

Final HERMES Results on Single-Spin Asymmetries in Lepto-Production of Oppositely Charged Pion Pairs from the Transversely Polarized Hydrogen Target

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arXiv:0803.2367 [hep-ex]

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Quark Structure of Nucleon

- **quark number density:**

measures spin averaged distribution

$$f_1^q = \text{[diagram of a circle with a black dot]} \quad \textit{well known!!!}$$

- **quark helicity distribution:**

measures helicity difference

precise inclusive measurement: HERMES PRD75(2007)

flavor-separated measurement: HERMES PRD71(2005)

$$g_1^q = \text{[diagram of two circles with black dots and red arrows pointing right, green arrows pointing right]} - \text{[diagram of two circles with black dots and red arrows pointing left, green arrows pointing right]} \quad \textit{known!}$$

- **transversity distribution:**

measures helicity flip

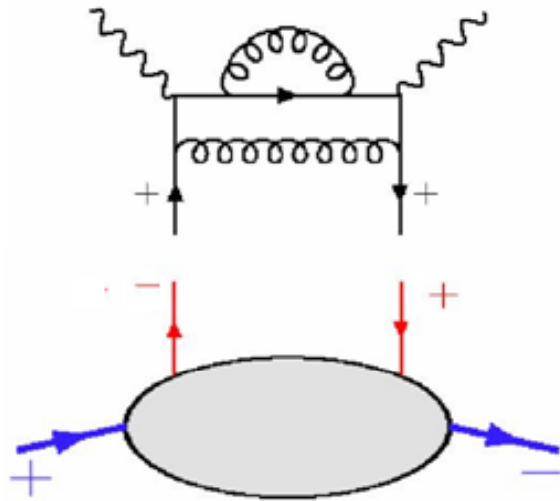
first measurement: HERMES PRL94 (2005)

$$h_1^q = \text{[diagram of a circle with a black dot, a red arrow pointing up, and a green arrow pointing up]} - \text{[diagram of a circle with a black dot, a red arrow pointing down, and a green arrow pointing up]} \quad \textit{first glimpses!}$$

- completes leading-twist picture of nucleon structure
- no gluon transversity \rightarrow weaker Q^2 evolution than f_1 and g_1
- related to relativistic effects inside the nucleon

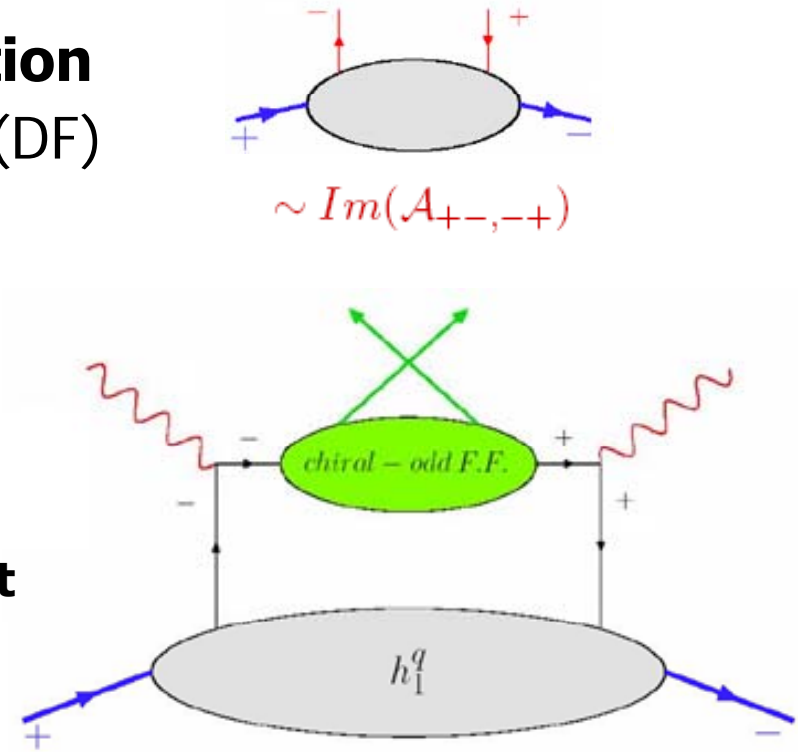
Measurement of Transversity Distribution

- Chirality of the transversity distribution
chiral-odd quark Distribution Function (DF)



cannot be determined in inclusive DIS

need another
chiral-odd object



Semi-Inclusive DIS: coupled to a chiral-odd Fragmentation Function (FF)

- Semi-Inclusive DIS (SIDIS) Cross Section

$$\sigma^{ep \rightarrow ehX} = \sum_q h_1^q \otimes \sigma^{eq \rightarrow eq} \otimes FF^{q \rightarrow h}$$

