delta \bar{q}_s, \Delta G$	$\Delta q_{NS}^p, \Delta q_{NS}^n, \Delta \Sigma, \Delta G$
symmetric sea: $\Delta \bar{q}_s = \Delta \bar{u}_s = \Delta \bar{d}_s = \Delta \bar{s} = \Delta \bar{s}$	no assumption (in the fit)
$\eta_{u_v}, \eta_{d_v}$ fixed by $F, D$ $\gamma_{u_v}, \gamma_{d_v} \neq 0$ fixed $a_G = a_{sea} + 1$ $\left. \begin{array}{l} \frac{b_{\bar{q}_s}}{b_G} \Big _{pol} = \frac{b_{\bar{q}_s}}{b_G} \Big _{unpol} \\ b_{\bar{q}_s} = 8.08, b_G = 5.61 \end{array} \right\} *$ $\gamma_{\bar{q}_s} = 0, \gamma_G = 0$ $\rho = 0$ for all densities → 7 fit parameters	$\eta_{q_p^{NS}}, \eta_{q_n^{NS}}$ fixed by $F, D$ $\gamma_{q_p^{NS}} = \gamma_{q_n^{NS}} \neq 0$ fixed $\left\{ \begin{array}{l} \text{no such} \\ \text{relations} \end{array} \right.$ $b_G = 5.61$ $\gamma_\Sigma \neq 0$ fixed, $\gamma_G = 0$ $\rho = 0$ for all densities → 7 fit parameters
$\Lambda_{QCD}^{(4)} = 291 \pm 30 \text{ MeV}$ $Q_0^2 = 4 \text{ GeV}^2$ data: $Q^2 > 1 \text{ GeV}^2$	$\alpha_s(M_Z^2) = 0.117 \pm 0.002$ $Q_0^2 = 4 \text{ GeV}^2$ data: $Q^2 > 1 \text{ GeV}^2$

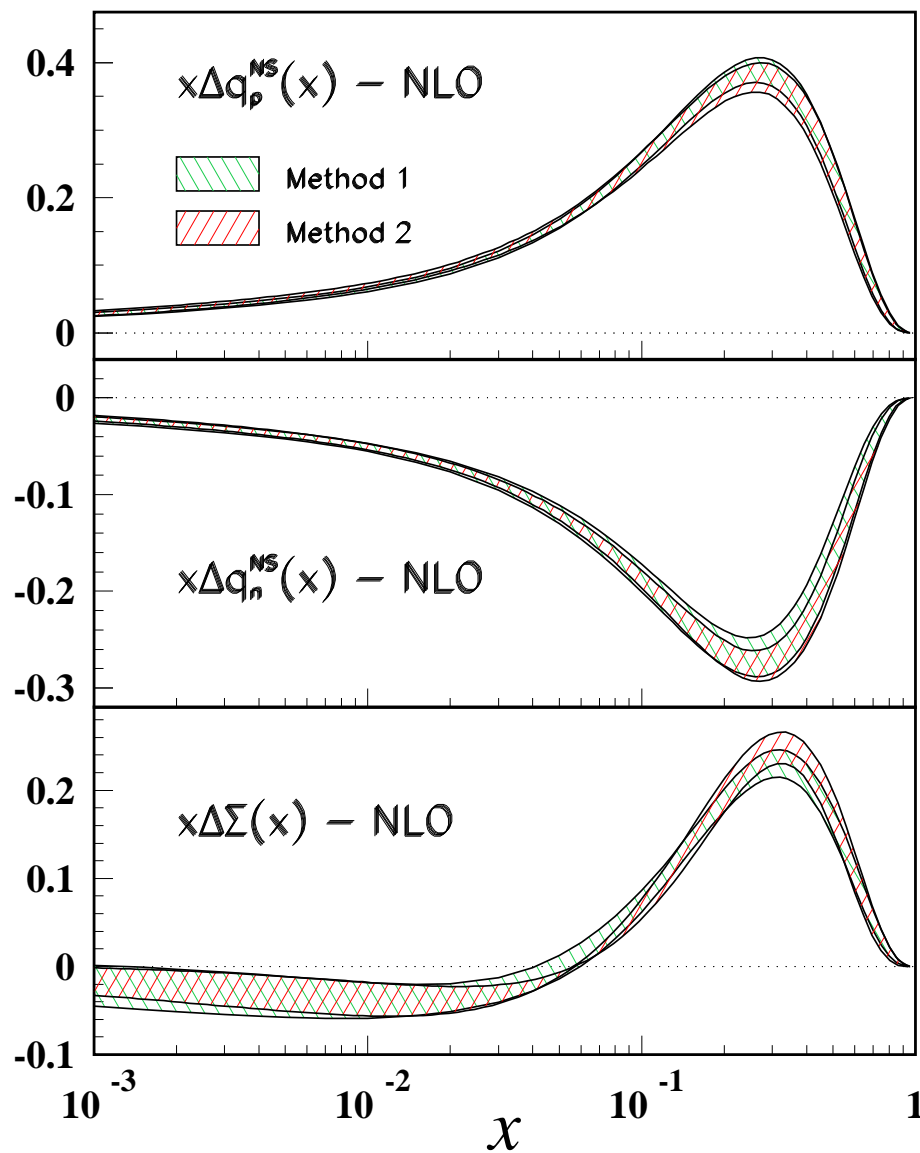
\* lead to positivity for  $\Delta \bar{q}_s$  and  $\Delta G$

# NLO QCD Fit



☞ Fits are performed on  $g_1(x, Q^2)$   
and give a good final description

# NLO QCD Fit



$Q_0^2 = 4.0 \text{ GeV}^2$

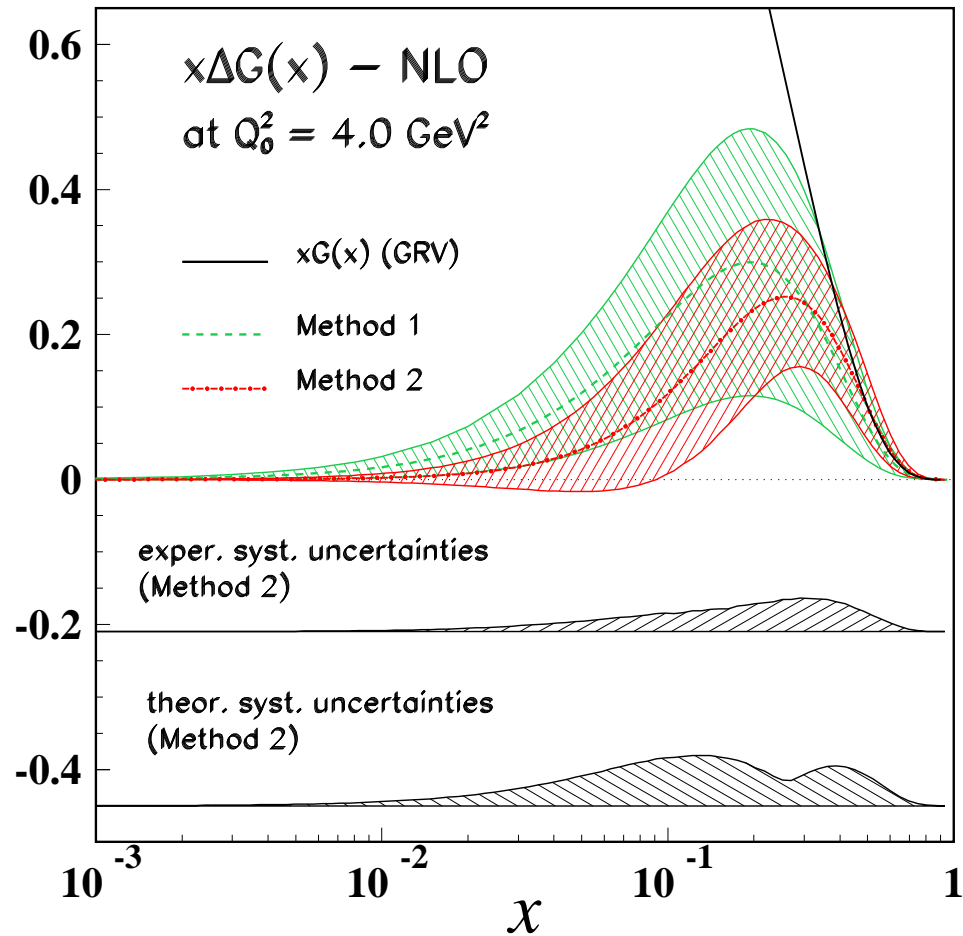
☞  $\Delta\Sigma = 0.201 \pm 0.103$

☞ valence quarks dominate

☞  $\Delta\bar{q}_s = -0.070 \pm 0.028$

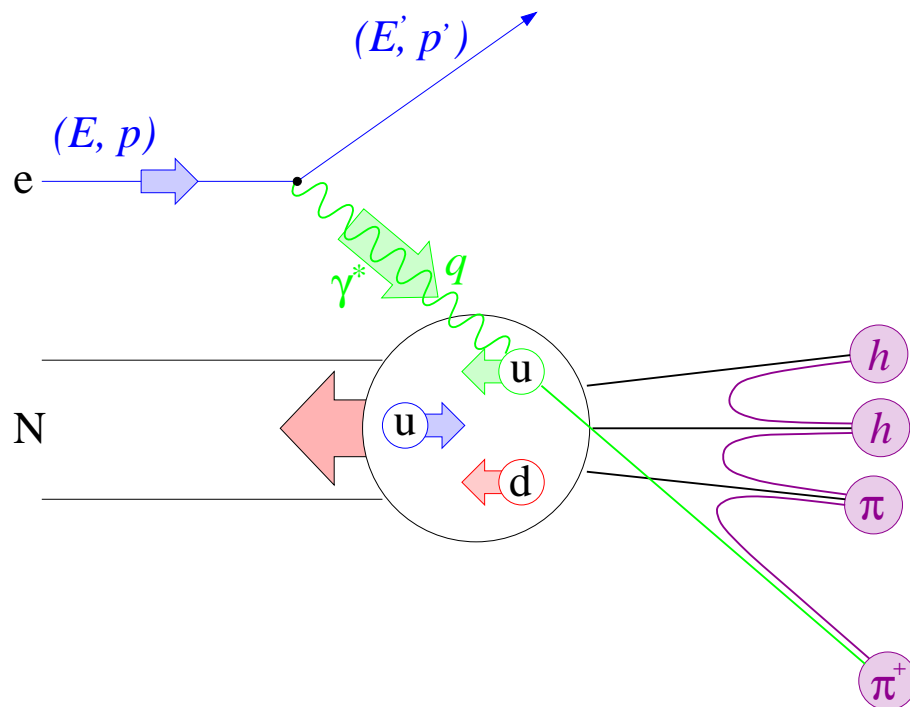
very small sea quark polarization

# NLO QCD Fit



☞  $\Delta G$  still largely unconstrained ...