\Downarrow \Downarrow
chiral-odd DF **chiral-odd FF**

Two-Pion SIDIS Production

semi-inclusive DIS on a transversely polarized hydrogen target

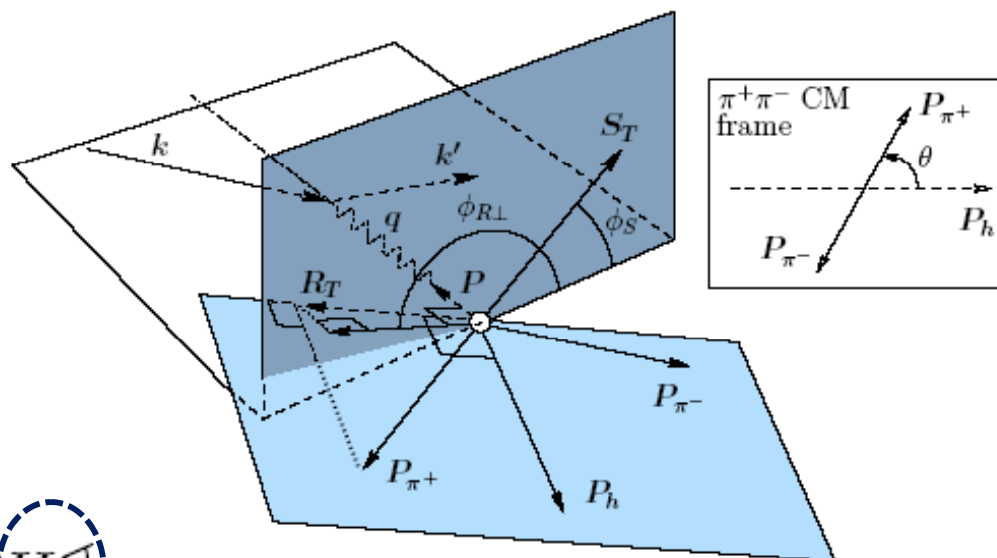
$$e + p^\uparrow \rightarrow e' + \pi^+ + \pi^- + X$$

The target-spin asymmetry:

$$A_{U\perp} \equiv \frac{1}{|S_\perp|} \frac{N^\uparrow - N^\downarrow}{N^\uparrow + N^\downarrow} \sim \frac{\sigma_{UT}}{\sigma_{UU}}$$

$$\sigma_{UU} \sim f_1 D_1$$

$$\sigma_{UT} \sim \sin(\phi_{R\perp} + \phi_S) \sin \theta h_1 \overset{\triangleleft}{H_1}$$



- The asymmetry is related to **transversity**
- It appears with an unknown **Dihadron FF** sensitive to quark transverse quark polarization
- Simpler probe of transversity than one-hadron SIDIS: universal factorization and known Q^2 evolution

Dihadron Fragmentation Function

Dihadron FF H_1^{\triangleleft} : transfer of the transverse spin of the fragmenting quark to the orientation of the hadron pair

Dihadron FFs can be expanded in terms of Legendre functions of $\cos\theta$:

$$D_1(\cos\theta) \simeq D_1 + D_1^{sp} \cos\theta + D_1^{pp} \frac{1}{4}(3\cos^2\theta - 1)$$

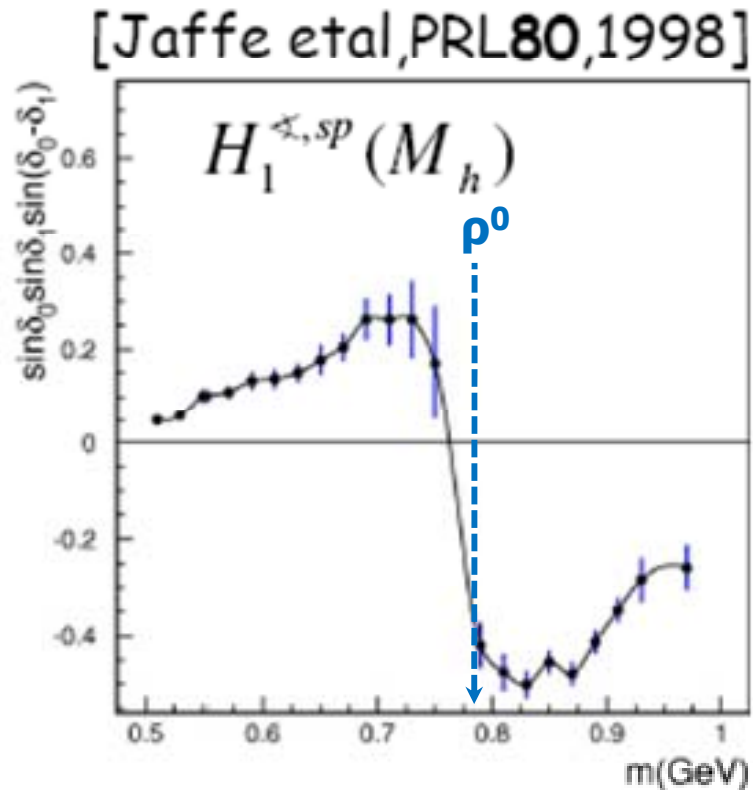
$$H_1^{\triangleleft}(\cos\theta) \simeq H_1^{\triangleleft,sp} + H_1^{\triangleleft,pp} \cos\theta$$

sp : interference between s - and p -wave components of the hadron pair

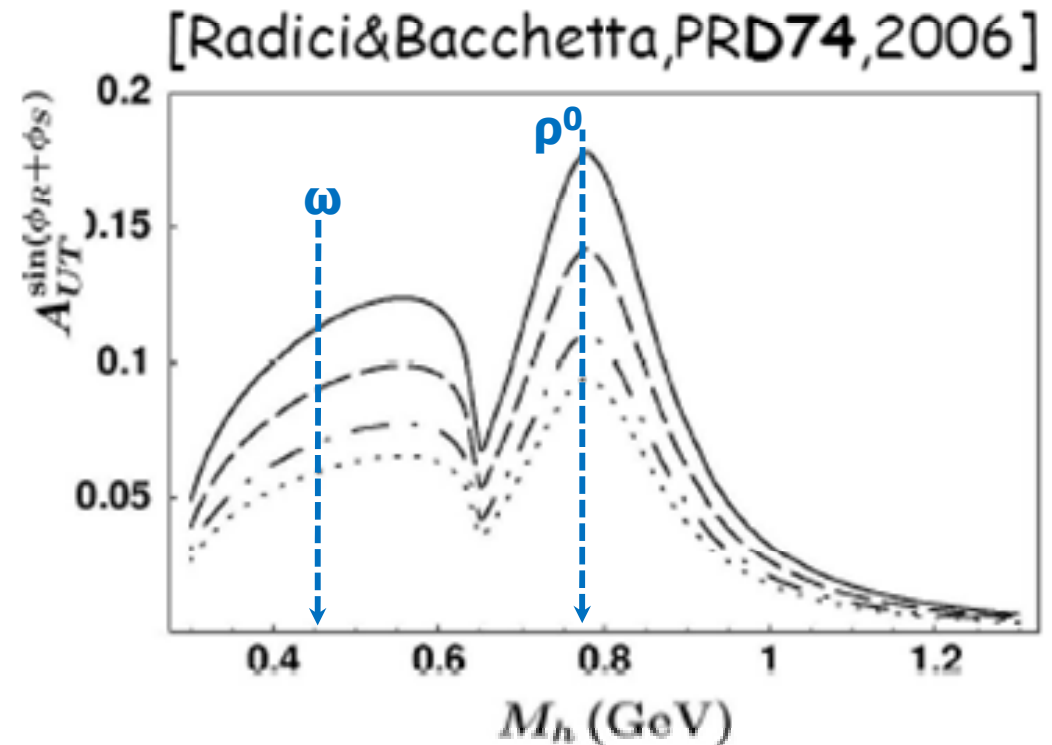
The transverse target-spin asymmetry becomes

$$A_{U\perp} \sim \sin(\phi_{R\perp} + \phi_S) h_1 \frac{H_1^{\triangleleft,sp} \sin\theta + \frac{1}{2} H_1^{\triangleleft,pp} \sin(2\theta)}{f_1(D_1 + \cos\theta D_1^{sp} + \frac{1}{4}(3\cos^2\theta - 1) D_1^{pp})}$$