# Semi-Inclusive Deep Inelastic Scattering



$$\vec{e} + \vec{N} \longrightarrow e + h + X$$

☞ Flavor tagging : correlation between fast hadron and struck quark flavor

Factorization of cross section :

$$\sigma^h(x, Q^2, z) \propto \sum_q e_q^2 q(x, Q^2) D_q^h(z, Q^2)$$

$D_q^h(z, Q^2)$  : fragmentation functions,  $h = \pi^{\pm,0}, K^{\pm} \dots$

## $\Delta q$ -Extraction

$$A_1^h(x, Q^2) = \frac{\sigma_h^{1/2} - \sigma_h^{3/2}}{\sigma_h^{1/2} + \sigma_h^{3/2}} \simeq C \cdot \sum_q \frac{e_q^2 q(x, Q^2) \int dz D_q^h(z, Q^2)}{\underbrace{\sum_{q'} e_{q'}^2 q'(x, Q^2) \int dz D_{q'}^h(z, Q^2)}_{P_q^h(x, Q^2)}} \frac{\Delta q}{q}(x, Q^2)$$

☞ **Purities** : probability that hadron  $h$  originates from event with struck quark  $q$

- Spin independent quantities
- Can be calculated with Monte Carlo

☞ Extract  $\Delta q$  from

$$\vec{A} = P \cdot \vec{Q}$$

$$\vec{A} = \left( A_{1,p}(x), A_{1,d}(x), A_{1,p}^{\pi^\pm}(x), A_{1,d}^{\pi^\pm}(x), A_{1,d}^{K^\pm}(x) \right)$$

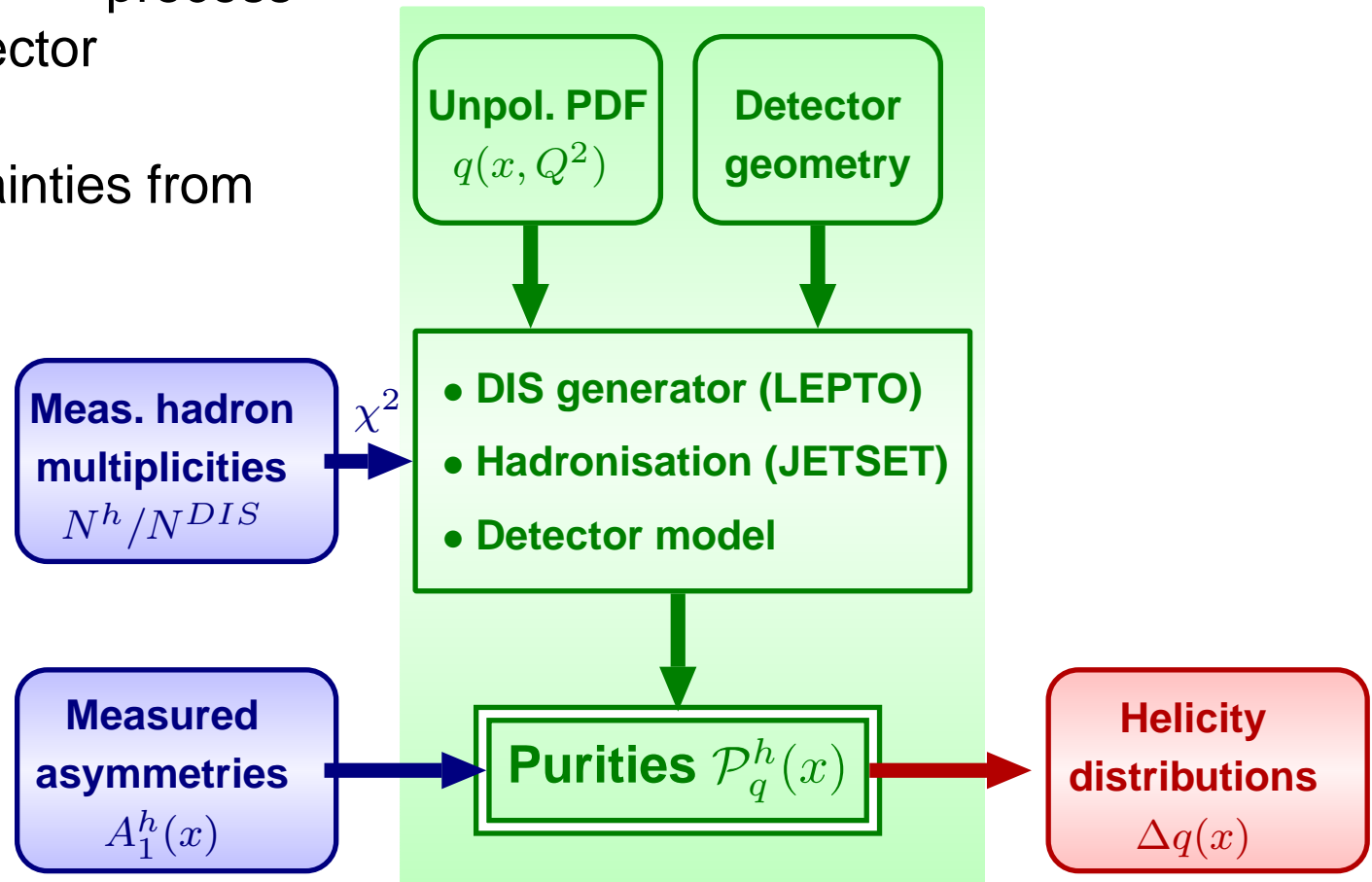
$$\vec{Q} = \left( \frac{\Delta u}{u}, \frac{\Delta d}{d}, \frac{\Delta \bar{u}}{\bar{u}}, \frac{\Delta \bar{d}}{\bar{d}}, \frac{\Delta s + \Delta \bar{s}}{s + \bar{s}} \right)$$

# Generation of Purities

- Use Monte Carlo model of DIS process (LEPTO), fragmentation process (JETSET) and detector

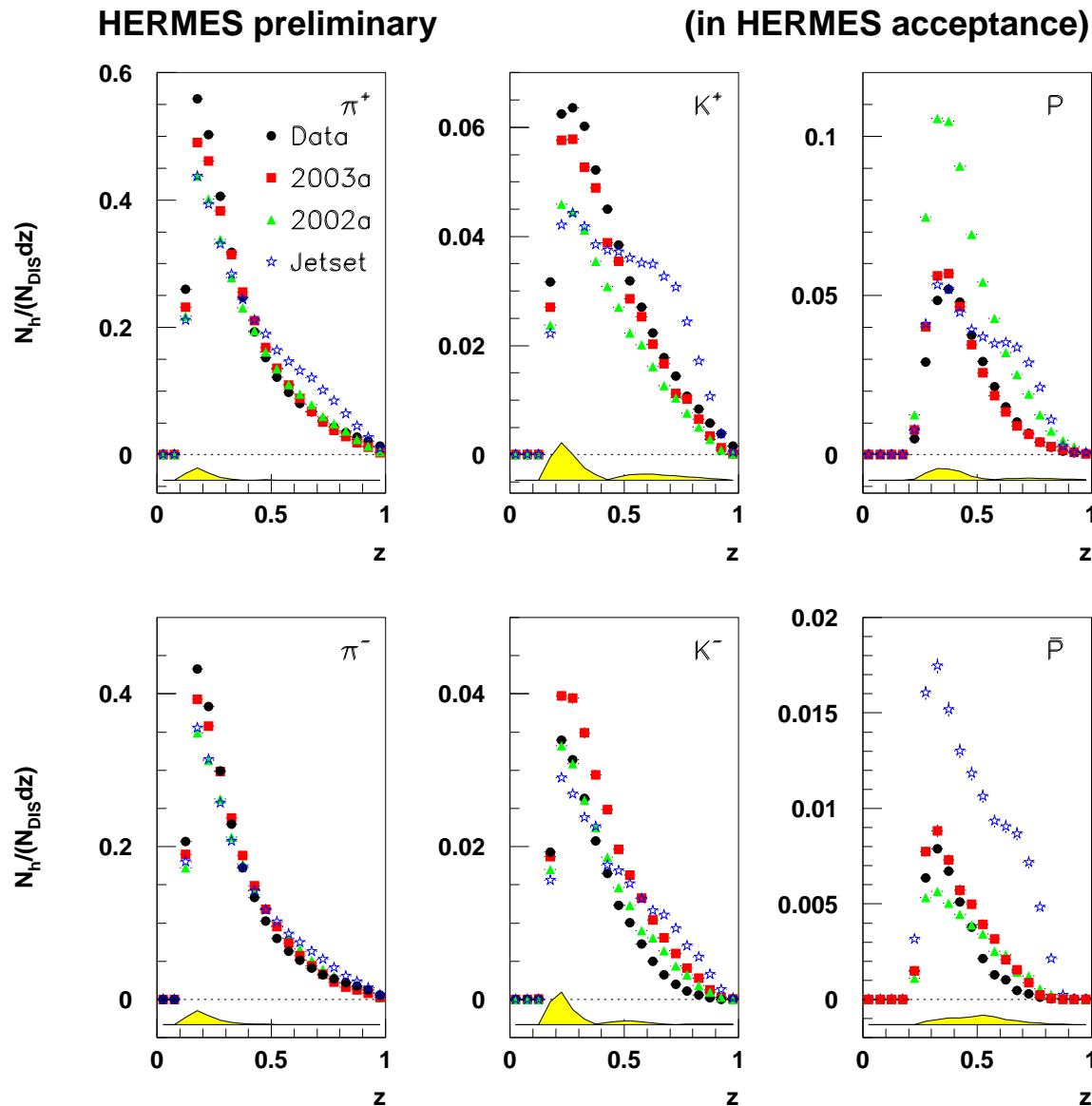
- Systematic uncertainties from

- Use of alternative PDF sets (GRV98LO, CTEQ5L)
- Variation of fragmentation parameters