Theoretical Predictions



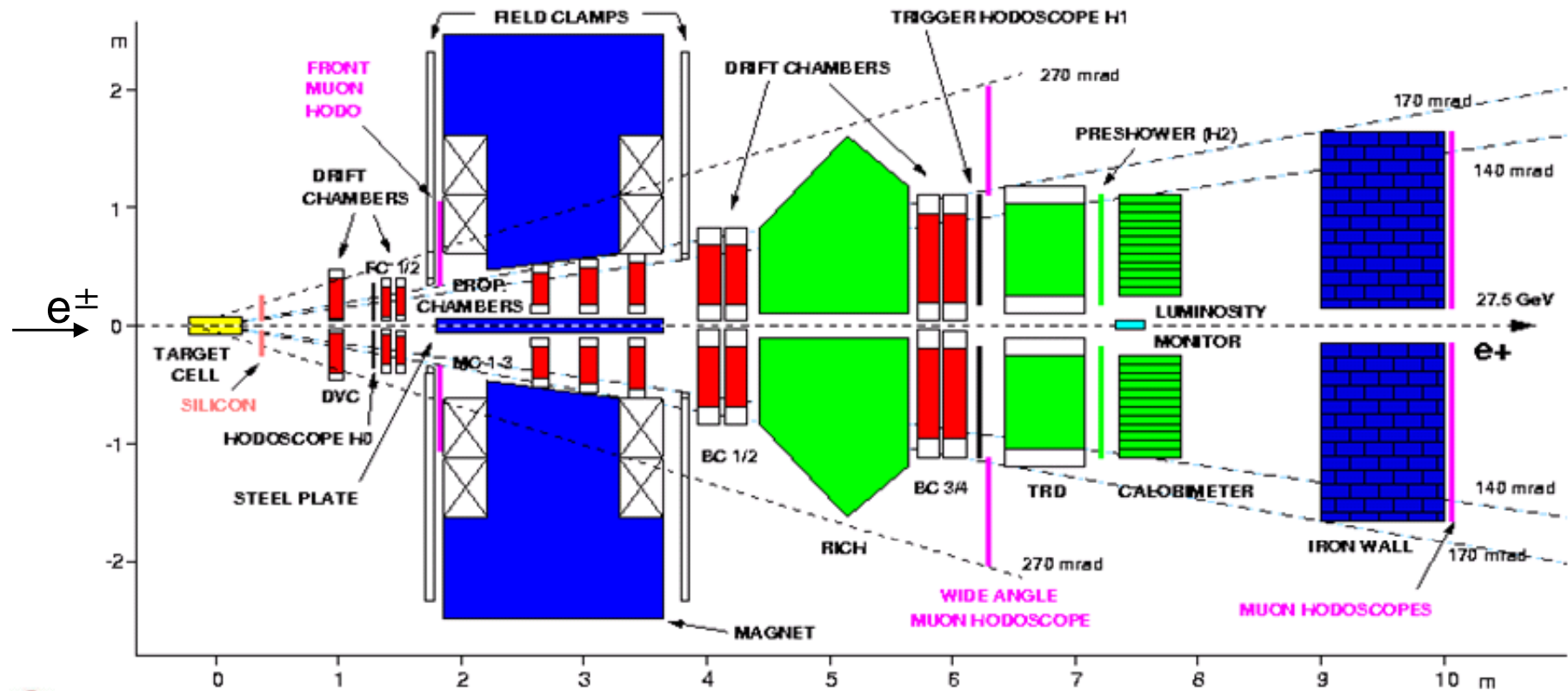
Sign Change $\sim \rho^0(770)$



**No Sign Change $\sim \rho^0(770)$
but Maximal Asymmetry**

**Dominance of real (Jaffe) vs. imaginary (Radici) part
of ρ^0 decay amplitude.**

HERMES Spectrometer



- Reconstruction: $\Delta p/p < 2\%$, $\Delta\theta < 0.6$ mrad
- Positron/Hadron separation efficiency: $> 99\%$
- Hadron Identification: **dual radiator RICH Detector:**
 π , K and p identification at 2 – 15 GeV/c
- Atomic hydrogen target with transversely polarization $\sim 75\%$
 - atomic pure gas target \rightarrow no dilution
 - flipping time ~ 90 s \rightarrow small systematic errors

Extracting Asymmetry Amplitude

Two-dimensional fit binned to $(\phi_{R\perp} + \phi_S)$ and $\theta' \equiv ||\theta - \pi/2| - \pi/2|$:

$$A_{U\perp}(\phi_{R\perp} + \phi_S, \theta') = \sin(\phi_{R\perp} + \phi_S) \frac{a \sin \theta'}{1 + b \frac{1}{4} (3 \cos^2 \theta' - 1)}$$

$$\text{where } a \equiv A_{U\perp}^{\sin(\phi_{R\perp} + \phi_S) \sin \theta} \sim \frac{h_1 H_1^{\langle, sp}}{f_1 D_1}$$

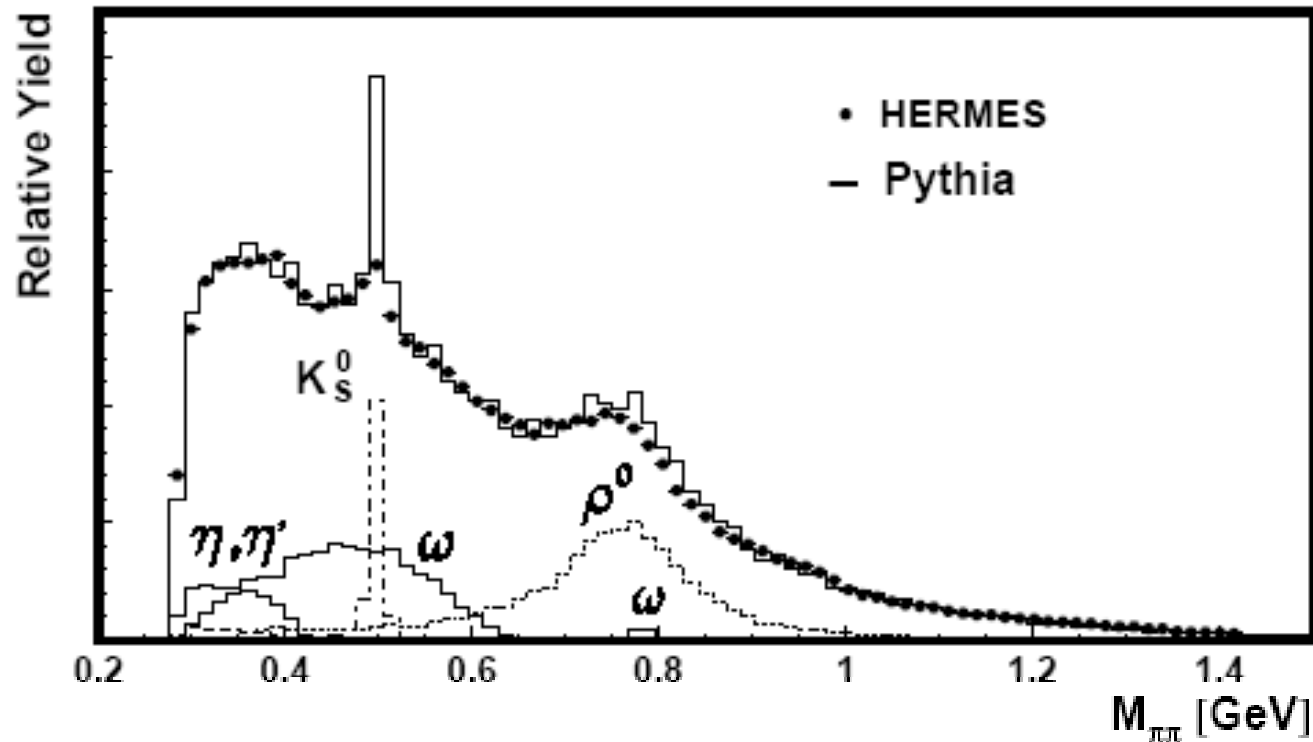
varying b within positivity limits:

$$-\frac{3D_1^p(z, M_{\pi\pi})}{2D_1(z, M_{\pi\pi})} \leq b \leq \frac{3D_1^p(z, M_{\pi\pi})}{D_1(z, M_{\pi\pi})}$$

- limits estimated by PYTHIA6 Monte Carlo
- take the center value in the range of a as asymmetry amplitude, the standard deviation as systematic uncertainty (doing a b -scan).

Monte Carlo Simulation

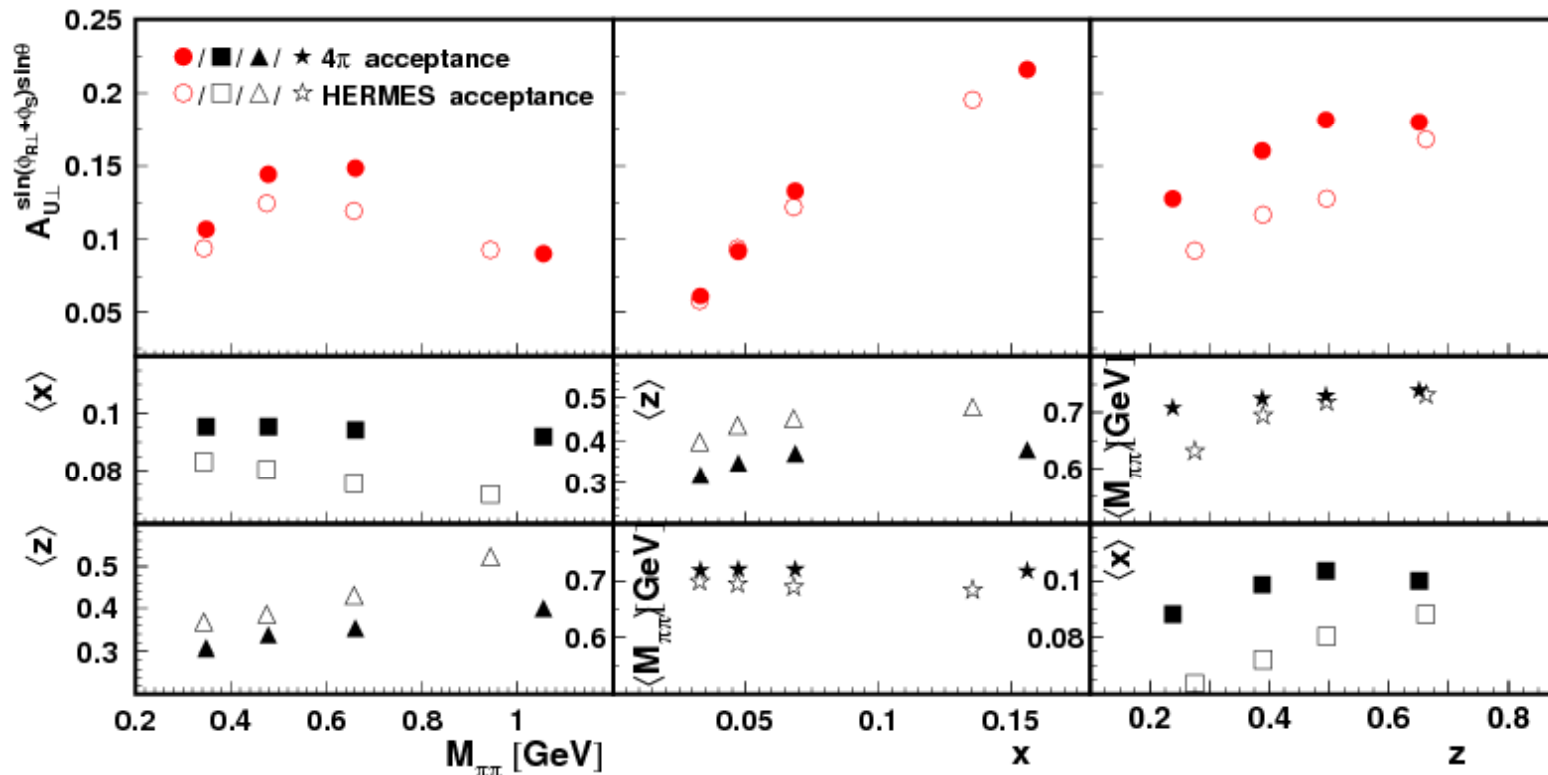
Tuned to HERMES single-hadron multiplicities



- MC describes two-hadron spectrum well
- ρ^0 and ω resonances contribute strongly to the spectrum
- $H_1^{\Delta,sp}$ is predicted to be maximal near $\rho^0(770)$ by theory

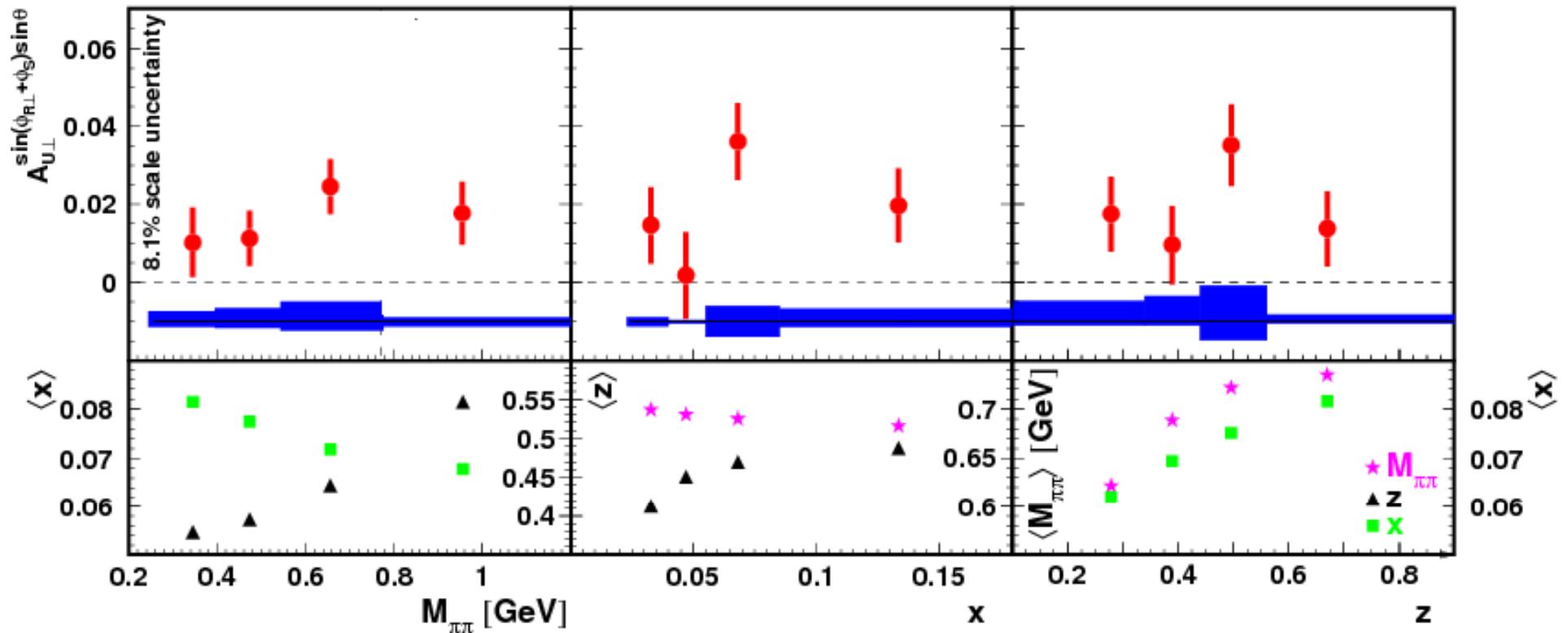
Estimate of Acceptance Effects

- Introduce target-spin dependence to the MC
- Combine models for Dihadron FF (*Bacchetta&Radici*[PRD74:114007,2006]), h_1 (*Schweitzer et al.*[PRD64:034013,2001];) and f_1 (*Gluck et al.* [EPJC5:461,1998])
- Compare the asymmetry amplitudes in 4π and HERMES acceptance.