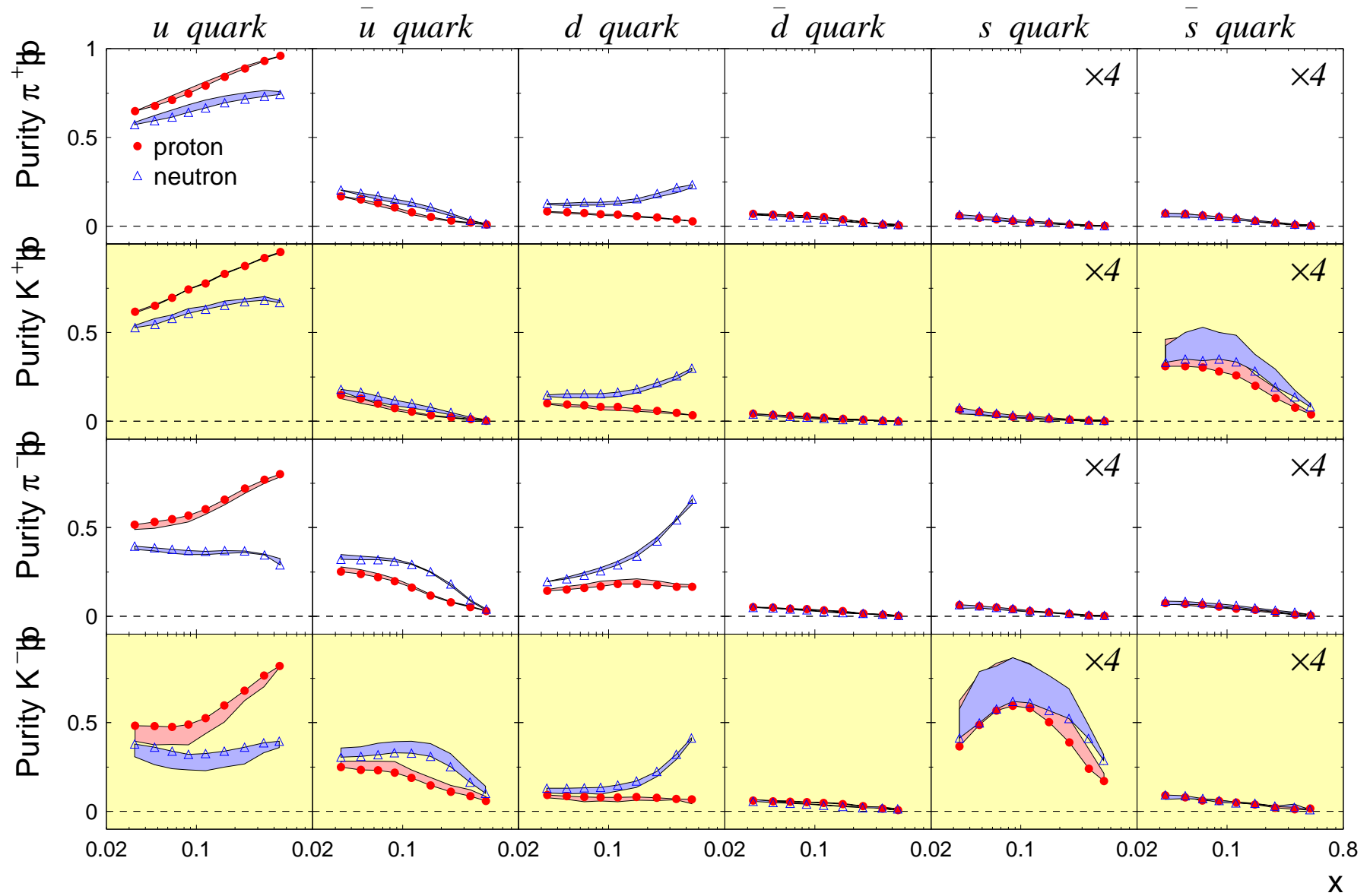
# Tuning of LUND Fragmentation Model



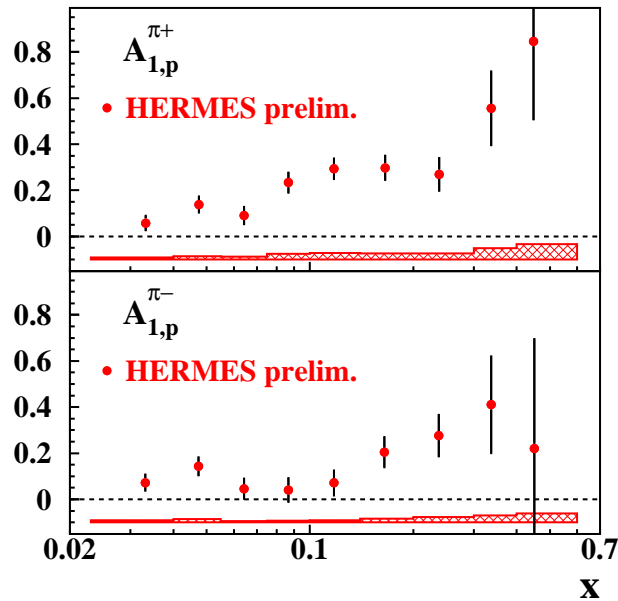
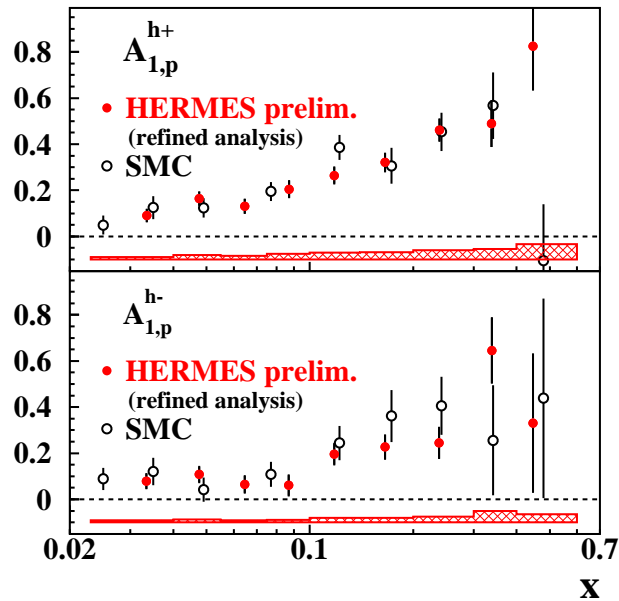
Default JETSET settings don't work for HERMES

☞ Use hadron production ratios and measured hadron multiplicities  $N^h/N^{DIS}$  in (iterative) tuning procedure

# HERMES Purities



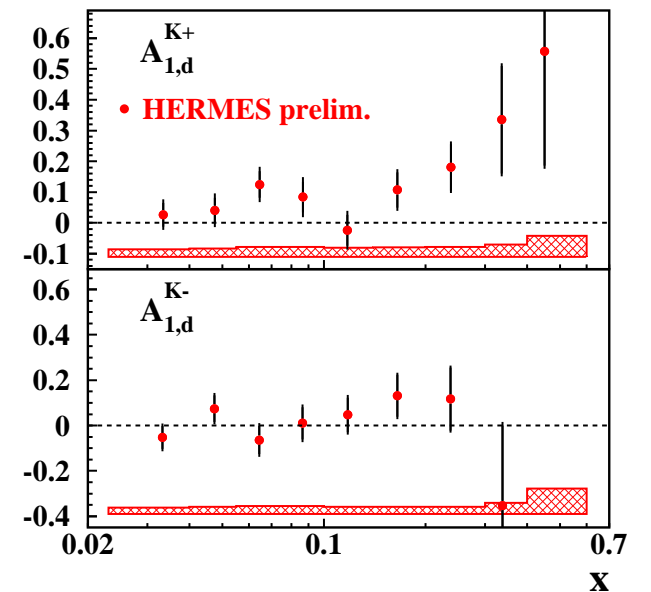
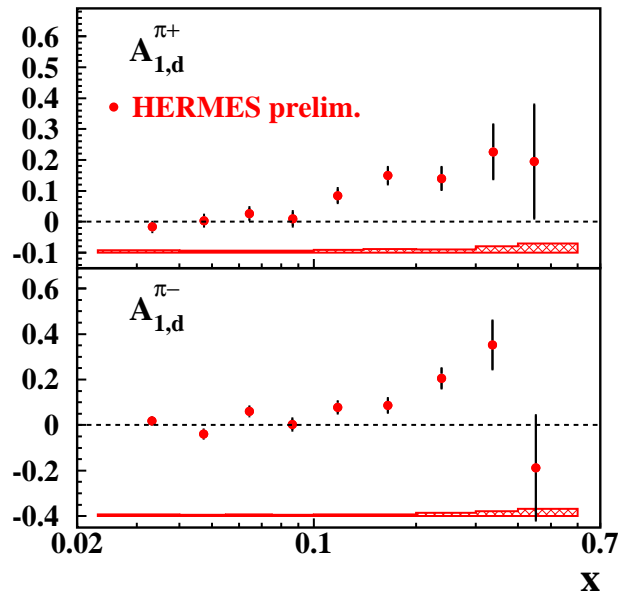
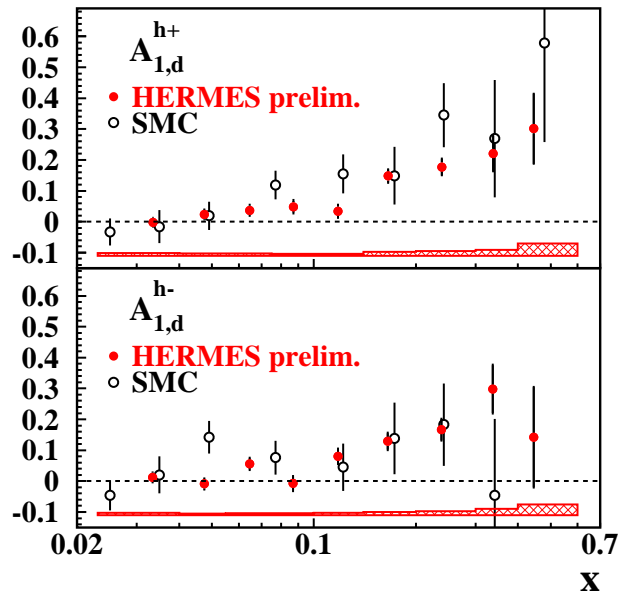
# Measured Hadron Asymmetries



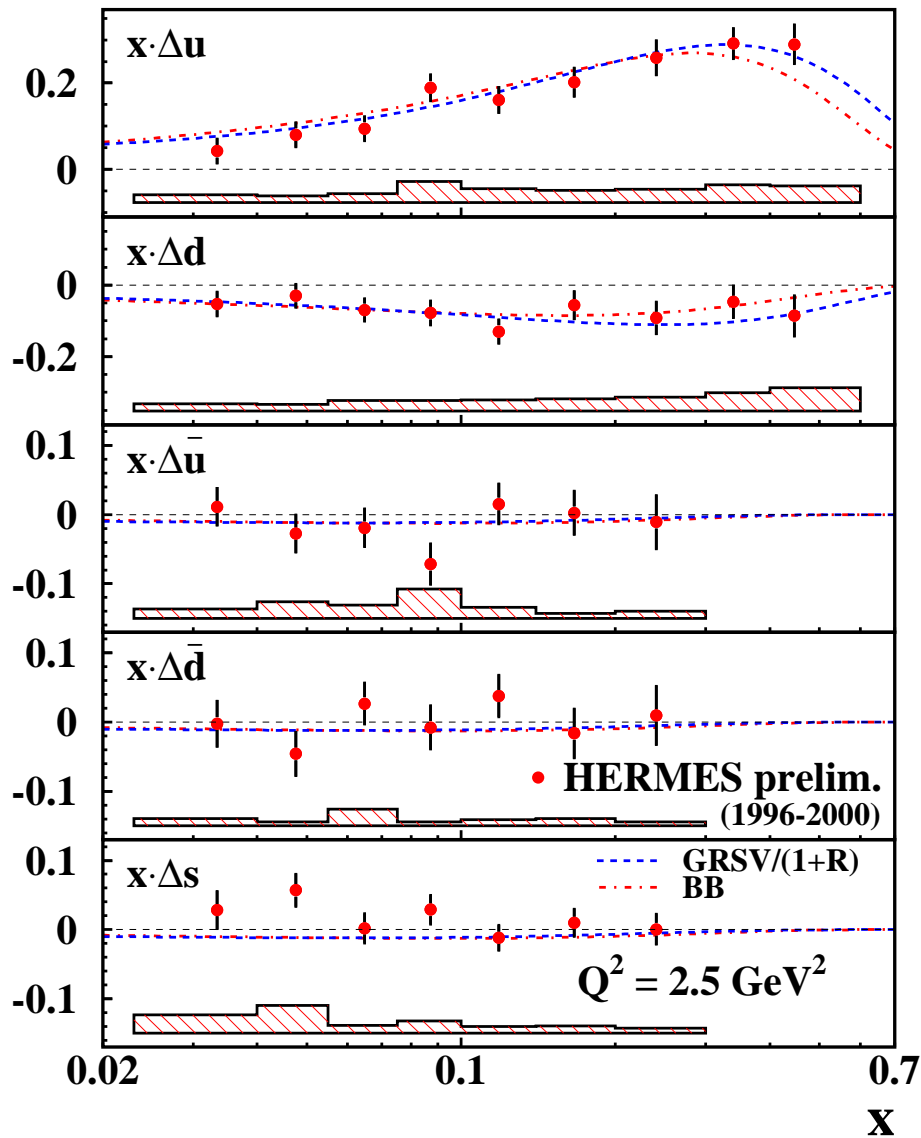
Kinematical range :

$$0.023 \leq x \leq 0.6$$

$$0.2 \leq z \leq 0.8$$

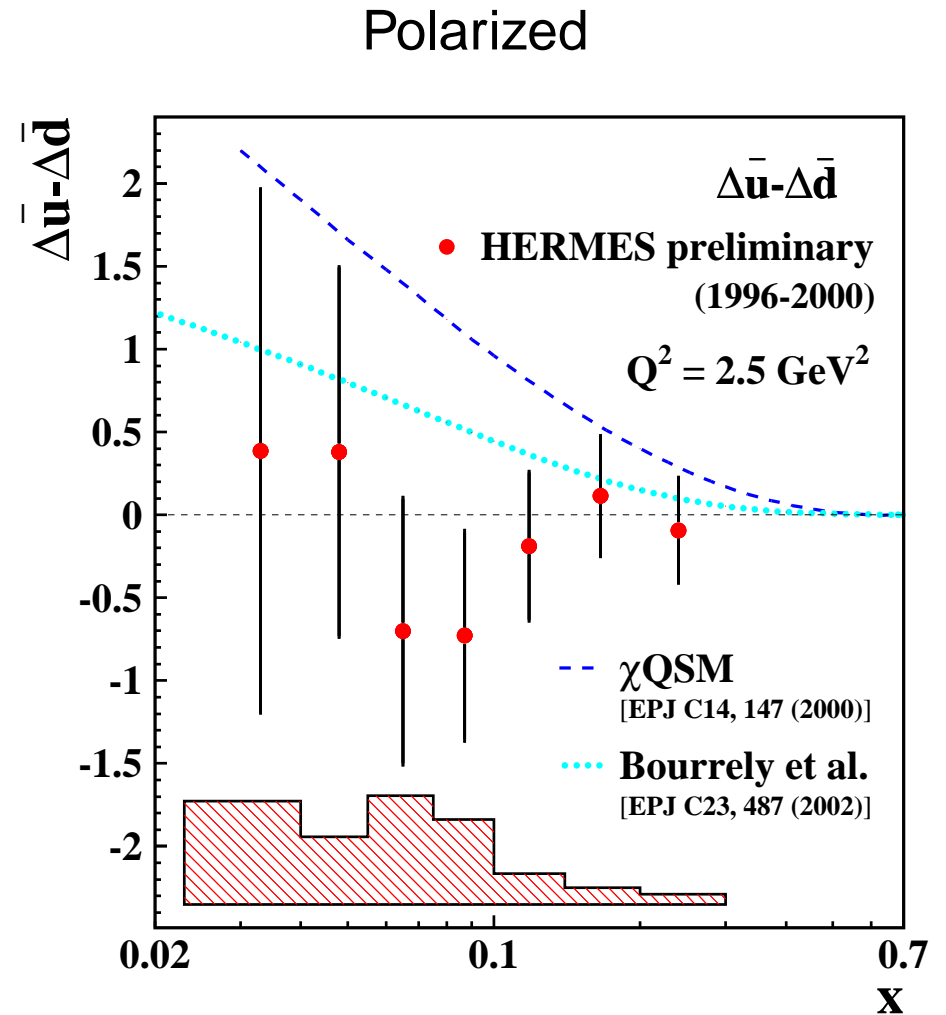
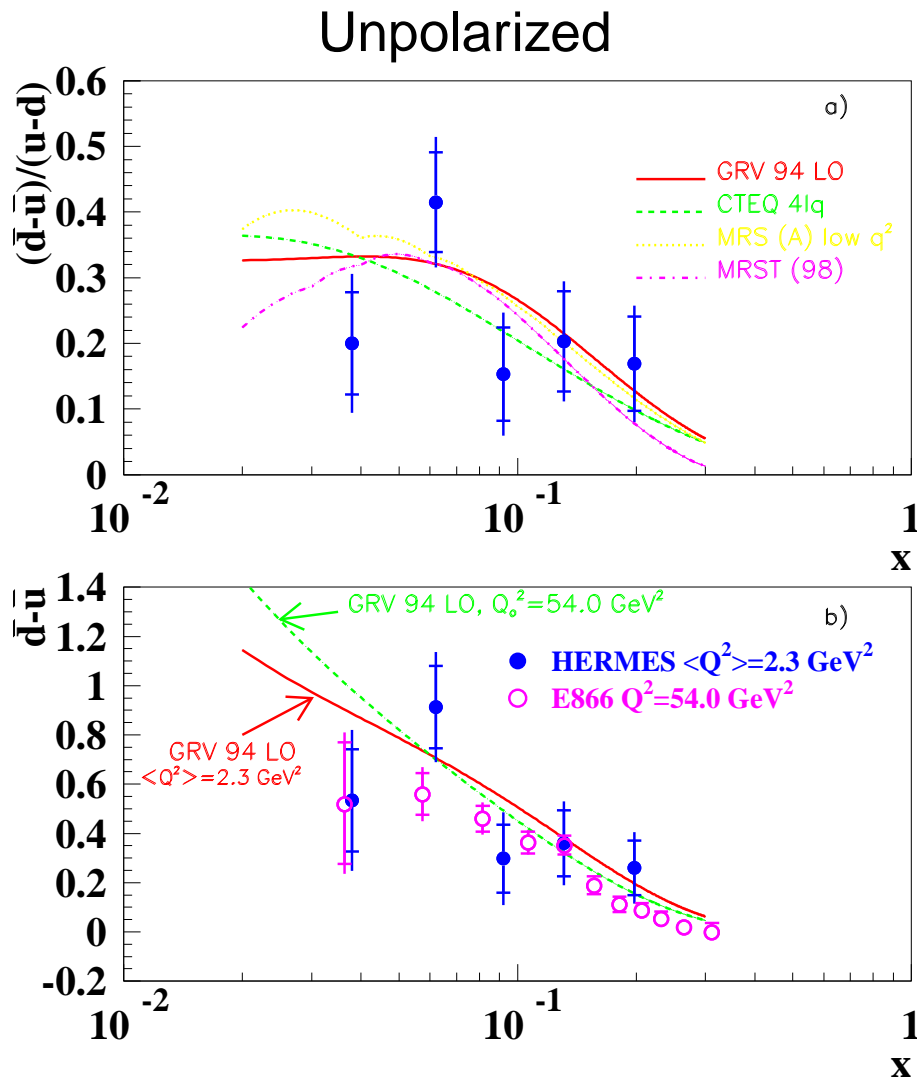


# Polarized Quark Distributions



- $u$ -quark strongly polarized
- $d$ -quark strongly anti-polarized
- Quark sea polarization small and
 
$$\frac{\Delta\bar{u}}{\bar{u}} \sim \frac{\Delta\bar{d}}{\bar{d}} \sim \frac{\Delta s + \Delta\bar{s}}{s + \bar{s}} \sim 0$$
- No indication of negative strange sea polarization
- Good agreement with LO-QCD fits

# Light Quark Sea Flavor Asymmetry



👉 No evidence of flavor asymmetry  $\Delta \bar{u} - \Delta \bar{d}$  in the light quark sea !

# Deep Inelastic Scattering on Spin 1 Target

$$\frac{d^2\sigma}{d\Omega dE^2} = \frac{\alpha^2 E'}{Q^2 E} L_{\mu\nu}(k, q, s) W^{\mu\nu}(P, q, S)$$

$L_{\mu\nu}$  : exactly calculable in QED

$$W^{\mu\nu} = -g^{\mu\nu} F_1(x, Q^2) + \frac{p^\mu p^\nu}{\nu} F_2(x, Q^2) + i\epsilon^{\mu\nu\lambda\sigma} \frac{q_\lambda}{\nu} (S_\sigma g_1(x, Q^2) + \frac{1}{\nu} (p \cdot q S_\sigma - S \cdot q p_\sigma) g_2(x, Q^2))$$

( for spin 1 target )

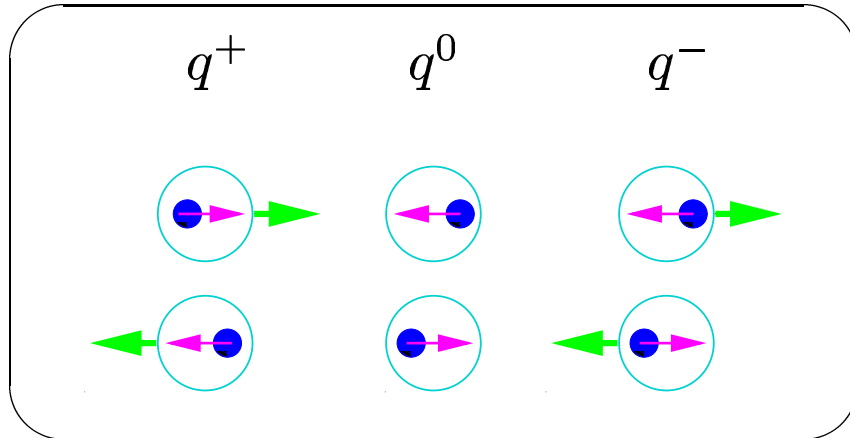
$$-b_1(x, Q^2) r_{\mu\nu} + \frac{1}{6} b_2(x, Q^2) (s_{\mu\nu} + t_{\mu\nu} + u_{\mu\nu}) + \frac{1}{2} b_3(x, Q^2) (s_{\mu\nu} - u_{\mu\nu}) + \frac{1}{2} b_4(x, Q^2) (s_{\mu\nu} - t_{\mu\nu})$$