- Fractional acceptance effect taken as systematic uncertainty

Extracted Asymmetry Amplitudes



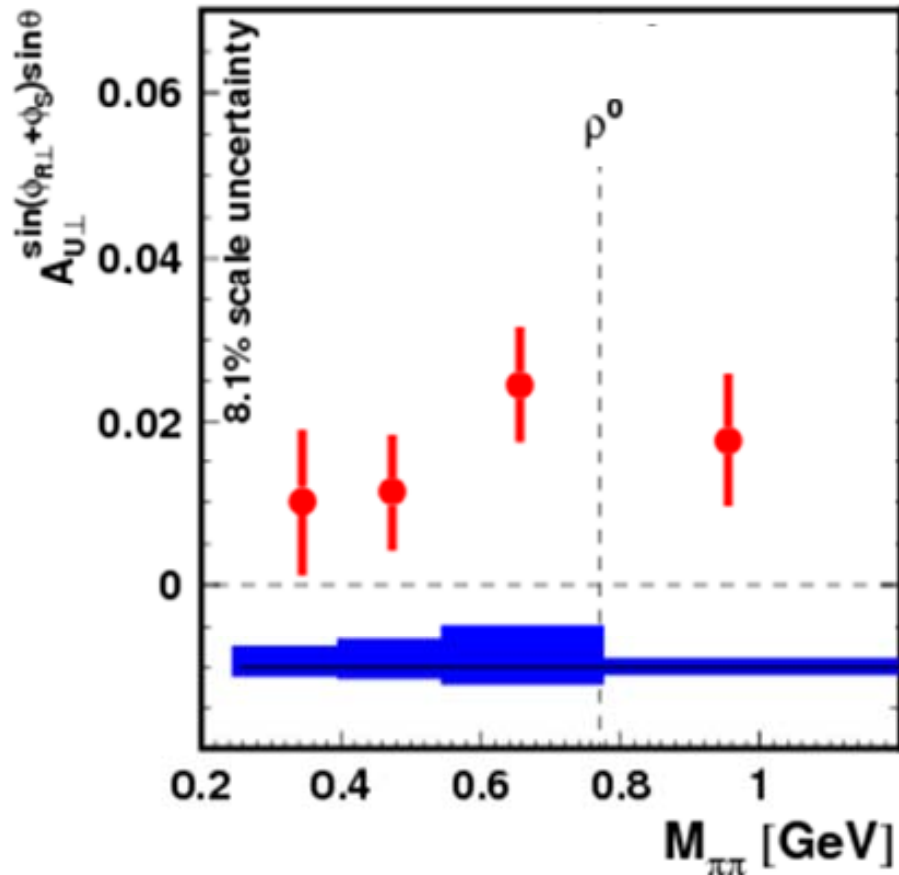
✓ average amplitude positive :

$$A_{U\perp}^{\sin(\phi_{R\perp}+\phi_S)\sin\theta} = 0.018 \pm 0.005_{\text{stat}} \pm 0.002_{\text{b-scan}} + 0.004_{\text{acc}}$$

✓ 8.1% scale systematic uncertainty contribution from target polarization

✓ the asymmetric error band combines *b-scan* effect and acceptance effect

Discussion of the Results



- ✓ Non-zero asymmetry amplitudes
- ✓ World first evidence of the Dihadron FF H_1^\triangleleft
- ✓ Positive amplitudes in the whole range of the invariant mass
 - rule out the sign change predicted by Jaffe
 - shape consistent with later model by Radici & Bacchetta
- ✓ Big contribution from s - p wave interference around $\rho^0(770)$
- ✓ Asymmetry results sensitive to transversity

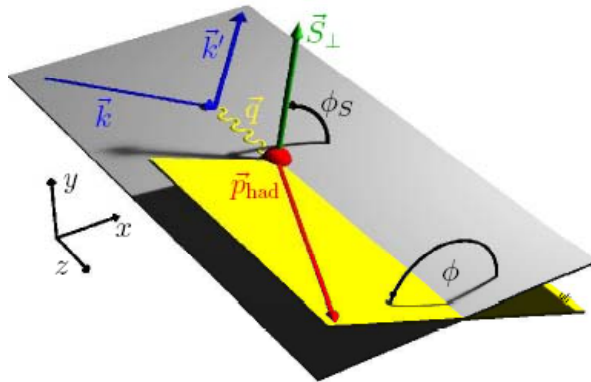
Summary

- ✚ Semi-Inclusive two-hadron production from a transversely polarized hydrogen measured at HERMES; Full data analyzed**
- ✚ First evidence for a spin-dependent Dihadron FF**
- ✚ Transversity can thus be accessed in two-pion SIDIS**
- ✚ No evidence of a sign change of the asymmetry amplitudes around $\rho^0(770)$: Jaffe's model not favored**
- ✚ An analogous mechanism can be studied in pp collisions at RHIC and SIDIS at COMPASS**
- ✚ Dihadron FF can be extracted from e^+e^- data at BELLE, which can be combined with SIDIS and pp collisions data to extract transversity**

Backup Slides

Semi-Inclusive DIS Cross Section

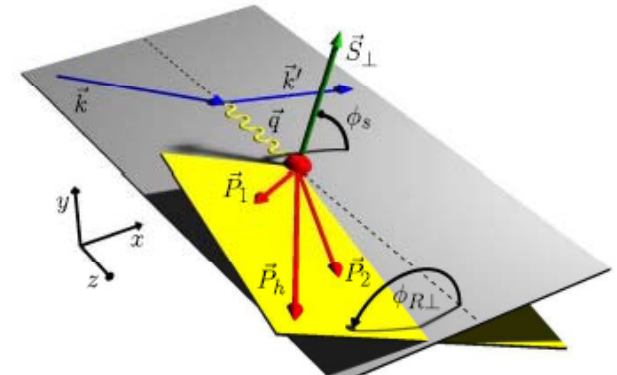
One-Hadron Production



$$\sigma_{UT} \sim \sin(\phi + \phi_S) \sum_q e_q^2 \mathcal{I} \left[\frac{k_T \hat{P}_{h\perp}}{M_h} h_1^q H_1^{\perp,q} \right]$$

- Convolution integral over intrinsic quark transverse momenta
- To extract $h_1 H_1^\perp$, need to deconvolve transverse momentum integral
- Competition with Sivers Effect
 → Well distinguished via Fourier component

Two-Hadron Production



$$\sigma_{UT} \sim \sin(\phi_{R\perp} + \phi_S) \sum e_q^2 h_1^q H_1^{\triangleleft}$$