 4 new structure functions

in the symmetric part of hadronic tensor

⇒ not sensitive to beam polarization

# $b_1$ Structure Function



$$F_1(x) = \frac{1}{3} \sum_q e_q^2 [q^+(x) + q^-(x) + q^0(x)]$$

$$g_1(x) = \frac{1}{2} \sum_q e_q^2 [q^+(x) - q^-(x)]$$

$$b_1(x) = \frac{1}{2} \sum_q e_q^2 [2q^0(x) - (q^-(x) + q^+(x))]$$

$$b_2(x) = 2x \frac{(1+R)}{(1+\gamma^2)} b_1(x)$$

$b_3$  &  $b_4$  higher twist functions

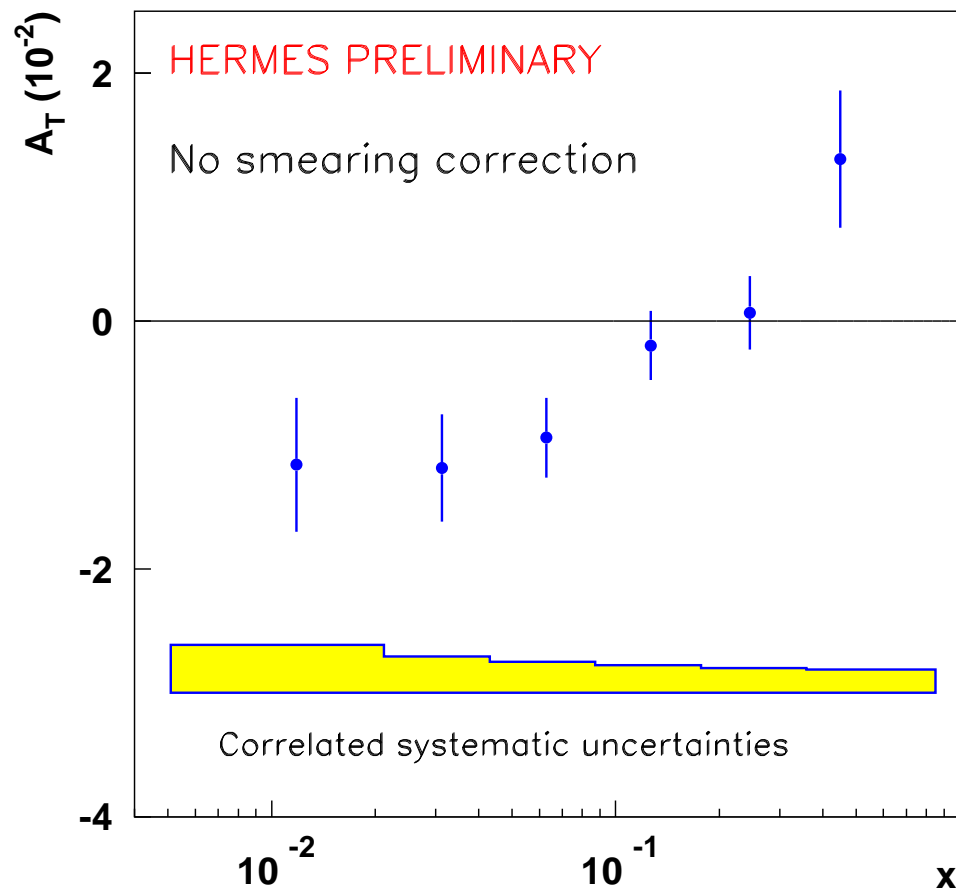
☞  $b_1(x)$  measures difference in parton distributions of  $m = 1$  and  $m = 0$  target

☞ In principle needed for  $g_1/F_1$  measurement

$$\sigma_{meas} = \sigma_u \left[ 1 + P_b V A_{||} + \frac{1}{2} T A_T \right]$$

HERMES :  $\langle T \rangle = 0.83 \pm 0.03$        $\langle V \rangle = 10^{-2}$

# The Tensor Asymmetry $A_T$



$$0.002 < x < 0.85, \quad Q^2 > 0.1 \text{ GeV}^2$$

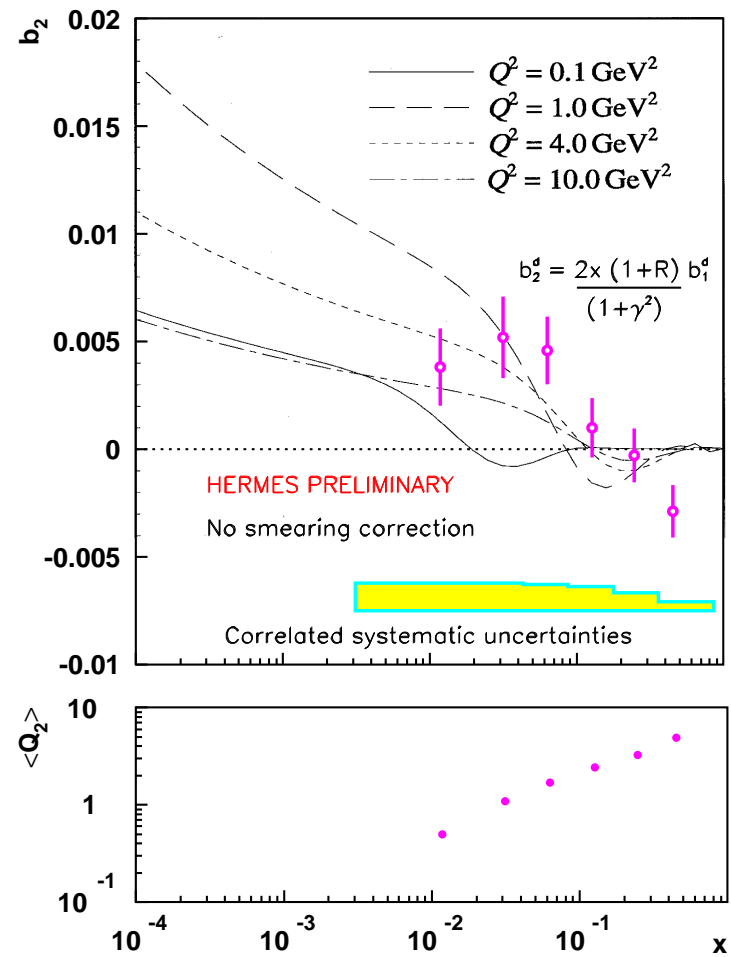
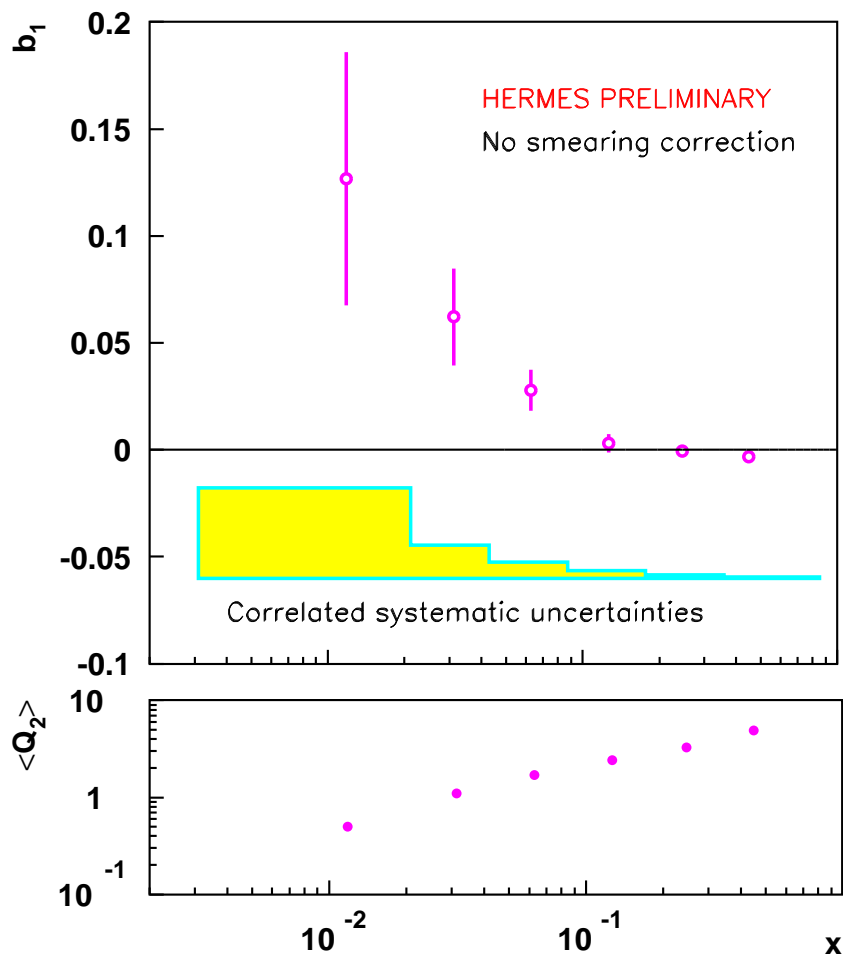
$$A_T = \frac{(\sigma^+ + \sigma^-) - 2\sigma^0}{3\sigma_u} \sim -\frac{2b_1}{3F_1}$$

$$A_{\parallel} = A_{\parallel}^{meas} \cdot \left[ 1 + \frac{1}{2} T A_T \right] \sim \frac{g_1}{F_1}$$

☞ Influence on  $A_{\parallel} < 1 \%$



# $b_{1,2}^d$ Structure Function

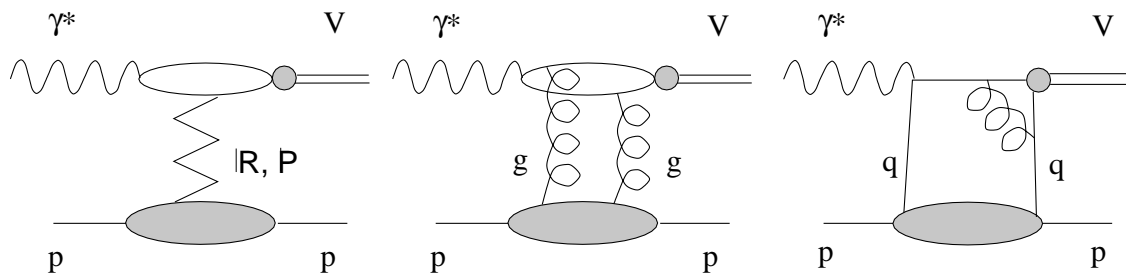


$$b_1^d = -\frac{3}{2} \cdot A_T \cdot F_1^d$$

K. Bora and R.L. Jaffe, PRD57 (1998) 6906

☞  $b_2^d$  signif. different from zero at low  $x$

# Exclusive Vector Meson Production @ HERMES



$$e + p, A \rightarrow e + p + \rho^0, \omega, \phi$$

$$0.5 < Q^2 < 5.0 \text{ GeV}^2,$$

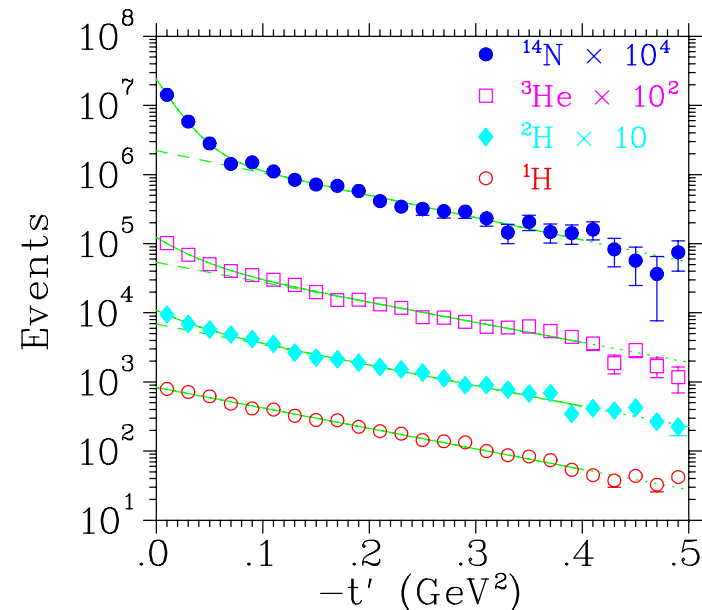
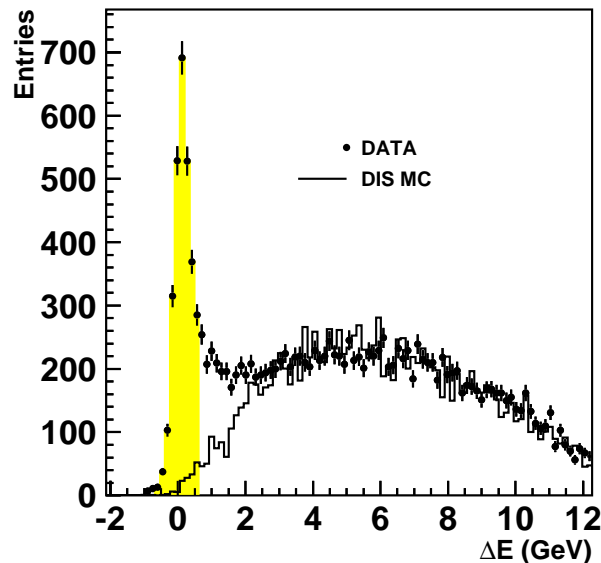
$$4.0 < W < 6.0 \text{ GeV},$$

$$t < 0.5 \text{ GeV}^2$$

$\rho^0, \omega$  production at HERMES is dominated by **quark exchange**,  
 $\phi$  production dominated by **gluon exchange**

Exclusivity :  $\Delta E = \frac{(M_X^2 - M_p^2)}{2 M_p}$

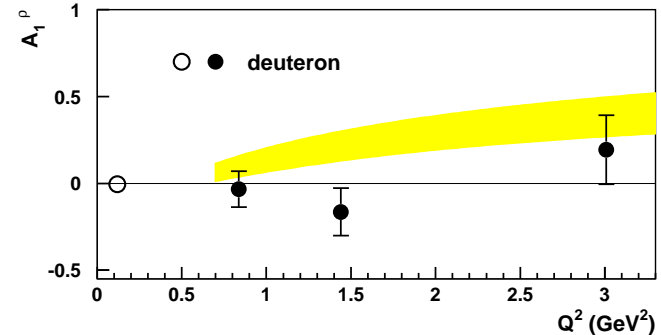
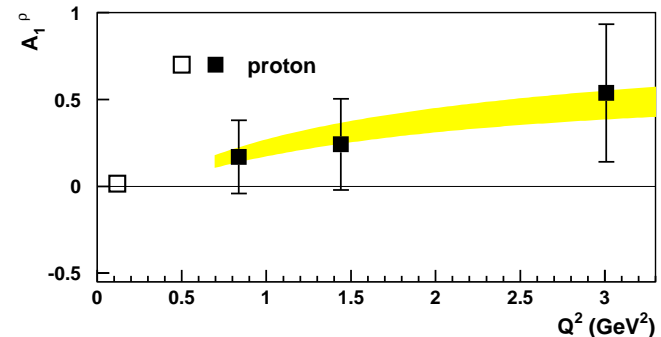
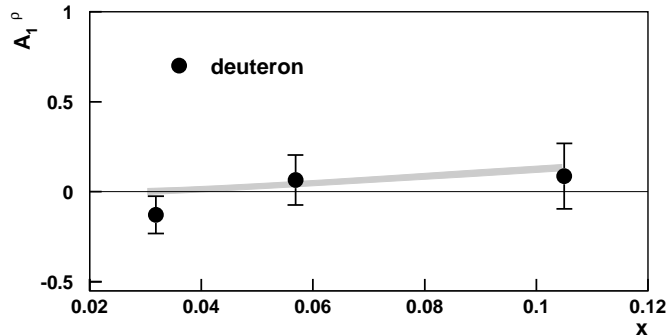
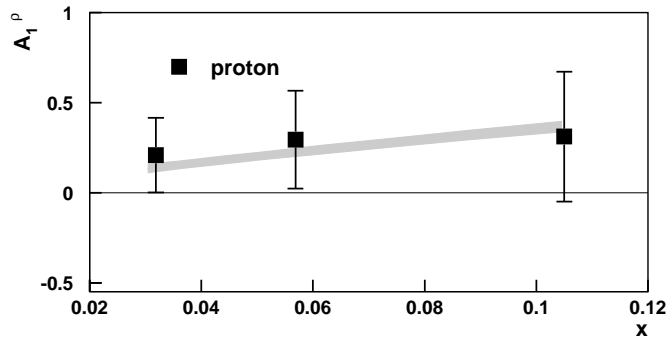
Incoherent / coherent diffractive production



# Double Spin Asymmetry in VM Production

$$A_{\parallel} \equiv \frac{\sigma^{\uparrow\downarrow} - \sigma^{\uparrow\uparrow}}{\sigma^{\uparrow\downarrow} + \sigma^{\uparrow\uparrow}} \quad A_1 = \frac{A_{\parallel}}{D} - \eta\sqrt{R}$$

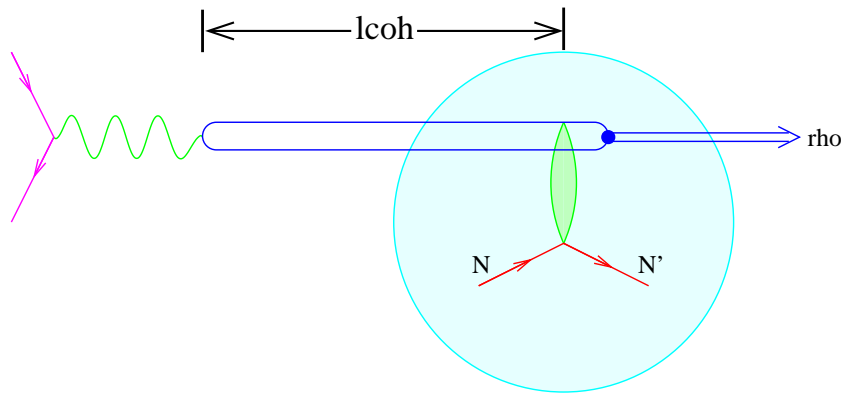
$$\begin{aligned} \langle A_1^{p,\rho} \rangle &= 0.23 \pm 0.14 \pm 0.02 & \langle A_1^{d,\rho} \rangle &= -0.040 \pm 0.076 \pm 0.013 \\ \langle A_1^{p,\phi} \rangle &= 0.20 \pm 0.45 \pm 0.03 & \langle A_1^{d,\phi} \rangle &= 0.17 \pm 0.27 \pm 0.02 \end{aligned}$$



$A_1^{\rho} = 2 A_1^N / (1 + (A_1^N)^2)$  (Fraas)  
 Asymmetry due to **unnatural parity**  
 or **di-quark exchange**

Regge model with parameter fits  
 to  $g_1^p$  and  $F_2^p$  (Kochchelev *et al.*)

# Coherence Length Effect in $\rho^0$ Production



$$\text{Coherence length : } l_c = \frac{2\nu}{Q^2 + M_{q\bar{q}}^2}$$

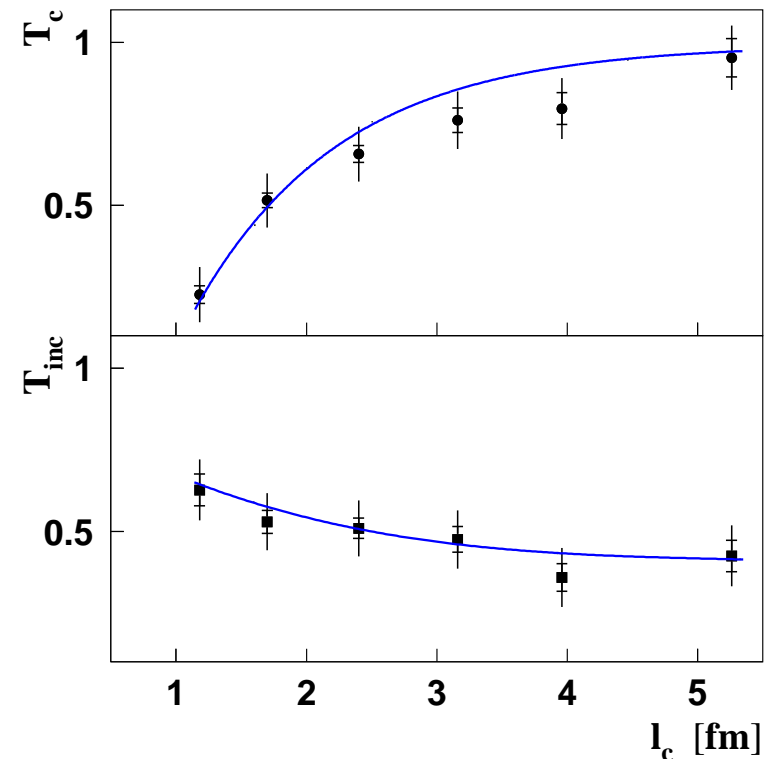
$l_c \ll r_A$  : weak EM ISI

$l_c \gg r_A$  : hadronic ISI

Examine nuclear transparency :  $T = \frac{\sigma_A}{A \cdot \sigma_p}$   
to look for color transparency ( $^{14}\text{N}$  data)

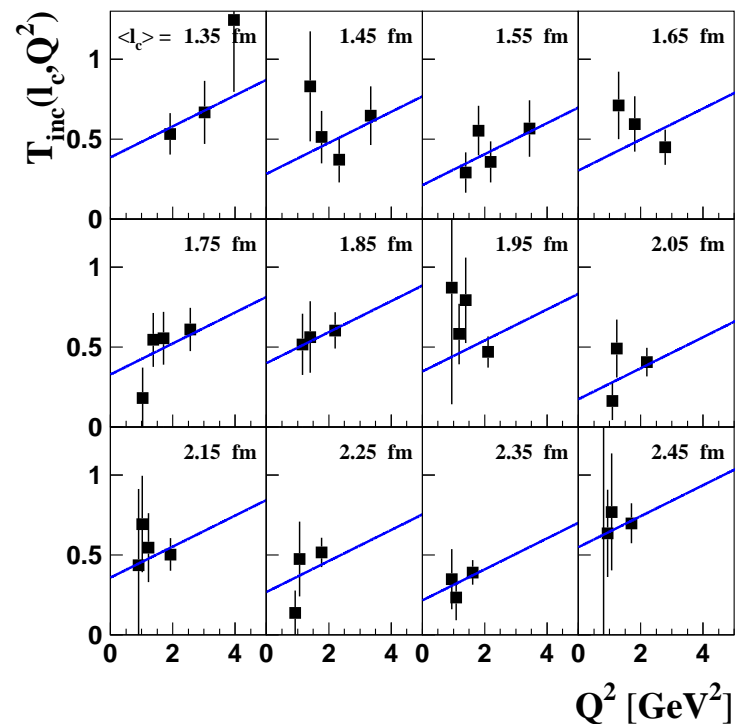
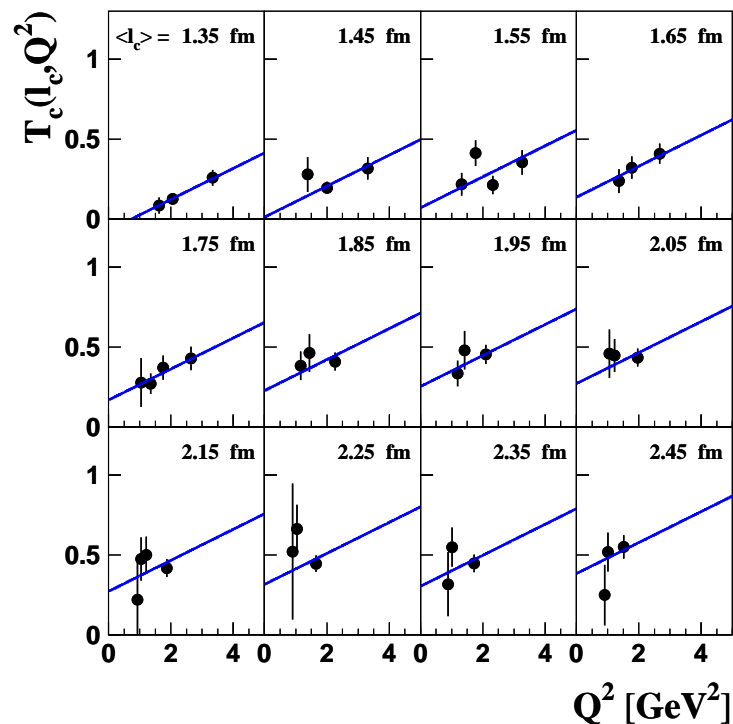
☞ Incoherent production : coherence length effect can mimic CT effects for  $l_c \ll r_A$