- ⊕ Only relative momentum of two-hadron survives the integral over $\vec{H}_{h\perp}$
 - ⊕ Directly proportional to $h_1 H_1^{\triangleleft}$
 - ⊕ Independent measurement of transversity from one-hadron case
- But:**
- ⊕ Lower statistics
 - ⊕ More kinematic dependence ($d^9\sigma$)
 - ⊕ No 2-hadron FF measured so far (can be measured by BELLE)

Spectrometer Acceptance Effect

The fully differential asymmetry depends on 9 kinematic variables:

$$x, y, z, \phi_{R\perp}, \phi_S, \text{ and } \theta, M_{\pi\pi}, \text{ and } P_{h\perp} \quad (d^2 P_{h\perp} = |P_{h\perp}| d|P_{h\perp}| d\phi_h).$$

Measured number of events convoluted with the experimental acceptance:

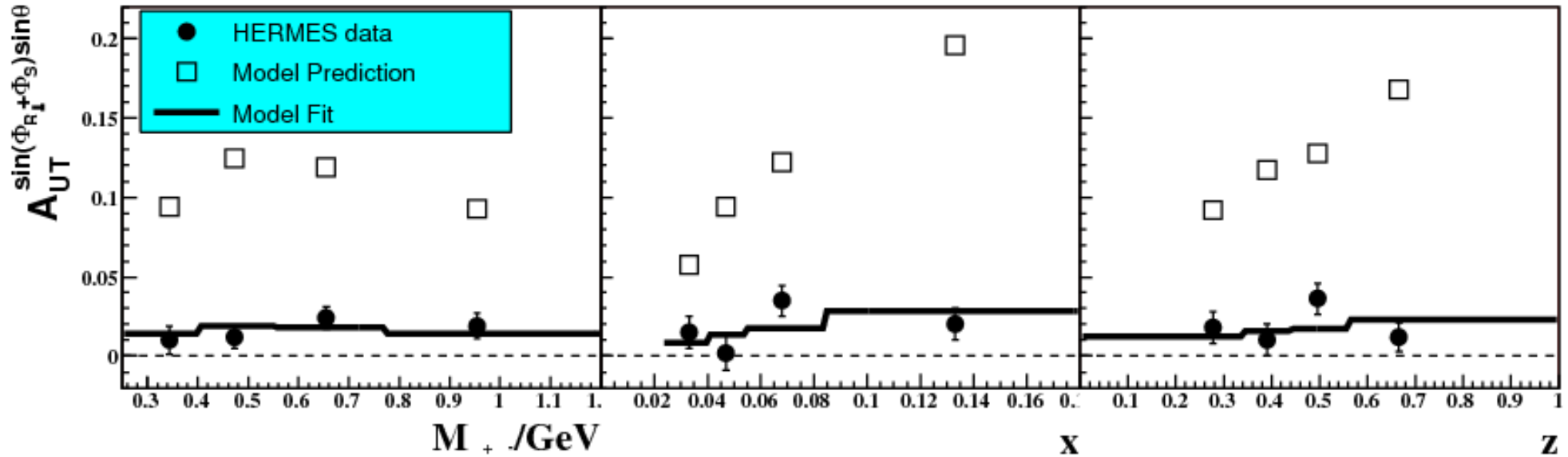
$$N^{\uparrow(\downarrow)}(\phi_{R\perp}, \phi_S, \theta, M_{\pi\pi}) \propto \int dx dy dz d^2 P_{h\perp} \epsilon(x, y, z, P_{h\perp}, \phi_{R\perp}, \phi_S, \theta, M_{\pi\pi}) \\ \times \sigma_{U\uparrow(\downarrow)}(x, y, z, P_{h\perp}, \phi_{R\perp}, \phi_S, \theta, M_{\pi\pi}),$$

To study the acceptance effect, the single target-spin asymmetry was introduced to the HERMES-tuned PYTHIA6 Monte Carlo simulation based on the theoretical model:

$$A_{UT}(x, y, z, M_{\pi\pi}, |\mathbf{P}_{h\perp}|, \phi_{R\perp}, \phi_S, \phi_h, \theta) \\ = -\sin(\phi_{R\perp} + \phi_S) \frac{B(y)}{A(y)} \sqrt{1 - 4 \left(\frac{M_\pi}{M_{\pi\pi}} \right)^2} \frac{\sum_q e_q^2 h_1^q(x) H_{1,q}^{\triangleleft, sp}(M_{\pi\pi}, z)}{\sum_q e_q^2 f_1^q(x) D_{1,q}(M_{\pi\pi}, z)}$$

- $H_{1,q}^{\triangleleft, sp}(z, M_{\pi\pi})$ and $D_{1,q}(z, M_{\pi\pi})$ from A. Bacchetta and M. Radici (hep-ph/0608037)
- $h_1^q(x)$ at $Q^2 = 2.5 \text{ GeV}^2$ from P. Schweitzer et al. (hep-ph/0101300)
- $f_1^q(x)$ at $Q^2 = 2.5 \text{ GeV}^2$ from GRV (M. Glueck, E. Reya, A. Vogt (hep-ph/9806404))

Theoretical and Extracted Amplitudes



Overestimated asymmetry from theory!