☞ Coherent production : nuclear form factor suppression at small  $l_c$



# Color Transparency in $\rho^0$ Production

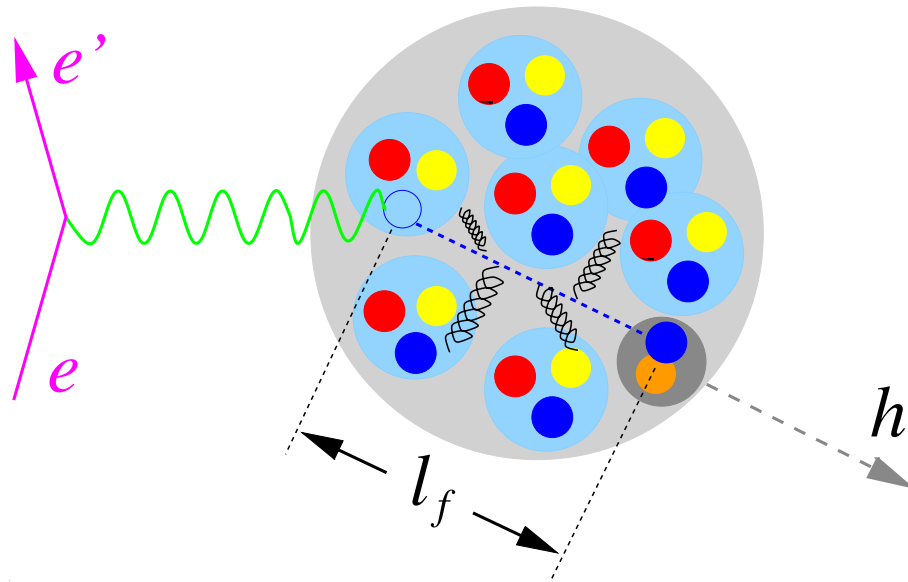
Fit  $Q^2$ -dependence of  $T^{coh/incoh}$  in  $l_c$ -bins with common slope



	$Q^2$ -dep. slope	Kopeliovich <i>et al.</i>
$^{14}\text{N}$ coherent	$0.070 \pm 0.021 \pm 0.017$	0.060
$^{14}\text{N}$ incoherent	$0.089 \pm 0.046 \pm 0.020$	0.048

Positive  $Q^2$  slope **indication of onset of Color Transparency**

# Fragmentation in Nuclear Environment



Nucleus acts as an ensemble of targets for the struck quark and produced hadron

☞ Hadron production from nuclei is influenced by **pre-hadronized quark interactions** & **produced hadron interactions** with spectator nucleons

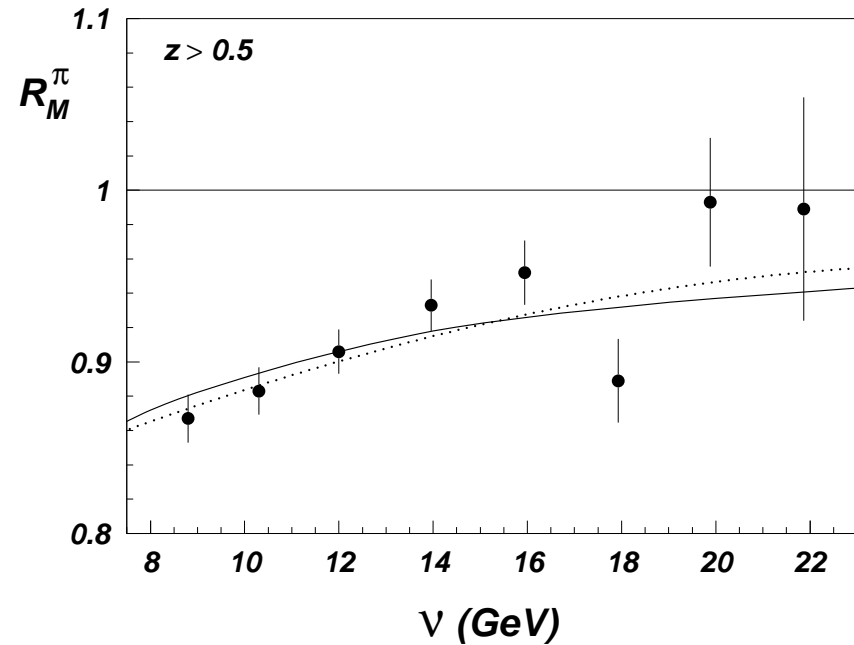
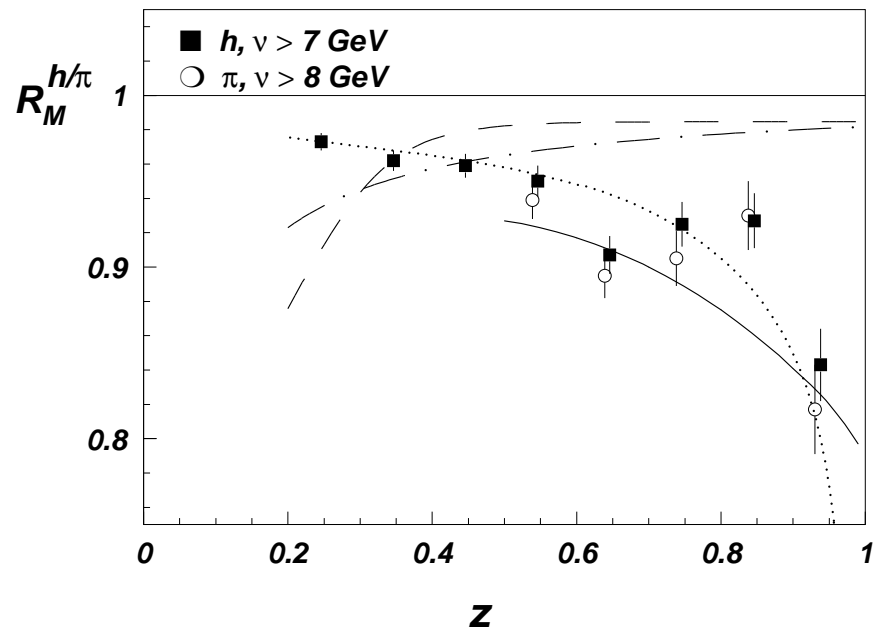
→ Models : hadronization process (phenomenological + QCD based models) + nuclear absorption

$\tau_f = l_f/c$  hadron formation time

☞ Reduction of multiplicity of  $R_M^h(z, \nu, p_t^2, Q^2) = \frac{N_h(z, \nu, p_t^2, Q^2) \Big|_A}{N_e(\nu, Q^2)} \Big|_D$

Use HERMES data on  $^{14}\text{N}$ ,  $^{84}\text{Kr}$ , ( $^4\text{He}$ ,  $^{20}\text{Ne}$ ) with  $z > 0.2$  &  $\nu > 7$  GeV

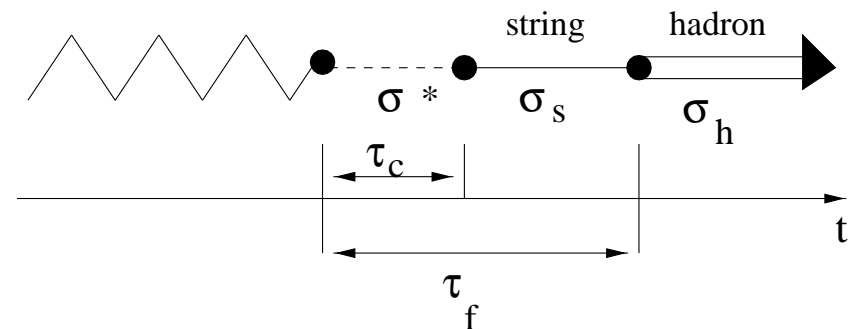
# Charged Hadron Multiplicity Ratios ( $^{14}\text{N}$ )



(dotted) 1 or 2 time-scale models

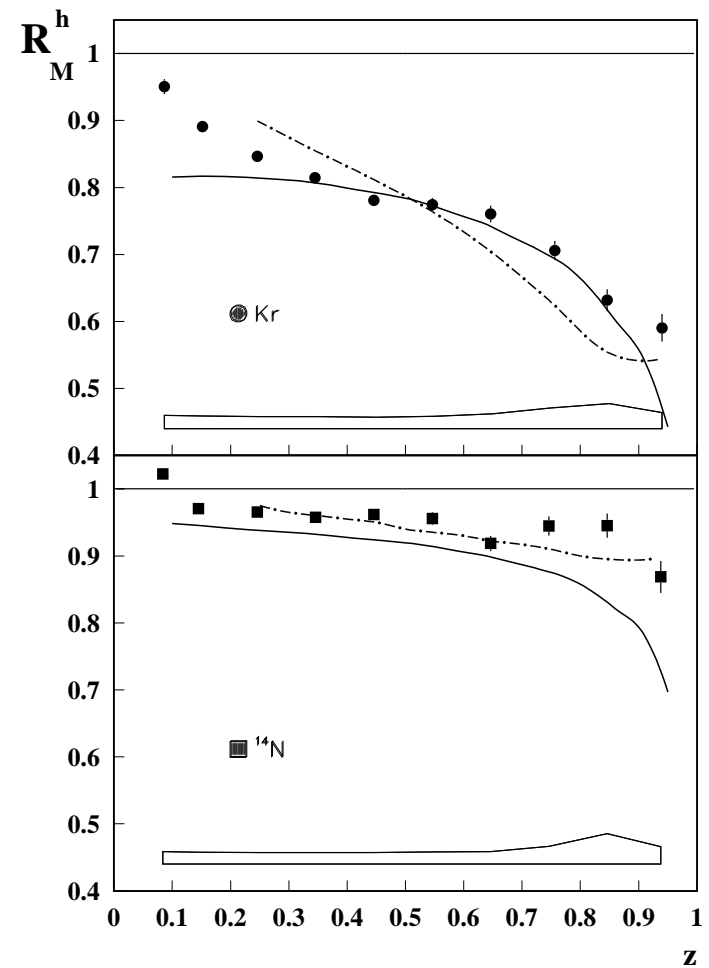
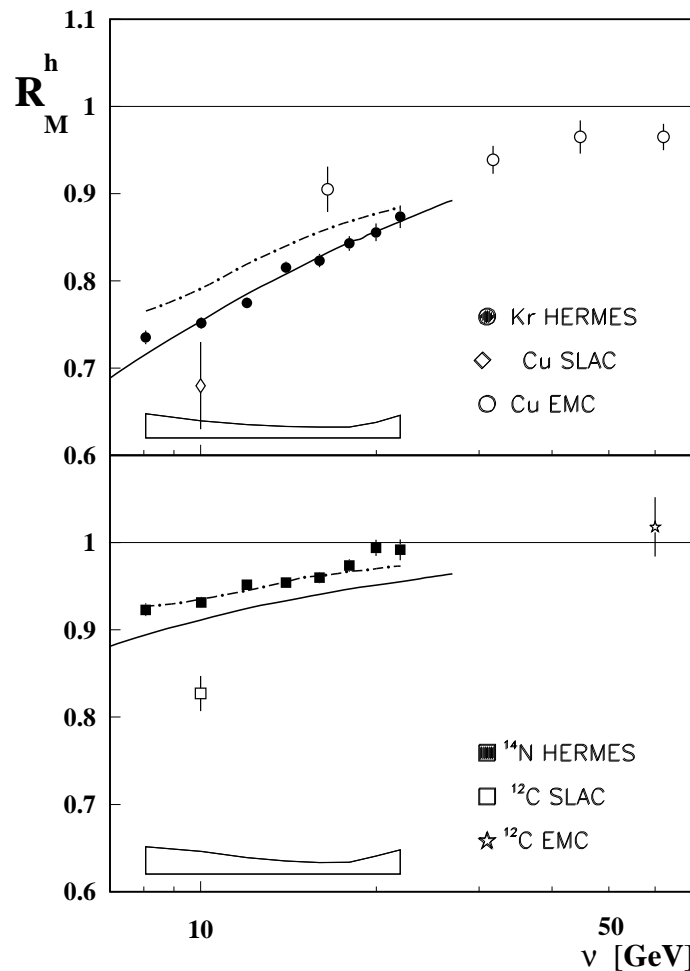
$$t_f^h = c_h(1-z)\nu, \quad \sigma^* = 0, \quad \sigma_h = 25 \text{ mb}$$

☞ Formation time fits



(solid, Kopeliovich *et al.*) Gluon bremsstrahlung model for pions

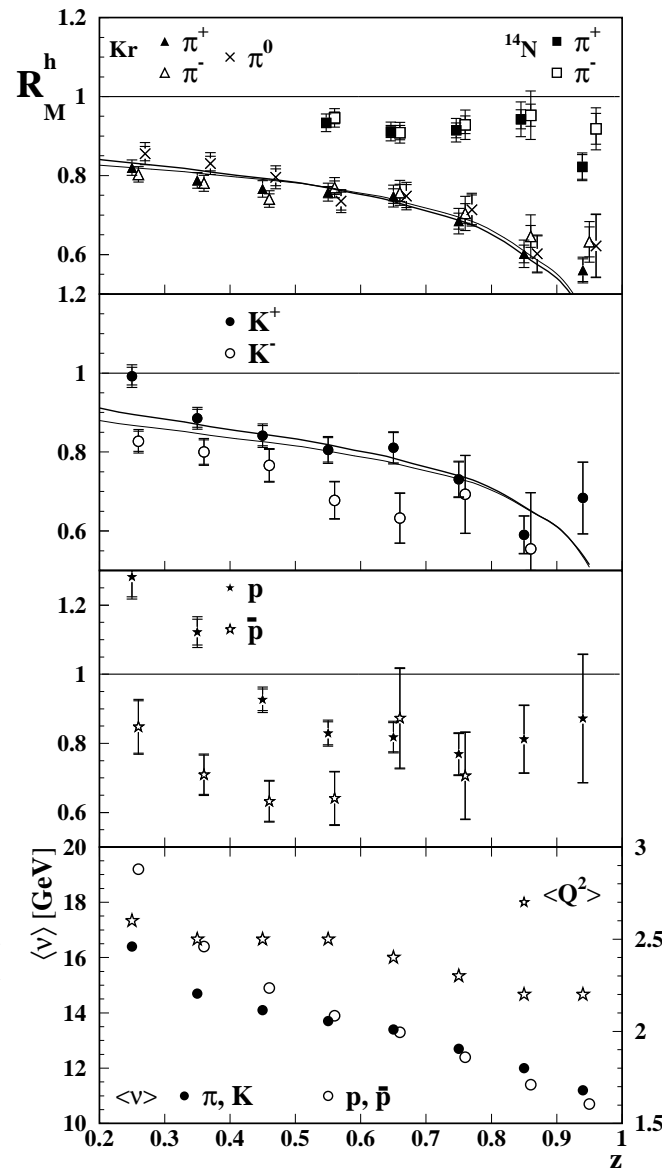
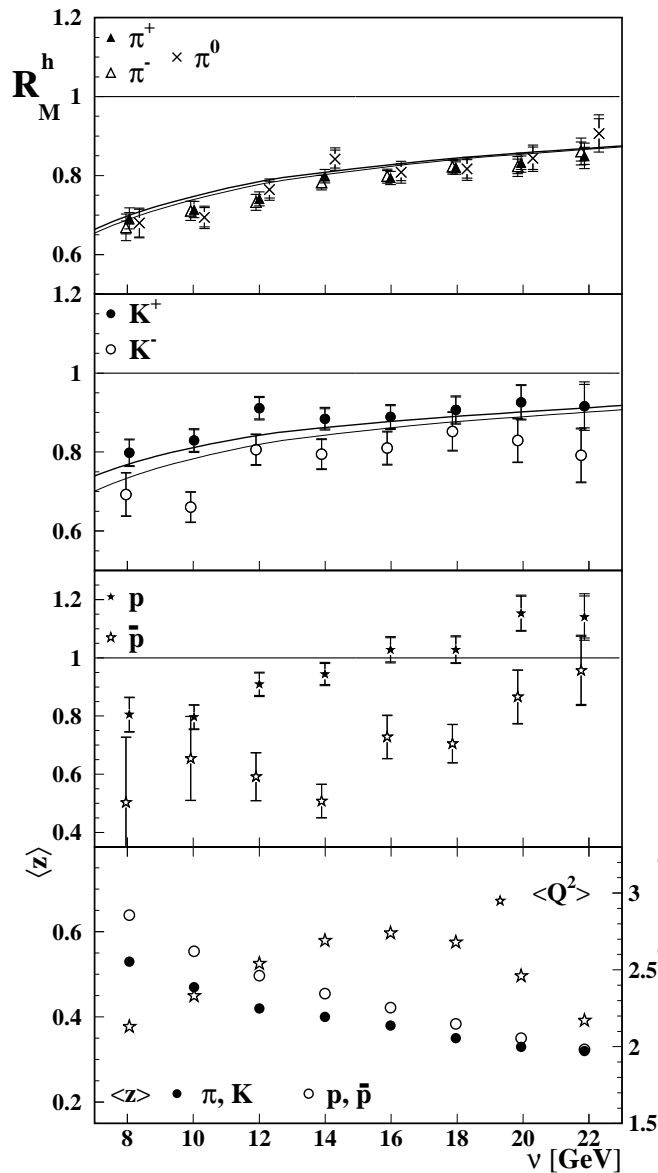
# Charged Hadron Multiplicity Ratios ( $^{14}\text{N}$ , $^{84}\text{Kr}$ )



Model calculations : (solid, Accardi *et al.*) rescaling of quark fragmentation functions + nuclear absorption; (dot-dashed, Wang *et al.*) medium modification of parton fragmentation due to multiple scattering and gluon bremsstrahlung (tuned to  $^{14}\text{N}$  data)



# $\pi^{\pm,0}, K^{\pm}, p$ & $\bar{p}$ Multiplicity Ratios ( $^{84}\text{Kr}$ )



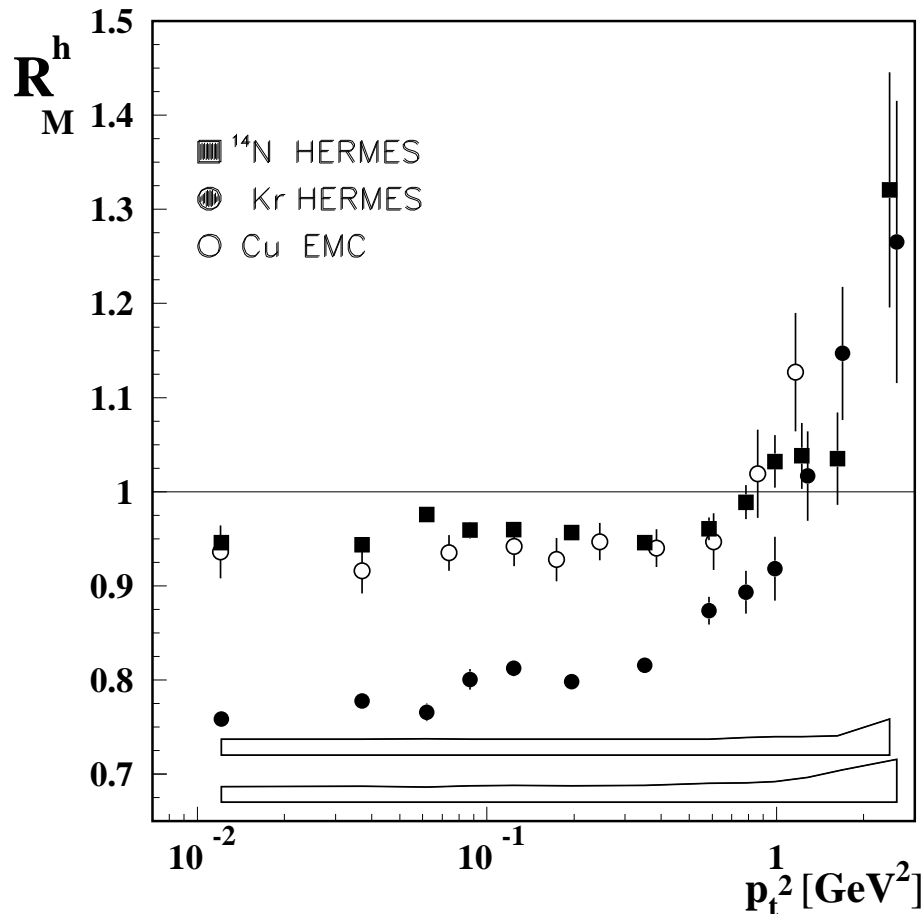
$R_M^{\pi^+} \sim R_M^{\pi^-} \sim R_M^{\pi^0}$ , but  
 $R_M^{K^+} > R_M^{K^-}$ ,  $R_M^p > R_M^{\bar{p}}$  and  
 $R_M^p > R_M^\pi$

☞ Different formation times of baryons and mesons; different hadron-nucleon interaction cross sections

☞ Mixing of quark and gluon fragmentation functions (Wang *et al.*);

$(1 - R_M^N)/(1 - R_M^{Kr})$  agrees with scaling law  $1 - R_M \propto A^\alpha$  with predicted  $\alpha = \frac{2}{3}$  (=  $\frac{1}{3}$  nuclear absorption only)

# Attenuation vs. $p_t^2$



Broadening of  $p_t$  distribution on nuclear target due to multiple scattering of propagating quark and hadron, ie. **Cronin effect**

Effect observed previously in heavy-ion and hadron-nucleus scattering

Enhancement predicted to occur at  $p_t \sim 1 - 2$  GeV

Possible A-dependence of Cronin effect in DIS

## Summary

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- New NLO QCD fit to world data on  $g_1(x, Q^2)$
- $\Delta u(x)$  and  $\Delta d(x)$  known to good precision, consistent with NLO fits of inclusive data
- First direct extraction of  $\Delta \bar{u}(x)$ ,  $\Delta \bar{d}(x)$  and  $\Delta s(x)$ , no significant polarization of the light quark sea
- First measurement of  $b_1^d$ , small but different from zero
- Measurement of double spin asymmetry in vector meson production on proton and deuteron
- Indication of color transparency effect in  $\rho^0$  production on  $^{14}\text{N}$
- First measurement of nuclear attenuation of pions, kaons and (anti)protons electroproduction in  $^{84}\text{Kr}$ .
- Observation of Cronin effect in DIS